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A 3D Numerical Approach to Assess the Temporal Evolution of Settlement Damage to Buildings on Cavities Subject to Weathering

Matteo O. Ciantia^{1,2} · Riccardo Castellanza³ · Jose A. Fernandez-Merodo⁴

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Abstract

The goal of this paper is to show how a recently developed advanced chemo-hydro-mechanical (*CHM*)-coupled constitutive and numerical model for soft rocks can be applied to predict the temporal evolution of settlement damage to buildings on cavities subject to weathering. In particular, a Building Damage Index (*BDI*) and its evolution with time is proposed. The definition of the *BDI* is inspired by the work of Boscardin and Cording (J Geotech Eng 115:1–21, 1989) and uses the surface differential settlements obtained by finite element (*FE*) analyses to assess how far a building is from a non-acceptable service condition. By modelling the reactive transport of chemical species in 3D and using a coupled *CHM* constitutive and numerical model, it is possible to simulate weathering scenarios and monitor the temporal evolution of surface settlements making the *BDI* time dependent. This approach is applied to evaluate the damage evolution of two buildings lying on two anthropic caves in a calcarenite deposit belonging to the Calcarenite di Gravina Formation. Standard and advanced experimental tests are performed on the in situ material, and the results are used to calibrate the constitutive model. The soundness of both constitutive relationship and reactive transport solver is subsequently tested by simulating two laboratory-scale boundary value experiments. The first is a model footing test on dry and wet calcarenite, while the second is a small-scale pillar that, after the saturation-induced short-term water weakening, fails due to a long-term dissolution weathering process. Finally, both 2D and 3D coupled *FE* analyses simulating different weathering scenarios and corresponding settlements affecting the buildings above the considered cavities are presented. Particular attention is placed on assessing the *BDI* and its temporal evolution.

Keywords Finite element method · Building damage index *BDI* · Weathering · Hydro-chemo-mechanical coupling · Soft rocks · Sinkholes

Abbreviations

<i>BDI</i>	Building damage index
<i>BT</i>	Brazilian test
<i>BVP</i>	Boundary value problem
<i>CHM</i>	Chemo-Hydro-Mechanical
<i>EDS</i>	Energy-dispersive X-ray spectrometer
<i>FE</i>	Finite element

<i>FEM</i>	Finite element method
<i>GHM</i>	GeHoMadrid <i>FEM</i> code
<i>inSAR</i>	Interferometric synthetic aperture radar
<i>LTD</i>	Long-term debonding
<i>ODE</i>	Ordinary differential equation
<i>PDE</i>	Partial differential equation
<i>SEM</i>	Scanning electron microscope
<i>SLS</i>	Serviceability limit state
<i>STD</i>	Short-term debonding
<i>TXD</i>	Drained triaxial tests
<i>UC</i>	Unconfined compression test

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List of symbols

n	Effective porosity
q_i	Component of the real seepage velocity along the i axis
a_p, m_p, M_{fc}, M_{fe}	Yield surface shape constitutive parameters
a_g, m_g, M_{gc}, M_{ge}	Plastic potential constitutive parameters
D_{ij}	Diffusion tensor

q_s	Volumetric flow rate of sink/source per unit volume	σ_{cw}	Uniaxial compression strength under wet conditions
C_S^k	Concentration associated with the source or sink	$\sigma_{tw,0}$	Initial tensile strength under wet conditions
$\sum_{n=1}^N R_n$	Chemical sink/source term for N chemical reactions	σ_{tw}	Tensile strength under wet conditions
C^k	Concentration of the k th compound	k	Constitutive parameter
[.]	Bulk fluid concentrations	$\rho_s, \zeta_s, \rho_t, \rho_s, \zeta_s, \zeta_t$	Hardening constitutive parameters
K_1, K_2	Reaction rate constants	σ_{ij}	Stress tensor
K_{gr}	Oedometric stiffness granular state	ξ_{sus}	Suspension process progress variable
δ_b	Constitutive parameter related to the extra stiffness caused by the bonds	ξ_{dis}	Dissolution reaction progress variable
$CaCO_{3(s)}$	Calcium carbonate species in the solid phase	$\xi_{dis,cr}$	Corresponds to ξ_{dis} when all diagenetic bonds have been dissolved
$H_3O^+_{(aq)}$	Acid ions		
ΔM	Dissolved mass		
f	Yield function		
p'	Mean effective stress		
p_s	Preconsolidation pressure		
p_t	Intersection of $f=0$ with the negative p' axis		
p_c	Intersection of $f=0$ with the positive p' axis		
p_m	Bonding-induced increase in preconsolidation pressure along p' axis		
p_{s0}, p_{t0}, p_{m0}	Yield surface initial size constitutive parameters		
p_{cell}	Cell pressure in triaxial tests		
q	Deviator stress		
S_r	Degree of saturation		
$S_{r,cr}$	Minimum S_r necessary for all the depositional bonds to suspend		
t	Time		
Y	Weathering function		
Y_E	Stiffness weathering function		
σ_a	Axial stress		
ε_a	Axial strain		
ε_h	Horizontal strain		
β	Angular distortion		
E	Young's modulus		
$E_{d,0}$	Young's modulus for the intact material under dry conditions		
E_w	Young's modulus for the under wet conditions		
$E_{w,0}$	Young's modulus for the intact material under wet conditions		
$\sigma_{cd,0}$	Initial uniaxial compression strength under dry conditions		
σ_c	Uniaxial compression strength		
$\sigma_{cw,0}$	Initial uniaxial compression strength under wet conditions		

1 Introduction

Sinkholes, of both natural and anthropogenic origin, represent an important geological hazard in Europe and, worldwide and every year, cause significant property losses and casualties. Sinkhole formation is often the end result of complex physical hydraulic chemical phenomena (weathering) inducing continuous changes of the soils and rocks forming the earth crust causing a progressive reduction in mechanical properties including strength and deformability and variations of permeability. From an engineering perspective, the weathering-induced degradation of mechanical properties makes such phenomenon quite relevant as it generates deformation in the considered geotechnical systems and can compromise its mechanical stability in the worst case. For instance, leaching chemical-aggressive species can degrade the bond strength of cemented soils, causing settlements of structures founded on these materials (Lollino et al. 2013). In evaporites, the interaction of water with the gypsum pillars of an abandoned mine can transform this rock into a much weaker and compressible material, which can eventually collapse under the weight of the overburden (Castellanza et al. 2010). Also the simple saturation of a dry porous carbonate rock, limestone or other karstic formations leads to considerable changes in strength and stiffness that may cause large surface settlements unacceptable for the service life of existing structures, or even collapse in the form of sinkholes (Parise and Lollino 2011; Parise and Vennari 2017; Sowers 1996).

The substantial increase in sinkhole formation in the Apulian region in the last decades (Parise and Lollino 2011; Parise and Vennari 2017; Sowers 1996) has pushed the regional authorities to introduce new regulations regarding the procedures and requirements needed for risk assessment (L.R. 2002/19). In particular, in the annex introduced in 2006 specifically regarding the risk associated with underground mines (A.d.b. Puglia 2006), it is specified that for all existing structures in high-risk regions (PG3) two options are possible: the first is to fill the cavity with materials with

similar mechanical properties of the host Calcarenite, the second is to perform numerical analyses to assess and predict the mechanical behaviour of the geosystem and propose eventual consolidation measures to fulfil required levels of serviceability and safety. Also a simple planning permission to change the use class of a construction now requires the application of one of these two options. When a building is resting on the top of an abandoned cavity (Fig. 1), the engineering question to be addressed is: how long will the building remain in serviceability conditions?

Despite considerable progress made in recent years in the study of the interactions between the soil (or rock) mass and the environment (including hydraulic, thermal and chemical coupling phenomena) (Alonso et al. 1990; Cekerevac and Laloui 2004; Della Vecchia and Romero 2013; Gajo et al. 2015; Gens 2010; Hueckel and Borsetto 1990; Jommi 2000;

Uchaipichat and Khalili 2009), the application of advanced models to perform 3D numerical simulations to address such question is rare. In particular, chemo-hydro-mechanical (CHM)-coupled advanced numerical simulations are usually performed for 2D idealized problems to show the robustness of integration schemes or to simulate laboratory-scale boundary value problems (Fernandez-Merodo et al. 2007; Tamagnini et al. 2002; Tamagnini and Ciantia 2016).

In engineering practice, according to Eurocode 7 (EC7-BSI 2004), it is necessary to demonstrate that building serviceability requirements can be met at the serviceability limit state (SLS). Typically, building settlements (either gross or distortional) have to be smaller than limiting values which depend on the building type, ground type, and design approach. The choice of the analytical or numerical method used to assess the expected values of settlements is left to

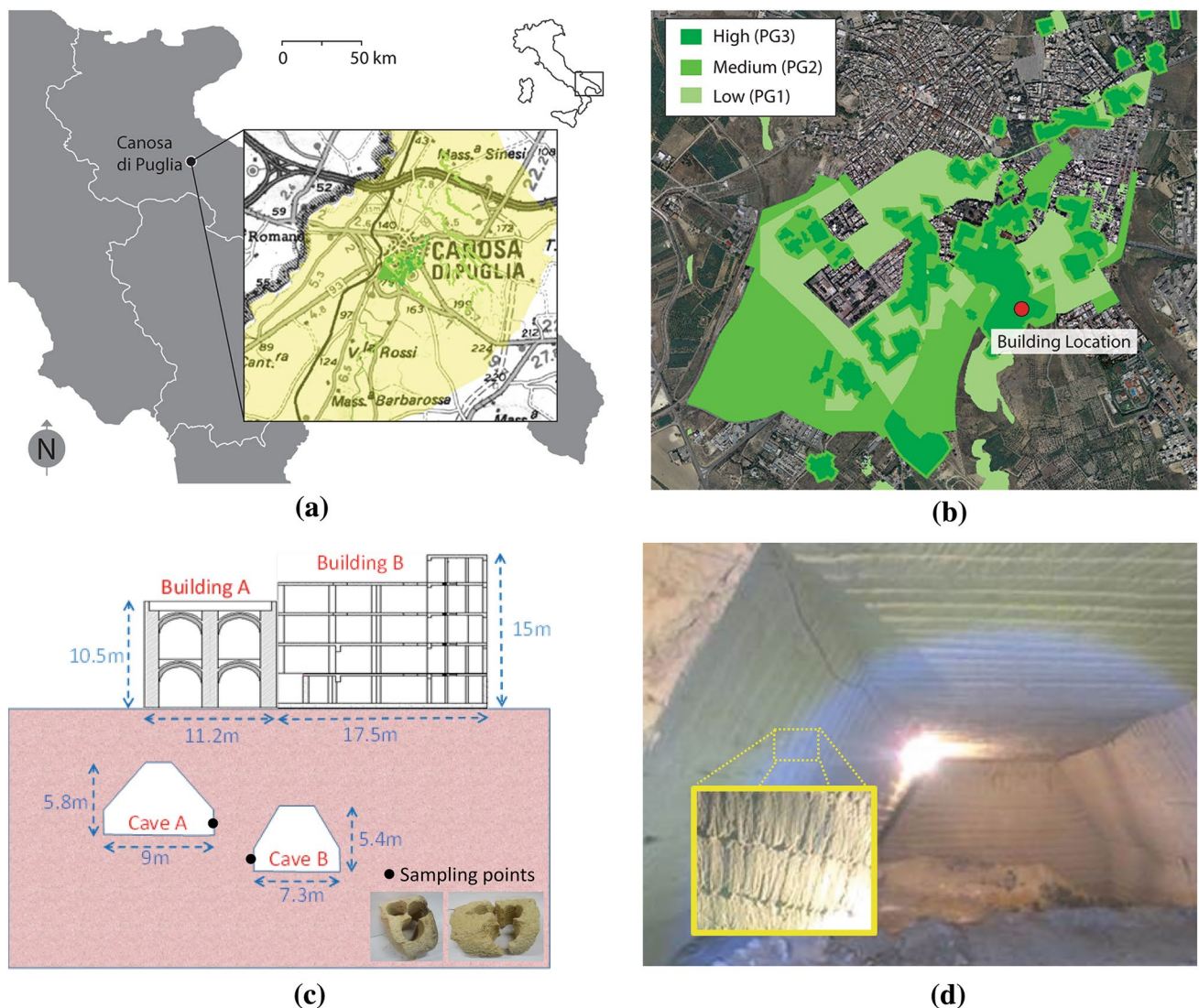


Fig. 1 **a, b** Map of Canosa di Puglia with the highlighted high-, medium- and low-risk zones and case study location (http://93.51.158.165/gis/map_default.phtml), **c** section view of cave interacting with building; **d** picture of Cave A

the engineer, and to this end, elastic methods, Winkler-based analyses and standard finite element (*FE*) analyses may typically be used (Knappett and Craig 2012). However, the effect of weathering on serviceability of buildings is not contemplated by the design code, and in particular, no specific requirements for considering this are given in EC7. As shown by Conte et al. (2010), a simple way to model weathering in *FE* analyses is to assume that a portion of the domain consists of a formation with lower mechanical characteristics. As described therein, the authors show how weathering changes stability of a weathered slope modelled in 2D. However, limit state analyses do not provide reliable deformation results as the deformations associated with c - ϕ analysis are not representative of reality.

This work proposes to exploit a *CHM*-coupled numerical model to study the serviceability conditions of buildings lying on cavities affected by environmental weathering by introducing a practical scalar index: the building damage index (*BDI*). To answer to the question ‘how long will the building remain in safety conditions’, instead of assuming a strength profile and then performing a strength reduction analysis, hydro-chemical weathering scenarios are postulated and, by means of the reactive transport of contaminants, they are simulated. In this way, the spatial-temporal evolution of rock strength and stiffness will develop, and the surface settlements will induce damage to the structure until it is no longer safe. The method hence requires the use of both a coupled *CHM* constitutive model and a *FE* code which solves the hydro-mechanical problem and the transport of chemical species in porous medium. Small-scale coupled weathering experiments (needed to calibrate and validate the model) are then a prerequisite of fundamental importance for the proposed approach. In fact, in order to make reliable future predictions of the *BDI*, the model must first capture the temporal evolution of weathering at the laboratory scale.

