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A NEW METHOD TO CALCULATE ALLOMETRIC LENGTH-MASS RELATIONSHIPS OF DINOSAURS

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ABSTRACT—Body mass is an important determinant of most biological functions, and knowing the mass of extinct animals is essential in order to learn about their biology. It was the aim of this paper to develop a method of mass estimation which would make it possible to determine allometric length-mass relationships for the different groups of dinosaurs. Mass is calculated from graphical reconstructions of fossils, or from photos of skeletal mounts or live animals. Body shape of animals is described by high order polynomial equations. Integration of the polynomial gives body mass of a 'round' animal, which is then corrected for animal width by intersection with a second equation ($Y = 1 - ax^2$). The method was validated by predicting body mass of extant animals of known mass and with complex body shapes (kangaroos, emu, elephant, giraffe, rhinoceros). Body mass increased allometrically with total length in all groups of dinosaurs (Ankylosauria, Ceratopsia, Ornithopoda, Prosauropoda, Sauropoda, Stegosauria and Theropoda), but 95% confidence intervals were very large for Ankylosauria and Stegosauria so that, for those groups, the resulting regression equations have little predicting power. Scaling exponents were least for the Sauropoda which may have grown less massive to function at their great body size. Scaling exponents were greatest for the Theropoda, but it was speculated that small coelurosaurs, as the precursors of birds, may have grown less massive compared to other theropods. Mass estimated by the 'polynomial' method presented here did not differ significantly from mass estimates in the literature where these were available.

INTRODUCTION

The dinosauria underwent an extraordinary radiation over more than 150 million years, and one of the most striking features about dinosaurs is the great range of sizes they achieved which is unparalleled among terrestrial animals. This great diversity raises many biological questions about their physiology (Spotila et al., 1991; Reid, 1997), morphology (Alexander, 1985; Christiansen, 1997) and ecology (Dunham et al., 1989; Farlow, 1993). In order to answer most of these questions, however, it is necessary to estimate body mass. The rate of most biological processes, for example metabolic rate (Coulson and Hernandez, 1983), thermal physiology (Seebacher et al., 1999), and digestion (Schmidt-Nielsen, 1984), change with body mass according to well known but complex scaling laws (Schmidt-Nielsen, 1984; West et al., 1997).

A number of different techniques, such as measuring the volume of scale models (Colbert, 1962; Alexander, 1985; Farlow et al., 1995; Paul, 1988), relating bone circumference to body mass (Anderson et al., 1985), and using the mathematical method of 3-D slicing (Henderson, 1999), have been applied already to estimate dinosaur body mass. Similar techniques have also been used to estimate mass of other extinct animals, notably that of extinct mammals whose mass was estimated from osteological measurements of a large number of modern species within that group (Christiansen, 1999a). Also, the mass of the pelycosaur *Edaphosaurus* has been estimated by graphic double integration, whereby the sum of the volumes of numerous cylinders into which the body is divided gives an estimate of total mass, as well as by extrapolations from osteological measurements and length-mass relationships of extant mammals and alligators (Hurlburt, 1999).

The aims of this study were to develop a computationally simple method to estimate mass of dinosaurs from reconstructions published in the literature. The value of such a method would lie in the fact that, because graphical reconstructions are easily accessible, it would be possible to estimate body mass of a comparatively large number of species so that allometric relationships of dinosaurs could be determined. Hence, it was the second aim of this study to find power equations relating

body mass to body length of the major taxonomic groups of dinosaurs. Such allometric equations would be very useful for future studies and they would make it possible, for example, to determine body mass of newly discovered dinosaurs, because body length can be derived from (relatively complete) fossils.

The method I developed to estimate body mass of living and extinct animals relies on describing the two-dimensional outline of animals mathematically, and then integrating to estimate the volume and, hence, mass, after correcting for body width. The validity of the technique was tested by estimating the mass of extant animals for which independent mass measurements are available, and which represent a great diversity of body shapes.

MATERIALS AND METHODS

The technique presented is an extension of methods used to calculate the mass of crocodiles over a great size range (2.6–1,010 kg), where it worked very well when validated against empirical data (Seebacher et al., 1999). However, crocodiles are of relatively simple body shape, and the technique was further developed here to include more complex body shapes. Hence, the validity of predictions was tested by estimating the mass of animals with complex and varied body shape. Photographs of museum specimens (Zoology Museum, University of Queensland, Brisbane, Australia) were taken to estimate the mass of taxidermic mounts of Red Kangaroos (*Macropus rufus*) and a Red-necked Wallaby (*Macropus rufogriseus*), as well as of skeletal mounts of *M. rufogriseus* (Fig. 1) and an emu, *Dromaius novaehollandiae*. In addition, I determined the mass of an elephant (*Elphas maximus*), a giraffe (*Giraffa camelopardalis*), and a rhinoceros (*Diceros bicornis*) from photographs published in Walker et al. (1964). Photographs of museum specimens were used rather than measurements of the specimens themselves in order to emulate the two dimensional character of dinosaur reconstructions in the literature. Body mass for *Macropus* was also determined independently from allometric field data relating hind foot length to body mass (Tony Pople, unpubl. data), and ranges of body mass for the emu, giraffe, elephant and rhinoceros were taken from the literature (Table 1).

