# Evidence for halo kinematics among cool carbon-rich dwarfs 

J. Farihi, ${ }^{1 \star}$ A. R. Arendt, ${ }^{1}$ H. S. Machado ${ }^{2}$ and L. J. Whitehouse ${ }^{1}$<br>${ }^{1}$ Department of Physics and Astronomy, University College London, London WC1E 6BT, UK<br>${ }^{2}$ Department of Astronomy, University of California, Berkeley, CA 94720-3411, USA

Accepted 2018 April 5. Received 2018 March 30; in original form 2018 March 10


#### Abstract

This paper reports preliminary, yet compelling, kinematical inferences for $N \gtrsim 600$ carbonrich dwarf stars that demonstrate around $30-60$ per cent are members of the Galactic halo. The study uses a spectroscopically and non-kinematically selected sample of stars from the SDSS, and cross-correlates these data with three proper motion catalogues based on Gaia DR1 astrometry to generate estimates of their 3D space velocities. The fraction of stars with halo-like kinematics is roughly 30 per cent for distances based on a limited number of parallax measurements, with the remainder dominated by the thick disc, but close to 60 per cent of the sample lies below an old, metal-poor disc isochrone in reduced proper motion. An ancient population is consistent with an extrinsic origin for $\mathrm{C} / \mathrm{O}>1$ in cool dwarfs, where a fixed mass of carbon pollution more readily surmounts lower oxygen abundance and with a lack of detectable ultraviolet-blue flux from younger white dwarf companions. For an initial stellar mass function that favours low-mass stars as in the Galactic disc, the dC stars are likely to be the dominant source of carbon-enhanced, metal-poor stars in the Galaxy.


Key words: proper motions - binaries: general - stars: carbon - stars: chemically peculiarstars: kinematics and dynamics - Galaxy: halo.

## 1 INTRODUCTION

The first dwarf carbon (dC) star was confirmed over 40 years ago, and, as with many astronomical discoveries past and present, it was discovered serendipitously in a large survey. G77-61 was first identified in the Lowell Observatory proper motion survey (Giclas, Burnham \& Thomas 1961), with the same purpose-built telescope and data that successfully discovered Pluto (Giclas 1958). Some decades later when a trigonometric parallax was obtained by the US Naval Observatory, the cool main-sequence star was initially unremarkable, and only later noted to be unusually red for its absolute magnitude. An optical spectrum eventually revealed strong molecular carbon bands, making G77-61 the first dC star (Dahn et al. 1977).

During the intervening decades, scientific progress on the origin and broader Galactic context of dC stars has been modest. Prior to the Sloan Digital Sky Survey (SDSS), roughly one dozen dC stars were identified by proper motion and objective prism surveys (Bothun et al. 1991; Green, Margon \& MacConnell 1991; Heber et al. 1993; Warren et al. 1993; Liebert et al. 1994; Lowrance et al. 2003), for which a giant stellar luminosity and thus distance (Wallerstein \& Knapp 1998) would imply highly unbound Galactic velocities. To date, only three dC stars have published trigonometric parallaxes (Harris et al. 1998), all with $9.6 \mathrm{mag} \leq M_{V} \leq 10.0 \mathrm{mag}$,

[^0]while ongoing work at the USNO indicates this range can vary up to around $\pm 2 \mathrm{mag}$ (Plant et al. 2016). Until forthcoming Gaia data releases that include a substantial number of reliable dC star parallaxes (duplicity may influence measurement errors), proper motion remains the best universal indicator of carbon star luminosity.

The SDSS has been transformative in terms of increasing both the number and diversity of definite and candidate dC stars. In the early years of the survey, including commissioning and DR1 data, spectroscopic fibres were dedicated to search for carbon stars on the basis of their photometric colours. This yielded a few hundred objects and increased the number of possible dC stars by roughly an order of magnitude (Margon et al. 2002; Downes et al. 2004). Proper motions based on the USNO-B1 catalogue (Monet et al. 2003) suggested the majority of the few hundred carbon stars thus discovered were bona fide dwarfs. However, by far the largest spectroscopic sample of (faint) carbon stars identified to date is the prodigious collection of 1211 SDSS sources described by Green (2013, hereinafter G13).

