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Some advanced parametric methods for assessing waveform distortion in a smart grid with renewable generation

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Abstract

Power quality (PQ) disturbances are becoming an important issue in smart grids (SGs) due to the significant economic consequences that they can generate on sensible loads. However, SGs include several distributed energy resources (DERs) that can be interconnected to the grid with static converters, which lead to a reduction of the PQ levels. Among DERs, wind turbines and photovoltaic systems are expected to be used extensively due to the forecasted reduction in investment costs and other economic incentives. These systems can introduce significant time-varying voltage and current waveform distortions that require advanced spectral analysis methods to be used. This paper provides an application of advanced parametric methods for assessing waveform distortions in SGs with dispersed generation. In particular, the Standard International Electrotechnical Committee (IEC) method, some parametric methods (such as Prony and Estimation of Signal Parameters by Rotational Invariance Technique (ESPRIT)), and some hybrid methods are critically compared on the basis of their accuracy and the computational effort required.

Keywords: Smart grid; Dispersed generation; Power quality; Waveform distortion; DFT; Parametric methods

1 Introduction

Currently, significant modifications are taking place in distribution systems as they move toward the future use of smart grids (SGs). The main objectives of SGs are the efficient use of energy, the reduction of losses in the system, improvement in the power quality (PQ), and to encourage the use of distributed generation, in particular renewable energy sources [1-4]. In this context, the increasing use of controllable and non-linear loads and the new needs of liberalized markets impose new PQ requirements in order to avoid dangerous effects [5-7].

Among the disturbances mentioned above, the distortions of the voltage and current waveforms are of great interest, and they have been discussed extensively in the literature. Both types of distortions are due mainly to the extensive use of electronic power converters to supply loads and to connect dispersed generation (DG) units or electrical storage systems to the grid.

Photovoltaic systems (PVSs) and wind turbine systems (WTSs) are the fastest growing systems for meeting the

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requirements of dispersed generation. Their growth is due to the expected cost reduction and to active government policies in many countries that have encouraged their use in power grids in the last few decades. These DG units can be interfaced to the grid through either partially rated power converters or full-scale power electronic devices that can inject harmonic currents that cause voltage distortions [6-8]. Therefore, there is a pressing need to study the impacts of such DG systems on waveform distortions in distribution networks [9]. Thus, the main objective of this paper is to apply some of the advanced methods for the assessment of the waveform distortions that are caused by different configurations of PVSs and WTSs [10-20].

PVSs and WTSs generate distorted, time-varying waveforms. As a result, great attention is required to evaluate the PQ indices to acquire information that must be deduced from the analyses of the spectral components of the waveforms and their locations as a function of time [5,21].

The International Electrotechnical Committee's (IEC) standard recommendations for signal processing use the Discrete Fourier Transform (DFT) over successive, rectangular time windows with the time duration set to 10



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or 12 cycles of the fundamental period for 50-Hz systems or 60-Hz systems, respectively, to evaluate the spectral components [22,23]. However, even though the standard method can provide a global quantification of the waveform distortion, it has limited ability to obtain more detailed information in the analysis of a single spectral component. This is due to some well-known problems that characterize the DFT, i.e., the spectral leakage that arises when the duration of the time window is not correctly synchronized with the fundamental period of the power system [5].

Many solutions have been proposed in the relevant literature to overcome the spectral leakage problems by using DFT-based methods or parametric methods, such as Prony and Estimation of Signal Parameters by Rotational Invariance Technique (ESPRIT) [24-30]. In particular, in [27,28], the Sliding-Window Prony method and the Sliding-Window ESPRIT method were used to provide an accurate estimation of both the harmonic and interharmonic components with high-frequency resolution, but the computational burden was excessive. Other authors have proposed hybrid methods that include DFT and parametric methods to analyze the different frequency bands of a signal separately to reduce the computational burden and provide acceptable accuracy [29,30].

Recently, some authors [31,32] proposed two new, modified sliding-window parametric methods based on modifications of the Prony and ESPRIT signal models. In fact, these methods are based on the observation of the reduced time variability of the frequencies of the spectral components. Then, the frequency values of the spectral components were assumed to be constant over time, thereby reducing the number of unknown parameters of the signal model and the dimension of related equation systems to be solved.

The main aims of this paper can be summarized as follows:

- To provide a depth application of some methods for the assessment of waveform distortion caused by PVS and WTS generators. In particular, the DFT method, parametric methods (Prony and ESPRIT), hybrid methods, and modified sliding-window parametric methods are presented and critically compared on the basis of the accuracy of the results they produce and their computational burdens, taking into account both test and measured waveforms.
- To explore and compare the theoretical waveform distortions introduced by PVS and WTS generators and the distortions detected by the considered methods in some current waveforms measured at the point of common coupling of PVS and WTS.

The paper is organized as follows. Section 1.1 describes waveform distortions in detail that result from the different configurations of the PVS and the WTS schemes. In Section 1.2, the Sliding-Window ESPRIT and Prony methods are exposed, and in Section 1.3, detailed descriptions of the sliding-window hybrid methods and the sliding-window modified parametric methods are presented. In Section 1.4, we describe several case studies that were based on synthetic and measured waveforms of PVSs and WTSs. This article's conclusions are given in Section 2, and the DFT method is discussed in Appendix A.

1.1 Waveform distortion in PV systems and WT systems

It is well known that solar energy and wind energy currently are the most diffuse sources of renewable energy. The following sub-sections provide an overview of the waveform distortions caused by the most common PVS and WTS configurations. The overview deals with the primary spectral emissions that result from disturbances introduced by the specific nature of the system that is being considered, and it also deals with the secondary spectral emissions that are due to disturbances caused by other sources near the system, such as non-linear loads and power communication signals [18]. Note that the distortions introduced by the PVSs and WTSs generally correspond to spectral components that are included in a wide range of frequencies.

For the sake of clarity, in the following, the spectral components up to 2 kHz are referred as 'low-frequency components', and the spectral components over 2 kHz are referred as 'high-frequency components'.

1.1.1 Photovoltaic systems

Photovoltaic panels are connected to the grid through an inverter that converts DC to AC and ensures that particular specifications for voltage and frequency are met and that other important tasks are performed, such as maximum power point tracking (MPPT) [10].

Three-phase or single-phase inverters are used, with the former ensuring no zero-sequence emission in the spectra of the waveforms. Multi-string inverters also are available to obtain the combined benefit of the previous configurations [19].

Figure 1 shows the most diffuse topology solutions for the inverters, i.e., (i) inverters with line frequency isolation transformers (Figure 1a), (ii) inverters with high-frequency isolation transformers (Figure 1b), and (iii) inverters without isolation transformers (Figure 1c) [10,19].

