



THE UNIVERSITY *of* EDINBURGH

Edinburgh Research Explorer

Data assimilation of soil water flow via ensemble Kalman filter: infusing soil moisture data at different scales

Citation for published version:

Zhu , P, Shi, L, Zhu, Y, Zhang, Q, Huang, K & Williams, M 2017, 'Data assimilation of soil water flow via ensemble Kalman filter: infusing soil moisture data at different scales' Journal of Hydrology. DOI: 10.1016/j.jhydrol.2017.10.078

Digital Object Identifier (DOI):

[10.1016/j.jhydrol.2017.10.078](https://doi.org/10.1016/j.jhydrol.2017.10.078)

Link:

[Link to publication record in Edinburgh Research Explorer](#)

Document Version:

Peer reviewed version

Published In:

Journal of Hydrology

General rights

Copyright for the publications made accessible via the Edinburgh Research Explorer is retained by the author(s) and / or other copyright owners and it is a condition of accessing these publications that users recognise and abide by the legal requirements associated with these rights.

Take down policy

The University of Edinburgh has made every reasonable effort to ensure that Edinburgh Research Explorer content complies with UK legislation. If you believe that the public display of this file breaches copyright please contact openaccess@ed.ac.uk providing details, and we will remove access to the work immediately and investigate your claim.



1 **Data assimilation of soil water flow via ensemble Kalman filter:**
2 **infusing soil moisture data at different scales**

3 Penghui Zhu^a, Liangsheng Shi^{a*}, Yan Zhu^a, Qiuru Zhang^a, Kai Huang^b, Mathew Williams^c

4 ^a State Key Laboratory of Water Resources and Hydropower Engineering Sciences, Wuhan
5 University, Wuhan, Hubei 430072, China

6 ^b Guangxi Institute of Hydraulic Research, Nanning, Guangxi 530023, China

7 ^c School of GeoSciences and National Centre for Earth Observation, University of Edinburgh,
8 Edinburgh EH9 3FF, United Kingdom

9

10

11

12 *Corresponding author, E-mail: liangshs@whu.edu.cn

13 **Abstract**

14 This paper assesses the value of multi-scale near-surface (0~5cm) soil moisture observations to
15 improve state-only or state-parameter estimation based on the ensemble Kalman filter (EnKF). To
16 the best of our knowledge, studies on assimilating multi-scale soil moisture data into a distributed
17 hydrological model with a series of detailed vertical soil moisture profiles are rare. Our analysis
18 factors include spatial measurement scales, soil spatial heterogeneity, multi-scale data with
19 contrasting information and systematic measurement errors. Results show that coarse-scale soil
20 moisture data are also very useful for identifying finer-scale parameters and states given biased
21 initial parameter fields, but it becomes increasingly difficult to recover the finer-scale spatial
22 heterogeneity of soil property as the observation grids become coarser. In state-only estimation,
23 near-surface soil moisture data result in improvement for shallow soil moisture profiles and
24 degradation for deeper soil moisture profiles, with stronger influences from finer-scale data. With
25 the decrease of background spatial heterogeneity of soil property, the value of coarse-scale data
26 increases notably. Soil moisture data at two scales with contrasting information are found to be both
27 useful. By updating spatially correlated soil hydraulic parameters, deviated observations still contain
28 considerably useful information for finer-scale state-parameter estimation. More importantly, by
29 presenting a difference information assimilation method we successfully extract useful information
30 from soil moisture data containing systematic measurement errors. The current study can be
31 extended to consider more complex atmosphere input and topography, etc.

32 *Key words:* data assimilation, multi-scale soil moisture data, distributed hydrologic model

33 1. Introduction

34 Data assimilation (DA), as a tool to improve model parameters and state predictions using
35 observational data, has been frequently applied to hydrological practices (Chen and Zhang, 2006;
36 Clark et al., 2008; Houser et al., 1998; Liu et al., 2012; Moradkhani et al., 2005; Samuel et al., 2014;
37 Shi et al., 2012; Weerts and El Serafy, 2006; Xu and Gómez-Hernández, 2016). Soil moisture is a
38 key variable in the land surface system and also an important source of observable data in DA. There
39 still exist several aspects that might increase the difficulty of using soil moisture data for the
40 improvement of hydrological simulations. One is that different measurement techniques yield soil
41 moisture data of different scales, resolutions and accuracies (Susha et al., 2014; Vereecken et al.,
42 2008); the second is that soil moisture itself exhibits high spatial and temporal variability at a variety
43 of scales (Crow and Wood, 1999; Famiglietti et al., 1999; Gaur and Mohanty, 2013; Hu et al., 1998;
44 Korres et al., 2015); another is that the scale mismatch between monitoring and modeling often
45 occurs (Blöschl and Sivapalan, 1995; Western and Blöschl, 1999). Based on the aforementioned
46 reasons, it remains a challenge to assimilate soil moisture data from multiple scales into modeling
47 results to optimize estimation efficiently and effectively.

48 In order to capture the spatiotemporal characteristics (correlation length, variability, mean
49 value, etc.) of soil moisture, a variety of measurement techniques have been developed. Vereecken
50 et al. (2008) classified soil moisture measurements into two main categories: contact-based and
51 contact-free methods. The former requires direct contact with the soil (e.g. time domain
52 reflectometry), and typically provides point-scale measurements with high temporal and spatial
53 resolutions as well as field-scale spatiotemporal soil moisture dynamics. The latter mainly includes
54 remote sensing methods and hydro-geophysical methods (e.g. ground penetrating radar), and is

55 more suitable for large and medium-scale monitoring (Romano, 2014; Vereecken et al., 2008). A
56 critical evaluation of almost all the classical and modern soil moisture measurement means was
57 presented by Susha et al. (2014), which reconfirmed that “both classical and modern techniques
58 exhibit uncertainty related to the accuracy, precision, coverage and volume of measurements”. Many
59 other remarkable reviews are also available for interested readers, among which Fang and Lakshmi
60 (2014), Robinson et al. (2008) and Romano (2014) are highly recommended. The emergence of
61 various soil moisture measurement techniques provides a good opportunity for hydrological data
62 assimilation, but how to evaluate the value of soil moisture data from multiple scales is challenging
63 work.

64 As the term “scale” appears on different occasions, it is imperative to present the general
65 meaning of it. In hydrology, the term “scale” may be defined from three perspectives, i.e. process
66 scale (or characteristic scale of a process), observation scale and modeling scale (Blöschl and
67 Sivapalan, 1995). The process scale is the scale that natural phenomena exhibit, and for a stochastic
68 process, it refers to the scale of natural variability, which can be quantified by the correlation length
69 of a natural process or variable (Western and Blöschl, 1999). The correlation length can be
70 represented by the “range”, which is a key parameter of the variogram. The range is the maximum
71 distance of correlation. First proposed by Blöschl and Sivapalan (1995) and later adopted and
72 improved by Korres et al. (2015), Romano (2014) and Vereecken et al. (2008), the concept of
73 observation and modeling scale consists of a triplet of “support”, “spacing”, and “extent”, and
74 applies to both spatial and temporal dimensions. Support refers to the integration volume or area (or
75 time) of a single sample or model element, spacing to the distance (or time interval) between
76 samples, and extent to the overall measurement or simulation domain. In this study, the scale of soil

77 moisture observations is specified with the “support” component, which is related to the spatial
78 resolution in the sensors’ terminology.

79 The horizontal supports of frequently used techniques are on the order of centimeters for the
80 handheld probes (e.g. ECH2O and FDR), meters for the geophysical methods (e.g. GPR),
81 decameters or hectometers for the air-borne sensors (e.g. SAR, synthetic aperture radar and PBMR,
82 L band push broom microwave radiometer), and hectometers or kilometers for the space-borne
83 sensors (e.g. SMOS) (Fang and Lakshmi, 2014; Korres et al., 2015; Koyama et al., 2009; Koyama
84 et al., 2010; Vereecken et al., 2008). Multi-scale soil moisture data may contain useful information
85 of the surface-subsurface hydrological system at different spatio-temporal levels, and methods that
86 can assimilate multi-scale data as well as accessing the value of them are needed. Durand and
87 Margulis (2007) assimilate synthetic 25 km passive microwave (PM) observations and synthetic 1
88 km near infrared (NIR) narrowband albedo observations into a land surface model with a resolution
89 of 1 km based on the EnKF approach. Lievens et al. (2015) provide an algorithm that deals with the
90 assimilation of 25 km SMOS soil moisture data into the Variable Infiltration Capacity (VIC) model
91 with a resolution of 12.5 km. Montzka et al. (2012) give an overview of multivariate and multi-scale
92 data assimilation in terrestrial systems and state that both the PF (Particle Filter) and the EnKF are
93 useful algorithms that can infuse multi-scale data. They note that multi-scale data assimilation can
94 be performed in two ways: to use the observation operator, or to rescale the observations to the
95 model scale prior to assimilation.

96 Although methods already exist for the assimilation of multi-scale data, their applications in
97 terrestrial systems are limited (Montzka et al., 2012). One reason is that there might exist a mismatch
98 between the scale at which data are measured and the scale at which simulations are conducted.

99 Synthetic or real-world studies concerning the “scale-mismatch” problem in multi-scale data
100 assimilation are highly required. Another reason is that soil moisture data measured at different
101 scales may conflict with each other, and insights on how to deal with conflicting data are lacking
102 (Montzka et al., 2012). A third reason is that soil moisture at different scales exhibit spatial and
103 temporal variability which is affected by several factors, such as soil, land use, meteorology,
104 topography, and measurement scale (De Lannoy et al., 2006; Korres et al., 2013; Korres et al., 2015;
105 Western et al., 1998). For the top-layer soil moisture data set of the OPE³ field in De Lannoy et al.
106 (2006), the horizontal range of soil moisture increases in wetter periods, during which a vertical flux
107 of precipitation exists. Korres et al. (2013) find the combined influences of soil property,
108 precipitation, land use pattern, evapotranspiration and analysis scale on surface soil moisture
109 patterns in the modeling study on an agricultural field. For the soil moisture data sets of
110 Rs15mCatchCrop and Rs150mCatchCrop in Korres et al. (2015), the mean range value changes
111 from 432m to 711m, indicating that the correlation length increases with the measurement support.
112 The above factors that affect soil moisture variability will also affect data assimilation efficiency,
113 and it is too complicated to comprehensively consider their influences.

114 In addition, biased data (data with systematic measurement errors) at a certain scale may
115 impede the successful utilization of data at other scales and lead to deterioration of data assimilation.
116 Existing studies with respect to bias estimation and correction in DA can be seen in Dee (2005),
117 Pauwels et al. (2013) and Ridler et al. (2014), etc. These studies, although based on different
118 assumptions, present very insightful and effective approaches that can be applied in DA. As there is
119 certain limitations for different methods, how to eliminate the data biases in DA is still worth study.

120 This paper is an attempt to conduct state-only or dual state-parameter estimation in subsurface

121 hydrology using multi-scale soil moisture observations. Under the ensemble Kalman filter (EnKF)
122 framework, synthetic soil moisture observations from three support scales 600 m, 3000 m and 9000
123 m are assimilated into a fully coupled distributed unsaturated-saturated water flow model (Zhu et
124 al., 2012) with a resolution of 600 m. We will investigate the influences of measurement scale
125 (horizontal support), soil spatial heterogeneity (in terms of parameter correlation length), conflicting
126 soil moisture data from two scales (caused by different precipitation/irrigation time series) and
127 systematic measurement errors on retrieving soil moisture profiles and estimating saturated soil
128 hydraulic conductivities.

129 **2. Methodology**

130 2.1. Fully coupled unsaturated-saturated water flow model

131 A fully coupled unsaturated-saturated water flow model developed by Zhu et al. (2012) is
132 selected to simulate the soil water and groundwater flow. The validity and efficiency of the model
133 have been demonstrated by comparing its simulation results with those of Hydrus1D, the Variably-
134 Saturated Two-Dimensional Water Flow and Transport Model (SWMS2D), the 3D model
135 HydroGeoSphere, and FEFLOW. Moreover, by applying to a practical irrigation district, the
136 Yonglian Irrigation District, Inner Mongolia, China, the model reveals its applicability in simulating
137 large-scale unsaturated-saturated water flow.

138 According to the experimental findings which demonstrate that the vertical fluxes are often
139 dominant over the lateral fluxes in the unsaturated zone at the hillslope scale (Sherlock et al., 2002),
140 it is usually considered reasonable in large-scale simulations to care only about the vertical flow and
141 neglect the horizontal flux in the vadose zone (Chen et al., 1994). Therefore, the heavy

142 computational burden of numerically modeling large-scale water flow can be reduced by
 143 simplifying the three-dimensional (3D) Richards' equation in the unsaturated zone to the 1D
 144 equation. In the model, the whole unsaturated-saturated domain is horizontally divided into several
 145 sub-areas according to the spatially distributed inputs such as soil type, vegetation, meteorological
 146 condition and topography. For each sub-area, a 1D vertical soil column is used to represent the
 147 averaged unsaturated flow in that area. It is also assumed that only vertical fluxes exist between the
 148 unsaturated zone and the saturated zone. Then, the 1D Richards' equation of each column is coupled
 149 with the 3D groundwater flow equation through the vertical flux from the unsaturated zone to the
 150 groundwater table.

