

## Research Article

# On the Convergence of Implicit Picard Iterative Sequences for Strongly Pseudocontractive Mappings in Banach Spaces

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We study the convergence of implicit Picard iterative sequences for strongly accretive and strongly pseudocontractive mappings. We have also improved the results of Ćirić et al. (2009).

## 1. Introduction and Preliminaries

Let  $E$  be a real Banach space with dual  $E^*$ . The symbol  $D(T)$  stands for the domain of  $T$ .

Let  $T : D(T) \rightarrow E$  be a mapping.

*Definition 1.* The mapping  $T$  is said to be *Lipschitzian* if there exists a constant  $L > 0$  such that

$$\|Tx - Ty\| \leq L \|x - y\| \quad (1)$$

for all  $x, y \in D(T)$ .

*Definition 2.* The mapping  $T$  is called *strongly pseudocontractive* if there exists  $t > 1$  such that

$$\|x - y\| \leq \|(1 + r)(x - y) - rt(Tx - Ty)\| \quad (2)$$

for all  $x, y \in D(T)$  and  $r > 0$ . If  $t = 1$  in inequality (2), then  $T$  is called *pseudocontractive*.

We will denote by  $J$  the *normalized duality mapping* from  $E$  to  $2^{E^*}$  defined by

$$J(x) = \{f^* \in E^* : \langle x, f^* \rangle = \|x\|^2 = \|f^*\|^2\}, \quad (3)$$

where  $\langle \cdot, \cdot \rangle$  denotes the generalized duality pairing. It follows from inequality (2) that  $T$  is *strongly pseudocontractive* if and only if there exists  $j(x - y) \in J(x - y)$  such that

$$\langle (I - T)x - (I - T)y, j(x - y) \rangle \geq k \|x - y\|^2 \quad (4)$$

for all  $x, y \in D(T)$ , where  $k = (t - 1)/t \in (0, 1)$ . Consequently, from inequality (4) it follows easily that  $T$  is *strongly pseudocontractive* if and only if

$$\|x - y\| \leq \|x - y + s[(I - T - kI)x - (I - T - kI)y]\| \quad (5)$$

for all  $x, y \in D(T)$  and  $s > 0$ .

Closely related to the class of pseudocontractive maps is the class of accretive operators.

Let  $A : D(A) \rightarrow E$  be an operator.

*Definition 3.* The operator  $A$  is called *accretive* if

$$\|x - y\| \leq \|x - y + s(Ax - Ay)\| \quad (6)$$

for all  $x, y \in D(A)$  and  $s > 0$ .

Also, as a consequence of Kato [1], this accretive condition can be expressed in terms of the duality mapping as follows.

For each  $x, y \in D(A)$ , there exists  $j(x - y) \in J(x - y)$  such that

$$\langle Ax - Ay, j(x - y) \rangle \geq 0. \quad (7)$$

Consequently, inequality (2) with  $t = 1$  yields that  $A$  is accretive if and only if  $T := (I - A)$  is pseudocontractive. Furthermore, from setting  $A := (I - T)$ , it follows from inequality (5) that  $T$  is strongly pseudocontractive if and only if  $(A - kI)$  is accretive, and, using (7), this implies that  $T = (I - A)$  is strongly pseudocontractive if and only if there exists  $k \in (0, 1)$  such that

$$\langle Ax - Ay, j(x - y) \rangle \geq k\|x - y\|^2 \tag{8}$$

for all  $x, y \in D(A)$ . The operator  $A$  satisfying inequality (8) is called *strongly accretive*. It is then clear that  $A$  is strongly accretive if and only if  $T = (I - A)$  is strongly pseudocontractive. Thus, the mapping theory for strongly accretive operators is closely related to the fixed point theory of strongly pseudocontractive mappings. We will exploit this connection in the sequel.

The notion of accretive operators was introduced independently in 1967 by Kato [1] and Browder [2]. An early fundamental result in the theory of accretive operators, due to Browder, states that the initial value problem

$$\frac{du}{dt} + Au = 0, \quad u(0) = u_0 \tag{9}$$

is solvable if  $A$  is locally Lipschitzian and accretive on  $E$ . If  $u$  is independent of  $t$ , then  $Au = 0$  and the solution of this equation corresponds to the equilibrium points of the system (9). Consequently, considerable research efforts have been devoted, especially within the past 15 years or so, to developing constructive techniques for the determination of the kernels of accretive operators in Banach spaces (see, e.g., [3–19]). Two well-known iterative schemes, the *Mann iterative method* (see, e.g., [20]) and the *Ishikawa iterative scheme* (see, e.g., [21]), have successfully been employed.

