# HF echo types revisited: aspect angle attenuation effects 

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#### Abstract

The high-spatial-resolution observations of the auroral E-region echoes by the Super Dual Auroral Radar Network (SuperDARN) HF radar at Pykkvibaer, Iceland considered in a previous study are re-examined. Both the spectral power and Doppler velocity of the E-region HF echoes exhibit strong dependence on the slant range and expected off-perpendicular magnetic aspect angle (aspect angle attenuation). We consider the aspect angle attenuation effects in identification of spectral HF echo types. It is argued that echoes with Doppler velocities close to the nominal value of the ion-acoustic speed $C_{s}(\sim 350 \mathrm{~m} / \mathrm{s})$ and echoes with velocities greatly exceeding the $C_{S}$ (up to $600 \mathrm{~m} / \mathrm{s}$ ) are more related in their generation mechanisms than previously thought. It is proposed to treat the echoes near the $C_{S}$ as aspect-angle-attenuated counterparts of the high-velocity echoes and that both types are generated directly by the modified two-stream instability with aspect angle attenuation resulting in the preferential phase velocity saturation at the $C_{s}$.


Keywords. Ionosphere (Auroral ionosphere; Ionospheric irregularities; Plasma waves and instabilities)

## 1 Introduction

Over the last decade, the HF coherent radar studies of the plasma waves in the auroral E region have been extremely successful in identifying fundamental differences between irregularity properties at decameter scales as compared to meter-scale irregularities observed with VHF radars (Milan and Lester, 1998, 1999, 2001; Jayachandran et al., 2000; Uspensky et al., 2001; Koustov et al., 2001, 2002, 2005; Makarevitch et al., 2001, 2002b,a, 2004; Milan et al., 2003, 2004; Makarevich, 2008; Carter and Makarevich, 2009). In particular, the HF echoes have been found to exhibit a wider


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variety of relationships between their spectral characteristics: spectral power, Doppler velocity and spectral width (Milan and Lester, 2001). This is often interpreted in terms of the decameter-scale waves generated through different and more numerous mechanisms (Milan and Lester, 2001; Koustov et al., 2002; Drexler et al., 2002; Drexler and St.-Maurice, 2005).

At VHF, the two predominant echo populations are referred to as Types I and II. Type I spectra are narrow and centered around the nominal value for the ion-acoustic speed $C_{S}$ in the $E$ region of $350 \mathrm{~m} / \mathrm{s}$, while Type II echoes have spectral widths of the order of $C_{s}$ and Doppler velocities much smaller than $C_{s}$. The Type I and Type II echoes are generally believed to be generated through the modified two-stream and gradient-drift plasma instabilities, respectively (e.g. Haldoupis, 1989).

Milan and Lester (2001) employed the data collected with the Super Dual Auroral Radar Network (SuperDARN) HF radar at Pykkvibaer, Iceland (also spelled as Thykkvibaer) to demonstrate that, in addition to the two populations resembling the VHF echo Types I and II, the HF radar observed 3 more populations. In particular, the HF radar regularly observed echoes with Doppler velocities substantially exceeding the nominal $C_{s}$ (up to $600 \mathrm{~m} / \mathrm{s}$ ) and exhibiting an unexpected variation with the L-shell angle $\phi$ (angle between the direction of observations and the expected direction of the plasma flow or magnetic L-shell). Later Milan et al. (2003) termed this population "super- $C_{s}$ " echoes. The echoes from population II showed the expected steady decrease of velocity with angle $\phi$, consistent with the so-called cosine law, i.e. that the line-of-sight (l-o-s) irregularity velocity should be proportional to the cosine of the flow angle $\theta$ (angle between the direction of observations and that of the plasma flow) assuming an approximately L-shell-aligned flow $\theta \cong \phi$. However, super- $C_{s}$ echoes showed an increase for small angles $\phi<35^{\circ}$ and a decrease at larger angles $\phi>35^{\circ}$ so that two separate populations have been introduced. A similar result has been obtained later by Makarevitch et al. (2002a) using the SuperDARN Syowa East HF radar observations but
no distinction between the two populations has been made in that study; they both were considered together and called the high-velocity echoes.

An interesting result obtained by Makarevitch et al. (2002a) was that the Doppler velocities of high-velocity echoes showed a clear decrease or attenuation with the expected off-perpendicular aspect angle $\alpha$ (angle between the direction of observations and the perpendicular to magnetic field line). This result was reminiscent of the echo power attenuation with the aspect angle established at all frequency ranges and similar to the irregularity velocity attenuation with the aspect angle reported at VHF (Ogawa et al., 1980; Nielsen, 1986; Kustov et al., 1994). However, an important difference was that the HF velocity at large aspect angles did not reach very small values near zero; the observed velocity minimum was $300-500 \mathrm{~m} / \mathrm{s}$. Interestingly, nearly simultaneous observations of the Doppler velocity at low VHF $(50 \mathrm{MHz})$ in the same study by Makarevitch et al. (2002a) clearly showed the expected behaviour (approaching zero) at large aspect angles. More recently, the VHF velocity dependence upon the aspect angle was re-examined using for the first time simultaneous and coincident measurements of the plasma drift velocity upon which the phase velocity is also strongly dependent; the VHF velocity attenuation was found to be even stronger than previously thought (Makarevich et al., 2006, 2007).

