Hindawi Publishing Corporation Mathematical Problems in Engineering Volume 2014, Article ID 278945, 7 pages http://dx.doi.org/10.1155/2014/278945



Research Article

Compressed Sensing and Low-Rank Matrix Decomposition in Multisource Images Fusion

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Received 14 March 2014; Accepted 19 June 2014; Published 7 July 2014

Academic Editor: Victoria Vampa

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We propose a novel super-resolution multisource images fusion scheme via compressive sensing and dictionary learning theory. Under the sparsity prior of images patches and the framework of the compressive sensing theory, the multisource images fusion is reduced to a signal recovery problem from the compressive measurements. Then, a set of multiscale dictionaries are learned from several groups of high-resolution sample image's patches via a nonlinear optimization algorithm. Moreover, a new linear weights fusion rule is proposed to obtain the high-resolution image. Some experiments are taken to investigate the performance of our proposed method, and the results prove its superiority to its counterparts.

1. Introduction

Fusion of multisource images that came from different modalities is very useful for obtaining a better understanding of the environmental conditions, for example, the fusion of multifocus images, the infrared (IR) images and visible images, the medical CT images and MRI images, and the multispectrum images and panchromatic images. Nowadays multiresolution based fusion approaches have been one of the popular techniques that is investigated by many researches and proves to present state-of-the-art result [1-4], including pyramid-based methods and discrete wavelet transform-(DWT-) based methods. In recent years, a new developed compressive sensing (CS) [5–8] theory is introduced into image fusion. It is well known that the compressive sensing theory provides a possible way of recovering sparse signals from their projection onto a small number of random vectors, so compressive sensing indicated a possible way of recovering high-resolution signals from their low-resolution version.

Assume that a signal $\mathbf{x} \in \mathbf{R}^N$ is compressible under a dictionary $\mathbf{\Psi} \in \mathbf{R}^{N \times N}$: $\mathbf{x} = \mathbf{\Psi} \boldsymbol{\theta}$, where $\|\boldsymbol{\theta}\|_0 = K$ is the number of nonzero components of $\boldsymbol{\theta}$. The main idea of CS is to recover the original signal \mathbf{x} from its compressive measurements $\mathbf{y} = \mathbf{\Phi} \mathbf{x} \in \mathbf{R}^M$, where $\mathbf{N} \gg \mathbf{M}$. Under the condition that the matrix $\mathbf{\Phi} \mathbf{\Psi}$ satisfies the restricted isometry

property (RIP), the signal \mathbf{x} can be accurately recovered from only $M \geq K$ measurements [5], by solving such an optimization problem,

$$\min_{\theta} \quad \|\boldsymbol{\theta}\|_{0}$$
s.t. $\mathbf{v} = \mathbf{\Phi}\mathbf{x} = \mathbf{\Phi}\mathbf{\Psi}\boldsymbol{\theta}$. (1)

Therefore, there are many advantages of combining the CS technique and image fusion application [9–14].

Nowadays the applications of compressive sensing technology into image processing can be classified into three categories: compressive sensing based imaging [15–21], compressive sensing based image processing [22–26], and "compressive sensing" form applications [27–29]. Imaging is one of the most successful applications of compressive sensing theory, where a few sensors or low-resolution sensors are employed to achieve high-resolution imaging, such as optical imaging [16, 17], medical imaging [18, 19], and hyperspectral imaging [20, 21]. Compressive sensing is also used to transform images to other spaces to obtain more efficient analysis, such as the texture classification [22] and superresolution image construction [23]. Numerous works are of the "compressive sensing" form applications; that is, if the task can be reduced to the optimization problem shown in

(1), these works are also called compressive sensing based applications.

In image fusion, most of the available compressive sensing based fusion schemes are of "compressive sensing" form [9-14, 27, 28]; that is, they did not consider the simultaneous fusion and super-resolution of multisource images. In this paper, we indicate another solution for simultaneous fusion and super-resolution of multisource images via the recent developed compressive sampling theory. Under the sparsity prior of images patches and the framework of the compressive sensing theory, the multisource images fusion is reduced to a signal recovery problem from the compressive measurements. A set of multiscale dictionaries are learned from some groups of high-resolution sample image's patches via a nonlinear optimization algorithm. Moreover, a new linear weights fusion rule is proposed. Some experiments are taken to investigate the performance of our proposed method, and the results prove its superiority to its counterparts.

