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Department of Chemical Engineering

An Integrated Approach to Artificial Neural Network based Process Modelling

Agus Saptoro

This thesis is presented for the Degree of
Doctor of Philosophy
of
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Statement of Originality

To the best of my knowledge and belief, this thesis contains no material previously published by any other person except where due acknowledgement has been made.

This thesis contains no material which has been accepted for the award of any other degree or diploma in any university.

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SUMMARY

ANN technology exploded into the world of process modelling and control in the late 1980's. The technology shows great promise and is seen as a technology that could provide models for most systems without the need to understand the fundamental behaviour or relationships among the process variables. Today, ANN applications have been applied successfully in a number of areas of process modelling and control, with the best-established applications being in the area of inferential measurements or soft sensors.

Unfortunately, 'the free lunch did not have much meat'. Overtime, people focused more on the true capabilities and power of ANN, the ability to model nonlinear relationships in data without having to define the form of the nonlinearity. However, there is often a tendency to merely plug in the data, turn the ANN training software on, and blindly accept the results. This is probably inevitable since, to date, there are no textbooks or scientific journal papers providing an integrated and systematic approach for ANN model development addressing pre-modelling, training and post-modelling stages. Therefore, addressing issues in those three phases of ANN model development is essential to support and to improve further applications of ANN technology in the area of process modelling and control.

The model development issues in pre-modelling and training phases were addressed by reviewing current practice and existing techniques. For each issue, a novel method was proposed to improve the performance of ANN models. The new approaches were tested in a variety of benchmarking studies using artificial samples and coal property datasets from power station boilers.

The research work in the post-modelling stage analysis which emphasises on taking the lid off black box model, proposes a novel technique to extract knowledge from the models and simultaneously obtain better understanding of the process. Post-modelling phase issues were addressed thoroughly including construction of prediction limit, sensitivity analysis and development of mathematical representation of the trained ANN model.

Confidence intervals of the ANN models were analysed to construct the prediction boundary of the model. This analysis provides useful information related to interpolation and extrapolation of the model. It also highlighted how good the ANN models can be used for extrapolation purposes.

An effort based on sensitivity analysis of hidden layers is also proposed to understand the behaviours of the ANN models. Using this technique, knowledge and information are retrieved from the developed models. A comparative study of the proposed techniques and the current practice was also presented.

The last topic addressed in this thesis is knowledge extraction of ANN models using mathematical analysis of the hidden layers. The proposed analysis is applied in order to open the black box of the ANN models and is implemented to simulated and real historical plant data so that useful information from those data and better understanding of the process are obtained.

All in all, efforts have been made in this thesis to minimise the use of abstract mathematical language and in some cases, simplify the language so that ANN modelling theory can be understood by a wider range of audience, especially the new practitioners in ANN based modelling and control. It is hoped that the insight provided in the dissertation will provide an integrated approach to pre-modelling, training and post-modelling stages of ANN models. This 'new guideline' of ANN model development is unique and beneficial, providing a systematic framework for the preparation, design, evaluation and implementation of ANN models in process modelling and control in particular and prediction / forecasting tool in general.

Keywords: artificial neural networks, pre-modelling, modelling, post-modelling, opening the black box, an integrated approach.

Brief Biography of the Author

Agus Saptoro received the Bachelor of Engineering in Chemical Engineering with academic distinctions from the Faculty of Engineering Gadjah Mada University, Indonesia in 2002. Prior to joining Department of Chemical Engineering National Institute of Technology Indonesia in 2003, he worked as a process control engineer at a Polymer Fibre Plant in Semarang, Indonesia. He received Master degree scholarship from Asian Development Bank through TPSDP project to pursue Master of Engineering at Department of Chemical Engineering Curtin University of Technology which commenced in March 2005. In September 2006, his master program was converted into PhD degree and his research project was supported by Curtin International Research Tuition Scholarship from March 2007 to December 2008. He currently holds the position of lecturer at Department of Chemical Engineering Curtin University Technology, Sarawak, Malaysia.

Journal Publications arising from this Thesis

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Saptoro, A., Yao, H.M, Tadé, M.O. and Vuthaluru, H.B., 2008, "Prediction of coal hydrogen content for combustion control in power utility using neural network approach", Chemometrics and Intelligent Laboratory Systems, 94 (2), 149-159.

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Saptoro, A., Vuthaluru, H.B. and Tadé, M.O., 2008, "Optimising artificial neural networks topology using hierarchical two-population genetic algortihm", 12th APCChE Congress, Dalian, China.

Saptoro, A., Vuthaluru, H.B. and Tadé, M.O., 2006, "Partial Least Squares and Neural Networks based Model of Coal-Fired Power Plant Boiler", CHEMECA, Auckland, New Zealand.

Saptoro, A., Vuthaluru, H.B. and Tadé, M.O., 2006, "A Comparative Study of Prediction of Elemental Composition of Coal using Empirical Modelling", IFAC Symposium on Advanced Control of Chemical Processes, Gramado, Brazil.