Dinosaur body dimensions, from which mass estimates were

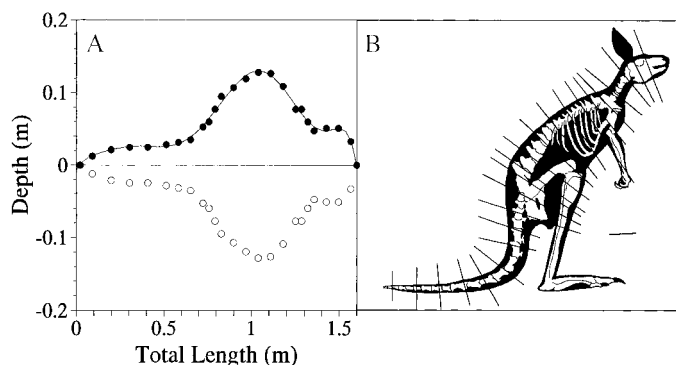


FIGURE 1. *Macropus rufogriseus* as an example to demonstrate the method used to calculate dinosaur body mass. The depth of the animal was measured at regular intervals from a skeletal reconstruction (right panel). The measured depth was then plotted in a cartesian coordinate system with $y = 0$ as the body midline. A polynomial (solid line) was fitted to the depth measurements (solid circles) at the dorsal surface (=half total depth). The volume of revolution of the polynomial was determined by integration over the total length.

made, were determined from published reconstructions separately for ankylosauria, marginocephalia, ornithopoda, prosauropoda, sauropoda, stegosauria, and theropoda (see Table 2 for references). An effort was made to use reconstructions based on particular museum specimens. However, these were not always available, and some reconstructions were used which identified specimens by genus only and which made no reference to particular fossil specimens (Table 2).

The two-dimensional outline of animals was described by polynomial equations which were fitted to measurements taken from photographs or drawings (see below). Polynomials were fitted to the measured values by the Marquardt-Levenberg method in CurveExpert 1.2 software. Note that polynomials are a mathematical series of the form

$$Y = a_0x^0 + a_1x^1 + a_2x^2 \dots a_nx^n$$

where in the present case x = total length (m) and Y = mass (kg). As with most mathematical series, the precision of the solution will increase the more terms are added to the series. In practical terms, this means that very simple animal shapes, such as the outline of a crocodile, can be described adequately by a second order polynomial (Seebacher et al., 1999), but the mathematical description of more complex shapes, such as those of dinosaurs or kangaroos, require higher order polynomials. Hence, in all mass estimates reported below, eighth order polynomials were used to describe body outlines.

TABLE 1. Total length (m) and body mass (kg) of extant animals of various body shapes estimated by the 'polynomial' method. Independent mass estimates are also given, and these are based on allometric field data for *Macropus* or on values in the literature. Sources for the specimens or photos used to estimate mass by the polynomial method, and sources for independent mass estimates are given.

Species	TL	Estimated		Independent	
		Mass	Source	Mass	Source
<i>Macropus rufus</i> (male) ¹	2.07	63.4	UQZM	62.9	Field Data
<i>Macropus rufus</i> (female) ¹	1.51	21.3	UQZM	24.4	Field Data
<i>Macropus rufogriseus</i> ¹	1.58	23.3	UQZM	24.6	Field Data
<i>Macropus rufogriseus</i> ²	1.50	20.8	UQZM	21.5	Field Data
<i>Dromaius novahollandiae</i> ³	1.52	18.4	UQZM	30–55	del Hoyo et al. (1992)
<i>Elphas maximus</i>	5.53	4,855.7	Walker (1964)	5,000	Walker (1964)
<i>Giraffa camelopardalis</i>	3.74	899.7	Walker (1964)	550–1,800	Walker (1964)
<i>Diceros bicornis</i>	3.12	1,313.7	Walker (1964)	1,000–1,800	Walker (1964)

¹Taxidermic mount.

²Skeletal reconstruction.

³Skeletal reconstruction of juvenile or small adult.

The depth of the body was defined and measured as the linear distance between the ventral and dorsal surfaces perpendicular to the vertebral column. Measurements were taken at regular intervals of no more than 10% of total length for 'regular' sections of the body, such as long tails, but at intervals of less than 5% for more 'irregular' sections, such as the pectoral and pelvic girdles (Fig. 1B). The measured depth was then plotted in a cartesian coordinate system with $y = 0$ as the centreline of the body, and the polynomial was fitted to the positive y -values (0.5 total depth = dorsal surface; Fig. 1A).

Integration of the polynomial [$f(x)$] over the total length of the animal gives the volume of the round animal; the volume of revolution of any equation is calculated as $V = \pi \int f(x)^2 dx$ (Stewart, 1991). The volume was multiplied by the density to give an estimate of mass. Density was assumed to be 1,000 kg m⁻³ for all animals (Alexander, 1989; Hurlburt, 1999) except for the emu where it was assumed to be 850 kg m⁻³ to account for airsacks. It is likely that some theropoda possessed airsacks, but the extent of their occurrence is not known (Ruben et al., 1997). Hence, to avoid unnecessary speculation, I followed Alexander (1989) and Hurlburt (1999), except for the emu which undoubtedly have airsacks.

Few animals are round, however, so that mass estimates of 'round' animals described above have to be corrected for width. Again, the width of dinosaurs was estimated from skeletal reconstructions. However, relatively few published reconstructions represent cross-sections or 'top-down' views of dinosaurs, so that available width measurements were applied also to other species within the same taxonomic group for which there were no width estimate available. For example, ratios of depth:width (see below) which were based on measurements of *Sauropelta* (Carpenter, 1984) were assumed to be applicable also to *Nodosaurus*. Cross-sectional or top-down views were available for some species of each taxonomic group (Borsuk-Bialynicka, 1977; Carpenter, 1981, 1984; Lucas, 1994; McIntosh, 1997; Paul, 1988, 1990; Sereno, 1990) except for prosauropods which were assumed to be of similar shape as sauropods. In addition, width was also determined from skeletal reconstructions of *Muttaborrasaurus* (QM F6140) and *Probactrosaurus* (a cast of MHP 2231/1) kept at the Queensland Museum, Brisbane, Australia. Again, two-dimensional photographs of the specimens of *Muttaborrasaurus* and *Probactrosaurus* were used rather than taking measurements on the three dimensional reconstructions.