Note that the different topologies and operating conditions of plants produce different waveform distortions. However, in general, it has been observed that every PVS has a low level of distorting spectral components



that increases slightly as the amount of power being produced increases.

Practical experience has indicated that PVSs constituted by multiple inverters produce lower levels of emissions than PVSs that have a unique, large-size inverter [20]. The spectral emissions of PVSs at the point of common coupling (PCC) determine both the low- and high-frequency spectral components.

The low-frequency emissions can be due to both background distortion and over-modulation by the inverter. The amplitudes of these low-frequency spectral components in a single photovoltaic plant are generally characterized by a current total harmonic distortion (THDi) smaller than 10%, but in resonance conditions, significant voltage distortions and problems for the electric network have been documented [19].

The high-frequency emissions basically are due to the PVS inverter and they are specifically due to the pulsewidth modulation (PWM) technique that is used. These emissions are always present during the power production of the system, and they are null when the inverter is turned off; moreover, for the current waveform of a single photovoltaic plant in ideal operating conditions, the amplitudes of these high-frequency spectral components are higher than those of the low-frequency spectral components [18,19]. These spectral components depend on the type of inverter and on its switching frequency, and they are mostly harmonics that appear as sidebands that are centered around integer multiples of the switching frequency [19,33]. Since the switching frequency is generally in a range between 10 and 20 kHz, actually, there still are no adequate and consolidated standards for these high-frequency emissions. Currently, however, the increasing number of spectral components above 2 kHz has resulted in an increased intensity of research activities on this issue [19]. Note that, also at high-frequency, there are often spectral components due to the background voltage, which could become relevant for the series resonance effect.

1.1.2 Wind turbine systems

At the current time, the main large wind turbine schemes are (i) the fixed-speed wind turbine system, (ii) the doubly fed induction generator (DFIG), and (iii) the full-converter wind turbine generator [17,34,35]. Figure 2 shows the block schemes of the three configurations.

Figure 2a shows a fixed-speed wind turbine system in which a squirrel-cage induction generator (SCIG) works in a speed-limited range above the synchronous speed. An electronic soft starter generally is provided to avoid the increase of current during the start-up phase. Also, a bank of capacitors is used to compensate for the reactive power.

The spectral emissions of this scheme primarily are caused by the action of the soft starter, which introduces odd harmonic components at low frequency. Triple



components are usually due to voltage unbalances. Generally, for this configuration, the most significant components detected at the PCC are the 3rd, 5th, 7th, 9th, 11th, and 13th harmonic orders [17].

In a DFIG, the windings of the stator are connected directly to the grid, whereas, on the rotor circuit, there is a back-to-back, partial-scale static converter with a rated power that is roughly equal to 30% of the generator's power.

For this scheme, the spectral emissions in the grid are mainly due to the static converter. Three main types of spectral emissions can arise at the PCC, i.e., (i) inherent components, (ii) switching spectral components, and (iii) spectral components due to the unbalance conditions and/or background voltages [17,36].

The first category includes mostly low-frequency components, and it is due to a non-sinusoidal air gap flux, which produces distorted voltages and currents at the frequencies $f_k = |6 k(1 - s) \pm 1| f_{0,s}$, with k = 1, 2, ..., and where *s* is the generator slip, and $f_{0,s}$ is the fundamental frequency of the stator voltage. These spectral components are time-varying with the speed of the DFIG rotor.

The spectral components that belong to the second class are due to both the rotor-side and grid-side converters and are linked to the PWM technique that was used. They are mostly high-frequency spectral components, but in over-modulation conditions, low-frequency components also can be detected. Under ideal conditions, the aforesaid harmonics and interharmonics are as follows: (i) for the grid side, in correspondence with the frequencies $f_{k,m}^{\text{PWM}g} = \left[kf_{sw,g} \pm mf_{0,s}\right]$, with k, m = 1, 2, ... and where $f_{0,s}$ is the nominal frequency of the system, and $f_{\text{sw,g}}$ is the PWM switching frequency on the grid side; (ii) for the rotor side, in correspondence with the frequencies $f_{k,m}^{\text{PWM},r} = \left[kf_{sw,r} \pm mf_{0,r}\right]$, with k, m = 1, 2, ... and where $f_{0,r} = sf_{0,s}$ is the fundamental frequency of the waveform to generate for the rotor winding, and $f_{sw,r}$ is the PWM

Note that the rotor-side converter works at a frequency that is linked to the generator slip and that the aforesaid spectral components could be shifted because of the air-gap coupling between the rotor current and the stator circuit [36].

The third type of spectral emissions is the spectral components that are introduced by not-ideal operating conditions and by the WTS's auxiliary, non-linear loads, such as controllers and motors [12,17,36].

Figure 2c shows the full-converter wind-turbine generator scheme, which consists of a permanent-magnet synchronous generator connected to the grid by means of a full-scale, power electronic converter with a rated power that is 110% of the generator's power.

Also in this scheme, the emission of spectral components is caused mainly by the static converter, but unlike the previous case, there is no direct influence on the airgap flux, so the spectral content of the waveforms at the PCC is less. The most significant components are harmonics of $6 k \pm 1$ order (5th, 7th, 11th, 13th,...) at low frequency, typical of a six-pulse, three-phase bridge. However, for the high frequency, the typical spectral components of the PWM technique are detected. The Unbalanced condition and background voltage can introduce additional distortions [12-17,34,35].

WTS spectral emissions appear to vary significantly when they are observed over a large period of time; this is because they depend on wind conditions and, as a result, on electrical production. In addition, the harmonic emissions increase as the amount of power generated increases.

1.2 Basic parametric methods for the assessment of time-varying waveform distortion

This section deals with two of the most popular parametric methods used to assess waveform distortion in power systems, i.e., the ESPRIT and the Prony methods, which are used as the basis of the other hybrid methods presented in Section 1.3.

1.2.1 The SW ESPRIT method

The ESPRIT method is one of the most well-known subspace methods that model waveform samples by means a linear combination of M complex exponentials added to white noise r(n). In more detail, a given sequence of sampled data x(n) of size N is approximated by [37]:

$$\hat{x}(n) = \sum_{k=1}^{M} A_k e^{j\psi_k} e^{\left(\alpha_k + j2\pi f_k\right)nT_s} + r(n),$$
(1)

$$n = 0, 1, ..., N-1$$

where T_s is the sampling time, and A_k , ψ_k , f_k , and α_k are the amplitude, the initial phase, the frequency, and the damping factor of the *k*th complex exponential, respectively, which are the unknown parameters to be evaluated.