Saptoro, A., Vuthaluru, H.B. and Tadé, M.O., 2006, "Design of Feed-Forward Neural Networks Architecture for Coal Elemental Composition Prediction", International Conference on Modelling and Simulation, Kuala Lumpur, Malaysia.

Saptoro, A., Vuthaluru, H.B. and Tadé, M.O., 2006, "Prediction and Monitoring of Unburnt Carbon in Fly Ash in Coal-Fired Power Plant", International Conference on Modelling and Simulation, Kuala Lumpur, Malaysia.

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TABLE OF CONTENTS

	Page
Statement of Originality	ii
Summary	iii
Brief Biography of the Author	v
Acknowledgments	vi
Journal Publications arising from this Thesis	v
Refereed Conference Publications arising from this Thesis	v
Table of Contents	viii
List of Figures	xiii
List of Tables	xvi
List of Acronyms	xix

PART A
INTRODUCTION AND LITERATURE REVIEW

Chapter 1 Introduction 1

1.1 Artificial neural networks based soft sensors and models of chemical processes 1
1.2 Motivations for this study 3
1.3 Objectives and Contributions 4
1.3.1 Objectives 4
1.3.2 Contributions 4
1.4 Scope of the study 5
1.5 Layout of the thesis 5

Chapter 2 Research Background and Literature Review 8

2.1 Artificial neural networks (ANN) 8

2.2 Applications of ANN in Chemical Engineering 14
2.3 The use of ANN in coal combustion technology 15
2.4 ANN based process modelling: model development, procedure and pitfalls 18

PART B
PRE-MODELLING STAGES OF ANN BASED MODELS

Chapter 3 An integrated data preparation procedure for developing artificial neural network model 56

3.1 Input variable selection 56
3.1.1 Entropy, mutual information and partial mutual information 57
3.1.2 Input variable selection based on grey superior analysis 64

3.2 Approaches to deal with outliers and noisy data 66
3.2.1 Outlier detection and elimination based ANN modelling 67
3.2.2 Robust ANN model against outliers/noisy data 73

3.3 Approaches to deal with incomplete / missing data 78

3.4 Approaches to deal with small sample dataset 86

3.5 Data splitting for ANN based modelling 90

3.6 Data transformation for ANN based modelling 93

3.7 **Design case studies** 95
3.7.1 Experiments for input variable selection 95
3.7.2 Experiments for dealing with outliers 113
3.7.3 Experiments for dealing with missing data 116
3.7.4 Experiments for dealing with small sample data set 121
3.7.5 Experiments for data splitting methodology 124
3.7.6 Experiments for data transformations 129

3.8 Concluding remarks 132
3.8.1 Input variable selection 132
3.8.2 Approaches to deal with outliers 133
3.8.3 Approaches to deal with missing data 133
3.8.4 Approaches to deal with small sample dataset 134
3.8.5 Data splitting 134
3.8.6 Data transformation 134

PART C
MODELLING STAGES OF ANN BASED MODELS 136

Chapter 4 Training stages of ANN based models: performance assessment of different settings 136

4.1 Analysis of number of hidden layers and hidden neurons 136

4.2 Choice of network weight and bias initialisation algorithms 137

4.3 Choice of activation functions 144

4.4 Choice of error measure 147

4.5 Choice of training algorithm 149
4.5.1 Variants of Back-Propagation Training Algorithms 149
4.5.2 Differential Evolution 156
4.5.3 Hybrid DE-Bayesian Regulation training algorithm 158

4.6 Simulation studies 159
4.6.1 Experiments for analysis of number of hidden layers and neurons 159
4.6.2 Experiments for the choice of network weight and bias initialisation algorithm 166

4.6.3 Experiments for the choice of activation functions 169
4.6.4 Experiments for the choice of error measure 173
4.6.5 Experiments for the choice of training algorithm 175

4.7 Concluding remarks 177
4.7.1 Analysis of number of hidden layers and hidden neurons 177
4.7.2 The choice of weight and bias initialisation algorithm 177
4.7.3 Choice of the transfer function 178
4.7.4 Choice of the error measure 178
4.7.5 Choice of training algorithm 179
4.7.6 General comments 179

PART D
POST-MODELLING STAGES OF ANN BASED MODELS: THE WIDEST RESEARCH GAPS IN ANN BASED PROCESS MODELLING

Chapter 5 Prediction interval of ANN models 180

5.1 Prediction interval construction based on regression model 181
5.2 Density estimator assisted prediction interval: a new approach 183
5.3 Simulation studies 184
5.4 Conclusion