Width and depth were measured at the same point of the body, which gives a ratio of the linear measurements of width:depth. However, because the lateral surfaces of animals do not follow straight lines, the linear width:depth ratio has to be translated to a more curvaceous shape. Hence, the actual shape of animals was represented by a curve with the equation

TABLE 2. Mass estimates (kg) of dinosaurs determined by the 'polynomial' technique. The total length (TL, m) as well as the reference in which reconstructions were published are given. Species names and museum numbers of specimens on which reconstructions were based are given where available.

Species	Museum #	TL	Mass	Reference
Ankylosauria				
<i>Ankylosaurus magniventris</i>	—	6.6	1,719.2	Carpenter (1990)
<i>Euoplocephalus tutus</i>	BMNH 5161	6.1	2,675.9	Carpenter (1981)
<i>Nodosaurus</i>	—	5.0	684.8	Carpenter (1997)
<i>Pinacosaurus gangeri</i>	—	4.8	707.2	Carpenter (1990)
<i>Saichania</i>	—	6.6	1,417.2	Carpenter (1990)
<i>Sauropelta edwardsi</i>	AMNH 3035 AMNH 3056	5.2	902.9	Carpenter (1984)
Marginocephalia				
<i>Centrosaurus</i>	—	4.7	1,079.7	Forster and Sereno (1997)
<i>Chasmosaurus</i>	—	5.0	1,658.7	Paul (1990)
<i>Homocephale</i>	—	3.0	73.7	Paul (1990)
<i>Monoclonius</i>	—	6.0	1,833.6	Paul (1990)
<i>Pentaceratops sternbergii</i>	—	7.5	4,846.0	Paul (1990)
<i>Protoceratops andrewsi</i>	AMNH 6467	1.4	23.7	Brown and Schlaikjer (1940)
<i>Psittacosaurus mongoliensis</i>	AMNH 6253	1.5	12.1	Sereno (1990)
<i>Stegoceras</i>	—	2.0	26.7	Forster and Sereno (1997)
<i>Triceratops horridus</i>	BSP1964 I458 USNM 4842	8.0	4,964.0	Ostrom and Wellnhofer (1985)
Ornithopoda				
<i>Anatosaurus annectens</i>	YPM 1190 USNM 2414	8.8	3,990.8	Galton (1970)
<i>Anatotitan</i>	—	1.20	7,594.4	Brett-Surman (1997)
<i>Bactrosaurus johnsoni</i>	AMNH 6553	6.0	1,588.9	Godefroit et al. (1998) Paul (1990)
<i>Camptosaurus prestwichii</i>	OUM J.3303	3.5	268.4	Galton and Powell (1980)
<i>Corythosaurus casuarius</i>	AMNH 5240	8.1	3,078.5	Galton (1970)
<i>Dryosaurus altus</i> ¹	YPM, CM, HMN, BMNH, DMN, AMNH	3.2	104.3	Galton (1977), Sues and Norman (1990)
<i>Gasparinisaura cincosaltensis</i>	MUCPv-208	0.65	0.98	Coria and Salgado (1996)
<i>Heterodontosaurus</i>	—	1.0	1.8	Brett-Surman (1997)
<i>Hypsilophodon foxii</i>	BMNH R196	1.4	7.0	Galton (1974), Paul (1990)
<i>Iguanodon mantelli</i>	BMNH R 5764	5.1	678.4	Norman (1980)
<i>Iguanodon bernissartensis</i>	IRSNB 1535	7.9	3,775.7	Norman (1980)
<i>"Kritosaurus" incurvimanus</i>	—	6.5	1,895.0	Weishampel and Horner (1990)
<i>Muttaborrasaurus langdoni</i> ²	QM F6140	9.1	4,100.4	QM, Bartholomai and Molnar (1981)
<i>Ouranosaurus nigeriensis</i>	—	5.9	1,120.4	Norman and Weishampel (1990)
<i>Parasaurolophus</i>	—	9.0	5,056.8	Brett-Surman (1997)
<i>Probactrosaurus gobiensis</i> ²	MHP 2231/1	3.5	179.3	QM; Rozhdestvensky (1966)
<i>Shatungosaurus</i>	—	17.0	22,467.1	Brett-Surman (1997)
<i>Tenontosaurus</i>	—	4.5	242.9	Brett-Surman (1997)
<i>Thescelosaurus</i>	—	1.5	7.9	Brett-Surman (1997)
<i>Yandusaurus</i>	—	1.5	6.6	Brett-Surman (1997)
Prosauropoda				
<i>Anchisaurus sinensis</i>	—	2.8	84.0	Dong (1992)
<i>Lufengosaurus huenei</i>	—	6.2	1,193.3	Dong (1992)
<i>Massospondylus</i>	—	4.0	136.7	Paul (1990)
<i>Plateosaurus engelhardti</i>	AMNH 6810	6.5	1,072.6	Galton (1986)
<i>Riojasaurus</i>	—	10.0	3,038.7	van Heerden (1997)
<i>Thecodontosaurus antiquus</i> ¹	ANSP BRSMG BMNH, YPM	2.6	24.6	Benton et al. (2000)
Sauropoda				
<i>Amargasaurus cazaui</i>	—	10.3	6,852.9	Salgado and Bonaparte (1991)
<i>Apatosaurus louisae</i>	CM 3018	21.0	22,407.2	Christiansen (1997) McIntosh et al. (1997)
<i>Barosaurus</i>	—	26.0	20,039.5	McIntosh et al. (1997)
<i>Brachiosaurus altithorax</i> ³	FCM	21.0	28,264.6	Riggs (1903) McIntosh et al. (1997)
<i>Camarasaurus lewisi</i> ⁴	BYU 9047	15.4	11,652.2	McIntosh et al. (1996) McIntosh et al. (1997)
<i>Dicraeosaurus</i>	—	12.0	4,421.5	McIntosh et al. (1997)
<i>Diplodocus carnegiei</i>	CM	25.7	19,654.6	Holland (1910)
<i>Haplocanthosaurus</i>	—	14.0	14,528.6	McIntosh et al. (1997)
<i>Mamenchisaurus hochuanensis</i> ⁵	—	21.0	18,169.7	McIntosh et al. (1997)
<i>Omeisaurus tiafuensis</i>	ZDM T5701 ZDM T5702 ZDM T5703 ZDM T5704	20.0	11,796.0	He et al. (1988), Paul (1990)
<i>Opisthocoelicaudia skarzynskii</i>	ZPAL MgD-I/48	11.4	10,522.2	Borsuk-Bialynicka (1977)
<i>Patagosaurus</i>	—	15.0	9,435.4	McIntosh et al. (1997)
<i>Seismosaurus halli</i>	NMMNH 369	40.0	49,275.5	Gillette (1994)
<i>Shunosaurus lii</i>	ZDM T5402	8.7	4,793.5	Dong and Tang (1984) Zhang (1988)