151 The Richards' equation is used to describe the simplified vertical flow through the unsaturated
 152 zone (Vogel et al, 1996),

$$153 \quad \frac{\partial \theta}{\partial t} = \frac{\partial}{\partial z} \left(K_h \left(\frac{\partial h}{\partial z} - 1 \right) \right) - S \quad (1)$$

154 where θ is the volumetric water content; h is the pressure head; t is time; K_h is the unsaturated
 155 soil hydraulic conductivity, which varies with the pressure head; z is the vertical coordinate and S is
 156 the source/sink terms.

157 For the saturated zone, the 3D groundwater flow equation is applied,

$$158 \quad \mu_1 \frac{\partial H}{\partial t} = \frac{\partial}{\partial x_j} \left(K_s \frac{\partial H}{\partial x_i} \right) - S \quad (2)$$

159 where μ_1 is the elastic storage coefficient; H is the total water head; t is time; x_i and x_j are the spatial
 160 coordinates ($x_i, x_j = x, y, z$); K_s is the saturated hydraulic conductivity. This 3D groundwater flow
 161 equation is simplified using the concept of Vertical/Horizontal Splitting (Lardner and Cekirge, 1988),
 162 and then solved using water balance analysis method.

163 The vertical flux between the unsaturated zone and the groundwater table is expressed by the

164 head gradient between the adjacent nodes in the unsaturated and saturated zones. The head matrix
165 of the unsaturated and saturated zones are put together to form the unified global matrix, some of
166 whose elements should be revised according to the water-balance-based coupling between the two
167 zones. After solving the global head matrix, soil moistures in the unsaturated zone are acquired
168 using the famous van Genuchten model. Detailed descriptions of the model construction can be seen
169 in Zhu et al. (2012).

170 We select this model because on one hand, it is a distributed subsurface flow model which is
171 suitable for investigating the impacts of horizontal observation scales in data assimilation practices,
172 and on the other hand, it can simultaneously give detailed vertical soil moisture profiles for different
173 sub-areas.

174 2.2. Ensemble Kalman Filter (EnKF)

175 Data assimilation (DA) is the process that combines modelling results and observations to
176 generate the optimal states. The traditional standard Kalman filter is a widely applied sequential
177 data assimilation approach suitable for small and linear systems with Gaussian error statistics. When
178 implementing DA for large and nonlinear problems, some variants of the standard Kalman filter are
179 believed to be more capable. The ensemble Kalman filter (EnKF), first proposed by Evensen (1994),
180 is a Monte Carlo variant of the standard Kalman filter, and has proved highly applicable in
181 complicated nonlinear hydrological problems (Komma et al., 2008; Pathiraja et al., 2016; Reichle
182 et al., 2002; Shi et al., 2015; Song et al., 2014; Xie and Zhang, 2010; Xu and Gómez-Hernández,
183 2016). Different from the standard Kalman filter's explicit computation of the prior covariance
184 matrix, the EnKF uses an ensemble of model realizations to approximate the covariance of the state
185 vector.

186 In this study, the profile pressure head and soil moisture of the 1D soil columns are to be
 187 calibrated. The augmented state vector S_k that will be updated at time step k is,

$$188 \quad S_k = (m_k^T, h_k^T, \theta_k^T)^T \quad (3)$$

189 where m_k is the parameter vector, h_k and θ_k are the variable (pressure head and soil moisture)
 190 vectors. The dimension of the state vector is $N_s = N_m + N_h + N_\theta$, where N_m is the number of
 191 unknown parameters of all the soil columns; N_h or N_θ is the total number of one dimensional
 192 nodes of the soil columns. In this study, we choose the simultaneous updating of h_k and θ_k . The
 193 updated soil moisture θ_k is used for result analysis, and the updated pressure head h_k are inserted
 194 back in the flow model because the pressure head is selected as the main variable to be directly
 195 solved in the model.

196 Whenever the observations are available, the state vector of each ensemble member i should
 197 be updated via,

$$198 \quad S_{k,i}^a = S_{k,i}^b + K_k (d_{obsk,i} - H_k S_{k,i}^b) \quad (4)$$

199 where $S_{k,i}^b$ and $S_{k,i}^a$ denote the state vectors before and after assimilation, respectively; H_k is the
 200 observation operator mapping the model states to the observation space $H_k S_{k,i}^b$, which in other
 201 words, is the observation prediction. Let d_{obsk} denote the observation with a dimension of N_d at
 202 time step k , then for each realization i the observation vector is,

$$203 \quad d_{obsk,i} = d_{obsk} + \varepsilon_{k,i} \quad (5)$$

204 where $\varepsilon_{k,i}$ is the independent white noise of the observation, which varies among realizations
 205 (Burgers et al., 1998). Serving as a weighting factor between model predictions and observations,
 206 the Kalman gain K_k is calculated by,

$$207 \quad K_k = C_k^b H_k^T (H_k C_k^b H_k^T + R_k)^{-1} \quad (6)$$

208 where R_k is the error covariance matrix of the observations at time step k ; C_k^b is the prior error
 209 covariance matrix of the state vector and can be approximated by,

$$210 \quad C_k^b \approx \frac{1}{N_e-1} \sum_{i=1}^{N_e} [(S_{k,i}^b - \overline{S_k^b})(S_{k,i}^b - \overline{S_k^b})^T] \quad (7)$$

$$211 \quad \overline{S_k^b} \approx \frac{1}{N_e} \sum_{i=1}^{N_e} S_{k,i}^b \quad (8)$$

212 where N_e is the ensemble size; $\overline{S_k^b}$ is the ensemble mean of the state vector before assimilation.

213 2.3. Method of assimilating multi-scale soil moisture observations

214 Recalling section 2.2, it can be found that the observation operator H_k and the covariance
 215 matrix C_k always appear together as the product $C_k^b H_k^T$ or $H_k C_k^b H_k^T$ in the updating step. If the
 216 observational variables are just part of the state variables to be updated, H_k will be a $N_d \times N_s$
 217 matrix with an element of 1 where there is an observation prediction and 0 where there isn't. Under
 218 this condition, $C_k^b H_k^T$ and $H_k C_k^b H_k^T$ can actually be obtained by directly selecting several lines
 219 from C_k instead of calculating the whole of it, therefore the computational burden can be greatly
 220 reduced (Chen and Zhang, 2006). However, in our study the multi-scale soil moistures are not the
 221 direct state variables to be solved in the governing equations of the model, thus the whole state error
 222 covariance matrix C_k is supposed to be calculated and additional handling of H_k , $H_k C_k^b H_k^T$, as
 223 well as $C_k^b H_k^T$ is needed. We avoid this by augmenting the state vector S_k with the multi-scale
 224 observation d_k , which can be constructed from the direct model state variables using a ‘‘sub-model’’.
 225 A sub-model herein refers to the method and process used before data assimilation to transform the
 226 direct model variables to the predicted measurements when the direct model variables are not
 227 observable. The augmented state vector will then become,

$$228 \quad S_k = (m_k^T, h_k^T, \theta_k^T, d_k^T)^T \quad (9)$$

229 where d_k is the constructed model prediction of the multi-scale observation d_{obsk} . Thus, the

230 elements of H are still 1s and 0s, and the convenience as stated in Chen and Zhang (2006) is
231 retained. Note that by using different sub-models, different indirect model predictions can be
232 constructed according to their relationships with direct model predictions. Another advantage of the
233 augmented form of S_k is that data from two or more scales and of different types can be
234 assimilated simultaneously.

235 In our synthetic study, coarse-scale soil moisture data is constructed by aggregating several
236 finer-scale soil moisture data. The Area-Weighted-Average method is adopted to generate the
237 aggregated coarse-scale soil moisture with the following expression,

$$238 \quad ASM = \frac{\sum_i^n A_i \theta_i}{\sum_i^n A_i} \quad (10)$$

239 where n is the number of model grids within a same parent coarse observation grid; A_i is the area
240 of a finer grid, that is, the area of a horizontal sub-area of the modeling domain; θ_i is soil moisture
241 of a finer grid; ASM is the aggregated coarse-scale soil moisture. Note that the construction of
242 area-averaged soil moisture by Eq. (10) is only for generating synthetic observations (in the
243 reference modeling) and observation predictions (in the uncertain modeling) to drive the data
244 assimilation of soil water flow in our synthetic study, in other cases the weights of finer grids in the
245 aggregation of model results to coarse-scale grids do not necessarily depend on the area of finer
246 grids.

247 2.4. Method of treating biased data—difference information assimilation method

248 In order to deal with the possible systematic measurement errors, we present a very simple and
249 easy to use method based on EnKF, which is termed as “difference information assimilation”. The
250 term difference information means the difference between observations, whether temporally or
251 spatially. In our present study, only the spatial difference is involved. Assume that at a certain time

252 point, N observational grids are measured by the same sensor and that these N measurements
 253 correspond to the following truth vector:

$$254 \quad d_t = (d_t^1, d_t^2, \dots, d_t^N)^T \quad (11)$$

255 where the superscript 1, 2, and N denote different physical measurement locations. If the systematic
 256 measurement error δ is failed to be eliminated, the original observation vector can be expressed as:

$$257 \quad d_{obs} = (d_{obs}^1, d_{obs}^2, \dots, d_{obs}^N)^T = (d_t^1 + \delta + \varepsilon^1, d_t^2 + \delta + \varepsilon^2, \dots, d_t^N + \delta + \varepsilon^N)^T \quad (12)$$

258 where ε^i ($i=1, 2, \dots, N$) is random error. If this d_{obs} is directly assimilated, severe damage may
 259 be caused. Therefor the observation vector is transformed to such a form:

$$260 \quad \widetilde{d_{obs}} = (d_{obs}^1 - d_{obs}^2, d_{obs}^2 - d_{obs}^3, \dots, d_{obs}^{N-1} - d_{obs}^N, d_{obs}^N - d_{obs}^1)^T \quad (13)$$

$$261 \quad \widetilde{d_{obs}} = (d_t^1 - d_t^2 + \varepsilon^1 - \varepsilon^2, d_t^2 - d_t^3 + \varepsilon^2 - \varepsilon^3, \dots, d_t^N - d_t^1 + \varepsilon^N - \varepsilon^1)^T \quad (14)$$

$$262 \quad \widetilde{d_{obs}} = (\widetilde{d_{obs}^1}, \widetilde{d_{obs}^2}, \dots, \widetilde{d_{obs}^N})^T \quad (15)$$

263 where $\widetilde{d_{obs}^i}$ is the i th reconstructed observational data, representing the information difference
 264 between d_{obs}^i and d_{obs}^{i+1} . Note that if the random error ε^i of the original observations obeys a
 265 normal distribution $N(0, \sigma^2)$, and different observations are independent, then the random error of
 266 the constructed observational data $\widetilde{d_{obs}^i}$ will also obey a normal distribution, but the variance will
 267 be $2\sigma^2$.

268 The difference information is assimilated into the physical model using the form of augmented
 269 state vector described in Section 2.3, and can be jointly assimilated with other observational data
 270 with different scales or types. More exactly, the observation differences will be included in d_k of
 271 formula (9), and the model states will be updated not based on the original observations but on the
 272 observation differences.

273

274 3. Numerical experiments

275 Synthetic experiments are designed to explore the value of multi-scale near-surface (0~5 cm)
276 soil moisture observations in state-parameter estimation. A reference modeling or “true run” is
277 performed firstly, in which parameters and state variables are seen as “true” values. The EnKF runs
278 are then conducted for the same time period using wrong soil hydraulic parameters. Initial and
279 boundary conditions of the EnKF runs and the “true run” are set to be identical, as this study only
280 focuses on parameter errors. The EnKF runs assimilate soil moisture observations draw from the
281 reference modeling to compensate for errors arising from wrong parameters. In addition, the open-
282 loop run without assimilating any observational data and with just the same configurations as the
283 EnKF runs is performed in ensemble mode for comparison.