Chapter 6 Opening the black box of ANN models 188

6.1 Review of existing approaches 189
6.2 The proposed technique 192
6.3 Experiments 197
6.4 Results and Discussion 197

6.5 Conclusions and Comments 202

PART E

CONCLUSIONS AND RECOMMENDATIONS

Chapter 7 Conclusions and recommendations 204

7.1 Conclusions 204

7.2 Recommendations for further research directions 207

REFERENCES 208

LIST OF FIGURES

CHAPTER 1

Figure 1.1	Schematic diagram of thesis layout	7

CHAPTER 2

Figure 2.1	A simple representative model of (a) a biological neuron and (b) an artificial neuron	10
Figure 2.2	A typical feedforward ANN architecture	11
Figure 2.3	ANN architectures : (a) feedback (b) feedforward	11-12
Figure 2.4	Schematic diagram of a multilayer feedforward ANN	13
Figure 2.5	Three main stages of ANN model development	19
Figure 2.6	Different types of transfer functions	49

CHAPTER 3

Figure 3.1	Typical learning in an ANN model	74
Figure 3.2	The characteristic of the influence function of MSE	75
Figure 3.3	MSE vs LOGMSE: characteristics of the influence functions	78
Figure 3.4	Schematic diagram of proposed BPCA-ANN	85
Figure 3.5	(a) a standard NN model (b) MTD-NN model	89
Figure 3.6	Schematic diagram of artificial neural network ensemble	90
Figure 3.7	ANN simulation for dataset 1	110
Figure 3.8	ANN simulation for dataset 2	110
Figure 3.9	ANN simulation for dataset 3	111
Figure 3.10	ANN simulation for dataset 4	111
Figure 3.11	ANN simulation for dataset 5	112
Figure 3.12	ANN simulation for dataset 6	112
Figure 3.13	Performance comparison of the ANN, MTD-ANN and E-ANN	123

CHAPTER 4

Figure 4.1	Histogram of the rand function	138
Figure 4.2	Histogram of the randn function	138

Figure 4.3 Histogram of the rands function 139
Figure 4.4 Histogram of the randnr function 140
Figure 4.5 Histogram of the randnc function 141
Figure 4.6 Linear Transfer function *(purelin)* 145
Figure 4.7 Logarithmic Sigmoid Transfer Function 145
Figure 4.8 Hyperbolic Tangent Transfer Function 146
Figure 4.9 Radial Basis Transfer Function 146
Figure 4.10 Triangular Transfer Function 147
Figure 4.11 Softmax Transfer Function 147
Figure 4.12 Simulation results representing MSE vs number of hidden nodes for experiment 1 159
Figure 4.13 Evaluation of capabilities of one, two and three hidden layer ANN models 162
Figure 4.14 Simulation results representing MSE vs number of hidden nodes for experiment 2 163
Figure 4.15 Evaluation of capabilities of one, two and three hidden layer ANN models having 8 hidden neurons 165
Figure 4.16 Comparison of Training performance of ANN training using different random initialisattion algorithm 167
Figure 4.17 Training effectiveness of the ANN model 170
Figure 4.18 Training effectiveness of the ANN model 171
Figure 4.19 Training efficiency of the ANN model 171-172
Figure 4.20 Generalisation capability of the ANN model 173
Figure 4.21 Training and testing performance of mse- and logmse- ANN models 174
Figure 4.22 Training efficiency of the mse- and logmse ANN models 174
Figure 4.23 Comparisons of different algorithms for ANN training 175-176

CHAPTER 5

Figure 5.1 Prediction interval for sample serial number 1 – 75 (case study 1) 185
Figure 5.2 Prediction interval for sample serial number 76 – 150 (case study 1) 185
Figure 5.3 Prediction interval for sample serial number 151–300 (case study 1) 186
Figure 5.4 Prediction interval for sample serial number 301–375 (case study 1) 186

Figure 5.5 Prediction interval for case study 2 187

CHAPTER 6

Figure 6.1 True values vs predicted values using trained ANN model 198

Figure 6.2 True values vs predicted values using extracted model 202

LIST OF TABLES

CHAPTER 1

Table 1.1	Issues in ANN based modelling	3

CHAPTER 3

Table 3.1	Statistical properties of dataset 1	96
Table 3.2	Statistical properties of dataset 2	96
Table 3.3	Statistical properties of dataset 3, 4 and 5	96
Table 3.4	Statistical properties of dataset 6	96
Table 3.5	Statistical properties of dataset 1 after data division	98
Table 3.6	Statistical properties of dataset 2 after data division	98
Table 3.7	Statistical properties of dataset 3 after data division	98
Table 3.8	Statistical properties of dataset 4 after data division	99
Table 3.9	Statistical properties of dataset 5 after data division	99
Table 3.10	Statistical properties of dataset 6 after data division	99
Table 3.11	Input variables for calorific value prediction (current practice)	102
Table 3.12	The degree of contribution of each input variable on the output variable (grey superior analysis on dataset 1)	103
Table 3.13	The degree of contribution of each input variable on the output variable (grey superior analysis on dataset 2)	103
Table 3.14	The degree of contribution of each input variable on the output variable (PMI analysis on dataset 1)	104
Table 3.15	Hample distance assisted PMI analysis on dataset 1	104
Table 3.16	The degree of contribution of each input variable on the output variable (PMI analysis on dataset 2)	104
Table 3.17	Hample distance assisted PMI analysis on dataset 2	105
Table 3.18	The degree of contribution of each input variable on the output variable (grey superior analysis on dataset 3)	105
Table 3.19	The degree of contribution of each input variable on the output variable (grey superior analysis on dataset 4)	105
Table 3.20	The degree of contribution of each input variable on the output variable (grey superior analysis on dataset 5)	106