In the following, after describing the method used to calculate the temporal evolution of the *BDI*, a brief overview of 3D contaminant transport modelling concepts is presented. Subsequently, the main elements of a recently developed advanced multiscale coupled *CHM* constitutive model (Ciantia and di Prisco 2015) used to describe the

degradation of the soft carbonate rock induced by changes in degree of saturation (short-term debonding) and chemical dissolution (long-term debonding) (Ciantia et al. 2015a, b; Ciantia and Hueckel 2013) are described. Standard mechanical and advanced *CHM* experimental tests on the calcarenite from site are also performed and used to calibrate the model. Experimental results of two boundary value experiments reproducing weathering scenarios at the laboratory scale are also presented and used for validation. Finally, 2D and 3D coupled *FE* analyses simulating long-term effect of the weathering-induced settlements and the temporal evolution of *BDI* of a building in Canosa di Puglia built on top of an abandoned cavity (Fig. 1) are presented. Attention is placed on comparing how the *BDI* evolves with time for the 2 and 3D cases.

2 A Time-Evolving Building Damage Index, *BDI*(*t*)

Despite the fact that final stages of sinkhole formation in soft rocks is usually characterized by a rapid brittle type of global failure (Lollino and Andriani 2017), recent interferometric synthetic aperture radar (*inSAR*) measurements show that ground movements start to accumulate with time several months before the collapse (Chang and Hanssen 2014; Intrieri et al. 2015; Jones and Blom 2014; Nof et al. 2013). In the Marsala Panatletico 2011 sinkhole, signs of instability, such as open fractures and detachment blocks, were observed already 1 year prior to collapse (Fazio et al. 2017). Leucci et al. (2002) show that due to leakage of water into the ground can cause differential surface settlements causing the opening of fractures on the overlying buildings. The formation of cracks on buildings, implying ground level subsidence, months before the Gallipoli sinkhole of 2007 (Fig. 2) were also observed (Delle Rose 2007). These surface settlements, if identified within time, can avoid disasters and allow for actions for risk mitigation (De Giorgi and Leucci 2014).

All these observations lead to the need of introducing an approach able to estimate the level of safety of the buildings lying on rocks susceptible to weathering prior to the brittle

Fig. 2 Air and street views of sinkhole in Gallipoli occurred in 2007 (Polimeno 2007)



collapse of the geosystem, namely the building damage index, BDI . The formulation of the BDI is inspired by the Eurocode 7 serviceability limit states (which are defined as states that correspond to conditions beyond which specified service requirements for a structure or structural member are no longer met) and the work of Boscardin and Cording (1989) that related the level of damage of buildings to surface settlements. Accordingly, the surface differential settlements obtained by FE analyses are here used to assess how far a building is from a non-acceptable service condition. By modelling the reactive transport of chemical species and using a coupled CHM constitutive model where physical time is an intrinsic variable and rock damage is accounted for, it is possible to simulate weathering scenarios and monitor the temporal evolution of surface settlements and hence a BDI function of time. The $BDI(t)$ is clearly strongly dependent on the weathering scenario assumed and on the constitutive model used to reproduce the mechanical behaviour. It gains in reliability as both the weathering mechanism reproduced, and the coupled constitutive models become more realistic. While advanced constitutive relationships for calcarenites are now well established (Ciantia and di Prisco 2015), realistic hydro-chemical weathering scenarios for underground cavities such as the ones reported by Ghabezloo and Pouya (2006) are harder to validate due to complexity of the processes involved. Nevertheless, in the absence of in situ experimental data on the hydro-chemical initial and boundary conditions, one may assume worst-case scenarios, that would in any case result more realistic than a classical stability analysis through simultaneous homogenous strength reduction in all the whole domains (Castellanza et al. 2008). Temporal evolution of surface settlements are then used to determine the corresponding evolution of horizontal strain and angular distortion at the base of the building used to employ the well-known Boscardin and Cording abacus and to calculate $BDI(t)$ that, referring to Fig. 3, is defined as:

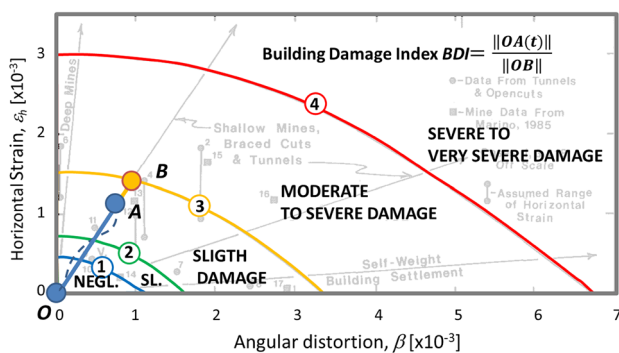


Fig. 3 Definition of the building damage index (BDI) in Boscardin and Cording (1989) plot

$$BDI(t) = \frac{\|OA(t)\|}{\|OB\|} \quad (1)$$

where $\|OA(t)\|$ is the distance of the current state from the origin, while $\|OB\|$ is the distance from level of damage 3 to the origin obtained as an extension of OA . When the $BDI < 1$, the settlement-induced damage on the building is slight or negligible, while if the $BDI > 1$, the damage is moderate or severe.

In order to employ Boscardin and Cording's abacus to define the subsidence induced damage to the building and use Eq. (1), the following assumptions are required:

- (i) the weathering effect causes surface settlements (subsidence) like the ones induced by tunnelling excavation,
- (ii) the building stiffness is not considered as it is assumed not to affect the subsidence profiles, and the building displacement and deformations are assumed to coincide with the ones of the rock and
- (iii) the building is assumed to comply with the Boscardin and Cording (1989) mechanical and geometrical assumptions.

The first assumption is deemed to be reasonable as the bell-shaped subsidence basin that characterizes sinkholes (Gutiérrez et al. 2008) has 2D sections which are very similar to the typical Gaussian-shaped transverse settlement observed in tunnelling excavation (Peck 1969). The latter two also limit the use of this approach to a certain typology of buildings, the one used to construct the abacus.

Despite the fact that this work uses a simplified method to define the level of structural damage, the methodological approach would remain unchanged also when running full soil–structure interaction simulations and can also be applied using other abaci or building damage criteria (e.g. Burland 1995; Burland and Wroth 1974; Franzius et al. 2006; Potts and Addenbrooke 1997; Son and Cording 2005).

The key aspect needed to introduce the $BDI(t)$ is to link the evolution of surface settlements to the hydro-chemical time-dependent weathering processes, and this is only possible if the mechanical behaviour is described by means of advanced coupled CHM constitutive and numerical models.

3 Constitutive and Numerical Modelling of Weathering in Soft Porous Carbonate Rocks

The FEM code used in this work is the GeHoMadrid code (GHM) developed by prof. M. Pastor and co-workers (Fernandez-Merodo et al. 2007). GHM is a non-commercial research code which solves the hydro-mechanical problem, following the $u - p_w$ Biot coupled formulation (Zienkiewicz

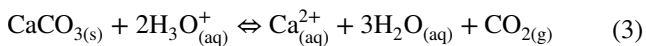
and Shiomi 1984), and hence the hydraulic problem (new seepage velocity, pore-pressure and saturation variations) and the mechanical response are solved simultaneously.

3.1 Modelling the Transport of Chemical Species in Porous Medium

From a mathematical point of view, the transport of a reactive compound is derived by fulfilling a mass balance equation for an elementary volume of the porous medium (see Zheng and Bennett 2002). The effects of chemical reactions on solute transport are generally included in the advection–diffusion equation through a chemical sink/source term, which can be formulated for each chemical compound of interest and added to the general advective–dispersive partial differential equation as follows:

$$\frac{\partial(nC^k)}{\partial t} = \frac{\partial}{\partial x_i} \left(nD_{ij} \frac{\partial C^k}{\partial x_j} \right) - \frac{\partial}{\partial x_i} (nq_i C^k) + q_S C_S^k + \sum_{n=1}^N R_n \quad (2)$$

where C^k is the concentration of the k th compound, n is the effective porosity, q_i is the component of the real seepage velocity along the i axis, D_{ij} is a diffusion tensor, incorporating the effects of dispersion, q_S is the volumetric flow rate of sink/source per unit volume and C_S^k is the concentration associated with the source or sink and $\sum_{n=1}^N R_n$ is the chemical sink/source term representing the rate of change in solute mass of a particular species due to N chemical reactions. In this work, as in Fernandez-Merodo et al. (2007), it is assumed that the chemical reaction governing the dissolution of calcium carbonate forming the porous carbonate rock is given by the global equation:



where the subindexes (g), (aq) and (s) refer to gas, aqueous and solid phases, respectively. The calcium carbonate species in the solid phase ($\text{CaCO}_{3(s)}$) are assumed to be fixed, while the acid ions $\text{H}_3\text{O}^+_{(aq)}$ are mobile. The transport equation for both species can be written as:

$$\begin{aligned} \frac{\partial[\text{H}_3\text{O}^+]}{\partial t} &= \frac{\partial}{\partial x_i} \left(D_{ij} \frac{\partial[\text{H}_3\text{O}^+]}{\partial x_j} \right) - \frac{\partial}{\partial x_i} (q_i[\text{H}_3\text{O}^+]) - K_1[\text{CaCO}_3] \\ \frac{\partial[\text{CaCO}_3]}{\partial t} &= -K_2[\text{H}_3\text{O}^+] \end{aligned} \quad (4)$$

where K_1 and K_2 are two constants characterizing the reaction rate and “[.]” indicates the amount of chemical concentration (i.e. solute mass per unit volume of water). The algorithm concerning the convection–diffusion reactive problem, developed for 2D problems by Fernandez-Merodo et al. (2007), was extended to the 3D case and tested here for the first time. Details of the numerical integration procedure are given in Appendix 1.

3.2 Modelling the Mechanical Behaviour

As shown in Fig. 4a where the first sketches of Prof. Nova are reported (Nova 1992, 1997), rock behaviour can be mathematically described by extending the strain-hardening plasticity framework used to model soils by increasing the size of the yield locus giving the material tensile strength. In particular, the intersections of the yield locus ($f = 0$) with the positive and negative p' axis are called $p_c = p_s + p_m$ and p_t, p_s acts as preconsolidation pressure, as it is for soils, and it is assumed to depend on both plastic volumetric and deviatoric strain rates. In contrast, p_t and p_m account for the effects of interparticle bonding. The existence of bonds therefore implies a nonzero tensile strength ($p_t > 0$) (Di Prisco et al. 1992) and an increase in the yield stress along radial loading paths. p_m

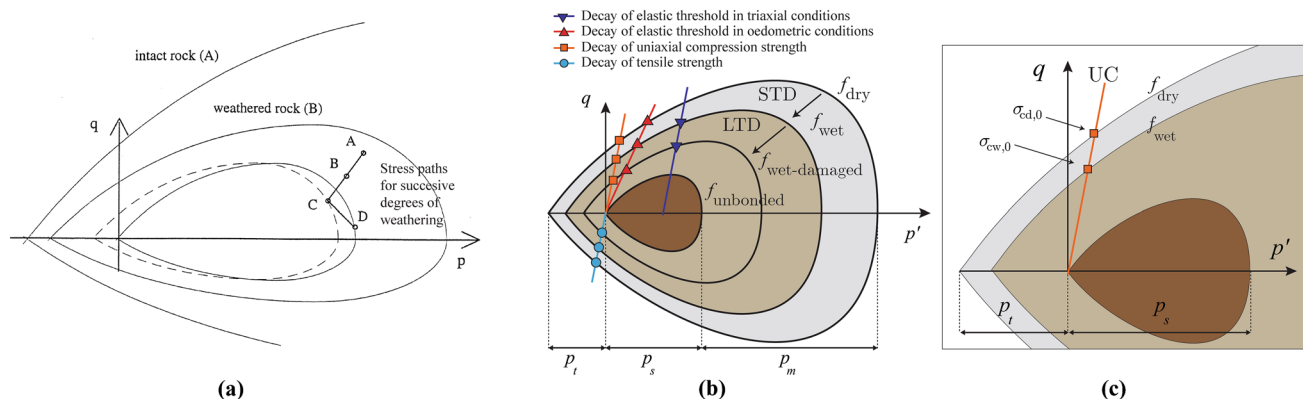


Fig. 4 a Concept of weathering for bonded geomaterials induced by shrinkage of the yield locus proposed by Nova (1992, 1997) and b, c current version of the weathering model driven by the STD and LTD mechanisms (Ciantia and di Prisco 2015)

corresponds to this increase in the case of isotropic compression path. Although p_t and p_m can generally be considered as two independent hardening variables, they are usually assumed to be linearly related, $p_t = kp_m$ (Lagioia and Nova 1995). To incorporate weathering, Nova and co-workers (Nova et al. 2003) introduced a scalar measure (going from 1 to 0) of weathering, namely the weathering function, Y . The latter described the shrinkage of the yield locus induced by non-mechanical processes (Lumb 1962) in a phenomenological way. Recently, micro- and macro-experimental evidence has shown the existence of two types of bonding, depositional and diagenetic, Ciantia et al. (2015a, b) and Ciantia and di Prisco (2015) redefined the weathering function by means of a multiscale approach (Fig. 4b, c). This allowed the weathering to be described using physical quantities namely the degree of saturation (S_r) and the normalized dissolved mass (ξ_{dis}) of calcium carbonate (Fig. 5). A detailed description of the Nova model is given in Ciantia and di Prisco (2015), and hereafter the hardening laws:

$$\dot{p}_s = \rho_s p_s (\dot{\epsilon}_v^p + \zeta_s \dot{\epsilon}_s^p) \quad (5)$$

$$\dot{p}_t = -\rho_t p_t (\dot{\epsilon}_v^p + \zeta_t \dot{\epsilon}_s^p) + \frac{p_t}{Y} \dot{Y} \quad (6)$$

$$\dot{Y} = \Xi \dot{\xi}_{\text{dis}} + \Sigma \dot{S}_r \quad (7)$$

$$\dot{Y}_E = \Xi_E \dot{\xi}_{\text{dis}} + \Sigma_E \dot{S}_r \quad (8)$$

and the constitutive relationship:

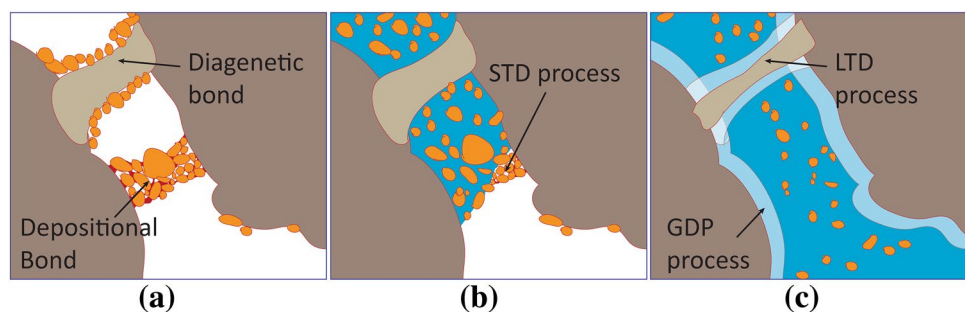
$$\begin{aligned} \dot{\sigma}_{ij} = & D_{ijkl}^{ep} \dot{\epsilon}_{hk} + \left(D(\Xi)_{ij}^{\text{LTD}} + D(\Xi_E)_{ij}^{\text{DAMAGE-dia}} \right) \dot{\xi}_{\text{dis}} \\ & + \left(D(\Sigma)_{ij}^{\text{STD}} + D(\Sigma_E)_{ij}^{\text{DAMAGE-dep}} \right) \dot{S}_r \end{aligned} \quad (9)$$

are reported to ease the discussion on the numerical results. Y and Y_E represent the strength and stiffness weathering functions, which are the key functions that link the strength and stiffness evolution to the weathering driving variables, S_r and ξ_{dis} . In Appendix 2 the full expression of the weathering functions is reported.