A common approach used in plasma irregularity studies is to employ spectral characteristic data (Power, Velocity, Width, and Skewness, if available) collected with coherent radars and analyse different populations in the Watermann scatter plots, e.g. W-V, P-V, and P-W, (Watermann et al., 1989; Hanuise et al., 1991; Milan and Lester, 2001) or, for large data statistics, similar point occurrence plots (Milan et al., 2003; Makarevich, 2008; Carter and Makarevich, 2009). As velocity depends strongly on the flow angle, often a velocity-L-shell angle (V-A) plot is also analysed. In such an approach it is tacitly assumed though that either the echoes are coming predominantly from locations with small aspect angles or that the aspect angle effects are not important. In other words, the aspect angle effects in identification of various echo types are not considered.

The aim of this study is to re-examine the HF echo populations by considering explicitly the effects arising from the power and velocity dependencies upon the aspect angle. It will be demonstrated that population I with velocities near the $C_{s}$ is closely related to population III with velocities exceeding the $C_{s}$ and that one can treat population I as aspect-angle-attenuated high-velocity echoes from population III.

## 2 Observations

In this study, we consider the data from the same two intervals as those selected by Milan and Lester (2001), i.e. two radar scans starting at 03:30 UT and 21:16 UT on 24 Febru-
ary 1997 of the SuperDARN Pykkvibaer HF radar. The radar scans through 16 azimuthal directions (radar beams $0-15$ ) in $\sim 3.25^{\circ}$ steps. The radar measures a 17-lag Auto Correlation Function from which estimates of the Doppler velocity, power, and spectral width of ionospheric echoes in 75 range bins for each of the 16 radar beams are obtained. The measured Doppler velocity corresponds to the 1-o-s irregularity velocity and is, by convention, positive for irregularities propagating towards the radar. The sounding frequency is usually fixed somewhere between 9 and 18 MHz . On 24 February 1997, the radar operated in the "myopic" mode designed to provide high-spatial-resolution observations of the short ranges where E-region backscatter normally occurs. In this scan mode, the range gate length is 15 km with the first range gate of 180 km . The radar frequency was 10 MHz during both intervals of interest. In addition to the original study by Milan and Lester (2001), the reader is referred to an earlier study for more details on the radar's technical characteristics and operations (Milan et al., 1997).

Figure 1 shows the scatter plots of (a) and (c) the spectral width and (b) and (d) the L-shell angle versus the Doppler velocity as measured by the SuperDARN Pykkvibaer HF radar during the two intervals of interest. This figure is almost identical to Fig. 6, panels (b), (c), (e), and (f), of Milan and Lester (2001). The minor differences in a small number of echoes being excluded are due to the slightly different data selection criteria employed as described below. All groundand sea-scatter echoes were excluded using the standard SuperDARN criteria of low width and velocity. The F-region echoes at farther ranges were also excluded using the variable range threshold introduced later in Figs. 2 and 3. The additional echoes excluded had small velocities of the same polarity as the expected F-region convection flow for a particular interval of interest: positive in (a) and (b) and negative in (c) and (d). They also referred to farther ranges of 630990 km , had the same velocity polarity as the majority of echoes at these ranges and opposite polarity to that of echoes at closer ranges. The excluded echoes were therefore almost definitely of the F-region origin.

In Fig. 1 three populations of the E-region echoes are identified. These populations and their description below are consistent with those given by Milan and Lester (2001). The echoes from population I have smaller widths and velocities near the nominal $C_{s}$ of $350 \mathrm{~m} / \mathrm{s}$. They are observed at small L-shell angles $\phi<30^{\circ}$, Figs. 1b and d. The echoes from population II are only present in the first scan, Figs. 1a and b. They have smaller velocities which exhibit a clear decrease with angle $\phi$, Fig. 1b. These two populations have been identified by Milan and Lester (2001) as Type I and Type II echoes according to VHF classification. The echoes with higher velocities up to $600 \mathrm{~m} / \mathrm{s}$ are also present in Fig. 1; they are referred to as population III. In both examples presented in Fig. 1, these echoes have a range of widths 30$200 \mathrm{~m} / \mathrm{s}$ and an interesting velocity variation with the L-shell angle $\phi$ with velocity maximum reached near $\phi=30^{\circ}$. This is


Fig. 1. Scatter plots of (a) and (c) the spectral width and (b) and (d) the L-shell angle versus Doppler velocity for two intervals on 24 February 1997. Also shown are the echo populations I, II, and III identified in a previous study (see text for details).
contrary to behaviour of population II echoes whose velocities steadily increase towards the smallest observed angles $\phi$.