Table 3.21	The degree of contribution of each input variable on the output variable (PMI analysis on dataset 3)	106
Table 3.22	Hample distance assisted PMI analysis on dataset 3	106
Table 3.23	The degree of contribution of each input variable on the output variable (PMI analysis on dataset 4)	107
Table 3.24	Hample distance assisted PMI analysis on dataset 4	107
Table 3.25	The degree of contribution of each input variable on the output variable (PMI analysis on dataset 5)	107
Table 3.26	Hample distance assisted PMI analysis on dataset 5	107
Table 3.27	The degree of contribution of each input variable on the output variable (grey superior analysis on dataset 6)	108
Table 3.28	The degree of contribution of each input variable on the output variable (PMI analysis on dataset 6)	109
Table 3.29	Hample distance assisted PMI analysis on dataset 6	109
Table 3.30	Summary of grey superior analysis based ANN modeling	113
Table 3.31	Number of detected outliers using various methods	114
Table 3.32	Percentage of detected outliers using various methods	114
Table 3.33	Dealing with outliers: performances of different scenarios	115
Table 3.34	Percentage of improvement of LOGMSE based ANN compared MSE based ANN	116
Table 3.35	Statistical properties of dataset used in experiment	117
Table 3.36	Symbols used in the experiment	117
Table 3.37	Simulation results of all training datasets tested using Testing0	118
Table 3.38	Simulation results of all training datasets tested using Testing1	119
Table 3.39	Simulation results of all training datasets tested using Testing5	119
Table 3.40	Simulation results of all training datasets tested using Testing10	119
Table 3.41	Simulation results of all training datasets tested using Testing20	120
Table 3.42	Simulation results of all training datasets tested using Testing30	120
Table 3.43	Simulation results of all training datasets tested using Testing40	120
Table 3.44	Simulation results of all training datasets tested using Testing50	121
Table 3.45	Simulation results of all training datasets tested using Testing75	121
Table 3.46	Datasets used in simulation study	122
Table 3.47	Improvement percentages of MTD-ANN and E-ANN compared with ANN	124

Table 3.48 Statistical Properties of Case Study 1 Data 124
Table 3.49 Statistical Properties of Case Study 2 Data 125
Table 3.50 Statistical Properties of Data after Data Division for Case Study 1 126
Table 3.51 Statistical Properties of Data after Data Division for Case Study 127
Table 3.52 ANN model performance trained with training data developed from different data division method 129
Table 3.53 Statistical Properties of Data used in Experiment 130
Table 3.54 Min and Max Values of Transformed Datasets 131
Table 3.55 ANN model performance trained using different transformation methods 132
Table 3.56 Computational time of the use of different data transformation 132

CHAPTER 4

Table 4.1 Recommended numbers of hidden nodes suggested by several authors 162
Table 4.2 Summary of code used in different hidden notes configuration 163
Table 4.3 Recommended numbers of hidden nodes suggested by several authors 166
Table 4.4 Codes of hidden nodes configuration used Figures 4.4.a and 4.4.b 168
Table 4.5 Training accuracy and training time 170
Table 4.6 Testing accuracy and training time 170
Table 4.7 Combinations of activation functions used in the experiment 171
Table 4.8 Generalisation of the different training algorithms of ANN 179

CHAPTER 6

Table 6.1 Relative contributions using different techniques 199
Table 6.2 Coefficient of the regression model 201

LIST OF ACRONYMS

ACO	Ant Colony Optimisation
ANN	Artificial Neural Networks
ARD	Automatic Relevance Determination
BPCA	Bayesian Principal Component Analysis
C	Carbon
CSTR	Continuous Stirred Tank Reactor
CV	Calorific Value
DCS	Distributed Control System
E-ANN	Ensemble Artificial Neural Networks
EM	Expectation - Maximisation
ED	Eucledian Distance
FC	Fixed Carbon
FCC	Fluid Catalytic Converter
GA	Genetic Algorithm
H	Hydrogen
initnw	Nguyen-Widrow layer initialisation function
ITA	Information Theoretic Approach
KS	Kennard-Stone
Kurt	Kurtosis
LOGMSE	Mean Squared Error based on Cauchy distribution
logsig	logarithmic sigmoid transfer function
M	Moisture
MCD	Minimum Covariance Determinant
MD	Mahalanobis Distance
MDKS	Kennard-Stone based on Mahalanobis Distance Method
MF	Membership Function
MI	Mutual Information
ML	Maximum Likelihood
MLP	Multilayer Perceptron
MR	Multiple Regression
MSE	Mean Squared Error