3.3 Chemo-Hydro-Mechanical FEM Coupling

Despite that the mechanical part uses a Lagrangian approximation and the transport part an Eulerian one, the key point of the coupling is that both solvers use the same finite element mesh. Coupled formulation in GeHoMadrid uses for instance elements of kind T6P3 (triangle), Q8P4 (quadrilateral) in two dimensions or H8P4 (hexahedra), B20P4 (bricks) in three dimensions. The unknowns of the ‘‘transport solver’’ are the concentrations of CaCO_3 and H_3O^+ , Eq. (4). The coupling uses a ‘‘staggered’’ algorithm which works as follows: knowing the seepage velocity and the concentration value of CaCO_3 and H_3O^+ for each node at time t , the transport solver computes the new values at time $t + dt$. The normalized dissolved mass, ξ_{dis} , is calculated using Eq. (26) in Appendix 2, and it is used as an input in the hydro-mechanical solver affecting the mechanical response (see Eq. 9). For a partially saturated sample, a water retention curve needs to be defined, which, knowing the pore pressure, allows the saturation degree S_r , that governs the *STD* to be determined. As described in Fernandez-Merodo et al. (2007), since the two phenomena analysed have different time steps, the computations are arranged in such a way that there is an inner loop with small time steps for transport within the hydro-mechanical main loop, and several time steps are computed with the transport solver for each hydro-mechanical step. Another simplifying assumption can be made by not considering changes in seepage velocity; if the seepage velocity is constant, there is no change in pore pressure. The mechanical behaviour can be computed with a simple displacement formulation. For sake of simplicity, in this work the weathering path considered is as follows: during saturation, because the inundation phase is assumed to be rapid enough to prevent any dissolution, only the *STD* process is assumed to take place; consequently, ξ_{dis} is constant, while S_r evolves from 0 to 1. As detailed in Ciantia et al. (2015b), *STD* evolves for a limited range of degree of saturation. Once $S_r > S_{r,\text{cr}}$ dissolution is assumed to start, and hence *LTD* starts evolving with ξ_{dis} . Although features such as pressure solution (Rutter and Elliott 1976), opening of cracks and discontinuities (Lollino and Andriani 2017),

Fig. 5 Microscopic weakening processes: **a** saturation-induced short-term debonding of depositional bonds; **b, c** dissolution-driven long-term debonding and grain dissolution process (Ciantia et al. 2015a)



chemical enhanced crack propagation (Hueckel et al. 2017) and strain localization cannot be captured by GHM and the adopted constitutive model, the definition and use of the $BDI(t)$ would remain unchanged even if more advanced numerical methods such as $FDEM$ (Geomechanica Inc 2016) or $P-FEM$ (Rodriguez et al. 2016) were to be used. Note that in the latter case a coupled constitutive relationship would still be required.

4 Experimental Results and Model Calibration

The material tested in the laboratory was retrieved from the man-made cave of the selected case study (represented in Fig. 1) that was excavated in a calcarenite deposit in the urban area of Canosa di Puglia. The calcarenite is characterized by a porosity of 59% and a unit weight in a dry condition of 11.1 kN/m^3 . The experimental tests performed to adequately characterize the soft rock and calibrate the constitutive model are:

- (i) Thin sections, scanning electron microscope (SEM) imaging with punctual energy-dispersive X-ray spectrometer (EDS) measurements to identify the chemi-

cal composition and the presence of depositional and diagenetic bonds (Fig. 6).

- (ii) Uniaxial (UC), Brazilian (BT) and drained triaxial tests (TXD), on saturated samples to define the shape of the yield locus (Fig. 7).
- (iii) UC and BT tests on dry ($S_r = 0$), partially saturated ($0 < S_r < 1$) and saturated ($S_r \sim 1$) samples to calibrate the strength (Y) and stiffness (Y_E) weathering functions for the STD mechanism (Fig. 8).
- (iv) The post-peak responses of the UC and TXD tests are used to calibrate the mechanical hardening parameters, ρ_s , ρ_f and ζ_f .
- (v) UC and BT tests on saturated intact and artificially (with acid) pre-weathered samples to calibrate the strength and stiffness weathering function for the LTD mechanism, are performed (Fig. 9).

Following Ciantia et al. (2015a), by analysing the thin sections with both a polarized light microscope and SEM , it was possible to identify the presence of both depositional and diagenetic bonds (Fig. 6). Punctual EDS analyses (Fig. 6) performed during SEM imaging of the thin sections confirm that both type of bonds are formed by CaCO_3 microcrystals. While UC and BT tests are very useful to identify the yield locus at low confinement pressures, the TXD test

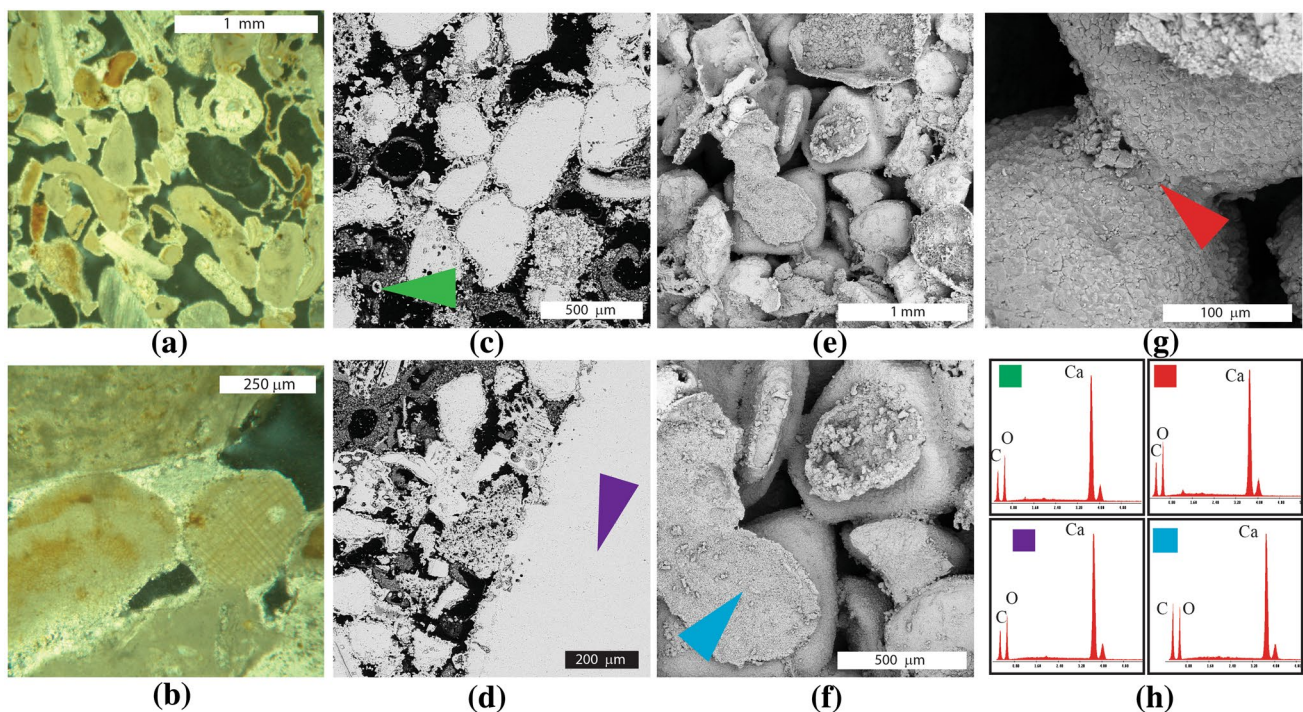


Fig. 6 Optical microscope (a, b) and SEM (c, d) images of thin sections of the in situ calcarenite. (e, f, g) SEM images of 3D microstructure with different magnifications, and h corresponding punctual chemical analyses of the same calcarenite sample

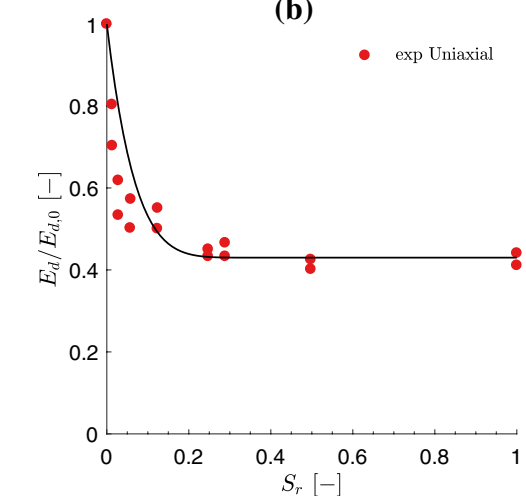
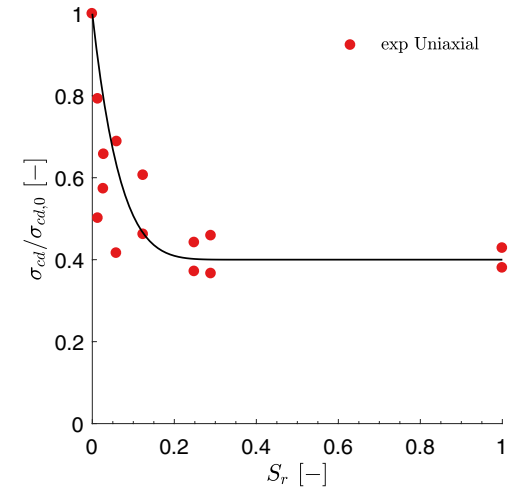
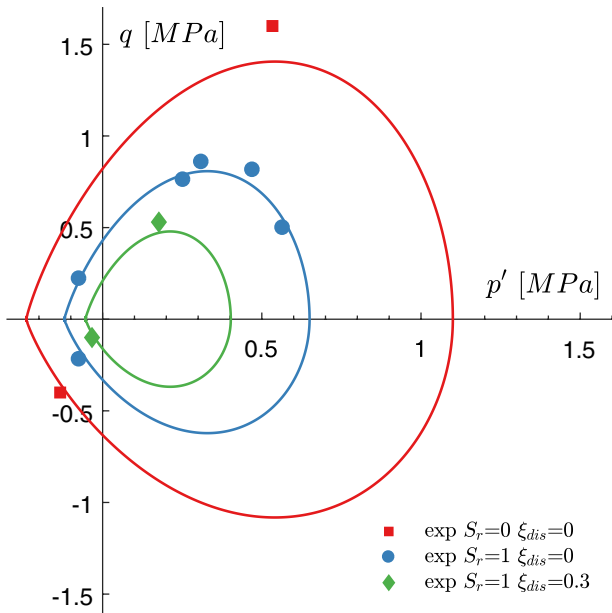
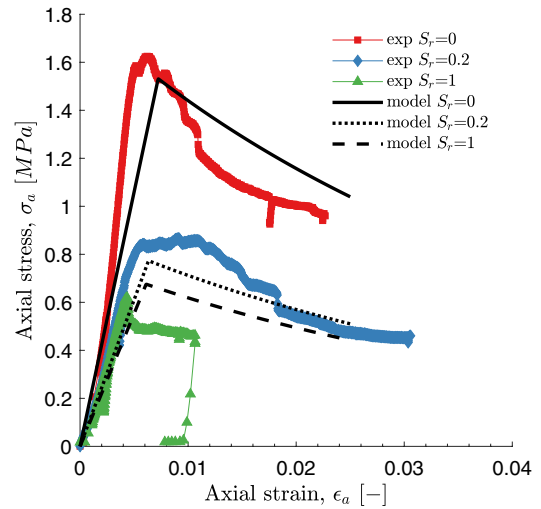
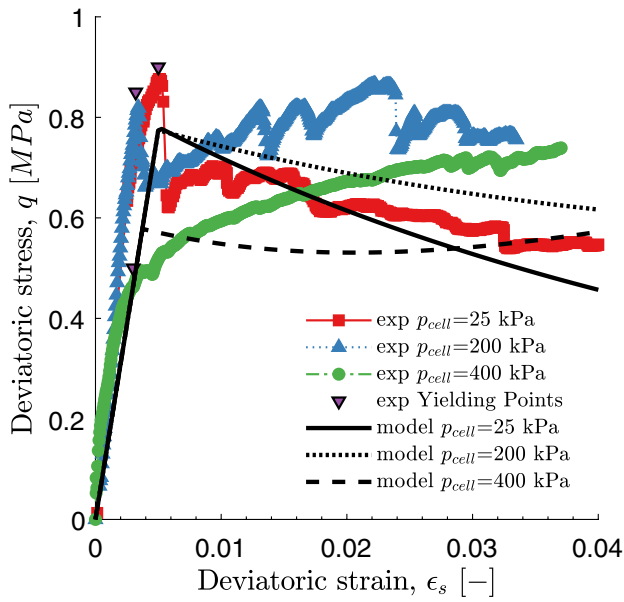