The prototype dC star has both clear halo kinematics and is among the most metal-poor stars known (Dahn et al. 1977; Plez \& Cohen 2005). In addition, there are a handful of proper motion selected dC stars with parallaxes and high velocity that are either halo or thick disc members (Warren et al. 1993; Harris et al. 1998). On the other hand, there are two spectroscopic composite dC systems containing a sufficiently blue white dwarf that were known prior to SDSS (Heber et al. 1993; Liebert et al. 1994), and another nine systems have been found in SDSS spectra (Rebassa-Mansergas et al. 2010;

G13; Si et al. 2014). These systems appear to have disc kinematics and this is consistent with the relative warmth and youth of the white dwarf components. A thorough and unbiased investigation into the Galactic origin of all dC stars is likely to require both Gaia and the large ground-based spectroscopic follow-up surveys coming online in the next few years.

In this work, the SDSS carbon star sample of G13 is crossmatched with recently published proper motion catalogues based on the astrometry from Gaia DR1, and SEGUE pipeline radial velocities, yielding robust 3D data for over 500-600 sources. These astrometric data sets represent several substantial improvements over previously available measurements, especially for faint and both fast- and slow-moving sources (Munn et al. 2004). Reduced proper motions for a sub-sample of over 600 stars with confident measurements suggest the bulk of dC stars lie below the thin-disc main sequence, and contain both thick-disc and halo stars of sub-solar metallicities. Based on the existing parallax data, $U V W$ space velocities are calculated for known dC star absolute magnitudes, where a median luminosity yields a fraction of halo stars that is at least 30 per cent, and a clear thick disc component. The data, catalogue matching, and sub-sample selection are described in Section 2, and the results are presented in Section 3. Preliminary conclusions are presented in Section 4 with an eye towards confirmation with Gaia DR2.

## 2 SAMPLE DEFINITION AND SELECTION

This study makes use of the existing SDSS catalogue data, correlating a large sample of dC star candidates with both radial velocity determinations and with the state-of-the-art proper motion catalogues based on Gaia DR1. Below are described the overall sample and catalogues, and additional criteria are imposed to ensure a relatively high-fidelity sub-sample for analysis.

### 2.1 Catalogue data

The basis of this kinematical study is the catalogue of carbon stars from G13, where selection was not based on proper motion or photometric colour, but instead took advantage of cross-correlation between existing spectroscopic targets and carbon star spectral templates within SDSS DR7 and DR8. In addition to a modest number of spurious objects that are readily rejected by visual inspection, G13 also identified dozens of carbon-rich white dwarfs, as well as a similar number of bluer stars showing carbon bands (referred to as G-type) that strongly cluster in colour space and which may be warmer counterparts to dC stars. While the sample may be incomplete or insensitive to dC stars with spectra that are sufficiently distinct from classical carbon giants, there is no kinematical bias, and hence the space motions of hundreds of carbon stars can be analysed with confidence.

The G13 sample of dC candidates was cross-matched with three recently published proper motion catalogues, all of which are based on Gaia DR1 astrometry. The first catalogue is that employed by Deason et al. (2017), where Gaia DR1 is used to recalibrate the SDSS astrometric mapping from first principles. Because this catalogue was produced and provided by the Institute of Astronomy (V. Belokurov 2017, private communication), it is referred to as IoA hereinafter. The second proper motion catalogue covering the SDSS footprint is HSOY (Altmann et al. 2017), and is based on combining Gaia DR1 astrometry with PPXML (Roeser, Demleitner \& Schilbach 2010), where the latter is tied to astrometry from 2MASS and USNO-B1. The third catalogue is GPS1 (Tian et al. 2017) and
is a combination of astrometry from Gaia DR1, Pan-STARRS, and SDSS.

Proper motion tables were uploaded locally and from VizieR ${ }^{1}$ into TOPCAT ${ }^{2}$ for manipulation. It was first necessary to cross-match the J2000 SDSS designations from G13 table 1 with the DR12 data base to obtain up to date SDSS parameters including, critically, objID and specObjID, which only became unique and permanent catalogue identifiers after DR7. Cross-matching with the IoA proper motion catalogue was done by objID, whereas for HSOY and GPS1 the catalogue matching was done by right ascension and declination converted to degrees from J2000 designations. In these latter two cases, a search radius of 6 arcsec was found to be ideal, as the epochs of some GPS1 catalogue positions were ambiguous. The matched tables were then joined using concatenation in topcat.
A critical part of the available kinematical data for the carbon star sample are the radial velocities sourced from the SEGUE survey and pipeline (Lee et al. 2008; Yanny et al. 2009). The radial velocities thus produced were measured by cross-correlation against either the SDSS commissioning templates (Stoughton et al. 2002) or ELODIE spectroscopic templates (Prugniel \& Soubiran 2001) degraded to SDSS resolution, with ELODIE templates often providing the best match. Each entry in the cross-matched catalogues above was queried with the crossid software provided by the SDSS by matching its position to the nearest primary object, with the retrieved primary objID checked to ensure it matched that of each dC candidate.