The rest of this paper is organized as follows. Our proposed simultaneous fusion and super-resolution scheme of multisource images is expounded in Section 2. In Section 3, some experiments are made to compare the proposed method with other related segmentation approaches. The conclusions are finally summarized in Section 4.

2. Simultaneous Fusion and Super-Resolution **Scheme of Multisource Images**

In this section, the foundations of our proposed method are illustrated, including the super-resolution multisource images fusion, the super-resolution multisource images fusion via compressive sensing, and the dictionary learning algorithm used in our approach.

2.1. Super-Resolution Multisource Images Fusion. Assume that the multisource images $\{Y_i^{low}, i = 1, 2, ... S\}$ to be fused are low-resolution images; that is, the *i*th source images $\mathbf{Y}_{i}^{\text{low}}$ are a low-resolution version of X_i^{high} :

$$\mathbf{Y}_{i}^{\text{low}} = \mathbf{M}\mathbf{X}_{i}^{\text{high}} + \mathbf{v}_{i} \quad (i = 1, \dots, S),$$
 (2)

where S is the number of source images, M is the downresolution operator, and \mathbf{v}_i is the measurement noise of the ith source image. We aim to recover a high-resolution image \mathbf{X}^{high} from the multisource low-resolution images $\{\mathbf{Y}_{i}^{\text{low}}, i =$

The patches based fusion is adopted in our method; that is, X^{high} is processed in raster-scan order, from left to right and top to bottom, and then sequentially recovered. Let $\mathbf{x}_{j}^{\text{high}} \in \Re^{n}$ denote the jth $\sqrt{n} \times \sqrt{n}$ local patch vector extracted from a high-resolution fusion image $\boldsymbol{X}^{\text{high}}$ at the spatial location j: $\mathbf{x}_{j}^{\text{high}} = \mathbf{R}_{j} \mathbf{X}^{\text{high}}$, where \mathbf{R}_{j} denotes a rectangular windowing operator and the overlapping is allowed. Given a set of $p \times p$ ($p \in Z^+$) LR patches taken from

$$\mathbf{Y}_{i}^{\text{low}}: \{\mathbf{y}_{i,1}^{\text{low}}, \mathbf{y}_{i,2}^{\text{low}}, \dots, \mathbf{y}_{i,Q}^{\text{low}}\} \in \mathbf{\Re}^{m} \ (m=p^{2}), \ (i=1,\dots,S; \ j=1,\dots,Q), \ \text{we have}$$

$$\mathbf{y}_{i,1}^{\text{low}} = \mathbf{H} \mathbf{x}_{i,1}^{\text{high}} + \mathbf{n}_{i,1}$$

$$\mathbf{y}_{i,2}^{\text{low}} = \mathbf{H} \mathbf{x}_{i,2}^{\text{high}} + \mathbf{n}_{i,2}$$

$$\vdots$$

$$\mathbf{y}_{i,Q}^{\text{low}} = \mathbf{H} \mathbf{x}_{i,Q}^{\text{high}} + \mathbf{n}_{i,Q}.$$
(3)

A simple example of the matrix $\mathbf{H} \in \Re^{4 \times 16}$ is as follows:

Our aim is to reconstruct the fusion image X^{high} from the high-resolution patches $\mathbf{x}_{i}^{\text{high}}$ (i = 1,...,S) from a set of the corresponding $q \times q$ ($q \in Z^+$) HR patches $\mathbf{x}_{i,i}^{\text{high}}$ (i = $1, \ldots, S; j = 1, \ldots, Q \in \Re^n (n = q^2)$. This is a simultaneous fusion and super-resolution problem of multisource images.

2.2. Super-Resolution Multisource Images Fusion via Compressive Sensing. According to the recent developed compressive sampling theory [5, 6], it is capable of recovering $\mathbf{x}_{i,j}^{\hat{\mathbf{h}}\text{igh}}$ (i = $1, \ldots, S; j = 1, \ldots, Q$) from $\mathbf{y}_{i,j}^{\text{low}}$ under the sparsity prior of $\mathbf{x}_{i,j}^{\text{high}}$; that is, $\mathbf{x}_{i,j}^{\text{high}}$ can be represented as a sparse linear combination by an overcomplete dictionary $\mathbf{D}_{i}^{\text{high}} \in \Re^{n \times K}$ that is not coherent with the measurement (or sampling) matrix **H**; that is,

$$\mathbf{x}_{i,j}^{\text{high}} = \mathbf{D}_{i}^{\text{high}} \boldsymbol{\alpha}_{i,j}. \tag{5}$$

