

# Comparison of Measured and FAO-56 Modeled Evaporation from Bare Soil

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**Abstract:** This paper evaluates how well the FAO-56 style soil water evaporation model simulates measurements of evaporation ( $E$ ) from bare soil. Seven data sets were identified from the literature and in all but one case, the individuals who took the measurements were contacted and they provided the writers with specific weather and soils data for model input. Missing weather and soils data were obtained from online sources or from the National Climatic Data Center. Simulations for three possible variations of soil data were completed and compared. The measured and the FAO-56 simulated  $E/ET_o$  and cumulative evaporation trends and values were similar. Specifically, the average evaporation weighted percent difference between the measured and the simulated cumulative evaporation was between  $-7.5$  and  $-0.5\%$ . This evaluation suggests model accuracy of about  $\pm 15\%$  with the use of sound weather data and a fairly generalized understanding of soil properties in the location being evaluated.

**CE Database subject headings:** Evapotranspiration; Evaporation; Lysimeters; Irrigation scheduling; Soil water; Transpiration; Measurement.

## Introduction

In California and many other states, data from a network of agricultural weather stations is accessible via the World Wide Web to provide estimates of local reference evapotranspiration which, when coupled with crop coefficient ( $K_c$ ) values, can be used for irrigation scheduling and water management. The California Irrigation Management Information System (CIMIS) weather stations identify the water use of a 10–15 cm tall unstressed irrigated grass for the reference evapotranspiration ( $ET_o$ ) (Eching and Moellenberndt 1998).  $ET_o$  is estimated using solar radiation, air temperature, vapor pressure, and wind speed measurements as inputs into a version of the Penman equation modified by Pruitt and Doorenbos (1977). Multiplying the local  $K_c$  value for the crop of interest by the local daily  $ET_o$  value provides an estimate of daily crop evapotranspiration ( $ET_c$ ).

FAO-56 (Allen et al. 1998) offers a method for dividing  $ET_c$  into evaporation ( $E$ ) and transpiration ( $T$ ) components. This is done by splitting  $K_c$  into two terms, the basal crop coefficient ( $K_{cb}$ ) and the soil evaporation coefficient ( $K_e$ ), where  $K_c = K_{cb} + K_e$ . This dual  $K_c$  approach was used for cumulative evaporation predictions in a CALFED/ARI Evaporation Study by Cal Poly Irrigation Training and Research Center (ITRC) (Burt et al. 2002) that estimated the amount of evaporation from California agricultural lands under three rainfall scenarios.

Allen et al. (2000) compared the predicted evaporation using these two ET partitioning methods with Kimberly, Id. data sets. The results indicate that the FAO-56 estimated cumulative soil evaporation for the growing season was about two times greater than that calculated with the Wright (1982) method that uses a time-based decay function. Since these data were collected on large precision weighing lysimeters that measured  $E$  and  $T$  collectively, there was no conclusive evidence as to which method provides a more accurate partitioning prediction. Both of these methods neglect diffusive water losses (from deep soil) that comprise part of the total evaporation component. These diffusive losses may be 5–10% of total ET (Allen, personal communication, 2001).

This paper is a companion paper to another written by Allen et al. (2005). Allen et al. (2005) introduce the FAO-56 dual crop coefficient procedure and associated two-stage evaporation model and algorithms that were used in the Cal Poly ITRC CALFED/ARI Evaporation Study. Allen et al. (2005) also recommend parameter values, and demonstrates the integration of the procedure to create  $K_c$  at the beginning of the season. That paper also introduces an expansion of the FAO-56 evaporation model to consider three-stage evaporation. The two- and three-stage models are also described in Chapter 6 and in Appendix B of the Cal Poly ITRC CALFED/ARI Evaporation Study report (Burt et al. 2002).