For the 1211 objects in table 1 of G13, the above SDSS DR12 query produced a total of 1344 matches, thus indicating that 112 dC candidates possessed two or more spectroscopic observations, and therefore the same number of specObj ID. These objects with duplicate spectra were flagged, evaluated, and consolidated so that all cross-matched catalogues had exactly 1211 entries. Stars with more than a single spectrum and radial velocity determination were assessed by taking the mean radial velocity, after weighting by the spectroscopic $\mathrm{S} / \mathrm{N}$.

### 2.2 Data cuts

Fig. 1 plots the SEGUE pipeline reported error in radial velocity as a function of the SDSS pipeline parameter snMedian_r (spectroscopic $\mathrm{S} / \mathrm{N}$ over the photometric $r$ band), demonstrating a clear correlation. After visual inspection of all 1211 spectra, only sources with snMedian_r $>5$ were retained for analysis. This data cut served not only to remove objects with large uncertainties in their radial velocity, but also to ensure the target spectrum was that of a genuine carbon star, as a handful of contaminants were identified by visual inspection (see G13).

Another requirement for the kinematical analysis was that the total proper motion be greater than at least a few standard errors. These vary among the three proper motion catalogues, and are generally constant near $2{\text { mas } \mathrm{yr}^{-1} \text { up to } 18 \text { th magnitude, but can rise to }}_{\text {to }}$ 4 mas $\mathrm{yr}^{-1}$ at the faint end of SDSS $r$ band or Gaia $G$ band (Altmann et al. 2017; Deason et al. 2017; Tian et al. 2017). Because the G13 sample contains over 600 sources fainter than $r=19.0 \mathrm{AB}$ mag, the adopted requirement is a total proper motion $\mu>10$ mas $\mathrm{yr}^{-1}$, which should be at least $5 \sigma$ for brighter stars and always above $2 \sigma$.
The top of Table 1 lists the number of G13 stars present in various proper motion catalogues, and those remaining after the two

[^1]

Figure 1. SDSS and SEGUE pipeline parameters for the error in radial velocity from spectral template matching, versus the spectroscopic S/N in the $r$ band. This latter quantity, snMedian_r was in general the highest of all the available S/N diagnostics in both the standard SDSS and SEGUE spectroscopic parameters. There are 1187 stars with determined radial velocities plotted as grey circles, but after a cut at snMedian_r $>5$ to eliminate unreliable data, there are 961 stars remaining and overplotted as black circles.

Table 1. Space velocity inferences for a sub-sample of bona fide dC stars.

| Catalogue | IoA ${ }^{\text {a }}$ | HSOY | GPS 1 |
| :---: | :---: | :---: | :---: |
| $N\left(\mathrm{G} 13 \cap \mathrm{SDSS} v_{\text {rad }}\right)$ | 978 | 962 | 965 |
| $N\left(\cap \mu>10 \mathrm{mas} \mathrm{yr}^{-1}\right)$ | 652 | 680 | 671 |
| $N(\cap$ snMedian_r $>5$ ) | 535 | 598 | 637 |
| $M_{r}=11.0 \mathrm{AB}$ mag: |  |  |  |
| $\langle V\rangle\left(\mathrm{km} \mathrm{s}^{-1}\right)$ | -53 | -57 | -58 |
| $\sigma_{V}\left(\mathrm{~km} \mathrm{~s}^{-1}\right)$ | 61 | 68 | 69 |
| $2 \times f\left(V<-200 \mathrm{~km} \mathrm{~s}^{-1}\right)$ | 0.04 | 0.08 | 0.08 |
| $f\left(T>200 \mathrm{~km} \mathrm{~s}^{-1}\right)$ | 0.14 | 0.16 | 0.16 |
| $M_{r}=9.5 \mathrm{AB}$ mag: |  |  |  |
| $\langle V\rangle\left(\mathrm{km} \mathrm{s}^{-1}\right)$ | -93 | -103 | -105 |
| $\sigma_{V}\left(\mathrm{~km} \mathrm{~s}^{-1}\right)$ | 85 | 102 | 107 |
| $2 \times f\left(V<-200 \mathrm{~km} \mathrm{~s}^{-1}\right)$ | 0.21 | 0.28 | 0.30 |
| $f\left(T>200 \mathrm{~km} \mathrm{~s}^{-1}\right)$ | 0.28 | 0.30 | 0.32 |
| $M_{r}=8.0 \mathrm{AB}$ mag: |  |  |  |
| $\langle V\rangle\left(\mathrm{km} \mathrm{s}^{-1}\right)$ | -174 | -195 | -197 |
| $\sigma_{V}\left(\mathrm{~km} \mathrm{~s}^{-1}\right)$ | 146 | 182 | 195 |
| $2 \times f\left(V<-200 \mathrm{~km} \mathrm{~s}^{-1}\right)$ | 0.71 | 0.77 | 0.78 |
| $f\left(T>200 \mathrm{~km} \mathrm{~s}^{-1}\right)$ | 0.54 | 0.56 | 0.56 |