284 3.1 Flow domain description and boundary conditions

285 A $9000 \times 9000 \times 3$ m cuboid domain with a number of 225 600×600 m sub-areas is created. Soil
286 materials in the vertical direction are set to be uniform for simplification, since only the horizontal
287 scale is the target of our study. The 1D vertical soil columns are divided into 31 elements with 5 cm
288 thickness for the top two elements near soil surface and 10 cm thickness for the rest. The soil type
289 of all sub-areas in the reference modeling is selected as sandy loam from Carsel and Parrish (1988).
290 Soil parameters are as follows: $\alpha = 7.5 \text{ m}^{-1}$, $n = 1.89$, $\theta_r = 0.065$, $\theta_s = 0.41$, except the
291 saturated soil hydraulic conductivity K_s , which varies among sub-areas and will be specified in
292 Section 3.3. Initial total heads of all the simulation domain are -210 cm. By setting a constant water
293 table of 210 cm below soil surface, the number of unsaturated nodes will not change during the
294 whole simulation period and no water flux exists between horizontal sub-areas. Fig. 1 shows the

295 daily-averaged time series of precipitation and potential evaporation, in which (a) and (c) are used
296 as the upper boundary conditions for all the cases unless otherwise specified. The unsaturated-
297 saturated flow in this study is simulated with a time step of 0.01 days.

298 *[Fig. 1]*

299 3.2 Observations

300 In this synthetic study, near-surface soil moisture observations from three horizontal scales 600
301 m, 3000 m and 9000 m, denoted by θ_{600} , θ_{3000} and θ_{9000} are used. The 600 m soil moisture data
302 can correspond to some sensing instrument with a footprint of intermediate scale, for example, the
303 cosmic-ray soil moisture probe (Zreda et al., 2008; Zreda et al., 2012). The 9000 m soil moisture
304 data can correspond to the SMAP mission (Das et al., 2011; Entekhabi et al., 2010). The 3000 m
305 measurement scale may represent the future 3000 m soil moisture product from SMAP or other
306 missions although not mature at present. The 600 m-scale near-surface soil moisture observations
307 are drawn from the linear mean of the top two nodes of the vertical soil columns in the reference
308 modeling, representing an observation depth of 5 cm. The 3000 m and 9000 m-scale near-surface
309 soil moisture observations are generated by Equation (10). Soil moisture observations from the three
310 scales are all assumed to be unbiased and only suffer a random measurement error of $0.04 \text{ m}^3/\text{m}^3$
311 unless otherwise stated. The generation of these soil moisture data is under simplified conditions,
312 since in reality the sensing depths of instruments will change with soil moisture content and coarse-
313 scale observations are not necessarily the area-average of finer-scale observations. This
314 simplification will not affect the main purpose of our study.

315 3.3 Experimental setup and data assimilation scenarios

316 The parameter K_s (m/day) is taken as the unknown factor. There are in total 225 parameters to
 317 be estimated for the whole study area. It is assumed that the logarithmic hydraulic conductivity field
 318 $Y(x) = \ln K_s(x)$ obeys a normal distribution and is second-order stationary with a two-
 319 dimensional covariance function defined by a separable exponential form:

$$320 \quad C_Y(\mathbf{h}) = \sigma_Y^2 \exp\left(-\frac{|h_x|}{\lambda_x} - \frac{|h_y|}{\lambda_y}\right) = \sigma_Y^2 \exp\left(-\frac{|x_1-x_2|}{\lambda_x} - \frac{|y_1-y_2|}{\lambda_y}\right) \quad (16)$$

321 where (x_1, y_1) and (x_2, y_2) are the 2D coordinates, σ_Y^2 is the variance, λ_x and λ_y are the
 322 correlation lengths in x and y directions. The prior mean and variance of the logarithmic hydraulic
 323 conductivity field are selected to be 0.5 and 1. The correlation lengths λ_x and λ_y are specified in
 324 Table 1, considering different soil spatial heterogeneities. Initial realizations of the logarithmic
 325 hydraulic conductivity field are generated using the above statistics. The reference field is given by
 326 randomly selecting a realization from realizations generated using a mean value of -0.5 and the same
 327 variance and correlation lengths as the initial field of the EnKF system. The model structural errors
 328 are ignored in this study since the same model is applied in the reference modeling and the EnKF
 329 runs. An ensemble size of 200 is selected. The total simulation time is 80 days, and the assimilation
 330 frequency is once a day.

331 Concerning the measurement scale (horizontal support), soil spatial heterogeneity, conflicting
 332 soil moisture data from two scales and systematic measurement errors, four scenarios are considered.

333 **Scenario 1**

334 Under a given background condition (correlation length of the $\ln K_s$ field is 9000 m), soil moisture
 335 observations from different scales are available, the data value of these soil moisture observations
 336 need to be accessed. Two sub-scenarios are analyzed, the first is updating state variables only, while
 337 the unknown parameters are not cared, the second is simultaneously updating unknown parameters

338 and state variables.

339 **Scenario 2**

340 For a given soil moisture product, data assimilation efficiency under different background
341 conditions needs to be accessed. In this study, the background soil heterogeneity, in terms of the
342 spatial correlation length of the $\ln K_s$ field is considered.

343 **Scenario 3**

344 Under a given background condition, multi-scale soil moisture observations with contrasting
345 information are available, the assimilation results need to be compared. Finer-scale data assimilation
346 can be driven by different coarse-scale observations, which may provide contrasting soil moisture
347 information with completely different temporal trends. Intuitively, detailed spatial soil moisture
348 features can be better captured by finer-scale soil moisture data. However, due to the commonly
349 existing spatial heterogeneity of soil properties, precipitation or evapotranspiration, etc., soil
350 moisture on a particular area may not be represented by the observation of a given scale. It is not
351 clear that which data scale is optimal if the scale of study areas does not match with the observation
352 scales.

353 **Scenario 4**

354 Under a given background condition, soil moisture observations from two scales are available,
355 but one data has systematic errors, and the other is unbiased with only random errors.

356 In corresponding to the four scenarios, a series of experiments are conducted, the detailed
357 specifications of which are listed in Table 1, and described in Section 4. It should be mentioned that
358 the sources of uncertainty in a hydrological modeling are not limited to the soil hydraulic
359 conductivity only, and other factors such as the meteorological input, land use type, topography and

360 the van Genuchten parameters, etc. can also result in great uncertainty of the model states. As the
361 main purpose of this study is to explore the idea and method of assimilating multi-scale soil moisture
362 observations, we reasonably select the soil hydraulic conductivity as the only unknown factor to
363 simplify the research. Sensitivity of the value of multi-scale soil moisture observations to different
364 factors mentioned above will be the topic of a future study, using the idea and method presented in
365 the current study.

366 *[Table 1]*

367 3.4 Performance assessment

368 To evaluate the data assimilation effectiveness, root mean square error (RMSE) relative to the
369 “true run” are computed based on the ensemble mean values of the unknown parameters and state
370 variables:

$$371 \text{RMSE} = \sqrt{\frac{1}{N} \sum_{i=1}^N [E(x_i) - x_i^{true}]^2} \quad (17)$$

372 where N is the number of nodes or the number of unknown parameters, $E(x_i)$ is the ensemble
373 mean value of the i th state variable or parameter, x_i^{true} is the synthetic “true value” in the reference
374 modeling. Because the saturated soil moisture content θ_s is treated as a known and correct
375 parameter, the focus should be on the unsaturated vertical nodes. Unless otherwise stated, N is $22 \times$
376 $225 = 4950$ when calculating the RMSE of profile soil moistures for the whole simulation domain,
377 where 22 is the number of unsaturated vertical nodes in each sub-area and 225 is the number of sub-
378 areas. N is 225 when calculating the RMSE of unknown parameters. If only shallow layer, say 0~50
379 cm soil moistures are cared, then N will be $7 \times 225 = 1575$. If the soil moisture RMSE of certain
380 sub-areas is cared, then N will equal the total number of unsaturated or cared vertical nodes of these
381 sub-areas.

382 **4. Results and discussion**

383 4.1 Dual state-parameter estimation using soil moisture observations from different scales

384 In Case 1~3, near-surface (0~5 cm) soil moisture observations from three footprints (600 m,
385 3000 m and 9000 m) are assimilated into the same uncertain modeling, respectively. Both the
386 saturated soil hydraulic conductivities and state variables are updated. The reference $\ln K_s$ field, the
387 ensemble mean $\ln K_s$ field of the initial realizations and the estimated ensemble mean $\ln K_s$ fields
388 (at the end of the simulation period) are shown in Fig. 2. The 225 estimated ensemble mean values
389 of $\ln K_s$ versus their reference values at day 1, 10, 50 and 80 are plotted in Fig. 3.

390 From Fig. 2 and 3 it can be seen that the initial ensemble mean $\ln K_s$ field does not show any
391 spatial tendency, compared with the reference field. At the end of the simulation period, the $\ln K_s$
392 field confined by the 600 m-scale soil moisture data is almost the same as the reference field. Major
393 features of the reference $\ln K_s$ field can also be captured by the 3000 m-scale data. When the
394 observation scale rises to 9000 m, the capability to recover the 600 m-scale $\ln K_s$ field decreases
395 dramatically (Fig. 2). Generally, the estimated $\ln K_s$ values using finer-scale soil moisture data
396 approach the reference values more rapidly and accurately (Fig. 3). In Fig. 3, the $\ln K_s$ estimates
397 from coarser-scale soil moisture data are more concentrated with respect to their reference
398 counterparts, indicating that the estimated $\ln K_s$ spatial variance is underestimated by assimilating
399 coarse-scale data, which can also be seen in Fig. 2. Note that the reference $\ln K_s$ field in Case 1~3
400 has a spatial mean and a spatial standard deviation of -0.225 and 0.737. While the 9000 m-scale soil
401 moisture data can drive the spatial mean of the $\ln K_s$ field close to that of the reference $\ln K_s$ field
402 (from the initial value 0.504 to the final -0.147), it cannot recover the spatial variance (from the

403 initial spatial standard deviation 0.004 to the final 0.078). In conclusion, it is difficult to use coarse-
404 scale soil moisture data to capture the finer-scale spatial heterogeneity of soil property.

405 *[Fig. 2]*

406 *[Fig. 3]*

407 The temporal evolution of RMSEs of ln Ks and profile soil moisture for Case 1~3 and the
408 open-loop run are plotted in Fig. 4. Note that at beginning profile soil moistures of all the cases are
409 set to be the same as that of the reference modeling and during the early time period precipitation
410 haven't yet infiltrated into deeper soil. It's easy to see that soil moisture observations from all the
411 three scales have positive effects on reducing profile soil moisture RMSE, but with the increase of
412 observation scale, the efficiency decreases obviously. Improvements for profile soil moisture are in
413 accordance with improvements for parameters. Detailed soil moisture profiles of a representative
414 sub-area (Sub-area 183) at the end of the simulation time are plotted in Fig. 5 (a), including the
415 reference modeling, the open-loop run and the EnKF runs.

416 *[Fig. 4]*

417 *[Fig. 5]*

418 4.2 Soil moisture profile retrieval without updating unknown parameters using soil moisture
419 observations from different scales

420 As stated by Moradkhani et al. (2005) and Xie and Zhang (2010), in many data assimilation
421 practices only dynamic state variables are updated while parameters are not. In Case 4~6 of this
422 study, the saturated soil hydraulic conductivity is not updated, and other settings are the same as
423 those of Case 1~3. The 0~200 cm and 0~50 cm profile soil moisture RMSEs for Case 4~6 and the
424 open-loop run are shown in Fig. 6 (a) and (b), respectively. As the initial profile soil moistures are

425 set to be correct, with the infiltration of precipitation under wrong soil hydraulic conductivity fields,
426 soil moisture RMSEs all gradually increase with time at the early stage. From Fig. 6 (a), at the early
427 period (about 0~10 days) when precipitation has not yet infiltrate into deeper soil, near-surface soil
428 moisture data from all the three scales are found to improve profile soil moisture estimation
429 compared with the open-loop run, and finer-scale data is more efficient. However, the RMSE using
430 θ_{600} grows larger than that using θ_{3000} after about 10 days, and then larger than that using θ_{9000}
431 at day 16, and later it grows distinctly beyond the soil moisture RMSE of the open-loop run. The
432 RMSE using θ_{3000} also grows larger than that of the open-loop run. In contrast, for Case 6 using
433 θ_{9000} , there is always a slight drop of the RMSE from that of the open-loop run during the whole
434 simulation period. The above results tell that wrong hydraulic conductivity can lead to spurious soil
435 moisture correlations between surface and deep nodes of the soil profile, and therefore assimilating
436 near-surface soil moisture data can actually worsen soil moisture estimation.

437 *[Fig. 6]*

438 From Fig. 6 (b), it can be seen that at most assimilation steps, near-surface soil moisture data
439 can improve the 0~50 cm profile soil moisture, and generally improvement from finer-scale
440 observations is larger, except during day 12~40, when soil moisture RMSE using θ_{600} exhibits a
441 greater fluctuation. In the long run, for shallow-layer soil moisture estimation finer-scale data is
442 more efficient. Detailed soil moisture profiles (at the end of the simulation period) of a
443 representative soil column without updating the soil hydraulic conductivity fields is plotted in Fig.
444 5 (b), for comparison with Fig. 5 (a). Related studies can be found as for using surface soil moisture
445 data to modify deeper soil moisture profiles (Chen et al., 2011; Lievens et al., 2015; Walker et al.,
446 2001), among which Chen et al. (2011) reveal similar results with this Section.