The Mann and Ishikawa iterative schemes are global and their rate of convergence is generally of the order  $O(n^{-1/2})$ . It is clear that if, for an operator  $U$ , the classical iterative sequence of the form,  $x_{n+1} = Ux_n$ ,  $x_0 \in D(U)$  (the so-called *Picard iterative sequence*) converges, then it is certainly superior and preferred to either the Mann or the Ishikawa sequence since it requires less computations and, moreover, its rate of convergence is always at least as fast as that of a geometric progression.

In [22, 23], Chidume proved the following results.

**Theorem 4.** *Let  $E$  be an arbitrary real Banach space and  $A : E \rightarrow E$  Lipschitz (with constant  $L > 0$ ) and strongly accretive with a strong accretive constant  $k \in (0, 1)$ . Let  $x^*$  denote a solution of the equation  $Ax = 0$ . Set  $\epsilon := (1/2)(k/(1 + L(3 + L - k)))$  and define  $A_\epsilon : E \rightarrow E$  by  $A_\epsilon x := x - \epsilon Ax$  for each  $x \in E$ .*

*For arbitrary  $x_0 \in E$ , define the sequence  $\{x_n\}_{n=0}^\infty$  in  $E$  by*

$$x_{n+1} = A_\epsilon x_n, \quad n \geq 0. \tag{10}$$

*Then  $\{x_n\}_{n=0}^\infty$  converges strongly to  $x^*$  with*

$$\|x_{n+1} - x^*\| \leq \delta^n \|x_0 - x^*\|, \tag{11}$$

*where  $\delta = (1 - (1/2)k\epsilon) \in (0, 1)$ . Moreover,  $x^*$  is unique.*

**Corollary 5.** *Let  $E$  be an arbitrary real Banach space and  $K$  a nonempty convex subset of  $E$ . Let  $T : K \rightarrow K$  be Lipschitz (with constant  $L > 0$ ) and strongly pseudocontractive (i.e.,  $T$  satisfies inequality (5) for all  $x, y \in K$ ). Assume that  $T$  has a fixed point  $x^* \in K$ . Set  $\epsilon_0 := (1/2)(k/(1 + L(3 + L - k)))$  and define  $T_{\epsilon_0} : K \rightarrow K$  by  $T_{\epsilon_0}x = (1 - \epsilon_0)x + \epsilon_0Tx$  for each  $x \in K$ . For arbitrary  $x_0 \in K$ , define the sequence  $\{x_n\}_{n=0}^\infty$  in  $K$  by*

$$x_{n+1} = T_{\epsilon_0}x_n, \quad n \geq 0. \tag{12}$$

*Then  $\{x_n\}_{n=0}^\infty$  converges strongly to  $x^*$  with*

$$\|x_{n+1} - x^*\| \leq \delta^n \|x_0 - x^*\|, \tag{13}$$

*where  $\delta = (1 - (1/2)k\epsilon_0) \in (0, 1)$ . Moreover,  $x^*$  is unique.*

Recently, Ćirić et al. [24] improved the results of Chidume [22, 23], Liu [14], and Sastry and Babu [18] as in the following results.

**Theorem 6.** *Let  $E$  be an arbitrary real Banach space and  $A : E \rightarrow E$  a Lipschitz (with constant  $L > 0$ ) and strongly accretive with a strong accretive constant  $k \in (0, 1)$ . Let  $x^*$  denote a solution of the equation  $Ax = 0$ . Set  $\epsilon := (k - \eta)/L(2 + L)$ ,  $\eta \in (0, k)$  and define  $A_\epsilon : E \rightarrow E$  by  $A_\epsilon x := x - \epsilon Ax$  for each  $x \in E$ . For arbitrary  $x_0 \in E$ , define the sequence  $\{x_n\}_{n=0}^\infty$  in  $E$  by*

$$x_{n+1} = A_\epsilon x_n, \quad n \geq 0. \tag{14}$$

*Then  $\{x_n\}_{n=0}^\infty$  converges strongly to  $x^*$  with*

$$\|x_{n+1} - x^*\| \leq \theta^n \|x_0 - x^*\|, \tag{15}$$

*where  $\theta = (1 - ((k - \eta)/(k(k - \eta) + L(2 + L)))\eta) \in (0, 1)$ . Thus the choice  $\eta = k/2$  yields  $\theta = 1 - k^2/2[k + 2L(2 + L)]$ . Moreover,  $x^*$  is unique.*