TABLE 2. (Continued)

Species	Museum #	TL	Mass	Reference
Stegosauria				
<i>Huayangosaurus taibii</i>	ZDM T7001	4.5	301.4	Zhou (1984)
<i>Kentrosaurus</i>	HMN	4.0	321.1	Galton (1997)
<i>Scelidosaurus harrisonii</i>	—	3.0	64.5	Galton (1997)
<i>Stegosaurus stenops</i>	USNM4934 USNM4714	6.5	2,610.6	Galton (1997), Paul (1990)
<i>Tuojiangosaurus multispinus</i>	CV 209	7.0	1,134.3	Dong (1990)
Theropoda				
<i>Afrovenator abakensis</i>	UCOBA1	7.6	826.6	Sereno et al. (1994)
<i>Albertosaurus libratus</i>	AMNH 5458	8.6	2,465.0	Paul (1988)
<i>Allosaurus fragilis</i>	USMN 4734	7.4	952.0	Paul (1988)
<i>Alxasaurus elesitaiensis</i>	IVPP 88402	3.9	199.9	Russell and Dong (1993a)
<i>Archaeopteryx lithographica</i>	HMN MB. 1880/81	0.4	0.25	Paul (1988)
<i>Avimimus portentosus</i>	PIN 3907-1 PIN 3907-3	1.5	21.4	Paul (1988)
<i>Carcharodontosaurus saharicus</i>	SGM Din-1; 1922X34	12.0	6,173.2	Currie (1996) Sereno et al. (1996)
<i>Ceratosaurus nasicornis</i>	USMN 4735	5.7	418.4	Paul (1988)
<i>Coelophysis bauri</i>	AMNH 7223	2.7	16.0	Paul (1988)
<i>Compsognathus longipes</i>	BSP AS I563	0.8	3.5	Ostrom (1978)
<i>Deinonychus antirrhopus</i> ¹	YPM, AMNH	3.0	104.7	Ostrom (1969)
<i>Deltadromeus agilis</i>	SGM-Din2	8.0	1,048.9	Sereno et al. (1996)
<i>Eoraptor lunensis</i>	PVSJ512	1.0	2.7	Sereno et al. (1993)
<i>Giganotosaurus carolinii</i>	MUCPv-CH-1	12.5	6,594.8	Coria and Salgado (1995)
<i>Herrerasaurus ischigualastensis</i>	MCZ706 PVSJ53, 373, 407 PVL2566	5.0	347.8	Sereno and Novas (1992)
<i>Metriacanthosaurus shangyouensis</i>	CV 00215	7.9	1,225.6	Paul (1988)
<i>Ornitholestes hermanni</i>	AMNH 619	2.1	13.5	Paul (1988)
<i>Ornithomimus bullatus</i>	GA 100/11	6.0	585.7	Paul (1988)
<i>Sinornithoides youngi</i>	IVPP V9612	1.2	2.2	Russell and Dong (1993b)
<i>Sinraptor dongi</i>	IVPP 10600	7.0	1,009.0	Currie and Zhao (1993)
<i>Suchomimus tenerensis</i>	MNN GDF500	11.0	3,816.1	Sereno et al. (1998)
<i>Syntarsus rhodesiensis</i>	QG 1	2.2	13.8	Paul (1988)
<i>Tyrannosaurus rex</i>	CM 9380 AMNH 5027	12.0	6,650.9	Paul (1988)
<i>Velociraptor antirrhopus</i>	YPM 5232 AMNH 3015	3.1	44.3	Paul (1988)

¹Numerous fragments kept at the museums listed.

²Mass estimates were based on photos, taken by the author, of skeletal reconstructions at the Queensland Museum, Brisbane, Australia. The original fossil descriptions are given in the references.

³The reconstruction of *Brachiosaurus* in McIntosh et al. (1997) does not give species name or museum locality. The length of the femur and humerus are consistent, however, with the description of *B. altithorax* given in Riggs (1903) who comments on the great length of the femur in this species.

⁴As for *Brachiosaurus*, species name and museum catalog numbers are not given for the graphical reconstruction of *Camarasaurus* in McIntosh et al. (1997). The length of the femur given by McIntosh et al. (1997) seems to indicate, however, that the reconstruction is of *C. lewisi*, based on comparative data given in McIntosh et al. (1996).