${ }^{a}$ This catalogue appears incomplete for total proper motions $\mu>50-100$ mas $^{\mathrm{yr}}{ }^{-1}$ (see the text).
data cuts. It is noteworthy that all three proper motion catalogues provide a similar total number of raw matches with the dC star candidate sample, and also after the proper motion cut, but then differ by several tens of stars after the $\mathrm{S} / \mathrm{N}$ requirement is imposed. In the highest fidelity sub-samples, the IoA catalogue contains the fewest matches, which appears to be due to a deficit of the highest proper motion stars. Relative to GPS1, the IoA catalogue has 34 fewer sources with $\mu>100$ mas $_{\text {yr }}{ }^{-1}$, and 55 fewer sources with $\mu>50$ mas $_{\mathrm{yr}}{ }^{-1}$. Owing to the highest number of reliable matches (and thus likely completeness) in GPS1, results from this catalogue are adopted here, but the findings from all three catalogues are similar and listed in Table 1.


Figure 2. Reduced proper motion in $g$ band versus $g-i$ colour, both in AB magnitudes, using the GPS1 cross-matched sample of 980 stars plotted as grey circles. After making a total proper motion cut $\mu>10 \mathrm{mas} \mathrm{yr}^{-1}$ to eliminate sources with proper motion consistent with zero (see the text), this number reduces to 677 stars that are plotted as black circles. Three stellar isochrones are plotted using the Dartmouth stellar evolution models (Dotter et al. 2008), and are intended to serve as rough guides for the (older) thin disc, thick disc, and halo. The position of G77-61 is marked with a large red star, and while it is known to be a halo star and one of the most metal-poor objects known, its position suggests it is not far from the norm.

## 3 KINEMATICAL INFERENCES

In the following, both reduced proper motion and 3D space velocity estimates are used to infer the likely Galactic orbital and birth regions of bona fide dC stars. Galactic $U V W$ space velocities are calculated for all three sets of proper motion catalogue cross-matches and for a range of distance estimates based on measured dC star parallaxes.

### 3.1 Reduced proper motion

In this section, results for the GPS1 cross-matched sub-sample are analysed, and in the next section all three catalogues are compared (and shown to be similar). Reduced proper motions were calculated following Munn et al. (2017), using their equation (2). Ignoring corrections for Galactic latitude, the reduced proper motion in SDSS $g$ band is
$H_{g}=g+5 \log \mu+5=M_{g}+5 \log v_{\tan }-3.379$,
where $\mu$ is the magnitude of the proper motion in $\operatorname{arcsec} \mathrm{yr}^{-1}$ and $v_{\tan }$ is the velocity in the plane of the sky in $\mathrm{km} \mathrm{s}^{-1}$. The lefthand side of the equation is used to plot the GPS1 crossed-matched stars in Fig. 2, and the right-hand side is used to plot theoretical isochrones. First are plotted all 980 stars in common with G13 and GPS1, and then this number is reduced to 677 stars with significant proper motions. The plot demonstrates that the cut to eliminate proper motions consistent with zero generally acts to de-populate the brighter regions of the diagram. The first noteworthy feature of Fig. 2 is the possibility of up to three weakly defined loci. There is a dense group radiating along $(x, y)=(2.0,19)$, a more diffuse clump near $(2.2,17)$, and a relatively small number of stars focused around $(0.8,15)$. If these features are real, which is not completely certain, then they could hint at clusters of stars with similar metallicity and kinematics. The latter group with the bluest colours is almost certainly the G-type carbon dwarfs described by G13.

