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Ranking and transformation error assessment of shear strength parameters correlations

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Abstract

Shear strength is responsible for soil ability to withstand applied loads and considered the most important engineering properties of soil. Shear strength can be measured directly in the field or in the laboratory, however many empirical correlations were developed to predict shear strength from simple basic and index properties of soil. The main reasons for using these correlations that direct measurements are costly, time consuming, and not always applicable. The correlated shear strength parameter deviates from its actual value, by a transformation error, causing larger uncertainty that affects the overall design. The current commonly used transformation error values have shortcomings that warrant the need for further research. To offer avenues for improving the current values, a database contains geotechnical investigation results for 5087 boreholes collected from Egypt, UAE, Iraq, and Indonesia were created. The database served to assess inherent variability, measurement error, and transformation error more consistently. The most commonly used empirical correlations were ranked based on amended Theil inequality coefficient method, then the transformation error was determined using uncertainty propagation combined with the second moment probabilistic method (RUP-SMP). The adapted methodology can be used as standard procedures to evaluate different empirical correlations for other geotechnical properties. Framework for combining the predicted transformation error with other uncertainties was introduced to determine the overall uncertainty in shear strength parameters.

Keywords: Geotechnical variability, Transformation error, Empirical correlations evaluation, Correlations ranking, Uncertainty propagation

Background

In contrast to other engineering materials, soil resist applied loads by means of friction and cohesion between particles that is known as shear strength. The shearing resistance of soil depends mainly on soil composition, stress history, strain, strain rate, voids ratio, cohesion, and friction between particles [17]. A functional form that considers all these parameters are too complex and several simplifications were done to assess the shear strength of soil. The most widely used functional form of shear strength is the Mohr-Coulomb equation, which simplify the soil shear strength to depend only on cohesion, internal friction angle, and confining stress [2].



Soil cohesion and internal friction angle, the shear strength parameters, can be measured directly in the field or in laboratory. Direct measurement of shear strength parameters is costly, time consuming, and not always applicable [23] that necessitate the development and use of empirical correlations. These empirical correlations were derived from data fitting for a specific site conditions that may cause deviation of the correlated soil properties if used in other sites. This deviation of the correlated values from its real value is known as transformation error. Transformation error is considered one of the main three sources of uncertainty in geotechnical properties. The other sources are inherent variability and measurement errors. Inherent variability is originated mainly from different in situ geologic processes in contrast to measurement error that is caused by random sampling and testing characteristics [24].

For major geotechnical projects, such as offshore piles, deterministic design is not always enough and further consideration of geotechnical uncertainties is deemed necessarily [22]. Several methods were proposed to consider these uncertainties, but its implementation is a challenging task due to the difficulty of assessing the uncertainties in soil properties. The current commonly used transformation error values had shortcomings that warrant the need for further research. Main shortcomings are: it didn't cover all soil types; it covered only a very limited amount of empirical correlations; it depends mainly on literature values; and different sources of uncertainties were combined although it was originated from different soil conditions. To overcome these shortcomings and to offer avenues for improving the current transformation error values, a database contains geotechnical investigation results for 5087 boreholes collected from Egypt, UAE, Iraq, and Indonesia was created. The database served to assess inherent variability, measurement error, and transformation error more consistently. In addition, it offered unified shear strength parameters estimation from different correlations.

In this paper, the most commonly used shear strength correlations were ranked based on both position conformity and trend conformity using amended Theil inequality coefficient (ATIC) method as proposed by Song et al. [28]. ATIC method considers both trend and position conformities between the correlated and measured values enabling more accurate ranking than other statistical ranking measures. Correlations ranking served to assess the most credible correlation to be used for shear strength parameters determination at specific site condition. The transformation error was determined using rule-based uncertainty propagation combined with second moment probabilistic method (RUP-SMP). The deduced transformation error values can be used as guidance in the absence of other, more accurate, site-specific values. Framework for combining the predicted transformation error with other uncertainties was introduced that can be used to determine the overall uncertainty of shear strength parameters.

Materials and resources

Geotechnical database

Subsurface investigation reports were collected from reputable geotechnical firms in Egypt, UAE, Iraq, and Indonesia. The collected reports contained field and laboratory tests results for more than 35,000 boreholes collected during the last 3 years. The most recent boreholes were classified based on project type and completeness of information. The most reliable boreholes were entered with consistent and unified units

into the geotechnical database. The data was checked with the source data to ensure the quality and consistency of information. Checking was carried out by comparing between entered and source data to insure that the required data are correctly and completely entered. Checking took into consideration the mandatory fields, type of data, and needed data for the research. The database was designed to have 98 tables to enable future extension of the entered data. To serve the current research, only 27 tables were filled with 5087 boreholes. In addition, 2 extra tables were entered for data quality checking to store the path of the borehole documents.

Shear strength correlations

Shear strength correlation development was started as early as forty of the twentieth century and new correlations are still being developed. Most of correlations for cohesive soils are based on soil plasticity because cohesion depends mainly on clay mineral types, clay particle size, clay proportion, and bond between particles. For internal friction angle, the correlations are based on dry density and relative density because shearing resistance depends mainly on particle size distribution, shape of particles, and surface texture [11]. Table 1 summarizes the used empirical correlation for undrained cohesion and Table 2 for drained internal friction angle. Some of these correlations were modified from its original form to be in consistent units by using standard unit conversion factors.

Adapted methodology

Because of the importance and popularity of using shear strength correlations, the geotechnical community should pay more attention to the credibility of these correlations. Analyzing the degree of consistency between the correlated and observed values is a probable method of correlation validation. Amended Theil inequality coefficient (ATIC) method as introduced by Song et al. [28] will be used to rank different shear strength correlations based on the difference in position and trend between the correlated and observed values. The transformation error of each correlation will be determined using rule-based uncertainty propagation (RUP) as demonstrated by Farrance and Frenkel [6] combined with the second moment probabilistic method (SMP) proposed by Phoon et al. [25].

Correlations ranking

Theil inequality coefficient (TIC) was widely used for validating the simulation model in industrial and telecommunication applications since 1977 until now. TIC method does not have any restrictions on the correlated and observed values, its principal is simple, and easy to be applied. For number (n) of observed values (x_o) and correlated values (x_c) , the TIC is given by:

$$C(X_o, X_c) = \frac{\sqrt{\sum_{i=1}^{n} (x_o(i) - x_c(i))^2}}{\sqrt{\sum_{i=1}^{n} x_o(i)^2 + \sqrt{\sum_{i=1}^{n} x_c(i)^2}}}$$
(1)

where, $C(X_o, X_c)$ is the TIC.