Model (1) can be written in a matrix form as:

$$\hat{x} = V \Phi^n H + r, \tag{2}$$

where:

$$\begin{split} \hat{x} &= [\hat{x}(n)...\,\hat{x}(n+N_{1}-1)]^{T}, H = [h_{1}...h_{M}]^{T}, \\ r &= [r(n)...\,r(n+N_{1}-1)]^{T}, \\ V &= \begin{bmatrix} 1 & 1 & ... & 1 \\ e^{(\alpha_{1}+j2\pi f_{1})T_{s}} & e^{(\alpha_{2}+j2\pi f_{2})T_{s}} & ... & e^{(\alpha_{M}+j2\pi f_{M})T_{s}} \\ \vdots & \vdots & \ddots & \vdots \\ e^{(\alpha_{1}+j2\pi f_{1})(N_{1}-1)T_{s}} & e^{(\alpha_{2}+j2\pi f_{2})(N_{1}-1)T_{s}} & ... & e^{(\alpha_{M}+j2\pi f_{M})(N_{1}-1)T_{s}} \end{bmatrix} \\ \mathbf{\Phi} &= \begin{bmatrix} e^{(\alpha_{1}+j2\pi f_{1})T_{s}} & 0 & ... & 0 \\ 0 & e^{(\alpha_{2}+j2\pi f_{2})T_{s}} & ... & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & ... & e^{(\alpha_{M}+j2\pi f_{M})T_{s}} \end{bmatrix}, \end{split}$$

 $h_k = A_k e^{j\psi_k}$ and with $N_I < N$ the selected order of the correlation matrix. The symbol Φ represents the rotation matrix, and its properties can be used to determine a solution for the system (2). In particular, problem (2) can be solved by introducing the matrix \hat{S} of the eigenvector associated with the first M eigenvalues of the correlation matrix R_x and a matrix Ψ that has the same eigenvalues of Φ and verifies the relationship:

$$\hat{\boldsymbol{S}}_2 = \hat{\boldsymbol{S}}_1 \boldsymbol{\Psi},\tag{3}$$

where $\hat{S}_1 = \begin{bmatrix} I_{N-1} & 0 \end{bmatrix} \hat{S}$, $\hat{S}_2 = \begin{bmatrix} 0 & I_{N-1} \end{bmatrix} \hat{S}$ and I_{N-1} is an identity matrix of order N-1. Then, by using the least squares approach, the matrix Ψ can be estimated as:

$$\hat{\boldsymbol{\Psi}} = \left(\hat{\boldsymbol{S}}_1^* \hat{\boldsymbol{S}}_1\right)^{-1} \hat{\boldsymbol{S}}_1^* \hat{\boldsymbol{S}}_2 \tag{4}$$

Note that the eigenvalues $\hat{\lambda}_i$ of the matrix Ψ are the elements of the main diagonal of Φ , so $\hat{\lambda}_i = e^{(\alpha_i + j2\pi f_i)T_s}$, and the unknown damping factors and frequencies can be computed as real and imaginary parts, respectively, of the natural logarithm of these eigenvalues. For the amplitudes, it is necessary to use another least squares approach in which the theoretical definition of the correlation matrix R_x [28] is:

$$\boldsymbol{R}_{x} = \boldsymbol{V}\boldsymbol{A}\boldsymbol{V}^{H} + \sigma_{w}^{2}\boldsymbol{I}, \tag{5}$$

where *A* is the diagonal matrix of the squares of the unknown amplitudes, *I* is an identity matrix, and σ_w^2 is the variance of the white noise. In this way, by assuming that the noise *r* is negligible, the initial phases also can be evaluated by making appropriate substitutions in Equation 2 and solving the modified equation.

If the analyzed waveform is time-varying, the Sliding-Window ESPRIT is used with a window that slides forward successively over time in order to obtain the time-dependent estimates of the parameters of the ESPRIT model [5,28].

The reliability of the results and the computational burden of the ESPRIT method are dependent significantly on the number of exponentials *M*, the order *N* of the correlation matrix, and the sampling frequency [38].

1.2.2 The SW Prony method

The Prony method is another parametric method for spectral analysis. This method models the waveform samples by means of a linear combination of M complex exponentials. Specifically, a given sequence of sampled data x(n) of size N is approximated by [5]:

$$x(n) = \sum_{k=1}^{M} h_k z_k^n \quad n = 0, 1, ..., N-1,$$
(6)

where $h_k = A_k e^{i\psi_k}$ and $z_k = e^{(\alpha_k + j\omega_k)T_s}$. To achieve this estimation of the unknown parameters in a traditional way, a severely non-linear problem should be solved [5], but the Prony's intuition allows another approach to be used, i.e., the initial problem is divided into two systems of linear equations, which can be solved easily.

In the first step of the aforesaid approach, the following system of linear equations is solved to determine the damping factors and the frequencies:

$$\sum_{m=0}^{M} a(m)x(n-m) = 0, n = M, M+1, ..., N-1$$
(7)

System (7) is comprised of (N - M) linear equations, and the coefficients a(m) are the M unknowns to be computed. By imposing a(0) = 1, system (7) can be written in matrix form as:

$$\begin{bmatrix} x(M) & x(M-1) & \dots & x(1) \\ x(M+1) & x(M) & \dots & x(2) \\ \vdots & \vdots & \vdots & \vdots \\ x(N-1) & x(N-2) & \dots & x(N-M) \end{bmatrix} \cdot \begin{bmatrix} a(1) \\ a(2) \\ \vdots \\ a(M) \end{bmatrix} = -\begin{bmatrix} x(M+1) \\ x(M+2) \\ \vdots \\ x(N) \end{bmatrix}$$
(8)

After the coefficients a(m) have been determined, the polynomial F(z) can be obtained:

$$F(z) = \sum_{m=0}^{M} a(m) z^{M-m}$$
(9)

The roots z_k of F(z) are used to calculate the damping factors and the frequencies of each exponential by means of simple relationships.

The second step provides the amplitude and phase of each exponential by calculating the h_k . This is possible by replacing the obtained z_k in system (6) and, so, by solving another system of linear equations that in matrix form is [5]:

$$\begin{bmatrix} z_1^0 & z_2^0 & \dots & z_M^0 \\ z_1^1 & z_2^1 & \dots & z_M^1 \\ \vdots & \vdots & \vdots & \vdots \\ z_1^{M-1} & z_2^{M-1} & \dots & z_M^{M-1} \end{bmatrix} \cdot \begin{bmatrix} h_1 \\ h_2 \\ \vdots \\ h_M \end{bmatrix} = \begin{bmatrix} x(1) \\ x(2) \\ \vdots \\ x(M) \end{bmatrix}$$
(10)

If the analyzed waveform is time-varying, the Sliding-Window Prony is used once again with sliding windows in order to obtain the time-dependent estimates of the parameters of the Prony model [5,27]. In [27], an adaptive technique also was proposed in order to achieve an optimal and adaptive duration of the sliding window. The accuracy and computational burden of the Prony method depend significantly on the number of exponentials M, the number N of samples for analysis window, and the sampling frequency [38].