The purpose of this study was to provide an independent evaluation of how the FAO-56 style model predicts bare soil evaporation. Measured bare soil evaporation data sets (identified in the literature) were compared to simulations of those evapora-

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**Table 1.** Summary of Measured Bare Soil Evaporation Data Sets Used to Evaluate the Modified FAO-56 Model

Data set number	Source	Location	Soil type	Evaporation measurement method
1	Ritchie (1972)	Temple, Tex.	Houston black clay; 55% fine montmorillonitic clay	Lysimeter
2	Parlange et al. (1992)	Davis, Calif	Yolo clay loam	Lysimeter
3	Howell et al. (1995)	Bushland, Tex.	Pullman clay loam	Lysimeter
4				
5				
6	Wright (1982, personal communication, 2001)	Kimberly, Id.	Portneuf silt loam	Lysimeter
7	Farahani and Bausch (1995)	Fort Collins, Colo.	Sandy clay loam <sup>a</sup>	Bowen Ratio

<sup>a</sup>Farahani (personal communication, 2000) stated that the laboratory evaluation of the soil from the study location classified it as a sandy clay loam. Soil survey maps identify the soil in the area as a Kim loam.

tion events. Three types of simulations were used, which differed in their methods of defining the required soil parameters used in the FAO-56 model.

## Method

To assess the effectiveness of the FAO-56 style model in simulating bare soil evaporation, measured bare or near-bare soil (when the Leaf Area Index  $\leq 0.15$ ) evaporation events found in the literature were compared to simulations of these events. Data from

five sources presented seven evaporation events using either lysimeters to measure water input and daily evaporation or Bowen Ratio equipment to estimate the daily evaporation from 12-h measurements. Table 1 summarizes general information regarding each of these studies, while Tables 2–6 present detailed information regarding each study.

The weather, irrigation, and evaporation data required to run the comparison simulations were provided by the scientists (personal communication) who published or made the evaporation measurements, except for the Ritchie (1972) paper, which contained much of the necessary data. When required, additional weather data were obtained using the World Wide Web sites for CIMIS (2001a, b) and Colorado Agricultural Meteorological Net-

**Table 2.** Summary for Data Set 1: Houston Black Clay

Parameter	Parameter values for data set
Data set number	1
Source	Ritchie (1972)
Location	Temple, Tex.
Soil	Houston black clay; 55% fine montmorillonitic clay
Supporting weather data	Ft. Hood, Tex.; W. of Temple; from NOAA
Evaporation measurement method	1.83 m $\times$ 1.83 m $\times$ 1.22 m deep lysimeter; backfilled by layers using saturated sieved soil from pit
Start date	April 27, 1969
Date end	May 8, 1969
Total days	12
Reported preirrigation volumetric soil water ( $\text{m}^3 \text{m}^{-3}$ )	Not stated
Reported volumetric soil water at field capacity ( $\text{m}^3 \text{m}^{-3}$ )	Not stated
Reported volumetric soil water at permanent wilting point ( $\text{m}^3 \text{m}^{-3}$ )	Not stated
Rain; Amount (mm) and number of events: Start to end	48.4, 6
Irrigation: Amount (mm) and number of events: Start to end	None
Crop	Sorghum
Planting date	Not stated
Emergence date	April 10, 1969
Leaf area index (LAI) at data end <sup>a</sup>	0.15
Other measured LAI	0.03 April 27, 1969

<sup>a</sup> $E$  and  $T$  data as partitioned in Ritchie (1972) indicated that loss from transpiration is very small when the leaf area index is 0.15 or less.