Table 1 Undrained cohesion empirical correlations

Cor. ID	Name	Formulae	Soil type	Reference	Notes
C01	Bjerrum and Simons [1]	$C_{\rm U} = \sigma_{\rm O}'(0.45\sqrt{I_{\rm P}}), I_{\rm P} > 0.5,$	Normally consolidated clay	[2]	Scatter: ±25 %
C02	Bjerrum and Simons [1]	$C_U = \sigma_0'(0.18\sqrt{l_L}), l_L > 0.5$	Normally consolidated clay	[2]	Scatter: ±30 %
C03	Skempton and Henkel [27]	$C_u = \sigma_o'(0.11 + 0.37l_P)$	Normally consolidated clay	[27]	-
C04	Karlsson and Viberg [13]	$C_U = \sigma_O'(0.5w_L), w_L > 0.2$	Normally consolidated clay	[2]	Scatter: ±30 %
C05	Edil and Benson [5]	$C_u = \frac{144.9}{e^{1.72l_L}}$	Cohesive soils in Southeastern Wisconsin	[5]	$R^2 = 0.58$
C06	Edil and Benson [5]	$C_U = \frac{191.4}{e^{3w_L}}$	Cohesive soils in Southeastern Wisconsin	[5]	$R^2 = 0.38$
C07	Edil and Benson [5]	$C_{u} = \sigma_{o}'(\frac{0.5}{e^{1.1l_{L}}})$	Cohesive soils in Southeastern Wisconsin	[5]	$R^2 = 0.43$
C08	Worth and Houlsby (1985), Mitchell and Soga [17]	$C_U = \sigma_O'(0.129 + 0.435l_P)$	General	[17]	-
C09	Roy and Dass [26]	$C_u = 98.07(0.131\gamma_b - 0.138)$	Cohesive soils in Sisra, India	[26]	R = 0.84
C10	Roy and Dass [26]	$C_u = 98.07(0.178\gamma_d - 0.198)$	Cohesive soils in Sisra, India	[26]	R = 0.76
C11	Roy and Dass [26]	$C_u = 98.07(0.3w - 0.059)$	Cohesive soils in Sisra, India	[26]	R = 0.65
C12	Mitchell and Soga [17]	$C_U = \frac{1}{(l_L - 0.21)^2}$	General	[17]	_
C13	Kang et al. [12]	$C_u = \sigma_o' \Big(I_p^2 - 1.12 I_P + 0.4398 \Big)$	Low plasticity clay	[12]	R = 0.695
C14	Kang et al. [12]	$C_{U} = \sigma_{O}'(0.7575 - 0.74l_{P})$	Highly plastic clay	[12]	R = 0.608
C15	Hara et al. [8]	$C_u = 98.07(0.297N^{0.72})$	Alluvial clays in Japan	[8]	R = 0.93
C16	Terzaghi et al. [31]	$C_u = 3.6N$	Cohesive soil	[31]	
C17	Nixon [19]	$C_u = 11.965N$	Clay	[19]	
C18	Décourt [4]	$C_u = 12.455N$	Clay	[4]	
C19	Hettiarachchi and Brown [10]	$C_U = 4.1 N_{60}$	Cohesive soil	[10]	
C20	Nassaji and Kalan- tari [18]	$C_u = 1.6N + 15.4$	Tehran fine grained soil	[18]	R = 0.72

 C_u soil undrained cohesion (kPa), w_L liquid limit (decimal entry), I_P plasticity index (decimal entry), σ_o' effective overburden pressure (kPa), I_L liquidity index (decimal entry), γ_b soil bulk density (g/cm³), γ_d soil dry density (g/cm³), w water content (decimal entry), N SPT no of blows, and N_{60} adjusted SPT N value to 60 % of energy

From Eq. (1), $C(X_o, X_c)$ ranges between 0 and 1. When its value is more close to 0, it indicates that there is a better degree of consistency between the correlated and observed parameters and that the correlation is more credible.

The TIC is simple and easy to understand but it suffers of many flaws which have been discussed in detail by Song et al. [28]. The amended TIC model proposed by Song et al.

P10

P11

P12

P13

P14

P15

Peck et al. (1953)

Suzuki et al. [29]

Meyerhof (1976)

Ohsaki et al. (1959)

(1996)

Munenori and Akihiko

[21]

[9]

[29]

[15]

[14]

[20]

Cor. ID	Name	Formulae	Soil type	Reference	Notes
P01	Roy and Dass [26]	$\emptyset_d = 34.2\gamma_b - 29.57$	Cohesionless soils in in Sisra, India	[26]	R = 0.99
P02	Roy and Dass [26]	$\emptyset_d = 44.2\gamma_d - 41.74$	Cohesionless soils in in Sisra, India	[26]	R = 0.86
P03	Roy and Dass [26]	$\emptyset_d = 1.028w + 21.53$	Cohesionless soils in in Sisra, India	[26]	R = 0.83
P04	Meyerhof [16]	$\emptyset_d = 0.15D_r + 28$	General	[16]	-
P05	Gupta [7]	$\emptyset_d = 0.14D_r + 28$	High compressibility sand	[7]	-
P06	Gupta [7]	$\emptyset_d = 0.115D_r + 31.5$	Medium compressibility sand	[7]	-
P07	Gupta [7]	$\emptyset_d = 0.10D_r + 34.5$	Low compressibility sand	[7]	-
P08	Shioi and Fukui (1982)	$\emptyset_d = 15 + \sqrt{18N'_{70}}$	For roads and bridges	[2]	-
P09	Shioi and Fukui (1982)	$\emptyset_d = 0.36N_{70} + 27$	For buildings	[2]	-

General

sand

General

General

For sandy soils

For gravelly soils

Clean quartz to siliceous

 $\emptyset_d = \sqrt{0.3N} + 27$

 $\emptyset_d = \sqrt{20N} + 18$

 $\emptyset_d = \sqrt{12N} + 25$

 $\emptyset_d = \frac{10N}{35} + 27$

 $\emptyset_d = \sqrt{20N} + 15$

Hatanaka and Uchida [9] $\emptyset_d = 20 + \sqrt{15.4(N_1)_{60}}$

Table 2 Internal friction angle empirical correlations

 \emptyset_d drained internal friction angle, γ_h bulk density (q/cm³), γ_d dry density (q/cm³), w water content (%), D_r relative density (%), N SPT N value, N'_{70} adjusted SPT N value to 70 % of energy and overburden pressure of 100 kPa, N_{60} adjusted SPT N value to 60 % of energy

[28] covers many of the TIC method flaws especially the position and trend differences between the observed and correlated values so it will be used in this study.

Position conformity

For the position conformities between the observed (x_o) and correlated (x_c) values, the following equation is used:

$$D(X_o, X_c) = e^{-\xi C(X_o, X_c)}$$
 (2)

where D represents the position conformity, ξ is the model parameter and it will be taken = 1.0 because all the used correlation has the same weight for position conformity. For number (n) of observed values (x_o) and correlated values (x_c) , the TIC is given by and $C(X_o, X_c)$ is defined as:

$$C(X_o, X_c) = \begin{cases} \frac{\sqrt{\sum_{i=1}^{n} (x_o(i) - x_c(i))^2}}{\sqrt{\sum_{i=1}^{n} x_o(i)^2}}, & \sqrt{\sum_{i=1}^{n} x_o(i)^2} \neq 0\\ \sqrt{\sum_{i=1}^{n} x_c(i)^2}, & \sqrt{\sum_{i=1}^{n} x_o(i)^2} = 0 \end{cases}$$
(3)

where n is the number of observation points, x_o is the observed values, and x_c is the correlated values.

 $D(X_o, X_c)$ value ranges between 0 and 1. When it is close to 1, it indicates better consistency between the position of the correlated and observed values.

