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Catalytic activities of noble metal atoms on WO₃ (001): nitric oxide adsorption

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Abstract

Using first-principles density functional theory calculations within the generalized gradient approximation, we investigate the adsorption of NO molecule on a clean WO₃(001) surface as well as on the noble metal atom (Cu, Ag, and Au)-deposited WO₃(001) surfaces. We find that on a clean WO₃ (001) surface, the NO molecule binds to the W atom with an adsorption energy (E_{ads}) of -0.48 eV. On the Cu- and Ag-deposited WO₃(001) surface where such noble metal atoms prefer to adsorb on the hollow site, the NO molecule also binds to the W atom with $E_{ads} = -1.69$ and -1.41 eV, respectively. This relatively stronger bonding of NO to the W atom is found to be associated with the larger charge transfer of 0.43 *e* (Cu) and 0.33 *e* (Ag) from the surface to adsorbed NO. However, unlike the cases of Cu-WO₃(001) and Ag-WO₃(001), Au atoms prefer to adsorb on the top of W atom. On such an Au-WO₃ (001) complex, the NO molecule is found to form a bond to the Au atom with $E_{ads} = -1.32$ eV. Because of a large electronegativity of Au atom, the adsorbed NO molecule captures the less electrons (0.04 *e*) from the surface compared to the Cu and Ag catalysts. Our findings not only provide useful information about the NO adsorption on a clean WO₃(001) surface as well as on the noble metal atoms deposited WO₃(001) surfaces but also shed light on a higher sensitive WO₃ sensor for NO detection employing noble metal catalysts.

Keywords: Surface; Catalytic; Charge transfer; Bond length

Background

NO*x* gases such as NO and NO₂ which are produced from the reaction of nitrogen and oxygen gases in the air during combustion damage not only our environment including air pollution and land contamination but also human health. Therefore, it has attracted much attention in recent years to develop a high-performance NO*x*-sensing equipment [1-4]. For the detection of NO*x*, a number of gas sensors using semiconducting metal oxides such as ZnO [5-7], MoO₃ [8,9], In₂O₃ [10], SnO₂ [11,12], TiO₂ [13], and WO₃ [14] have been reported theoretically and experimentally.

Tungsten oxide (WO₃) has many unusual properties which make it suitable for various applications, e.g., high sensitivity of reducing and oxidizing gases [14], excellent electron transport and photosensitivity, and high stability-

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resisting photocorrosion in aqueous solvent [15-20]. Especially, WO₃ sensors have been widely applied for the detection of NOx gases [21-23]. In order to enhance the performance for NO₂ detection, WO₃ sensors have utilized the addition of metal atoms [24,25] as catalysts. However, there have been relatively few reports for the WO₃ sensor detecting NO molecule [26,27], and furthermore, theoretical studies for the adsorption of NO on WO₃ surfaces are still lacking. In this sense, an accurate first-principles density functional theory (DFT) calculation for the NO adsorption on WO₃ surfaces is highly desirable for the application of WO₃ sensors to NO detection.

In this work, we perform a first-principles DFT calculation to investigate the adsorption of NO molecule on a clean WO₃(001) surface as well as on the noble metal atom (Cu, Ag, and Au) deposited WO₃(001) surface. Here, the (001) surface (see Figure 1a,b) of γ -monoclinic WO₃ is taken into account because it is the most stable at room temperature [28]. We demonstrate that the Cu-, Ag-, and Au-deposited WO₃(001) surfaces exhibit different catalytic behaviors for NO adsorption, that is, the magnitude of adsorption energy (E_{ads}) is in the order of



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Cu > Ag > Au. This different binding behavior of NO on $WO_3(001)$ depending on the noble metal species can be traced to the difference in charge transfer from the substrate to adsorbed NO molecule. Based on our DFT results, we will discuss the enhanced sensitivity of WO_3 sensors for NO detection by employing the noble metal catalysts.