To investigate the three populations in further detail, in particularly, considering the effects of aspect angle attenuation of the spectral power and Doppler velocity, Fig. 2 presents the data from one of the two interval shown in Fig. 1. As the second interval 21:16-21:18 UT contained only 2 populations, it is analysed first. The first two panels show the range-versus-beam spatial plots colour-coded in (a) the spectral power and (b) the Doppler velocity. For further analysis, standard power-range correction was performed by assuming a $r^{-3}$ power decrease with slant range $r$ (e.g. Greenwald et al., 1975; Makarevich, 2008). The spatial plots clearly show the E-region echo band at near ranges $r=405-900 \mathrm{~km}$ which curves away from the radar for larger beam numbers. The sense of curvature is the same as those of zero aspect angle lines at 110 km shown by the yellow curves for 3 selected electron density profiles. The aspect angles were computed for the frequency of observations of 10 MHz assuming that the radar beam undergoes refraction
as described by Uspensky et al. (1994). The spectral power maxima along each beam (black dots) are located in the middle of the band, with the bottom line representing well most maxima. A similar representation of the power maxima locations by the model aspect angle lines has been employed for various VHF and HF radar systems (e.g. Koustov et al., 2001, 2002; Makarevitch et al., 2001, 2002b, 2004).

The echoes at farther ranges $600-990 \mathrm{~km}$ are more patchy and their velocity is often of the opposite sign to that of the near-range echoes (e.g. in beams $0-3$, cells with white diagonal) or much smaller than that observed at near ranges for the same beams (e.g. in beams 4-7). In addition, the spectral power clearly shows a decrease with range at the largest ranges within the E-region band, while a steady power increase with range is observed at farther ranges $630-990 \mathrm{~km}$ in beams $0-3$ that have most coverage in range. The above signatures clearly differentiate between the echoes of the Fand E-region origin, which is highlighted by the black-white histogram-style line separating the F- and E-region bands. In the following analyses, the F-region echoes at ranges above the black-white line were not considered.


Fig. 2. Panels (a) and (b) show, respectively, the spectral power and Doppler velocity maps for 21:16-21:18 UT on 24 February 1997. The cells with white diagonal in panel (b) represent negative velocities. The black-white line indicates the chosen boundary between the F- and E-region backscatter bands. The coloured vertical lines show the 3 selected beams. The black dots show the power maxima along each beam. The thick yellow curves are the lines of zero aspect angle at an altitude of 110 km assuming electron density profiles with the density maxima (3.7, 4.2, 4.7) $\times 10^{4} \mathrm{~cm}^{-3}$ for the top, middle and bottom curves, respectively. Panels (c) and (d) show, respectively, slant range profiles of the spectral power and velocity along the 3 selected beams. The digits show the beam numbers. The vertical dashed lines show the range of maximum power along each beam. Panels (e) and (f) are the scatter plots of (e) the spectral width and (f) the L-shell angle versus velocity. The data points are colour-coded in spectral power as given by the colour bar in panel (a). The horizontal dashed line in (c) and (d) and vertical dashed line in (e) and (f) show the nominal ion-acoustic speed of $350 \mathrm{~m} / \mathrm{s}$. The coloured lines in (e) and (f) connect the data points for the 3 selected beams (the same as in panels c and d ).

In the next presentation, the power (c) and velocity (d) data from 3 selected beams are considered. These beams are indicated by the vertical lines in Figs. 2 a and b and the corresponding beam numbers are also shown by the digits in Fig. 2d. The important feature here is that the power curves for beams 2 and 8 have a well-defined bell-like shape, with maxima at the ranges 495 km and 585 km , respectively, shown by the vertical dashed lines. A similar feature is observed in beam 12, but with a dip that occurs near $r=630 \mathrm{~km}$.

In the velocity data, Fig. 2d, for each beam, the velocity reaches a maximum at a range which is close to that of the power maximum shown by the vertical dashed line. An important feature for this study is that, for all 3 beams, the velocities at the nearest ranges where the echoes were observed (430-630 km) are close to each other and to the nomi-
nal ion-acoustic speed $C_{s}$ of $350 \mathrm{~m} / \mathrm{s}$ shown by the horizontal dashed line. In beam 2, all points are close to $C_{S}$, while in beam 8 only two closest ranges (leftmost triangles), at which power is at or close to its minimum, have velocities near the $C_{s}$. Similarly, in beam 12, the points that are closest to the $C_{s}$ in velocity are observed at $\sim 630 \mathrm{~km}$; these are the points near the power minimum. Moreover, on the other side of the power maximum (larger ranges) velocity and power both decrease with range increasing until velocity reaches $\sim 400 \mathrm{~m} / \mathrm{s}$, i.e. values that are close to the $C_{S}$ dashed line.

Figures 2 e and f are identical to Figs. 1c and d, but with some important additional information provided. Thus all points are colour-coded in power and the data points in Fig. 2f from the 3 selected beams are highlighted by the symbols and connecting lines (the same as in Fig. 2d). The


Fig. 3. The same as Fig. 2 but for 03:30-03:32 UT and with the reversal in velocity polarity in panels (b), (d), and (f).
yellow-to-red points with the largest power have largest velocities of $550-600 \mathrm{~m} / \mathrm{s}$, which is obvious in both Figs. 2e and f. As power decreases so does velocity, which is most obvious for points at small L -shell angles $\phi=10^{\circ}-35^{\circ}$ including the data in beam 8 (triangles). The same feature as in Fig. 2d is observed here, i.e. that velocities with smaller power are near the $C_{S}$ (vertical dashed line in Figs. 2e and f).