Trend conformity

For the trend conformities between the observed and correlated values, the following equation is used:

$$T(X_o, X_c) = e^{-\lambda \delta(X_o', X_c')} \tag{4}$$

where T represents the trend conformity, λ is the model parameter = 1 (because all correlations have the same weight), and $\delta(X'_c, X'_o)$ is defined as:

$$\delta(X'_o, X'_c) = \begin{cases} \frac{\sqrt{\sum_{i=1}^{n-1} (x'_o(i) - x'_c(i))^2}}{\sqrt{\sum_{i=1}^{n-1} x'_o(i)^2}}, & \sqrt{\sum_{i=1}^{n-1} x'_o(i)^2} \neq 0\\ \sqrt{\sum_{i=1}^{n-1} x'_c(i)^2}, & \sqrt{\sum_{i=1}^{n-1} x'_o(i)^2} = 0 \end{cases}$$

$$(5)$$

where n is the number of observation points, x_o' is the observed values' first derivative, and x_c' is the correlated values' first derivative. $T(X_o, X_c)$ value ranges between 0 and 1. When it is close to 1, it indicates better consistency between the trend of correlated and observed values.

Integration of position and trend conformities

For selecting the most credible correlation, the degrees of consistency between the observed values and all correlated values should consider both position and trend conformities at the same time. Principal component analysis is used to correlate between $D(X_0, X_c)$ and $T(X_0, X_c)$ to have a single value that be used for correlations ranking as follows:

$$S_{ij} = \frac{a_{ij}}{a_{\cdot j}} \tag{6}$$

where S_{ij} is the standardized position and trend conformity; j=1 for position conformity or 2 for trend conformity; $a_{i1}=D(X_o,X_c)$; $a_{i2}=T(X_o,X_c)$; and $a_{j}=\frac{\sum_{i=1}^{p}a_{ij}}{p}$; and p is the number of correlations

The covariance (V) of the standardized position and trend conformity is a 2×2 symmetrical matrix as follows:

$$V = \begin{bmatrix} v_{11} & v_{12} \\ v_{21} & v_{22} \end{bmatrix} \tag{7}$$

where v_{mn} is the coefficient of variation (CoV) of (S_{mj}, S_{nj}) , m = 1, 2 and n = 1, 2. The ranking index y_j based on principal component analysis can be determined from the following equation:

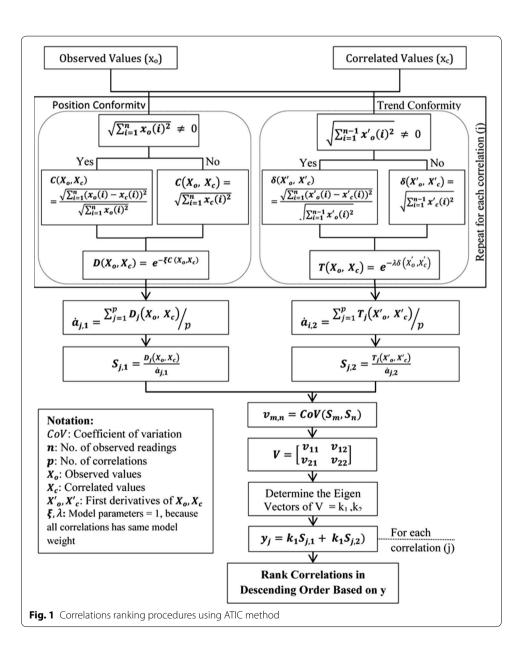
$$y_j = k_1 S_{j1} + k_2 S_{j2} (8)$$

where k_1 and k_2 are the Eigen Vectors of the covariance matrix V shown in Eq. 7.

Figure 1 summarizes the calculation procedure and equations for correlations ranking based on ATIC method.

Transformation error assessment

Uncertainties in geotechnical design parameters are inevitable due to the complex nature of the soil. Phoon and Kulhawy [23] defined the sources of uncertainties to be inherent variability (ω), measurement errors (e), and transformation uncertainty (ϵ). Phoon et al. [25] proposed a second-moment probabilistic approach (SMP) to characterize different geotechnical variabilities. SMP is complex when there is more than on measured property within the functional relationship. To overcome this complexity,



rule-based uncertainty propagation (RUP) as introduced by Farrance and Frenkel [6] to be combined with SMP is proposed (RUP-SMP).

The RUP-SMP method

If a design property, y, is determined from input variables x_1 , x_2 ,..., x_n through a functional relationship, then uncertainties in the x's, $u(x_i)$, will propagate through the calculation to an uncertainty in y, u(y), equals to [6]:

$$u^{2}(y) = \sum_{i=1}^{n} \left(\frac{\partial T}{\partial x_{i}}\right)^{2} u^{2}(x_{i})$$
(9)

Phoon et al. [25] proposed, for a design geotechnical property (ξ_d) is determined from uncorrelated measured properties (ξ_{mi}) through a functional relationship has a transformation uncertainty of (ε) such that:

$$\xi_d = T(\xi_{mi}, \varepsilon) \tag{10}$$

Knowing that the measured property (ξ_{mi}) with mean value (t) contains inherent variability (ω) and measurement error (e) that can be reasonably assumed as random and uncorrelated, that is:

$$\xi_{mi} = t_i + \omega_i + e_i \tag{11}$$

Then the design geotechnical property can be expressed as:

$$\xi_d = T(t_i + \omega_i + e_i, \varepsilon) \tag{12}$$

By combining Eqs. (12) into (9), then uncertainties in (ξ_d) due to the propagation of uncertainties in (ξ_{mi}) can be expressed as:

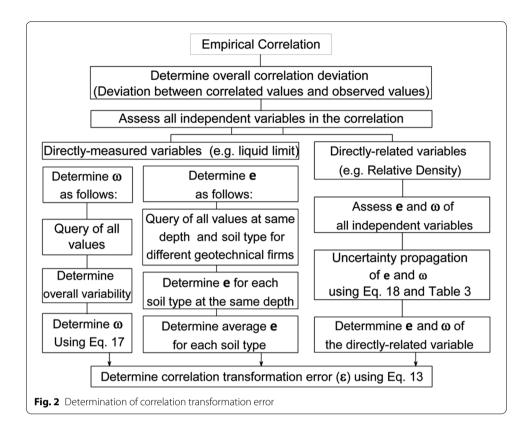
$$u^{2}(\xi_{d}) = \sum_{i=1}^{n} \left\{ \left(\frac{\partial T}{\partial \omega_{i}} \right)^{2} u^{2}(\omega_{i}) + \left(\frac{\partial T}{\partial e_{i}} \right)^{2} u^{2}(e_{i}) \right\} + \left(\frac{\partial T}{\partial \varepsilon} \right)^{2} u^{2}(\varepsilon)$$
(13)

where the uncertainity (u) can be expressed as the standard deviation (*SD*) of the variables [30]. Knowing the values of the overall uncertainity of the design property, inherent variability and measurement error in the measured property, the transformation error can be assessed. The transformation error assessment can be used to decide if the correlated parameters are adequate for its intended purpose, if it is consistent with observed parameters, and to be used for determining the overall geotechnical uncertainty needed in reliability based analysis and design. In the following section, the proposed method for determining the transformation uncertainties is introduced as shown in Fig. 2.