MTD	Mega Trend Diffusion
MTD – ANN	Hybrid Mega Trend Diffusion and Artificial Neural Networks
MVE	Minimum Volume Estimator
MVT	Multivariate Trimming
NLPCA	Nonlinear Principal Component Analysis
O	Oxygen
PC	Principal Component
PCA	Principle Component Analysis
PCR	Principle Component Regression
PLS	Partial Least Square
PMI	Partial Mutual Information
PPCA	Probabilistic Principal Component Analysis
PSD	Pseudo Standard Deviation
PSO	Particle Swarm Optimisation
purelin	linear transfer function
RAND	uniformly distributed random number generator
RANDN	normally distributed random number generator
RANDS	symmetric distributed random number generator
RANDNC	normally distributed random number generator that generates a random weight matrix columns of which are normalised to the value of one
RANDNR	normally distributed random number generator that generates a random weight matrix rows of which are normalised to the value of one
RD	Robust Distance
RS	Random Selection
S	Sulphur
SD	Standard Deviation
Skew	Skewness
SOM	Kohonen Self Organising Map
SVD	Singular Value Decomposition
SPXY	Sample Set Partitioning based on Joint X – Y Distances
tansig	hyperbolic tangent transfer function
VM	Volatile Matter

Chapter 1
INTRODUCTION

1.1 Artificial Neural Networks based soft sensors and models of chemical processes

Empirical modelling is a method for the development of models based on process / experimental data. Since physical modelling is not always obtainable and very time consuming, empirical modelling is a more popular method for gaining insights into the overall (input-output) process behaviour. The developed models are usually used for prediction of future process values using historical data or estimation of unmeasured variables using easily measurable variables.

Most chemical and industrial processes exhibit nonlinear behaviour, therefore, empirical nonlinear models are required instead of the linear ones. In this regard, ANN as an empirical nonlinear modelling technique has been used extensively in recent years to model a wide range of physical and chemical phenomena. ANN is very attractive whenever it is necessary to model complex or less understood processes with large input and output datasets, as well as to replace models that are too complicated to solve in real time [1, 2].

ANN technology exploded into the world of process modelling and control in the early 1990's. The technology shows great promise and is seen as a technology that could provide models for most of our systems without the need to understand the fundamental behaviour or relationships of the process. Today, ANN applications have been applied successfully in a number areas of process modelling and control, with the best-established applications being in the area of inferential measurements or soft sensors.

Unfortunately, the free lunch did not have much meat. With time, researchers shifted their focus more to the true capabilities and power of ANN, the ability to model nonlinear relationships in data without having to define the form of the nonlinearity. However, researchers soon realised that blindly applying black box modelling technique may provide a satisfactory fit for historical data but often leads to poor

performance for using online in a closed-loop control application, or on time-variant processes. The ANN model is a more black-box approach, making it difficult to extract process understanding from the model, and it is only valid in the operating region over which the data was modelled.

Regardless of the power of ANN to solve problem effectively, there are also many issues associated with a systematic approach of ANN model development. There is often a tendency to merely plug in the data, turn the ANN training software on, and blindly accept the results. On other hand, several questions as listed below arose regarding pre-modelling phases, modelling stages and post-modelling stages.

How do we select representative input variables?

How to deal with outliers/noises, eliminate them or develop robust ANN model against them?

How do we build and apply the ANN model in scenarios where some measurements are missing and the data is incomplete?

How to handle small size of datasets as building a good ANN model requires sufficient historical/experimental data?

Given such available historical/experimental data, how do we divide these datasets into training and testing/validation data?

To ensure consistency among different magnitudes of input variables of varying scales, which data transformation should be used?

To resume the ANN training, which weight initialisation algorithm should be used?

What activation functions should be used for hidden and output layers?

As there are many training algorithms, which one will give faster and better result?

What learning criteria should be used?

How many hidden layers should be used?

Table 1.1 Issues in ANN based modelling.

Issues on ANN based modelling		
Pre-modelling phase	Modelling / Training stage	Post-modelling phase
Data collection and Input Variable Selection	*Weight initialisation*	*Prediction limit / confidence interval*
Outliers /noise	*Choice of activation function*	*Sensitivity analysis*
Incomplete / missing data	*Choice of training algorithm*	*Extracting knowledge from ANN model*
Small sample dataset	*Choice of learning criteria*	
Data splitting	*Number of hidden layers*	
Data transformation		

Unfortunately, to date, there are no textbooks or scientific journal papers providing an integrated and systematic approach of ANN model development addressing all the above questions. Moreover, current ANN technology applications mostly lack post-modelling phase analysis as listed in Table 1.1. Therefore, addressing issues in the three phases of ANN model development is essential to support and to improve further applications of ANN technology in the area of process modelling and control.