447 Combining the results of Section 4.1 and 4.2, it can be concluded that finer-scale soil moisture
448 data have greater influence on data assimilation, under the premise that the observation grid is not
449 smaller than the modeling grid. It should be noted that the “greater influence” can be positive (Fig.
450 4), but it can also be negative (Fig. 6 (a)).

451 4.3 Data assimilation under different degrees of soil spatial heterogeneity in terms of soil hydraulic
452 conductivity

453 In Case 7, Case 3 and Case 8, soil moisture data from the 9000 m-scale covering a number of
454 225 model grids is used. The difference of the three cases lies in the background parameter
455 correlation length (see Table 1). We artificially select these three parameter correlation lengths to
456 make the comparison more distinct. The RMSE evolutions for $\ln K_s$ fields and profile soil moisture
457 are exhibited in Fig. 7. It can be seen that soil moisture data have no effect, slight positive effect,
458 and obvious positive effect on parameter estimation under a parameter correlation length of 1800
459 m, 9000 m and 60000 m, respectively. The RMSE evolution of profile soil moistures is in
460 accordance with that of $\ln K_s$ fields. The above results indicate that it’s hard to use the 9000-scale
461 data to improve the 600 m-scale state and parameter estimation with a strong spatial heterogeneity
462 of soil property. But when the spatial heterogeneity of soil property becomes weaker, the 9000-scale
463 data can provide rather valuable information for even the much finer 600 m-scale model grids.

464 The information gain from the 3000 m-scale soil moisture observation in respect of the spatial
465 heterogeneity of the parameter field is also tested (Cases 2, 9 and 10). Similar phenomenon is
466 observed (results not shown), except that the 3000 m-scale data is also useful when the spatial
467 correlation length of the $\ln K_s$ field is 1800 m. In conclusion, the value of coarse-scale soil moisture
468 observations for finer-scale state-parameter estimation greatly depends on the degree of background

469 soil spatial heterogeneity.

470 *[Fig. 7]*

471 4.4 Data assimilation using multi-scale soil moisture observations with contrasting temporal trends

472 In Cases 11~13, we mimic Scenario 3 in which the upper boundary of the simulation filed is
473 controlled by two different precipitation/irrigation strategies, which is demonstrated in Fig. 8. Most
474 of the sub-areas in Fig. 8 (shallow grey areas) still receive the precipitation series in Fig. 1 (a), while
475 20 sub-areas (dark grey areas) in the top left corner of the study domain receive a different
476 precipitation series in Fig. 1 (b). A 3000 m-scale soil moisture observation covering the top left 25
477 model grids and a 9000 m-scale observation covering all the domain are given. The correlation
478 length of the $\ln K_s$ field is 9000 m. Fig. 9 gives the temporal evolution of the 3000 m-scale and the
479 9000 m-scale soil moisture observations, as well as the near-surface soil moisture changes of Sub-
480 areas 61~65 in the reference modeling. It is obvious that the trend of 9000 m-scale soil moisture
481 observation is much more similar to those of Sub-areas 61~65, while the 3000 m-scale observation
482 exhibits a totally different temporal trend. For Sub-areas 61~65, it is natural to question which one
483 of the 9000 m-scale (Case 12) and the 3000 m-scale (Case 11) observations can provide better
484 estimation results, and whether simultaneously assimilation of these two data set can yield further
485 improvement (Case 13).

486 *[Fig. 8]*

487 *[Fig. 9]*

488 *[Fig. 10]*

489 The RMSE of $\ln K_s$ versus time as well as that of profile soil moisture for Sub-areas 61~65 are
490 demonstrated in Fig. 10. Results show that during the early period (about 0~9 days) the RMSE of

491 In Ks conditioned on the 9000 m-scale soil moisture data drops faster than that conditioned on the
492 3000 m-scale data, probably due to the similar temporal trend of the 9000 m-scale data with those
493 of Sub-areas 61~65. But in the long run, the temporally deviated 3000 m-scale data gives better
494 estimation, which might be attributed to the smaller scale-mismatch compared with the 9000 m-
495 scale data, and the horizontal correlation of the ln Ks field. Considering both a short and a relatively
496 long assimilation period, the simultaneously assimilation of 3000 m- and the 9000 m- scale
497 observations is advantageous, because the corresponding RMSE curve always keeps close to the
498 better one of the other two curves by the separate assimilation. The result of profile soil moisture
499 follow that of parameter estimation. In conclusion, the influences of both the scale-mismatch and
500 the contrast of observable information should be considered when assimilating multi-scale soil
501 moisture data.

502 In practice, the usefulness of soil moisture data from a certain scale depends on several factors,
503 including the spatial heterogeneity of soil properties, the spatial variation of precipitation or
504 evapotranspiration, the degree of scale-mismatch between observations and simulations, etc. To
505 judge the data value of multi-scale soil moisture data with contrasting information, it is not enough
506 to consider only one factor. Our results demonstrate that by updating spatially correlated soil
507 hydraulic parameters, deviated observations still contain considerably useful information to identify
508 finer-scale states and parameters. The limitation of this section is that the influencing factors
509 mentioned previously are not thoroughly considered. Taking a more systematic analysis of the data
510 value of multi-scale data with contrasting information in DA can be the subject of a separate study.

511 4.5 Data assimilation using soil moisture data with systematic measurement errors

512 In real-world problems, soil moisture observations are subjected to both random errors and

513 systematic errors. Systematic errors of observations should be removed before data are used.
514 However, sometimes elimination of systematic observation errors cannot be guaranteed because of
515 the complex error components.

516 In a virtual experiment we assume that the 600 m-scale soil moisture observation suffer a
517 systematic bias of $0.03 \text{ m}^3/\text{m}^3$ from the true value. The random error is still $0.04 \text{ m}^3/\text{m}^3$. This data is
518 assimilated with model results to test the impact of systematic observation errors on dual state-
519 parameter estimation through Case 14. In Case 15, the result of EnKF by simultaneously utilizing
520 the unbiased 3000 m-scale soil moisture data and the 600 m-scale data with a bias of $0.03 \text{ m}^3/\text{m}^3$, is
521 tested. Note that by applying the augmented form of the state vector stated in Section 2.3 (formula
522 (9)), data from different sources and of different types can be assimilated simultaneously. In Case
523 16, the 600 m-scale biased soil moisture data are assimilated using the difference information
524 method described in Section 2.4. Other settings of Case 14~16 are identical with those of Case 1~3.

525 *[Fig. 11]*

526 The RMSEs of $\ln K_s$ fields and profile soil moisture for Case 14~16 and Case 2 are plotted in
527 Fig. 11. It can be seen that the direct assimilation of biased 600 m-scale soil moisture observation
528 severely damages the estimate of $\ln K_s$ fields and profile soil moisture. Even when the unbiased
529 3000 m-scale data is integrated together, the assimilation result does not get better obviously,
530 indicating the decisive effect of the biased 600 m-scale observation over the unbiased 3000 m-scale
531 observation. The above results illustrate that directly assimilating soil moisture data with systematic
532 measurement errors can not only lead to deterioration of data assimilation but also impede the
533 successful utilization of data at other scales. By applying the difference information assimilation
534 method (Case 16), the 600 m-scale biased-data results in great improvement of parameter and soil

535 moisture estimation. The limitation of the method used here is that the systematic observational
536 errors are assumed to be constant at different spatial locations. Another limitation is that for unbiased
537 observational data with only random errors, part of the information content can be reduced by
538 assimilating the observation difference instead of the original data. The difference information
539 assimilation method can be classified as the bias-blind systems stated in Dee (2005), with the
540 observational data reprocessed before assimilation. Bias-aware assimilation methods, on the other
541 hand, is advantageous in that they can explicitly give online bias estimation (Pauwels et al., 2013;
542 Ridler et al., 2014) and can also take into consideration the forecast biases, but they are also based
543 on specific assumptions, for example, assumptions about the source and nature of the biases in the
544 system (Dee, 2005). The forecast bias in this study caused by wrong initial model parameters are
545 implicitly reduced by jointly update the unknown parameters with state variables. The observation
546 bias is implicitly eliminated by assimilating the difference information instead of the original
547 information. To explicitly estimate the forecast and observation biases falls outside the scope of this
548 study.

549 **5. Conclusions**

550 In this paper we present a multi-scale data assimilation scheme based on the EnKF method and
551 a distributed subsurface water flow model, focusing on unsaturated zone state-only or state-
552 parameter estimation with near-surface (0~5 cm) soil moisture observations. The value of near-
553 surface soil moisture data from three measurement scales, namely 600 m, 3000 m and 9000 m, on
554 reducing the 600 m-scale model errors are accessed (Scenario 1). Using the 9000 m and the 3000
555 m-scale soil moisture observations, the influence of soil spatial heterogeneity in terms of saturated

556 soil hydraulic conductivity on data assimilation efficiency is considered (Scenario 2). The results of
557 assimilating 3000 m-scale and 9000 m-scale soil moisture data which exhibit obviously different
558 temporal trends, are compared (Scenario 3). In addition, the severe damage of directly assimilating
559 soil moisture data with systematic measurement errors is demonstrated and a difference information
560 method based on the multi-scale EnKF scheme (Scenario 4) is proposed.

561 Results and conclusions are summarized as follows:

562 Coarse-scale soil moisture data also contain very useful information for finer-scale state and
563 parameter estimation with biased initial $\ln K_s$ fields, but with the increasing of measurement scales,
564 the data assimilation efficiency decreases a lot (RMSE of soil moisture increases from 0.002 using
565 600 m data to 0.012 using 9000 m data). From Case 1~3 (Section 4.1), it can be seen that the a soil
566 moisture observation scale of 3000 m still brings great improvements to the 600 m-scale state-
567 parameter estimation (RMSEs of $\ln K_s$ and soil moisture reduced to 0.373 and 0.007 from 1.035
568 and 0.014 of the open-loop run). The 9000 m-scale soil moisture data can drive the spatial mean of
569 the $\ln K_s$ field to the reference field, but it cannot recover the spatial variability. Soil heterogeneity
570 have great effects on the efficiency of data assimilation. When the correlation length of the $\ln K_s$
571 field increases from 1800 m to 9000 m and to 60000 m, notable improvement can be seen using the
572 9000 m-scale soil moisture data to estimate the 600 m-scale states and parameters.

573 In dual state-parameter estimation, the profile soil moisture estimation is in accordance with
574 the estimation of the $\ln K_s$ field. Without updating the $\ln K_s$ field, assimilation of near-surface soil
575 moisture data can lead to improvement for shallow soil moisture profiles and damage for deeper
576 (>50cm in this study) soil moisture profiles, and the smaller the measurement scale is, the larger the
577 influence will be, given that the measurement scale is not smaller than the model scale.

578 When data from different scales are available but with contrasting temporal trends, their
579 influences on data assimilation are subtle, and factors should be considered simultaneously. In
580 Section 4.4, compared with the 9000 m-scale soil moisture data, the 3000m-scale data exhibits a
581 more different temporal trend with the soil moisture temporal evolution of study areas, but the letter
582 still brings much greater improvements (RMSEs of ln Ks and soil moisture further reduced to 0.446
583 and 0.010 from 1.048 and 0.166) except during the early period (0~9days). Joint assimilation of
584 multi-scale soil moisture data with contrasting information is found to be advantageous but need to
585 be further investigated.

586 Given that the measurement scale is not smaller than the model scale, finer-scale data is more
587 efficiency on driving data assimilation, but should be used with caution. The direct assimilation of
588 the 600 m-scale soil moisture data with systematic measurement errors results in the deterioration
589 of data assimilation and also causes the failure of assimilating unbiased 3000 m-scale soil moisture
590 data. By applying a spatial difference information assimilation method, we successfully eliminate
591 the disadvantageous effect of the biased 600 m-scale observational data and prove that the multi-
592 scale EnKF data assimilation scheme is able to take full advantage of data, even with systematic
593 measurement errors.

594 Based on the results of this study, the general conclusion is that the EnKF approach is proved
595 to provide a promising framework to use multi-scale soil moisture data. The current study only
596 covers a few aspects in DA with multi-scale data, and should extended to consider unbiased initial
597 parameter ensemble, or/and other factors such as meteorological input, land use type, topography,
598 etc.

599

600 **Acknowledgement**

601 This study was supported by the Excellent Young Scientist Foundation of the National Natural
602 Science Foundation of China Grant 51522904 and the National Natural Science Foundation of
603 China Grant 51479144. The fifth author was supported in part through Guangxi Agricultural
604 Technology Transformation Fund Grant 14125004-4. MW was supported by the UK National
605 Centre for Earth Observation.