Directly-measured properties variability

For soil properties that directly measured in the laboratory or in the field (e.g. liquid limit, plastic limit, bulk density, dry density, maximum and minimum dry densities,.. etc.), it is apparent that the transformation error can be assumed as zero. Equation (12) simplified to:

$$\xi_d = T(t_i + \omega_i + e_i) \tag{14}$$



Applying in Eq. (13)

$$SD^{2}(\xi_{d}) = SD^{2}(\omega) + SD^{2}(e) \tag{15}$$

Assuming a single mean value for the measured property [23], then the coefficient of variation (CoV) can be expressed as

$$CoV^{2}(\xi_{d}) = CoV^{2}(\omega) + CoV^{2}(e)$$
(16)

The overall property variability can be determined directly by determining the $SD(\xi_d)$ and $CoV(\xi_d)$ of all the property's measured values for different soil types. For the same soil type at the same depth, it is reasonable to assume that the inherent variability is minimal and the variability arises only from the measurement error. To assess the measurement error, the SD(e) and CoV(e) of the property values having same soil type and depth were determined. Then, the inherent variability will be equal to

$$CoV^{2}(\omega) = CoV^{2}(\xi_{d}) - CoV^{2}(e)$$
(17)

The assumption that the inherent variability is minimum and can be neglected for same soil type and depth is not always true, especially if the distance between the boreholes is large. Some inherent variability exists due to the horizontal spatial variation. This deviation of the measurement and inherent variability values will not affect the value of the deduced transformation error because both inherent variability and measurement error are summed as shown in Eq. (16) . Additional file 1: Appendix Table A1 shows the variability parameters of different directly-measured soil properties.

Directly-related properties variability

Most of the literatures dealt with the soil properties that deduced from theoretical relations (e.g. dry density, relative density,.. etc.) as a measured property [25]; Phoon and Kulhawy [23, 24, 32] without considering functional form effect on uncertainty propagation. Because the indirect properties have a theoretical basis, ideally, there is no transformation error. Nevertheless, some transformation error may appear due to simplification and idealization of the used theory, but these errors can be ignored [25]. Equation (13) is simplified to:

$$u^{2}(\xi_{d}) = \sum_{i=1}^{n} \left\{ \left(\frac{\partial T}{\partial \omega_{i}} \right)^{2} u^{2}(\omega_{i}) + \left(\frac{\partial T}{\partial e_{i}} \right)^{2} u^{2}(e_{i}) \right\}$$
(18)

Thus the inherent variability of the indirect property $u^2(\omega_d)$ is:

$$u^{2}(\omega_{d}) = \sum_{i=1}^{n} \left\{ \left(\frac{\partial T}{\partial \omega_{i}} \right)^{2} u^{2}(\omega_{i}) \right\}$$
(19)

And the measurement error can be calculated from:

$$u^{2}(\mathbf{e}_{d}) = \sum_{i=1}^{n} \left\{ \left(\frac{\partial T}{\partial e_{i}} \right)^{2} u^{2}(e_{i}) \right\}$$
 (20)

Additional file 1: Appendix Table A2 shows the variability parameters of different directly-related soil properties.

Correlation transformation error

The transformation error of shear strength correlation can be determined using RUP-SMP methods by substituting the values of inherent variability and measurement error in Eq. (13). The uncertainty propagation formulae appeared in Eq. (13) is more dependent on the soil-property/correlation functional form. The functional form of different soil properties and correlations investigated in this study are summarized in Table 3. Detailed uncertainty rules for different correlations are given in Additional file 1: Appendix Table A3.

Results and discussion

Correlation ranking

Undrained cohesion

From 1447 unconfined compressive strength test, 114 records were selected to rank different undrained cohesion correlations. These sets of records were selected using SQL query from the database with the condition of having all related measured soil properties needed for the correlations shown in Table 1. The reason for this condition (Table 4) is to maintain the consistency and accuracy of the ranking procedure. Undrained cohesion correlations were ranked using the ATIC method, the principal component analysis revealed that the position conformity has more effect than trend conformity. The final rank value (y_j) for each correlation is calculated based on Eq. (21).

ID	Functional form	Variability expression	Uncertainty rule
—— U1	$d = Ax_1$	$\xi_d = T(t_{x1} + \omega_{x1} + e_{x1}) + \varepsilon$	$SD^{2}(\xi) = \left\{ SD^{2}(\omega_{X_{1}}) + SD^{2}(e_{X_{1}}) \right\} + SD^{2}(\varepsilon)$ $CoV^{2}(\xi_{d}) \approx \left\{ CoV^{2}(\omega_{X_{1}}) + CoV^{2}(e_{NX_{1}}) \right\} + \frac{SD^{2}(\varepsilon)}{m\xi_{d}}$
U2	$d = Ax_1^B$	$\xi_d = T(t_{x1} + \omega_{x1} + e_{x1}) + 10^{\varepsilon}$	$SD^{2}(\xi_{d}) = B^{2} \left\{ SD^{2}(\omega_{X_{1}}) + SD^{2}(e_{X_{1}}) \right\} + (\ln 10)^{2} SD^{2}(\varepsilon)$
U3	$d = Ae^{Bx_1}$	$\xi_d = T(t_{x1} + \omega_{x1} + e_{x1}) + e^{\varepsilon}$	$CoV^{2}(\xi_{d}) = B^{2}\{SD^{2}(\omega_{x_{1}}) + SD^{2}(e_{x_{1}})\} + SD^{2}(\varepsilon)$
U4	$d = Ax_1 \pm B$	$\xi_d = T(t_{x1} + \omega_{x1} + e_{x1}) + \varepsilon$	$SD^{2}(\xi_{d}) = A^{2} \{SD^{2}(\omega_{X_{1}}) + SD^{2}(e_{X_{1}})\} + SD^{2}(\varepsilon)$
U5	$d = A(x_1 \pm B)^C$	$\xi_d = T(t_{x1} + \omega_{x1} + e_{x1}) + 10^{\varepsilon}$	$SD^{2}(\xi_{d}) = C^{2} \left\{ \frac{SD^{2}(\omega_{X_{1}}) + SD^{2}(e_{X_{1}})}{(\bar{X}_{1} \pm B)^{2}} \right\} + (\ln 10)^{2} SD^{2}(\varepsilon)$
U6	$d = Ax_1 \pm Bx_2$	$\xi_d = T(t_{x1} + \omega_{x1} + e_{x1}) + T(t_{x2} + \omega_{x2} + e_{x2}) + \varepsilon$	$SD^{2}(\xi_{d}) = \left\{ SD^{2}(\omega_{X_{1}}) + SD^{2}(e_{X_{1}}) \right\}$
U7	$d = Ax_1(x_2^B)$	$\xi_d = T(t_{x1} + \omega_{x1} + e_{x1})$ $* T(t_{x2} + \omega_{x2} + e_{x2}) * 10^{\varepsilon}$	$+ \left\{ SD^{2}(\omega_{x_{2}}) + SD^{2}(e_{x_{2}}) \right\} + SD^{2}(\varepsilon)$ $CoV^{2}(\xi_{d}) = \left\{ CoV^{2}(\omega_{x_{1}}) + CoV^{2}(e_{x_{1}}) \right\}$ $+ B^{2} \left\{ CoV^{2}(\omega_{x_{2}}) + CoV^{2}(e_{x_{2}}) \right\}$
U8	$d = Ax_1 \left(e^{Bx_2} \right)$	$\xi_d = T(t_{x1} + \omega_{x1} + e_{x1}) \\ *T(t_{x2} + \omega_{x2} + e_{x2}) * e^{\varepsilon}$	$+ (\ln 10)^{2} SD^{2}(\varepsilon)$ $CoV^{2}(\xi_{d}) = \left\{ CoV^{2}(\omega_{x_{1}}) + CoV^{2}(e_{x_{1}}) \right\}$ $+ B^{2} \left\{ CoV^{2}(\omega_{x_{2}}) + CoV^{2}(e_{x_{2}}) \right\} + SD^{2}(\varepsilon)$
U9	$d = Ax_1(Bx_2 + C)$	$\xi_d = T(t_{x1} + \omega_{x1} + e_{x1}) * T(t_{x2} + \omega_{x2} + e_{x2}) * 10^{\varepsilon}$	$CoV^{2}(\xi_{d}) = \left\{CoV^{2}(\omega_{X_{1}}) + CoV^{2}(e_{X_{1}})\right\}$
			$+\left(\frac{B}{B\bar{x}_2+C}\right)^2\left\{SD^2(\omega_{x_2})+SD^2(e_{x_2})\right\}$
			$+ (\ln 10)^2 SD^2(\varepsilon)$

Table 3 Rule-based uncertainty expression for different soil functional forms

where A, B and C: constants with no uncertainty, x_i soil property, \bar{x}_i : mean value of the soil property

$$y_j = 0.7793S_{j1} + 0.6267S_{j2} (21)$$

Summary of the ranking results based on the procedures shown in Fig. 1 are given in Table 5 with some statistical measures that are commonly used for correlations evaluation.