The key feature for this study in Fig. 2 f is that the points near the $C_{s}$ at $\phi=10^{\circ}-35^{\circ}$, which have been termed population I in Fig. 1d, no longer seem to be completely unrelated to high-velocity population III with velocities near $600 \mathrm{~m} / \mathrm{s}$. On the contrary, as highlighted by the beam 8 and 12 data (triangles and diamonds, respectively) and other similar groups of points, both populations appear to be simply two "extreme cases" of the same common group of points, with points near $350 \mathrm{~m} / \mathrm{s}$ and $600 \mathrm{~m} / \mathrm{s}$ connected by lines that often have several, evenly-spaced points in between, for example for beam 8 (triangles) or for the lower branch of the beam 12 data (diamonds).

We next analyse the data from the other interval, which was previously presented in Figs. 1a and b. Figure 3 has the same format as Fig. 2 but with the polarity of the Doppler velocities reversed for convenience in panels (b), (d), and (f). In panels (a) and (b), echoes at farther ranges are less patchy
than in Fig. 2. However, other features that allowed us to distinguish between the E- and F-region scatter bands are still present, including the predominantly different polarities and different magnitudes (for the same beam) of the l-o-s velocities measured.
Figure 3a shows that the primary power maxima (black dots) are in the middle of the band, similar to Fig. 2a, but here they do not appear to be described by a single aspect angle curve. Rather, they fall into 2 major groups with the maxima from the first (second) group observed in beams 0-3 (4-8) and appearing close to the top (middle) yellow curve. The first (second) group is clearly associated with the blue (red) cells in Fig. 3b. The red cells in Fig. 3b are high-velocity echoes of population III, similar to Fig. 2.

Population I is also present at shorter ranges (yellow and green cells in Fig. 3b below the bottom yellow curve), while the new low-velocity population II (blue and green cells in Fig. 3b) is observed between the high-velocity echoes (red cells in Fig. 3b) and the F-region band. The three clusters of points are also evident in Fig. 3e: with velocity magnitudes (I) near $350 \mathrm{~m} / \mathrm{s}$, (II) below $200 \mathrm{~m} / \mathrm{s}$, and (III) above $500 \mathrm{~m} / \mathrm{s}$.

The most important feature for this study is also present here, i.e. that the points at the shortest ranges in beams 5 and 8 have velocities close to the $C_{S}$, Figs. 3 c and d. One
should note, however, that for beam 2 it is the secondary maximum that has been used as reference ( 465 km , indicated by the black vertical dashed line) since the primary maximum at 555 km referred to population II (plateau in velocity in Fig. 3d). Similar local maximum and inflection point were observed in the beam 5 and 8 data, respectively, at 670 and 840 km . They also referred to population II. In beam 2, all velocities near the secondary power maximum at 465 km were close to $C_{s}$.

The difference between Figs. 2d and 3d is that on the other side of power maximum (toward increasing range) there is a sharp drop-off in velocity in beams 2 and 5 . This is contrary to what is seen in Fig. 2d in beams 2 and 12, where velocity was gradually approaching $C_{s}$ at farther ranges. The velocity variation along beam 8 is different as it does not decrease significantly at ranges beyond 630 km staying near $550 \mathrm{~m} / \mathrm{s}$, Fig. 2d. However, one can argue that had there been echoes at $r>675 \mathrm{~km}$, their velocities would also have shown a decrease to the $C_{s}$ values.

Interestingly enough, Fig. 3d shows that if one considers even farther ranges of near 800 km for beam 5, the velocity does return to the $C_{S}$ level. In addition, velocity is close to $C_{S}$ in beam 8 at farther ranges. However, in this beam it is rather difficult to say whether these echoes belong to population I or population II as the difference between the velocity plateau near 800 km and the $C_{s}$-level is small (unlike in beams 2 and 5). This feature is discussed later in Sect. 3.

From Fig. 3f one can conclude that, similar to Fig. 2f, points at smaller angles $\phi=10^{\circ}-45^{\circ}$ near $C_{s}$ form a common group with points near $600 \mathrm{~m} / \mathrm{s}$. The echo power is progressively smaller for points in the beam 5 and 8 data (triangles and diamonds, respectively) as velocity gradually decreases until it reaches the $C_{s}$ level so that choosing any threshold velocity and/or power to separate the two populations appears to be rather artificial. Thus Fig. 3 shows that, similarly to Fig. 2, populations I and III do not appear to have a sharp boundary between them as far as velocity variation with range is concerned. This is in contrast with transition between populations I and II.

## 3 Discussion

The echo power decrease with the aspect angle, often referred to as the aspect angle power attenuation, is a wellestablished property of coherent radar backscatter from ionospheric irregularities in the auroral E region (e.g. Haldoupis, 1989; Sahr and Fejer, 1996, and references therein). A similar velocity decrease with the aspect angle has also been reported (Ogawa et al., 1980; Nielsen, 1986). The aspect angle attenuation of power has been found to occur at all frequency ranges with comparisons between observations at different frequencies suggesting that echoes at low VHF ( 50 MHz ) are less aspect sensitive than those observed near 150 or 400 MHz (Haldoupis, 1989).

