

University of Dundee

A methodological approach to assess the hazard of underground cavities subjected to environmental weathering

Castellanza, Riccardo ; Lollino, Piernicola; Ciantia, Matteo

Published in:
Tunnelling and Underground Space Technology

DOI:
[10.1016/j.tust.2018.08.041](https://doi.org/10.1016/j.tust.2018.08.041)

Publication date:
2018

Document Version
Peer reviewed version

[Link to publication in Discovery Research Portal](#)

Citation for published version (APA):
Castellanza, R., Lollino, P., & Ciantia, M. (2018). A methodological approach to assess the hazard of underground cavities subjected to environmental weathering. *Tunnelling and Underground Space Technology*, 82, 278-292. <https://doi.org/10.1016/j.tust.2018.08.041>

General rights

Copyright and moral rights for the publications made accessible in Discovery Research Portal are retained by the authors and/or other copyright owners and it is a condition of accessing publications that users recognise and abide by the legal requirements associated with these rights.

- Users may download and print one copy of any publication from Discovery Research Portal for the purpose of private study or research.
- You may not further distribute the material or use it for any profit-making activity or commercial gain.
- You may freely distribute the URL identifying the publication in the public portal.

Take down policy

If you believe that this document breaches copyright please contact us providing details, and we will remove access to the work immediately and investigate your claim.

1 **A methodological approach to assess the hazard of underground cavities**
2 **subjected to environmental weathering.**

3
4 *Castellanza Riccardo¹, Lollino Piernicola², Ciantia Matteo³*

5
6 ¹*Department of Earth and Environmental Sciences, University of Milano-Bicocca, Milano*
7 *(ITALY) (riccardo.castellanza@unimib.it)*

8
9 ²*IRPI - Consiglio Nazionale delle Ricerche, Bari (ITALY) (p.[lollino@ba.irpi.cnr.it](mailto:p.lollino@ba.irpi.cnr.it))*

10
11 ³*School of Science and Engineering, University of Dundee, Dundee*
12 *(m.o.ciantia@dundee.ac.uk)*

13
14
15
16 **Keywords:** methodological approach, environmental weathering, soft rocks, numerical
17 modelling, hazard assessment

18
19
20 **Abstract**

21 Soft highly porous carbonate rocks such, as calcarenites, and soluble sulphate rocks, as gypsum, are
22 very common in the Mediterranean region and, due to their microstructure and chemical
23 composition, are prone to water induced weathering mechanisms. Cliffs, underground cavities and
24 other morphological features in such formations are hence affected by intense erosion phenomena
25 and weathering processes responsible of unexpected collapses and sinkholes. Just considering the
26 Apulian region (Italy), 150 sinkholes have been recorded since 1925, with increasing frequency since
27 2000 (Fiore et al. 2018). The geosystem's failure is often the short or long-term result of a very
28 complex hydro-chemo mechanical process taking place at the micro-scale which can be detected
29 and analysed by means of field and laboratory experimental test campaigns. Therefore, stability
30 problems are often related to changes of the mechanical properties of the rock forming the cave
31 caused by environmental weathering processes, despite the external boundary conditions are not
32 changing with time. The paper deals with the assessment of hazard associated to the stability of
33 abandoned underground caves, which is nowadays frequently required for land and urban planning
34 activities. A methodological approach for hazard assessment based on a step-by-step procedure is
35 proposed. This includes in-situ surveys, laboratory experimental studies, theoretical analyses and
36 finally numerical investigations. The approach derives from the experience developed from several
37 case studies analysed by the authors. In this work, two of these are presented. The first one concerns
38 the stability of an anthropic cavity in a calcarenite formation which is affected by a water induced
39 short-term and long-term debonding processes. The second one regards the stability of a three-

40 level abandoned gypsum mine, the lowest level being partially flooded by water. The
41 methodological procedure aims to evaluate the factors controlling the change of the mechanical
42 properties of the rock leading to failure, so that efficient remediation measures can be designed in
43 order to avoid any further decay of the rock mass stability with time.

44 The proposed methodological approach, validated on real case studied, shows the convenience of
45 performing advanced experimental, theoretical and numerical studies to properly assess the hazard
46 in space and time and to better design the mitigation measures if they are required. The adoption
47 of the proposed approach reduced the remediation costs of the second case study to one order of
48 magnitude.

49

50 **1. Introduction**

51

52 The assessment of hazard associated to the stability of man-made underground caves, which were
53 exploited and abandoned some decades ago, is still nowadays frequently underestimated during
54 land and urban planning activities. This is generally related to the loss of historical memory
55 concerning the existence of old underground caves in land management processes, as well as the
56 change of the boundary conditions working on the cave systems that leads to the consequent
57 variation of the rock material properties over time, even in a relatively short time. High risk
58 conditions are also enhanced by the fast development of urban areas, which gives frequently rise
59 to the existence of buildings and infrastructures lying over caves that cannot be considered as safe.
60 Recent case studies of collapse of man-made underground caves, with consequent sinkholes
61 affecting urbanized areas, are well described in the literature, as for example those involving the
62 calcarenite caves in Southern Italy ([Parise and Lollino 2011](#), [Vattano et al. 2013](#)), the metal mining
63 caves in Canada ([Betournay, 2009](#)), the siltstone Longyou caverns in China ([Li et al. 2009](#), [Yang et al.](#)
64 [2011](#)), the limestone mines in the Netherlands and Belgium ([Bekendam 1998](#); [Van Den Eeckhaut et](#)
65 [al. 2007](#)).

66 Instability of caves is frequently associated to the occurrence of degradation of the mechanical
67 properties of the rock surrounding the cave as a consequence of environmental processes. In
68 particular, water infiltration from ground surface or pipe leakage, increment of relative humidity of
69 the cave environment, as well as more extreme cave flooding are all related to the increment of the
70 degree of saturation of the rock over time and the consequent rock degradation (Figure 1). This is

71 particularly true for those rocks that are highly sensitive to the interaction with water, as for
72 example evaporitic rocks and soft porous rocks. Several studies have been proposed on this subject,
73 as for example those concerning the iron ore abandoned mines in Lorraine, as discussed in [Grgic et](#)
74 [al. \(2006\)](#), the aging of gypsum in underground mines ([Auvray et al. 2004](#), [Castellanza et al. 2010](#))
75 and the works on the debonding processes affecting the calcarenite outcropping in Southern Italy
76 ([Andriani and Walsh, 2007](#); [Ciantia and Hueckel, 2013](#); [Ciantia et al. 2014, 2015](#)).

77 The methods for the assessment of stability of underground caves that are available in the scientific
78 literature can be generally classified according to three classes: phenomenological, analytical and
79 numerical approaches. Phenomenological methods are generally based on abaci that show areas
80 representing stable or unstable cave configurations on the basis of geometrical parameters of the
81 cave and strength parameters of the rock, as derived from a large number of case studies ([Potvin](#)
82 [and Milne 1992](#), [Nickson 1992](#), [Carter 1992](#), [Goodings and Abdulla 2002](#)). Analytical closed-form
83 solutions have been instead widely used to calculate elastic solutions for roofs with very simple
84 geometries, such as caves with circular or rectangular shape ([Obert and Duvall 1967](#), [Jaeger and](#)
85 [Cook 1979](#)), followed by closed form solutions accounting for the elasto-plastic behaviour of the
86 rock material ([Lippmann 1971](#), [Ribacchi and Riccioni 1977](#), [Brown et al. 1983](#), [Detournay and](#)
87 [Fairhurst 1987](#), [Panet 1995](#), [Carranza-Torres and Fairhurst 1999](#), [Gesualdo et al. 2001](#), [Diederichs](#)
88 [and Kaiser 1999](#)).

89 Recently, numerical modelling has provided a powerful tool to explore the stress-strain state within
90 the rock mass around the cavities and the corresponding displacement field induced by a specific
91 loading condition or changes of boundary conditions, also adopting advanced non-linear
92 constitutive models. To mention a few, [Mortazavi et al. \(2009\)](#) propose a numerical investigation of
93 the failure mechanism of rock pillars in underground openings by taking into account the effect of
94 pillar geometry and pillar strength parameters for typical situations existing in the Canadian mines.
95 [Bekendam \(1998\)](#) studied the stability of calcarenite and limestone mine pillars in the Netherlands
96 by means of two-dimensional elasto-plastic finite element (FE) models, also implementing time-
97 dependent creep processes, whereas [Parise and Lollino \(2011\)](#) highlighted with the same 2D FE
98 approach the role of the degradation processes of the limestone and calcarenite rock surrounding
99 caves in Southern Italy in the development of sinkholes. [Ferrero et al. \(2010\)](#) detect the areas of
100 highest stress concentration and calculate the corresponding safety factors of the most loaded
101 pillars by means of 3D FE analysis of old underground calcareous quarries in the Western Alps (Italy).
102 [Ghabezloo and Pouya \(2004\)](#) perform a FE analysis aimed at studying roof stability of limestone

103 caves in France due to tensile strength degradation induced by karst processes. [Diederichs \(2003\)](#)
104 investigates rock fracture mechanisms and global collapse of caves by means of the distinct element
105 method, whereas [Wang et al. \(2011\)](#) explore the failure mechanisms of underground cave pillars by
106 means of the application of the Rock Fracture Propagation Analysis. From a theoretical point of
107 view, a well-consolidated experience has been gathered in the numerical application of simple
108 elasto-plastic constitutive models, such as those implementing the Mohr-Coulomb or the Hoek-
109 Brown failure criterion (Pelizza et al. 2000, Zhang et al. 2016, [Fazio et al. 2017](#), Jiang et al. 2017).
110 Trinh and Jonsson (2013) developed an elasto-plastic finite element model of an underground
111 cavern room in hard rocks, also accounting for the effects of reinforced bolts. On the other hand,
112 more advanced constitutive models have been recently implemented in numerical codes to
113 simulate the variation of the rock mechanical properties due to environmental factors and the
114 coupled chemo-mechanical processes associated ([Fernandez-Merodo et al. 2007](#); [Grgic et al. 2006](#);
115 [Ciantia and Castellanza 2016](#); [Tamagnini and Ciantia 2016](#)).

116 Based on the aforementioned technological development, the paper aims to propose a procedure
117 of hazard assessment for underground caves, based on the experience and the theoretical research
118 developed by the Authors in some recent case histories. In particular, a methodological approach
119 based on in-situ surveys (including the use of Laser-Scan techniques to define model geometry),
120 laboratory and field investigations, theoretical and numerical analyses are presented in the
121 following. Afterwards, two case studies are discussed within the framework of the procedure
122 proposed and some conclusions regarding the evolution of the cave stability over time are drawn
123 accordingly.

124 **2. Methodological approach**

125 The proposed methodological approach for the quantitative assessment of failure susceptibility
126 associated to the presence of underground caves follows a procedure formed of six steps (Figure 2):

- 127 1) *In-situ survey*: preliminary field surveys should be carried out both inside the caves and at
128 the ground surface according to either conventional topographical survey methods or
129 advanced tools, as laser-scan techniques, in order to define a three-dimensional geometrical
130 model of the overall area; then, a detailed geological and hydro-geological analysis should
131 follow to define the lithological model, the geo-structural setting and the eventual existence
132 of hydro-geological features, as water circulation or infiltration from ground surface;

133 2) *Choice of the conceptual model*: this second stage should be aimed at defining the general
134 features of the real problem's schematization and is represented by the choice between a
135 2D or a 3D model geometry (based on the eventual existence of plane-strain conditions), as
136 well as the choice between a continuum or a discontinuum model, according to the eventual
137 existence of relevant joints;

138 3) *Experimental analysis*: this step is finalized at defining the factors that play a major role in
139 the stability of the rock mass around the cave, as current mechanical properties of the
140 involved material, susceptibility of the rock to weathering and degradation processes,
141 propagation of weathering according to sharp-front or preferential ways, etc. At this stage,
142 accurate laboratory tests aimed at characterizing the most important physical and
143 mechanical properties of both the intact and the weathered rock material (unit weight,
144 porosity, water content, elastic stiffness, uniaxial compressive strength, tensile strength,
145 shear strength at high stress levels), as well as defining how the weathering degree changes
146 with time and in space, should be performed. In particular, the laboratory tests should give
147 an indication of the degree of in-situ weathering occurred from the time of cave excavation
148 to the present, the thickness of the layer affected by the weathering process, the in-situ
149 environmental conditions as well as the evolution of the weathering process; to this purpose,
150 artificial weathering scenarios can be useful to define the law of variation of the rock
151 strength in the short- and in the long-term. In particular, it is convenient to define: i) a short
152 term weathering to describe the quick reduction of geomechanical properties of the rock
153 material from dry to wet conditions; ii) a long term weathering associated to a relatively slow
154 weathering process usually induced by chemical dissolution processes.

155 The results of the experimental analysis are then used to both initialize the initial conditions
156 of the numerical model and to define a set of representative environmental scenarios in
157 order to assess the cave stability in the short- and in the long-term.

158 4) *Theoretical analysis*: The mathematical model needed to describe the main features of the
159 geomechanical behaviour of the rock, i.e. the constitutive model, should be here defined
160 and calibrated using the experimental test results. Due to the large difference of timescales
161 between mechanical and chemical processes (Ciantia and Hueckel, 2013) the assumption of
162 uncoupled chemo-mechanical behaviour is considered to be reasonable (Ciantia et al, 2014).
163 The use of elastic constitutive models, adopted for the application of simple analytical

164 methods in preliminary hazard assessment (see section #1), should be avoided as the elasto-
165 plastic behaviour that characterises any geomaterial should be properly taken into account.
166 A Mohr-Coulomb elastic-perfectly plastic model is deemed to be appropriate for problems
167 where shear type of failure is dominant (when the mean effective stress, p' , is low), whereas
168 an elasto-plastic model with the Hoek-Brown failure criterion (Hoek and Brown, 1997)
169 should be instead preferred in order to account, according to the equivalent continuum
170 approach, for the influence of the eventual rock mass fracturing state or the non-linearity of
171 the failure envelope at high p' . In a complex 3-D boundary value problem these simple
172 constitutive models could be correctly used only to detect the critical areas where local
173 plastic yielding starts to develop, since the eventual brittle behaviour of the rock material is
174 not accounted for.

175 Coupled hydro-chemo-mechanical advanced constitutive models could be eventually used
176 to reduce the risk of oversimplification of both the spatio-temporal weathering evolution
177 and the material mechanical behaviour (Ciantia et al., 2018).

178 5) *Numerical analysis*: in this stage of the methodology the chosen elasto-plastic constitutive
179 model is used to run FE analyses in order to define a quantitative assessment of the stability
180 of the underground cave in the current state and eventually a possible scenario of the
181 evolution of the stability with time (step #6: *hazard assessment*). At this stage, Preliminary
182 results obtained with analytical methods based on elastic theory for either roof or pillar
183 stability problems should be compared with the results of numerical elasto-plastic models.
184 The choice of a 2D or 3D model depends on the eventual existence of plane strain conditions.
185 In case of complex geometries, 3D modelling is mandatory. For those problems where no
186 precise information of specific input data is available, 2-D sensitivity analyses are suggested
187 to highlight the influence of specific factors, as the initial stress state of the rock mass or the
188 flow rule of the constitutive model adopted. In general, the numerical model should be
189 aimed at simulating the current state of the rock mass domain, by implementing the
190 mechanical and hydraulic boundary conditions, the excavation process of the cave and the
191 existing loading conditions.