⁵The reconstruction of *Mamenchisaurus* in McIntosh et al. (1997) fits the description of *M. hochuanensis* given in Dong (1992), and for which a complete specimen exists. The other species, *M. constructus*, is known from an incomplete specimen only.

$$y = 1 - ax^2$$

where y = depth, x = width, and the linear width:depth ratio = $(1/a)^{0.5}$ (Fig. 2). In Fig. 2, the cross-sections of a 'round' body shape and that of a realistically shaped hypothetical animal are shown, and the ratio between the areas under the curves $(1-ax^2)$:round) in, for example, the positive quadrant is the same as the ratio between the volumes of the 'round' animal and an animal with realistic $(1 - ax^2)$ body shape. Hence, the areas under the two curves were determined by integrating in the positive quadrant of the coordinate system, and the final body volume, and mass, were calculated by multiplying the mass estimate of the round animal shape by the ratio of the areas under these curves.

For example, squaring and integrating the polynomial fitted to the data from the wallaby (Fig. 1B) and multiplying by density gives a body mass of 28.1 kg for the round shape. The linear ratio between width and depth was only 0.87, however, so that using the volume of a round animal would lead to an

overestimate of body mass. The area under the curve of $y = 1 - ax^2$ was calculated from the measured width:depth ratio, to give the ratio of the integrals of $1 - ax^2$: circle which was 0.74, so that the final body mass was $28.1 * 0.74 = 20.8$ kg.

Leg mass was calculated separately, and legs were assumed to be cylinders. Length and width of the legs was determined from reconstructions, and leg width was measured at intervals of at least 10% total leg length. The width was then averaged for the whole length to give the diameter of the cylinder.

Non-linear regression equations were fitted to calculated mass (y) and total length (x) data using least-squares regression procedures in Systat 8.0 (SPSS Inc.) software. Model I regression was chosen, because total length was assumed to be fixed in the analysis, and the high coefficients of determination (Table 3) indicate that the regression model was appropriate and that it explained most of the variation in the data (Sokal and Rohlf, 1981). All regressions are presented as allometric power equations, i.e., $Mass = aTotal\ Length^b$, and 95% confidence intervals were calculated for the exponent.

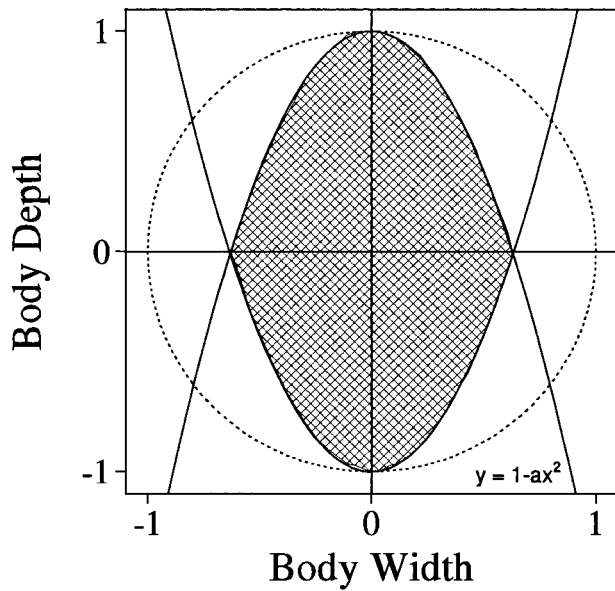


FIGURE 2. Body mass of the round animal is corrected for real animal width by superimposing the curve $Y = 1 - ax^2$ (solid line) onto a cross section of the round body shape (dotted line). Note that in order to show the resulting animal shape (hatched area) $Y = 1 - ax^2$ as well as $Y = -(1 - ax^2)$ were plotted. The ratio of areas under the curves of the circle and $Y = 1 - ax^2$ in the positive quadrant, for example, is the same as the ratio of their respective volumes. Hence, by integrating the two curves in the positive quadrant, and multiplying the volume of the round animal by the ratio of the integrals, the mass of the realistically shaped animals could be determined.

Museum Abbreviations: AMNH, American Museum of Natural History, New York, USA; ANSP, Academy of Natural Sciences, Philadelphia, USA; BMNH, British Museum (Natural History), London, UK; BRSMG, Bristol City Museum and Art Gallery, Bristol, UK; BSP, Bayerische Staatssammlungen für Paläontologie, Munich, Germany; BYU, Brigham Young University, Provo, USA; CM, Carnegie Museum, Pittsburgh, USA; CV, Municipal Museum of Chungking, China; DNM, Dinosaur National Monument, Utah, USA; FCM, Field Columbian Museum, Columbia, USA; GI, Geological Institute, Ulan Bator, Mongolia; HMN, Humboldt Museum für Naturkunde, Berlin, Germany; IRSNB, Institut Royal des Sciences Naturelles de Belgique, Brussels, Belgium; IVPP, Institut of Vertebrate Paleontology and Paleoanthropology, Beijing, China; MCZ, Museum of Comparative Zoology, Cambridge, UK; MNN, Musée National du Niger, Niger; NMMNH, New Mexico Museum of Natural History, Albuquerque, USA; OUM, Oxford University Museum, Oxford, UK; PIN, Palaeontological Institute, Moscow, Russia; PVSJ, Museo de Ciencias Naturales, Universidad Nacional de San Juan, San Juan, Argentina; QG, Queen Victoria Museum, Salisbury, UK; QM, Queensland Museum, Brisbane, Australia; SGM, Ministère de l'Énergie et des Mines, Rabat, Morocco; UCOPA, University of Chicago, Chicago, USA; UQZM, University of Queensland Zoology Museum, Brisbane, Australia; USNM, United States National Museum, Washington DC, USA; YPM, Peabody Museum Yale University, New Haven, USA; ZDM, Zigong Dinosaur Museum, Sichuan, China; ZPAL, Institut of Paleobiology, Polish Academy of Sciences, Warsaw, Poland.