1.3 Advanced parametric methods for the assessment of time-varying waveform distortion

In this section, two types of advanced parametric methods for spectral analysis are analyzed: the Threestep Sliding-Window Hybrid method and the Sliding-Window Modified Parametric method. These methods are based on the parametric methods considered in Section 1.2 and are able to provide both accurate results and reduced computational burden.

1.3.1 The Three-step sliding-window hybrid method

The Three-step Sliding-Window Hybrid method is a joint parametric-DFT scheme that was developed in three stages in which either the sliding-window (SW) ESPRIT, the SW Prony, or the SW DFT can be used alternatively to estimate (i) the fundamental and the interharmonic components in the 0 to 100 Hz band, (ii) the harmonics, and (iii) the interharmonics at frequency f > 100 Hz of power system waveforms [29,30], reducing the typical problems that characterize the SW DFT and the SW parametric method (i.e., spectral leakage problems and high computational efforts). Figure 3 shows the block diagram of the three-step method.

In more detail, in the first step, the SW parametric method (Prony or ESPRIT) is applied to the output of a low-pass band filter of 0 to 200 Hz, in order to estimate the power system's fundamental and the interharmonics in the frequency range from 0 to 100 Hz. Then, the filtered waveform is approximated with a linear combination of exponentials according to either the (1) (SW ESPRIT) or (6) (SW Prony).

In the second step, the SW DFT is used to evaluate the harmonic components; in fact, there is also an estimation of the fundamental frequency among the outputs of the first step, so it is possible to set the duration of the DFT analysis window equal to an integer multiple of the fundamental period \hat{T}_{fund} , greatly limiting the spectral leakage.

As shown in Figure 3, the waveform analyzed by the synchronized DFT is obtained by subtracting from the original signal x(n) the reconstructed waveform $\hat{x}_{l.f.}(n)$ that was obtained by the first step. The duration of the analysis window in this step can be set to 10 cycles



(12 cycles) of the fundamental period \hat{T}_{fund} , for 50-Hz systems (60-Hz systems), according to the IEC recommendations, but if it is required, it also is possible to select a different number of cycles [29]. We note that the aforesaid synchronization of the DFT time window guarantees a very accurate estimation of the harmonic components with a reduced computational effort, and this is attributable to the significant limitation of the spectral leakage due only to the possible presence of interharmonics at frequencies f > 100 Hz in $x_I(n)$, which yields relatively low errors [5,29].

The waveform $\hat{x}_{harm}(n)$ in Figure 3 was obtained summing the estimated harmonics and using the results to compute the residual $x_2(n)$ by subtracting $\hat{x}_{harm}(n)$ from $x_1(n)$. The waveform $x_2(n)$ is analyzed in the third step by the same parametric method used in the beginning of the scheme.

Note that, in the first and third steps, the number of exponentials required in the model was considerably lower than the number needed in the application of SW ESPRIT or SW Prony to the full band signal. This positive outcome resulted from the explanation of the decomposition of the waveform in different frequency ranges separately analyzed in the first and third steps. As a result, the Three-step SW method has a significantly lower computational burden than SW ESPRIT or SW Prony while still providing highly accurate results.

In order to improve the global performances of the Three-step SW method, each step could have a different duration of the analysis window, and then, the results could be processed and associated with a common time interval.

1.3.2 The sliding-window modified parametric method

The Sliding-Window Modified Parametric methods are based on a reduction of the unknown parameters in the signal model in the original parametric methods with obvious improvements in terms of computational efforts. In fact, starting from the consideration that the damping factors and the frequencies of spectral components in power system applications are slightly variable versus time [25,39-43], the estimation of frequencies is conducted only a few times, and the damping factors are assumed to be constant along the entire signal to be analyzed [31,32].

Specifically, in [32], the frequencies of the spectral components were computed initially by the analysis of the first sliding window, the *basis window*, and then, the values that were obtained were assumed to be constant with time, and they were imposed as known quantities in the successive sliding windows (*no-basis windows*). The damping factors were assumed to be null in the SW M-Prony and fixed to previously calculated values during the analysis of the '*basis window*' in the SW M-ESPRIT [32].

We note that, to elude masking effects due to significant variation of the frequencies, it is expected that the estimation of the frequencies would be repeated periodically. If the deviation between the values obtained was greater than a fixed threshold, the frequencies are updated and the analysis restarts with these new values. We also note that a different choice is required for the damping factors in the Prony and ESPRIT methods. The damping factors, in fact, are able to take into account temporal variations of the amplitudes of the spectral components and to link two consecutive sliding windows smoothly.

When the duration of the windows is very short (one to two times the fundamental period), the damping factors have very low values, and their contribution is negligible. This is the case for the SW Prony, so for this method, the damping factors are set equal to zero. However, for the SW ESPRIT, the duration of the analysis window is significantly larger (four to five times the fundamental period), so in this case, the damping factors are assumed to be constant for the no-basis windows and equal to the damping factors estimated for the basis window [32].

Figure 4 shows the block diagram of the Sliding-Window Modified Parametric methods.

In the first window (basis window for k = 0), a traditional parametric algorithm (TPA) is used to estimate all of the unknown parameters $(A_k^{BW}, f_k^{BW}, \psi_k^{BW}, \alpha_k^{BW})$, which, then, are stored; in this window, the research for the optimal values for M and N_1 or N (respectively for the ESPRIT-based and Prony-based method) is effected, updating them if the reconstruction error overcomes a prefixed threshold. The same algorithm is also used after k_f windows, where another basis window is generated in order to avoid the masking effect. The choice of the value k_f is related to the particular nature of the analyzed waveform. In the no-basis windows, a modified parametric algorithm (MPA) is used only for the computation of the unknown amplitudes A_k and initial phases ψ_k of the spectral components, since the frequencies are equal to f_k^{BW} , and the damping factors are forced to be null or equal to α_k^{BW} for the Prony and ESPRIT methods, respectively. Specifically, the equations solved in the MPA when ESPRIT is used are as follows:

i)
$$\begin{cases} \boldsymbol{R}_{x} = \boldsymbol{V}_{BW} \boldsymbol{A} \boldsymbol{V}_{BW}^{H} + \sigma_{w}^{2} \boldsymbol{I} \\ \hat{\boldsymbol{x}} = \boldsymbol{V}_{BW} \boldsymbol{\Phi}_{BW}^{n} \boldsymbol{H} \end{cases}$$
(11)

When Prony is used, the equation system solved in MPA is as follows:

i)
$$x(n) = \sum_{k=1}^{M} h_k (\hat{z}_k^{\text{BW}})^n$$
, $n = 0, 1, ..., N-1$ (12)

The assumption of constant frequencies and damping factors inside the no-basis windows decreases the number of unknown parameters to be estimated, and the



computational effort is reduced significantly compared to the classical Prony or ESPRIT approach [32].