From the results given in Table 5, the best correlation to deduce the undrained cohesion for the studied data is correlation no. C16, which was deduced by Terzaghi et al. [31] that relates the undrained cohesion with the standard penetration test N value. The results of this correlation are shown in Fig. 3. Figure 3a shows the correlated versus observed undrained cohesion with the values of correlation coefficient (R²), mean absolute deviation (MAD), and root mean square of deviation (RMSD). Figure 3b shows the frequency distribution of correlated vlues' bias with the values of average bias, bias CoV, and ranking index (RD). The bias in the correlated undrained cohesion distribution follows a lognormal distribution as shown in Fig. 3b. It can be noted that the bias distribution is almost symmetrical around bias-value of 1.0 (the best bias value at which the correlated value is equal the observed value).

The worst-ranked correlation of the studied data is correlation C18, the results of this correlation are given in Fig. 4. Similar figures and values for the rest of correlations are given in Additional file 1: Appendix Figure A1. It can be noted that the determination

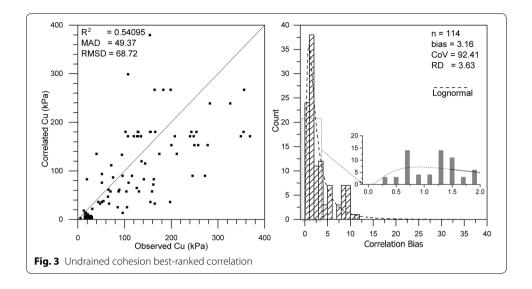
Table 4 Undrained cohesion correlations ranking results based on ATIC method with commonly used statistical measures in correlations evaluation

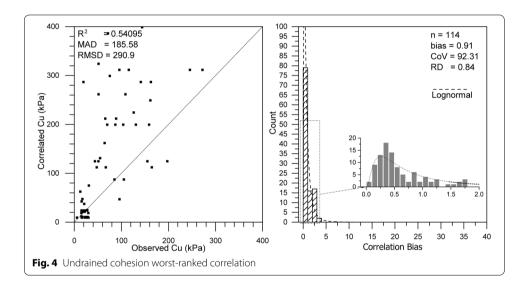
Cor. ID	ATIC meth	od			Statistic	cal measu	res			
	$D(X_o, X_c)$	$T(X_o,X_c)$	Уj	Rank	R ²	MAD	RMSD	Bias	Bias CoV	RD
C1	0.408	0.363	1.579	10	0.0052	88.73	124.63	8.17	168.73	15.54
C2	0.427	0.357	1.604	8	0.0065	85.84	118.59	6.26	157.18	11.16
C3	0.407	0.363	1.578	11	0.0026	88.65	124.96	8.23	164.01	15.31
C4	0.409	0.348	1.548	14	0.0383	91.04	124.48	7.84	178.10	15.55
C5	0.246	0.068	0.630	18	0.3119	121.62	195.39	0.63	79.36	0.62
C6	0.485	0.366	1.738	4	0.1928	63.56	100.61	2.37	90.49	2.55
C7	0.517	0.276	1.608	7	0.2156	63.36	91.93	2.39	118.38	3.15
C8	0.414	0.361	1.584	9	0.0026	87.25	122.91	7.01	164.04	12.98
C9	0.392	0.369	1.559	12	0.1550	91.41	130.3	8.90	98.60	11.81
C10	0.389	0.370	1.556	13	0.0001	93.7	131.38	15.15	297.70	47.43
C11	0.367	0.364	1.501	15	0.3901	100.57	139.38	80.56	146.31	143.07
C12	0.278	0.086	0.733	17	0.0054	119.08	178.31	47.66	161.84	90.15
C13	0.433	0.359	1.621	6	0.0880	79.16	116.37	5.66	128.16	8.62
C14	0.489	0.322	1.651	5	0.0715	68.8	99.59	2.40	133.58	3.49
C15	0.238	0.210	0.916	16	0.5845	138.62	199.97	0.56	55.41	0.54
C16	0.610	0.393	2.042	1	0.5410	49.37	68.72	3.16	92.41	3.63
C17	0.138	0.085	0.453	19	0.5410	175.25	275.48	0.95	92.41	0.88
C18	0.124	0.076	0.406	20	0.5410	185.58	290.9	0.91	92.41	0.84
C19	0.577	0.343	1.870	3	0.5410	49.42	76.53	2.38	92.41	2.6
C20	0.534	0.416	1.941	2	0.5410	56.29	87.32	1.96	57.72	1.48

where R^2 determination coefficient, MAD mean absolute deviation, RMSD root mean square of deviation, Bias observed to correlated values' ratio, Bias CoV bias coefficient of variation, RD ranking distance. Equations for these statistical measures are given in Additional file 1: Appendix

Table 5 Drained internal friction angle correlations ranking results based on ATIC method with commonly used statistical measures in correlations evaluation

Cor. ID	ATIC meth	od			Statistic	al measu	ures			
	$D(X_o, X_c)$	$T(X_o, X_c)$	Уј	Rank	R ²	MAD	RMSD	Bias	Bias CoV	RD
P1	0.916	0.492	1.584	1	0.6095	2.17	3.02	0.95	6.32	0.078
P2	0.908	0.453	1.468	2	0.6084	2.97	3.3	1.08	6.30	0.105
Р3	0.879	0.407	1.324	4	0.2732	3.89	4.44	0.91	8.79	0.12
P4	0.890	0.312	1.038	8	0.4410	3.09	4.01	0.97	11.96	0.12
P5	0.900	0.329	1.093	7	0.4410	2.79	3.63	0.98	11.22	0.112
P6	0.880	0.371	1.216	6	0.4410	3.59	4.39	0.92	8.70	0.113
P7	0.837	0.392	1.275	5	0.4410	5.5	6.11	0.86	7.79	0.155
P8	0.894	0.279	0.940	11	0.5345	2.81	3.86	1.01	10.59	0.107
P9	0.897	0.282	0.951	10	0.4938	2.43	3.75	0.98	8.98	0.09
P10	0.859	0.446	1.439	3	0.6199	4.44	5.21	1.15	7.74	0.174
P11	0.787	0.181	0.634	15	0.6199	6.32	8.2	0.87	12.53	0.17
P12	0.772	0.289	0.958	9	0.6199	7.94	8.87	0.82	8.90	0.194
P13	0.829	0.279	0.934	12	0.5345	5.45	6.43	0.88	9.20	0.145
P14	0.879	0.263	0.889	13	0.5712	2.58	4.42	1.00	10.10	0.101
P15	0.828	0.181	0.639	14	0.6199	4.41	6.45	0.95	13.58	0.138





coefficient (R^2) for best and worst ranked correlations is equal which proof that the R^2 can't be considered alone for correlation evaluation.