Fig. 7 **a** Results of the drained triaxial compression tests on saturated calcarenite at three different confining pressures and, **b** calibrated yield locus of dry ($S_r=0$), saturated ($S_r=1$) and Saturated weathered ($\xi_{dis}=0.3$) calcarenite

are needed to identify the yield locus shape at high pressures (Fig. 7). In Fig. 8a typical axial stress–strain curves at different degrees of saturation are shown; the strength and stiffness reduction associated with higher saturation degrees are clearly visible. Figure 8b, c shows the normalized trend of σ_c and E versus S_r . These results have been obtained by performing more than 40 UC tests on specimen with 38 mm

Fig. 8 **STD**—**a** results of the axial stress–strain curves of the uniaxial compression (UC) tests on the in situ calcarenite sample at different degree of water saturation, S_r ; **b** and **c** normalized reduction in UCS and Young modulus with S_r

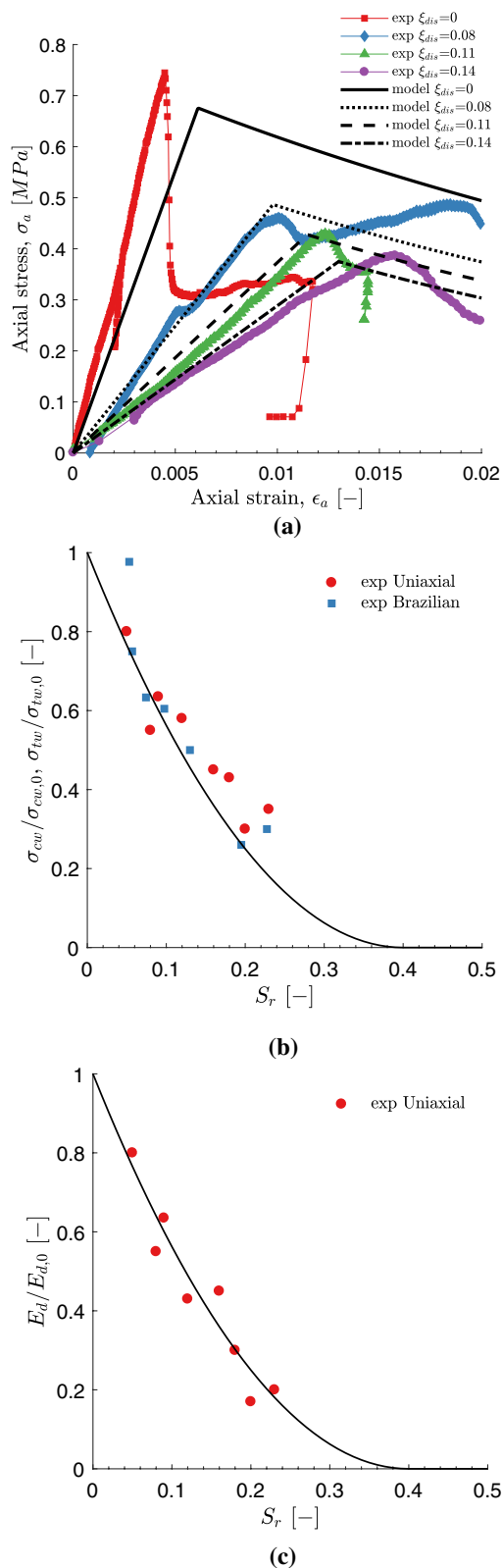


Fig. 9 LTD—**a** results of the axial stress–strain curves of UC tests on the in situ calcarenite sample at different levels of accumulated dissolved mass index, ξ_{dis} ; **b** and **c** normalized reduction in UCS and Young modulus with ξ_{dis}

diameter using a displacement-controlled loading frame at 0.05 mm/min. The LTD process has been analysed by means of a two-step experimental test: following the same procedure of Castellanza and Nova (2004), the samples were first weathered by means of an acid solution (pH = 2.8) in order to accelerate the weathering process. In this initial phase, the dissolved mass ΔM is the measured variable and ξ_{dis} is evaluated by means of Eq. (26). Subsequently, the samples are tested, and in Fig. 9b, c, the dependence of both strength and stiffness on ξ_{dis} is illustrated, while in Fig. 9a, a selection of axial stress and strain curves at different values of ξ_{dis} is shown. With the experimental tests presented, the constitutive model is calibrated, and the corresponding parameters and model fitting curves are reported in Tables 1, 2, 3, 4 and Figs. 7a, 8a, 9a.

5 Model Validation at the Laboratory Scale

As it was already mentioned, the reliability of the approach is strongly affected by various aspects, but the most critical is the correct numerical reproduction of weathering mechanism taking place. The capability of the model to capture rock weathering from a quantitative point of view at the laboratory scale is then a prerequisite. As the CHM initial and boundary conditions in the laboratory can be controlled with reasonable accuracy, before using the approach as a predicting tool, the calibrated model should first capture the laboratory-scale response. For this reason, two BVP laboratory tests were performed and simulated with the already calibrated model. The first (BVP #1) is a model footing test on dry and wet calcarenite, while the second (BVP #2) is a loaded small-scale pillar subject to both the STD and LTD weathering mechanisms. For this latter the experimental results are taken from Ciantia et al. (2015b). The calcarenite samples of the two BVP's were prepared from a Calcarenite di Gravina Formation block extracted few miles from the analysed cavity, hence have different initial strength conditions (p_{m0}), but the rest of the model parameters are the same.

5.1 BVP#1 Model Footing Tests on Dry and Wet Calcarenite

BVP#1 is aimed to prove the capability of both the constitutive model and numerical code to properly simulate the short-term water-weakening effects (STD) on the bearing capacity of a small-scale footing. Two experimental tests were run, and the results are shown Figs. 10 and 11a, while the FE simulation results are reported in Fig. 11b. Both experiment and numerical simulation are performed controlling the vertical displacement of the rigid footing. It is worth noting the formation of a

Table 1 Yield surface parameters and initial conditions

a_f (-)	m_f (-)	M_{fc} (-)	M_{fe} (-)	k (-)	p_{s0} (kPa)	p_{m0} (kPa)	p_{t0} (kPa)
0.8	0.99	1.8	1.4	0.27	200	450	121.5

Table 2 Plastic potential and mechanical hardening/softening parameters

a_g (-)	m_g (-)	M_{gc} (-)	M_{ge} (-)	ρ_s (-)	ζ_s (-)	ρ_t (-)	ζ_t (-)
1e-6	0.9	1.657	1.657	10	-0.1	5	0

Table 3 Weathering parameters

$\xi_{dis,cr}$ (-)	$S_{r,cr}$ (-)	$\sigma_{cd,0}$ (kPa)	$\sigma_{cw,0}$ (kPa)	$E_{d,0}$ (MPa)	$E_{w,0}$ (MPa)
0.4	0.25	1600 ± 100	740 ± 100	315.0 ± 100	150.0 ± 50

Table 4 Elastic parameters

K_{gr} (MPa)	ν (-)	p_r (MPa)	δ_b (-)
45 ± 5	0.09 ± 0.02	1000	5 ± 1

curve is characterized by an initial linear path until a specific point described as the generalized yielding point (see Fig. 11a) followed by a nonlinear hardening characterized by an increase in bearing capacity as the vertical displacement, s_v , increases (Nova and Parma 2011). Concerning the numerical simulation, it can be observed that the dry and wet behaviour of the calcarenite is very well captured by the model in terms of load displacement curves for the different environmental conditions (i.e. dry and wet) which are considered by assuming a value of $S_r=0$ and 1 for the dry and wet foundation, respectively. The *FE* results also show that, as the prescribed vertical settlement of the rigid footing increases, the stresses below the foundation increase and that the yielding of the rock mainly develops in tabular zone that propagates in depth forming a plastic bulb. This can be observed in Fig. 11b, c, in terms of evolution of the bonding internal variable p_m and volumetric plastic strains, respectively. Interestingly, there is a very good match in terms of size and shape of the plastic bulb determined numerically (Fig. 11b, c) and experimentally at the end of the test (Fig. 10e, f).

5.2 BVP#2: STD and LTD Processes Inducing Model Pillar Failure

The second BVP simulation is devoted to reproduce the failure of a pillar induced by a *LTD* process occurring after a *STD* process (see Fig. 12a). The experimental test simulates the degradation processes that might occur in a rock pillar within an underground cavity, when the rock is first soaked by water and then subjected to chemical weathering (Castellanza et al. 2008). As the applied vertical stress is smaller than the saturated strength of the calcarenite, the *STD* will not induce failure, whereas similar experiments where the pillar failure is induced by *STD* are reported in Ciantia et al. (2015b).

The testing layout and an illustration of the different stages of the test are shown in Fig. 12a, b, respectively. Figure 12c shows the problem geometry, the spatial discretization adopted in the *FE* simulation and the assumed boundary conditions. In the first stage of the test (OA), the specimen is loaded in uniaxial conditions, starting from a dry state. Then the specimen is saturated at constant axial stress by imposing

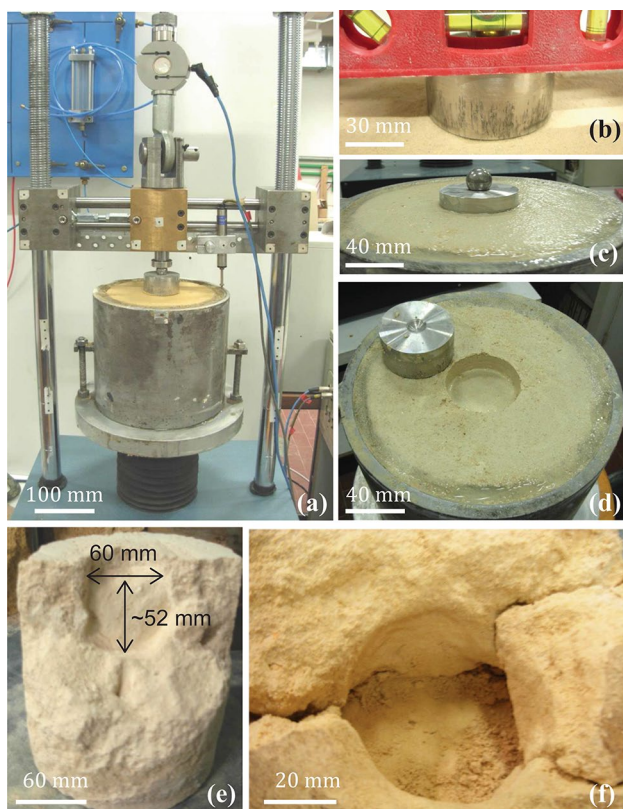


Fig. 10 a Experimental apparatus; b–d typical punching behaviour; e, f pictures of typical debonded bulbs just below the foundation

punching mechanism transforming the calcarenite into an unbonded soil just located in a bulb below the foundation (see Fig. 10d–f). The experimental load–displacement

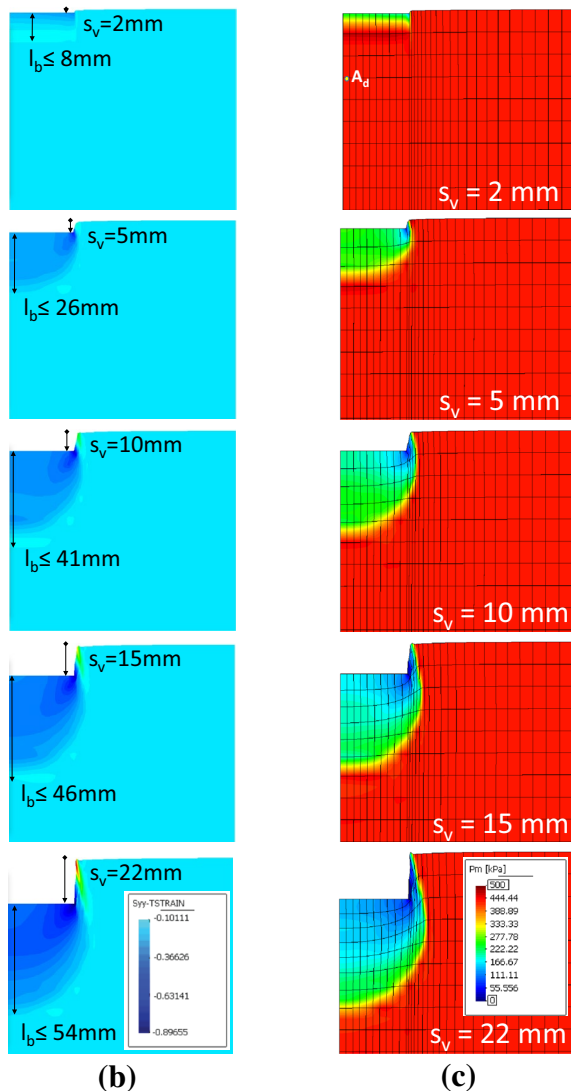
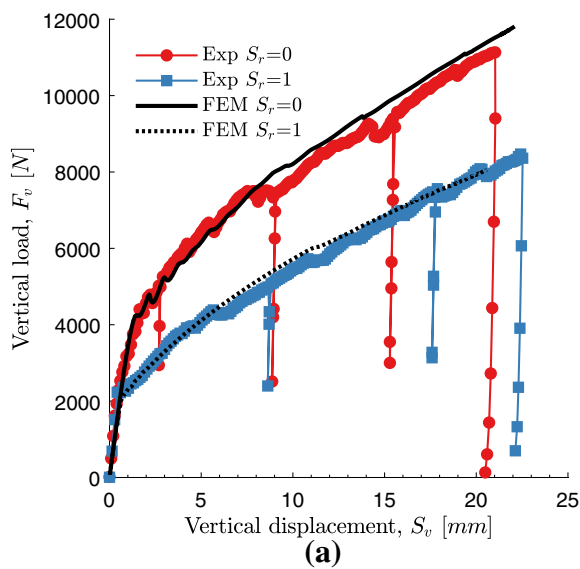


Fig. 11 **a** Experimental results and numerical simulation in ($S_r = 0$) and wet ($S_r = 1$) conditions; **b** evolution of vertical plastic strains and **c** bonding variable p_m under the model footing

an upward water flow (stage AB), up to full saturation (stage BC) during a period of 2 min. It can be observed how the sample deforms due to the stiffness reduction experienced during the *STD* (Fig. 13a). In the final stage of the test (CD), the specimen is brought to failure by a long-term exposure to an acid solution ($\text{pH} = 3.7$) on the lateral surface. The isochrones of the computed S_r , ξ_{dis} and p_m are shown in Fig. 14. The first three columns (0 to 10 min) show the effect of the *STD*, driven by an increase in S_r from the bottom of the specimen, on the bonding-related internal variable p_m . The last three columns (20 to 70 min) show the effect of the *LTD*, driven by an increase in ξ_{dis} from the lateral boundary of the specimen, on p_m . The response of the material during the first loading stage—performed in steps—is almost linearly elastic. The subsequent *STD* produces additional deformations during the wetting stage. The progressive chemical dissolution of intergranular bonds gives rise to progressively increasing deformations with time at constant stress, eventually leading to the failure of the specimen when the reduction in uniaxial rock strength due to the *LTD* is such that the axial load cannot be sustained any longer. The FE simulations, as demonstrated by the comparison between experimental observations and numerical predictions, are used to calibrate the diffusion tensor D_{ij} to correctly capture this behaviour. In the simulation, the dissolution constants K_1 and K_2 are taken from the work of Ciantia (2013) that obtained them performing dissolution tests on the same calcarenite. The computed isochrones of the axial stress (σ_y) and of ξ_{dis} along a radius at the specimen mid-height are shown in Fig. 13b, c, respectively. As the acid flows into the specimen from the lateral boundary, the values of ξ_{dis} are not uniform along the section, but minimum at the specimen axis and maximum at the boundary. The inhomogeneous degradation process resulting from the horizontal acid flow causes a progressive weakening of the external portion of the specimen that induces a reduction in axial stress close to the lateral boundary and a corresponding stress increase at the specimen axis, due to stress redistribution within the specimen. This phenomenon is qualitatively similar to the one observed in the pillars of abandoned mines (Fig. 12d) or in ancient temple columns (Fig. 12e) when the intact rock is exposed to long-term chemical degradation (Parise and Lollino 2011; Tamagnini et al. 2002).