**Table 3.** Summary for Data Set 2: Yolo Clay Loam

Parameter	Parameter values for data set
Data set number	2
Source	Parlange and Katul (1992)
Location	Davis, Calif.
Soil	Yolo clay loam
Supporting weather data	CIMIS Sta No. 6—Davis, Calif.
Evaporation measurement method	6 m diameter $\times$ 1 m deep lysimeter
Start date	September 14, 1990
Date end	September 23, 1990
Total days	10
Reported preirrigation volumetric soil water ( $\text{m}^3 \text{m}^{-3}$ )	September 13, 1990 0.31: 0–0.75 m deep
Reported volumetric soil water at field capacity ( $\text{m}^3 \text{m}^{-3}$ )	0.26 at $-1/3$ bar; 0–0.3 m deep <i>(the writers note that this looks too low for a clay loam, but these are the values indicated from neutron probe readings)</i>
Reported volumetric soil water at permanent wilting point ( $\text{m}^3 \text{m}^{-3}$ )	0.15 at $-15$ bar; 0–0.3 m deep
Rain: Amount (mm) and number of events: Start to end	18.1, 1
Irrigation: Amount (mm) and number of events: Start to end	None
Crop	None
Planting date	
Emergence date	
Leaf area index (LAI) at data end	
Other measured LAI	



**Table 4.** Summary for Data Sets 3, 4, and 5: Pullman Clay Loam

Parameter	Parameter values for data sets		
	3	4	5
Data set number	3	4	5
Source		Howell et al. (1995)	
Location		Bushland, Tex.	
Soil		Pullman clay loam	
Supporting weather data		1. On site measurements 2. Amarillo Int. Airport, 15 miles east; Acquired from NOAA	
Evaporation measurement method		Avg. from two 3 m × 3 m × 2.3 m deep lysimeters undisturbed soil monoliths <sup>a-c</sup>	
Start date	October 7, 1989	September 18, 1991	September 27, 1992
Date end	November 6, 1989	October 28, 1991	November 5, 1992
Total days	31	41	40
Reported preirrigation volumetric soil water (m <sup>3</sup> m <sup>-3</sup> )	October 13, 1989 <sup>d</sup> 0.36: 0–0.3 m and 0.24: 0.3–1.9 m	Not measured	October 9, 1992 <sup>e</sup> 0.29: 0–0.2 m, and 0.32: 0.2–2 m
Reported volumetric soil water at field capacity (m <sup>3</sup> m <sup>-3</sup> )		0.338; from 0 to 1.6 m deep	
Reported volumetric soil water at permanent wilting point (m <sup>3</sup> m <sup>-3</sup> )		0.216; from 0 to 1.6 m deep	
Rain: Amount (mm) and number of events: Start to end	13.0, 5	25.3, 6	13.0, 6
Irrigation: Amount (mm) and number of events: Start to end	61.1, 4	79.5, 4	82.7, 4
Crop		Winter wheat	
Planting date	October 10, 1989	September 27, 1991	September 29, 1992
Emergence date	October 18, 1989	October 7, 1991	October 9, 1992
Leaf area index (LAI) at data end <sup>f</sup>	Approx 0.15	<0.15	Approx 0.15
Other measured LAI	Not measured	0.4 on December 5, 1991	0.13 on November 2, 1992

<sup>a</sup>1989: Averages of lysimeter data are from NW Lysimeter Wheat—Irrigated and SW Lysimeter Wheat—Dryland; irrigations for the two treatments were matched during the fall and winter.

<sup>b</sup>1991: Averages of lysimeter data are from SE Lysimeter Wheat—Deficit Irrigated and NE Lysimeter Wheat—Irrigated; irrigations for the two treatments were matched during the fall and winter.

<sup>c</sup>1992: Averages of lysimeter data are from NW Lysimeter Wheat—Dryland and SW Lysimeter Wheat—Irrigated; irrigations for the two treatments were matched during the fall and winter.

<sup>d</sup>Measured before a 10.3 mm irrigation on October 13, 1989 and after a 1 mm rain on October 5, 1989, a 0.5 mm rain on October 6, 1989, and a 0.5 mm rain on October 10, 1989.

<sup>e</sup>Measured before 11 mm irrigation on October 9, 1992 and after a 38.8 mm irrigation on October 2, 1992 and a 7.5 mm rain on October 7, 1992.