192 More sophisticated approach, suitable to describe the brittle failure mechanism of cavities
193 are now suitable to be applied in 2D models (Lollino and Andriani, 2017), although in this

194 paper it is shown that the continuum approach is still one of the most convenient tool to
195 perform quantitative hazard assessment analyses especially in 3D.

196 6) *Hazard assessment*: If stable conditions result from the model representing the current state
197 of the rock-mass (final result of step #5: numerical analysis), a strength reduction calculation
198 stage, simulating the weathering mechanisms both for STD and LTD weathering processes,
199 should be performed to derive an indication of the safety factor. This can be done using the
200 $c-\phi$ reduction numerical technique (Griffiths and Lane, 1999; Aliguer et al, 2013).

201 Rock weathering can be subdivided in two main temporal stages: one in the short term (STD)
202 and the other in the long term (LTD). The first can be considered as the result of an imbibition
203 process: water penetrates through the porous structure causing an instantaneous drop in
204 strength (Cherblanc et al, 2016). The second one is the result of the chemical dissolution of
205 the rock mass when interacting with water for long time periods inducing further damage
206 (Ciantia et al, 2015a). The driving scalar variables of this two hydro micro-scale weathering
207 mechanisms were found to be the saturation degree, S_r , and normalized dissolved mass, ξ_{dis} ,
208 respectively (see Ciantia et al, 2014). The concept of non-mechanical softening driven by the
209 two-latter mentioned scalar quantities (S_r and ξ_{dis}) introduced by Ciantia et al, 2013 using a
210 multiscale approach (see Ciantia and di Prisco, 2016), is extended to the practical
211 methodology of the $c-\phi$ allowing to obtain a physical time evolution of the safety factor
212 (Ciantia et al, 2015b). In fact, as the evolution of the yield locus can be described as a function
213 of saturation degree, S_r , for the STD process, the dissolved mass, ξ_{dis} , induces in the LTD
214 process a similar shrinkage of the yield locus (Tamagnini and Ciantia, 2016).

215 On the other hand, as explained by Ciantia and Hueckel (2013), the worst weathering
216 scenario is the one characterized by a rapid saturation and consequent fresh water recycle.
217 Under these conditions, using specific weathering experimental test results that describe the
218 strength evolution with S_r , for the short term debonding (STD) and physical time for the long
219 term debonding LTD (step #3), it is possible to build the $c-\phi$ reduction coefficient - time
220 abacus for the intact rock in an uncoupled manner and without having to solving the chemo-
221 hydraulic problem. Consequently, the classical $c-\phi$ reduction numerical analysis combined
222 with the procedure here presented enables to estimate the evolution with time of the safety
223 factor, $F_s(t)$.

224 From a conceptual point of view, the stability factor of an ideal man-made cave, F_s , can be
225 considered as evolving with time according to the scheme proposed in Figure 3. The figure
226 reports that the stability factor of an underground cave at the time of excavation, i.e. initial
227 conditions, is represented by F_0 and corresponds to the unweathered mechanical properties
228 of the rock material. As weathering process proceeds with time, the stability factor of the
229 cave, $F_s(t)$, tends to reduce due to rock mechanical weakening and the corresponding law of
230 variation might be potentially defined by performing numerical analyses implementing
231 different sets of rock mechanical properties corresponding to different steps of the
232 degradation process. Therefore, at time t_r , when a stability factor of the cave equal to F_r has
233 been reached and analysis for remediation is required, two possible approaches for
234 remediation can be followed (Figure 3): 1) structural interventions, aimed at increasing rock
235 mass strength, or 2) conservative interventions, aimed at preventing any further mechanical-
236 weakening weathering process. The first can generally lead to an increment of the stability
237 factor (curve 1), whereas the latter is intended to maintain the cave stability constant over
238 time (curve 2). Frequently, the second option includes preservation of air ventilation,
239 reduction of water infiltration, prevention of chemical dissolution processes, creation of rock
240 surfaces impervious to environmental weathering using specific chemical consolidation
241 products, these being advisable for those cases when environmental preservation is
242 required, as for cultural heritage sites. In this case, the increment of stability factor should
243 be interpreted as the distance between curve (2) and curve (a) leading to rock mass failure,
244 at time t_F , in Figure 3. Such conservative interventions should be pursued along with
245 monitoring activities aimed at controlling that the environmental conditions corresponding
246 to curve (2) are effectively maintained in situ. This means that the environmental variables
247 should be monitored as first and the rock mechanical properties should be controlled in
248 order to kept them about constant over time, also by performing in-situ or laboratory tests
249 at regular time intervals.

250 The following case studies specify in detail the application of the methodology proposed to highlight
251 how the effects of the environmental weathering could be practically evaluated in situ and in
252 laboratory, how these effects can be taken into account using simple constitutive models and how
253 complex three-dimensional finite element analyses could be very useful to assess hazard from a
254 quantitative point of view. All the numerical analyses are run using GTS-NX FEM code (2010) and
255 the NAFEMS (1983) suggestions have been considered for the setup of the analyses.

256 In this research, a deterministic approach has been adopted with its inherent limitations. Such
257 drawback leaves room for further research and may be addressed by employing a probabilistic
258 approach (Griffiths and Fenton, 2004; Fenton and Griffiths, 2008; Gong et al. 2018).

259 **3. Case studies**

260 Two representative case studies are here presented in order to describe the methodology outlined
261 in the previous section and highlight some criteria which might be adopted in the procedure of
262 hazard assessment of underground caves in urbanized areas. The first case is represented by man-
263 made caves excavated in a calcarenite deposit in the urban area of Canosa di Puglia (Southern Italy),
264 whereas the second one is a large multiple-level cave system formed of pillars and rooms located in
265 San Lazzaro di Savena (BO, Northern Italy). For both the cases, rock is affected by high susceptibility
266 to weathering processes and hazard conditions exist since the cavities lie below a densely urbanised
267 area.

268 **3.1. Case study #1: Canosa di Puglia (Southern Italy)**

269 In this case study the stability of two caves (Figure 4) excavated about two centuries ago within a
270 calcarenite deposit belonging to the “Calcarenite di Gravina” Formation is investigated. The first,
271 cave A, is overlaid by an older (B1 in Figure 4b) and a more recent building (B2 in Figure 4b); in
272 particular, the recent building is founded on piles that cross the cave and transfer the structural
273 loads below the cave. Cave B is instead characterized by a more complex geometry, with a building
274 located at the ground surface (see Figure 4).

275 A plan view of the buildings and the cave geometry is shown in Figure 4b; owing to the complex
276 subsurface geometry, it was decided to carry out a 3D laser-scan survey (see Figure 4c) according to
277 Step #1 in Figure 2. The advantage of using such technology is the high-accuracy geo-referentiation
278 of the interacting bodies. A geological survey is also performed to define the state of the rock mass,
279 with regard to the eventual existence of joints, local stratigraphy, possible presence of water and
280 evidence of environmental weathering within the cave. The main outcomes of the geological survey
281 indicate that the rock mass can be classified as massive, i.e. no presence of relevant discontinuities,
282 no water circulation is observed around the cave, relative humidity ranges between 60% and 90%
283 and temperature is between 12° and 20°. Based on the results of the geometrical and geological
284 survey (step #1), the conceptual model, developed according to step #2, implied the adoption of a
285 3D FEM analysis aimed at studying the behaviour of the rock mass as a continuum. Owing to the

286 homogeneous state of the Calcarenite formation, just few points (see Figure 4b) are chosen for
287 sampling the material to be tested experimentally (Step #3). 110-mm diameter cores are drilled for
288 a depth of about 70 cm from the inner surface of the cave; then, 38-mm and 54-mm diameter
289 samples are retrieved within the larger cores at a distance of 10, 20 and 50 cm from the cave
290 boundary surface in order to assess the variation of the rock mechanical properties with depth from
291 the cave wall, z_s in Figure 5.

292 It is known that calcarenites from southern Italy exhibit high susceptibility to water induced
293 weathering (Castellanza and Nova (2004), Andriani and Walsh (2007), Castellanza et al. (2009)) and
294 therefore, the experimental campaign is aimed at investigating the effects of the two microscale
295 debonding processes that could take place in the short (STD) – and long-term (LTD) (see Ciantia et,
296 al 2014 for details including sample preparation). Referring to the eventual mechanical decay
297 induced by water saturation of the calcarenite (STD) and the slow chemically-induced mechanical
298 decay of the saturated rock (LTD), the following experimental analysis (Step #3) has been carried
299 out:

- 300 - Micro-scale tests (Figure 6), including thin sections, SEM (Scanning Electron Microscopy) and
301 XRPD (X-Ray Powder Diffraction), reveal that: i) the microstructure of the calcarenite is
302 characterized by the presence of diagenetic (DG) and depositional (DP) bonds that connect
303 calcite grains with organogeneous origin, as well as ii) an average porosity equal to $n = 0.45$ and
304 iii) a 98% mean composition of calcite;
- 305 - STD laboratory weathering is explored by means of Uniaxial Compressive Test (UCT) and
306 Brazilian Test (BT) on dry, partially saturated and saturated (wet) calcarenite (Figure 7a),
307 and a reduction of both strength and stiffness up to 50% of the corresponding values
308 representative of dry conditions is recorded after few minutes of soaking of a dry calcarenite
309 specimen (Figure 7b). Since these tests are thought to reflect the effects of water infiltration
310 in the cave, such a marked reduction should be properly considered for hazard assessment.
311 For details related to saturation process and sample preparation see Ciantia et al. (2014).
- 312 - LTD laboratory weathering tests such as “chemical” creep tests on calcarenite specimens
313 subjected to water flux under constant load. For the specific case study, such tests have
314 proved that the DG bonds dissolve very slowly when flushed by water with a pH value of 7,
315 thus causing a strength reduction of 5% after 8 months. On the contrary, if a pH value of 2.8

316 is adopted the same strength reduction occurs in just few hours. The LTD tests can be seen
317 as the worst representative weathering scenario of a flooded cave (Ciantia et al. 2014).

318 - The effects of in-situ weathering were evaluated by performing UCT and BT on saturated
319 specimens retrieved at 10, 20 and 50 cm from the cave wall (see Figure 5). Despite the
320 significant scatter, the test results, as reported in Figure 8, do not show significant reduction
321 of the rock uniaxial compressive strength (UCS) and stiffness with z_s . These results suggest
322 that no significant weathering has developed with z_s after more than 250 years of exposition
323 to the environmental conditions. Therefore, it can be inferred that if the current
324 environmental conditions (H_r (relative humidity) < 100% and no water infiltration) are
325 maintained, the mechanical properties of the rock are supposed to remain constant in these
326 cavities.

327 The theoretical analysis (step #4) is carried out on the basis of the results of the experimental
328 analysis performed (step #3). An elastic-perfectly plastic model with non-associated Mohr-Coulomb
329 (MC) failure criterion and tension cut-off is chosen and consequently calibrated to reproduce the
330 mechanical behaviour of the calcarenite. Despite the curvilinear yield locus generally observed
331 (Ciantia et al. 2014, Figure 9a), at low stress levels the failure envelope of the Gravina calcarenite
332 can be reasonably approximated as linear by using a Mohr-Coulomb yield criterion (Figure 9b). In
333 this case, the main drawback of using perfect plasticity models is the impossibility of capturing the
334 observed brittle behaviour of the calcarenite, so that a more rigorous approach should consider the
335 application of sophisticated constitutive models able to cope with the mechanical and chemical
336 softening process (Nova et al. 2003, Ciantia and di Prisco, 2016).

337 In general, it should be point out that the soundness of the numerical analyses implementing simple
338 constitutive models (MC and HB models) is conditioned by the two following assumptions:

- 339 1. all the stress points lie within the elastic domain, so that the distance from the failure
340 envelope for each single point is a local indication of the safety margin;
- 341 2. when the stress point reaches the yield locus, the onset of a global failure mechanism could
342 imply the overestimation of the strength capacity of the rock structure, since the real
343 softening response is neglected. From this point of view, a numerical model providing only
344 local plastic zones can instead be considered as acceptable.

345 Assuming the simplified approach discussed above, the MC failure envelopes (Figure 10) of the
346 calcarenite for different saturation degree are calibrated using laboratory tests results. Since the
347 caves studied are daily used as a car parking for Cave A and historical visit for Cave B (hence
348 prolonged flooded conditions can be excluded) hazard assessment is performed only for the STD
349 process. In particular, the weathering scenario considered is an initially dry material (f_{dry}) that is
350 gradually saturated (f_{STD}) until a state of complete saturation is attained (f_{wet}).

351 Once the constitutive model is calibrated and the simplifying assumptions are clearly stated, the the
352 3D FEM numerical analysis required for the hazard assessment of the cavity-building system can be
353 performed (*step#5* in Figure 2). In Figure 11, 3D geometrical solids have been created from the laser-
354 scansions to describe the foundations system of the buildings and the volume of the cavities. A
355 proper numerical domain has been considered in order to minimize the side effects on the
356 numerical results considering an average distance of 10 m from the cave boundaries. The selected
357 meshes (Figure 11b) is formed of 100000 and 400000-node-tetrahedric linear elements for Cave A
358 and Cave B respectively. For the Cave B the major discontinuities retrieved in the survey have been
359 explicitly taken into account by modelling a solid interface (made of solid elements) where the
360 strength parameter was reduced with respect to the massive calcarenite (cohesion reduced to 20%
361 of the intact one, friction angle to 70% and dilatancy set to 0).

362 A preliminary series of analyses with quadratic elements (8 noded) with different mesh sizes are
363 also performed to assess the influence of the mesh dependency of the numerical solution and define
364 the best compromise in terms of computational time.

365 The construction stage procedure is composed of four stages for both Cave A and B:

- 366 1) a geostatic stress initialization referred to a free field condition, i.e. before both cave
367 excavation and building construction, is assumed; the set of parameters prescribed for the
368 calcarenite at this stage is equal to that corresponding to dry conditions (see Figure 10) and
369 a value of k_0 equal to 0.5 is used following the in-situ investigations (*step #2*);
- 370 2) the numerical simulation of the excavation is carried out by removing the elements in 10
371 load steps, following the actual excavation process based on historical reports. During such
372 numerical stage, the development of plastic yielding in the rock mass surrounding the cave
373 is carefully monitored to identify eventual failure mechanisms. This numerical analysis

374 corresponds to *a-posteriori* assessment of the stability conditions of the rock mass during
375 the excavation process;

376 3) the simulation of the building construction at ground surface is performed considering the
377 exact sequence of building construction. In particular, only the pressure transmitted to the
378 foundation has been considered for B1 and B3 buildings, whereas the complete soil-
379 structure interaction system is simulated for B2. As for stage 2, the eventual development
380 of plastic mechanisms is verified to assess the stability of the cave system during
381 construction.