Here the "sparsity" of the decomposition coefficient $\alpha_{i,j} \in$ \Re^K means $\|\alpha_{i,j}\|_0 = S \ll n < K$, and K is the number of elements (or atoms) in the dictionary $\mathbf{D}_i^{\text{high}}$. Under this sparsity assumption, $\mathbf{x}_{i,j}^{\text{high}}$ can thus be reconstructed by taking only $m \ge O(S \log n)$ measurements. As soon as the sparse coefficient $\alpha_{i,j}$ is determined by

$$\min_{\boldsymbol{\alpha}_{i,j}} \|\boldsymbol{\alpha}_{i,j}\|_{0}$$
s.t.
$$\mathbf{y}_{i,j}^{\text{low}} = \mathbf{H}\mathbf{x}_{i,j}^{\text{high}} = \mathbf{H}\mathbf{D}_{i}^{\text{high}}\boldsymbol{\alpha}_{i,j},$$
(6)

estimation of $\mathbf{x}_{i,j}^{\text{high}}$ can be obtained using (5). In our method, a linear fusion rule is performed on the $\{\mathbf{Y}_i^{\text{low}}, \mathbf{Y}_2^{\text{low}}, \dots, \mathbf{Y}_S^{\text{low}}\}$ with each $\mathbf{Y}_i^{\text{low}} = \{\mathbf{y}_{i,1}^{\text{low}}, \mathbf{y}_{i,2}^{\text{low}}, \dots, \mathbf{y}_{i,Q}^{\text{low}}\}$. Considering the patch by patch processing pattern, we write the low-resolution fusion patch as

$$\mathbf{y}_{j}^{\text{low}} = \sum_{i=1}^{S} w_{i,j} \mathbf{y}_{i,j}^{\text{low}}.$$
 (7)

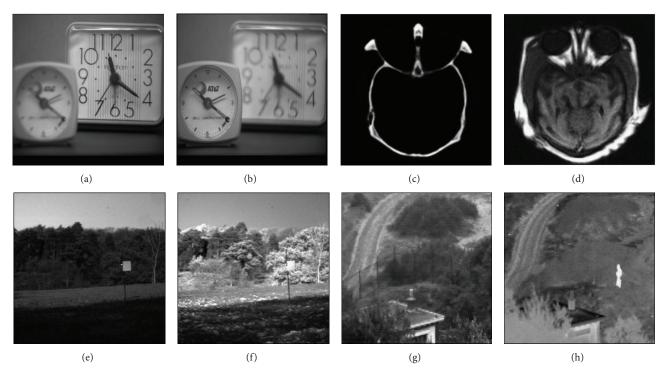


FIGURE 1: Multisource images.



FIGURE 2: Fusion results of Figures 1(a) and 1(b).

Therefore, its high-resolution version can be written as

$$\mathbf{x}_{j}^{\text{high}} = \sum_{i=1}^{S} w_{i,j} \mathbf{x}_{i,j}^{\text{high}}.$$
 (8)

In our proposed method, we determine the weights according to the following formula:

$$w_{i,j} = \frac{1}{S-1} \times \left(\frac{\sum_{k=1,k\neq i}^{S} \left\| \mathbf{y}_{i,j}^{\text{low}} - \mathbf{H} \mathbf{D}_{i}^{\text{high}} \boldsymbol{\alpha}_{i,j} \right\|_{2}^{2}}{\sum_{k=1}^{S} \left\| \mathbf{y}_{k,j}^{\text{low}} - \mathbf{H} \mathbf{D}_{k,j}^{\text{high}} \boldsymbol{\alpha}_{k,j} \right\|_{2}^{2}} \right)$$

$$= \frac{1}{S-1} \times \left(1 - \frac{\left\| \mathbf{y}_{i,j}^{\text{low}} - \mathbf{H} \mathbf{D}_{i}^{\text{high}} \boldsymbol{\alpha}_{i,j} \right\|_{2}^{2}}{\sum_{k=1}^{S} \left\| \mathbf{y}_{k,j}^{\text{low}} - \mathbf{H} \mathbf{D}_{k,j}^{\text{high}} \boldsymbol{\alpha}_{k,j} \right\|_{2}^{2}} \right).$$
(9)