<sup>f</sup>*E* and *T* data as partitioned in Ritchie (1972) indicated that loss from transpiration is very small when the leaf area index is 0.15 or less.

work (CoAgMet) (2001) or by requesting hard copies of data not available on the web from the National Climatic Data Center. Specific contact and WWW links for these sources are found in the reference section of this paper (NOAA 2001; USDA-NRCS 2001). CoAgMet solar radiation data were corrected due to obvious discrepancies from theoretical incoming solar radiation, and grass reference evapotranspiration (ET<sub>o</sub>) was recalculated using the FAO-56 Penman–Monteith equation with hourly time steps.

The required weather data for the simulations were

1. Occurrence dates and amounts of precipitation or irrigation (mm/d);
2. Average daily wind speed (m/s);
3. Minimum daily relative humidity (%); and
4. Daily grass reference evapotranspiration, ET<sub>o</sub> (mm/d).

The required soil data were

1. The effective depth of soil evaporation layer (*Z<sub>e</sub>*, m);
2. Stage 1 readily evaporable water (REW, mm);

3. Total evaporable water through evaporation Stages 1 and 2 (TEW<sub>2</sub>, mm);
4. Total evaporable water through evaporation Stages 1, 2, and 3 (TEW<sub>3</sub>, mm);
5. Evaporation reduction coefficient (*K<sub>r2</sub>*) at the end of Stage 2 and beginning of Stage 3 (*K<sub>r2</sub>*=0 if there is no Stage 3). See Fig. 1; and
6. Cracking nature of the soil, not required, but offers insight into Stage 3 evaporation potential.

Unlike the weather data, which are generally well defined using the available sources, data for the specific soil at a location are often not readily available and may vary to some degree with time or management practices. In this evaluation, required soil data were obtained with three different methods and provided three series of simulations to compare against the measured evaporation amounts. Specifically, the measured and FAO-56 simulated ratio of daily *E* to ET<sub>o</sub> and cumulative *E* for the events were

**Table 5.** Summary for Data Set 6: Portneuf Silt Loam

Parameter	Parameter Values for Data Set
Data set number	6
Source	Wright (1982, personal communication, 2001); Allen (personal communication, 2001)
Location	Kimberly, Id.
Soil	Portneuf silt loam
Supporting weather data	National Weather Serv. 0.6 m north
Evaporation measurement method	1.83 m × 1.83 m × 1.22 m lysimeter; backfilled by layers, compacted to original bulk density, and saturated with bottom excess water removed using sintered extraction candles
Start date	August 1, 1977
Date end	September 24, 1977
Total days	55
Reported preirrigation volumetric soil water ( $\text{m}^3 \text{m}^{-3}$ )	0.05–0.1
Reported volumetric soil water at field capacity ( $\text{m}^3 \text{m}^{-3}$ )	0.32
Reported volumetric soil water at permanent wilting point ( $\text{m}^3 \text{m}^{-3}$ )	Lower limit of plant available water=0.12–0.16
Rain: Amount (mm) and number of events: Start to end	26.2, 12
Irrigation: Amount (mm) and number of events: Start to end	215.3, 4
Crop	Start of data period is after the harvest of garden peas and end of period is before planting of winter wheat.
Planting date	
Emergence data	
Leaf area index (LAI) at data end	
Other measured LAI	

presented graphically for visual analysis and compared statistically.

These three series of simulations represent an array of possible methods for choosing the soil data that one might use, and the comparison of the results from the three series offers an assessment of the possible impact on the estimation caused by differences between the methods. Prior to describing the differentiation of the soil parameter selections for these three series of simulations, a short discussion of Stage 3 evaporation and the cracking nature of the soils is appropriate.