The HF observations have suggested that decameter-scale waves are perhaps even less aspect sensitive, with echoes regularly observed at the expected aspect angles of $\alpha \cong 5^{\circ}$ (Makarevitch et al., 2002b,a) and often at very large aspect angles of $\alpha>10^{\circ}-15^{\circ}$ (Milan et al., 2004). One should bear in mind though that none of the above-cited studies at HF have performed rigorous ray-tracing simulations using electron density measurements to estimate the aspect angles. The majority of aspect angle estimates were based on a simple geometric optics model described by Uspensky et al. (1994) that was also employed in this study. In this approach, the power and velocity variations with range can be described in terms of the expected aspect angles at a given height for each range cell assuming either no refraction (geometrical or rectilinear aspect angles) or some electron density profile ("real" aspect angles). Several profiles are often tried to determine which profile results in a better match between the power maxima and locations of zero aspect angles (e.g. Koustov et al., 2001; Makarevitch et al., 2004).

For the SuperDARN Pykkvibaer HF radar, the geometrical aspect angles at 110 km do not reach zero anywhere in the near field-of-view (see recent study by Makarevich, 2008, and their Fig. 1). At the same time, this radar regularly observes the E-region echoes at near ranges (Milan and Lester, 2001; Makarevich, 2008), which implies appreciable refraction and electron density for majority of observations. In this study, 3 electron density profiles were used to determine whether power variation with range can be reasonably described in terms of expected aspect angle, Sect. 2. Given that the two considered intervals referred to two significantly different time sectors, it is not surprising that the power maxima locations were different and described well by the two aspect angle models that were not exactly the same.

In the past, much debate has been generated about whether all "true" aspect angles in VHF observations are in fact small $\left(<1^{\circ}-2^{\circ}\right)$, whereas the corresponding "real" aspect angles are significantly overestimated (see review paper by Moorcroft, 2002, and references therein). In other words, the effects of refraction, reflection and multiple scattering at VHF were argued to be regularly underestimated. Certainly, these effects are expected to be even larger at HF. Theoretically, the waves at large aspect angles should be rapidly destroyed by diffusive damping as electrons that are highly mobile along magnetic field lines short out the fields supporting the waves (e.g. Farley, 2009). However, nonlinear and nonlocal processes may provide some support to the waves at large aspect angles through an increase in the scattering of electrons (Hamza and St-Maurice, 1995) and through a mode conversion at a spatial discontinuity in the aspect angle (Drexler and St.-Maurice, 2005), respectively, with the latter scenario being applicable mostly to decameter waves.

In the present study, we focus on the power and velocity variation with range bearing in mind that it can also be described in terms of the expected "real" aspect angle. The exact values in aspect angle (including maximum reached) are
not important for this study, and the model presented later in this section only considers aspect angles below $2^{\circ}$, i.e. it is within the small "true" aspect angle paradigm described above.

The other interesting feature of HF observations is that that echoes with unusually large Doppler velocities at and above $600 \mathrm{~m} / \mathrm{s}$ are not that uncommon (Milan and Lester, 2001; Milan et al., 2003; Makarevich, 2008). Termed "super- $C_{s}$ " and high-velocity echoes by Milan and Lester (2001) and Makarevitch et al. (2002a), respectively, to distinguish from echoes near the nominal $C_{s}$ values of $\sim 350 \mathrm{~m} / \mathrm{s}$ typical of the VHF and UHF backscatter, they have been originally found to occur at relatively low L-shell angles of $\phi<45^{\circ}$. More recently however, similar echoes near $600 \mathrm{~m} / \mathrm{s}$ have been found to occur at all L-shell angles (all 16 beams) sampled with a single HF radar (Makarevich, 2008). This has been attributed to the two-stream plasma wave generation within the instability cone (low flow angles) with possible energy transfer to waves at large flow angles.

In the present study, it was demonstrated that the two populations of HF echoes near 350 and $600 \mathrm{~m} / \mathrm{s}$ are more closely related than perhaps thought previously as the echoes with "intermediate" power and velocity values were regularity observed, Figs. 2f and 3f. Both the HF power and velocity behaviour were typical of those observed in other studies that employed oblique-sounding auroral HF radars (Koustov et al., 2001; Makarevitch et al., 2002b) with the power and velocity reaching their respective maxima at ranges $r_{P}$ and $r_{V}$ (with $r_{P}$ typically being close to $r_{V}$ ) and decreasing with range increasing/decreasing from $r_{P}$ or $r_{V}$. Such a behavior is believed to be related to the power and velocity attenuation with the aspect angle as demonstrated by numerous previous studies at HF (Koustov et al., 2001, 2002; Uspensky et al., 2001; Makarevitch et al., 2001, 2002b, 2004) and as described below.