Methods

Our DFT calculations were performed using Vienna ab initio simulation package (VASP) with the projector augmented wave method [29-32]. For the exchangecorrelation energy, we employed the generalized gradient approximation functional of Perdew-Burke-Ernzerhof [33]. The electronic wave functions were expanded in a plane wave basis with an energy cutoff of 400 eV. The WO₃(001) surface was modeled by a periodic fouratomic-layer slab composing two alternate WO₂ plus O layers with approximately 16 Å of vacuum in between the slabs. The k-space integration was carried out using a Monhkorst-Pack grid [34] of $4 \times 4 \times 1 k$ points in the surface Brillouin zone of the monoclinic (1×1) unit cell whose size is as large as the cubic (2×2) unit cell. We relaxed all atoms except the bottom layer along the calculated forces until all the residual force components were less than 0.01 eV/Å. For the interaction of the NO molecule with the clean and metal-deposited WO₃(001) surfaces, we initially placed the NO molecule about 3.5 Å away from the surfaces and obtained the adsorption structure by fully structural optimization.

Results and discussion

NO adsorption on a clean WO₃ (001) surface

We first investigate the adsorption of a single NO molecule on a clean WO₃ (001) surface. Figure 1a,b shows the top and side views of the optimized WO₃ (001) surface, respectively. For the adsorption of NO on WO_3 (001), we consider the three different adsorption sites such as top W (hereafter denoted as S_1), top O (S_2), and hollow (S_3) sites. We find that the N atom of NO is bonding to the substrate atoms, consistent with a previous theoretical calculation [21]. However, in the hollow site, the O atom of NO can be bound to the substrate atoms (denoted as S_4). We calculate the adsorption energy defined as [35] $E_{ads} = E(NO/surf) - E(surf) - E(NO)$, where E(NO/surf) is the total energy of the NO-adsorbed WO₃ (001) system, E(surf) is the energy of a clean WO₃ (001) before NO adsorption, and E(NO) is the energy of a free NO molecule, obtained using a $12 \times 12 \times 12$ Å³ supercell calculation. As shown in Figure 1f, the S_1 configuration is

found to be the most stable with $E_{ads} = -0.48$ eV, larger in magnitude than $E_{ads} = -0.05$, -0.05, and -0.03 eV for S₂, S₃, and S₄, respectively; see Figure 2a. We note that, in the S₁ configuration, the bond length d_{N-W} between the N and W atoms is calculated to be 2.07 Å, which is much shorter than the sum (3.7 Å) of van der Waals radius of the two atoms [14,36]. Thus, we can say that NO molecule can form a chemical bond with the WO₃ (001) surface.

To evaluate charge transfer in the S_1 configuration, we perform Bader charge analysis for NO before and after its adsorption on the WO₃(001) surface [37,38]. The results for a free NO molecule and adsorbed NO on various substrates are given in Table 1. We find that, upon NO adsorption on a clean WO₃(001) surface, the electrons in the N (O) atom increase (decrease) from 4.44 (6.56) to 4.84 (6.35) e, giving rise to an increase of 0.19 e in adsorbed NO molecule. This fact shows that adsorbed NO molecule captures electrons from the WO₃(001) surface, indicating that NO behaves as a charge accepter. Indeed, the charge density difference, defined as $\Delta \rho = \rho_{\text{NO/WO3}} - (\rho_{\text{NO}} + \rho_{\text{WO3}})$, clearly shows a charge transfer from the O (in NO molecule) and W atoms to the N atom; see Figure 3a. As a consequence of the additional electrons in NO in the $NO/WO_3(001)$ system, the bond length $d_{\text{N-O}}$ of NO molecule slightly increases to 1.181 Å, compared to that (1.170 Å) of a free NO molecule; see Table 1.

It is noteworthy that the abovementioned charge transfer from the $WO_3(001)$ surface to NO molecule leads to a reduction of conduction electrons in WO_3

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	NO	NO/WO ₃	NO/Cu-WO ₃	NO/Ag-WO ₃	NO/Au-WO ₃
N (e)	4.44	4.84	5.00	4.91	4.64
O (e)	6.56	6.35	6.43	6.42	6.40
N + O (e)	11	11.19	11.43	11.33	11.04
d _{N-O} (Å)	1.170	1.181	1.212	1.203	1.182

Table 1 Charge analysis and bond length of NO molecule

Bader charges of N and O atoms in a clean WO₃(001) surface and various noble metal atom-deposited WO₃(001) surfaces are given. Bader charges of N and O atoms in an isolated NO molecule are also given in the first column. The bond length $d_{\text{N-O}}$ in each system is also given.