The FAO-56 model presented in Allen et al. (1998) allowed evaporation to occur in a two-stage process similar in appearance to the empirical model presented by Ritchie (1972). In the FAO-56 model, the relative evaporation rate ( $K_r = E/E_p$ , where  $E_p$  = potential evaporation rate for wet soil) decreases linearly with increasing cumulative evaporation during Stage 2. In this study, a third stage of evaporation is represented by changing the slope of the falling rate of Stage 2. Stage 3 evaporation is associated with a slow and steady vapor transfer rate between moist deep soil and the dry air above, or with soil cracking that exposes deeper soil to the surface evaporation potential. The option for Stage 3 evaporation was added to the FAO-56 model by Allen (1998) to simulate deeply cracking soils in the Imperial Valley of California. The three-stage FAO-56 style model was described by Allen et al. (2005). The values for  $TEW_3$  and  $K_{r2}$ , the value for  $K_r$ ,

**Table 6.** Summary for Data Set 2: Sandy Clay Loam<sup>a</sup>

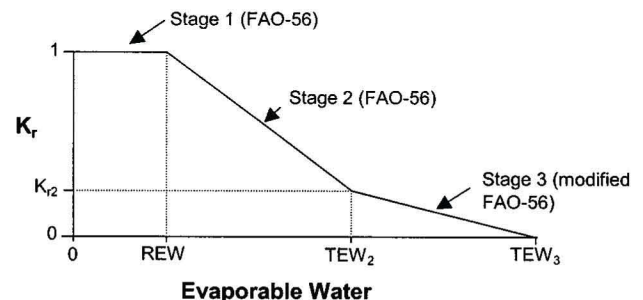
Parameter	Parameter values for data set
Data set number	7
Source	Farahani and Bausch (1995)
Location	Fort Collins, Colo.
Soil	Sandy clay loam
Supporting weather data	CoAgMet Sta. Ftc03—Fort Collins
Evaporation measurement method	Bowen ratio equipment <sup>b</sup> : <i>ET</i> Measurements are for 7 a.m. to 7 p.m. Values were adjusted to account for 24 h of evaporation by multiplying measured evaporation by $R_{s-24 \text{ h}}/R_{s-7 \text{ a.m.}-7 \text{ p.m.}}$ .
Start date	May 15, 1993
Date end	June 8, 1993
Total days	25
Reported preirrigation volumetric soil water	0.28
Reported volumetric soil water at field capacity	0.34
Reported volumetric soil water at permanent wilting point	0.265
Rain: Amount (mm) and number of events: Start to end	56.1, 10
Irrigation: Amount (mm) and number of events: Start to end	none
Crop	Field corn
Planting date	April 28, 1993
Emergence date	May 12, 1993
Leaf area index (LAI) at data end <sup>c</sup>	0.16
Other measured LAI	0.3 on June 14, 1993

<sup>a</sup>Farahani stated that the laboratory evaluation of the soil from the study location classified it as a sandy clay loam. The maps identify the area as a Kim loam.

<sup>b</sup>12 h *ET* measured with Bowen Ratio equipment was calibrated in Bushland, Tex. against lysimeter measurements.

<sup>c</sup>*E* and *T* data as partitioned in Ritchie (1972) indicated that loss from transpiration is very small when the leaf area index is 0.15 or less.

at the start of Stage 3, were based on unpublished work presented in the Imperial Irrigation District Water Use Assessment for the Years 1987–1996. For this research, Stage 3 evaporation was used if specific soils were identified as cracking soils in the USDA-NRCS Soil Survey Division Official Soil Series Descriptions. The soil parameter selection process for each of the three series of simulations follows.

**Fig. 1.** Three stage soil evaporation process



**Table 7.** Typical Soil Water Characteristics for Different Soil Types; Reproduction of Table 19 in Allen et al. (1998)