The aspect angle varies with range along each radar beam reaching a minimum at some range $r_{0}$. These ranges for zero aspect angle for different electron densities were shown by the yellow curves in Figs. 2 and 3. The linear fluid theory of auroral irregularities predicts that the growth rate and the phase velocity should be maximized at $r_{0}$ and decrease with the aspect angle increasing in magnitude on both sides of $r_{0}$. This is exactly what is observed for power in Figs. 2 and 3 except that in some beams there is a secondary power maximum at near ranges (e.g. at $r \cong 540 \mathrm{~km}$ in beam 12 in Fig. 2c). This secondary power maximum most likely occurs since the echoes at these radar cells are generated through a different mechanism. The fact that velocity near 540 km in beam 12 (and adjacent beams) is also lower than the nominal value of $C_{s}$ of $350 \mathrm{~m} / \mathrm{s}$ and nearly constant with range at $505-585 \mathrm{~km}$ suggests that these echoes may simply belong to population II echoes that are only observed at small L-shell angles for this interval (unlike those in Fig. 3). As was noted in Sect. 2, at these small L-shell angles it is rather difficult to distinguish between the populations I and II. In this beam, however, the
data suggest that only points at $585-630 \mathrm{~km}$ near the power minimum should be classified as population I. The distinction is clearer at larger L-shell angles $\phi \cong 40^{\circ}$ (beam 5) for the other interval where a gap in velocity was observed between points in Figs. 3d, f. Hence one can argue that it is incorrect to lump all points near and below $350 \mathrm{~m} / \mathrm{s}$ into one population I as it has been done in Fig. 1d.

The analysis of observations presented in this study shows that the echoes from population I with velocities near the $C_{S}$ may be interpreted as aspect-angle-attenuated echoes from population III with velocities near $600 \mathrm{~m} / \mathrm{s}$ rather than as a stand-alone population. The spectral power showed a gradual decrease as velocity was decreasing from $\sim 600 \mathrm{~m} / \mathrm{s}$ to $\sim 350 \mathrm{~m} / \mathrm{s}$ along the same beam at small $\phi$. This often occurred on both sides of the maximum in the power profile (e.g. beam 12 in Fig. 2d). Also, the echoes with the largest spectral powers generally had the largest velocities, Figs. 2 f and 3 f .

Notwithstanding the importance of this interpretation, one should emphasise that statistically-speaking populations I and III are different. That is they are evident as separate peaks in either 1-D velocity distributions or in 2-D distributions in the $\mathrm{W}-\mathrm{V}$ and $\mathrm{P}-\mathrm{V}$ point occurrence plots (see Milan et al., 2003, and their Fig. 6), although the troughs between the peaks are not deep, which is consistent with the present study. This means that there is a preferentially observed velocity near the $C_{s}$. So the question why there are two statistically separate populations is still valid, although it perhaps should be reformulated as: Why does the aspect angle attenuation of HF velocity stop near the $C_{s}$ rather than continuing all the way to very low values near zero, which is observed at VHF and UHF (e.g. Ogawa et al., 1980; Foster et al., 1992), or stopping somewhere between 350 and $600 \mathrm{~m} / \mathrm{s}$ ?

To discuss this issue in more detail, Fig. 4 shows two models of the phase velocity variation with the flow and aspect angles. The red surface shows the phase velocity calculated using the expressions from the linear fluid theory (e.g. Fejer and Kelley, 1980). In these calculations we used the typical values of collision frequencies $v_{i}=726 \mathrm{~s}^{-1}$ and $v_{e}=31243 \mathrm{~s}^{-1}$ and a convection velocity of $1000 \mathrm{~m} / \mathrm{s}$ that have also been used by Makarevich (2008). The velocity shown was normalised to the selected convection speed so that the $C_{s}$ plane is at 0.35 . The lowest achievable velocity in this approach is the $C_{s}$, which is obtained from the zero growth rate condition (when wave amplitude is saturated). The red half-oval at the bottom (i.e. at the $z=V=0$ plane) is the projected red velocity surface; it shows the limits in flow $\left(\theta_{0}\right)$ and aspect $\left(\alpha_{0}\right)$ angles on the wave generation in this regime. The range of aspect angles at which linear wave modes can be generated is largest along the plasma flow, $\alpha \leq \alpha_{0}(\theta=0) \cong 2^{\circ}$. It then decreases and reaches zero at $\theta=\theta_{0} \cong 60^{\circ}$, at which point the waves can only be generated perpendicular to the magnetic field $\alpha=\alpha_{0}\left(\theta=\theta_{0}\right)=0$. At $\theta>\theta_{0}$, no linear wave modes should exist. This is consistent with narrowing of the aspect angle cone with flow


Fig. 4. Surfaces of the phase velocity model dependence upon the flow and aspect angles. The red (blue) surface shows the model assuming that the phase velocity reaches minimum at the ion-acoustic speed $C_{s}$ (cosine component of the ion-acoustic speed $C_{S} \cos \theta$ ) represented by the plane (thick curves).
angle increase demonstrated experimentally by Makarevich (2008). One should also note that the electron drift velocity used here is somewhat large ( $1000 \mathrm{~m} / \mathrm{s}$ ); for a smaller velocity of $500 \mathrm{~m} / \mathrm{s}$ the largest flow and aspect angles achievable in the linear regime would be smaller: $\theta_{0} \cong 30^{\circ}$ and $\alpha_{0}(\theta=0) \cong 1^{\circ}$ (Makarevich, 2008).