382 4) the simulation of the in-situ weathering processes is finally performed by reducing the
383 strength parameters of the calcarenite during saturation, as described in Figure 10. For this
384 purpose, the strength and stiffness parameters of the rock domain are reduced from dry to
385 wet (Figure 10), thus simulating the STD process. An overview of some stress components
386 are shown in Figure 12b and Figure 12c in order to identify domain areas with a significant
387 stress concentration, as well as plastic strains are monitored. Both for Cave A and B, the
388 numerical results indicate that even for a completely saturated material (f_{wet}) no failure
389 mechanism develops, since only local plastic zones form at the base of some piles (see Figure
390 12b for Cave A) or at the corners of the cave system (see Figure 12d for Cave B). For cave B
391 only, an additional reduction of the yield surface is considered to simulate also the long term
392 debonding process (f_{LTD}). During the LTD experimental test, a strength reduction of 5% in 8
393 months was recorded. This process is simulated adopting the strength reduction method.
394 After a strength reduction factor of 4, corresponding to 10 year of constant water flux, the
395 cave system is still not affected by a global failure mechanism. In fact plastic zones are only
396 located in the lateral wall of cave B and no critical failure of the roof is recorded (Figure 12d).
397 Finally, as shown in Figure 12e, the calculated displacements in this critical scenario generate
398 a surface subsidence of few millimetres (max value is 2.5mm) that does not induce any
399 damage in the building B3.

400 Based on the results of the whole numerical process, the cave systems can be classified as safe, both
401 under dry and wet conditions (step # 6, hazard assessment). Nevertheless, the cave system should
402 be kept as dry as possible by means of air ventilation and by preventing water infiltration.

403

404

405 3.2. Case study #2: San Lazzaro cave (BO, Northern Italy)

406 This case study is represented by an abandoned gypsum mine (Figure 13) in the village of San Lazzaro
407 di Savena, close to Bologna (Italy). Here, mining was carried out until the end of the '80s following
408 the "room and pillar" method and the final cave system ($\approx 350.000 \text{ m}^3$) is organized according to
409 three floors (Figure 14). During the mining operations, a karst cave was intercepted and karst water
410 flowed into the mine ($\approx 80.000 \text{ m}^3$). As a consequence, the lower mining level was completely
411 flooded and this condition has lasted up to the present due to the cave abandonment. Moreover,
412 water circulation and infiltration from ground surface produced critical conditions prone to
413 instability in several portions of the mining levels. In this context, buildings and infrastructures were
414 constructed above the first and second level of the cave in the '70s and nowadays a large urbanized
415 area around the Savena river is located downstream of the cave area, being at risk of flooding of a
416 large volume of water.

417 Geomechanical properties of gypsum are known to change over time; in fact, water, or even air
418 humidity, dissolve or weaken gypsum rock (Grgic et al. 2006). Therefore, the aim of the present
419 study is the evaluation of the safety conditions of both the pillars and the cave roofs as well as the
420 assessment of the effects of a possible collapse of the mine system on the buildings located at
421 ground surface.

422 According to the methodology described in Section 2, a topographical survey by means of a total
423 station, along with the analysis of existing maps, allowed to define the geo-referenced three-
424 dimensional system of the cave and the detailed geometry of the ground surface of the urbanized
425 slope. Moreover, detailed geological surveys are carried out with the aim of identifying the major
426 issues in place. In particular, the quarry is hosted in macrocrystalline gypsum layers belonging to the
427 Gessoso Solfifera Formation, overlaid by a silty clay layer, as shown in Figure 14b. The rock mass can
428 be considered as massive, except for some areas, where some inclined joint sets, with large spacing,
429 and the presence of karst phenomena are observed. A detailed geomechanical survey of the pillars
430 is also carried out in order to acquire the parameters useful for the rock mass classification RMR
431 (Bieniawski 1973), Q system (Barton et al. 1974) and GSI (Hoek 1977). The chemical analyses of the
432 subsurface lake water indicate a conductivity of about 2100-2200 μS , a concentration of sulfates of
433 1350-1450 mg/l and an average temperature T of 9°C. A large part of the shallower cave level is
434 affected by rainfall water infiltrating from the ground surface and from the karst system: these
435 phenomena are believed to increase over time due to the strong solubility of gypsum rock.

436

437 As for the previous case, the conceptual model here adopted (Step #2) is defined based on the in-
438 situ surveys. In particular, a 3-D continuum model is chosen based on the massive aspect of the rock
439 mass and a FE model has been developed accordingly, as described in detail afterwards. Following
440 the equivalent continuum approach (e.g. Hoek and Brown, 1997) the presence of large-spaced joints
441 and discontinuities is taken into account by treating the rock mass as a continuum with reduced
442 geomechanical properties.

443 First of all, a standard geomechanical characterization by UC, BT and TX tests on the fresh gypsum
444 (Unweathered Rock - UR) was performed as shown in Figure 15. Then, in order to study the spatial
445 effect of weathering, a series of UC and BT tests were performed on specimens taken at different
446 drilling depths (70 m, Figure 14), at an average spacing of about 5 m, with the value of the in-situ
447 water content. The tests were performed on 8-cm diameter specimens enabling to define the whole
448 failure envelope of the material with depth. Due to the experimental test results, the gypsum rock
449 was classified into three levels of weathering: the portion above the 1st level was indicated as fresh
450 *unweathered rock* (UR), whereas the gypsum corresponding to the 1st and 2nd levels, since it was in
451 prolonged contact with humid air, was named *humid rock* (HR). Finally, the gypsum surrounding the
452 3rd level, being flooded by water, has been named as *flooded rock* (FR). UR gypsum is found to be
453 characterized on average by a UCS strength of 12 MPa, a Young modulus E of 2.1 GPa and it can be
454 classified as EL according to Deere and Miller (1966). Figure 14b shows the boreholes dedicated to
455 evaluate the weathering process. Nevertheless, in the same area more than 25 boreholes were
456 already present and a large number of on site and laboratory investigations were performed during
457 and after the mining activity. This guarantees the homogeneity assumption here considered.

458

459 In particular, Figure 16 summarizes the variation of UCS (σ_c , Figure 16a), secant Young modulus (E_s ,
460 Figure 16b) and tensile strength (σ_t , Figure 16 c) as a function of depth. The UCS strengths of HR and
461 FR are found to be respectively 20-30% and 50-60% less than the corresponding strength of UR. A
462 similar trend is also found for the tensile strength reduction, whereas the same drop of stiffness (\approx
463 65%) is observed for both the HR and the FR. The dispersion of the data in Figure 15 and especially
464 in Figure 16 is due to the size of the gypsum crystals (about 1 cm), compared to the reduced
465 diameter of the specimens (between 4 and 8 cm) necessary to reproduce weathering in laboratory
466 time.

467 To corroborate the reduction of strength as an effect of flooding (FR), an additional series of UC
468 tests was performed on smaller specimens ($D = 24$ mm; $H/D = 2$) immersed in situ in the 3rd level
469 water for different time lags. The results are reported in Figure 17a and show a marked reduction
470 (up to 50% drop of the dry UCS) just after 15 days of immersion; after this initial reduction, no further
471 drops are observed within one year of immersion. These results are consistent with the amount of
472 strength reduction observed at the depth of the flooded level (Figure 16). Finally, a small-scale test
473 showing the collapse of a pillar after 10 days in a water flux of 2 l/h is shown in Figure 17b; this test
474 could be considered a further confirmation of the risk related to the pillar failure when an
475 unsaturated water enters the cave system.

476 An elastic-perfectly plastic model with an HB failure criterion is adopted for the gypsum rock mass
477 Figure 18a). The laboratory scale ($D = 80$ mm) strength envelope for the intact rock (UR_{LAB} line in
478 Figure 18b) is obtained by fitting the Mohr's circles at failure derived from the UC, BT and TX tests
479 (Figure 18a). Size effects are then accounted for by using a Weibull distribution: the in-situ mass size
480 larger than the critical size of 1 m (Castellanza et al. 2010) is accounted for by reducing the
481 laboratory UCS strength of about 35% (UR_{situ} line in Figure 18b). To take the weathering process into
482 account, a further strength reduction (equal to the UCS strength drop shown in Figure 16a) is used
483 to comply with the HR_{situ} and FR_{situ} strength (see also Table 1 for the specific parameter of the HB
484 failure loci referred to the in situ condition). Finally, the effect of the existence of a joint set in the
485 rock mass (see step #1) is accounted for by applying a reduced value of $GSI=82$ according to the
486 suggestions proposed by Cai et al. (2004). The final strength envelopes considering all the effects
487 (size, weathering and in-situ jointed state) are represented in Figure 18b with the labels $UR_{situ-jointed}$,
488 $HR_{situ-jointed}$ and $FR_{situ-jointed}$. The shallow silty clay layer is modelled using an elastic-perfectly plastic
489 Mohr-Coulomb model.

490
491 At this point the 3D FE analyses are carried out in order to develop hazard assessment according to
492 Step #5 in Figure 2. As shown in Figure 19, detailed 3D geometrical solids have been created for the
493 entire hill incorporating the mine system and the overlying building; an optimized discretization
494 mesh, highly refined in the area of the cave system, is adopted. As for the previous case, the impact
495 of mesh dependency on the numerical results is preliminary assessed by performing a series of
496 elastic analyses with different mesh refinements.

497 As a preliminary assumption, the pillars are considered as the structures of the cave system most
498 susceptible to failure and therefore hazard assessment is firstly focused on the evaluation of the

499 safety margin of each pillar with respect to collapse; in fact, according to the Authors, the collapse
500 of a single pillar would induce a process of sequential collapse of the adjacent pillars (pin failure
501 mechanism), which in turn is likely to generate consequent failures of the chamber roofs and
502 eventually give rise to a proper sinkhole phenomenon. Therefore, concerning the assessment of the
503 safety margin of each pillar, two different methodologies have been followed. In the first, a simple
504 3D elastic analysis that does not require any construction stage is enough to evaluate the safety
505 factor of each pillar with simplified approach; in the second, a fully non-linear analysis requiring a
506 construction stage procedure is used to identify the most critical pillars.

507 *Step #5 - Methodology 1:* according to [Obert and Duvall \(1967\)](#) approach, the safety factor of the
508 general pillar, i , is firstly calculated as the ratio between the *in-situ* UCS strength of the pillar at the
509 actual scale ($\sigma_{lim,i}$) and the mean value of the *in-situ* axial stress existing in the same pillar ($\sigma_{situ,i}$). In
510 particular, for the pillars located at the 1st and 2nd levels of the cave, the value of $\sigma_{lim,i}$ is considered
511 equal to the UCS strength corresponding to $HR_{situ-jointed}$, whereas for the pillars at the 3rd level it is
512 assumed equal to $FR_{situ-jointed}$. Differently from the conventional procedures usually accounting for
513 the loading area acting on the single pillar, the *in-situ* stresses $\sigma_{situ,i}$ of each pillar is evaluated based
514 on the results of a 3D FEM elastic analysis. Figure 20 shows the resulting contours of the vertical
515 stress in the pillars. For this calculation, the values of the tangent elastic modulus at 50% of the
516 compressive strength, E_{50} , are assumed and the $\sigma_{situ,i}$ are evaluated by averaging the vertical stresses
517 calculated in the Gauss points in the mid-height section of the pillar. The values of the calculated
518 safety factors are reported in the hazard map shown in Figure 21. Based on this approach, a large
519 number of pillars of 3rd level are in critical conditions ($1 < F_s < 1.1$) while pillars at the 2nd and 1st
520 levels (L1 and L2) result to be in safe conditions ($F_s > 1.6$) except for a single pillar (P7-1 - red area
521 in Figure 21), located at the 1st level ($F_s = 1.15$). It is worthwhile stressing that while critical pillars at
522 the 3rd level L3 have no buildings overlying at the ground surface, pillar P7-1 does.

523 *Step #5 - Methodology 2:* in this case a series of non linear elasto-plastic 3D FEM analyses are carried
524 out in order to simulate the actual conditions of the overall mine system. The above calibrated
525 elastic-perfectly plastic constitutive model adopting the HB failure envelope for each class of
526 weathered gypsum (UR, HR, FR; see step #3) is used. The numerical analyses are performed
527 according to the following construction stage procedure:

- 528 1) geostatic stress state is initialized before mine excavation and building construction,
529 assuming homogeneous gypsum rock mass conditions, represented by $UR_{situ-jointed}$;

- 530 2) mine excavation is simulated by removing groups of elements in accordance with the
531 historical sequence of cave exploitation;
- 532 3) building construction is simulated by the application of equivalent pressure loads;
- 533 4) in situ weathering process at present is simulated by means of the reduction of the HB model
534 parameters from $UR_{\text{situ-jointed}}$ to $HR_{\text{situ-jointed}}$ for the gypsum of the 1st and 2nd levels and to
535 $FR_{\text{situ-jointed}}$ for the gypsum of the 3rd level, as defined in Step #3. Plastic strains ϵ^p developed
536 only in some of the abandoned-mine pillars and contours of deviatoric plastic strains are
537 shown in Figure 22. The numerical results in terms of the amount and distribution of
538 deviatoric plastic strains confirms that: i) no global failure mechanism develops within the
539 roofs as no ϵ^p are recorded in such locations; ii) for the level L1, ϵ^p are concentrated in the
540 pillars, so that they can be considered as one of the weakest structures of the whole system;
541 iii) an amount of ϵ^p develops in pillar P7-1 of the 1st level. This result suggests that the elastic
542 analyses obtained with the [Obert and Duvall \(1967\)](#) approach presented above are
543 reasonable.
- 544 5) A long term *worst-scenario* process is simulated by progressively removing the most critical
545 pillars, starting from the removal of critical pillars in the 3rd level L3, which is the one
546 characterized by the minimum values of F_s , followed by progressively deactivating pillars and
547 roofs, as shown in Figure 23. The *worst-scenario* concludes when a large number of pillars at
548 the 3rd level, along with the roof and the overlying pillars at the 2nd level, are deactivated.
549 The sequence of pillar removal is performed according to the following procedure: the pillar
550 to be removed is the one closest to failure with relevant plastic strains and the minimum
551 safety factor evaluated with Obert and Duvall (1967) approach; whenever a pillar is removed
552 the load acting on the removed pillar is transferred to the surrounding pillars and therefore
553 the values of the F_s for the active pillars are updated always with Obert and Duvall (1967)
554 approach. According to this procedure, the implicit drawback represented by neglecting the
555 brittle behaviour and the crack propagation associated with the observed post-failure fragile
556 response of gypsum is reduced. As shown in Figure 23, this procedure allows to define a
557 subsidence basin of 30000m² at ground surface that do not significantly affect any building.
558 In this perspective, the performed 3D numerical analysis is capable of describing a very
559 critical scenario and should be considered as a tool for predicting the negative consequences
560 in terms of subsidence. These results were used to design a currently ongoing monitoring

561 campaign and to decide not to undertake any remediation measure to prevent settlement
562 damage to buildings (Ciantia et al. 2018).

563 6) An additional catastrophic scenario adopting 3D CFD analyses were used to evaluate the
564 amount of water that could be eventually ejected outside the mine and eventually flooding
565 the downstream village. It was decided to consider a further unfavourable condition which
566 is the simultaneous collapse of the entire roof of Level 3 to maximize the impact of the falling
567 down gypsum mass on the volume of water present in mine. The results are shown for
568 different time intervals in Figure 24. It could be shown that the analyses revealed the internal
569 buffering capacity of the intact portion of Level 2. Furthermore, the analyses allowed to
570 assess the volume and the velocity of the water that can flood out from Level 1 towards the
571 urbanized area. The estimated volume of the flooding water is about 2000 m³. It represents
572 approximately the 2% of the water that flood the mine. This amount is compatible with small
573 channelling works to bring this water in the Savena River located just outside the mine. The
574 forecasting of flooding water revealed again a low risk for the urbanized area. The technical
575 details can be found in Castellanza et al 2015.