RESULTS AND DISCUSSION

The 'polynomial' method reliably predicted body mass of extant animals (Table 1). For the four specimens of *Macropus*,

TABLE 3. Regression equations relating body mass (kg) to total length (m) for each taxonomic group of dinosaur. Regression equations are in the form $Y = aX^b$, and 95% confidence intervals for the exponent as well as coefficients of determination (R^2) are given.

Taxonomic group	a	b	± 95% CI	R^2
Ankylosauria	16.54	2.51	4.60	0.54
Ceratopsia	12.58	2.90	0.94	0.98
Ornithopoda	11.81	2.66	0.14	0.99
Prosauropoda	12.32	2.40	0.64	0.99
Sauropoda	214.44	1.46	0.36	0.86
Stegosauria	10.95	2.64	6.76	0.59
Theropoda	0.73	3.63	0.38	0.98

the predicted 'polynomial' mass was within 6.1% (range 0.76–14.6%) of the independently determined mass which would be well within the naturally occurring variations between animals of the same body length. The specimen of *Dromaius* used is that of a juvenile or small adult. An adult emu stands 1.5–1.9 m tall (del Hoyo et al., 1992) while the emu skeleton at the UQZM is 1.15 m tall, so that the lower mass estimate is reasonable.

The linear dimensions of *Giraffa*, *Elphas*, and *Diceros* were taken to lie in the middle of the range given by Walker et al. (1964), so that the mass estimates, which also lie in the middle of the range given (except for *Elphas* for which the mass was given as "about" 5,000 kg), appear to be accurate and confirm the validity of the technique (Table 1).

Calculated mass of dinosaurs increased allometrically with body length (Table 2, Fig. 3). The high coefficients of determination (R^2) associated with the curves fitted to the data (Table 3) indicate that the regression equations explain most of the variation in the data, except for Ankylosauria and Stegosauria where R^2 values were considerably less than for the other groups of dinosaurs. Similarly, small sample sizes and considerable variation between species resulted in very large 95% confidence intervals in the latter two groups so that the regression equations have very little predictive power. However, confidence intervals for the other groups of dinosaurs were relatively narrow given the statistically small sample sizes, and their magnitude is comparable to values reported for allometric equations relating body mass to osteological measurements in mammals (Christiansen, 1999b).

It is interesting to note that the slope (upper 95% CI) for sauropods is less than that for the other groups. This means that sauropods grew less massive with increasing body length compared to other dinosaurs (excluding ankylosaurs and stegosaurs given their extremely wide confidence intervals). A similar relationship exists for the scaling of long bones in mammals where the regression slopes of small mammals are consistently steeper than for large mammals (Christiansen, 1999a). These patterns indicate that there may be special morphological adaptations to cope with great body mass in the larger taxa (Christiansen 1999a) which may be at least partly dictated by the need to maintain locomotory potential (Christiansen, 1997).

Body mass increase with body length was steepest in theropods, but allometric differences between theropods, which were wholly bipedal, and other dinosaur groups, which were at least partly quadrupedal, may be explained by differences in their general body morphology. There may be reason to speculate, however, that small coelurosaurian theropods may have grown less massive than other theropods, because they may have shared mass-reducing morphological features with modern Aves which are believed to have evolved from small coelurosaurians (Padian et al., 1999; Sereno, 1999). Large coelurosaurians such as *Tyrannosaurus*, on the other hand, are likely to resemble other large (non-coelurosaurian) theropods as a result of size