(001), thereby forming the electron-depleted layer at the surface. This change of electrical character at the WO_3 (001) surface can be utilized to the WO_3 gas sensor where the contact resistance can be affected by the exposure of NO gas.

NO adsorption on Cu- or Ag-deposited WO₃ (001) surface We begin to optimize the adsorption structure of Cu or Ag on WO₃(001). We find that the adsorption of Cu (Ag) on the hollow site is more stable than the other adsorption sites such as top W and top O sites by 0.66 (0.14) and 0.75 (0.14) eV, respectively. Using Bader charge analysis, we find that the adsorption of Cu and Ag on the hollow site loses electrons to the WO₃(001) substrate by 0.7 and 0.6 *e*, respectively. Using the most stable adsorption configuration of Cu or Ag on WO₃(001), we continue to study the adsorption of NO on such noble metal atomdeposited WO₃(001) substrates. We consider three different adsorption configurations of NO, where N atom is





attached to W (denoted as M_1), O (M_2), and Cu or Ag (M_3) atoms. In addition, we also consider another adsorption configuration of NO, where O atom in NO molecule is attached to Cu or Ag atom (denoted as M₄). The calculated adsorption energy of NO for each adsorption configuration on Cu-WO₃(001) and Ag-WO₃ (001) is given in Figure 2b,c, respectively. We find that the M_1 configuration is the most stable with $E_{ads} = -1.69$ and -1.41 eV for NO/Cu-WO₃(001) and NO/Ag-WO₃ (001), respectively, which are much larger in magnitude than $E_{ads} = -0.48$ eV of the S₁ configuration at a clean WO3(001) surface. This indicates that Cu and Ag increases the strength of NO binding on $WO_3(001)$, thereby serving as catalysts. In the M1 configuration, the N atom is also bonding to the W atom with $d_{\text{N-Cu/Ag}}$ (bond length between N and Cu or Ag atoms) = 1.86 or 2.19 Å because of a Coulomb interaction between the negatively charged N atom and the positively charged Cu or Ag atom (see Figure 3b,c), as discussed below. We note that the values of d_{N-W} amount to 2.36 and 2.37 Å for NO/Cu-WO₃(001) and NO/Ag-WO₃(001), respectively. These values become longer than $d_{N-W} = 2.07$ Å in the S₁ configuration but are still much shorter than the sum (3.7 Å) of van der Waals radius of N and W atoms [14,36], therefore concluding that NO molecule adsorbs chemically on the Cu-WO₃ (001) and Ag-WO₃(001) substrates.

In Table 1, we find that for the M_1 configuration of NO/Cu-WO₃(001), the electrons in the N (O) atom increase (decrease) from 4.44 (6.56) to 5.00 (6.43) *e*, giving rise to an increase of 0.43 *e* in adsorbed NO molecule. On the other hand, for the M_1 configuration of NO/Ag-WO₃(001), the electrons in the N (O) atom are found to increase (decrease) from 4.44 (6.56) to 4.91 (6.42) *e*, giving rise to an increase of 0.33 *e* in adsorbed NO molecule. These results indicate that adsorbed NO molecule on Cu-WO₃(001) and Ag-WO₃(001) captures more electrons from the substrates compared to the case of NO adsorption at a clean WO₃(001) to NO. As

shown in Figure 3b,c, the calculated charge density difference $\Delta \rho$ shows charge transfer from the O (in NO molecule) and Cu-WO3(001) or Ag-WO3(001) substrate to the N atom, leading to the polar NO molecule with a negatively charged N atom. We note that, as a consequence of the presence of excess electrons in the polar NO molecule, the bond length $d_{\text{N-O}}$ of NO molecule increases to 1.212 and 1.203 Å for NO/Cu-WO₃(001) and NO/Ag-WO₃(001), respectively. These values of $d_{\text{N-O}}$ are longer than $d_{\text{N-O}} = 1.181$ Å for NO/WO₃(001) as well as $d_{\text{N-O}} = 1.170$ Å of a free NO molecule.