Internal friction angle

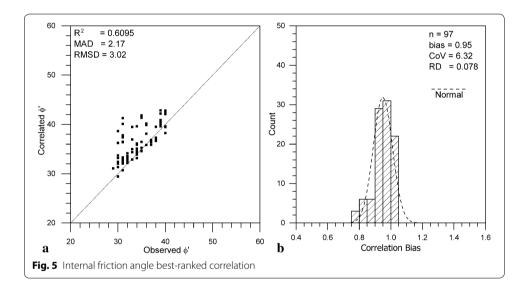
The values of drained internal friction angle deduced from different empirical correlations shown in Table 2 were compared to the observed (measured) internal friction angle from direct shear box. Total number of internal friction angle records in the database were 764 records. SQL query from the database was used to collect all the internal friction angle that has a corresponding measured values for all variables needed on all correlations to maintain consistency of the correlation ranking results. The resulted number of records were 97 test groups. Correlated internal friction angles were ranked based on the methodology given in Fig. 1. The difference among the position conformities of correlations' results is not significant in contrast to the trend conformities which has

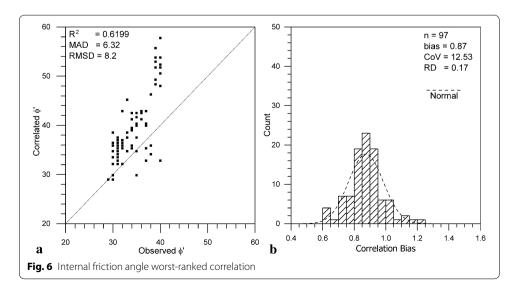
a significant effect. So the ranking of internal friction angle correlations shall be determined primarily by the trend conformities as in Eq. (22). Summary of the ATIC method results is given in Table 5.

$$y_j = 0.0968S_{j1} + 0.9951S_{j2} \tag{22}$$

From the results given in Table 5, the best correlation to deduce the internal friction angle from the studied data is correlation no. P01 that was proposed by Roy and Dass [26]. Figure 5 shows the correlated versus observed internal friction angle and the bias of the correlated values. The bias in the correlated internal friction angle follows a normal distribution as shown in Fig. 5b.

The worst-ranked corelation for the studied data is correlation no. P11. The results for this correlation is given in Fig. 6. Similar figures and values for the rest of correlations are given in Additional file 1: Appendix Figure A2.





Transformation error assessment

Geotechnical variability parameters for directly-measured and directly-related soil properties were determined based on Fig. 2 are shown in Additional file 1: Appendix Tables A1, A2. Summary of the results compared with the reported values [23] are given in Table 6.

The results of the geotechnical variabilities are in a good agreement with the literature values especially for the overall variability. Although measurement error CoV were larger than the literatures values due the large variation of the boreholes locations and involved geotechnical laboratories. In addition, the adapted methodology did not isolate completely the measurement error from the inherent variability. The directly-related soil properties has a significant deviation from the literature values especially for liquidity index because uncertainty propagation in the related properties were ignored in the literature.

Quantification of transformation error from empirical correlations is important for reliability based analysis and design [3]. In the presence of sufficient field and laboratory data, the transformation error from using different correlations can be identified. In the absence of sufficient information, Tables 7 and 8 summarize correlations' transformation error for different soil types for both undrained cohesion and internal friction angle. These values can be used as guidance for transformation error in other similar sites. The transformation error CoV of undrained cohesion ranges between 5 and 336 %. This high variation can be explained because most of the correlations are site specific and the sensitivity of undrained cohesion to soil stress history, mineral contents and site conditions. A conclusion can be made that a site-specific empirical correlation may not be applicable to another site. The transformation error for the most credible correlation (C16) ranged between 16 and 95 %.

The transformation error CoV of internal friction angle ranges between 1 and 33 %. The transformation error for the most credible correlation (P01) ranged between 5 and 19 %.

Table 6 Summary of geotechnical variability compared to reported values in the literature

Soil Property	Overall	variability	Inhere	nt variability	Measure	ement error
	CoV	Literature CoV ^a	CoV	Literature CoV	CoV	Literature CoV
Bulk density	5–9	3–20	2–8	3–20	1–8	1–2
Natural moisture Content	11-55	9–48	7-30	7–46	4-45	6–12
Liquid limit	7-25	8-41	4-15	7–39	5-24	3-11
Plastic limit	8-24	9–38	4-12	6-34	6-23	7–18
Maximum dry density	2-4	-	1-2	_	1-3	-
Minimum dry density	3-7	-	1–6	_	3-4	_
SPT (N)	22-90	24-77	18-80	19-62	13-70	15-45
Plasticity index	10-35	10-76	6-19	9-57	8-33	5-51
Liquidity index	57-146	60-88	36-96	60-88	44-114	_
Dry density	5-11	2–13	4-9	2-13	2-10	-
Relative density	15-35	11-36	6-24	11-36	8-18	-
Overburden pressure	7–9	_	2–8	-	1–8	-

 $^{^{\}rm a}$ The literature CoV was deduced from Equation 16

Table 7 Transformation error for different undrained cohesion correlations and soil types