1.2 Motivations for this study

ANN models have been traditionally designed without an integrated and systematic approach. Building ANN models sometimes is also facing undesirable conditions such as missing measurement/incomplete data and small sample dataset. Although the model users are satisfied with their predictive performance, understanding of the ANN function in its hidden layer is still poor. Hence the black-box nature results in difficulties to extract process knowledge from the data/models.

The first motivation for this research is to provide an integrated and systematic approach of ANN model development and propose novel / improved approaches to the existing analysis and methods. A second motivation, which drives many ANN researchers and users, is to propose techniques to open the black box of the ANN and simultaneously to extract process knowledge and understanding from the models.

1.3 Objectives and contributions

1.3.1 Objectives

The main objectives of this research are:

- To propose a systematic post-modelling phase analysis of the ANN models. The emphasise, in particular, is on opening the black-box of the ANN model in order to extract its process knowledge and to obtain mathematical relationships inside the hidden layers.
- To highlight integrated approaches of pre-modelling and modelling phases to provide guidance for ANN model development. Some issues in these two stages are thoroughly addressed using existing techniques and novel methods.
- To demonstrate how the proposed approaches are able to enhance the performance of the black box models.

1.3.2 Contributions

This research work in theoretical and sensitivity analysis of hidden layer is a direct contribution to ANN theory, design and its applications. Previously most of the work in ANN only focused on how to blindly develop ANN models and to implement them to predict output variables using given input variables. An integrated approach to pre-modelling, modelling and post-modelling staged of ANN models is also unique and beneficial, providing a systematic framework of the preparation, design, evaluation and implementation of ANN models. This framework will provide an integrated guidance for building ANN models. In addition, the post-modelling stage analysis which emphasise on taking the lid off black box model, will provide a novel technique to extract knowledge from the models and simultaneously to obtain better understanding of the process.

This research and development work has also a great significance with regards to its application in black box modelling approach and ANN predictive control. Having better performance and well understood models will simultaneously benefit the applications of black-box models and model predictive control.

1.4 Scope of the study

The overall scope of this study entails developing a framework for understanding ANN behaviour and extracting knowledge from ANN models. An integrated model development scheme of ANN models is also presented covering existing techniques and novel approaches. The FFANN structure is selected for this research as this structure has been used almost exclusively in many areas of prediction and modelling. Case studies on synthetic problems, coal properties prediction and modelling of coal-fired power plant were used to describe how all of the approaches work.

1.5 Layout of the thesis

This thesis is divided into seven chapters. In chapter two a literature review of the use of ANN, specifically in coal-power stations, is presented. This review also comprehensively covers the research gaps in current status of research on ANN and the roadmap for further research need. The background and motivations for this work are exclusively outlined in this chapter.

Chapter three deals with the issues in pre-modelling phase of ANN models. It provides an integrated scheme of input variable selection and data preparation for model development. Observations to the existing techniques and their novel approaches are performed and their influences on ANN model performance are studied.

Chapter four mainly discusses issues during training stages. This section attempts to explore the effects of internal model parameters and structure and also learning algorithms on the performance of ANN model. Novel techniques are proposed to improve the performance of the existing methods.

Chapters five to six presents post-modelling phase of ANN model development. Topics in these chapters, to date, are the widest gaps in the ANN research and applications, leaving the users and practitioners to only apply ANN without confidently knowing the prediction limits of their models and understanding what information / knowledge can be extracted from the model / hidden layers of ANN.

Chapter five provides theoretical analysis to construct the confidence intervals / prediction limits of the developed models. It also highlighted how good the ANN models can be used for extrapolation purposes. Chapter six addresses knowledge extraction of trained ANN model. Specifically, the focuses are to open the black box of the ANN model and to understand the behaviour of the developed model.

There are two approaches of knowledge extraction of ANN model discussed and proposed in this chapter. First approach is mainly based on sensitivity analysis of hidden layer and the other approach is a proposed technique to retrieve mathematical representation of the black box model. Using these two techniques, useful information from the data and better understanding of the process can be obtained.

In chapter seven, the conclusions from this study and the recommendations and future directions for research are presented. Appendices provide supplementary materials and information and related programme used in various chapters and sections.

To make the thesis clearer and more compact, while chapter two provides an overall literature review on current ANN research and applications and their research gaps and research need, other chapters also present a comprehensive literature review of related issues in each sections. The organisation of the thesis is described in Figure 1-1.