Three representative stellar isochrones are overplotted on Fig. 2, and are taken from the Dartmouth stellar evolution data base (Dotter et al. 2008). The choice of isochrones is somewhat arbitrary, and they were selected to represent a range of ages, metallicities, and associated kinematics as a visual guide to the broad characteristics of the reduced proper motions. It should also be noted that for a given stellar mass and $T_{\text {eff }}$, carbon dwarf colours should be somewhat distinct from those of their oxygen-rich, K and M dwarf counterparts. Model stellar atmospheres and spectra are not yet developed and available for dC stars, but these isochrones should nevertheless be instructive. The top track is for solar metallicity stars of age 5 Gyr , with tangential speed $50 \mathrm{~km} \mathrm{~s}^{-1}$ and should be a good proxy for older objects of the thin disc. The middle model is for modestly metal-poor stars of age 10 Gyr , moving at $100 \mathrm{~km} \mathrm{~s}^{-1}$, and should be a decent approximation for the metal-poor thick disc (Fuhrmann 2004). The bottom isochrone is for metal-poor Population II stars of age 15 Gyr and speed $200 \mathrm{~km} \mathrm{~s}^{-1}$, as would be expected for halo denizens. None of the isochrones have $\alpha$ element abundances different from solar.

While none of these definitively overlap with densely plotted regions of the diagram, they do provide a general indication of the underlying population. Ignoring the stars rejected due to proper motions consistent with zero, it is clear these are all dwarf stars. That is, based on the GPS1 measurements, there are at least 677 bona fide dC stars confirmed by their combination of brightness and proper motion. Another tentative conclusion that may be drawn is that there appears to be only a small fraction of thin disc stars, and the bulk of dC stars are more consistent with thick disc and halo origins. About 92 per cent of the plotted black sources lie below the isochrone representing the thin disc, and nearly 60 per cent lie below the isochrone depicting thick disc stars. Interestingly, G77-61 sits near the main locus and above the halo-like isochrone in Fig. 2 even though it is known to be an extremely metal-poor star. Thus the diagram is likely useful for the broad characteristics of the dC population, but not for any individual star.