Since more electrons transfer from the substrate to adsorbed NO molecule by the deposition of Cu or Ag atoms, one expects an enhanced reduction of conduction electrons in WO₃(001), therefore increasing the sensitivity of WO₃ sensor for NO detection. As a matter of fact, a recent experimental study showed that the deposition of Ag atoms in WO₃ sensor improves its sensitivity for NO detection [27]. We note that, even though NO adsorption induces more electron transfer from the Cu-WO₃(001) substrate compared to Ag-WO₃(001), Cu atoms would be easily oxidized at a usual operation temperature (above 150°C) of WO₃ sensor. This oxidizing effect in noble metal atoms should be cautioned for the gas-sensing performance of WO₃ sensor.

NO adsorption on Au-deposited WO₃ (001) surface

We first optimize the adsorption structure of Au on $WO_3(001)$. Unlike the cases of Cu and Au catalysts, Au atom adsorbs only on top of the W atom, as shown in Figure 1e. Here, the adsorption of Au captures electrons from the $WO_3(001)$ substrate by 0.34 *e* because of a high electronegativity of Au atom. For the adsorption of NO on Au- $WO_3(001)$, we consider several adsorption configurations of NO, where N atom is attached to Au (denoted as P₁), top W (P₂), top O (P₃), and hollow (P₄) sites. In addition, we also consider another adsorption configuration of NO, where O atom in NO molecule is attached to Au atom (P₅). The calculated adsorption energy of

NO for each adsorption configuration on Au-WO₃(001) is displayed in Figure 2d. We find that the P₁ configuration is the most stable with $E_{ads} = -1.32$ eV, which is relatively smaller in magnitude than $E_{ads} = -1.69$ and -1.41 eV for the M₁ configurations of NO/Cu-WO₃(001) and NO/ Ag-WO₃(001), respectively. In the P₁ configuration, the calculated bond length of adsorbed NO is $d_{N-O} = 1.182$ Å (see Table 1), which is shorter than 1.212 and 1.203 Å for NO/Cu-WO₃(001) and NO/Ag-WO₃(001), respectively. This shortest value of d_{N-O} is due to the fact that NO captures the least electrons (0.04 *e*) from Au-WO₃(001), as shown in Table 1. These features of NO/Au-WO₃(001) such as the smaller adsorption energy, the shorter bond length, and the less electron capture of adsorbed NO is traced to a large electronegativity of Au.

Conclusions

We have performed first-principles DFT calculations within the generalized gradient approximation for the adsorption of NO molecule on a clean WO₃(001) surface as well as on the Cu-deposited, Ag-deposited, and Au-deposited WO₃ (001) surfaces. We found that the NO molecule prefers to adsorb on the top of W atom at a clean WO₃(001) surface, where a charge transfer from WO₃(001) to NO occurs by 0.19 e and E_{ads} is calculated to be -0.48 eV. We also found that, on the Cu- and Ag-deposited WO₃(001) surface, the NO molecule also binds to the W atom with $E_{ads} = -1.69$ and -1.41 eV, respectively, accompanying the relatively larger charge transfer of 0.43 e (Cu) and 0.33 e (Ag) to adsorbed NO compared to the clean WO₃(001) surface. On the other hand, Au atoms on WO₃(001) prefer to adsorb on the top of W atom, and the NO molecule forms a bond to the Au atom with a small electron transfer of 0.04 e to adsorbed NO. We obtained a relatively smaller adsorption energy of $E_{ads} = -1.32$ eV for the NO/Au-WO₃ (001) system compared to NO/Cu-WO₃(001) and NO/Ag- $WO_3(001)$ because of a large electronegativity of Au atom. The present results demonstrated that the sensitivity of WO₃ sensors for NO detection can be improved by employing the noble metal catalysts such as Cu and Ag atoms.

Competing interests

The authors declare that they have no competing interests.

Authors' contributions

XYR, YJ, and JHC conceived the central ideas and drafted the manuscript. XYR carried out the calculations. SZ, CL, and SFL participated in the design of the study and discussed the result. All authors read and approved the final manuscript.

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