**Corollary 7.** *Let  $E$  be an arbitrary real Banach space and  $K$  a nonempty convex subset of  $E$ . Let  $T : K \rightarrow K$  be Lipschitz (with constant  $L > 0$ ) and strongly pseudocontractive (i.e.,  $T$  satisfies inequality (5) for all  $x, y \in K$ ). Assume that  $T$  has a fixed point  $x^* \in K$ . Set  $\epsilon_0 := (k - \eta)/L(2 + L)$ ,  $\eta \in (0, k)$  and define  $T_{\epsilon_0} : K \rightarrow K$  by  $T_{\epsilon_0}x = (1 - \epsilon_0)x + \epsilon_0Tx$  for each  $x \in K$ . For arbitrary  $x_0 \in K$ , define the sequence  $\{x_n\}_{n=0}^\infty$  in  $K$  by*

$$x_{n+1} = T_{\epsilon_0}x_n, \quad n \geq 0. \tag{16}$$

*Then  $\{x_n\}_{n=0}^\infty$  converges strongly to  $x^*$  with*

$$\|x_{n+1} - x^*\| \leq \theta^n \|x_0 - x^*\|, \tag{17}$$

*where  $\theta = (1 - ((k - \eta)/(k(k - \eta) + L(2 + L)))\eta) \in (0, 1)$ . Moreover,  $x^*$  is unique.*

In this paper, we study the convergence of implicit Picard iterative sequences for strongly accretive and strongly pseudocontractive mappings. We have also improved the results of Ćirić et al. [24].

## 2. Main Results

In the following theorems,  $L > 1$  will denote the Lipschitz constant of the operator  $A$  and  $k$  will denote the strong accretive constant of the operator  $A$  as in inequality (8). Furthermore,  $\epsilon > 0$  is defined by

$$\epsilon := \frac{k - \eta}{L + (1 + L)(k - \eta)}, \quad \eta \in (0, k). \quad (18)$$

With these notations, we prove the following theorem.

**Theorem 8.** *Let  $E$  be an arbitrary real Banach space and  $A : E \rightarrow E$  Lipschitz and strongly accretive with a strong accretive constant  $k \in (0, 1)$ . Let  $x^*$  denote a solution of the equation  $Ax = 0$ . Define  $A_\epsilon : E \rightarrow E$  by  $A_\epsilon x_n = (1 - \epsilon)x_{n-1} + \epsilon x_n - \epsilon Ax_n$  for each  $x_n \in E$ . For arbitrary  $x_0 \in E$ , define the sequence  $\{x_n\}_{n=0}^\infty$  in  $E$  by*

$$x_n = A_\epsilon x_n, \quad n \geq 1. \quad (19)$$

Then  $\{x_n\}_{n=0}^\infty$  converges strongly to  $x^*$  with

$$\|x_{n+1} - x^*\| \leq \rho^n \|x_0 - x^*\|, \quad (20)$$

where  $\rho = (1 - ((k - \eta)/(L + ((k - \eta)(1 + L + k)))\eta)) \in (0, 1)$ . Thus the choice  $\eta = k/2$  yields  $\rho = 1 - k^2/2[2L + k(1 + L + k)]$ . Moreover,  $x^*$  is unique.