Soil type (USA Soil Texture Classification)	Soil water characteristics			Evaporation parameters	
	$\theta_{FC}^a$ ( $m^3 m^{-3}$ )	$\theta_{WP}^b$ ( $m^3 m^{-3}$ )	$\theta_{FC}-\theta_{WP}$ ( $m^3 m^{-3}$ )	Stage 1 REW (mm)	Amount of water that can be depleted by evaporation Stages 1 and 2 TEW <sup>c</sup> ( $Z_e^d=0.10$ m) (mm)
Sand	0.07–0.17	0.02–0.07	0.05–0.11	2–7	6–12
Loamy sand	0.11–0.19	0.03–0.10	0.06–0.12	4–8	9–14
Sandy loam	0.18–0.28	0.06–0.16	0.11–0.15	6–10	15–20
Loam	0.20–0.30	0.07–0.17	0.13–0.18	8–10	16–22
Silt loam	0.22–0.36	0.09–0.21	0.13–0.19	8–11	18–25
Silt	0.28–0.36	0.12–0.22	0.16–0.20	8–11	22–26
Silt clay loam	0.30–0.37	0.17–0.24	0.13–0.18	8–11	22–27
Silty clay	0.30–0.42	0.17–0.29	0.13–0.19	8–12	22–28
Clay	0.32–0.40	0.20–0.24	0.12–0.20	8–12	22–29

<sup>a</sup> $\theta_{FC}$ =soil water content at field capacity ( $m^3$  of after per  $m^3$  of soil;  $m^3 m^{-3}$ ).

<sup>b</sup> $\theta_{WP}$ =soil water content at permanent wilting point ( $m^3 m^{-3}$ ).

<sup>c</sup>TEW=Total evaporable water=maximum depth of water that can be evaporated from the soil when the soil has been initially completely wetted (mm); TEW=1,000( $\theta_{FC}-0.5\theta_{WP}$ ) $Z_e$ .

<sup>d</sup> $Z_e$ =depth of surface soil layer that is subject to drying by way of evaporation (0.10–0.15 m).

### Simulation Series 1: General Soil Parameters from FAO-56 as Used in the CALFED/ARI Evaporation Study

The CALFED/ARI Evaporation Study (Burt et al. 2002) used general values for the REW and TEW<sub>2</sub> soil parameters as recommended in FAO-56 Table 19 (see Table 7 of this paper). The Houston black clay was simulated using average REW and TEW<sub>2</sub> values from Table 7 for clay. The clay loam, silt loam, and sandy clay loam soils were grouped together and were represented by typical REW and TEW values from Table 7 for a silt texture. Although Table 19 of FAO-56 contains characteristics of a silt

loam, it was felt that the REW and TEW values for a silt more closely matched the mix of the CALFED/ARI Evaporation Study soils. The  $Z_e$  parameter was set at 0.1 m.

The Portneuf silt loam soil at Kimberly, Id., which was not identified as having cracking tendencies, was modeled using a third stage of evaporation during the Series 1 simulation since three-stage evaporation was used in all simulations of silt loam soils in the CALFED/ARI Evaporation Study. The third stage, and associated TEW<sub>3</sub>, provided better estimates than did a two-stage simulation for the Portneuf silt loam soil when a  $Z_e=0.1$

**Table 8.** Series 1 Simulation Soil Parameter Values.<sup>a</sup> These Follow the Soil Groupings Used in the CALFED/ARI Evaporation Study and Were Used in the Comparison between Measured and FAO-56 Simulated Bare Soil Evaporation.

	Houston black clay	Yolo clay loam	Pullman clay loam	Portneuf silt loam	Kim loam/sandy clay loam
Source	Ritchie (1972)	Parlange et al. (1992)	Howell et al. (1995)	Wright (personal communication, 2001)	Farahani and Bausch (1995)
Stage 1 REW (mm)	10	9	9	9	9
Stages 1 and 2 TEW <sub>2</sub> (mm)	26	24	24	24	24
Stages 1, 2, and 3 TEW <sub>3</sub> (mm) <sup>b</sup>	50	—	45	40	—
$K_{r2}$ : Evaporation Coefficient at end of Stage 2 <sup>b</sup>	0.2	—	0.2	0.2	—
$Z_e$ or the effective depth of soil evaporation layer (m) <sup>c</sup>	0.1	0.1	0.1	0.1	0.1
Cracking nature of simulated soil <sup>d</sup>	Yes	No	Yes	No <sup>d</sup>	No

<sup>a</sup>Soil parameters for the soils in the Series 1 simulations were grouped consistently with the method used in the CALFED/ARI evaporation study that estimated evaporation from California agricultural lands. In that study the clay loam, silt loam, and sandy clay loam soils were grouped together and the Stage 1 and Stage 2 soil parameters for this group were represented by the parameters for an average silt soil as identified in Table 19 of Allen et al. (1998). Note that  $Z_e$  in the CALFED/ARI Evaporation Study was set at 0.1 for all soils.