References:

606

607 Blöschl, G. and Sivapalan, M., 1995. Scale issues in hydrological modelling: A review.

608 Hydrological Processes, 9(3-4): 251-290.

609 Burgers, G., Jan Van Leeuwen, P. and Evensen, G., 1998. Analysis Scheme in the Ensemble Kalman

610 Filter. Monthly Weather Review, 126(6): 1719-1724.

611 Chen, F., Crow, W.T., Starks, P.J. and Moriasi, D.N., 2011. Improving hydrologic predictions of a

612 catchment model via assimilation of surface soil moisture. Advances in Water Resources, 34(4):

613 526-536.

614 Chen, Y. and Zhang, D., 2006. Data assimilation for transient flow in geologic formations via

615 ensemble Kalman filter. Advances in Water Resources, 29(8): 1107-1122.

616 Chen, Z., Govindaraju, R.S. and Kavvas, M.L., 1994. Spatial averaging of unsaturated flow

617 equations under infiltration conditions over areally heterogeneous fields. 1. Development of models.

618 Water Resources Research, 30(2): 523-533.

619 Clark, M.P. et al., 2008. Hydrological data assimilation with the ensemble Kalman filter: Use of

620 streamflow observations to update states in a distributed hydrological model. Advances in Water

621 Resources, 31(10): 1309-1324.

622 Crow, W.T. and Wood, E.F., 1999. Multi-scale dynamics of soil moisture variability observed

623 during SGP'97. Geophysical Research Letters, 26(23): 3485-3488.

624 Das, N.N., Entekhabi, D. and Njoku, E.G., 2011. An algorithm for merging SMAP radiometer and

625 radar data for high-resolution soil-moisture retrieval. IEEE Transactions on Geoscience and Remote

626 Sensing, 49(5): 1504-1512.

627 De Lannoy, G.J.M., Verhoest, N.E.C., Houser, P.R., Gish, T.J. and Van Meirvenne, M., 2006.

628 Spatial and temporal characteristics of soil moisture in an intensively monitored agricultural field
629 (OPE3). *Journal of Hydrology*, 331(3-4): 719-730.

630 Dee, D. P., 2005. Bias and data assimilation. *Q.J.R. Meteorol. Soc.*, 131: 3323–3343.
631 doi:10.1256/qj.05.137

632 Durand, M. and Margulis, S.A., 2007. Correcting first - order errors in snow water equivalent
633 estimates using a multifrequency, multiscale radiometric data assimilation scheme. *Journal of*
634 *Geophysical Research Atmospheres*, 112(D13): 3710-3711.

635 Entekhabi, D. et al., 2010. The soil moisture active passive (SMAP) mission. *Proceedings of the*
636 *IEEE*, 98(5): 704-716.

637 Evensen, G., 1994. Sequential data assimilation with a nonlinear quasi-geostrophic model using
638 Monte Carlo methods to forecast error statistics. *Journal of Geophysical Research Oceans*, 99(C5):
639 10143-10162.

640 Famiglietti, J.S. et al., 1999. Ground-based investigation of soil moisture variability within remote
641 sensing footprints during the Southern Great Plains 1997 (SGP97) Hydrology Experiment. *Water*
642 *Resources Research*, 35(6): 1839-1851.

643 Fang, B. and Lakshmi, V., 2014. Soil moisture at watershed scale: Remote sensing techniques.
644 *Journal of Hydrology*, 516(6): 258-272.

645 Gaur, N. and Mohanty, B.P., 2013. Evolution of physical controls for soil moisture in humid and
646 subhumid watersheds. *Water Resources Research*, 49(3): 1244-1258.

647 Houser, P.R. et al., 1998. Integration of soil moisture remote sensing and hydrologic modeling using
648 data assimilation. *Water Resources Research*, 34(12): 3405-3420.

649 Hu, Z., Chen, Y. and Islam, S., 1998. Multiscaling properties of soil moisture images and

650 decomposition of large- and small-scale features using wavelet transforms. *International Journal of*
651 *Remote Sensing*, 19(13):2451-2467.

652 Komma, J., Blöschl, G. and Reszler, C., 2008. Soil moisture updating by Ensemble Kalman Filtering
653 in real-time flood forecasting. *Journal of Hydrology*, 357(3-4): 228-242.

654 Korres, W., Reichenau, T.G. and Schneider, K., 2013. Patterns and scaling properties of surface soil
655 moisture in an agricultural landscape: An ecohydrological modeling study. *Journal of Hydrology*,
656 498: 89-102.

657 Korres, W. et al., 2015. Spatio-temporal soil moisture patterns – A meta-analysis using plot to
658 catchment scale data. *Journal of Hydrology*, 520: 326-341.

659 Koyama, C.N., Korres, W., Fiener, P. and Schneider, K., 2009. High-resolution soil moisture
660 estimation from ALOS PALSAR Fine Mode (Dual Polarization) data in agricultural areas. *EGU*
661 *General Assembly Conference Abstracts*, 11: 4980.

662 Koyama, C.N., Korres, W., Fiener, P. and Schneider, K., 2010. Variability of surface soil moisture
663 observed from multitemporal C-band synthetic aperture radar and field data. *Vadose Zone Journal*,
664 9(9): 1014--1024.

665 Lardner, R.W. and Cekirge, H.M., 1988. A new algorithm for three-dimensional tidal and storm
666 surge computations. *Applied mathematical modelling*, 12(5): 471-481.

667 Lievens, H. et al., 2015. SMOS soil moisture assimilation for improved hydrologic simulation in
668 the Murray Darling Basin, Australia. *Remote Sensing of Environment*, 168: 146-162.

669 Liu, Y. et al., 2012. Advancing data assimilation in operational hydrologic forecasting: progresses,
670 challenges, and emerging opportunities. *Hydrology and Earth System Sciences*, 16(10): 3863-3887.

671 Montzka, C., Pauwels, V.R., Franssen, H.J., Han, X. and Vereecken, H., 2012. Multivariate and

672 multiscale data assimilation in terrestrial systems: a review. *Sensors*, 12(12): 16291-16333.

673 Moradkhani, H., Sorooshian, S., Gupta, H.V. and Houser, P.R., 2005. Dual state–parameter
674 estimation of hydrological models using ensemble Kalman filter. *Advances in Water Resources*,
675 28(2): 135-147.

676 Moradkhani, H., Hsu, K., Gupta, H. and Sorooshian, S., 2005. Uncertainty assessment of hydrologic
677 model states and parameters: Sequential data assimilation using the particle filter. *Water Resources
678 Research*, 41(5):237-246.

679 Pathiraja, S., Marshall, L., Sharma, A. and Moradkhani, H., 2016. Hydrologic modeling in dynamic
680 catchments: A data assimilation approach. *Water Resources Research*, 52(5): 3350-3372.

681 Pauwels, V. R. N., De Lannoy, G. J. M., Hendricks Franssen, H.-J., and Vereecken, H., 2013.
682 Simultaneous estimation of model state variables and observation and forecast biases using a two-
683 stage hybrid Kalman filter. *Hydrol. Earth Syst. Sci.*, 17: 3499-3521.

684 Reichle, R.H., McLaughlin, D.B. and Entekhabi, D., 2002. Hydrologic Data Assimilation with the
685 Ensemble Kalman Filter. *Monthly Weather Review*, 130(1): 103-114.

686 Ridler, M.-E., H. Madsen, S. Stisen, S. Bircher, and R. Fensholt., 2014. Assimilation of SMOS-
687 derived soil moisture in a fully integrated hydrological and soil-vegetation-atmosphere transfer
688 model in Western Denmark. *Water Resour. Res.*, 50: 8962–8981.

689 Robinson, D.A. et al., 2008. Soil Moisture Measurement for Ecological and Hydrological
690 Watershed-Scale Observatories: A Review. *Vadose Zone Journal*, 7(1): 358.

691 Romano, N., 2014. Soil moisture at local scale: Measurements and simulations. *Journal of
692 Hydrology*, 516: 6-20.

693 Samuel, J., Coulibaly, P., Dumedah, G. and Moradkhani, H., 2014. Assessing model state and

694 forecasts variation in hydrologic data assimilation. *Journal of Hydrology*, 513: 127-141.

695 Sherlock, M.D., McDonnell, J.J., Curry, D.S. and Zumbuhl, A.T., 2002. Physical controls on septic
696 leachate movement in the vadose zone at the hillslope scale, Putnam County, New York, USA.
697 *Hydrological Processes*, 16(13): 2559-2575.

698 Shi, L., Zeng, L., Zhang, D., and Yang, J., 2012. Multiscale-finite-element-based ensemble Kalman
699 filter for large-scale groundwater flow. *Journal of hydrology*, 468: 22-34.

700 Shi, L., Song, X., Tong, J., Zhu, Y. and Zhang, Q., 2015. Impacts of different types of measurements
701 on estimating unsaturated flow parameters. *Journal of Hydrology*, 524: 549-561.

702 Song, X., Shi, L., Ye, M., Yang, J. and Navon, I.M., 2014. Numerical Comparison of Iterative
703 Ensemble Kalman Filters for Unsaturated Flow Inverse Modeling. *Vadose Zone Journal*, 13(2): 1-
704 12.

705 Susha Lekshmi, S.U., Singh, D. N., and Maryam Shojaei Baghini, 2014. A critical review of soil
706 moisture measurement. *Measurement*, 54: 92-105.

707 Vereecken, H. et al., 2008. On the value of soil moisture measurements in vadose zone hydrology:
708 A review. *Water Resources Research*, 44(4): 253-270.

709 Vogel, T., Huang, K., Zhang, R., van Genuchten, M.Th., 1996. The HYDRUS Code for Simulating
710 One-dimensional Water Flow, Solute Transport, and Heat Movement in Variably-saturated Media,
711 Version 5.0, Research Report No. 140. U.S. Salinity Laboratory Agricultural Research Service U.S.
712 Department of Agriculture Riverside, California.

713 Walker, J.P., Willgoose, G.R. and Kalma, J.D., 2001. One-dimensional soil moisture profile
714 retrieval by assimilation of near-surface observations: a comparison of retrieval algorithms.
715 *Advances in Water Resources*, 24(6): 631-650.

716 Weerts, A.H. and El Serafy, G.Y.H., 2006. Particle filtering and ensemble Kalman filtering for state
717 updating with hydrological conceptual rainfall-runoff models. *Water Resources Research*, 42(9):
718 123-154.

719 Western, A.W., Blöschl, G. and Grayson, R.B., 1998. Geostatistical characterisation of soil moisture
720 patterns in the Tarrawarra catchment. *Journal of Hydrology*, 205(1–2): 20-37.

721 Western, A.W. and Blöschl, G., 1999. On the spatial scaling of soil moisture. *Journal of Hydrology*,
722 217(3-4): 203-224.

723 Xie, X. and Zhang, D., 2010. Data assimilation for distributed hydrological catchment modeling via
724 ensemble Kalman filter. *Advances in Water Resources*, 33(6): 678-690.

725 Xu, T. and Gómez-Hernández, J.J., 2016. Joint identification of contaminant source location, initial
726 release time and initial solute concentration in an aquifer via ensemble Kalman filtering. *Water*
727 *Resources Research*, 52(8): 6587-6595.

728 Zhu, Y., Shi, L., Lin, L., Yang, J. and Ye, M., 2012. A fully coupled numerical modeling for regional
729 unsaturated–saturated water flow. *Journal of Hydrology*, 475: 188-203.

730 Zreda, M., Desilets, D., Ferré, T.P.A. and Scott, R.L., 2008. Measuring soil moisture content non-
731 invasively at intermediate spatial scale using cosmic-ray neutrons. *Geophysical research letters*,
732 35(21), L21402. <http://dx.doi.org/10.1029/2008GL035655>.

733 Zreda, M. et al., 2012. COSMOS: the COsmic-ray Soil Moisture Observing System. *Hydrology and*
734 *Earth System Sciences*, 16(11): 4079 - 4099.

735

736

737 **Figure and Table Captions**

738

739

740

741 **Fig. 1.** Time series of daily precipitation and potential evaporation, (a) and (c) are used in all the
742 cases; (b) is only used in Case 11~13 for Scenario 3.

743 **Fig. 2.** Illustration of the $\ln K_s$ fields in Scenario 1 (Case 1~3): (a) reference field; (b) ensemble
744 mean of the initial ensemble members; (c) ~ (e) estimated ensemble mean $\ln K_s$ fields at the end of
745 the simulation period by 600 m-, 3000 m- and 9000 m-scale soil moisture data, respectively.

746 **Fig. 3.** Estimated ensemble mean values of $\ln K_s$ by soil moisture data from 600 m-, 3000 m- and
747 9000 m- scales in Case 1~3 of Scenario 1. (a) ~ (d) Represent the results of day 1, 10, 50 and 80,
748 respectively. Results corresponding to different observation scales are denoted by different data tags.

749 **Fig. 4.** Temporal evolution of RMSEs for the $\ln K_s$ fields and profile soil moistures in Scenarios 1
750 (Case 1~3 and the open-loop run). Different lines represent results by soil moisture data from 600
751 m, 3000 m, and 9000 m scales, respectively.