### 3.2 Galactic space velocities

The 3D space velocities were calculated for all three proper motion catalogue subsamples to ensure the results were consistent. Here $(U, V, W)$ refers to a right-handed coordinate system where $U$ is positive towards the Galactic anticentre, $V$ is positive in the direction of Galactic rotation, and $W$ is positive towards the North Galactic pole. The sample of SDSS dC stars does not have parallaxes or other distance determinations, and thus the velocities in the plane of the sky depend linearly on the actual distances. Below, a range is explored that should encompass the bulk of dC stars.
While there are only three dC stars with published parallaxes, roughly 20 stars have been monitored by the USNO over the past decades. Harris et al. (1998) report $9.6 \mathrm{mag} \leq M_{V} \leq 10.0 \mathrm{mag}$ for three stars, with G77-61 at the faint end of this range, and Plant et al. (2016) cite unpublished work where dC stars measured to date have 7.5 AB mag $<M_{r}<11.5 \mathrm{AB}$ mag (note the use of the SDSS $r$ band rather than $V$ ). Translating the $r=13.2 \mathrm{AB}$ mag (Zacharias et al. 2013) measured for G77-61 into an absolute magnitude yields $M_{r}=9.4 \mathrm{AB}$ mag for this prototype dC star, and this places it in the centre of the absolute brightness distribution.
Based on the above parallax data, and the fact that G77-61 is a part of the principal broad locus in the reduced proper motion diagram, it is likely that $M_{r}=9.5 \mathrm{AB}$ mag is a good approximation for the bulk of dC stars. However, to ensure that that any inferences are not skewed by an inappropriate choice of stellar distances, $U V W$ cal-
culations are also made for absolute magnitudes $\pm 1.5$ mag brighter and fainter. Ideally, a better method could employ a random sampling of $M_{r}$ based on a known distribution, or use dC star colours as a proxy for $T_{\text {eff }}$ and hence luminosity. However, neither of these approaches is currently feasible. The distribution of dC star luminosities is not well-determined, and the USNO program stars were intentionally selected to sample a range of properties and should not be considered representative of the underlying population. Despite the range of $M_{r}$ quoted above, the colour of stars with parallaxes are tightly clustered (J. A. Munn 2018, private communication). For this reason, and because mass, metallicity, and carbon abundance all affect luminosity and colour, using a range of $M_{r}$ for the entire sample is the most efficient approach prior to Gaia parallax measurements.
Fig. 3 plots all three sub-samples of dC stars as Galactic $V$ histograms, and as Toomre energy diagrams in order to distinguish between disc- and halo-like kinematics. While these are all essentially similar, the absence of the relatively high proper motion stars in the IoA catalogue is apparent. Two broad conclusions can be tentatively drawn from these results, on the basis that $M_{r}=9.5 \mathrm{AB} \mathrm{mag}$ is a decent approximation of the dC population. First, dC stars lag behind the rotation of the Galactic disc, implying that old stars are the dominant species, either thick disc or halo. The non-Gaussian shape of the distribution indicates there are at least two components. Secondly, there are a substantial number of stars with total (peculiar) space velocities above $200 \mathrm{~km} \mathrm{~s}^{-1}$, and are therefore halo members. This may be a conservative estimate, as halo stars often have total velocities above $150-200 \mathrm{~km} \mathrm{~s}^{-1}$ (Pauli et al. 2006), and the reduced proper motion diagram suggests a higher halo fraction.
Table 1 lists the statistical characteristics for each of the three proper motion catalogue subsamples, and for each of the three absolute magnitudes and hence distance approximations. For each of the latter, the mean Galactic $V$ is listed together with its dispersion and two estimates of the fraction of stars with halo-like space motions. Stars with $V<-200 \mathrm{~km} \mathrm{~s}^{-1}$ are not rotating with the Galactic disc, and because there should be an equal number of retro- and pro-grade halo objects, this fraction is doubled to approximate a Gaussian distribution of non-rotating stars. Another statistic selects stars with $T>200 \mathrm{~km} \mathrm{~s}^{-1}$ as objects with probable halo velocities. These fractions may be lower limits to the true fraction of halo stars, as their distribution in $V$ is only a single dimension (Chiba \& Beers 2000; Fuhrmann 2004), and total space motion ignores directionality (and dispersion).
The most conservative result is that calculated for $M_{r}=11.0 \mathrm{AB}$ mag and suggests that at least around $10-15$ per cent are halo stars, and that a typical dC star lags behind the Galactic disc by $50-60 \mathrm{~km} \mathrm{~s}^{-1}$. In this case there would be a substantial old disc component in the stellar population, because the thick disc has $\langle V\rangle=-30 \mathrm{~km} \mathrm{~s}^{-1}$ (Chiba \& Beers 2000). The least conservative estimates are calculated for $M_{r}=8.0 \mathrm{AB}$ mag and would imply that at least 55 per cent of dC stars are members of the halo; while potentially remarkable, it is unlikely based on parallax work that this is the case (and the dispersion in $V$ would be roughly twice that of halo stars!). The case adopted here for interpretation is the middle panel of the table for $M_{r}=9.5 \mathrm{AB}$ mag, where at least about 30 per cent of dC stars were formed in the Galactic halo. In this case the dC population has a $\sigma_{V}$ similar to halo stars, but where the mean is roughly half that for a pure halo population. This is probably best explained by a mixture of halo and thick disc stars. It is noteworthy that the middle luminosity assumption produces a similar fraction of stars with halo-like kinematics via two diagnostics, and also consistent with the reduced proper motions.


Figure 3. Space velocity plots for the sub-samples of SDSS dC candidates with matches in each of the IoA, HSOY, and GPS 1 proper motion catalogues, with $M_{r}=9.5 \mathrm{AB}$ mag. The left-hand panels are Galactic $V$ velocity histograms. The dashed lines show the number of catalogue matches that also have an SDSS spectroscopic pipeline parameter snMedian_r $>5$. The solid lines include only those subsets with total proper motion $\mu>10 \mathrm{mas}^{-1}$, and thus measurements that are greater than $2 \sigma$ to $5 \sigma$ (Altmann et al. 2017; Deason et al. 2017; Tian et al. 2017). Following on the exclusion of proper motions consistent with zero, the peaks in $V$ all shift to negative velocities that lag behind Galactic disc rotation (see Table 1). The right-hand panels are Toomre diagrams for the solid-lined histogram stars. Contours for total (peculiar) space velocity $T^{2}=U^{2}+V^{2}+W^{2}$ are labelled as dashed grey lines, and the colour of each data point is weighted by $T$ with white corresponding to zero and black to $250 \mathrm{~km} \mathrm{~s}^{-1}$ and beyond. There are almost 200 stars with unambiguous, halo-like velocities among the stars in the GPS1 sub-sample, which has the highest number of matches. However, with $T=209 \mathrm{~km} \mathrm{~s}^{-1}$, G77-61 would not stand out in these diagrams, and so the halo fraction estimates in Table 1 are likely to be somewhat conservative.