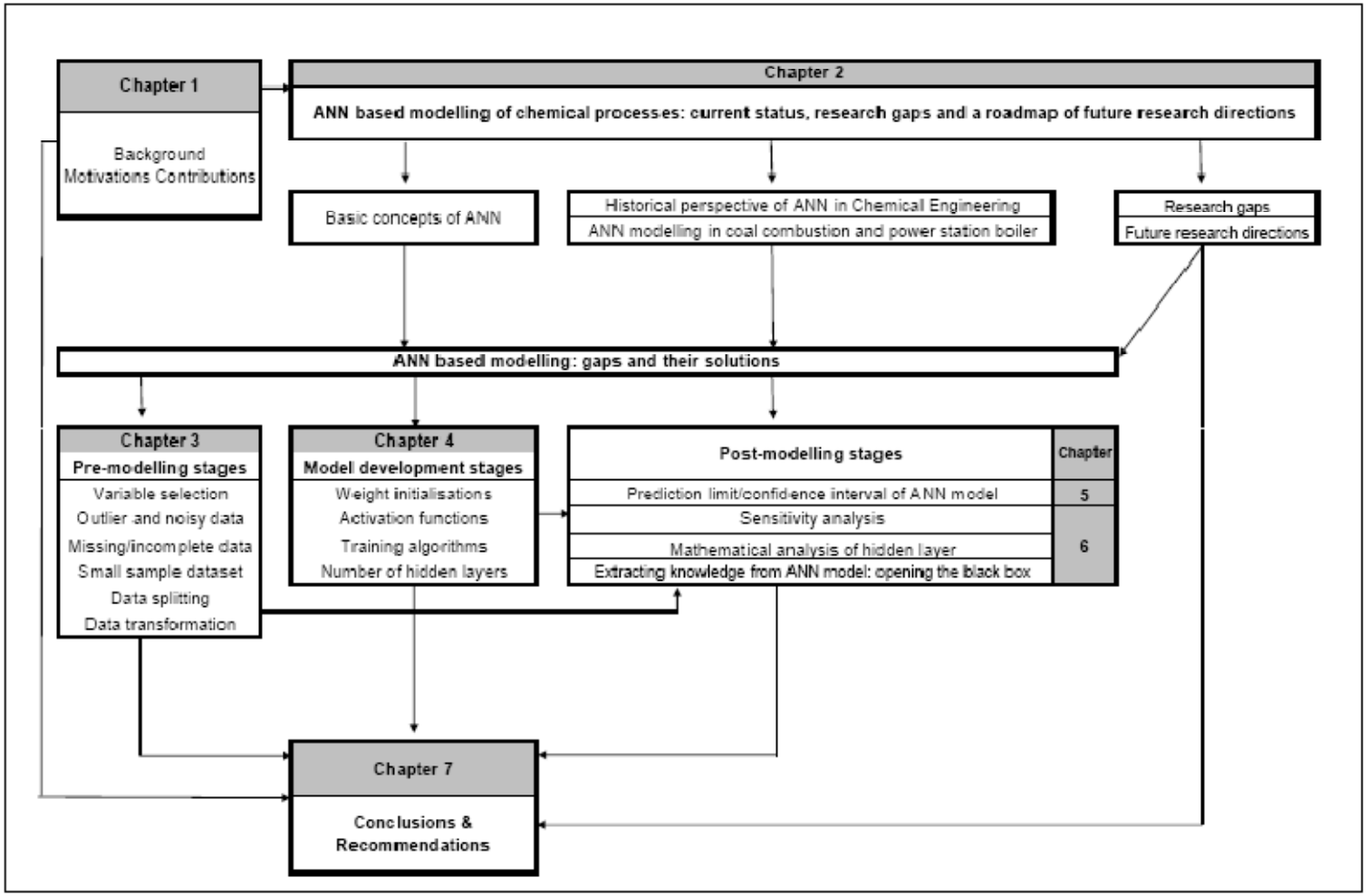

Figure 1.1 Schematic diagram of thesis layout.

Chapter 2
RESEARCH BACKGROUND AND LITERATURE REVIEW

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Chapter 3

AN INTEGRATED DATA PREPARATION PROCEDURE FOR DEVELOPING ARTIFICIAL NEURAL NETWORK MODEL

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CHAPTER 4
MODELLING STAGES OF ANN BASED MODELS

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Chapter 5
Prediction Interval of the ANN Model

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Chapter 6
Opening the Black Box of ANN Models

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CHAPTER 7
CONCLUSIONS AND RECOMMENDATIONS

The aim of this research work was to address pre-modelling, training and post-modelling phases of the ANN predictive model since to date there is no systematic and integrated approach into ANN model design covering all the modelling issues above. This chapter summarised the main findings made during this research into three main sections, which are pre-modelling stages, training phases and post-modelling stages. The chapter concludes with recommendations for future work to further enhance the ANN modelling especially the post modelling part.

7.1 CONCLUSIONS

7.1.1 Pre-modelling phases

Several issues exist before the dataset is trained to develop an ANN process model. Being able to select appropriate input variables and examining and treating the data are essential to have a good predictive model. The main features of the proposed methods and findings in this part are:

- Proposed a grey superior analysis based approach in order to select optimum set of input variables. Using this approach, preliminary knowledge related to the degree of importance of each variable is also obtained. Compared with popular partial mutual information based technique, this proposed method was demonstrated to be superior.
- Treatment of outliers in the dataset is an important issue. Most ANN users tend to have outlier elimination to have ‘a good quality of dataset’. However, deleting suspicious outliers can eliminate important information inside the datasets. Hence, based on the preliminary work from Liano, in this robustification of the network by modifying its error measure was carried out to reduce the influences of the outliers into the model performance.
- Current ANN technology is not able to deal with missing information in its training set and testing set. The most popular way to handle missing data is zero or mean substitution or deletion procedures. A new hybrid techniques BPCA-ANN was proposed to deal with missing input variables in both

training and testing sets and it is evident that the proposed approach perform very well in this regard.