752 **Fig. 5.** Soil moisture profiles of the representative sub-area for the reference modeling, the open-
753 loop run and the EnKF runs in Scenario 1 (Case 1~6 and the open-loop run): (a) parameters are
754 updated; (b) parameters are not updated.

755 **Fig. 6.** Temporal evolution of RMSEs for profile soil moistures in Case 4~6: (a) the whole
756 unsaturated zone; (b) 0~50 cm soil depth.

757 **Fig. 7.** Temporal evolution of RMSEs for the $\ln K_s$ fields and profile soil moisture in Scenario 2
758 (Case 3, 7 and 8), given different parameter correlation lengths λ .

759 **Fig. 8.** Illustration of the upper boundary conditions used in Case 11~13 of Scenario 3. Most of the
760 sub-areas (shallow grey areas) still receive the precipitation series in Fig. 1 (a), while 20 sub-areas
761 (dark grey areas) in the top left corner of the study domain receive a different precipitation series in
762 Fig. 1 (b). The locations of Sub-area 61~65 are labeled with the red Arabic numerals.

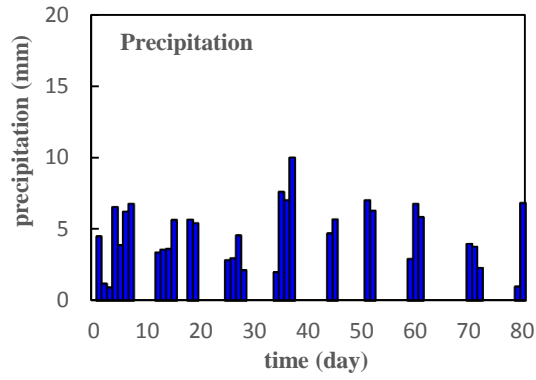
763 **Fig. 9.** Temporal trends of the 3000 m-scale (Case 11) and the 9000 m-scale (Case 12) soil moisture
764 data in comparison with the average soil moisture changes of Sub-areas 61~65 in Scenario 3.

765 **Fig. 10.** Temporal evolution of RMSEs for the $\ln K_s$ fields and profile soil moistures of Sub-areas
766 61~65 in Scenarios 3 (Case 11~13 and the open-loop run). Different lines represent results by soil
767 moisture data from a 3000 m- grid, a 9000 m- grid and the combined 3000 m- and 9000 m- grids,
768 respectively.

769 **Fig. 11.** Temporal evolutions of RMSEs for the $\ln K_s$ fields and profile soil moistures of Case 2, 14,
770 15 and 16, as well as the open loop run in Scenario 4.

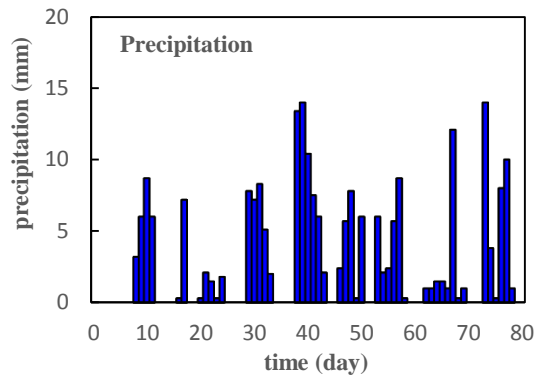
771 **Table 1** Specifications of all the cases
772

773 **Fig. 1.**



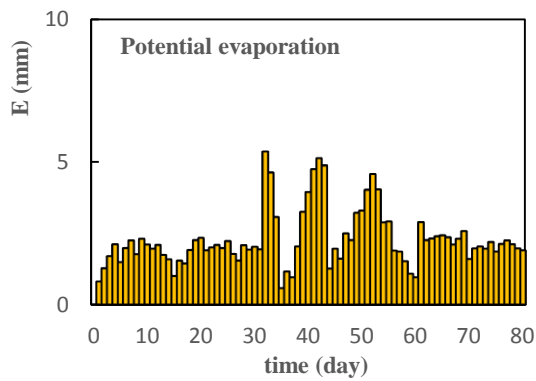
774

(a)



775

(b)



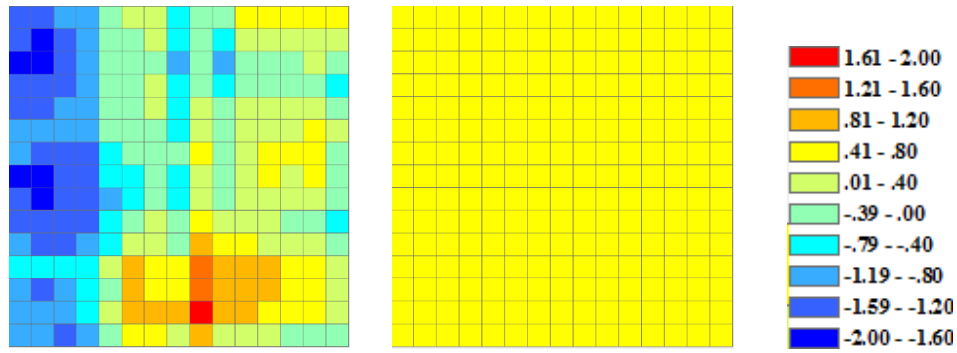
776

(c)

777 **Fig. 1.** Time series of daily precipitation and potential evaporation, (a) and (c) are used in all the

778 cases; (b) is only used in Case 11~13 for Scenario 3.

779 **Fig. 2.**



780 (a)

(b)

781 (c)

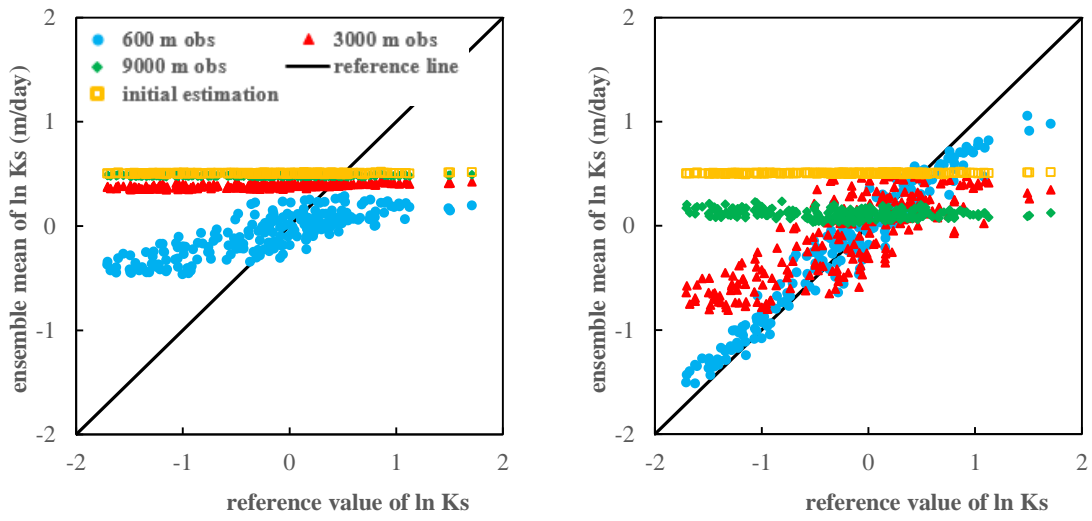
(d)

(e)

782 **Fig. 2.** Illustration of the ln Ks fields in Scenario 1 (Case 1~3): (a) reference filed; (b) ensemble
783 mean of the initial ensemble members; (c) ~ (e) estimated ensemble mean ln Ks fields at the end of
784 the simulation period by 600 m-, 3000 m- and 9000 m-scale soil moisture data, respectively.

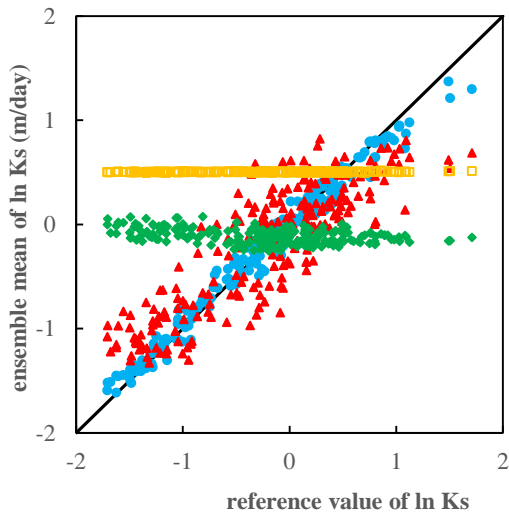
785

786 **Fig. 3.**

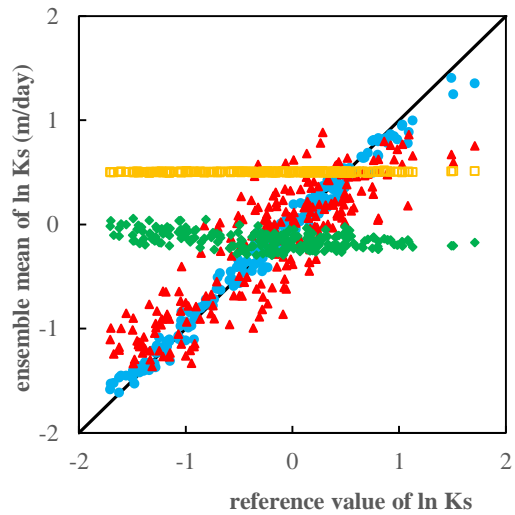


787

(a)

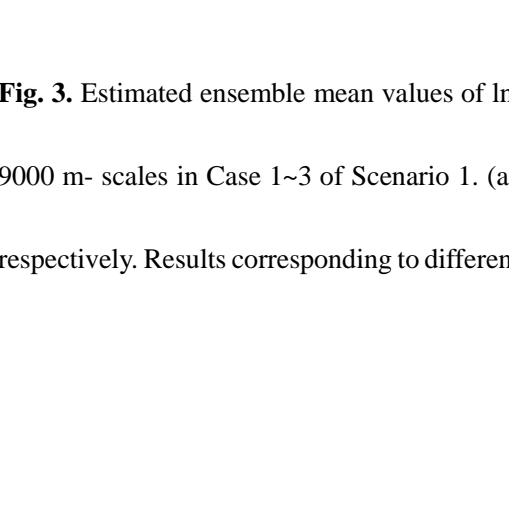


(b)

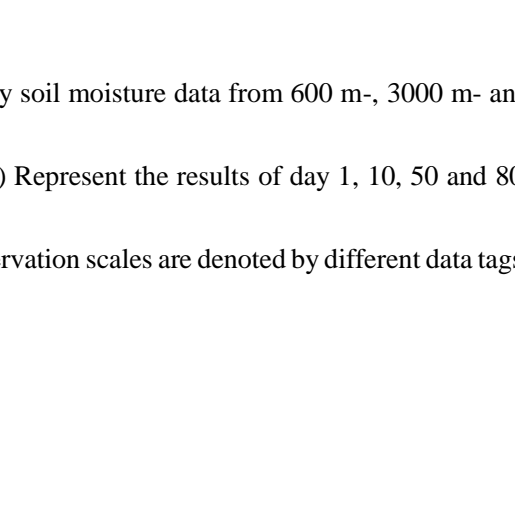


788

(c)



(d)



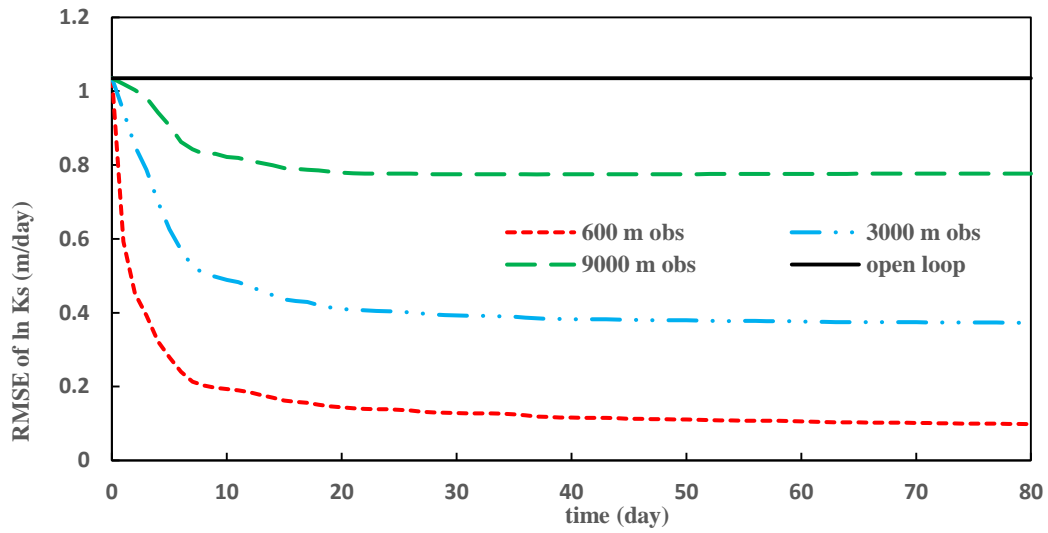
789 **Fig. 3.** Estimated ensemble mean values of ln Ks by soil moisture data from 600 m-, 3000 m- and