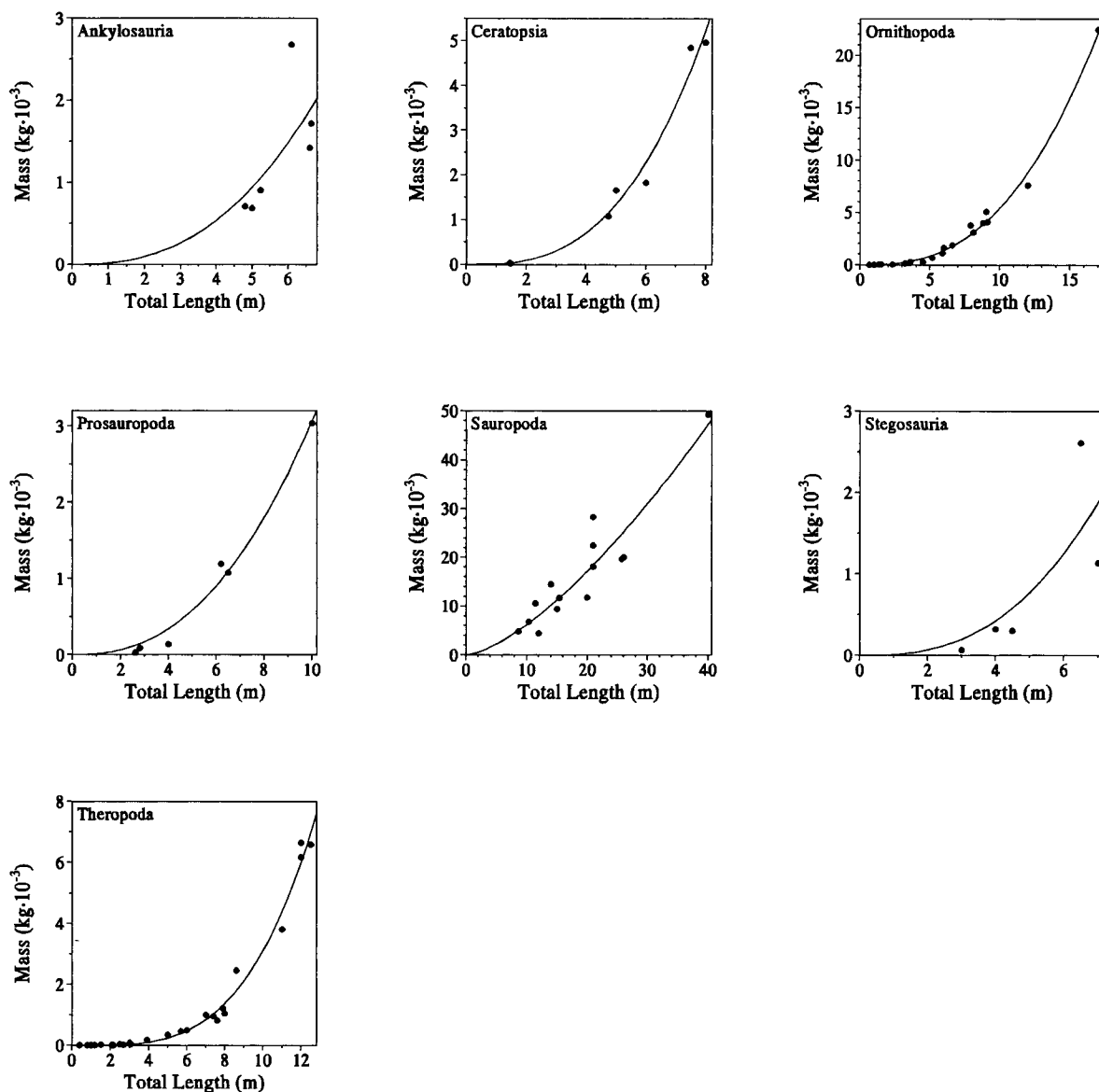


FIGURE 3. Calculated body mass of dinosaurs plotted against total length for each of the dinosaur groups. Details of the allometric equations (solid lines) fitted to the data are given in Table 3.

related convergence (Holtz, 1994). Note, however, that it is not known to what extent even small coelurosaurian theropod dinosaurs displayed anatomical features, such as airsacs, seen in modern birds (Ruben et al., 1997). The only evidence for the existence of airsacs comes from soft-tissue preservation in fossils of two small coelurosaurs (Dal Sasso and Signore, 1998; Martill et al., 2000), so that my argument here must be treated as speculative with respect to airsacs, although theropods undoubtedly share numerous characteristics with Aves (Feduccia, 1999). Nonetheless, in order to explore a possible differences in scaling exponents between different groups of theropods, I repeated the regression analysis for theropods after dividing the data into "small coelurosaurs" (*Alxasaurus*, *Archaeopteryx*, *Avimimus*, *Compsognathus*, *Deinonychus*, *Ornitholestes*, *Sinornithoides* and *Velociraptor*) and "other" theropods. The regression slope for "small" coelurosaurs is indeed less ($a = 3.19$, $b = 2.82 \pm 0.40$ 95%CI, $R^2 = 0.99$) than that for "other" theropods ($a = 0.69$, $b = 3.65 \pm 0.55$ 95%CI).

Most techniques which have been employed to estimate the

mass of dinosaurs and other extinct animals are similar in that they are based on models or reconstructions from fossils (Colbert, 1962; Alexander, 1985; Paul, 1988; Farlow et al., 1995; Christiansen, 1997; Henderson, 1999; Hurlburt, 1999), except for mass estimates based on bone circumferences (Anderson et al., 1985). Hurlburt (1999) also presents methods which predict body mass of a pelycosaur from regression equations relating mass to either total length, or long bone dimensions of alligators and mammals. These methods would be inappropriate for dinosaurs, because dinosaur body shape is too complex and varied to make crocodylians an appropriate model organism. Moreover, long bones in mammals do not follow a uniform scaling relationship, but subgroups within the Mammalia scale differently (Christiansen, 1999a), so that assuming 'mammals' to be representative of 'dinosaurs' would be inappropriate.

Overall, my mass estimates do not differ significantly from estimates in the literature for the same species where these are available (two sample *t*-test: $t = -1.49$, $df = 59$, $P = 0.14$; Table 4), and there are no systematic differences between my

TABLE 4. Comparisons between body mass (kg) of dinosaurs estimated by the polynomial method and body mass for the same genera cited in the literature.