- To be able to train the ANN successfully, the number of the training set should be as much as possible. However, in many cases, this does not always happen. Database of experiments or several operational parameters is small, on the other, ANN model is required to be built using this small sample dataset. In this work, MTD based ANN and ANN ensemble were applied and the results show that using one of this technique could improve the performance of the model in the case of only small training set available.
- The way the dataset was divided into the training and testing sets is believed to have a great impact on the predictive capability of the network. However, there is no guidance in how these datasets should be splitted. A proposed data division method based on Kennard-Stone algorithm using mahalanobis distance criterion proved to be superior to the standard Kennard Stone and SPXY algorithms
- Data transformation is also a crucial issue during pre-modelling stages of the ANN model. To determine, which data scaling technique should be used, however, is not an easy task. The finding from this work indicated however, that the choice of data transformation technique depends solely on the type of activation functions in the hidden and output nodes. Among other transformation techniques, the log based transformation is comparably recommended for all types of transfer functions

7.1.2 Training stages

- The choice of number of hidden layers and hidden nodes is paramount since it will influence not only the complexity of the model but also its predictive capability and training time. Many "rules-of-thumb' have been proposed to estimate optimum number hidden nodes. This research however indicated that these general guidelines mostly do not perform well to find optimum hidden nodes numbers and they can only be used as preliminary prediction of lower and upper limit of the trial-error-method. In this work, combination of this two approach, trial-error and empirical formula proved to be a quicker process rather than tedious trial-error method without any boundary. One

hidden layer was also found to be sufficient as function approximator since multi hidden layer add complexity and do not show much better results.

- Weight initialisation will direct the network optimisation into its optimal solution. Random number generation is the most widely used weight and bias initialisation for ANN training. Among several random number generation approaches, technique based on Nguyen Widrow algorithm was found to be consistent to achieve convergence and its optimal solution
- Different configurations of transfer functions are possible to be used during ANN training. This research however, indicated that the use of tansig, logsig and radbas functions are recommended for hidden nodes since they provide sufficient nonlinearity to capture input-output variable relationship.
- MSE criterion is the most popular objective function for training and optimising the network. But since MSE is highly sensitive to the presence of the outlier, a bounded function based on logmse error measure was tested and the results show that this type of error measure tends to lead the training process having better convergence and performances.
- The last 'design variable' which must be selected during training phases is training algorithm. Several variants of back propagation algorithms exist and evolutionary based algorithms are currently popular. A comparative study of the different training algorithms were carried out and the results indicated that in terms of generalisation capability, the global optimisation like differential evolution is able to enhance the performance of traditional algorithms such as trainlm or trainbr. However, these hybrid algorithms have a limitation in terms of computational time where it was found to be nearly 12 fold. From this study, the use of trainlm is still recommended as it gives a faster convergence and comparably good results.

7.1.3 Post-modelling phases

Compared with other two phases, the post-modelling stages, namely prediction interval construction and knowledge extraction are rarely to discuss and present. This work presents a preliminary study of the post modelling phases of ANN modelling

and lays a foundation for further research and applications. From this study, two conclusions can be drawn:

- Constructing prediction interval is necessary to examine how confidence the prediction is and how good the model when it is used for extrapolation. Since, linear regression based confidence interval does not take into account the distribution of the data, a Kernel density estimator based prediction interval was proposed. The results show that this technique is able to build a prediction interval in various degree of confidence.
- Research on knowledge extraction of the ANN model should be directed on opening the black box and obtaining mathematical representation of the overall ANN models. Our preliminary study show that it is possible to extract the simple models from the trained ANN model

7.2 RECOMMENDATIONS FOR FUTURE RESEARCH DIRECTIONS

Further research should be directed into the following areas to enhance the applicability of the proposed method:

- The use of tunable transfer function, that is, adaptive transfer function to comply with the dynamic nonlinearity of the input-output data
- The use of multiple error criteria to ensure that the optimisation process does not get stuck into local minima and also to guarantee that the optimum network is obtained using more stringent criterion
- Application of the proposed method in the last chapter in the grey box modelling. The obtained mathematical representation which is simpler and easy to understand surely will benefit the grey box application and process control in general.
- Further refinement of the approach to extract both qualitative and quantitative information from the trained ANN model. Possibly, more efforts should be directed to the analysing behaviour of the interconnected transfer functions toward network weights and biases to obtain a global function representing these interconnected functions.

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