(2) (4) <th>Cor. ID</th> <th>High plasticity CLAY</th> <th>y CLAY</th> <th>High plasticity SILT</th> <th>ty SILT</th> <th>Low plasticity CLAY</th> <th>y CLAY</th> <th>Low plasticity SILT-CLAY</th> <th>y SILT-CLAY</th> <th>Low plasticity SILT</th> <th>, SILT</th>	Cor. ID	High plasticity CLAY	y CLAY	High plasticity SILT	ty SILT	Low plasticity CLAY	y CLAY	Low plasticity SILT-CLAY	y SILT-CLAY	Low plasticity SILT	, SILT
21,48 16 4305 47 21,48 6 255 8 21,77 2246 16 42,76 46 21,97 6 252 8 21,18 156,13 114 21,69 21 41,52 119 44,318 138 20,76 118 159,17 116 207,42 225 416.8 119 44,122 138 20,76 118 12,39 50 207,42 225 416.8 113 441,22 138 222,42 1 12,39 210.65 228 236 131 411,22 138 222,42 1 144.55 105 128 232 248 86 365 124 156,91 1 <t< th=""><th></th><th>SD (kPa)</th><th>CoV (%)</th><th>SD (kPa)</th><th>CoV (%)</th><th>SD (kPa)</th><th>CoV (%)</th><th>SD (kPa)</th><th>CoV (%)</th><th>SD (kPa)</th><th>CoV (%)</th></t<>		SD (kPa)	CoV (%)	SD (kPa)	CoV (%)	SD (kPa)	CoV (%)	SD (kPa)	CoV (%)	SD (kPa)	CoV (%)
2246 16 4276 46 2197 6 552 8 21.18 15613 114 21369 231 415.22 119 443.18 138 220.76 15917 116 20742 22 416.8 119 441.2 138 220.76 15217 16 20742 125 416.8 113 441.2 138 222.42 12738 60 210.65 228 393.5 113 417.7 128 122.42 164.55 116 214.28 32 208.82 86 365.5 122.42 122.42 164.65 12 228.2 165 481.8 319 447.0 128.9 122.49 175.8 12 226.5 164 437.78 318 462.3 33.9 243.9 176.6 12 228.31 166 444.45 323 462.3 118 22.0 176.7 13 22	C01	21.48	16	43.05	47	21.48	9	25.5	∞	21.77	12
156.13 114 213.69 231 415.2 119 443.18 138 220.76 159.17 116 207.42 225 416.8 119 441.12 138 222.42 82.97 60 937.25 1015 1093.5 113 441.12 138 222.42 127.98 93 210.65 228 298.2 13 122.49 123 145.5 118 213 441.6 13 441.6 156 122.49 122.40 1	C02	22.46	16	42.76	46	21.97	9	25.2	œ	21.18	1
159.17 116 20742 216 416 119 441.22 138 22242 82.97 60 937.25 1015 10935 31 209.48 65 186.23 127.98 93 21065 228 298.82 86 396.5 124 156.91 144.95 105 186.73 202 288.82 86 396.5 124 156.91 144.95 105 124.88 202 288.82 18 440.63 134 156.91 156.92 156.91 156.92 156.92 156.92 156.92 156.92 156.92 156.92 156.92 156.92<	C03	156.13	114	213.69	231	415.52	119	443.18	138	220.76	117
8297 60 937.5 1015 1093.5 31 20948 65 186.23 127.98 93 210.65 228 393.55 113 411.7 128 124.9 144.95 105 126.5 228.82 86 366.5 124 152.49 161.52 118 242.8 415.62 119 440.63 137 153.24 165.64 118 242.8 126 483.18 319 450.61 155.91 155.91 165.64 123 126 438.18 319 450.62 332 245.96 173 172.8 126 444.45 318 462.3 336 245.96 173 1304.3 52 528.01 178 444.45 332 462.3 336 462.96 173 1304.3 52 528.0 103 104 353.4 116 118 118 118 118 118 118 118 11	C04	159.17	116	207.42	225	416.8	119	441.22	138	222.42	118
127.98 93 113 411.7 128 124.9 144.95 105 298.2 86 396.5 124 156.91 144.95 105 186.3 288.2 86 396.5 124 156.91 161.52 118 212.2 415.6 139 440.63 137 513.2 165.66 123 226.35 164 437.8 319 450.1 332 239.78 172.8 126 225.95 164 444.5 323 462.3 336 240.96 173 171.62 125 228.31 166 444.45 323 462.3 336 245.96 18 171.62 125 228.0 11 118 379.53 118 258.0 18 1804.9 640 243.8 264 360.9 103 18 18 18 18 18 18 18 18 18 18 18 18 18	C05	82.97	09	937.25	1015	109.35	31	209.48	65	186.23	66
144.95 105 98.8 86 396.5 124 156.91 161.52 118 420.6 15.6 119 440.63 137 15.32 165.62 118 420.6 119 440.63 137 217.32 217.32 169.66 123 226.3 164 437.8 319 450.1 332 239.78 239.78 239.78 240.96 217.32 240.96 217.32 240.96 217.32 240.96 2	900	127.98	93	210.65	228	393.55	113	411.7	128	122.49	65
16152 118 21428 232 415.62 119 440.63 137 217.32 16966 123 226.25 164 437.18 319 450.10 332 239.78 1728 126 225.95 164 437.78 318 456.22 332 240.96 17162 125 228.31 166 444.45 323 462.3 336 245.96 17 31932 232 228.31 166 444.45 323 462.3 336 245.96 17 31932 232 232 246 36.99 103 599.7 18 228.01 17 13063 136 69.73 75 364.43 104 353.74 116 153.77 153.77 13064 136 15 15 152.66 105 105 105 105 105 107 104.76 107 104.76 107 104.76 104.76 104.76 1	C07	144.95	105	186.73	202	298.82	98	396.5	124	156.91	83
169.66 123 226.25 165 438.18 319 45.01 332 239.78 1 172.8 126 25.55 164 437.78 318 456.2 332 240.96 1 171.62 125 228.31 166 444.45 323 462.3 336 245.96 1 319.32 232 228.31 166 444.45 323 462.3 336 245.96 1 879.49 640 243.8 264 360.9 103 599.7 118 538.5 2 130.63 130 64.38 172 364.43 104 353.4 105 538.5 1 130.63 136 69.73 17 162.6 105 163.7 163.7 164.76 163.7 164.76 164.76 164.76 164.76 164.76 164.76 164.76 164.76 164.76 164.76 164.76 164.76 164.76 164.76 164.76 <td< td=""><td>C08</td><td>161.52</td><td>118</td><td>214.28</td><td>232</td><td>415.62</td><td>119</td><td>440.63</td><td>137</td><td>217.32</td><td>115</td></td<>	C08	161.52	118	214.28	232	415.62	119	440.63	137	217.32	115
1728 126 437.78 318 456.22 332 249.96 171.62 125 228.31 166 444.45 323 462.3 336 245.96 1 319.32 228 228.31 166 444.45 323 462.3 336 245.96 1 319.32 232 258.02 279 411.11 118 379.53 118 528.01 1 879.49 640 243.8 264 36.97 187 538.5 1 130.63 130 69.73 75 365.02 105 338.24 105 223.8 1 130.63 15.59 17 195.26 56 50.6 16 164.76 <td>600</td> <td>169.66</td> <td>123</td> <td>226.25</td> <td>165</td> <td>438.18</td> <td>319</td> <td>457.01</td> <td>332</td> <td>239.78</td> <td>174</td>	600	169.66	123	226.25	165	438.18	319	457.01	332	239.78	174
17162 125 228.31 166 444.45 323 462.3 336 462.3 366 444.45 323 462.3 365.96 11 11 118 379.53 118 245.96 11 87949 640 243.8 264 360.9 103 599.7 187 588.5 2 130.63 15 264 365.0 105 38.24 107 53.38 1 130.63 69.73 75 365.0 56 50.6 16 164.76 1 182.21 13 67.18 73 498.88 143 343.93 107 256.94 1 2003.6 14 61.39 66 52.281 15 145.24 145 316.86 1 123.86 90 17.26 52.281 15 23.25 145.24 1 145.24 1 1 123.86 90 16 52.281 15 20.37 1	C10	172.8	126	225.95	164	437.78	318	456.22	332	240.96	175
319.3 232 258.02 279 411.11 118 379.53 118 228.01 1 879.49 640 243.8 264 36.9 103 599.7 187 538.5 2 130.63 95 158.68 172 364.43 104 353.74 110 153.77 2 178.88 130 69.73 75 365.02 105 56 50.6 16 164.76 164.76 182.21 13 67.18 73 498.88 143 343.93 107 556.94 1 200.36 146 61.39 66 52.281 150 463.58 145 316.86 1 123.86 90 17.26 19 20.379 58 91.89 29 145.24 1 153.77 112 23.34 25 231.25 66 32.95 10 11.105 11.105 11.105	C11	171.62	125	228.31	166	444.45	323	462.3	336	245.96	179
879.49 640 243.8 264 360.9 103 599.7 187 538.5 288.5 288.5 288.5 288.5 104 353.74 110 153.77 153.77 153.77 153.77 153.77 153.77 153.77 153.77 163.77 165.79 165.79 165.79 165.79 167.70 164.76 <td>C12</td> <td>319.32</td> <td>232</td> <td>258.02</td> <td>279</td> <td>411.11</td> <td>118</td> <td>379.53</td> <td>118</td> <td>228.01</td> <td>121</td>	C12	319.32	232	258.02	279	411.11	118	379.53	118	228.01	121
130.63 95 158.68 172 364.43 104 353.74 110 153.77 178.88 130 69.73 75 365.02 105 382.4 105 223.8 130.63 15.59 17 195.26 56 50.6 16 164.76 164.76 182.21 13 67.18 73 498.88 143 343.93 107 256.94 1 200.36 146 61.39 66 522.81 150 463.58 145 316.86 1 123.86 90 17.26 19 23.79 66 32.95 10 211.05 1	C13	879.49	640	243.8	264	360.9	103	599.7	187	538.5	285
178.88 130 69.73 75 365.02 105 338.24 105 223.8 130.63 95 15.59 17 195.26 56 16.76 164.76 182.21 133 67.18 73 498.88 143 343.93 107 256.94 1 200.36 146 61.39 66 522.81 150 463.58 145 316.86 1 123.86 90 17.26 19 203.79 58 91.89 29 145.24 1 153.77 112 23.34 25 231.25 66 32.95 10 211.05 1	C14	130.63	95	158.68	172	364.43	104	353.74	110	153.77	82
130.63 95 15.59 17 195.26 56 50.6 16 164.76 182.21 133 67.18 73 498.88 143 343.93 107 256.94 1 2003.6 146 61.39 66 52.281 150 463.58 145 316.86 1 123.86 90 17.26 19 203.79 58 91.89 29 145.24 1 153.77 112 23.34 25 231.25 66 32.95 10 211.05 1	C15	178.88	130	69.73	75	365.02	105	338.24	105	223.8	119
182.1 133 67.18 73 498.88 143 343.93 107 256.94 1 200.36 146 61.39 66 522.81 150 463.58 145 316.86 1 123.86 90 172.6 19 203.79 58 91.89 29 145.24 153.77 112 23.34 25 231.25 66 32.95 10 211.05 1	C16	130.63	95	15.59	17	195.26	56	50.6	16	164.76	87
200.36 146 61.39 66 522.81 150 463.58 145 316.86 123.86 90 17.26 19 203.79 58 91.89 29 145.24 153.77 112 23.34 25 231.25 66 32.95 10 211.05	C17	182.21	133	67.18	73	498.88	143	343.93	107	256.94	136
123.86 90 17.26 19 203.79 58 91.89 29 145.24 153.77 112 23.34 25 231.25 66 32.95 10 211.05 1	C18	200.36	146	61.39	99	522.81	150	463.58	145	316.86	168
153.77 112 23.34 25 231.25 66 32.95 10 211.05	C19	123.86	06	17.26	19	203.79	58	91.89	29	145.24	77
	C20	153.77	112	23.34	25	231.25	99	32.95	10	211.05	112