*Proof.* Existence of  $x^*$  follows from [5, Theorem 13.1]. Define  $T = (I - A)$  where  $I$  denotes the identity mapping on  $E$ . Observe that  $Ax^* = 0$  if and only if  $x^*$  is a fixed point of  $T$ . Moreover,  $T$  is strongly pseudocontractive since  $A$  is strongly accretive, and so  $T$  also satisfies inequality (5) for all  $x, y \in E$  and  $s > 0$ . Furthermore, the recursion formula  $x_n = A_\epsilon x_n$  becomes

$$x_n = (1 - \epsilon)x_{n-1} + \epsilon Tx_n, \quad n \geq 1. \quad (21)$$

Observe that

$$x^* = (1 + \epsilon)x^* + \epsilon(I - T - kI)x^* - (1 - k)\epsilon x^*, \quad (22)$$

and from the recursion formula (21)

$$\begin{aligned} x_{n-1} &= (1 + \epsilon)x_n + \epsilon(I - T - kI)x_n \\ &\quad - (1 - k)\epsilon x_n + \epsilon^2(x_{n-1} - Tx_n), \end{aligned} \quad (23)$$

which implies that

$$\begin{aligned} x_{n-1} - x^* &= (1 + \epsilon)(x_n - x^*) \\ &\quad + \epsilon[(I - T - kI)x_n - (I - T - kI)x^*] \\ &\quad - (1 - k)\epsilon(x_n - x^*) + \epsilon^2(x_{n-1} - Tx_n). \end{aligned} \quad (24)$$

This implies using inequality (5) with  $s = \epsilon/(1 + \epsilon)$  and  $y = x^*$  that

$$\begin{aligned} &\|x_{n-1} - x^*\| \\ &\geq (1 + \epsilon) \left( \left\| (x_n - x^*) + \frac{\epsilon}{1 + \epsilon} \right. \right. \\ &\quad \left. \left. \times [(I - T - kI)x_n - (I - T - kI)x^*] \right\| \right) \\ &\quad - (1 - k)\epsilon \|x_n - x^*\| - \epsilon^2 \|x_{n-1} - Tx_n\| \\ &\geq (1 + \epsilon) \|x_n - x^*\| - (1 - k)\epsilon \|x_n - x^*\| \\ &\quad - \epsilon^2 \|x_{n-1} - Tx_n\| \\ &= (1 + k\epsilon) \|x_n - x^*\| - \epsilon^2 \|x_{n-1} - Tx_n\|. \end{aligned} \quad (25)$$

Observe that

$$\begin{aligned} \|x_{n-1} - Tx_n\| &\leq \|x_{n-1} - Tx_{n-1}\| + \|Tx_{n-1} - Tx_n\| \\ &\leq \|Ax_{n-1}\| + \|x_{n-1} - x_n\| + \|Ax_{n-1} - Ax_n\| \\ &\leq L \|x_{n-1} - x^*\| + (1 + L) \|x_{n-1} - x_n\| \\ &= L \|x_{n-1} - x^*\| + (1 + L)\epsilon \|x_{n-1} - Tx_n\|, \end{aligned} \quad (26)$$

and so

$$\|x_{n-1} - Tx_n\| \leq \frac{L}{1 - (1 + L)\epsilon} \|x_{n-1} - x^*\|, \quad (27)$$

so that from (25) we obtain

$$\begin{aligned} \|x_{n-1} - x^*\| &\geq (1 + k\epsilon) \|x_n - x^*\| \\ &\quad - \frac{L\epsilon^2}{1 - (1 + L)\epsilon} \|x_{n-1} - x^*\|. \end{aligned} \quad (28)$$

Therefore

$$\|x_n - x^*\| \leq \frac{1 + L\epsilon^2/(1 - (1 + L)\epsilon)}{1 + k\epsilon} \|x_{n-1} - x^*\|, \quad (29)$$

where

$$\begin{aligned} \rho &= \frac{1 + L\epsilon^2/(1 - (1 + L)\epsilon)}{1 + k\epsilon} \\ &= 1 - \frac{\epsilon}{1 + k\epsilon} \left( k - \frac{L\epsilon}{1 - (1 + L)\epsilon} \right) = 1 - \frac{\epsilon}{1 + k\epsilon} \eta \\ &= 1 - \frac{k - \eta}{L + (k - \eta)(1 + L + k)} \eta. \end{aligned} \quad (30)$$

From (29) and (30), we get

$$\begin{aligned} \|x_n - x^*\| &\leq \rho \|x_{n-1} - x^*\| \\ &\leq \dots \\ &\leq \rho^n \|x_0 - x^*\| \\ &\longrightarrow 0 \end{aligned} \quad (31)$$

as  $n \rightarrow \infty$ . Hence  $x_n \rightarrow x^*$  as  $n \rightarrow \infty$ . Uniqueness follows from the strong accretivity property of  $A$ .  $\square$

The following is an immediate corollary of Theorem 8.