## 4 CONCLUSIONS

With the largest sample of dC star candidates assembled to date, and proper motion catalogues derived from Gaia DR1 astrometry, the analysis here demonstrates that at least around 680 are genuine main-sequence stars, and that a significant fraction have kinematical properties consistent with halo membership. Importantly, this spectroscopically identified sample is free of kinematical bias towards older and higher velocity stars.
The exact fraction of halo stars among carbon-rich dwarfs depends on the distance estimates used here based on a handful of parallaxes, and also where halo objects are distinguished from high-velocity disc stars. If objects with total space velocity below $200 \mathrm{~km} \mathrm{~s}^{-1}$ are considered to be disc stars, then the halo fraction is around 30 per cent for a population with $M_{r} \approx 9.5 \mathrm{AB}$ mag. The distribution of Galactic $V$ velocities suggests that dC stars are primarily a combination of halo and old thick dise members, with a small but real thin disc component. Overall, the dC stars lag behind the rotation of the Galaxy and are thus consistent with a relatively old population. Their positions in a reduced proper motion diagram suggest the bulk of stars are metal poor, and a halo fraction as high as 60 per cent. All of the above is consistent with the lack of photometric and spectral evidence for warm to hot white dwarf companions to the bulk of dC stars.
In a scenario where dC stars are formed via binary mass transfer from a carbon-rich giant (Dahn et al. 1977), stars with an intrinsically lower metal - and thus oxygen - abundance require a lower mass of atmospheric pollution to achieve $\mathrm{C} / \mathrm{O}>1$. The prototype dC star G77-61 is a single-lined spectroscopic binary with a 245 d period (Dearborn et al. 1986), and an ongoing radial velocity study of a few dozen dC stars is consistent with a 100 per cent binary fraction (Whitehouse et al. 2018). Together these two facts imply the dC stars are analogous to CEMP-s stars (Starkenburg et al. 2014; Hansen et al. 2016). The above facts may suggest that thin disc dC stars are rare, and only occur in systems with orbits favourable to efficient mass transfer, and where the carbon-rich giant evolves from a sufficiently early-type progenitor (Lau, Stancliffe \& Tout 2007).

An intriguing possibility is that the dC stars are not only the dominant type of carbon star, but also the most common CEMP star, in the Galaxy. This prospect has a firm basis in the behaviour of the initial stellar mass function, at least in the disc, where far more low-mass stars form than stars of higher mass, and specifically there are over three times as many M-type dwarfs than FGK stars. ${ }^{3}$ The occurrence of red dwarf stars peaks somewhere between M3 and M4 and in the mass range $0.2-0.4 \mathrm{M}_{\odot}$, both as field stars and as companions to the intermediate-mass progenitors of white dwarfs (Farihi, Becklin \& Zuckerman 2005; De Rosa et al. 2014). If correct, and with future modelling that incorporates the molecular bands that dominate dC star spectra, these cool dwarfs may provide the largest sample of nearby stars that represent the earliest stages of Galactic chemical evolution. The full potential of dC stars and their exact Galactic component fractions should soon be resolved via Gaia parallaxes.

## ACKNOWLEDGEMENTS

The authors acknowledge V. Belokurov and S. E. Koposov for providing their proper motion catalogue, J. A. Munn for exchanges
on the current state of dC star and SDSS astrometry, H. C. Harris and C. A. Tout for input on an early draft. This research has made use of the VizieR catalogue access tool, CDS, Strasbourg, France.