1.4 Numerical applications

The basic and advanced parametric methods shown in Sections 1.2 and 1.3, respectively, were used to analyze the waveform distortion due to PVSs and WTSs, and the accuracy of their results and the computational burden of the methods were compared. Several numerical experiments were conducted, analyzing both synthetic and measured waveforms in many operating conditions of DG units, but for sake of brevity, only four case studies are reported in this section, and all of them are referred to the analysis of the current waveforms.

Specifically, the synthetic and measured currents of PVSs and WTSs were analyzed by using the following:

- the IEC standard method (IECM);
- the Sliding-Window ESPRIT method (SWEM);
- the Sliding-Window Prony method (SWPM);
- the Three-step Sliding-Window ESPRIT-DFT-ESPRIT method (SWEDEM);

- the Three-step Sliding-Window Prony-DFT-Prony method (SWPDPM);
- the Sliding-Window Modified ESPRIT method (SWMEM);
- the Sliding-Window Modified Prony method (SWMPM).

The results of each case study were referred to the same duration of signal, and the IECM computational burden was considered as a reference for the other methods. It is important to emphasize that, for the IECM, since its frequency resolution was fixed at 5 Hz, the fundamental component was always detected in correspondence with 50 Hz, so the harmonic components are estimated also as multiples of 50 Hz.

All of the programs were conducted in MATLAB, and they were not optimized for computational speed because we were interested only in obtaining a rough and relative quantification of the efficiency of the different methods. The MATLAB programs were developed and tested on a Windows PC with an Intel i7-3770 3.4 GHz and 16 GB of RAM.

1.4.1 Case study 1: test signal of a photovoltaic system

The synthetic 3-s waveform emulated a current at the PCC of a PVS that had a full-bridge, unipolar inverter. It was a sort of an 'acid test,' since our aim was to observe the behavior of each of the methods in the analysis of a waveform with a very wide spectrum, i.e., exceeding a frequency of 20 kHz. Specifically, the waveform was assembled assuming a frequency modulation index m_f equal to 200 for the inverter PWM technique and the presence of all odd harmonics up to the 27th order for the low-frequency components. The fundamental component was fixed at 50.02 Hz, and it had an amplitude of 9 A. Also, a white noise with a standard deviation of 0.001 was added to the aforesaid components.

The sampling rate was 100 kHz in order to provide the most appropriate operating conditions for the parametric methods that were used so that they could provide estimates of the spectral components around the order $2m_{\beta}$ which are the most significant introduced by the aforesaid type of PWM and whose amplitudes were fixed up to 12% of the fundamental^a. For the parametric methods, the error threshold was fixed equal to 10^{-5} , and for all of the methods, the window of analysis slides of 0.04 s was used. In the second steps of both SWPDPM and SWEDEM, the analysis window was fixed equal to 5 cycles of the fundamental period.

Table 1 shows the average percentage errors in the estimates of the frequencies and amplitudes of five spectral components, particularly interesting in the comparison of the methods that were used. Specifically, the components that were examined were the fundamental and the harmonics of order 3rd, 11th, 401st, and 405th, with amplitudes equal to 1.6%, 6%, 12%, and 3% of the fundamental amplitude, respectively.

It was evident that SWEM, SWPM, SWMEM, and SWMPM always provided negligible percentage errors, with values almost of the same order of magnitude. As the first part of Table 1 shows, the percentage errors obtained using the SWEDEM and the SWPDEPM also were very low; however, the second part of Table 1 shows SWEDEM and SWPDEPM with higher errors for the amplitude than with the other basic and advanced parametric methods.

This behavior of the three-step methods in estimating the amplitudes of the fundamental and third harmonic was due to the presence of the low-pass band filter of 0 to 200 Hz, which introduces a little attenuation in the amplitude of the components in the frequency band of 0 to 100 Hz and slight distortions for the components near the filter cut-off frequency. However, it is important to emphasize that, for the other harmonic components (far from the filter cut-off frequency) both at low and high frequency, the errors in the amplitude were practically negligible. Table 1 shows that the IECM errors were globally higher, both in terms of frequency and amplitude, and that, for the high-frequency components, the average percentage error in the estimation of amplitudes increased, reaching values greater than 90%.

This was due to the desynchronization between the duration of the time window and the fundamental period,

	Fundamental	3rd	11th	401st	405th
(a) Average errors by frequency [%]					
SWEM	1.08×10^{-4}	0.0028	1.74×10^{-4}	2.93×10^{-6}	1.15×10^{-5}
SWPM	5.77×10^{-5}	0.0012	8.47×10^{-5}	1.18×10^{-6}	4.81×10^{-6}
SWEDEM	6.86×10^{-4}	1.58×10^{-5}	1.58×10^{-5}	1.58×10^{-5}	1.58×10^{-5}
SWPDPM	1.55×10^{-5}	1.60×10^{-5}	1.60×10^{-5}	1.60×10^{-5}	1.60×10^{-5}
SWMEM	1.12×10^{-4}	0.0023	1.50×10^{-4}	3.01×10^{-6}	1.89×10^{-6}
SWMPM	4.43×10^{-5}	0.0013	2.21×10^{-5}	2.27×10^{-6}	5.54×10^{-7}
IECM	0.04	0.04	0.04	0.04	0.04
(b) Average errors of amplitude [%]					
SWEM	9.85×10^{-4}	0.067	0.016	0.0081	0.031
SWPM	4.29×10^{-4}	0.026	0.0078	0.0037	0.017
SWEDEM	0.11	0.09	0.064	0.073	0.070
SWPDPM	0.11	0.66	0.073	0.074	0.071
SWMEM	5.27×10^{-4}	0.019	0.0056	0.0024	0.014
SWMPM	3.86×10^{-4}	0.023	0.0065	0.0032	0.014
IECM	0.060	0.70	0.28	82.31	91.51

Table 1 Case study 1: average percentage estimation errors

Average percentage estimation errors of (a) frequencies and (b) amplitudes of the fundamental, 3rd, 11th, 401st, and 405th harmonic components by means of SWEM, SWPDM, SWEDEM, SWPDEPM, SWMEM, SWMPM, and IECM.

which produces spectral leakage problems that increase as the harmonic order increases. Table 2 shows the computational times obtained by using all of the methods to analyze the 3-s waveform per unit of computational time required by IECM. It is evident that the basic parametric methods require greater computational time in order to provide accurate results; however, the advanced parametric methods reduced the computational effort significantly while simultaneously providing highly accurate results. Note that the SWEM (SWMEM) required less computational effort than the SWPM (SWPEM); this was due to under-sampling the signal before analysis [44].