**Corollary 9.** *Let  $E$  be an arbitrary real Banach space and  $K$  a nonempty convex subset of  $E$ . Let  $T : K \rightarrow K$  be Lipschitz (with constant  $L > 1$ ) and strongly pseudocontractive (i.e.,  $T$  satisfies inequality (5) for all  $x, y \in K$ ). Assume that  $T$  has a fixed point  $x^* \in K$ . Set  $\epsilon_0 := (k - \eta)/(L + (1 + L)(k - \eta))$ ,  $\eta \in (0, k)$  and define  $A_{\epsilon_0} : K \rightarrow K$  by  $A_{\epsilon_0} x_n = (1 - \epsilon_0)x_{n-1} + \epsilon_0 x_n - \epsilon_0 A x_n$  for each  $x_n \in K$ . For arbitrary  $x_0 \in K$ , define the sequence  $\{x_n\}_{n=0}^\infty$  in  $K$  by*

$$x_n = A_{\epsilon_0} x_n, \quad n \geq 1. \tag{32}$$

Then  $\{x_n\}_{n=0}^\infty$  converges strongly to  $x^*$  with

$$\|x_{n+1} - x^*\| \leq \rho_0^n \|x_0 - x^*\|, \tag{33}$$

where  $\rho_0 = (1 - ((k - \eta)/(L + (k - \eta)(1 + L + k)))\eta) \in (0, 1)$ . Thus the choice  $\eta = k/2$  yields  $\rho_0 = 1 - k^2/2[2L + k(1 + L + k)]$ . Moreover,  $x^*$  is unique.

*Proof.* Observe that  $x^*$  is a fixed point of  $T$  if and only if it is a fixed point of  $T_{\epsilon_0}$ . Furthermore, the recursion formula (32) is simplified to the formula

$$x_n = (1 - \epsilon_0)x_{n-1} + \epsilon_0 T x_n, \tag{34}$$

which is similar to (21). Following the method of computations as in the proof of the Theorem 8, we obtain

$$\begin{aligned} \|x_n - x^*\| &\leq \frac{1 + L\epsilon_0^2 / (1 - (1 + L)\epsilon_0)}{1 + k\epsilon_0} \|x_{n-1} - x^*\| \\ &= \left(1 - \frac{k - \eta}{L + (k - \eta)(1 + L + k)}\eta\right) \|x_{n-1} - x^*\|. \end{aligned} \tag{35}$$

Set  $\rho_0 = 1 - ((k - \eta)/(L + (k - \eta)(1 + L + k)))\eta$ . Then from (35) we obtain

$$\begin{aligned} \|x_n - x^*\| &\leq \rho_0 \|x_{n-1} - x^*\| \\ &\leq \dots \\ &\leq \rho_0^n \|x_0 - x^*\| \\ &\rightarrow 0 \end{aligned} \tag{36}$$

as  $n \rightarrow \infty$ . This completes the proof.  $\square$

*Remark 10.* Since  $L > 1$  and  $k < L$ , we have

$$L > k - \eta. \tag{37}$$

So we can easily obtain

$$\frac{1}{L + (k - \eta)(1 + L + k)} > \frac{1}{k(k - \eta) + L(2 + L)}. \tag{38}$$

Now

$$\begin{aligned} \rho &= 1 - \frac{(k - \eta)}{L + (k - \eta)(1 + L + k)}\eta \\ &< 1 - \frac{(k - \eta)}{k(k - \eta) + L(2 + L)}\eta \\ &= \theta. \end{aligned} \tag{39}$$

Thus the relation between Ćirić et al. [24] and our parameter of convergence, that is, between  $\theta$  and  $\rho$ , respectively, is the following:

$$\rho < \theta. \tag{40}$$

Our convergence parameter  $\rho$  shows the overall improvement for  $\theta$ , and consequently the results of Ćirić et al. [24] are improved.

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