790 9000 m- scales in Case 1~3 of Scenario 1. (a) ~ (d) Represent the results of day 1, 10, 50 and 80,

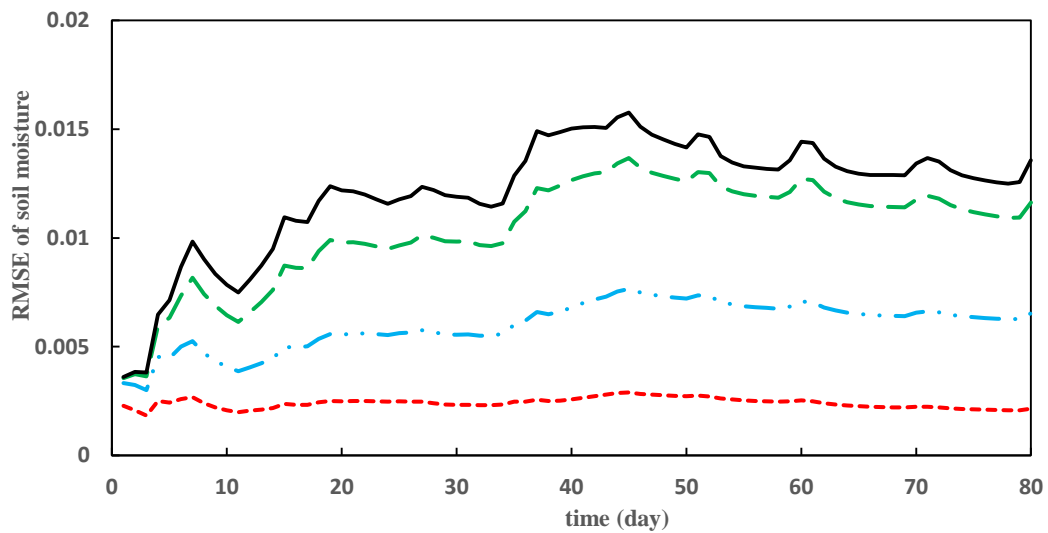
791 respectively. Results corresponding to different observation scales are denoted by different data tags.

792

793 **Fig. 4.**



794 (a)

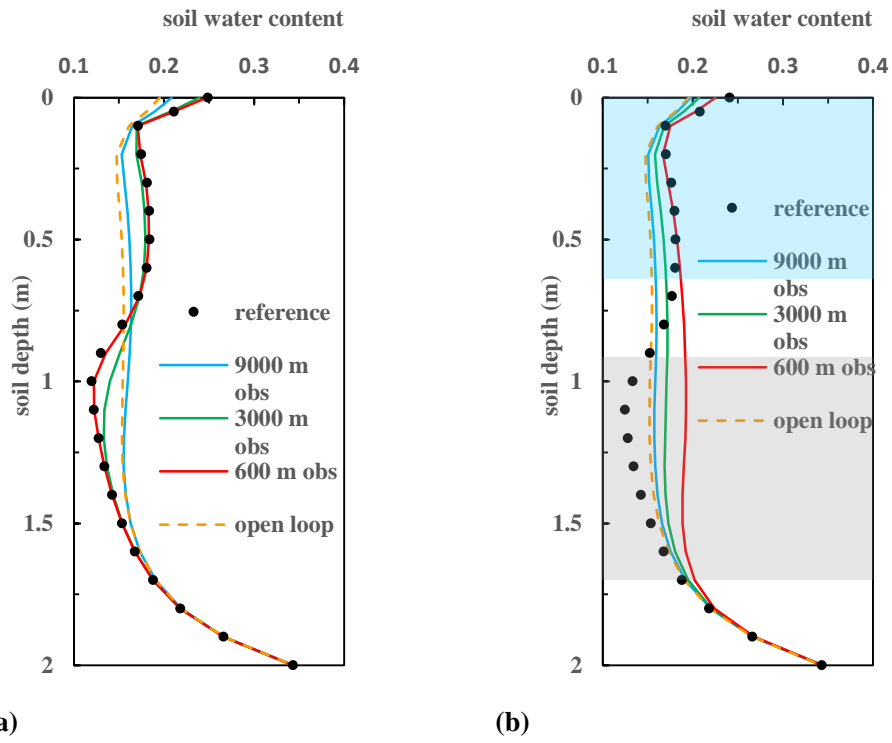


795 (b)

796 **Fig. 4.** Temporal evolution of RMSEs for the $\ln K_s$ fields and profile soil moistures in Scenarios 1
797 (Case 1~3 and the open-loop run). Different lines represent results by soil moisture data from 600
798 m, 3000 m, and 9000 m scales, respectively.

799

800 **Fig. 5.**



801

(a)

(b)

802 **Fig. 5.** Soil moisture profiles of the representative sub-area for the reference modeling, the open-
803 loop run and the EnKF runs in Scenario 1 (Case 1~6 and the open-loop run): (a) parameters are
804 updated; (b) parameters are not updated.

805

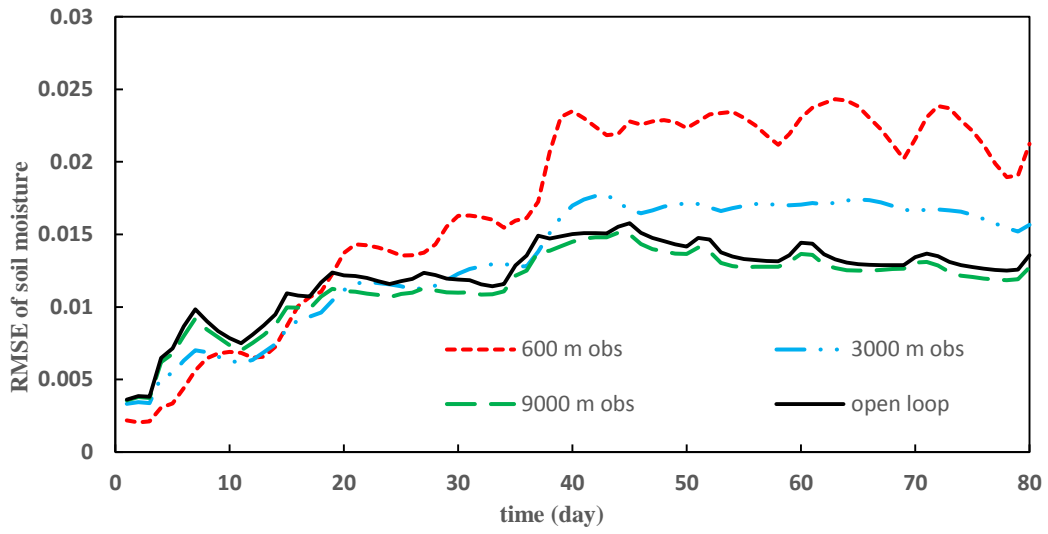
806

807

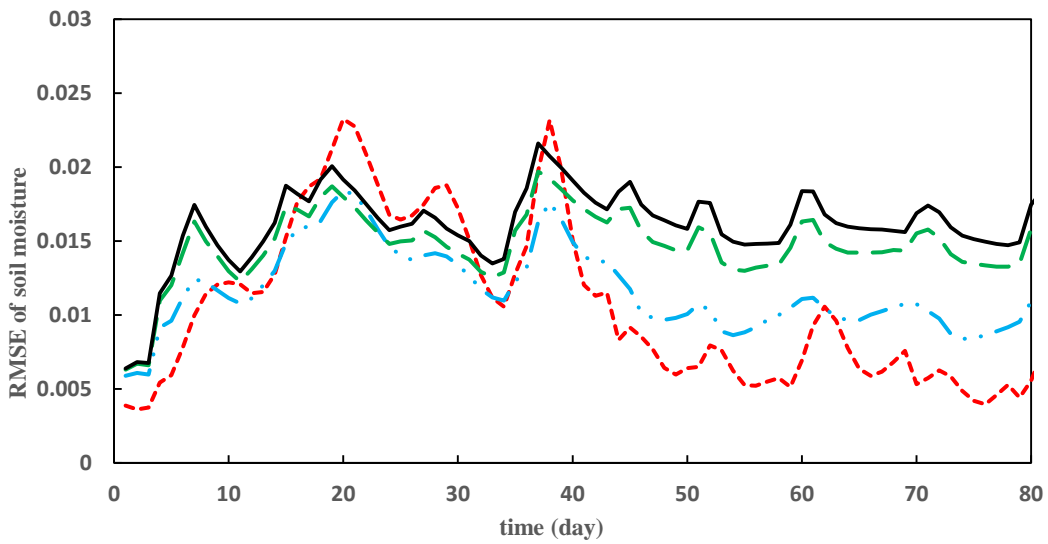
808

809

810 **Fig. 6.**



811 (a)



812 (b)

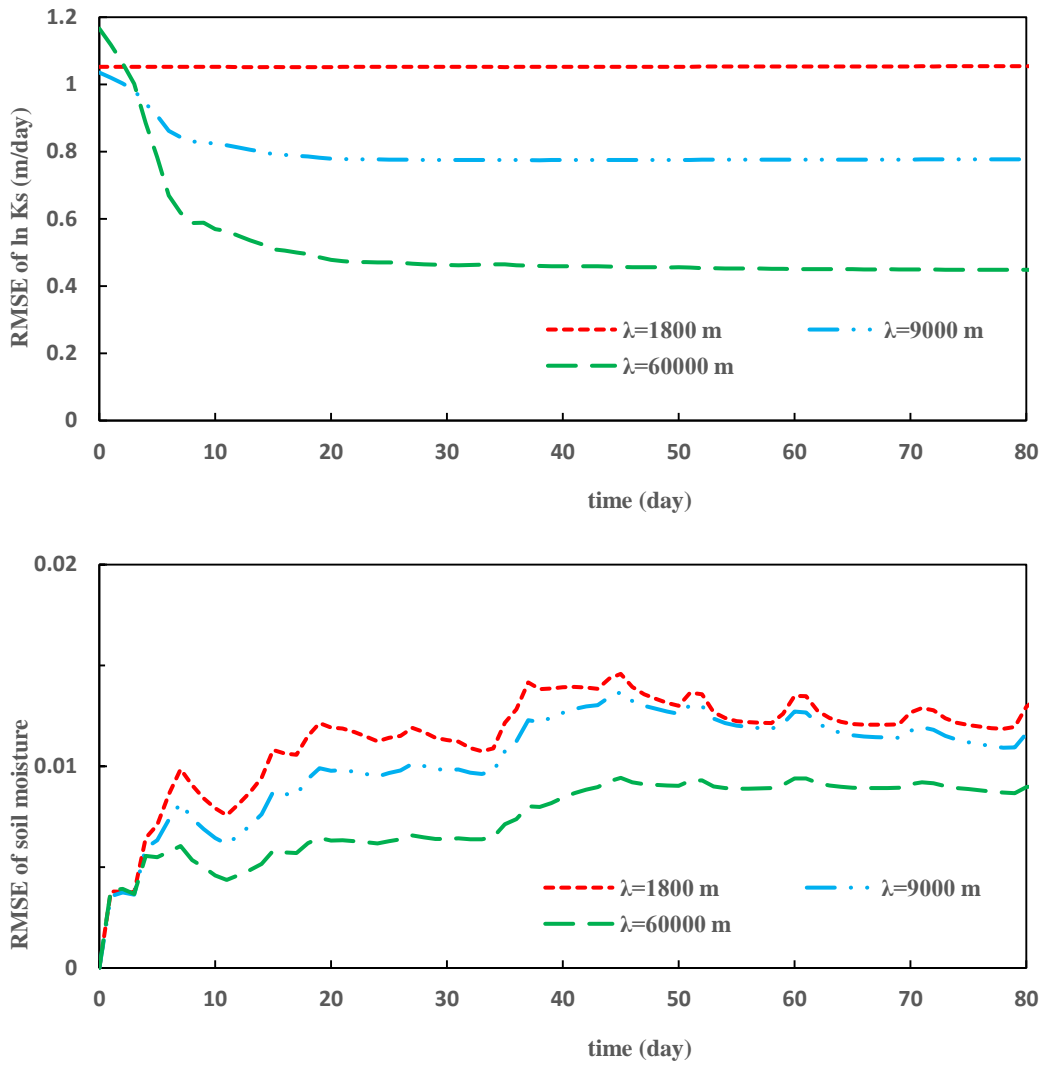
813 **Fig. 6.** Temporal evolution of RMSEs for profile soil moistures in Case 4~6: (a) the whole

814 unsaturated zone; (b) 0~50 cm soil depth.