6 Damage Analysis of Buildings Built on Top of an Abandoned Cavity in Canosa di Puglia

The $BDI(t)$ of the complex 3D geometry concerning the interaction of a cave (excavated about two centuries ago) and two buildings in a PG3 zone (Fig. 1) is here addressed. It should be noted that such situations are extremely common

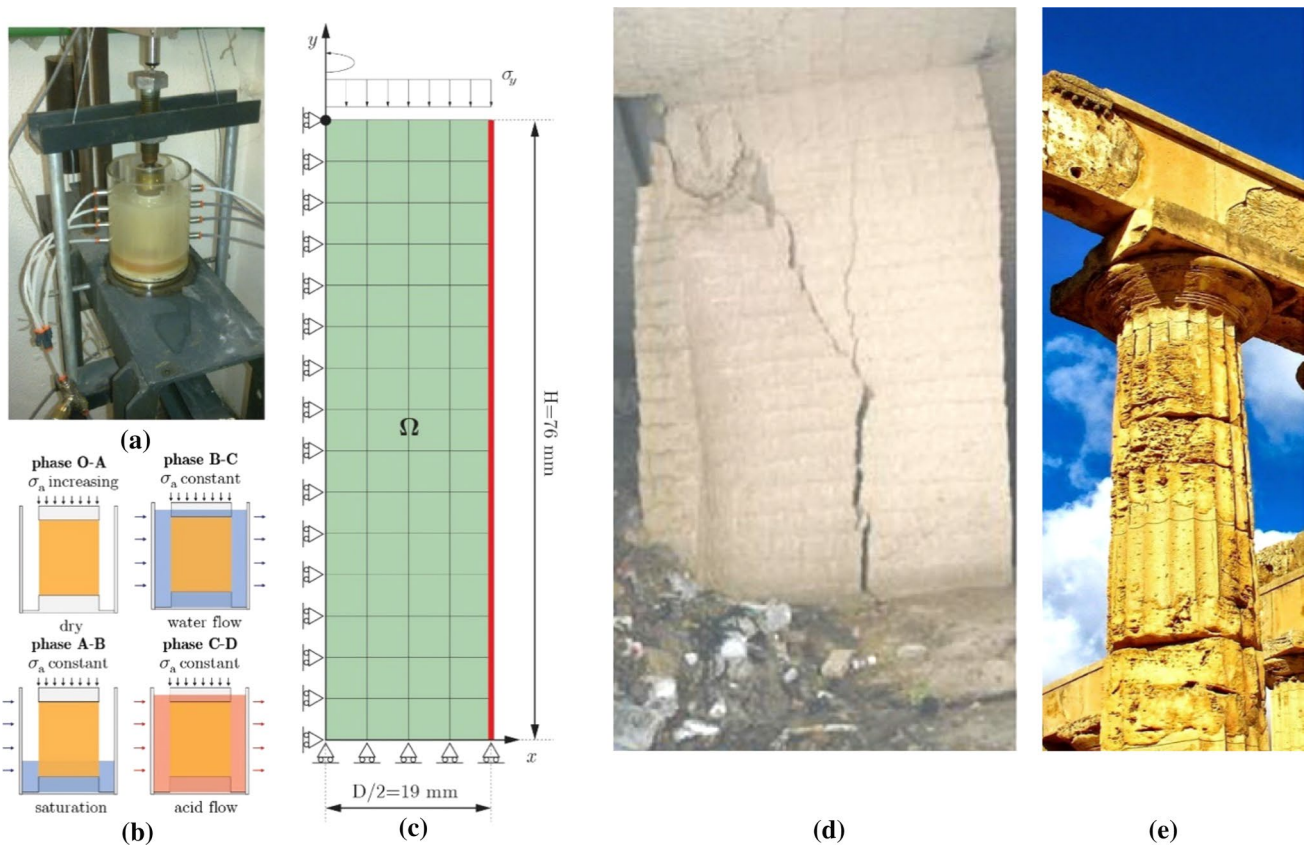


Fig. 12 **a** Small-scale pillar weathering test—experimental setup (Ciantia et al. 2015b); **b** description of testing stages; **c** geometry, spatial discretization and boundary conditions **d** example of failed

calcarenite pillar (Parise and Lollino 2011) and **e** weathering affecting an ancient column of a temple in Selinunte (Sicily, IT)

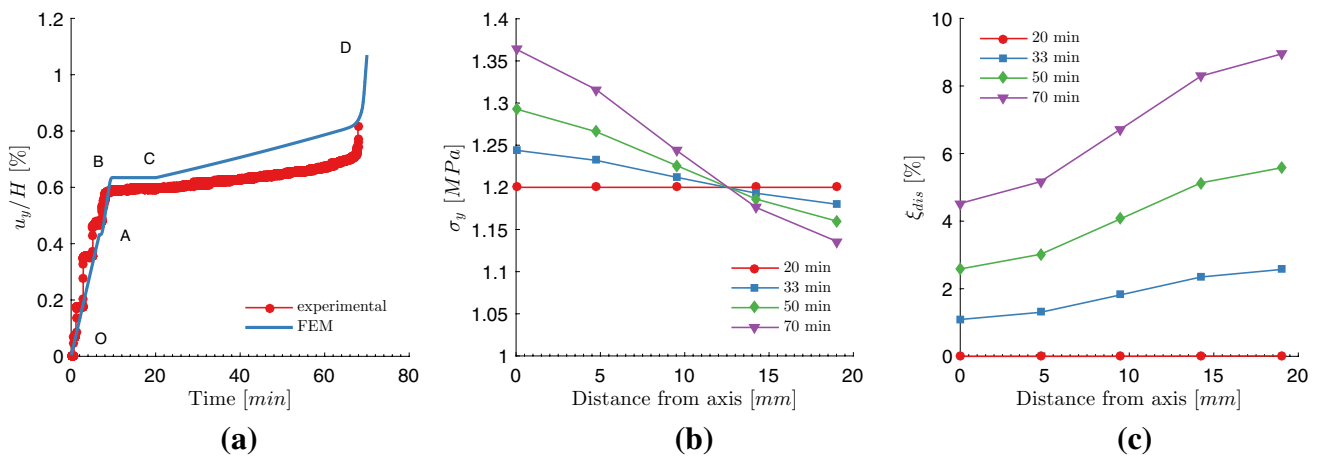


Fig. 13 FE simulation of the small-scale pillar weathering test: **a** displacement time experimental and numerical results; **b** isochrones of axial stress with distance from pillar axis; **c** isochrones of ξ_{dis} with distance from pillar axis

in the Apulian region (Parise and Vennari 2017), but this particular case study is considered as the authors were directly involved with the risk assessment of this cavity

(Ciantia et al. 2015c) and hence disposed of in situ material needed for the model calibration (see Sect. 4). The current global stability of the same geosystem determined by means

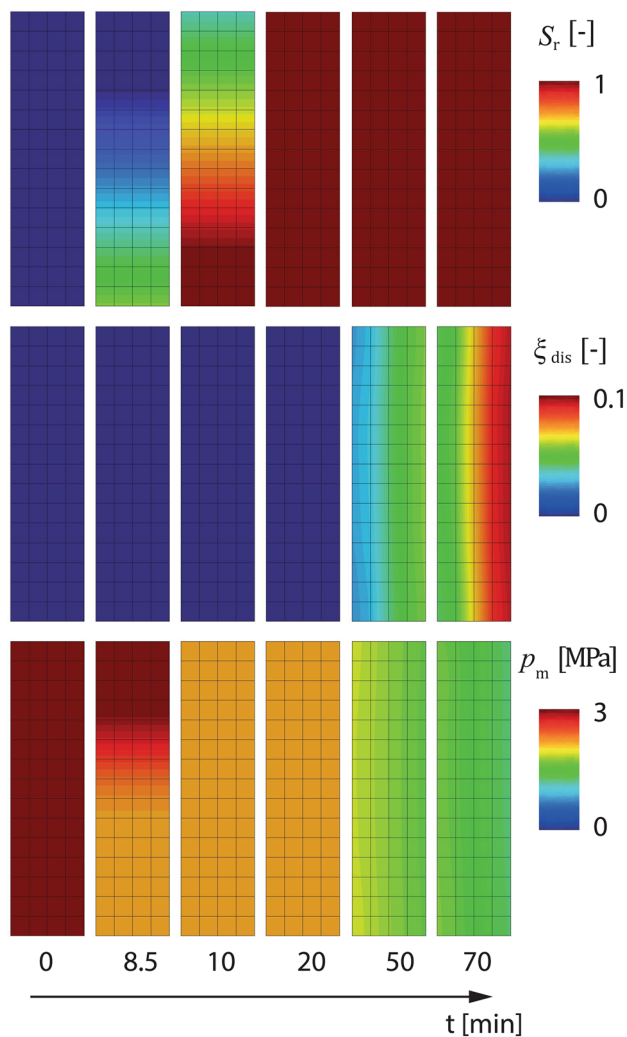


Fig. 14 *FE* simulation of the small-scale pillar weathering test: isochrones of S_r (first row), ξ_{dis} (second row) and p_m (third row) with time. Each snapshot represents half a sample as represented in Fig. 12c

of the standard $c-\phi$ reduction method (Potts et al. 1990) resulted to be 3.4 and 1.5 for the dry and saturated states, respectively (Ciantia et al. 2015c). Despite this current stable condition in both dry and saturated conditions, it is known that the long-term weathering of the rock could lead to subsidence and eventually to a failure mechanism such as the one in Fig. 2 (Ghabezloo and Pouya 2006). The $BDI(t)$ as introduced in Sect. 2 is hence used to tentatively predict the evolution of the damage on the buildings under study. The weathering scenario assumed consists of two phases:

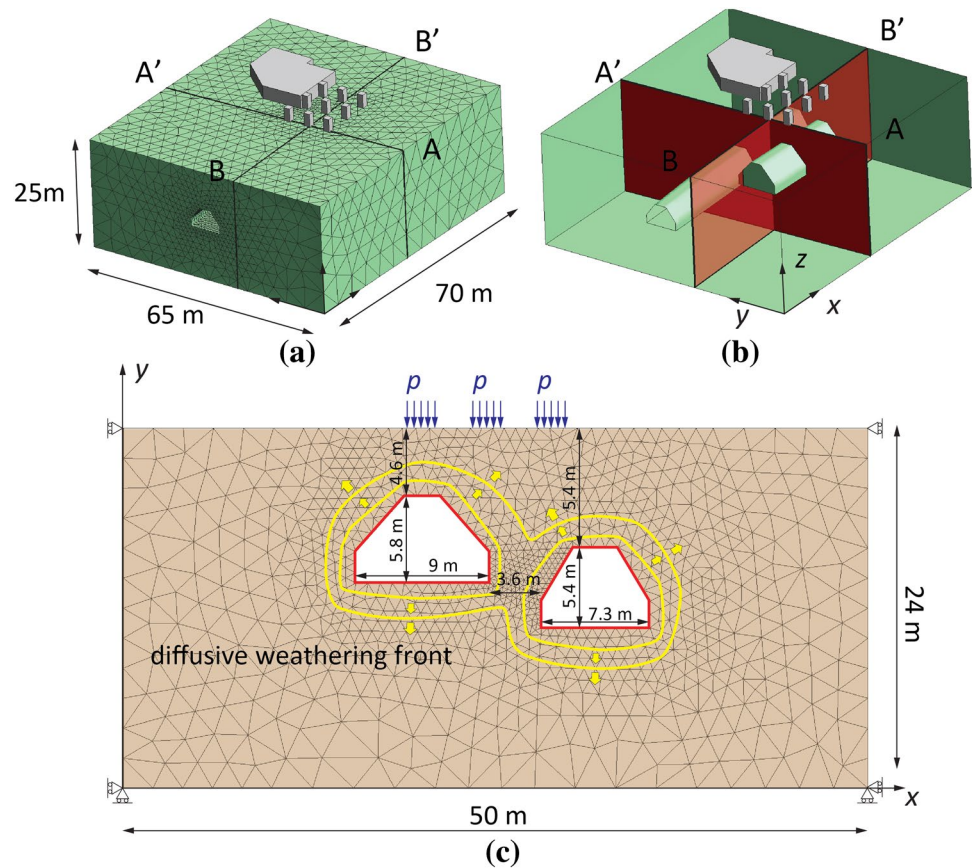
1. a saturation phase (*STD* process) that could be induced by heavy rainfalls or leakages from water supplies.
2. a long-term dissolution phase (*LTD* process) assuming the cavity remains saturated for long periods of time

in an open-system scenario (dissolved calcite ions are washed away).