Tables 3 and 4 are provided to make it clearer what occurred in terms of the accuracy and computational efforts when the sampling rate in SWEM and SWMEM remained at 100 kHz. Table 3 shows that there was an irrelevant gain in the accuracy of the results compared to the values shown in Table 1.

However, the computational burdens of SWEM and SWMEM (Table 3) were considerably greater than those observed for the same methods in Table 2. This proves that the optimal sampling rate for each parametric method guarantees the best performance with respect to accuracy and computational time. It also proves that the accuracy of the results was not affected by exceeding the optimal sampling rate, but the computational effort increased significantly, especially at the very high-sampling rates.

Table 2 shows that the computational time of SWEDEM was greater than that of SWPDPM. This was because the presence of the filter in the first step resulted in some negligible spectral components at low frequency that made it impossible to reduce the signal sampling rate in the first step of SWEDEM and maintain an acceptable accuracy.

It was interesting to observe that, in this case study, the advanced parametric methods required computational times that were, in the worst case (i.e., the SWEDEM and the SWMPM), an order of magnitude greater than that needed by the IECM. SWPDPM and SWMEM had computational times that were the same order of magnitude as that of the IECM, although these methods provided better

Table 2 Case study 1: computational time of all of the methods

	Computational time [p.u.]
SWEM	45.56
SWPM	618.03
SWEDEM	12.86
SWPDPM	4.24
SWMEM	2.87
SWMPM	10.27
IECM	1

The values are per unit of computational time required by IECM.

results than the method recommended by the IEC standards.

1.4.2 Case study 2: measurement of the current of the photovoltaic system

A 1-s current waveform measured at the PCC of a 10-kW, three-phase inverter without an isolation transformer, which, together with another twin-inverter, is included in a PVS. The sampling rate was 10 kHz, but in order to provide better operating conditions for the detection of spectral components by the parametric methods that were used, a resampling to 20 kHz was used [44].

The error threshold for the parametric methods was fixed at 10^{-3} , and the window of analysis slides of 0.04 s was used for all of the methods. In the second steps of the SWPDPM and the SWEDEM, the analysis window was fixed equal to 5 cycles of the fundamental period. Figure 5 shows the time trend of the measured current.

All of the methods that were used detected mainly low-frequency spectral components. In fact, in the frequency band from 5 to 10 kHz, the advanced methods that used the ESPRIT method and the DFT method detected the same components, but the values of amplitude were lower than the 0.05% of the fundamental, so they are not discussed here.

Table 5 shows the average values of frequency and amplitude of some spectral components detected by all of the methods that were used. Among the most significant spectral components, Table 5 reports the results related to the fundamental, a harmonic at about 1,000 Hz, and an interharmonic at about 2,915 Hz. They are good representatives that provide a perception of the behaviors of the methods that were used in the evaluation of the various types of spectral components.

First, as expected, it was evident that both harmonic and interharmonic components had low amplitudes and that each method was able to estimate them adequately, since the values that were obtained for both frequency and amplitude were in a narrow range.

The IECM provided an amplitude value of about 1 order of magnitude lower than the other methods only for the interharmonic detection, although the component was almost a multiple of 5 Hz (the IECM frequency resolution). This phenomenon was compatible with the observation in the previous case study; in fact, it confirmed that spectral leakage increases at high frequencies.

Table 6 shows the computational time, per unit of the computational time required by IECM, obtained by analyzing the current waveform by all of the methods. The advanced parametric methods always required less computational time than the basic parametric methods. In particular, all of the advanced parametric methods required a computational time that was 2 orders of magnitude less than those of SWEM and SWPM.

	Fundamental	3rd	11th	401st	405th
(a) Average errors of frequency [%]					
SWEM	7.80×10^{-5}	0.0013	1.10×10^{-4}	1.53×10^{-6}	6.02×10^{-6}
SWMEM	6.07×10^{-5}	7.39×10^{-4}	9.75×10^{-5}	3.22×10^{-6}	2.29×10^{-7}
(b) Average errors of amplitude [%]					
SWEM	5.30×10^{-4}	0.026	0.0092	0.0046	0.018
SWMEM	2.58×10^{-4}	0.029	0.0036	0.0034	0.014

Ta	ble	3	Case	study	y 1:	average	percentage	estimation	errors
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Average percentage estimation errors of (a) frequency and (b) amplitude of spectral components detected by SWEM and SWMEM.

Also, in this case, the SWMEM was the method that came the closest to matching the performance of IECM with respect to computational time. Note that, for the analysis of the measured current, all of the advanced parametric methods required computational times that were only 1 order of magnitude greater than that required by IECM.

1.4.3 Case study 3: test signal of wind turbine system

The synthetic 1-s waveform emulated a current at the PCC of a WTS that had a doubly fed induction generator. Also, this case study was a sort of 'acid test,' since our aim was to observe the behavior of each of the methods in the analysis of a waveform with a spectrum that exceeded a frequency of 2 kHz and that had embedded successive harmonic and interharmonic components.

The waveform was assembled assuming a frequency modulation index m_f of 40, and the fundamental frequency and amplitude were fixed at 50.02 Hz and 5.4 A, respectively. Figure 6 shows the low-frequency and the high-frequency spectrum of the test signal. White noise with a standard deviation of 0.001 was added to the signal in order to make the waveform more realistic and to stress the performance of the spectral analysis methods that were used.

The sampling rate was 20 kHz. For the parametric methods, the error threshold was fixed at 5×10^{-8} , and for all of the methods, the window of analysis slides was 0.04 s. In the second steps of both the SWPDPM and the SWEDEM, the analysis window was equal to 10 cycles of the fundamental period.

Table 7 shows the average percentage errors in the estimates of the frequency and amplitude of the five

Table 4 Case study 1: computational time for the oversampled waveform

	Computational time [p.u.]
SWEM	107.01
SWMEM	58.57

Relative computational time in p.u. of IECM time, when the analyzed waveform was over-sampled at 100 kHz.

spectral components, which are particularly interesting for comparing the methods that were used. Specifically, the components that were examined were the fundamental, the 5th, and the 38th order of harmonic and two interharmonics at 74.79 and 382.35 Hz.