576 As regards step #6 of the methodology (i.e. hazard assessment), some important considerations
577 arise based on the previously described results for this specific case study: i) the most critical part
578 of the cave system is represented by the 3rd level L3 where a large number of pillars result to be in
579 critical conditions; ii) assuming a catastrophic scenario of sequential pillar collapse, the consequent
580 subsidence basin and the amount of flooding water does not significantly affect the existing
581 buildings; iii) to increase the safety conditions, some structural reinforcements of the existing most
582 critical pillars should be considered. For flooded level 3, the proposed remediation measure consists
583 of reducing the inflow of fresh water, avoiding further dissolution as the current concentration of
584 the solute mass is at maximum. With respect to the initial idea to fill the entire level 3 with a fluidized
585 cemented soil as in Castellanza et al. (2010), the final cost of the proposed countermeasures is less
586 than one order of magnitude of the initial one. It means that a small investment in the proposed
587 methodological approach including experiments and theoretical and numerical predictions produce
588 a large amount of money saved.

589 **5. Conclusions**

590 The paper describes a methodological approach for hazard assessment of underground caves within
591 soft rock masses affected by weathering, based on a step-by-step procedure that includes in-situ

592 surveys, laboratory experimental studies, theoretical analyses and finally numerical investigations.
593 The procedure aims to evaluate the physical variables on which depend the variation of strength
594 and stiffness of the cave rock up to failure, so that efficient remediation measures can be adequately
595 defined. When the primary cause of instability is rock mechanical weakening evolving with time, as
596 triggered by water, humidity or chemical weathering, safety conditions of the underground cave are
597 observed to reduce with time, even if loading conditions are maintained constant with time. To
598 derive reliable assessments of the cave stability conditions, the methodological approach is applied
599 to three complex case histories, two of which considering underground cave systems in calcarenite
600 formations and one referring to an abandoned gypsum mine. The results suggest that:

- 601 - A detailed rock characterization, carried out through laboratory and field investigations, is
602 fundamental in order to identify the susceptibility of the examined rock to environmental
603 weathering, and hence should be planned as first.
- 604 - A three-dimensional elasto-plastic finite element model implementing the current state of
605 the rock mass and the eventual interaction with overlying structures needs to be carried out
606 in order to evaluate the initial safety condition of the considered system.
- 607 - To evaluate how safety conditions change in time due to weathering, the same numerical
608 model should be framed in order to assess future scenarios of the cave stability based on
609 the time evolution of weathering process. To do so, the rock characterization tests previously
610 developed should include some sort of tests replicating possible weathering scenarios at
611 laboratory scale.
- 612 - This methodological approach could be enriched by introducing the effect of rock brittleness
613 in the acceleration of the rock failure process. This requires to improve the numerical code
614 by including time-dependent coupled hydro-chemo-mechanical constitutive models,
615 combined with crack propagation algorithms to describe joint behaviour.

616

617

618 **Acknowledgements**

619 The authors wish to thank Professor Claudio di Prisco and Dr. Geol. Gianmarco Orlandi for many
620 fruitful discussions. In particular, they are grateful to Prof. Roberto Nova for his passion and
621 enthusiasm devoted to scientific investigation. The Municipality of San Lazzaro di Savena (BO)
622 and Mrs. Papagna, owner of the calcarenite mine in Canosa (BT), are also gratefully
623 acknowledged.

624

626

627

References

- 628 - Aliguer, I., Carol, I., Alonso, E.E. (2013). Numerical analysis and safety evaluation of a large arch dam
629 founded on fractured rock, using zero-thickness interface elements and a $c-\phi$ reduction method,
630 COMPLAS XI ,1233-1243.
- 631 - Andriani G.F., Walsh N. (2007). The effects of wetting and drying, and marine salt crystallization on
632 calcarenite rocks used as building material in historic monuments, Geological Society, London, Special
633 Publications, vol. 271, 179-188.
- 634 - Auvray C., Homand F., Sorgi C. (2004). The aging of gypsum in underground mines. Engineering
635 Geology, 74, 183 - 196.
- 636 - Barton, N., Lien, R., Lunde, J. (1974). Engineering classification of rock masses for the design of tunnel
637 support. Rock Mechanics. 6: 4, 189-236.
- 638 - Bekendam R.L. (1998). Pillar stability and large-scale collapse of abandoned room and pillar limestone
639 mines in South-Limburg, the Netherlands. PhD Thesis, Delft University of Technology, the Netherlands.
- 640 - Bètournay M.C. (2009). Abandoned Metal Mine Stability Risk Evaluation. Risk Analysis, Vol. 29, No. 10,
641 1355-1370. DOI: 10.1111/j.1539-6924.2009.01267.x
- 642 - Betti D., Buscarnera G., Castellanza R., Nova R. (2008). Numerical analysis of the life-time of an
643 abandoned gypsum mine, Proc. 12th International Conference IACMAG 2008, Goa (India), Oct. 2008,
644 1210-1218.
- 645 - Betti D., Castellanza R., (2008) La modellazione 3D a elementi finiti di opere in sotterraneo, Strade e
646 Autostrade, 1, 2008, 148-150.
- 647 - Bieniawski, Z.T. (1976). Rock mass classifications in rock engineering. Proc. Symposium on Exploration
648 for Rock Engineering. Balkema, Rotterdam, 97- 106.
- 649 - Brown, E. T., Bray, J. W., Ladanyi, B., and Hoek, E. (1983). "Ground response curves for rock tunnels." J.
650 Geotech. Engrg., ASCE, 109(1), 15-39.
- 651 - Cai M, Kaiser PK, Uno H, Tasaka Y, Minami M (2004). Estimation of rock mass deformation modulus
652 and strength of jointed hard rock masses using the GSI system. Int J Rock Mech Min Sci 41,3-19.
- 653 - Carranza-Torres, C., and Fairhurst, C. (1999). General formulation of the elasto-plastic response of
654 openings in rock using the Hoek-Brown failure criterion. Int. J. Rock Mech. Min. Sci., 36 (6), 777-809.
- 655 - Carter, T.G. (1992). A new approach to Surface Crown Pillar Design. Proc. 16th Can. Rock Mechanics
656 Symposium, Sudbury, 75-83.
- 657 - Castellanza R., Betti, D, Lambrughì (2009). Modellazione 3D dello scavo con TBM di tunnel in area
658 urbana, Gallerie 2•2009, 45-56.
- 659 - Castellanza R., Gerolymatou E., and Nova R. (2008). An Attempt to Predict the Failure Time of
660 Abandoned Mine Pillars, Rock Mechanics & Rock Engineering, 41 (3), 377-401, ISSN 0723-2632.

- 661 - Castellanza R., Nova R. (2004). Oedometric Tests on Artificially Weathered Carbonatic Soft Rocks,
662 Journal of Geotechnical and Geoenvironmental Engineering ASCE, 130, 7, 728-739.
- 663 - Castellanza R., Nova R., Orlandi G. (2010). Flooded gypsum mine remedial by chamber filling, Journal of
664 Geotechnical and Geoenvironmental Engineering ASCE Vol. 136(4), pp. 629-639, DOI: 10.1061• ASCE
665 GT.1943-5606.0000249.
- 666 - Castellanza, R., Orlandi, G. M., Di Prisco, C., Frigerio, G., Flessati, L., Fernandez-Merodo, J. F., Crosta, G.
667 (2015). 3D numerical analyses for the quantitative risk assessment of subsidence and water flood due
668 to the partial collapse of an abandoned gypsum mine. In IOP Conference Series: Earth and
669 Environmental Science (Vol. 26, No. 1, p. 012058). IOP Publishing.
- 670 - Ciantia, M. O., Hueckel, T. (2013). Weathering of submerged stressed calcarenites: chemo-mechanical
671 coupling mechanisms, Géotechnique, 63, No. 9, 768-785.
- 672 - Ciantia, M.O., Castellanza, R., Crosta, G.B. and Hueckel, T., (2015). Effects of mineral suspension and
673 dissolution on strength and compressibility of soft carbonate rocks. Engineering Geology, 184, 1-18.
- 674 - Ciantia, M.O., Castellanza, R. and Di Prisco, C., (2014). Experimental study on the water-induced
675 weakening of calcarenites. Rock Mechanics and Rock Engineering, 48(2), p 441-461.
- 676 - Ciantia, M.O. and Prisco, C., (2016). Extension of plasticity theory to debonding, grain dissolution, and
677 chemical damage of calcarenites. International Journal for Numerical and Analytical Methods in
678 Geomechanics, 40(3), 315-343.
- 679 - Ciantia, M. O., Castellanza, R., di Prisco, C., (2013). Chemo-mechanical weathering of calcarenites:
680 Experiments and theory. In Coupled Phenomena in Environmental Geotechnics (eds Manassero et al),
681 541-548.
- 682 - Ciantia, M. O., Castellanza, R., di Prisco, C., Hueckel, T. (2012). Experimental methodology for chemo-
683 mechanical weathering of calcarenites. In Multiphysical testing of soils and shales (eds L. Laloui and A.
684 Ferrari), 331-336.
- 685 - Ciantia, M. O., Castellanza, R. (2016). Modelling weathering effects on the mechanical behaviour of
686 rocks. European Journal of Environmental and Civil Engineering, 20(9), 1054-1082.
- 687 - Ciantia, M. O., Castellanza, R., Fernandez-Merodo, J. A. (2018). A 3D Numerical Approach to Assess the
688 Temporal Evolution of Settlement Damage to Buildings on Cavities Subject to Weathering. Rock
689 Mechanics and Rock Engineering, 1-24, <https://doi.org/10.1007/s00603-018-1468-3>, ISSN 1434-453X.
- 690 - Deere D. and Miller R.D. (1966). Engineering classification and index properties for intact rock. Univ. of
691 Illinois, Tech. Rept. No. AFWL-TR-65-116.
- 692 - Detournay E., Fairhurst C. (1987). Two-dimensional elastoplastic analysis of a long, cylindrical cavity
693 under non-hydrostatic loading. Int. J. Rock Mechanics Min. Sci., 24(4), 197-211.
- 694 - Diederichs, M.S., (2003). Rock fracture and collapse under low confinement conditions. Rock Mech.
695 Rock Engng., 36 (5), 339-381.

- 696 - Diederichs, MS. and Kaiser, PK. (1999). Tensile strength and abutment relaxation as failure control
697 mechanisms in underground excavations. *Int. Journal of Rock Mechanics and Mining Science*, 36: 1, 69-
698 96.
- 699 - Fazio N.L., Perrotti M., Lollino P., Parise M., Vattano M., Madonia G., Di maggio C. (2017). A three-
700 dimensional back-analysis of the collapse of an underground cavity in soft rocks. *Engineering Geology*,
701 228, 301 – 311.
- 702 - Fenton, G. A., Griffiths, D. V. (2008). *Risk assessment in geotechnical engineering* (Vol. 461). New York:
703 John Wiley & Sons.
- 704 - Fernandez-Merodo J. A., Castellanza R., Mabssout M., Pastor M., Nova R., Parma M. (2007). Coupling
705 transport of chemical species and damage of bonded geomaterials *Computers and Geotechnics*, vol.
706 34, issue 4, 200-215.
- 707 - Ferrero A.M., Segalini A., Giani G.P. (2010). Stability analysis of historic underground quarries.
708 *Computers & Geotechnics*, 37, 476–486. Gerolymatou E., Castellanza R., Nova R. & Vardoulakis I.
709 (2009). The weathering of the foundation of the Tholos of Asklepios at Epidaurus: experiments and
710 modelling. *Proc. of the 1st Int. Symposium on Computational Geomechanics (ComGeo I)*, Juan-les-Pins,
711 Cote d'Azur, France, April 29 – May 1st, 2009.
- 712 - Fiore A., Fazio N.L., Lollino P., Luisi M., Miccoli M.N., Pagliarulo R., Perrotti M., Pisano L., Spalluto L.,
713 Vennari C., Vessia G., Parise M. (2018). Evaluating the susceptibility to anthropogenic sinkholes in
714 Apulian calcarenites, southern Italy. *Advances in karst research: theory, fieldwork and applications*,
715 Geological Society, London, Special Publications, 466, Parise et al. (Eds).
- 716 - Gesualdo A., Minutolo V., Nunziante L. (2001). Local collapse in soft rock bank cavities. *ASCE Journal of*
717 *Geotech. and Geoenviron. Engng.*, 127(12), 1037 – 1041.
- 718 - Ghabezloo S., Pouya A. (2006). Numerical modelling of the effect of weathering on the progressive
719 failure of underground limestone mines. *Eurock 2006, Multiphysics Coupling and Long Term Behaviour*
720 *in Rock Mechanics: Proc. of the Int. Symp. ISRM, Eurock 2006, Liège, Belgium.*
- 721 - Goodings D.J., Abdulla W.A. (2002). Stability charts for predicting sinkholes in weakly cemented sand
722 over karst limestone. *Engineering Geology*, 65, 179 – 184.
- 723 - Gong, W., Juang, C. H., Martin, J. R., Tang, H., Wang, Q., Huang, H., (2018). Probabilistic analysis of
724 tunnel longitudinal performance based upon conditional random field simulation of soil properties.
725 *Tunnelling and Underground Space Technology*, 73, 1-14.
- 726 - Grgic D., Homand F., Giraud A. (2006). Modelling of the drying and flooding of underground iron mines
727 in Lorraine (France). *International Journal of Rock Mechanics & Mining Sciences*, 43 (2006), 388-407.
- 728 - Griffiths, D. V. , Lane, P. A. (1999). Slope stability analysis by finite elements, *Géotechnique*, 49, No. 3,
729 378–403.
- 730 - Griffiths, D. V., Fenton, G. A. (2004). Probabilistic slope stability analysis by finite elements. *Journal of*
731 *Geotechnical and Geoenvironmental Engineering*, 130(5), 507-518.
- 732 - GTS-NX (2010) *Geotechnical and Tunnel Analysis System – User’s Guide* (www.midasuser.com)

- 733 - Hoek, E. (1989). A limit equilibrium analysis of surface crown pillar stability. In Surface crown pillar
734 evaluation for active and abandoned metal mines, (ed. M.C. Betourney), 3-13. Ottawa: Dept. Energy,
735 Mines & Resources Canada.
- 736 - Hoek, E., Brown, E. T. (1997). Practical estimates of rock mass strength. *International Journal of Rock*
737 *Mechanics and Mining Sciences*, 34(8), 1165-1186.
- 738 - Jaeger, J.C., Cook, N.G.W. (1969). *Fundamentals of Rock Mechanics*. London: Chapman and Hall
739 593pp.
- 740 - Jiang Q., Feng X., Fan Y., Fan Q., Liu G., Pei S. (2017). In situ experimental investigation of basalt
741 spalling in a large underground powerhouse cavern. *Tunnelling and underground space technology*,
742 68, 82 – 94.
- 743 - Lagioia R, Nova R (1995). An experimental and theoretical study of the behaviour of a calcarenite in
744 triaxial compression. *Géotechnique*, 45(4): 633-648.
- 745 - Lollino, P., Andriani, G. F. (2017). Role of brittle behaviour of soft calcarenites under low confinement:
746 laboratory observations and numerical investigation. *Rock Mechanics and Rock Engineering*, 50(7),
747 1863-1882.
- 748 - Li L.H., Yang Z.F., Yue Z., Zhang L.Q. (2009). Engineering geological characteristics, failure modes and
749 protective measures of Longyou rock caverns of 2000 years old. *Tunnelling and Underground Space*
750 *Technology* 24 (2009) 190-207.
- 751 - Lippmann H. (1971). Plasticity in rock mechanics. *Int. J. Mech Sci.*, 13, 291 – 297.
- 752 - Mortazavi A., Hassani F.P., Shabani M. (2009). A numerical investigation of rock pillar failure
753 mechanism in underground openings. *Computers and Geotechnics*, 36, 691-697.
- 754 - NAFEMS (1983), International Association for the Engineering Modelling, Analysis and Simulation
755 Community (www.nafems.org)
- 756 - Nickson, S.D. (1992). Cable support guidelines for underground hard rock mine operations. MSc thesis,
757 University of British Columbia, Vancouver.
- 758 - Nova R., Castellanza R., Tamagnini C. (2003). A constitutive model for bonded geomaterials subject to
759 mechanical and/or chemical degradation. *Int. J. Num. Anal. Meth. Geomech.*, 27(9): 705-732.
- 760 - Obert, L., Duvall, W.I. (1967). *Rock Mechanics and the Design of Structures in Rock*. New York: Wiley.
761 65 pages.
- 762 - Panet, M. (1995). *Le calcul des tunnels par la méthode convergence-confinement*. Presses de l'école
763 nationale des Ponts et chaussées, Paris.
- 764 - Parise, M., Lollino, P. (2011). A preliminary analysis of failure mechanisms in karst and man-made
765 underground caves in Southern Italy. *Geomorphology* 134, 132-143.
- 766 - Pelizza S., Oreste P.P., Peila D., Oggeri C. (2000). Stability analysis of a large cavern in Italy for quarrying
767 exploitation of a pink marble. *Tunnelling and underground space technology*, 15 (4), 421 – 435.