## REFERENCES

Altmann M., Roeser S., Demleitner M., Bastian U., Schilbach E., 2017, A\&A, 600, L4
Bothun G., Elias J. H., MacAlpine G., Matthews K., Mould J. R., Neugebauer G., Reid I. N., 1991, AJ, 101, 2220

Chiba M., Beers T. C., 2000, AJ, 119, 2843
Dahn C. C., Liebert J., Kron R. G., Spinrad H, Hintzen P. M., 1977, ApJ, 216, 757
De Rosa R. J. et al., 2014, MNRAS, 437, 1216
Dearborn D. S. P., Liebert J., Aaronson M., Dahn C. C., Harrington R., Mould J., Greenstein J. L., 1986, ApJ, 300, 314
Deason A J., Belokurov V., Koposov S. E., Gómez F. A., Grand R. J., Marinacci F., Pakmor R., 2017, MNRAS, 470, 1259
Dotter A., Chaboyer B., Jevremović D., Kostov V., Baron E., Ferguson J. W., 2008, ApJS, 178, 89

Downes R. A. et al., 2004, AJ, 127, 2838
Farihi J., Becklin E. E., Zuckerman B., 2005, ApJS, 161, 394
Fuhrmann K., 2004, Astron. Nachr., 325, 3
Giclas H. L., 1958, Lowell Obs. Bull. No. 89
Giclas H. L., Burnham R., Thomas N. G., 1961, Lowell Obs. Bull. No. 112
Green P. J., 2013, ApJ, 765, 12 (G13)
Green P. J., Margon B., MacConnell D. J., 1991, ApJ, 380, L31
Hansen T. T., Andersen J., Nordström B., Beers T. C., Placco V. M., Yoon J., Buchhave L. A., 2016, A\&A, 588, A3

Harris H. C. et al., 1998, ApJ, 502, 437
Heber U., Bade N., Jordan S., Voges W., 1993, A\&A, 267, L31
Lau H. H. B., Stancliffe R. J., Tout C. A., 2007, MNRAS, 378, 563
Lee Y. S. et al., 2008, AJ, 136, 2050
Liebert J., Schmidt G. D., Lesser M., Stepanian J. A., Lipovetsky V. A., Chaffe F. H., Foltz C. B., Bergeron P., 1994, ApJ, 421, 733
Lowrance P. J., Kirkpatrick J. D., Reid I. N., Cruz K. L., Liebert J., 2003, ApJ, 584, L95
Margon B. et al., 2002, AJ, 124, 1651
Monet D. G. et al., 2003, AJ, 125, 984
Munn J. A. et al., 2004, AJ, 127, 3034
Munn J. A. et al., 2017, AJ, 153, 10
Pauli E. M., Napiwozki R., Heber U., Altmann M., Odenkirchen M., 2006, A\&A, 447, 173
Plant K. A., Margon B., Guhathakurta P., Cunningham E. C., Toloba E., Munn J. A., 2016, ApJ, 833, 232
Plez B., Cohen J. G., 2005, A\&A, 434, 1117
Prugniel P., Soubiran C., 2001, A\&A, 369, 1048
Rebassa-Mansergas A., Gänsicke B. T., Schreiber M. R., Koester D., Rodrguez-Gil P., 2010, MNRAS, 402, 620
Roeser S., Demleitner M., Schilbach E., 2010, AJ, 139, 2440
Si J., Luo A., Li Y., Zhang J., Wei P., Wu Y., Wu F., Zhao Y., 2014, Sci. China Phys. Mech. Astron. 57, 176
Starkenburg E., Shetrone M. D., McConnachie A. W., Venn K. A., 2014, MNRAS, 441, 1217
Stoughton C. L. et al., 2002, AJ, 123, 485
Tian H. J. et al., 2017, ApJS, 232, 4
Wallerstein G., Knapp G. R., 1998, ARA\&A, 36, 369
Warren S. J., Irwin M. J., Evans D. W., Liebert J., Osmer P. S., Hewett P. C., 1993, MNRAS, 1, 185
Whitehouse L. J., et al., 2018, MNRAS, submitted
Yanny B. et al., 2009, AJ, 137, 4377
Zacharias N., Finch C. T., Girard T. M., Henden A., Bartlett J. L., Monet D. G., Zacharias M. I., 2013, AJ, 145, 44

This paper has been typeset from a $\mathrm{T}_{\mathrm{E}} \mathrm{X} / \mathrm{LAT} \mathrm{T}_{\mathrm{E}} \mathrm{X}$ file prepared by the author.

[^2]
[^0]:    * E-mail: j.farihi@ucl.ac.uk

[^1]:    ${ }^{1}$ http://vizier.u-strasbg.fr/viz-bin/VizieR
    ${ }^{2}$ http://www.star.bris.ac.uk/ $\sim$ mbt/topcat

[^2]:    ${ }^{3}$ www.recons.org