The laboratory tests on the calcarenite collected in situ were used to calibrate the initial mechanical properties of the material which, assuming them to be the same for all the domains, were assigned as the model's initial state. During phase 1, simulated by setting $S_r = 1$ and hence using the 'wet' mechanical properties for the calcarenite, the geosystem remains in equilibrium. For this reason, in what follows, only the long-term chemical damage is considered (phase 2). In the absence of environmental hydraulic field data and boundary conditions, inspired by Ghabezloo and Pouya (2006), the cave boundaries were exposed to a different acidic pH environment. Such boundary conditions trigger the development of a coupled chemo-mechanical diffusion and deformation process. To consider the real geometry of the problem and realistic building loads, a 3D numerical analysis is performed, and the mesh and problem definition are shown in Fig. 15a, b. To highlight the importance of the three-dimensionality of the problem, a 2D plain strain analysis in correspondence of section A-A' is also performed. The mesh of section A-A' and the problem definition are shown in Fig. 15c. For the 3D *FEM* model discretization, 46,961 quadratic tetrahedral H10P4C4 elements (67,581 nodes and 169,270 degrees of freedom) are used, while the 2D model is meshed with 1879 triangular T6P3C3 elements (3920 nodes and 8642 degrees of freedom). Standard displacement boundary conditions have been applied to the external boundaries, with fixed horizontal and vertical displacements at the bottom and fixed horizontal displacements on the lateral boundaries. The external loads (i.e. the foundation loads) acting at the ground surface are kept constant, while the *LTD* process evolves from the inner boundary of the cave. To represent building A (see Fig. 1), a pressure of 150 kPa is imposed under each of the 9 square footings, while a pressure to represent building B a uniform pressure of 40 kPa is imposed under the area covered by it. For the 2D analysis, the same pressure of building A is applied despite the 2D geometrical limitations (plain strain hypothesis). On the cavity surfaces, a fixed constant concentration of $[H_3O^+]$ ions, corresponding to a pH of 6.7, is imposed. They will propagate into the rock by means of a diffusive phenomenon causing the long-term dissolution of $CaCO_3$. The reactive transport model parameters used for the simulations are those of *BVP#2* and are summarized in Table 5. To highlight the importance of the cavity environmental conditions, two further 3D simulations were run: one imposing a pH of 7.5, while in the other, the pH imposed at the cavity boundaries was set to 6.

Figures 16 and 17 report the main results as a function of physical time (days) from the beginning of the weathering process assumed (i.e. the *LTD* process) for the 2D and 3D

Fig. 15 a, b 3D mesh and sections considered for the BDI calculation, and c section, mesh, boundary and initial conditions for 2D simulation



simulations, respectively, for the 6.7 pH simulations. The dissolution process that evolves from the inner boundary is shown in the first column of Fig. 16 by the contour in time and space of the contaminant ion $[H_3O^+]$. As the contaminant concentration increases, the dissolution process evolves causing a mass reduction and a consequent increase in the scalar ξ_{dis} leading to a reduction in the bonding-related variables p_m and p_t (2nd column of Figs. 16 and 17). This strength reduction causes yielding of the rock to concentrate in correspondence of the partition wall for both the 2D and 3D simulations. As the exposure time with the $[H_3O^+]$ ions increases, the plastic strains localize into a shear band (3rd column) and the displacements increase (4th column). Nevertheless, before plastic strains localize into a shear band, as clearly shown in Fig. 18a, material degradation developing from the wall boundaries induces a stress redistribution in

the partition wall Fig. 18b. Although non-local approaches (Conte et al. 2010) should be adopted to avoid mesh dependency when looking at the failure mechanism, it was observed that further mesh refinement did not change the results of the simulation in terms of surface displacement with time. Interestingly, the failure of the partition wall does not cause a global failure mechanism, and this is due to the residual frictional strength within the shear band combined with the rooftop geometry. In fact, as represented in Fig. 18c, d, the stress corresponding to a point within the shear band starts from an initial elastic state, yields after about 120 days of acid exposure and evolves until critical state is reached. Figure 19 shows comparison of the displacement field for the 2D and 3D numerical simulations used to calculate the BDI for the 6.7 pH environment. The chemo-mechanical coupled induced displacements are well documented in terms

Table 5 Reactive transport parameters and initial conditions

Porosity, n (-)	Darcy isotropic permeability (m^2)	Isotropic diffusion coefficient, D (m^2/s)	K_1 (1/s)	K_2 (1/s)	$[CaCO_3]_0$ (mol/m^3)	$[H^+]_0$ (mol/m^3)	pH
0.59	$1e-12$	$1.16e-7$	$-1e-10$	-1.6	25,190	0.001	6.00
0.59	$1e-12$	$1.16e-7$	$-1e-10$	-1.6	25,190	$1.65e-4$	6.7
0.59	$1e-12$	$1.16e-7$	$-1e-10$	-1.6	25,190	$3.16e-5$	7.50

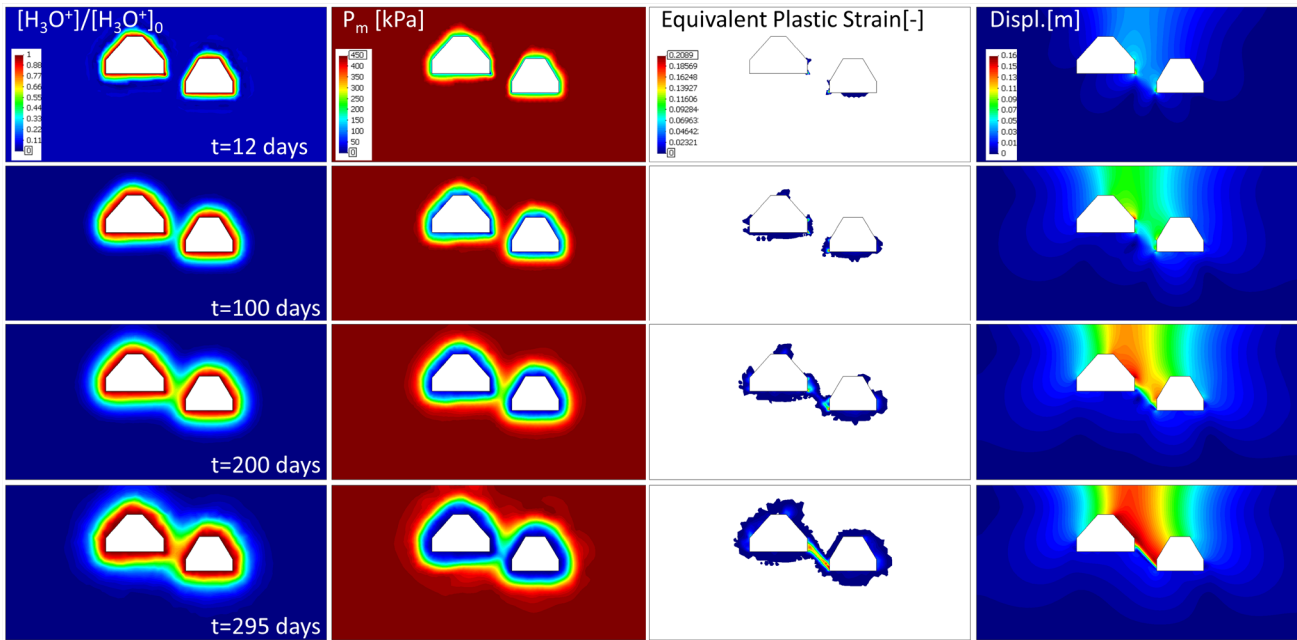


Fig. 16 2D FEM results: contour results by increasing time for the LTD process (considering column): #1 evolution of $[H_3O^+]$ contaminant; #2) internal variable related to bond strength p_m ; #3) equivalent plastic strains; #4) displacement modulus

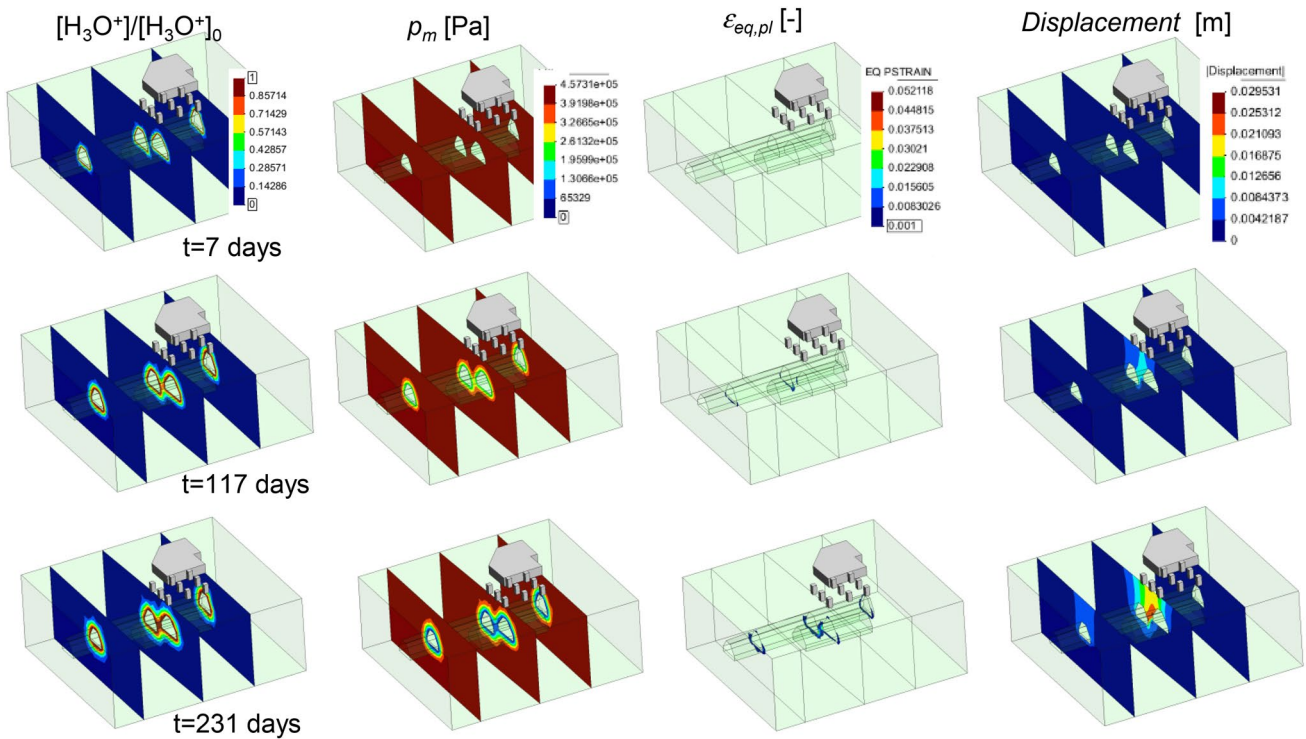


Fig. 17 3D FEM results: contour results by increasing time for the LTD process (considering column): #1 evolution of $[H_3O^+]$ contaminant; #2) internal variable related to bond strength p_m ; #3) equivalent plastic strains; #4) displacement modulus

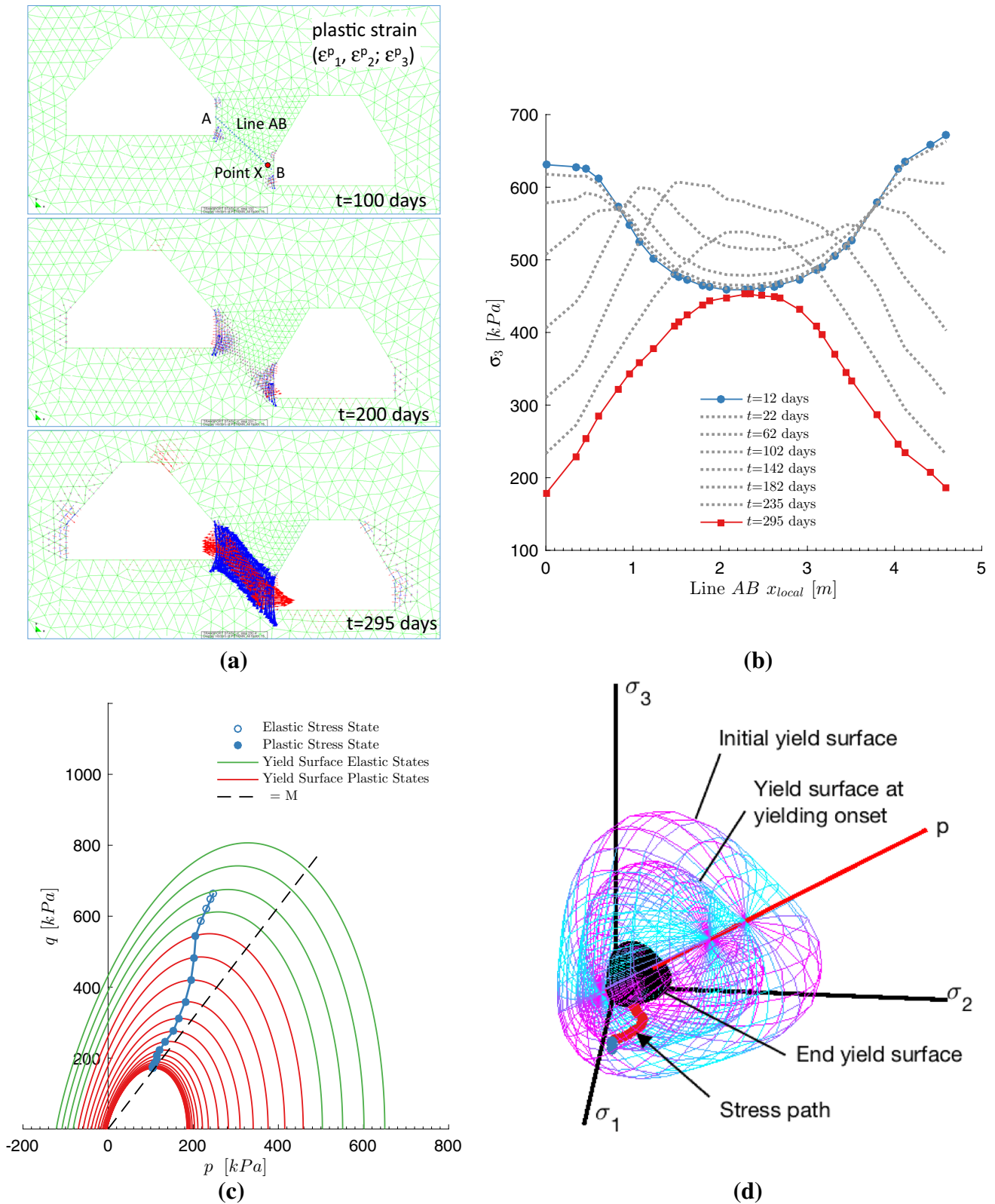


Fig. 18 LTD process: **a** evolution of principal plastic strain, **b** evolution of principal stress σ_3 along line A and B and stress path for point X along line AB on **c** rotating triaxial plane and **d** principal stress space