- 768 - Polimeno, A. (2007). Il crollo di via Firenze in Gallipoli. l'intervento dei vigili del fuoco, *Geologi e Territorio*, 4-2006/1-2007, 13-19 (in Italian)
- 769
- 770 - Potvin, Y., Milne, D. (1992). Empirical cable bolt support design. *Proc. of Int. Symposium on Rock Mechanics*, Sudbury, ON, Canada.
- 771
- 772 - Ribacchi R., Riccioni R. (1977). Stato di sforzo e di deformazione intorno ad una galleria circolare. *Gallerie*, 4, 7 - 18 (in Italian).
- 773
- 774 - Wang, S.Y., Sloan S.W., Huang M.L., Tang C.A. (2011). Numerical Study of Failure Mechanism of Serial and Parallel Rock Pillars. *Rock Mechanics and Rock Engineering*, 44, 179 - 198.
- 775
- 776 - Weibull W. (1939). The phenomenon of rupture in solids. *IngvetenskAkad. Handl.* No. 153.
- 777 - Yang Z., Yue Z., Li L. (2011). Design, construction and mechanical behavior of relics of complete large Longyou rock caverns carved in argillaceous siltstone ground. *Journal of Rock Mechanics and Geotechnical Engineering*. 2011, 3 (2): 131-152.
- 778
- 779
- 780 - Tamagnini, C., Ciantia, M.O., (2016). Plasticity with generalized hardening: constitutive modeling and computational aspects. *Acta Geotechnica*, pp.1-29.
- 781
- 782 - Trinh N., Jonsson K. (2013). Design considerations for an underground room in a hard rock subjected to a high horizontal stress field at Rana Gruber, Norway. *Tunnelling and underground space technology*, 38, 205 - 212.
- 783
- 784
- 785 - Van Den Eeckhaut, M., Poesen, J., Dugar, M., Martens, V., Duchateau, P. (2007). Sinkhole formation above underground limestone quarries: A case study in South Limburg (Belgium). *Geomorphology*, 91(1), 19-37.
- 786
- 787
- 788 - Vattano M., Di Maggio C., Madonia G., Parise M., Lollino P., Bonamini M. (2013). Examples of anthropogenic sinkholes in Sicily and comparison with similar phenomena in Southern Italy. *Proc. 13th Multidisciplinary Conference on Sinkholes and the Engineering and Environmental Impacts of Karst*, Carlsbad, New Mexico (USA), Land L., Doctor D.H., Stephenson J.B. (Eds.), 263 - 271.
- 789
- 790
- 791
- 792 - Zhang Q.B., He L., Zhu W.S. (2016). Displacement measurement techniques and numerical verification in 3D geomechanical model tests of an underground cavern group. *Tunnelling and underground space technology*, 56, 54 - 64.
- 793
- 794

796 **List of figure caption**

- 797 **Figure 1. Environmental weathering and cave instability**
- 798 **Figure 2. Flow chart of the methodological approach**
- 799 **Figure 3: Evolution of safety factor with time**
- 800 **Figure 4: Step #1 – (a) Picture of the in-situ survey for Cave A and B; (b) Plan of the existing buildings**
801 **superimposed to the planar extension of the caves (red points are the locations of the sampling cores; (c)**
802 **3D laser-scan reconstruction of the caves including some part of the buildings.**
- 803 **Figure 5: Step #3 - in situ drilling (left) and laboratory re-drilling for sample preparation (right)**
- 804 **Figure 6: Step #3 – (a) micromechanical investigations: SEM analyses, thin section, and schematic**
805 **reconstruction; (b) environmental weathering mechanism for calcarenite: short term weathering STD and**
806 **long term weathering (LTD).**
- 807 **Figure 7: Step #3- Experimental results: STD laboratory weathering by uniaxial test (UCS) and indirect**
808 **tensile test (BT): (a) axial stress – strain curves at different saturation degree; (b) UCS ad BT strength vs.**
809 **saturation degree**
- 810 **Figure 8: Step #3- Experimental results: in situ UCS strength and Young modulus vs. distance from cave**
811 **boundary surface**
- 812 **Figure 9: Step #4- (a) Advanced constitutive model: Yield surfaces at different saturation degree process**
813 **(STD) and dissolved mass (LTD) process (Nova et al. 2003); (b) Simplified constitutive model: Failure loci**
814 **for MC and HB model referred to the f_{wet} .**
- 815 **Figure 10: Step #4- Adopted constitutive model simulating the STD weathering process.**
- 816 **Figure 11: Step #5- Geometrical and numerical model : a) Cave A; b) Cave B with an hidden part of the mesh**
- 817 **Figure 12: Step #5-Numerical results (contours) - Cave A: (a) shear stresses; (b) plastic strains; Cave B: (c)**
818 **maximum principal stresses (compression are negative) (d) plastic strains after a total saturation ($f_{wet}: S_r=1$)**
819 **and after a LTD process (f_{LTD}) that correspond to a Strength Reduction Factor of 4,28; e) vertical**
820 **displacement at $S_r = 1$.**
- 821 **Figure 13: Step #1- preliminary survey for San Lazzaro cave.**
- 822 **Figure 14: Step #1- Planar view (a) and section (b) of the abandoned mine system interacting with buildings.**
- 823 **Figure 15: Step #3- Experimental results for fresh gypsum (UR): UC (Uniaxial Compression), BT (Indirect**
824 **Tensile Test) and TX test (multistage triaxial test).**
- 825 **Figure 16: Step #3- Experimental results: in situ existing weathering profile of compression strength,**
826 **stiffness and tensile strength.**
- 827 **Figure 17: Step #3- Experimental results: (a) Decay resistance to uniaxial specimens immersed in situ (in**
828 **the flooded quarry at Level L3); (b) Small-scale simulation of collapse of a pillar in a water flux.**
- 829 **Figure 18: Step #4- Failure envelopes adopted for the gypsum: (a) fitting with HB and MC criterion; (b) Hoek**
830 **and Brown failure loci for the in situ weathered gypsum;**
- 831 **Figure 19: Step #5- Geometrical model and discretization mesh. a) Perspective view and top view of the**
832 **solids; b) perspective view of the finite element mesh and detail of the mesh in the cave system.**
- 833 **Figure 20: Step #5 – Metodology 1 – Elastic analysis : Contour of the in situ vertical stress state of pillars**
834 **evaluated by 3D FEM analyses; in the right bottom corner an example of the vertical stress diagram used**
835 **to evaluate the average value of σ_{situ} is shown.**

836 **Figure 21: Step #5 – Metodology 1 : Pillar safety factor evaluated by combining the in situ stress level and**
837 **rock strength**

838 **Figure 22: Step #5 – methodology 2 -Numerical results: plastic strains at the present conditions**

839 **Figure 23: Step #5: Evaluation of subsidence basin after removing the critical pillar and roof of level L3:**
840 **Contour of plastic strain at section AA (left), contour of superficial subsidence (right)**

841 **Figure 24: Step #5 Forecast of the outgoing volume of water from level 1 in case of quick collapse of the**
842 **entire roof of level L3**

843 **TABLE**

844 **Table 1: Hoek and Brown (1997) failure criteria parameters for in situ condition without joints for the**
845 **gypsum layers: UR_{situ} (Unweathered Rock), HR_{situ} (Humid Rock), FR_{situ} (Flooded Rock)**

846

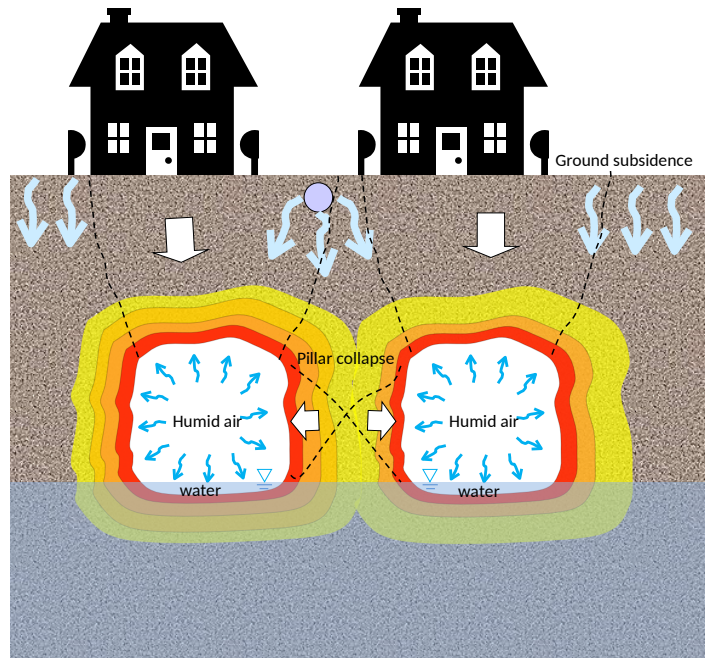
847

848

1 **Figure**

2 (please note that all the picture could be fit in one semicolon ; here the picture are
3 enlarged to facilitate the review process)

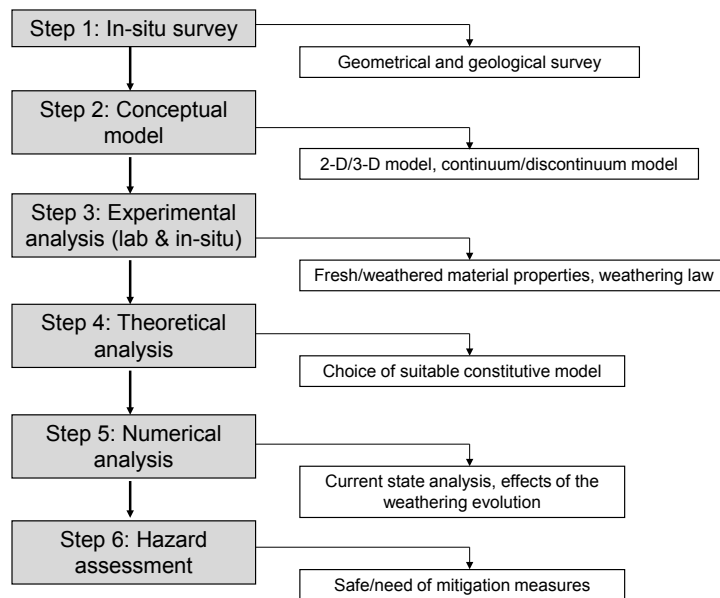
4



5

6

Figure 1. Environmental weathering and cave instability



7

8

Figure 2. Flow chart of the methodological approach

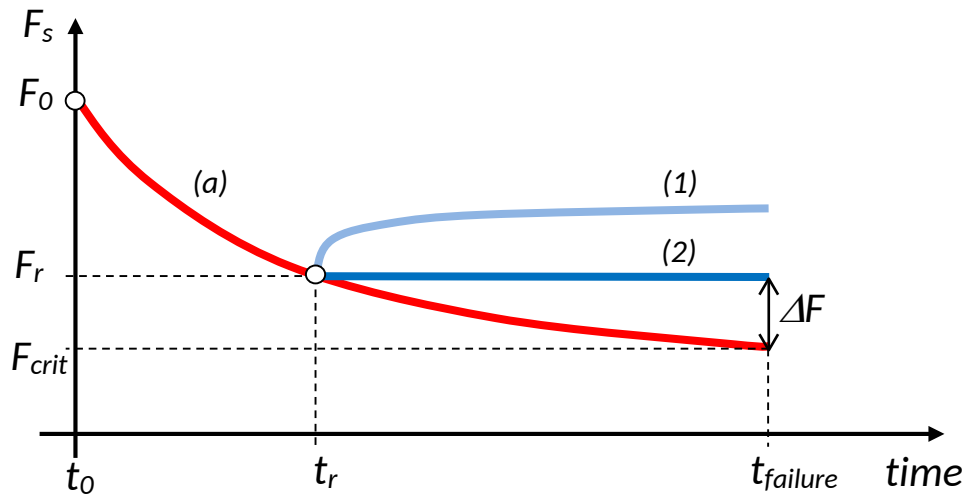
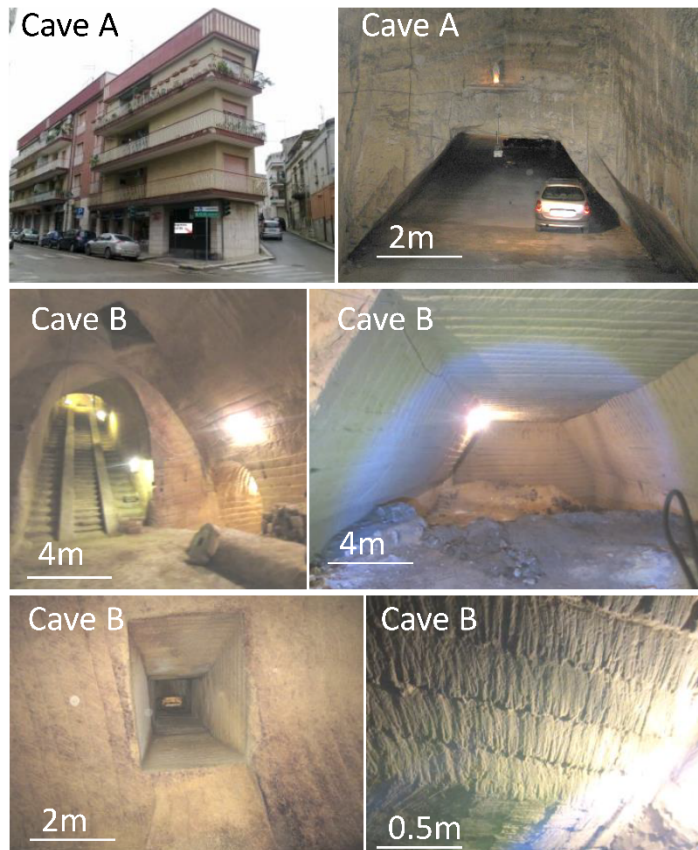
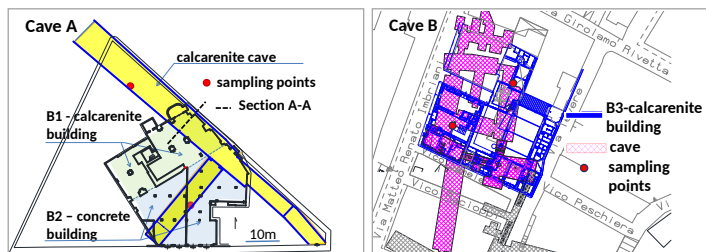