In this case study, it was observed that the SWPM, in order to provide reasonably accurate results, requires a very high number of exponentials M, and as a result, it also requires a high value of N for the optimal window of analysis. This is due to the contemporaneous presence of noise interference and many small spectral components in the signal. In fact, since the Prony signal model does not include noise, Prony-based methods require an increasing number of M in the presence of so many small spectral components and noise. Basically, the SWPM adds many spectral components to the real spectrum, since it also must individuate the noise spectrum to approach the analyzed waveform adequately.

However, it is easier for the SWEM to detect the spectrum, since noise is accounted for in its model.

However, as shown in Table 7, both the SWPM and the SWEM provide better results in terms of accuracy, with average percentage errors of the same order of magnitude.

Obviously, noise interference also was a problem for the SWMPM, which produced less accurate results than the SWMEM; however, it performed well in detecting the spectral components, with errors of the same order of magnitude as the basic parametric methods (error of less than 0.021% for the estimation of frequency and less than 0.9% for the estimation of the amplitude). The second part of Table 7 shows that the SWPDPM and the SWEDEM had some difficulties in estimating the amplitudes of the components up to the fifth harmonic; as underlined in case study 1, this was due to the effect of the low-pass band filter. However, the first part of Table 7 shows that the average percentage errors for these methods were comparable to the best results obtained by the basic methods.

However, in the estimations of both the frequency and the amplitude, the IECM had the largest errors, especially for the interharmonic components, which were detected with average percentage errors in the frequency



of 0.2% and 0.6% for the components near 74.79 and 382.35 Hz, respectively. For the same components, the average errors of amplitude were even worse, at 3% and 31%, respectively.

Table 8 shows the computational time required to analyze the test signal by all of the methods. Also in this case, the SWEM and the SWPM appear to be the slowest methods, whereas the advanced parametric methods had computational times that were significantly less than those of SWEM and SWPM. In fact, in the best case, they were only 1 order of magnitude greater than the time required by IECM. In particular, once again,

Table 5 Case study 2: average values

	Fundamental	Harmonic	Interharmonic
(a) Average values of frequency [Hz]			
SWEM	49.98	1001.38	2915.63
SWPM	49.97	1001.61	2914.50
SWEDEM	49.98	999.55	2911.02
SWPDPM	49.98	999.51	2912.03
SWMEM	49.98	1001.15	2912.28
SWMPM	49.97	1000.73	2912.00
IECM	50.00	1000.00	2915.00
(b) Average values of amplitude [A]			
SWEM	13.44	0.18	0.15
SWPM	13.39	0.24	0.15
SWEDEM	13.38	0.23	0.14
SWPDPM	13.39	0.23	0.14
SWMEM	13.44	0.27	0.15
SWMPM	13.44	0.24	0.14
IECM	13.40	0.20	0.052

Average values of (a) frequency and (b) amplitude of the fundamental, a harmonic, and an interharmonic detected by SWEM, SWPDEM, SWEDEM, SWPDEPM, SWMEM, SWMPM, and IECM.

SWMEM is the method that required a computational time that was the closest to that of IECM.

1.4.4 Case study 4: measured signal of wind turbine system A 6-s current waveform measured during the soft starting of a fixed-speed wind turbine was analyzed. The original sampling rate was 2,048 Hz, so a resampling at 10 kHz was conducted.

For the parametric methods, the error threshold was fixed equal to 10^{-7} , and the window of analysis slides was 0.02 s for all of the methods. In the second steps of both the SWPDPM and the SWEDEM, the analysis window was fixed equal to 3 cycles of the fundamental period. Figure 7 shows the highly time-varying trend of this waveform, which allowed us to test and compare methods also in the analysis of a non-stationary waveform.

As was predictable based on the theoretical considerations reported in Section 1.1, all of the methods identified the 3rd, 5th, 7th, and 11th harmonics as significant components, in addition to the fundamental. The amplitudes of the aforesaid components were characterized initially by an increasing trend up to a maximum value, after which the descending phase began and continued until each component achieved its steady-state value.

Table 6 Cas	e study	/ 2: con	nputational	time
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	Computational time [p.u.]
SWEM	9447.06
SWPM	5227.87
SWEDEM	21.59
SWPDPM	15.58
SWMEM	11.75
SWMPM	21.35
IECM	1

Computational time, in p.u. of the computational time required by the IECM, of all of the methods.



Table 7 Case study 3: average percentage er	rrors
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	Fundamental	74.79 Hz	5th	382.35 Hz	38th
(a) Average errors of frequency [%]					
SWEM	1.18×10^{-4}	0.0036	9.24×10^{-4}	0.0041	3.75×10^{-5}
SWPM	7.84×10^{-5}	0.0013	4.35×10^{-4}	0.0015	2.39×10^{-5}
SWEDEM	0.0056	0.0063	0.0042	0.0028	0.0042
SWPDPM	9.37×10^{-5}	0.0025	1.60×10^{-5}	0.0019	1.60×10^{-5}
SWMEM	3.88×10^{-4}	0.0041	0.0028	0.021	5.18×10^{-5}
SWMPM	0.0016	0.011	0.11	0.12	3.69×10^{-4}
IECM	0.04	0.28	0.04	0.64	0.04
(b) Average errors of amplitude [%]					
SWEM	0.0019	0.059	0.066	0.48	0.026
SWPM	0.0012	0.039	0.035	0.22	0.028
SWEDEM	0.19	2.80	2.01	0.43	0.25
SWPDPM	0.19	2.77	2.09	0.36	0.077
SWMEM	0.0014	0.027	0.20	0.89	0.011
SWMPM	0.0058	1.16	1.50	7.34	0.041
IECM	0.10	3.41	2.15	31.48	3.12

Estimation of the average percentage errors of the fundamental, harmonic components, and interharmonics obtained by SWEM, SWPM, SWEDEM, SWPDEPM, SWMEM, SWMPM, and IECM: (a) frequencies; (b) amplitudes.

Table 8 Case study 3: computational time

	Computational time [p.u.]
SWEM	2116.47
SWPM	6507.25
SWEDEM	79.79
SWPDPM	180.81
SWMEM	11.84
SWMPM	30.02
IECM	1

Computational time, in p.u. of the computational time required by the IECM, of all of the methods.

Table 9 reports the maximum peak values of amplitude for the fundamental, the fifth, and the seventh harmonics that were detected by the methods that were used.

The results presented in Table 9 provide evidence that the IECM had significant spectral leakage since the estimated values always were considerably lower than those obtained by the parametric methods. These lasts, in fact, estimate, for each component, values that differ slightly from each other.