The population III echoes in this model would correspond to the top ridge of the red surface at $\alpha=0$. The variation with the flow angle is not exactly consistent with the observations at the maximum measured velocity was observed at $\theta \cong 35^{\circ}$ (assuming $\theta=\phi$ ) rather than at $\theta=0$. This may indicate a significant rotation of the direction at which the maximum velocity is observed in the E-region. The population I in this model is represented by the bottom edge of the red surface at $C_{s}$. The populations I and III are connected by the black bell-shaped lines for each fixed flow angle value. A single bell-shaped line in the $\alpha-\theta$ space would roughly correspond to the data from a single radar direction (beam) in Fig. $2 f$ (in the $r-\phi$ space).

In the past, various mechanisms were employed to explain the observations of the high-velocity echoes at VHF (known as Type IV echoes) and more recently at HF. These mechanisms included the electron heating by the strong electric fields (Fejer et al., 1986), electrostatic ion cyclotron waves (Villain et al., 1987), strong gradients in the electron density (St.-Maurice et al., 1994), and convective nature of the twostream instability at decameter scales (Drexler et al., 2002). The difference between the VHF and HF observations appears to be that the high-velocity echoes are observed quite regularly by the radars observing at low flow angles (Milan et al., 2003; Makarevich, 2008) and that the echo characteristics do not match those of the VHF Type IV echoes (Moorcroft, 2002).

Importantly, Fig. 4 shows that both populations can be generated directly by the modified two-stream instability (even if marginally in case of population I, i.e. when the growth rate is only slightly above zero) when plasma convection speeds are sufficiently (but not unrealistically) large. The aspect angle attenuation results in the phase velocity being significantly reduced, with the smallest value $\left(C_{s}\right)$ reached at the red half-oval boundary. Thus in this approach one can successfully explain the preferential detection of echoes with velocities near the $C_{S}$ through the lower limit on the aspect angle attenuation of the phase velocity. However, a still outstanding question is: why this is not observed at higher frequencies. Multi-frequency UHF/VHF/HF measurements of the Doppler velocity at small flow angles are required to resolve this issue.

The blue surface in Fig. 4 shows an alternative model that assumes that the aspect angle attenuation of velocity does continue even beyond the aspect angle cone, until velocity reaches $C_{S} \cos \theta$ (two thick curves). This particular model is suggested here to give some additional insight into our results as well as into some of the previous results. As mentioned, in our observations the Doppler velocity of echoes from populations I or III did not reach below $C_{s}$. In other words, no echoes were observed that would have fallen onto the blue surface below the $C_{s}$ plane. However, the echoes with lower velocities in Fig. 3f (population II) did show a cosine-like variation. The HF echoes at the lowest angles $\phi<30^{\circ}$ could have been assigned to either population I or II, but extrapolating the HF velocities at $\phi=30^{\circ}-60^{\circ}$ for echoes from population II in Fig. 3f would give a coefficient of proportionality close to $350 \mathrm{~m} / \mathrm{s}$. The variation in range did not appear to cause any appreciable change in velocity for this population (Fig. 3d) with most points being away from the power maximum, which implies large aspect angles. This population did not appear to be related to either population I or population III as there were no points connecting population II to the other two when observed along the same beam. Instead, a sharp drop-off in velocity was observed in Fig. 3d, which was also accompanied by a sharp change in the rate of power decrease with range. One can conclude that the population II velocities can be described by the bottom edge of the blue surface in Fig. 4 but not by the blue surface itself.

This result appears to be consistent with that of Bahcivan et al. (2005) who employed the imaging radar system at 30 MHz in Anchorage, Alaska to demonstrate that the Doppler velocity variation with the flow angle was consistent with the $C_{s} \cos \theta$ model suggested in that study. Later Bahcivan and Hysell (2006) developed a theoretical model that provided a possible explanation of these results. Another result of Bahcivan et al. (2005) was that the measured velocity disagreed greatly with that computed using the linear fluid theory formulas with aspect angle variation taken into account, although no direct comparisons have been presented. Given large uncertainty in the aspect angle estimates and altitude-integration effects resulting in larger effective aspect
angles even at 140 MHz (Uspensky et al., 2003), it is possible that the large bulk of their observations at 30 MHz , where the altitude-integration effects are expected to be stronger, was performed at relatively large aspect angles. Our observations of echoes from population II that occurred at ranges away from the power and velocity maxima are consistent with the $C_{s} \cos \theta$ model, which suggests that the model possibly applies to observations at large aspect angles as illustrated in Fig. 4. The present study thus provides an alternative interpretation of the observations consistent with the $C_{S} \cos \theta$ model either at 10 MHz or at 30 MHz .