Figure 3: Evolution of safety factor with time

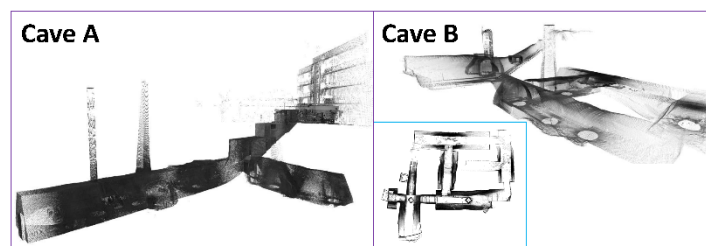
10
11
12



a)

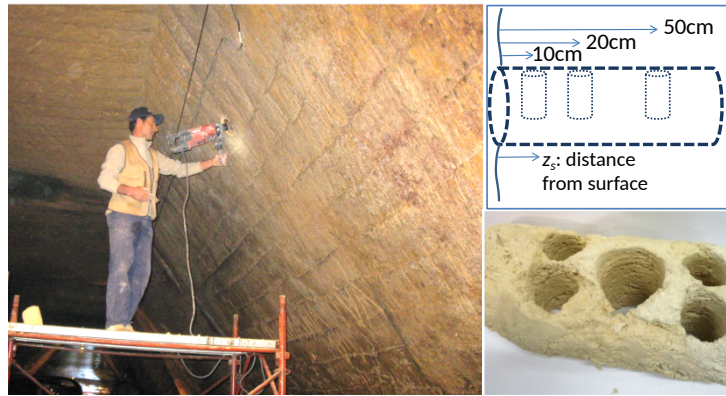


b)



c)

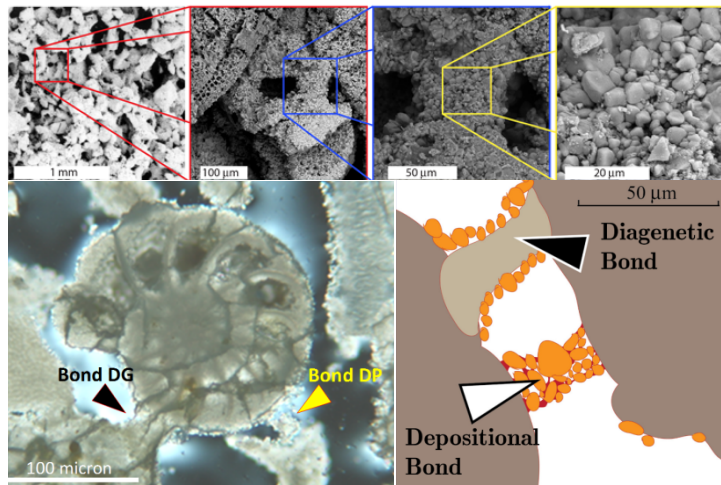
Figure 4: Step #1 - (a) Picture of the in-situ survey for Cave A and B; (b) Plan of the existing buildings superimposed to the planar extension of the caves (red points are the locations of the sampling cores); (c) 3D laser-scan reconstruction of the caves including some part of the buildings.



23

24

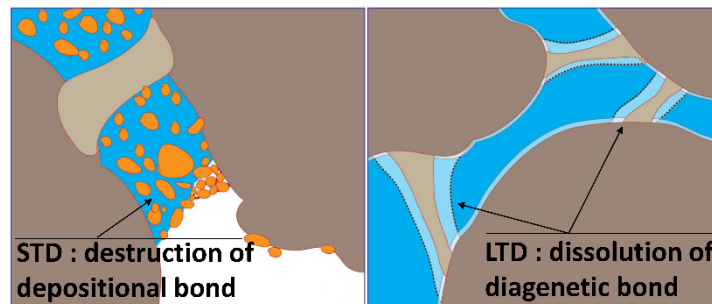
Figure 5: Step #3 - in situ drilling (left) and laboratory re-drilling for sample preparation (right)



25

26

a)



27

28

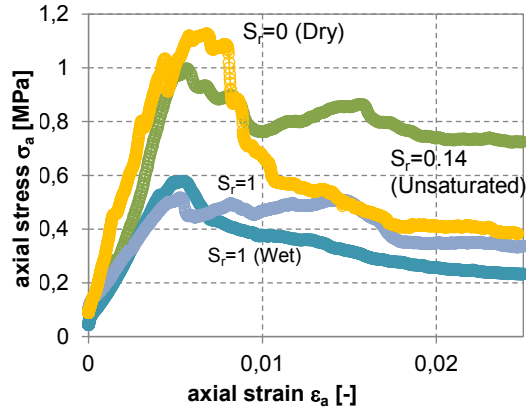
b)

29

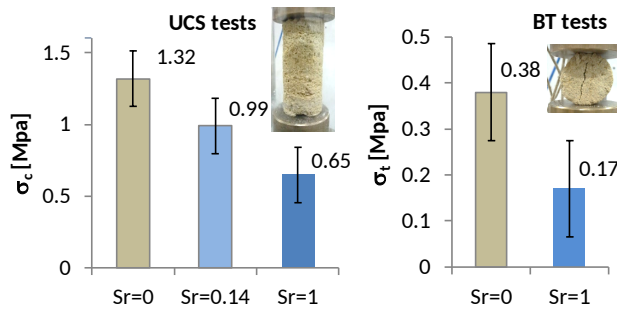
30

31

Figure 6: Step #3 - (a) micromechanical investigations: SEM analyses, thin section, and schematic reconstruction; (b) environmental weathering mechanism for calcarenite: short term weathering STD and long term weathering (LTD).



a)



b)

Figure 7: Step #3- Experimental results: STD laboratory weathering by uniaxial test (UCS) and indirect tensile test (BT): (a) axial stress – strain curves at different saturation degree; (b) UCS ad BT strength vs. saturation degree

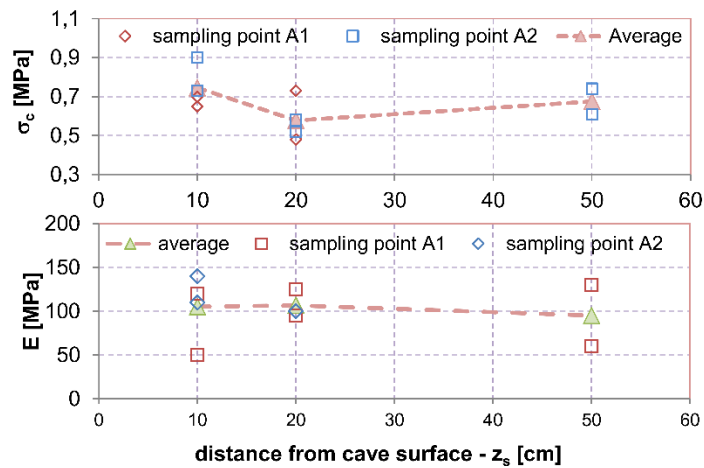
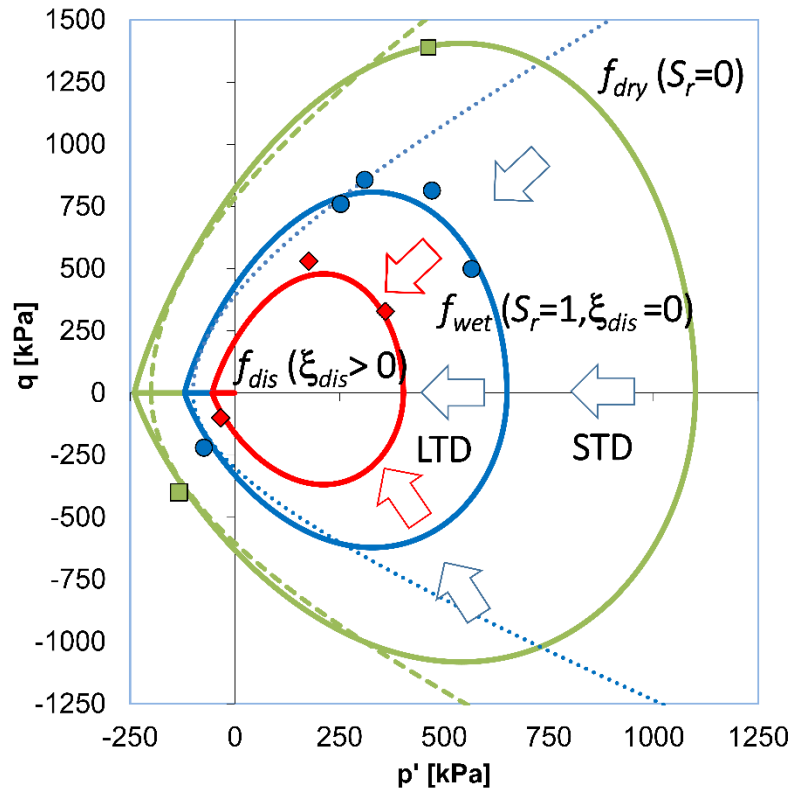
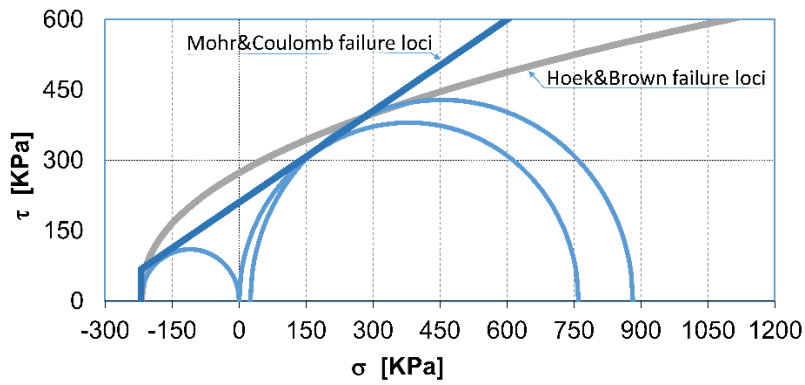


Figure 8: Step #3- Experimental results: in situ UCS strength and Young modulus vs. distance from cave boundary surface



a)



b)

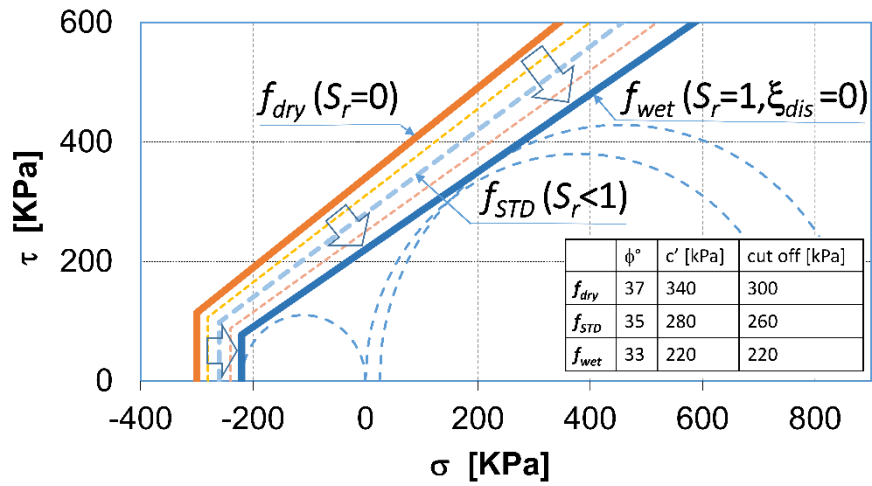
44

45

46

47

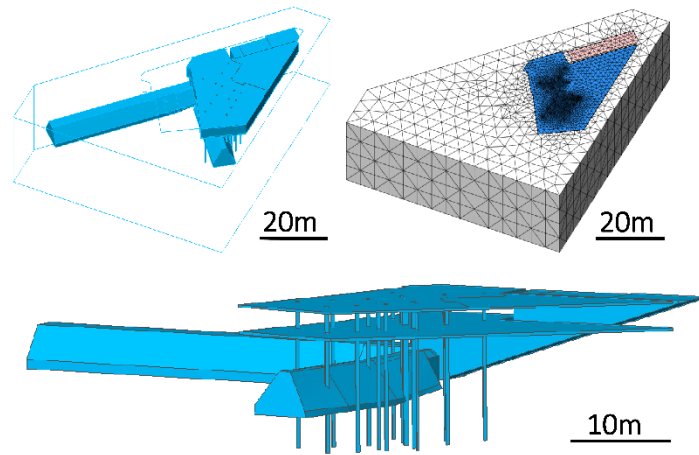
48 **Figure 9: Step #4-** (a) Advanced constitutive model: Yield surfaces at different saturation degree process
 49 (STD) and dissolved mass (LTD) process (Nova et al. 2003); (b) Simplified constitutive model: Failure loci
 50 for MC and HB model referred to the f_{wet} .



51

52

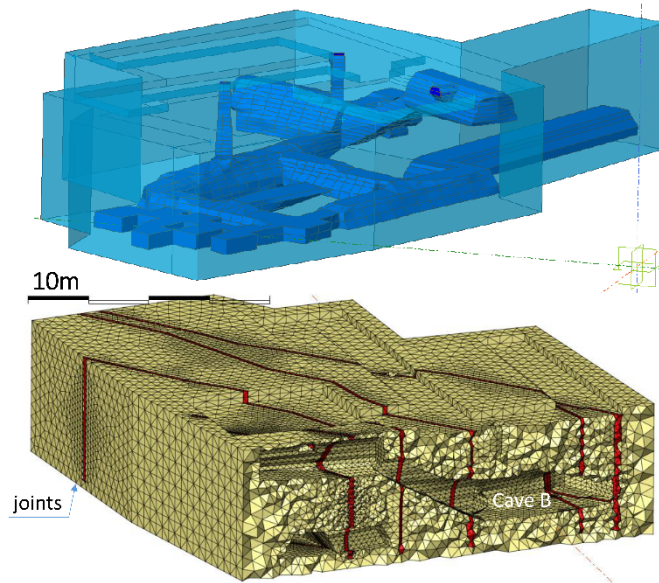
Figure 10: Step #4- Adopted constitutive model simulating the STD weathering process.