Table 8	Transformation	error 1	for	different	drained	internal	friction	angle	correlations
and soil	types								

Cor. ID	Gravell SAND	ly silty	Silty S	AND	Silty ve SAND	ery gravelly	Slightly slightly SAND	y gravelly v silty	Slightly SAND	y silty
	SD (°)	CoV (%)	SD (°)	CoV (%)	SD (°)	CoV (%)	SD (°)	CoV (%)	SD (°)	CoV (%)
P01	2.6	8	2.5	7	5.7	19	2.1	6	1.8	5
P02	2.5	7	2.6	7	1.9	6	3.9	12	2.7	8
P03	3.9	11	4.3	12	6.4	21	5.1	16	4.1	12
P04	4.0	12	1.4	4	6.1	20	1.1	4	2.8	8
P05	3.5	10	1.0	3	5.5	18	0.4	1	2.6	8
P06	4.8	14	0.9	3	7.6	25	3.8	12	3.2	9
P07	6.7	20	3.1	9	9.8	33	6.3	20	5.1	15
P08	3.9	11	4.2	11	3.5	12	2.9	9	5.2	15
P09	2.7	8	5.1	14	3.8	13	2.3	7	3.5	10
P10	5.3	15	6.5	18	0.8	3	3.4	11	5.1	15
P11	6.4	19	9.4	26	5.6	19	2.1	7	1.1	3
P12	2.5	7	10.2	28	8.7	29	7.5	23	6.4	19
P13	2.7	8	6.9	19	8.5	28	5.7	18	2.8	8
P14	5.5	16	5.6	15	1.6	5	2.8	9	3.3	10
P15	7.7	22	5.4	15	2.1	7	5.5	17	5.2	15

The transformation error values shown in Tables 7 and 8 can be incorporated in the following framework to deduce the overall geotechnical variability:

- 1. Determine geotechnical variability (SD and CoV) for directly-measured and directly-related soil properties using Eqs. (15) and (16) based on the procedures given in Fig. 2,
- 2. Identify which correlation would be used for determining shear strength parameter,
- 3. Use the values of correlation transformation error from Tables 7 and 8 as a guidance for the transformation error,
- 4. Choose the appropriate rule-based uncertainty expression from Table 3 (and Additional file 1: Appendix Table A3) based on the correlation functional form,
- 5. Determine the overall variability based on the chosen uncertainty expression.

Conclusions

Customized geotechnical database was created that contains 5087 boreholes from reputable geotechnical firms in Egypt, UAE, Iraq, and Indonesia. The database served to assess inherent variability, measurement error, and transformation error more consistently. The credibility and transformation error of geotechnical correlations that are commonly used to estimate undrained cohesion and internal friction angle were investigated. The correlations were ranked considering both position and trend conformity using Amended Theil Inequality Coefficient. The most credible correlation to deduce the undrained cohesion for the studied data is correlation no. C16. For internal friction angle, the most credible correlation is correlation no. P01. This conclusion is limited only to the studied data. For other sites, The proposed ATIC method can be used to determine the most crediable correlation.

Different geotechnical variability parameters for both directly-measure and directly-related soil properties were determined and compared with the literature values. The overall variability of the directly-measured properties showed good agreement with the literature values. The inherent variability and measurement error showed some deviation from the literature values, especially for the natural moisture content. This variation is due to the large variation of the boreholes locations and the measurement error wasn't completely isolated from the inherent variability. This deviation didn't affect the resulted transformation error because both inherent variability and measurement error has the same weight in the uncertainty expression. The directly-related soil properties showed deviation from the literature values, especially for the liquidity index, this is due to the literature didn't consider the uncertainty propagation in the used properties.

Transformation error of different correlations was determined based on rule based uncertainty propagation method. The transformation error CoV of undrained cohesion's correlations ranged between 6 and 1015 %. This large variation shows that most of these site-specific empirical correlations may not be applicable to deduce the undrained cohesion for other sites. The transformation error for the most credible correlation (C16) ranged between 16 and 95 %. The small deviation of transformation error indicates that this correlation can be reasonably used to determine the undrained cohesion for the studied data. The transformation error CoV of internal friction angle ranges between 1 and 33 %. The transformation error for the most credible correlation (P01) ranged between 5 and 19 %.

The deduced transformation error may be used as guidance, in the absence of more-accurate site specific values, for determining overall geotechnical variability that is needed in reliability based analysis and design. Framework for incorporating different geotechnical variabilities using rule-based uncertainty expression was introduced. This framework may be used to deduce the overall variability in a simpler way.

Additional file

Additional file 1: Appendix Additional tables and figures.

Authors' contributions

WD carried out the research work, literature review, data collection, analysis of results, and wrote the manuscript. KK studied the collected data and discuss the main findings of the research. AN and NS revised the manuscript. All authors read and approved the final manuscript.

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Competing interests

The authors declare that they have no competing interests.

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