Genus	Polynomial mass	Literature mass	Reference
Ceratopsia			
<i>Protoceratops</i>	23.7	177	Colbert (1962)
<i>Triceratops</i>	4,963.6	8,480 6,000 3,938	Colbert (1962) Alexander (1989) Henderson (1999)
Ornithopoda			
<i>Anatosaurus</i>	3,990.8	3,070	Colbert (1962)
<i>Camptosaurus</i>	268.4	383	Colbert (1962)
<i>Corythosaurus</i>	3,078.5	3,820	Colbert (1962)
<i>Dryosaurus</i>	104.3	70	Heinrich et al. (1993)
<i>Iguanodon</i>	3,775.7	5,400 4,510 3,790	Alexander (1989) Colbert (1962) Henderson (1999)
<i>Tenontosaurus</i>	243.0	600	Spotila et al. (1991)
<i>Thescelosaurus</i>	7.9	310	Anderson et al. (1985)
Sauropoda			
<i>Apatosaurus</i>	22,407.2	34,000 32,420 27,870 35,000 19,500	Alexander (1989) Colbert (1962) Colbert (1962) Anderson et al. (1985) Christiansen (1997)
<i>Brachiosaurus</i>	28,264.6	47,000 30,000 32,000 29,000 78,260 37,400	Alexander (1989) Reid (1997) Paul (1988) Anderson et al. (1985) Colbert (1962) Christiansen (1997)
<i>Camarasaurus</i>	11,652.2	8,800	Christiansen (1997)
<i>Dicraeosaurus</i>	4,421.5	5,400	Christiansen (1997)
<i>Diplodocus</i>	19,654.6	13,421 10,560 18,500 5,000 15,200	Henderson (1999) Colbert (1962) Alexander (1989) Anderson et al. (1985) Christiansen (1997)
<i>Mamenchisaurus</i>	18,169.7	14,300	Christiansen (1997)
<i>Omeisaurus</i>	11,796.0	9,800	Christiansen (1997)
<i>Opisthocoelicaudia</i>	10,522.2	22,000	Anderson et al. (1985)
<i>Shunosaurus</i>	4,793.5	3,400	Christiansen (1997)
Stegosauria			
<i>Stegosaurus</i>	2,610.6	1,780 3,100 2,530	Colbert (1962) Alexander (1989) Henderson (1999)
Theropoda			
<i>Albertosaurus</i>	2,465.0	2,500	Paul (1988)
<i>Allosaurus</i>	952.0	1,400 2,090 1,010	Alexander (1989) Colbert (1962) Paul (1988)
<i>Archaeopteryx</i>	0.25	0.26	Paul (1988)
<i>Avimimus</i>	22.2	14	Paul (1988)
<i>Ceratopsaurus</i>	472.6	670 524	Anderson (1985) Paul (1988)
<i>Coelophysis</i>	16.0	15.3	Paul (1988)
<i>Compsognathus</i>	3.5	2.5	Paul (1988)
<i>Deinonychus</i>	104.7	75	Spotila et al. (1991)
<i>Giganotosaurus</i>	6,594.9	6,000+	Coria and Salgado (1995)
<i>Ornitholestes</i>	13.5	12.6	Paul (1988)
<i>Ornithomimus</i>	585.7	440	Paul (1988)
<i>Sinornithoides</i>	1.9	2.5	Russell and Dong (1993)
<i>Tyrannosaurus</i>	6,650.9	7,400 5,700 6,890 4,500 7,224 5,700	Alexander (1989) Paul (1988) Colbert (1962) Anderson (1985) Henderson (1999) Farlow (1990)
Velociraptor	44.3	45	Paul (1988)

estimate and those of other authors (Fig. 4). There are, however, considerable differences in mass estimates reported in the literature for some species. For example, Colbert's (1962) mass estimate of 78,260 kg for *Brachiosaurus* is 30,000 kg heavier than the next closest estimate of Alexander (1989), and even Alexander's (1989) estimate exceeds my own and other esti-

mates by nearly 20,000 kg (Fig. 4). Anderson et al.'s (1985) estimate of *Opisthocoelicaudia* is double that of my own estimate as well as more than double that of mass estimates for sauropods of similar length given in Christiansen (1997). On the other hand, Anderson et al.'s (1985) mass estimate of 5,000 kg for *Diplodocus* is only about one half to one quarter that of

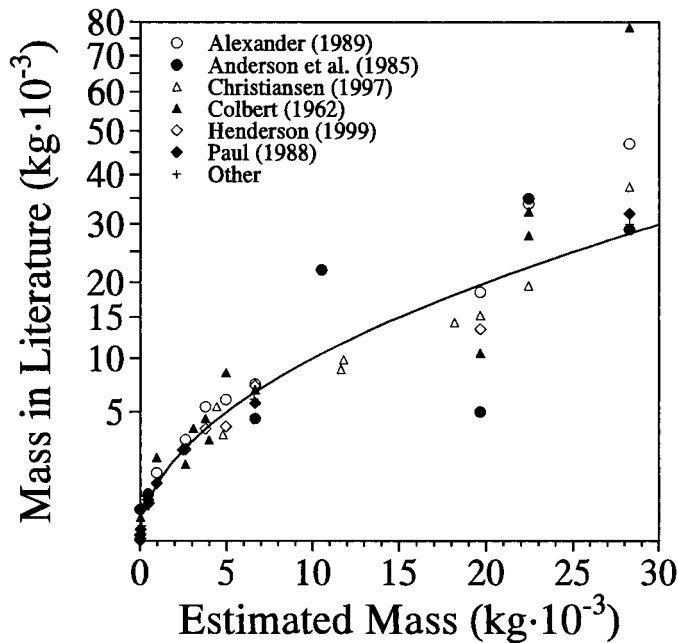


FIGURE 4. Mass estimates reported in the literature (y-axis) plotted against mass calculated by the polynomial method in this study (x-axis). Mass estimates by different authors are plotted separately (see legend), and there were no systematic differences between literature and polynomial mass estimates, although there are some outliers in the literature data (see text for discussion). Note that the y-axis is on a square root scale in order to improve the resolution at lower body mass. The line of equality ($y = x$) is shown (solid line).

other authors', and their mass for *Diplodocus* is less than a quarter of their estimate of *Opisthocoelicaudia* which, however, is less than half the length of *Diplodocus* (Fig. 4). It seems unlikely that the huge differences in the examples above reflect the real size range of the species, and the discrepancies are more likely owing to methodology.

It is inevitable that mass estimates of extinct animals vary, because the representation of a fossil as a living animal, although based on skeletal remains and on knowledge of living animals, is always subject to personal interpretation. Hence, methods of mass estimation which rely on three dimensional models or on graphical representations include the artists' 'error' of reproducing what he or she thinks the animals looked like when it was alive.

Mass estimates from bone measurements are not subject to this error, but Christiansen (1999a) has shown that there are systematic differences in allometric scaling of appendicular bones between groups of extant mammals. Hence, this approach too will have an error attached to it which is difficult to quantify for extinct animals. Given this level of uncertainty, it is encouraging that, except for some outliers, mass estimates by the polynomial method agree fairly well with literature values and that there are no systematic differences, which also supports the validity and utility of the allometric equations for estimating body mass of dinosaurs.

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