Because patches $\{\mathbf{x}_j^{\text{high}}\}$ are highly redundant and the recovery of \mathbf{X} from $\{\mathbf{x}_j^{\text{high}}\}$ becomes an overdetermined system, it is

straightforward to obtain the following least-square solution in the patch aggregation:

$$\mathbf{X} = \left(\sum_{j} \mathbf{R}_{j}^{T} \mathbf{R}_{j}\right)^{-1} \left(\sum_{j} \mathbf{R}_{j}^{T} \mathbf{x}_{j}^{\text{high}}\right). \tag{10}$$

2.3. Dictionary Learning Algorithm. The compressibility of patches shown in (5) is the sparsity prior used in our method. In order to generate several overcomplete dictionaries $\mathbf{D}_i^{\text{high}}$ ($i=1,2,\ldots,S$) that can represent well the underlying HR patches, we propose an algorithm to adaptively tune the dictionary from a set of High-Resolution multisource sample image's patches. In this section, we will reduce the learning of dictionary $\mathbf{D}_i^{\text{high}}$ ($i=1,2,\ldots,S$) as another sparsity-oriented optimization problem. Recent research on image statistics suggests that image patches can be well represented as a sparse linear combination of elements from an appropriately

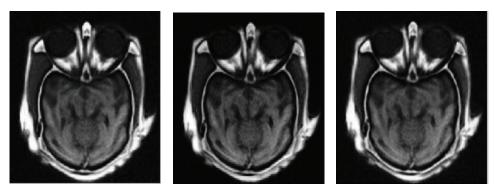


FIGURE 3: Fusion results of Figures 1(c) and 1(d).



FIGURE 4: Fusion results of Figures 1(e) and 1(f).



FIGURE 5: Fusion results of Figures 1(g) and 1(h).

chosen overcomplete dictionary. Under this assumption, the HR image patches set $\mathbf{Q}_i^{\text{high}} = \{\mathbf{q}_i^1, \mathbf{q}_i^2, \dots \mathbf{q}_i^Q \mid \mathbf{q}_i^j \in \Re^n, j = 1, \dots, Q\}$ $(i = 1, \dots, S)$ sampled from some training HR images can be represented as a sparse linear combination in a dictionary $\mathbf{D}_i^{\text{high}} = [\mathbf{d}_i^1, \dots, \mathbf{d}_i^K] \in \Re^{n \times K}$ $(i = 1, 2, \dots, S)$ $(\|\mathbf{d}_i^j\|_2 = 1, j = 1, \dots, K)$; that is,

$$\mathbf{q}_{i}^{j} = \mathbf{D}_{i}^{\text{high}} \boldsymbol{\beta}_{i}^{j}, \tag{11}$$

with the sparse coefficient vectors $\boldsymbol{\beta}_i^j \in \mathfrak{R}^K$ and $\|\boldsymbol{\beta}_i^j\|_0 \ll K$. The objective of designing $\mathbf{D}_i^{\text{high}}$ is to make the reconstruction

error over $\mathbf{Q}_i^{\text{high}}$ ($i=1,\ldots,S$) be minimal under the sparsity assumption; that is,

$$\min_{\boldsymbol{\beta}_{i}^{j}, \mathbf{D}_{i}^{\text{high}}} \quad \|\boldsymbol{\beta}_{i}^{j}\|_{0}
\text{s.t.} \quad \mathbf{q}_{i}^{j} = \mathbf{D}_{i}^{\text{high}} \boldsymbol{\beta}_{i}^{j}.$$
(12)

We reformulate (12) as follows:

$$\begin{aligned} & \min_{\mathbf{B}_{i}, \mathbf{D}_{i}^{\text{high}}} & \left\| \mathbf{B}_{i} \right\|_{0,1} \\ & \text{s.t.} & \mathbf{Q}_{i}^{\text{high}} = \mathbf{D}_{i}^{\text{high}} \mathbf{B}_{i}, \end{aligned} \tag{13}$$

where $\mathbf{B}_i = [\boldsymbol{\beta}_i^1, \boldsymbol{\beta}_i^2, \dots, \boldsymbol{\beta}_i^Q]$ is the coefficients matrix. In order to solve it, the KSVD dictionary learning algorithm is used