53

54

a)



55

56

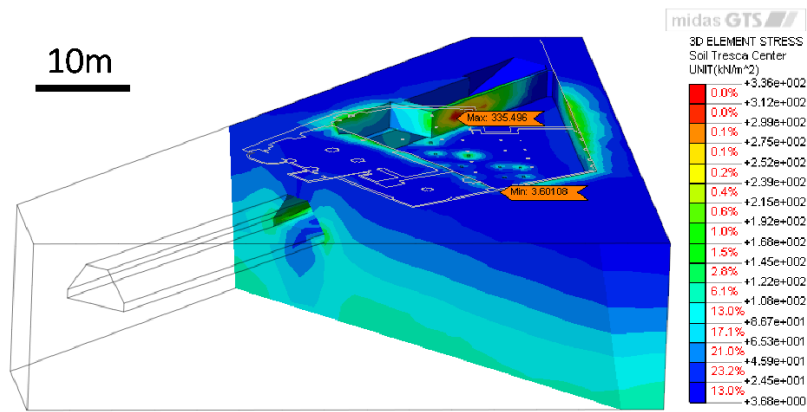
b)

57

58

Figure 11: Step #5- Geometrical and numerical model : a) Cave A; b) Cave B with an hidden part of the mesh

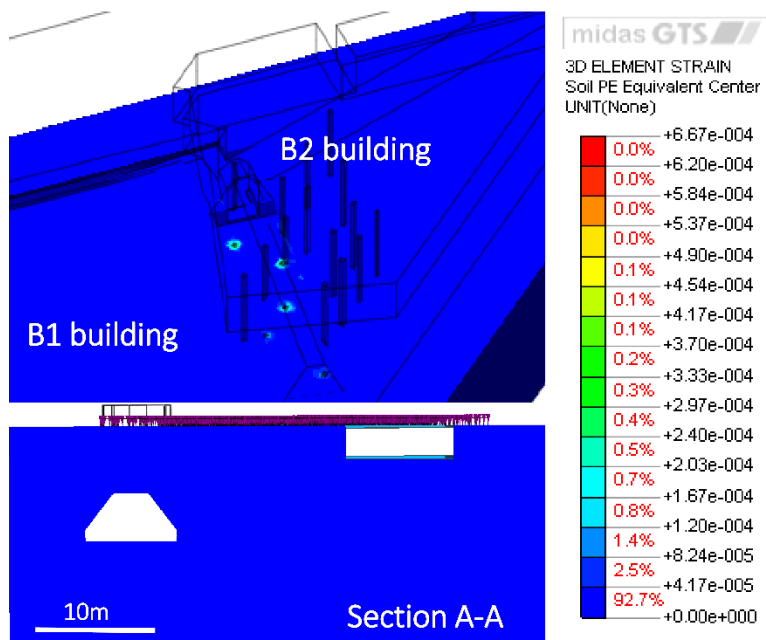
59



60

61

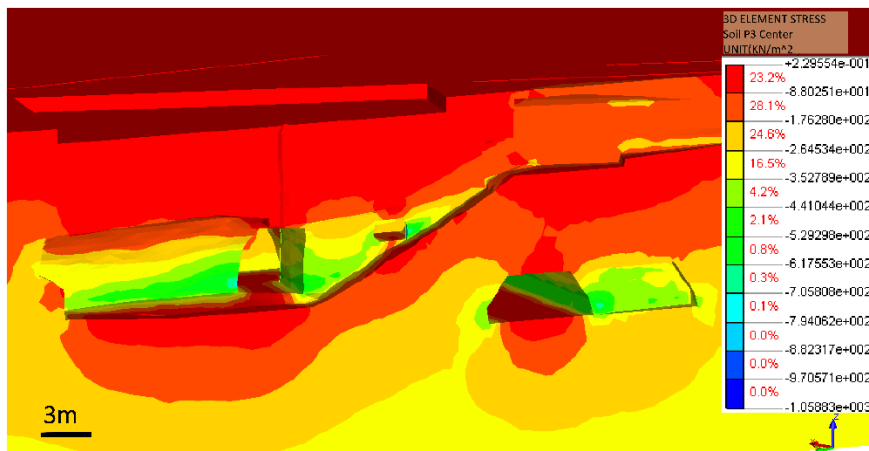
a)



62

63

b)



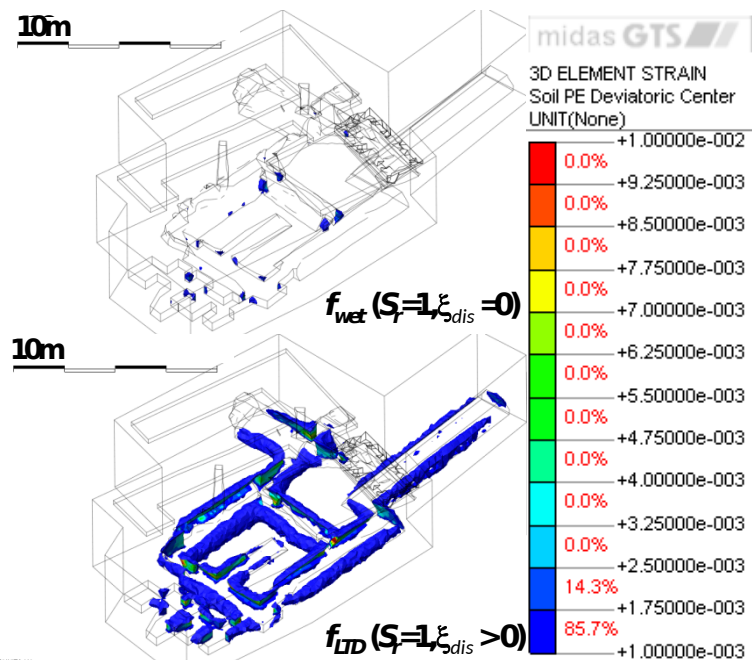
64

65

66

c)

67

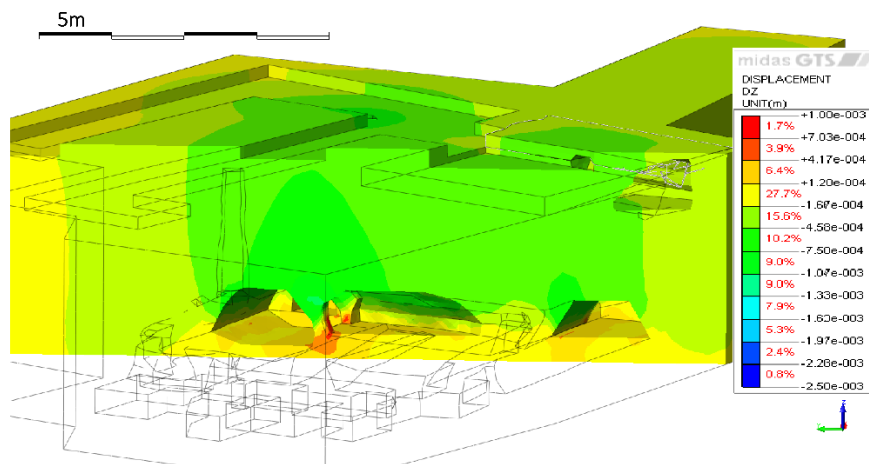


68

69

70

d)

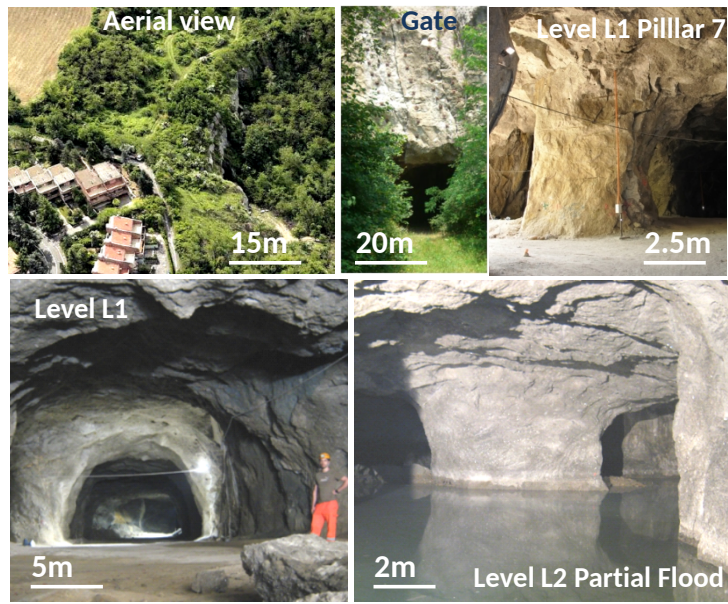


71

72

e)

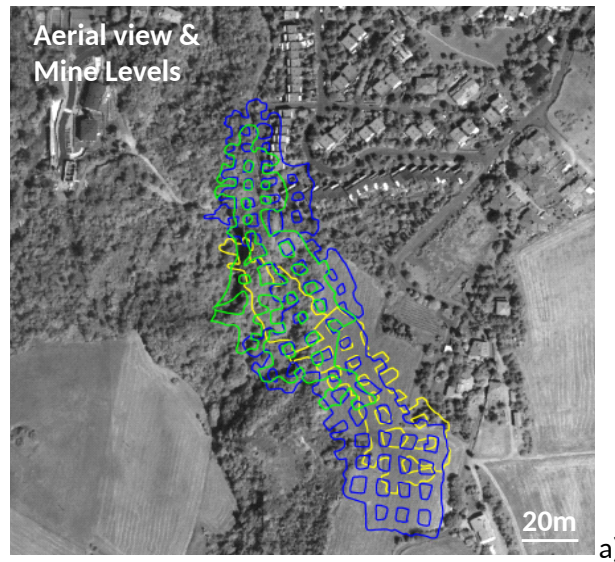
73 **Figure 12: Step #5-Numerical results (contours) - Cave A: (a) shear stresses; (b) plastic strains; Cave B: (c)**
 74 **maximum principal stresses (compression are negative) (d) plastic strains after a total saturation ($f_{wet}: S_r=1$)**
 75 **and after a LTD process (f_{LTD}) that correspond to a Strength Reduction Factor of 4,28; e) vertical**
 76 **displacement at $S_r=1$.**



77

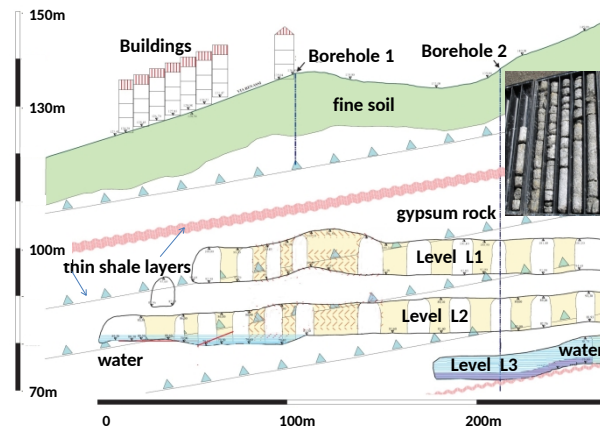
78

Figure 13: Step #1- preliminary survey.



79

80

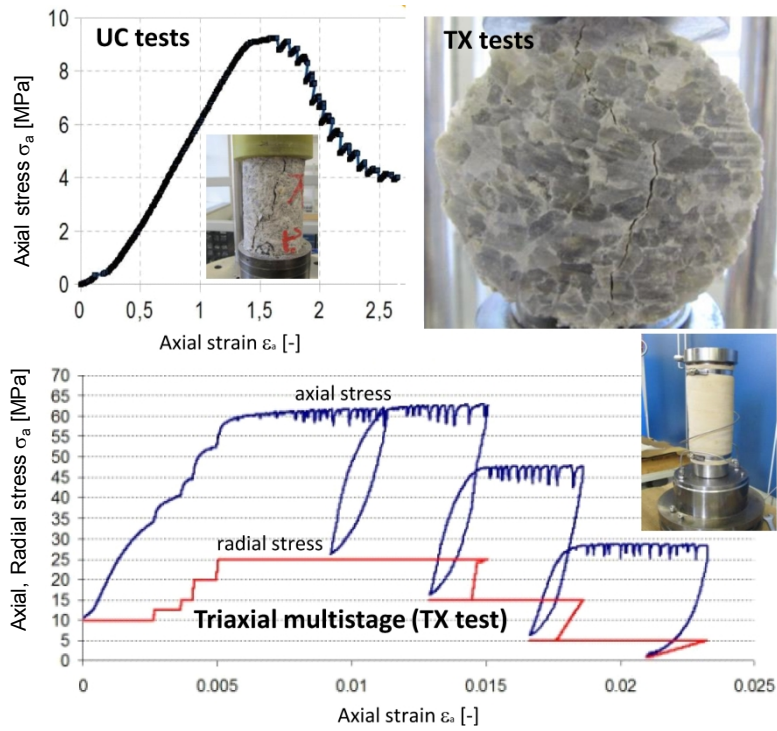


81

82

83

Figure 14: Step #1- Planar view (a) and section (b) of the abandoned mine system interacting with buildings.

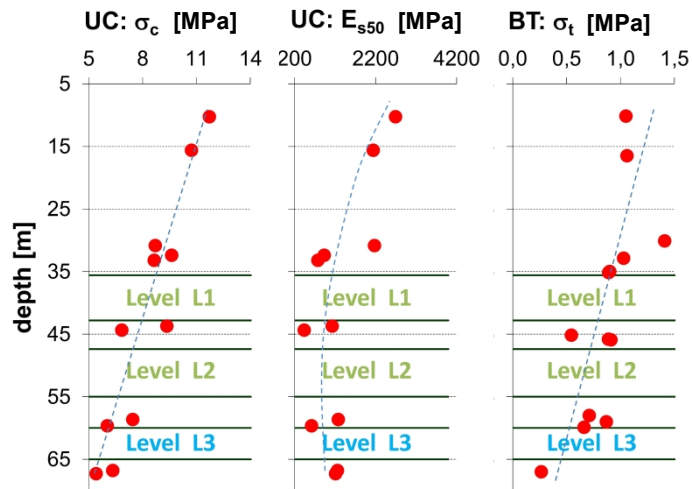


85

86

87

Figure 15: Step #3- Experimental results for fresh gypsum (UR): UC (Uniaxial Compression), BT (Indirect Tensile Test) and TX test (multistage triaxial test).



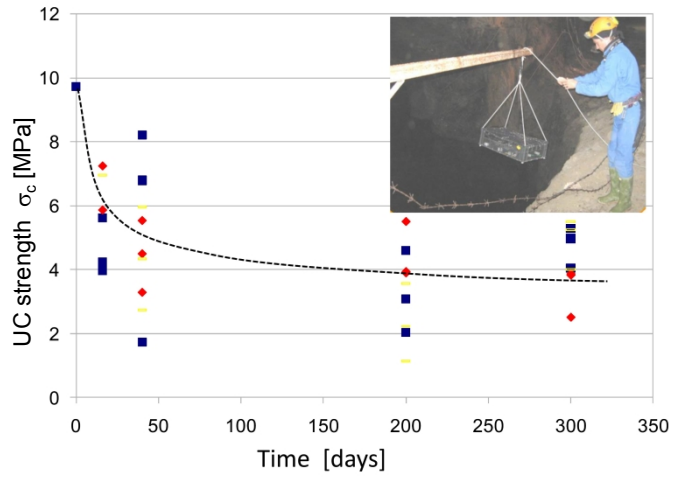
88

89

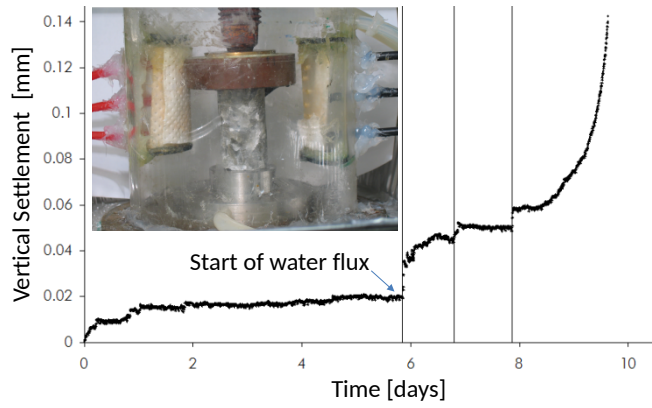
90

91

Figure 16: Step #3- Experimental results: in situ existing weathering profile of compression strength, stiffness and tensile strength.