Finally, in this study, a case was made for a continuous transition between the echoes from populations I and III associated with a gradual change in the expected aspect angle. Another possibility is a spatial convolution of the two distinct echo types observed, with preponderance of $C_{s}$ ("super- $C_{s}$ ") echoes at shorter (farther) ranges. Within this scenario, there are two cases: the two types of echoes may originate from two different heights or they may occur in the same scattering volume with different probabilities (adding to 1 ) depending on the range. The second case does not appear to be supported by observations as probabilistic nature of this case implies more random distribution of velocities within each range cell and hence more irregular velocity variation with range. One also expects that, on occasions, $C_{s}$ echoes may be observed where most "super- $C_{s}$ " echoes occur and vice versa. Nothing of the kind is observed in either of the two radar scans presented in Figs. 2 and 3 and, in general, for the entire event of interest.

In the first case, in which the echoes are coming from two different heights, one expects that the spectral width will be enhanced somewhere in the middle between the ranges where $C_{s}$ and "super- $C_{s}$ " echoes predominantly occur. In other words, the spectral width at "intermediate" velocity and power values should be enhanced. Figures 2 e and 3 e indeed show that the width at velocities $\sim 500 \mathrm{~m} / \mathrm{s}$ is somewhat larger than at smaller or larger velocities (near 0 and $600 \mathrm{~m} / \mathrm{s}$ ).

To investigate this possibility in more detail, Fig. 5 presents the elevation angle and spectral width measurements for the two intervals of interest in the same format as Fig. 2c. The power profiles are also shown in panels (a) and (c) for reference. The ranges of power maxima are shown by the dashed lines. The spectral width is expected to be enhanced between the power maximum and minimum ranges, which are also approximately the ranges where velocity is at maximum and closest to the nominal $C_{S}$, respectively. Indeed, the width reaches a maximum on the "ascending leg" of the power profile in beam 8 (5) for the first (second) interval at a range $555 \mathrm{~km}(535 \mathrm{~km})$. The width is also at (near) a local minimum at the dashed line in beam 12 (8) at a range 750 km ( 660 km ) for the first (second) interval. However, the width variation with range is mush less smooth than that of power or velocity and the local width maxima reached are only 200$250 \mathrm{~m} / \mathrm{s}$. In addition, one can argue that the width should be


Fig. 5. Elevation angle (a) and (c) and spectral width (b) and (d) variations with range for the two intervals of interest. The measurements in two selected beams (the same as the last two from Figs. 2c, d and $3 \mathrm{c}, \mathrm{d}$ ) are shown by triangles and diamonds. The power profiles (thin lines and symbols) scaled down by a factor of 2 are also shown in panels (a) and (c).
smaller at small aspect angles (large power and velocity) and increase with aspect angle (as power and velocity decrease) (Hamza and St.-Maurice, 1993), so that the fact that width has a local minimum at a range of maximum power does not necessarily support the spatial convolution scenario.

Moreover, the elevation angle measurements do not show any distinct differences between the ranges where $C_{s}$ and "super- $C_{s}$ " echoes predominantly occur, i.e. near 480 km and 595 km ( 645 km and 750 km ), respectively, in beam 8 (12) for the first interval, Fig. 5a. The observations in beam 12 do show a $1^{\circ}$ change in elevation angle at a range of 705 km , i.e. in the transitional region between $C_{s}$ and "super- $C_{s}$ " echoes, which would correspond to a change in virtual height of 10 km at these ranges. This would appear to be a significant difference. However, one should note that the elevation angle values were higher than expected for the E-region measurements; this is most likely due to uncalibrated nature and/or the $2 \pi$ ambiguity in the phase measurements and that any "raw" estimates of height (and even of height difference) should be taken with caution. For example, at these ranges the difference between virtual heights of the adjacent $15-\mathrm{km}$ range gates is 8 km . Hence in this analysis, we are interested only in the relative changes with range. In this sense, the differences in beam 12 are much more pronounced between observations at shorter ranges near 540 km and farther ranges
$630-765 \mathrm{~km}$, which supports our earlier conjecture that the echoes at these short ranges had a different origin. The differences in the elevation angle would be expected to be consistently more significant than the present $1^{\circ}-2^{\circ}$, for the first case with echoes coming from two different heights to be a preferred option.

Furthermore, the maximum spectral width values reached were somewhat smaller than those expected from the difference in typical velocities of the two populations. Thus, Danskin et al. (2004) demonstrated that a spectral width of $200 \mathrm{~m} / \mathrm{s}$ typically corresponds to a difference in velocity between two spectral types of $\sim 150 \mathrm{~m} / \mathrm{s}$ (see their Fig. 7). This is significantly lower than typical differences of $600-350=250 \mathrm{~m} / \mathrm{s}$ observed in the present study. We conclude from the above analysis that it is less likely that the trends observed are mostly due to the spatial convolution of two distinct types.

## 4 Conclusion

The HF echoes with Doppler velocities near the nominal value of the ion-acoustic speed $C_{s}$ of $350 \mathrm{~m} / \mathrm{s}$ and echoes with substantially greater velocities near $600 \mathrm{~m} / \mathrm{s}$ may represent two sides of the same phenomenon. Analysis of the spectral power and Doppler velocity variations with range shows that the echoes near $C_{s}$ can be treated as aspect-angleattenuated counterparts of the high-velocity echoes. This suggests that the HF echoes from both populations are generated through the same mechanism with the linear fluid formalism describing observations reasonably well when a lower limit on the phase velocity is considered.

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