Note that, as expected, the behaviors of the time trends of the frequencies were different; in fact, all of the parametric methods had spectral-component frequencies with negligible time variations.

Table 10 shows the computational time required by all of the methods to analyze the current's waveform. The results were similar to those in the previous case study. It is important to observe that the SWMEM required a computational time that was only double that of IECM.

2 Conclusions

In this paper, we analyzed some methods used to estimate waveform distortions caused by photovoltaic and wind turbine systems. An overview of the waveform distortions caused by the most common configurations of PVSs and WTS schemes was also provided.

The theoretical aspects of the basic and advanced parametric methods proposed in literature were presented, focusing on their high accuracy while, at the same time, emphasizing how the advanced parametric methods have the advantage of having computational times that are significantly less than those required by the basis parametric methods.

The basic parametric methods that were considered were the Sliding-Window ESPRIT method and the Sliding-Window Prony method. The advanced parametric methods were the following:

the Three-step Sliding-Window ESPRIT-DFT-ESPRIT method;

the Three-step Sliding-Window Prony-DFT-Prony method;

the Sliding-Window Modified ESPRIT method; the Sliding-Window Modified Prony method.

These methods were used in the spectral analysis of synthetic and measured currents of PVSs and WTSs in order to compare them in terms of the accuracy of the results they produced and computational efforts for both stationary and non-stationary waveforms. The waveforms were analyzed also by the IEC standard method, which we used as a reference for comparisons of computational times.

The case studies that were considered highlighted the importance of an adequate sampling rate for the parametric methods and the importance of the effect of noise on the detection of spectra by the Prony-based method when the signal components have very small amplitudes. In fact, in these cases, the ESPRIT-based methods can estimate the spectral components more easily, requiring a lower computational burden than the methods that use the Prony model.



Table 9 Case study 4: estimated peak values

Maximum peak value [A]					
	Fundamental	5th	7th		
SWEM	866.92	139.96	66.97		
SWPM	857.84	139.79	64.56		
SWEDEM	867.06	139.31	64.14		
SWPDPM	867.68	139.26	63.90		
SWMEM	864.24	143.03	70.99		
SWMPM	867.52	140.25	67.19		
IECM	814.20	133.40	58.50		

Peak values of the fundamental, 5th, and 7th harmonics detected by SWEM, SWPM, SWEDEM, SWPDEPM, SWMEM, SWMPM, and IECM.

All of the parametric methods were shown to have high levels of accuracy, exceeding that provided by the IECM, especially when the waveform spectrum was very wide. The IECM, in fact, failed in the detection of both interharmonic components and high-frequency harmonics.

Conversely, the advanced parametric methods took less computational effort than the basic parametric methods, with computational times of the same order of magnitude or no more than 1 order or magnitude greater than that of the IECM. The aforesaid numerical experiments also demonstrated that the SWMEM generally provided the best compromise between highaccuracy results and low computational effort.

It is important to note that, for very wide spectra, the three-step solution could inspire a new method for spectral analysis in which separating the waveform into lowand high-frequency components could result in the rapid and accurate detection of the spectral components of both the aforesaid bands by adapting the duration of the analysis window to the lowest frequency of each band.

3 Appendix A - IEC method

The standards IEC 61000-4-7 [23] and IEC 61000-4-30 [22] propose to use, for the spectral analysis of the non-stationary waveforms, the Sliding-Window Discrete Fourier Transform, which consists of applying the DFT to

Table To Case study 4. computational time	Table	10	Case	study	4:	computationa	l time
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	Computational time [p.u.]
SWEM	145.44
SWPM	367.38
SWEDEM	25.34
SWPDPM	57.26
SWMEM	2.34
SWMPM	4.29
IECM	1

Computational time, in p.u. of the computational time required by the IECM, of all of the methods.

consecutive windows that slide forward successively over time.

If x(n) is a waveform sampled data, it is possible to obtain the corresponding *N*-point DFT, X(k), as:

$$X(k) = \sum_{n=0}^{N-1} x(n) e^{-j2\pi \frac{k}{N}n}, \quad k = 0, 1, ..., N-1$$
(13)

The SW DFT, $X_m(k)$, by definition, follows from the (13), introducing, for the sampled waveform x(n) with length *L*, a window function w(n), generally rectangular, with size N < L:

$$X_m(k) = \sum_{n=0}^{N-1} x(n) w(n-m) e^{-j2\pi \frac{k}{N}n}, \ k = 0, 1, ..., N-1$$
(14)

where m is the starting time instant.

It is worth to observe that the aforesaid window function is very important both in terms of analysis resolution and of spectral leakage. Specifically, it is important to choose adequately the time duration T_w of the analysis window; in fact, for a sampling interval T_s , it is $T_w = NT_s$, and the frequency resolution of the spectrum is $f = 1/T_w$, so the selected value N has to be a compromise to obtain a good resolution both in time and in frequency. According to the IEC standard, for a rectangular window, the compromise is a time duration T_w equal to 10 and 12 cycles of fundamental period, respectively, for 50-Hz systems and 60-Hz systems [22,23].

Moreover, selecting a synchronized window with a T_w equal to an integer multiple of the waveform fundamental period, it is also possible to avoid the spectral leakage phenomenon, which is the most significant problem of the DFT method, because it impacts negatively on the analysis results accuracy. In this regard, the time duration recommended by the IEC standards becomes generally inadequate, especially in the presence of interharmonic components.

3.1 Endnote

^aNote that, as shown in [44], if fs is the chosen sampling rate, the Prony's method is able to detect a maximum component at a frequency of fs/4, whereas the ESPRIT method can estimate components up to fs/2. Then, the signal was under-sampled at 50 kHz before the application of SWEM and SWMEM.

Abbreviations

DER: distributed energy resources; DFIG: doubly fed induction generator; DFT: Discrete Fourier Transform; DG: dispersed generation; IEC: International Electrotechnical Committee; IECM: IEC standard method; MPPT: maximum power point tracking; PCC: point of common coupling; PQ: power quality; PVS: photovoltaic system; PWM: pulse-width modulation; SCIG: squirrel-cage induction generator; SG: smart grid; SW: sliding-window; ESPRIT: estimation of signal parameters by rotational invariance technique; SWEDEM: Three-step

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Sliding-Window ESPRIT-DFT-ESPRIT method; SWEM: Sliding-Window ESPRIT method; SWMEM: Sliding-Window Modified ESPRIT method; SWMPM: Sliding-Window Modified Prony method; SWPDPM: Three-step Sliding-Window Prony-DFT-Prony method; SWPM: Sliding-Window Prony method; THDi: current total harmonic distortion; WTS: wind turbine system.

Competing interests

The author declares that she has no competing interests.

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