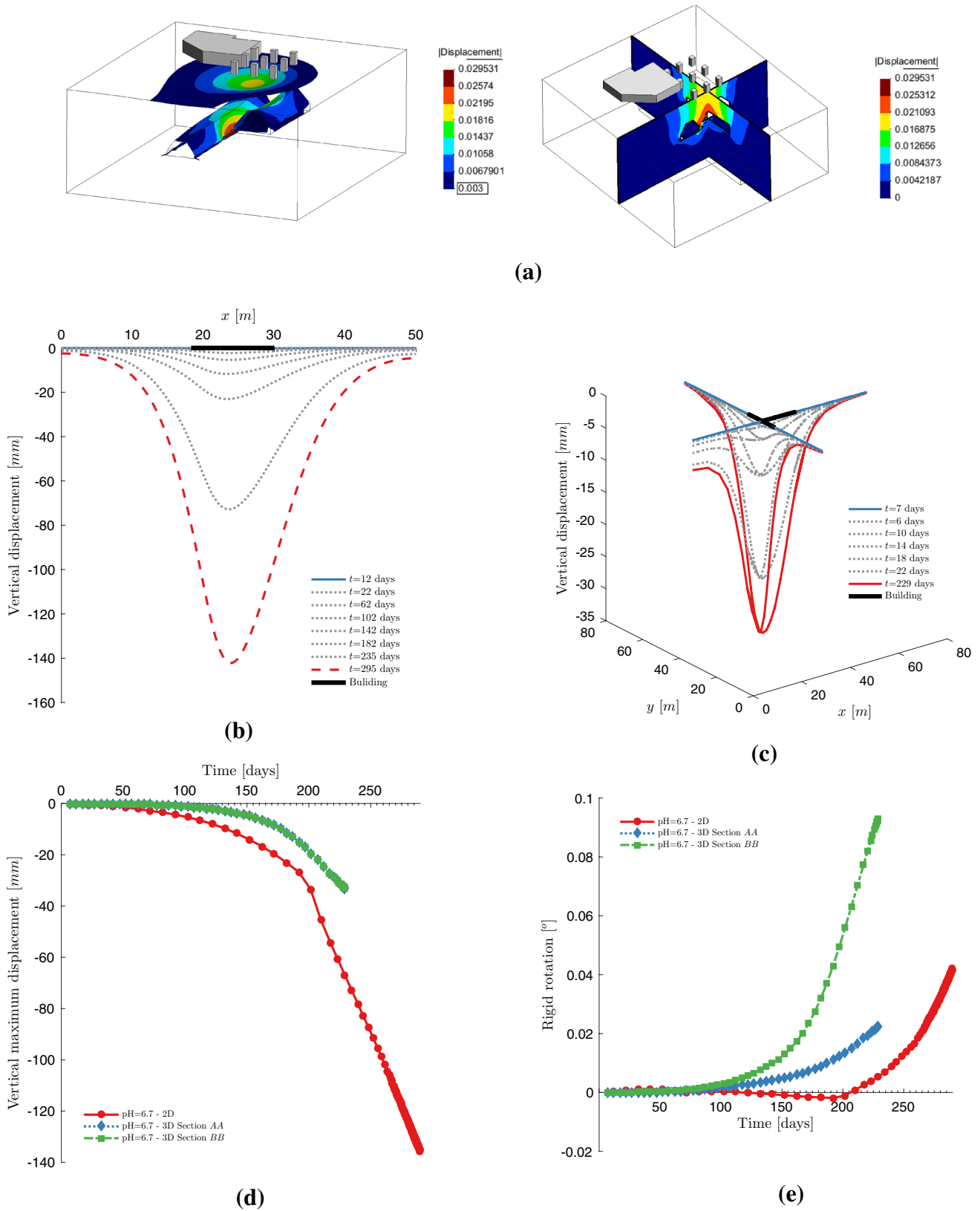


Fig. 19 Simulation results for pH = 6.7: **a** displacement contours of 3D FEM results showing subsidence basin induced by partition wall failure; 2D **b** and 3D **c** vertical displacements curves used to calculate

the BDI; **d** maximum vertical surface displacement temporal evolution time for 2 and 3D analysis, **e** rigid rotation vectors induced by LTD process

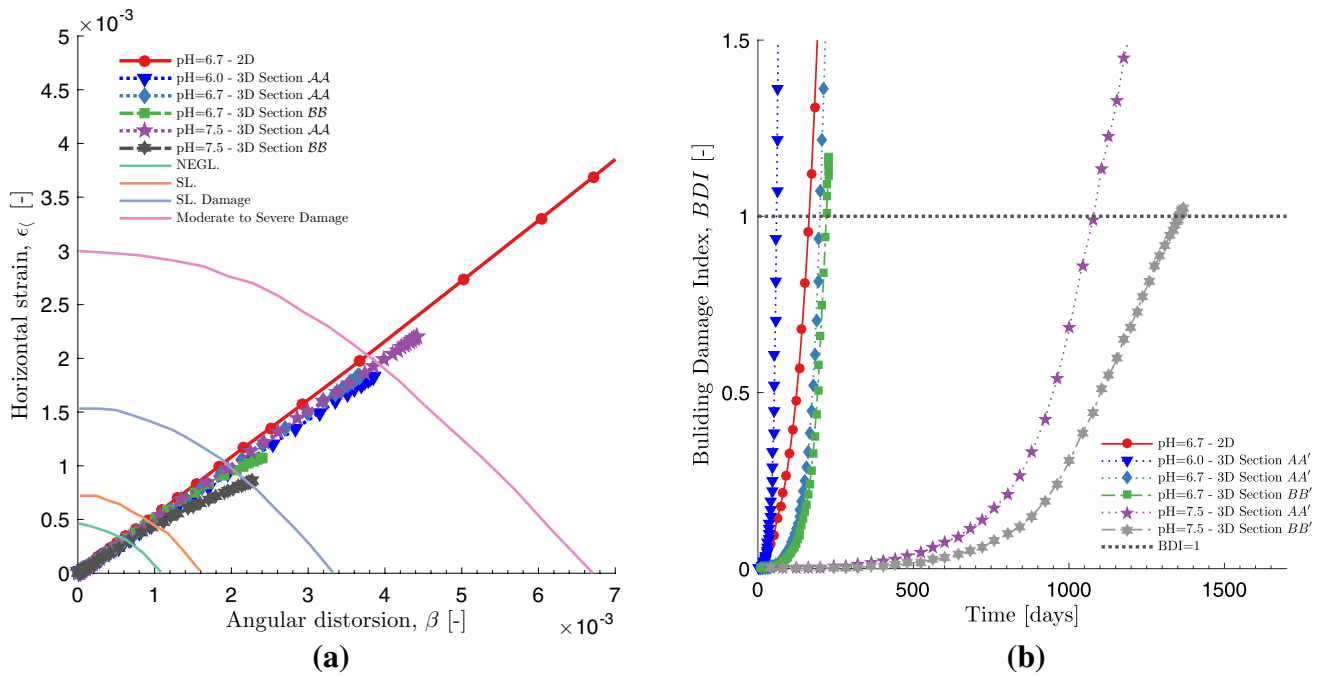


Fig. 20 **a** Building angular distortion—horizontal strain paths for the 2D and 3D *FEM* simulations in the Boscardin and Cording (1989) abacus and **b** corresponding temporal evolution of the building damage index $BDI(t)$

of the displacement contours (Fig. 19a) for the 3D simulation. The vertical displacement profiles with time for the 2D and 3D (section A-B) simulations are in Fig. 19b, c. The displacement time curves for the point with maximum surface displacement and the buildings rigid rotation evolution with time for the simulations run are reported in Fig. 19d, e. As expected, the 2D simulation deforms more than the 3D one thanks to the lateral support provided by the rock not intersected by the tunnel. The change in curvature of the displacement time curve (more visible for the 2D case) can be identified as the sinkhole inception time as from this point onward the displacement will accelerate until the simulations stops converging. Interestingly, the surface subsidence observed in the 3D simulation acquires a circular shape, and it is caused by the failure of the partition wall. Finally, in Fig. 20a the angular distortion horizontal strain paths for the 2 and 3D analyses with different pH conditions are reported. By means of Eq. (1), in Fig. 20b, the BDI evolving with time is also reported. The time needed to attain a BDI of one results to be 1080, 200 and 60 days for the 7.5, 6.7 and 6 pH case, respectively. The plot also shows how the three-dimensional effect delays the BDI attaining a value of unity from 165 to 200 days for the 6.7 pH simulation. In this contribution, only two sections were considered for the BDI assessment of building A; however, any section can be analysed and the final $BDI(t)$ would be the first one (section A-A' in this simulation) reaching a value of 1.

7 Conclusions

Many abandoned man-made caves induce sinkholes because of the degradation of the constituent soft rock. In this paper, the problem superficial subsidence prior to sinkhole formation in urban area is tackled and in particular:

- (i) A procedure to determine the temporal evolution of settlement damage to buildings by means of a building damage indicator, namely the building damage index, BDI is proposed. The weathering-induced temporal evolution of horizontal strain and angular distortion are used to introduce physical time to the BDI which is a practical scalar index of the evolution of serviceability of buildings.
- (ii) Despite all the limitations intrinsic to standard *FE* and local constitutive relationships, for the first time, a 3D numerical approach including the reactive transport of chemical species and an advanced strain-hardening plasticity constitutive model was used to tentatively predict the $BDI(t)$.
- (iii) To introduce a time-dependent building damage index, a weathering scenario must be assumed and consequently modelled. For this reason, the reactive transport of chemical species is fundamental as it enables to describe the spatial–temporal evolution of chemical species that reproduce numerically the assumed weathering scenario. The reliability of the

approach increases as the weathering mechanism reproduced is more realistic and with the soundness of the constitutive model which has to be hydro-chemo-mechanically coupled. It is shown how *BDI* is strongly dependent on the weathering scenario assumed.

- (iv) In order to determine the *BDI(t)* of a real building on an abandoned cavity in Southern Italy, standard mechanical and advanced chemo-hydro-mechanical (*CHM*) experimental tests on the in situ rock are performed and used to calibrate the constitutive model which accounts for the hydro-chemical damage effects induced by weathering.
- (v) Two model footing tests on a dry and wet calcarenite were performed, and a further small-scale boundary value experimental test from the literature is simulated to test the soundness of the model and the *FE* code to deal with *CHM*-coupled boundary value problems.
- (vi) For all simulations of the *LTD*-induced damage of the abandoned anthropic cavity, the *BDI* attained a value of 1 well before the progressive failure mechanisms starts to develop. For the same weathering scenario (6.7 pH case), smaller displacements are observed in the 3D model with respect to the 2D analysis and the *BDI* attains a value of one after a longer time.
- (vii) A plane strain 2D analysis followed by three more realistic 3D *FEM* stability analyses is performed. In all cases, the numerical results show that weathering of the porous rock causes displacements at the ground level that, before accelerating, slowly increases with time. Plastic strains begin to develop at the corners of the cavity by the partition wall well before they start to localize into a shear band. This plastic strain evolution induces a lot of stress redistribution within the rock. Despite the mesh dependency limitations, this result may suggest that such local failures can be very useful as collapse premonitory signs as in the model they start developing few months before failure. This is in accordance with what observed in the 2007 Gallipoli sinkhole where evident signs of damage on pillars were observed months before the collapse (Delle Rose 2007).
- (viii) Despite the non-symmetric geometry of the two cavities, the subsidence basin in the 3D analysis assumes a circular shape, which is typical for the sinkholes observed in these rocks (Parise and Lollino 2011). As recently observed by Nof et al. (2013) and Jones and Blom (2014) with interferometric synthetic aperture radar (*inSAR*), subsidence basins can be used a precursory signs of sinkhole formation. Interestingly, also the 3D *FEM* simulation presented here captures this feature.
- (ix) The numerical predictions show that, for open-system scenarios, it results that serviceability conditions are lost after 65 days of exposure in acidic environment (pH6), whereas the same level of damage is achieved after 3 years if the pH is set to 7.5. From an engineering perspective, the precautions to be taken to maintain the buildings in good serviceability conditions would be to monitor flood occurrence and to avoid the closing of ventilation raises. In fact, for this particular case, rock saturation and the corresponding *STD* would still not cause collapse and proper air ventilation would avoid the formation of aggressive acidic environments that, in the presence of water, would initiate the *LTD*.

Limitations of the *BDI* include aspects inherent to most deterministic numerical models of geotechnical problems. In particular the reliability of the approach will depend on: (i) the amount (and associated uncertainty) of information required concerning the geometry of the problem, (ii) the *CHM* material properties, the chemical reactions and processes, (iii) local heterogeneities and (iv) the assumption of the weathering scenarios. Many of these inconveniences may be addressed by employing a probabilistic approach (Griffiths et al. 2002; Griffiths and Fenton 2004; Zhang and Ng 2005). We also believe that in a near future remote sensing techniques such as the interferometric synthetic aperture radar (*inSAR*) from satellite images will provide temporal evolution of subsidence that will allow to test and improve the reliability of the proposed methodology.