Images	Measures	Our method	Method 1 [17]	Method 2 [18]
	E	7.3026	7.2996	7.3012
	MI	6.7899	6.7741	6.7560
	AG	2.9150	2.8183	2.8250
Figures 1(a) and 1(b)	SD	10.6438	10.6607	10.6643
	J	0.3438	0.3428	0.3432
	UIQI	0.9832	0.9901	0.9943
	CC	0.9881	0.9884	0.9882
Figures 1(c) and 1(d)	E	6.1440	6.4647	6.5612
	MI	5.0346	3.6546	3.9025
	AG	7.3064	6.1164	7.1345
	SD	8.7785	8.7267	8.9131
	J	6.0068	0.5881	6.9546
	UIQI	0.5446	0.5328	0.5421
	CC	0.6547	0.6459	0.6425
Figures 1(e) and 1(f)	E	7.6970	7.5243	7.6133
	MI	7.3204	5.7659	4.3234
	AG	10.1423	7.4218	9.3781
	SD	11.3244	10.6344	11.2825
	J	0.6622	0.6729	0.7545
	UIQI	0.7144	0.7204	0.7131
	CC	0.8395	0.8782	0.8179
Figures 1(g) and 1(h)	E	6.6827	6.2301	7.0025
	MI	2.1098	1.4961	1.5836
	AG	5.3866	3.5715	6.6887
	SD	8.5479	7.8916	8.7738
	J	0.5097	0.8127	0.2107
	UIQI	0.9116	0.9244	0.9079
	CC	0.5242	0.6333	0.4697

TABLE 1: The fusion result of different methods.

to train the dictionaries $\mathbf{D}_i^{\text{high}}$ $(i=1,\ldots,S)$ from $\mathbf{Q}_i^{\text{high}}$ $(i=1,\ldots,S)$ [30, 31].

3. Experiment Results

For evaluating the performance of the proposed fusion algorithm, in this section we have implemented them on some multisource images, including the multifocus images, infrared (IR) images, and visual images, as shown in Figure 1. The size of all images used in the test is 256 lines \times 256 columns and we aim to recover the 512 lines \times 512 columns images. We compare our method with the following two related methods.

Method (1). Consider the multimodal image fusion with joint sparsity model [32].

Method (2). Consider the image features extraction and fusion based on joint sparse representation [33].

For evaluating the performance of the proposed algorithm, the computed results are compared by visual quality subjectively and by some guidelines in fusion. The simulations are conducted in MATLAB R2009 on PC with Intel Core 2/1.8 G/1 G.

The fusion results of three methods are shown in Figures 2, 3, 4, and 5, and from left to right are Method 1, our method, and Method 2. From them we can see that the fusion images of our method can get higher-resolution images at the same time of fusing the multisource images. Compared with the rules in [32, 33], our proposed method has better preservation of directional information. The numerical guidelines are shown in Table 1, where some measures including the entropy (*E*), mutual information (MI), average gradient (AG), standard deviation (SD), cross entropy (*J*), universal image quality index (UIQI) [34], and correlation coefficient (CC) are calculated from the fusion images derived by different methods.

Here UIQI is used to estimate the subjective vision effect, which combined the spatial correlation, wrap of mean, and variance together, and it can embody the comparability between the fused image and original images. It is defined as

$$Q = \frac{\sigma_{AB}}{\sigma_A \sigma_B} \bullet \frac{2\mu_A \mu_B}{\mu_A^2 + \mu_B^2} \bullet \frac{2\sigma_A \sigma_B}{\sigma_A^2 + \sigma_B^2},\tag{14}$$

where σ_{AB} is the covariance of the fused source images A and B and σ_x and μ_x are the standard variance and the mean of the

image *x*, respectively. From it we can see that the numerical result accords with the subjective result.

4. Conclusions

In this paper we propose a novel super-resolution multisource images fusion scheme based on compressive sensing and dictionary learning. Under the sparsity prior of images patches and the framework of the compressive sensing theory, the multisource images fusion is reduced to a signal recovery problem from the compressive measurements. A new linear weights fusion rule is proposed. A set of multiscale dictionaries are learned from several groups of high-resolution (HR) sample image's patches, and a higher resolution fusion image can be obtained from multisource images. Some experiments are taken and the results prove its superiority to its counterparts.

Conflict of Interests

The authors declare that there is no conflict of interests regarding the publication of this paper.

Acknowledgment

This project is supported by the Natural Science Foundation of Jiangsu Province of China, under Grant no. BK20130769.

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