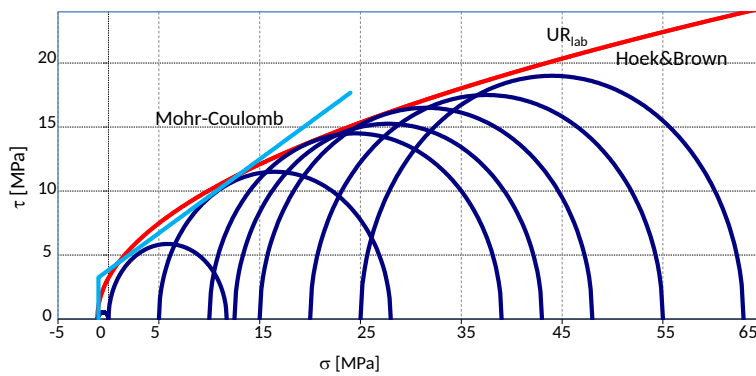


a)

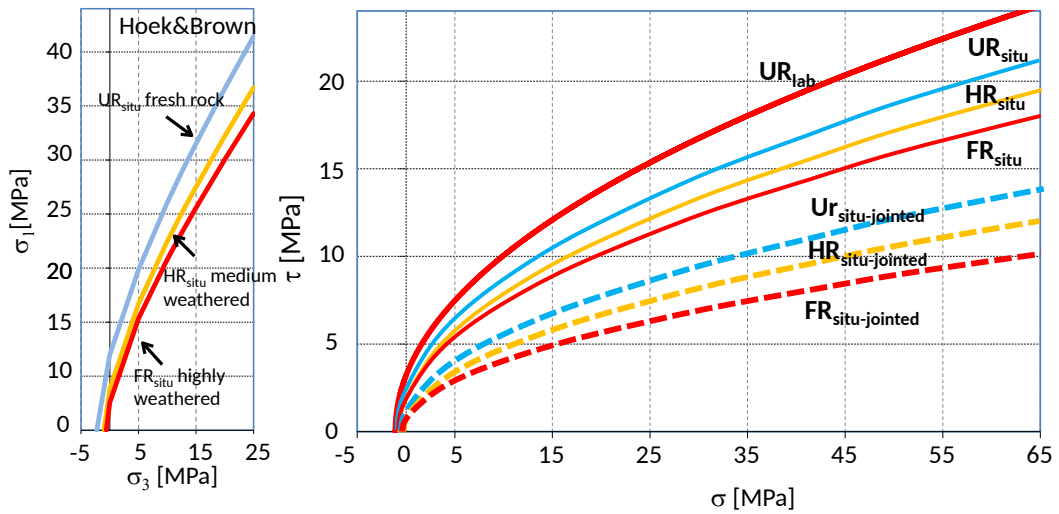


b)

Figure 17: Step #3- Experimental results: (a) Decay resistance to uniaxial specimens immersed in situ (in the flooded quarry at Level L3); (b) Small-scale simulation of collapse of a pillar in a water flux.



a)



100

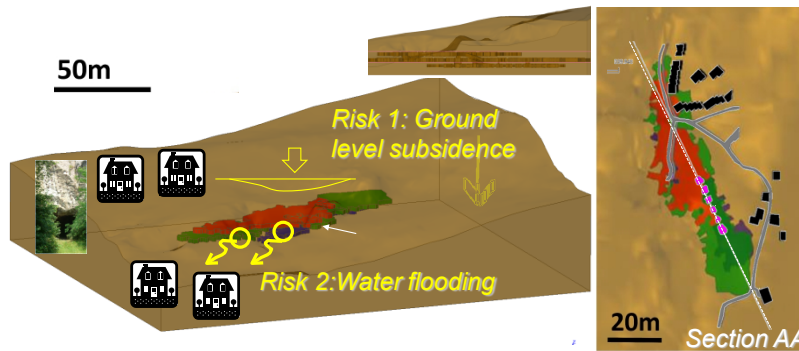
101

102

103

104

Figure 18: Step #4- Failure envelopes adopted for the gypsum: (a) fitting with HB and MC criterion; (b) Hoek and Brown failure loci for the in situ weathered gypsum;



105

106

a)

107

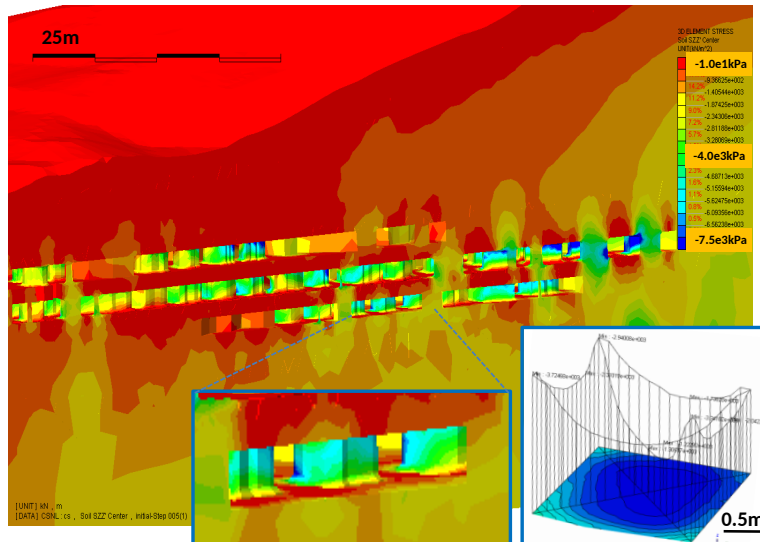
108

b)

109

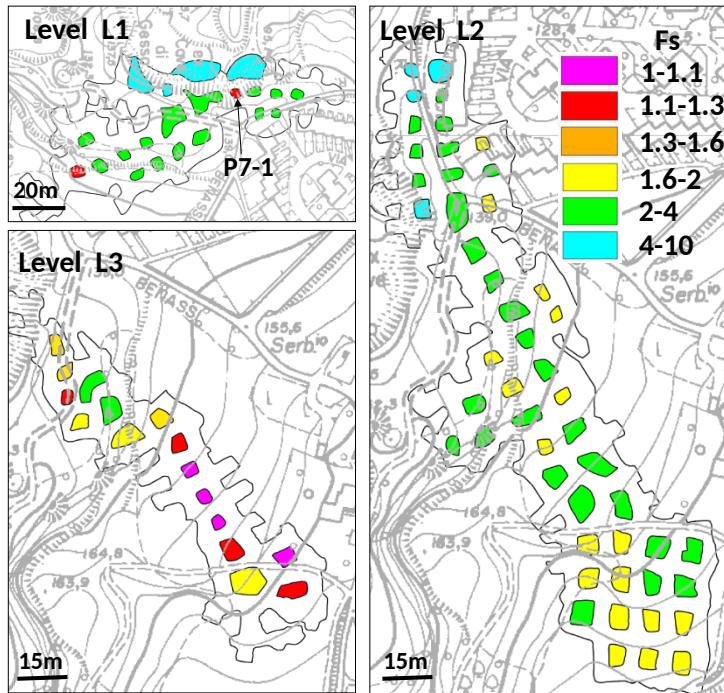
110

Figure 19: Step #5- Geometrical model and discretization mesh. a) Perspective view and top view of the solids; b) perspective view of the finite element mesh and detail of the mesh in the cave system.



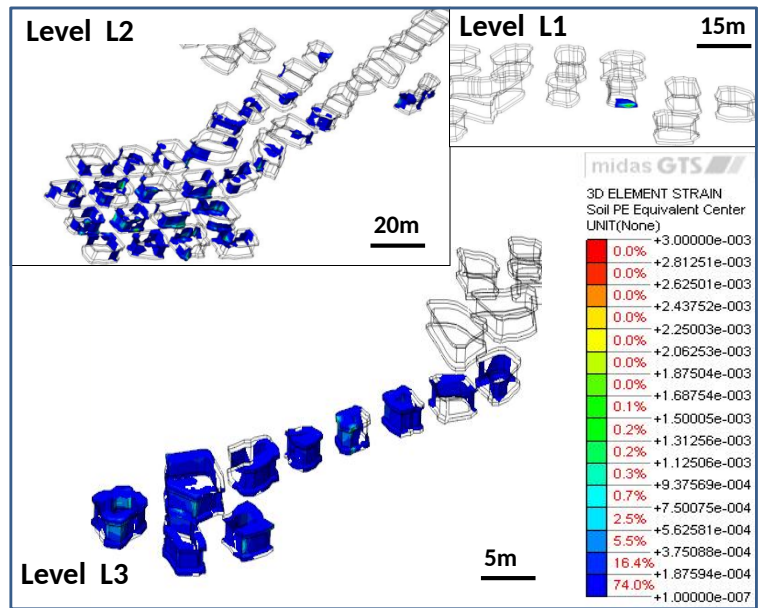
111

112 Figure 20: Step #5 - Metodology 1 - Elastic analysis : Contour of the in situ vertical stress state of pillars
 113 evaluated by 3D FEM analyses; in the right bottom corner an example of the vertical stress diagram used
 114 to evaluate the average value of σ_{situ} is shown.



115

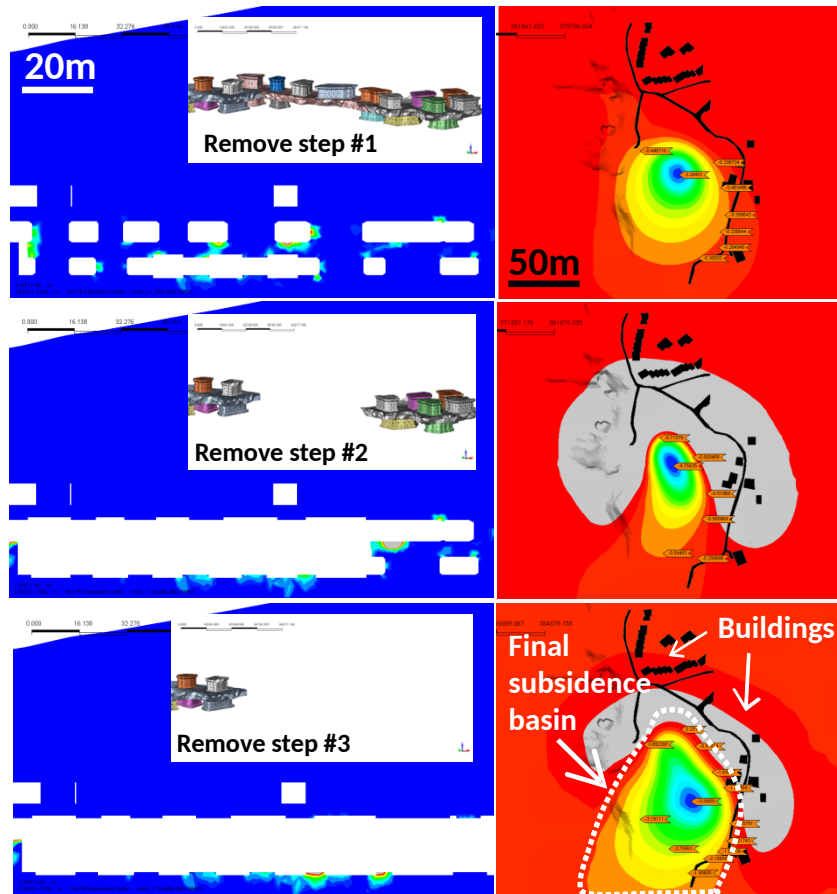
116 Figure 21: Step #5 - Metodology 1 : Pillar safety factor evaluated by combining the in situ stress level and
 117 rock strength



118

119

Figure 22: Step #5 - methodology 2 -Numerical results: plastic strains at the present conditions

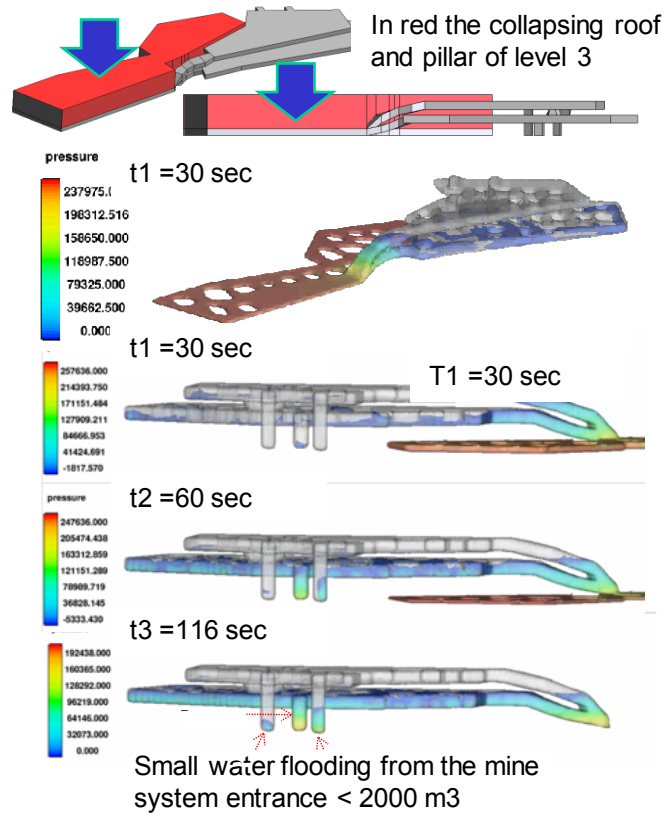


120

121

122

Figure 23: Step #5: Evaluation of subsidence basin after removing the critical pillar and roof of level L3: Contour of plastic strain at section AA (left), contour of superficial subsidence (right)



123

124

125

Figure 24: Step #5 Forecast of the outgoing volume of water from level 1 in case of quick collapse of the entire roof of level L3

Gypsum Rock	UR _{situ}	HR _{situ}	FR _{situ}
σ_{ci} [MPa]	11.72	8.39	6.36
σ_{ti} [MPa]	-1.53	-0.97	-0.66
m_b	7.65	6.17	5.16
s	1.00	0.51	0.29
a	0.50	0.50	0.50
D (Damage)	0.00	0.00	0.00
E_m [GPa]	1.93	1.36	1.02

126

127

128

129

130

Table 1: Hoek and Brown (1997) failure criteria parameters for in situ condition without joints for the gypsum layers: UR_{situ} (Unweathered Rock), HR_{situ} (Humid Rock), FR_{situ} (Flooded Rock)