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Appendix 1

The convection–diffusion reactive equation that governs the contaminant transport problem (Eq. 4) is split in a pure advection system of partial differential equations (*PDEs*) solved using the Taylor–Galerkin discretization technique

described in (Donea 1984; Löhner et al. 1984) already applied to both fluid dynamics and solid mechanics (Mabsout and Pastor 2003a, b; Peraire et al. 1986; Quecedo and Pastor 2002) and a system of ordinary differential equations solved with a fourth-order Runge–Kutta algorithm (Hirsch 1988; Lambert 1973). In particular, denoting with ∇ the vector differential operator, Eq. (4) is written in a more compact manner as:

$$\frac{\partial}{\partial t} \boldsymbol{\phi} + \bar{\nabla} \mathbf{F} = \bar{\nabla} \cdot (\mathbf{D} \bar{\nabla} \boldsymbol{\phi}) + \mathbf{S} \tag{10}$$

where we have introduced the vector of unknowns $\boldsymbol{\phi} = \begin{pmatrix} [\text{H}_3\text{O}^+] \\ [\text{CaCO}_3] \end{pmatrix}$, a flux vector $\mathbf{F} = \begin{pmatrix} \mathbf{q} [\text{H}_3\text{O}^+] \\ \mathbf{0} \end{pmatrix}$, a $\bar{\nabla}$ operator defined by $\bar{\nabla} = \begin{pmatrix} \nabla & 0 \\ 0 & \nabla \end{pmatrix}$, a diffusion matrix $\mathbf{D} = \begin{pmatrix} D_{ij} & 0 \\ 0 & 0 \end{pmatrix}$ and a source vector $\mathbf{S} = \Gamma \cdot \boldsymbol{\phi}$ with $\Gamma = \begin{pmatrix} 0 & -K_1 \\ -K_2 & 0 \end{pmatrix}$. The system can also be written in a non-conservative form as:

$$\frac{\partial}{\partial t} \boldsymbol{\phi} + \mathbf{Q} \bar{\nabla} \boldsymbol{\phi} = \mathbf{D} \bar{\nabla}^2 \boldsymbol{\phi} + \mathbf{S} \tag{11}$$

where we have supposed that $\nabla \cdot \mathbf{q} = 0$ as the flow is considered incompressible, $\mathbf{Q} = \begin{pmatrix} \mathbf{q} & 0 \\ 0 & 0 \end{pmatrix}$ and where we have supposed constants diffusion coefficients.

The mass balance equation includes convection, diffusion and retardation effect due to the chemical reaction between calcite and acid ions. Equation (11) combines both parabolic and hyperbolic PDEs with a source term \mathbf{S} , and it can be solved using a splitting operator technique in which each of the two operators, convective–diffusive transport and sources, is treated separately (Toro 2001):

$$\left. \begin{array}{l} PDE \quad : \quad \frac{\partial}{\partial t} \boldsymbol{\phi} + \mathbf{Q} \bar{\nabla} \boldsymbol{\phi} = \mathbf{D} \bar{\nabla}^2 \boldsymbol{\phi} + \mathbf{S}(\boldsymbol{\phi}) \\ \text{initial condition, IC} : \quad \boldsymbol{\phi}(\mathbf{x}, t^n) = \boldsymbol{\phi}^n(\mathbf{x}) \end{array} \right\} \tag{12}$$

We want to evolve $\boldsymbol{\phi}^n$ from time $t = t^n$ to the new value $\boldsymbol{\phi}^{n+1}$ at $t = t^{n+1}$ by a time step $\Delta t = t^{n+1} - t^n$. Therefore, two problems will be considered:

(i) A diffusion–advection problem of the type

$$\left. \begin{array}{l} PDE \quad : \quad \frac{\partial}{\partial t} \boldsymbol{\phi} + \mathbf{Q} \bar{\nabla} \boldsymbol{\phi} - \mathbf{D} \bar{\nabla}^2 \boldsymbol{\phi} = 0 \\ \text{initial condition, IC} : \quad \boldsymbol{\phi}(\mathbf{x}, t^n) = \boldsymbol{\phi}^n(\mathbf{x}) \end{array} \right\} \Rightarrow \boldsymbol{\phi}^{\text{adv-dif}} \tag{13}$$

(ii) and the source problem, which is an ordinary differential equation (ODE):

$$\left. \begin{array}{l} ODE : \quad \frac{d\boldsymbol{\phi}}{dt} = \mathbf{S}(\boldsymbol{\phi}) \\ IC : \quad \boldsymbol{\phi}(\mathbf{x}, t^n) = \boldsymbol{\phi}^{\text{adv-dif}} \end{array} \right\} \xrightarrow{\Delta t} \boldsymbol{\phi}^{n+1} \tag{14}$$

The initial condition IC of the advection–diffusion problem (13) is the initial condition $\boldsymbol{\phi}^n$ of the full problem, and the solution after a time step Δt is $\boldsymbol{\phi}^{\text{adv-dif}}$, which may be regarded as a predicted solution. ODE (14) is then solved by a time Δt and with initial condition $\boldsymbol{\phi}^{\text{adv-dif}}$, and the solution of Eq. (14) is then regarded as the approximate solution to the full problem. One may choose the best scheme for each type of sub-problem.

Adopted Taylor–Galerkin Scheme for Advective–Diffusive Transport

Concerning the advective-diffusion part, the scheme used in this work is a two-step Taylor–Galerkin algorithm, introduced in (Donea 1984; Löhner et al. 1984), and applied to both fluid dynamics and solid mechanics (Mabsout and Pastor 2003a, 2003b; Peraire et al. 1986; Quecedo and Pastor 2002). The method is based on a Taylor expansion in time of the solution at time step n ,

$$\boldsymbol{\phi}^{n+1/2} = \boldsymbol{\phi}^n + \frac{\Delta t}{2} \left. \frac{\partial \boldsymbol{\phi}}{\partial t} \right|^n \tag{15}$$

where the time derivative will be evaluated using the PDE as:

$$\left. \frac{\partial \boldsymbol{\phi}}{\partial t} \right|^n = -\mathbf{Q} \bar{\nabla} \boldsymbol{\phi}^n + \mathbf{D} \bar{\nabla}^2 \boldsymbol{\phi}^n \tag{16}$$

resulting in:

$$\boldsymbol{\phi}^{n+1/2} = \boldsymbol{\phi}^n + \frac{\Delta t}{2} \left(-\mathbf{Q} \bar{\nabla} \boldsymbol{\phi}^n + \mathbf{D} \bar{\nabla}^2 \boldsymbol{\phi}^n \right) \tag{17}$$

From here, we can obtain fluxes at time $n + 1/2$ and use them in the second step:

$$\boldsymbol{\phi}^{n+1} = \boldsymbol{\phi}^n + \Delta t \left. \frac{\partial \boldsymbol{\phi}}{\partial t} \right|^{n+1/2} = \boldsymbol{\phi}^n + \Delta t \left(-\mathbf{Q} \bar{\nabla} \boldsymbol{\phi}^{n+1/2} + \mathbf{D} \bar{\nabla}^2 \boldsymbol{\phi}^{n+1/2} \right) \tag{18}$$

From this point, we apply a standard Boubnov–Galerkin method to perform a discretization in space $\boldsymbol{\phi} = \mathbf{N}_\phi \hat{\boldsymbol{\phi}}$, obtaining

$$\mathbf{M} \Delta \hat{\boldsymbol{\phi}} = \Delta t \left(\int_{\Omega} (\nabla \mathbf{N}_\phi)^T (\mathbf{Q} \boldsymbol{\phi}^{n+1/2} - \mathbf{D} \nabla \boldsymbol{\phi}^{n+1/2}) d\Omega - \int_{\partial\Omega} \mathbf{N}_\phi^T (\mathbf{Q} \boldsymbol{\phi}^{n+1/2} - \mathbf{D} \nabla \boldsymbol{\phi}^{n+1/2}) \cdot \mathbf{n} d\Gamma \right) \tag{19}$$

where $\mathbf{M} = \int_{\Omega} \mathbf{N}_{\phi}^T \mathbf{N}_{\phi} d\Omega$ is the classical mass matrix and $\Delta \hat{\boldsymbol{\phi}} = \boldsymbol{\phi}^{n+1} - \boldsymbol{\phi}^n$. It is important to remark that the system of equations can be written in the form

$$\mathbf{M}\mathbf{x} = \mathbf{f} \tag{20}$$

and can be solved using an iterative Jacobi or “accelerated viscous relaxation scheme”. Both are described in (Zienkiewicz and Taylor 2000). The iterations are:

$$\mathbf{x}^{(k+1)} = \mathbf{x}^{(k)} + \mathbf{M}_L^{-1} (\mathbf{f} - \mathbf{M}\mathbf{x}^{(k)})$$

where \mathbf{M}_L is the lumped mass matrix, which is diagonal. The method can be considered as explicit, and provides an accurate solution in less than 5 iterations.

Adopted Runge–Kutta, Fourth-Order Accurate Scheme for the Source Term

The second part of the splitting concerns the source term:

$$\frac{d\boldsymbol{\phi}}{dt} = \mathbf{S}(\boldsymbol{\phi}) \tag{21}$$

Runge–Kutta (RK) algorithms provide a high accuracy in the evaluation of ODEs (Hirsch 1988; Lambert 1973). The general form of a RK algorithm is

$$\boldsymbol{\phi}^{n+1} = \boldsymbol{\phi}^n + \Delta t \sum_{k=1}^k \beta_k \mathbf{S}(\boldsymbol{\phi}_k) \tag{22}$$

with

$$\begin{aligned} \boldsymbol{\phi}_1 &= \boldsymbol{\phi}^n \\ \boldsymbol{\phi}_2 &= \boldsymbol{\phi}^n + \Delta t \alpha_2 \mathbf{S}(\boldsymbol{\phi}_1) \\ \boldsymbol{\phi}_3 &= \boldsymbol{\phi}^n + \Delta t \alpha_3 \mathbf{S}(\boldsymbol{\phi}_2) \\ &\dots \dots \dots \\ \boldsymbol{\phi}_k &= \boldsymbol{\phi}^n + \Delta t \alpha_k \mathbf{S}(\boldsymbol{\phi}_{k-1}) \end{aligned}$$

where the consistency condition $\sum_{k=1}^k \beta_k = 1$ has to be fulfilled.

Here we have chosen a fourth-order RK algorithm, as it provides an excellent combination of accuracy and computational effort. The coefficients are given by:

$$\begin{aligned} \alpha_2 &= \frac{1}{2}; \quad \alpha_3 = \frac{1}{2}; \quad \alpha_4 = 1; \\ \beta_1 &= \frac{1}{6}; \quad \beta_2 = \beta_3 = \frac{1}{3}; \quad \beta_4 = \frac{1}{6}; \end{aligned} \tag{23}$$

from where we obtain

$$\begin{aligned} \boldsymbol{\phi}_1 &= \boldsymbol{\phi}^n \\ \boldsymbol{\phi}_2 &= \boldsymbol{\phi}^n + \frac{1}{2} \Delta t \mathbf{S}(\boldsymbol{\phi}_1) \\ \boldsymbol{\phi}_3 &= \boldsymbol{\phi}^n + \frac{1}{2} \Delta t \mathbf{S}(\boldsymbol{\phi}_2) \\ \boldsymbol{\phi}_4 &= \boldsymbol{\phi}^n + \Delta t \mathbf{S}(\boldsymbol{\phi}_3) \\ \boldsymbol{\phi}^{n+1} &= \boldsymbol{\phi}^n + \frac{\Delta t}{6} [\mathbf{S}(\boldsymbol{\phi}_1) + 2\mathbf{S}(\boldsymbol{\phi}_2) + 2\mathbf{S}(\boldsymbol{\phi}_3) + \mathbf{S}(\boldsymbol{\phi}_4)] \end{aligned} \tag{24}$$

As $\mathbf{S}(\boldsymbol{\phi}) = \boldsymbol{\Gamma} \cdot \boldsymbol{\phi}$ with $\boldsymbol{\Gamma}$ constant:

$$\boldsymbol{\phi}^{n+1} = \left[1 + \Delta t \boldsymbol{\Gamma} + \frac{(\Delta t \boldsymbol{\Gamma})^2}{2} + \frac{(\Delta t \boldsymbol{\Gamma})^3}{6} + \frac{(\Delta t \boldsymbol{\Gamma})^4}{24} \right] \boldsymbol{\phi}^n \tag{25}$$

Appendix 2

As described in Ciantia and di Prisco (2015) the two driving variables of weathering of calcarenite are the normalized dissolved mass ξ_{dis} and the degree of saturation S_r . ξ_{dis} is the dissolution reaction progress variable calculated as

$$\xi_{dis} = \frac{\Delta M}{M_0} = \frac{[\text{CaCO}_3]_0 - [\text{CaCO}_3]}{[\text{CaCO}_3]_0} \tag{26}$$

where ΔM and M_0 are calcium carbonate’s dissolved and initial mass, respectively. The weathering function Y governs the size of the yield locus when the material is subject to environmental loads and is a scalar that goes from 1 (intact) to 0 (completely weathered) and can be written as:

$$Y = Y_{sus} + Y_{dis} \tag{27}$$

where

$$Y_{sus} = \begin{cases} \frac{\sigma_{cd}^d - \sigma_{cd}^w}{\sigma_{cd}^d} \left(1 - \frac{S_r}{S_{r,cr}} \right)^2 & S_r \leq S_{r,cr} \\ 0 & S_r > S_{r,cr} \end{cases} \tag{28}$$

$$Y_{dis} = \begin{cases} \frac{\sigma_{cd}^w}{\sigma_{cd}^d} \left(1 - \frac{\xi_{dis}}{\xi_{dis,cr}} \right)^2 & \xi_{dis} \leq \xi_{dis,cr} \\ 0 & \xi_{dis} > \xi_{dis,cr} \end{cases} \tag{29}$$

While the stiffness weathering function, Y_E , governs the stiffness of the material when subject to environmental loads and results:

$$Y_E = Y_{E,sus} + Y_{E,dis} \tag{30}$$

where

$$Y_{E,sus} = \begin{cases} \frac{E_0^d - E_0^w}{E_0^d} \left(1 - \frac{S_r}{S_{r,cr}} \right)^2 & S_r \leq S_{r,cr} \\ 0 & S_r > S_{r,cr} \end{cases} \tag{31}$$

$$Y_{E,\text{dis}} = \begin{cases} \frac{E_0^w}{E_0^d} \left(1 - \frac{\xi_{\text{dis}}}{\xi_{\text{dis,cr}}}\right)^2 & \xi_{\text{dis}} \leq \xi_{\text{dis,cr}} \\ 0 & \xi_{\text{dis}} > \xi_{\text{dis,cr}} \end{cases} \quad (32)$$

In Eqs. (28)–(32), σ_{c0}^w and σ_{c0}^d represent the uniaxial compression strengths of calcarenite rock under wet and dry conditions, respectively; E_0^d and E_0^w are the Young's moduli of the intact material in dry and wet states, respectively; $S_{r,cr}$ is the minimum degree of saturation necessary for all the depositional bonds to suspend, while $\xi_{\text{dis,cr}}$ is the normalized dissolved mass that corresponds to the ideal threshold between the bonded and the granular material state (all bonds have been dissolved).

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