815

816

817 **Fig. 7.**



818 **Fig. 7.** Temporal evolution of RMSEs for the ln Ks fields and profile soil moisture in Scenario 2

819 (Case 3, 7 and 8), given different parameter correlation lengths λ .

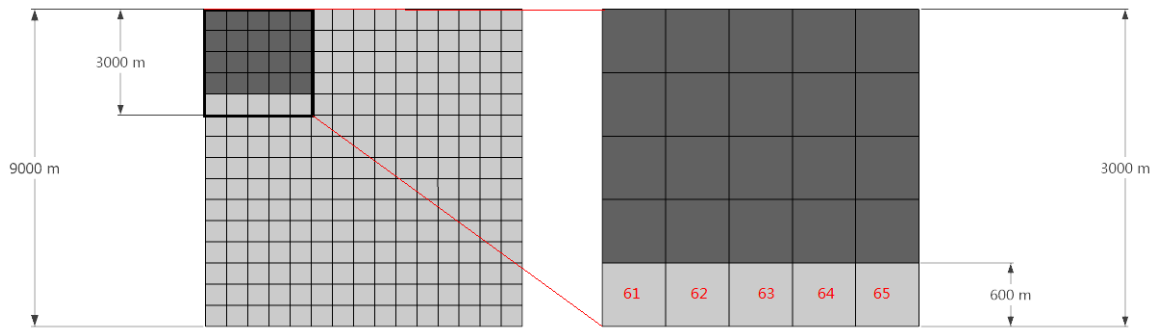
820

821

822

823

824 **Fig. 8**



825 **Fig. 8.** Illustration of the upper boundary conditions used in Case11~13 of Scenario 3. Most of the
826 sub-areas (shallow grey areas) still receive the precipitation series in Fig. 1 (a), while 20 sub-areas
827 (dark grey areas) in the top left corner of the study domain receive a different precipitation series in
828 Fig. 1 (b). The locations of Sub-area 61~65 are labeled with the red Arabic numerals.

829

830

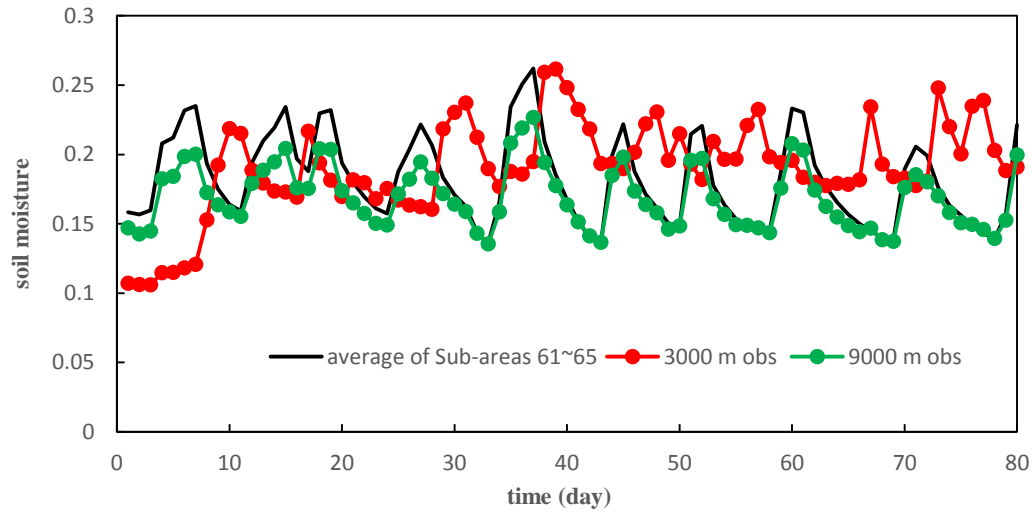
831

832

833

834

835 **Fig. 9.**



836

837 **Fig. 9.** Temporal trends of the 3000 m-scale (Case 11) and the 9000 m-scale (Case 12) soil moisture

838 data in comparison with the average soil moisture changes of Sub-areas 61~65 in Scenario 3.

839

840

841

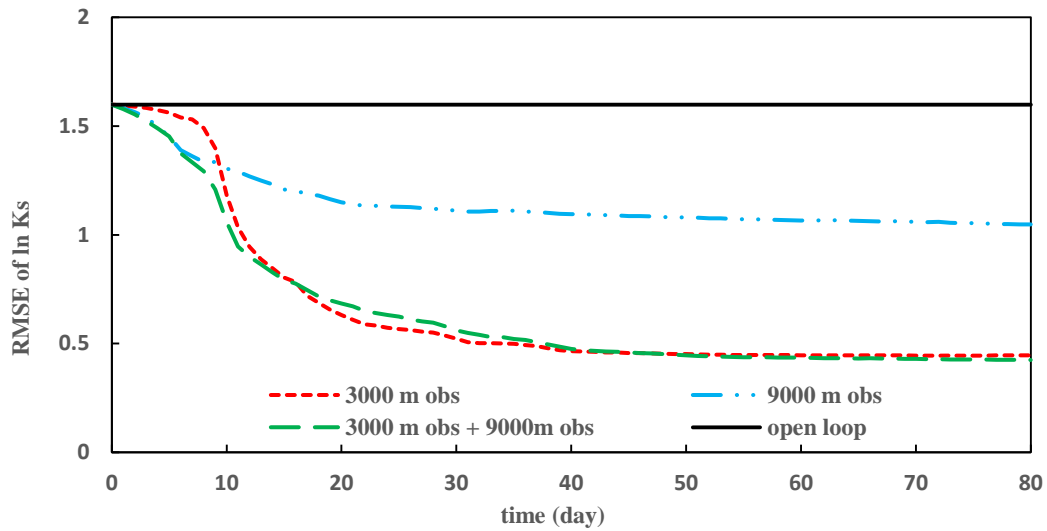
842

843

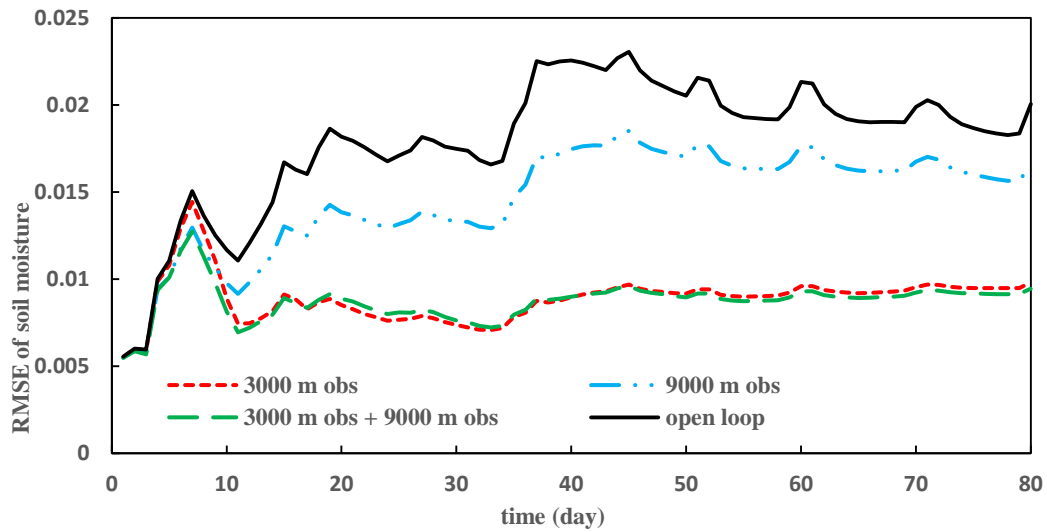
844

845

846 **Fig.10**



847



848

849

850

851 **Fig. 10.** Temporal evolution of RMSEs for the ln Ks fields and profile soil moistures of Sub-areas

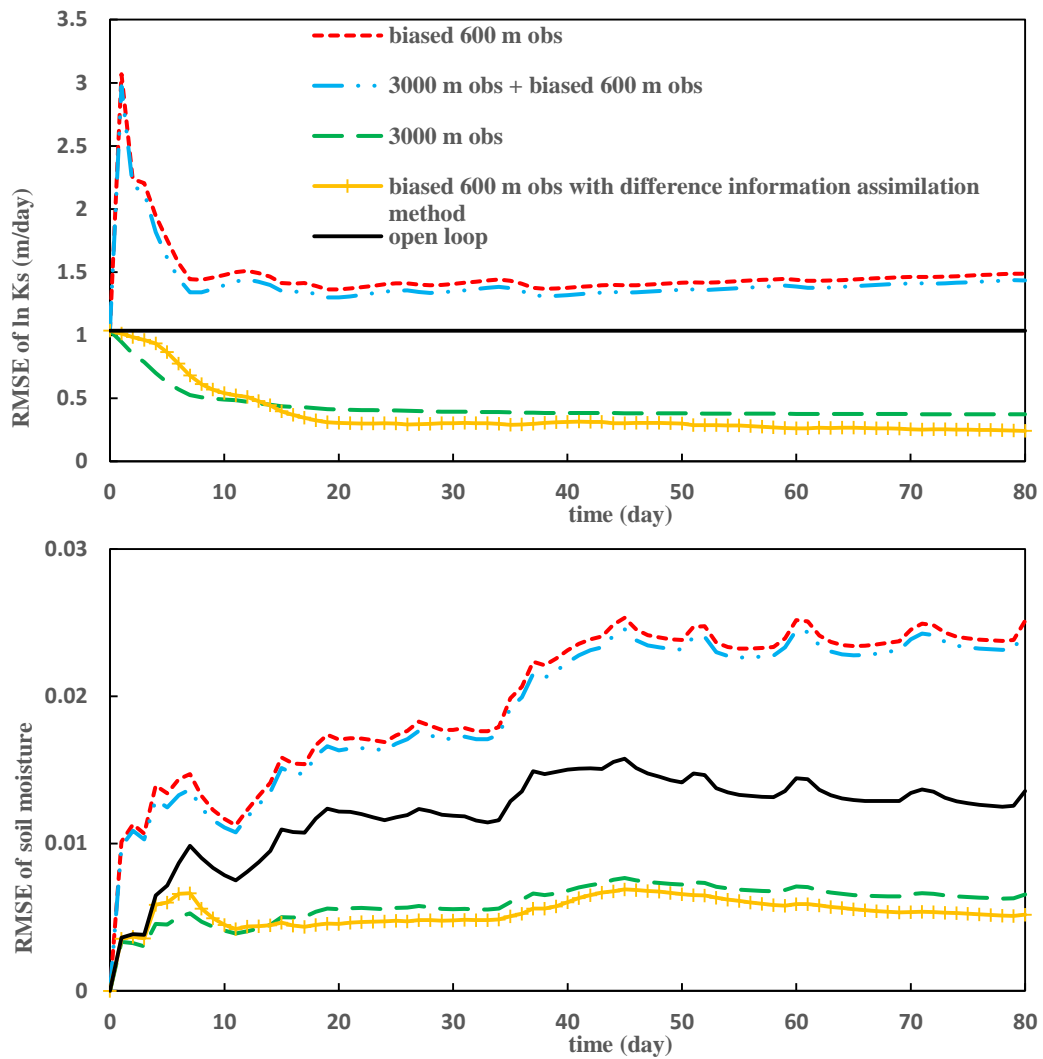
852 61~65 in Scenarios 3 (Case 11~13 and the open-loop run). Different lines represent results by soil

853 moisture data from a 3000 m- grid, a 9000 m- grid and the combined 3000 m- and 9000 m- grids,

854 respectively.

855

856 **Fig. 11.**



857 **Fig. 11.** Temporal evolutions of RMSEs for the $\ln K_s$ fields and profile soil moistures of Case 2, 14,
858 15 and 16, as well as the open loop run in Scenario 4.

859

860

861

862

863

Table 1

864

Specifications of all the cases

Scenario	Case	Observation scale (m)	Correlation			
			length of lnKs field (m)	Observation coverage	Parameter update	Systematic measurement error
1	1	600	9000	whole domain	Y	0
	2	3000	9000	whole domain	Y	0
	3	9000	9000	whole domain	Y	0
	4	600	9000	whole domain	N	0
	5	3000	9000	whole domain	N	0
	6	9000	9000	whole domain	N	0
2	3	9000	9000	whole domain	Y	0
	7	9000	1800	whole domain	Y	0
	8	9000	60000	whole domain	Y	0
	2	3000	9000	whole domain	Y	0
	9	3000	1800	whole domain	Y	0
	10	3000	60000	whole domain	Y	0
3	11	3000	9000	25 sub-areas	Y	0
	12	9000	9000	whole domain	Y	0
	13	3000、9000	9000	whole domain	Y	0
4	2	3000	9000	whole domain	Y	0
	14	600	9000	whole domain	Y	0.03
	15	600、3000	9000	whole domain	Y	0.03、0
	16	600	9000	whole domain	Y	0.03 (new method)

865

866