<sup>b</sup>Stage 3 evaporation parameters for the three-stage FAO-56 model were based on information from the report: Water Study Team. Imperial Irrigation District Water Use Assessment for the years 1987–1996 (1998). Received via Freedom of Information Act.

<sup>c</sup>FAO-56 recommends using values for  $Z_e$  between 0.1 and 0.15 m.  $Z_e$  was set to 0.1 m during Simulation Series 1 and 2.

<sup>d</sup>In the Series 1 simulations, the cracking soil designations match the USDA-NRCS Soil Survey Division Official Soil Series Description designations of this property for the actual soils from the five locations. However, some silt loam soils in the CALFED/ARI evaporation study were modeled using a third stage of evaporation. For the Series 1 simulations, the Portneuf silt loam at Kimberly was modeled better using a third stage of evaporation than without when  $Z_e=0.1$  m was used, and was modeled in this manner to represent those California silt loam soils where three stages of evaporation were used in the CALFED/ARI evaporation study.

**Table 9.** Series 2 Simulation Soil Parameter Values

	Houston black clay	Yolo clay loam	Pullman clay loam	Portneuf silt loam	Kim loam/sandy clay loam
Source	Ritchie (1972)	Parlange et al. (1992)	Howell et al. (1995)	Wright (personal communication, 2001)	Farahani and Bausch (1995)
Specific soil texture from evaporation experiment location	Clay; 55% fine montmorillinite clay	Clay loam	Clay loam	Silt loam	Loam, but sandy clay loam by lab analysis of soil at site
Stage 1 REW (mm)	—	7	8	8	8
Stage 1 and 2 TEW <sub>2</sub> (mm) <sup>a</sup>	—	18.7	23	37.5	20.8
Stages 1, 2, and 3 TEW <sub>3</sub> (mm) <sup>b</sup>	—	—	45	—	—
Evaporation Coefficient at end of Stage 2 <sup>b</sup>	—	—	0.2	—	—
Z <sub>e</sub> or the effective depth of soil evaporation layer for Stage 2 evaporation (m) <sup>a</sup>	—	0.1	0.1	0.15	0.1
Cracking nature of observed soil <sup>c</sup>	Yes	No	Yes	No	No

<sup>a</sup>The TEW for the Series 2 simulations were computed using Eq. 73 from Allen et al. (1998):  $TEW = 1,000(FC - 0.5WP)Z_e$ , where field capacity (FC) and wilting point (WP) were reported by the scientist and are listed in Table 1. As with the Series 1 simulations, all soils in the Series 2 simulations were modeled with a  $Z_e = 0.10$  m except the Portneuf silt loam, where  $Z_e = 0.15$  m as recommended Allen (personal communication, 2001) and Wright (personal communication, 2001). REW values for the Series 2 simulations were approximated from the reported FC and WP values. Scientist reported soil parameter values were not available for the Houston black clay. Therefore this soil was not simulated during Series 2.

<sup>b</sup>Stage 3 evaporation parameters for the extended FAO-56 model were based on information from the report: Water Study Team. Imperial Irrigation District Water Use Assessment for the Years 1987–1996 (1998). Received via Freedom of Information Act.

<sup>c</sup>Note that the cracking tendencies of the soils for the Series 2 and Series 3 simulations match the USDA-NRCS Soil Survey Division Official Soil Series Description designations of this property for the actual soils from the five locations. The change from cracking to noncracking designation for Portneuf silt loam was strengthened by statements from the local scientists: Allen (personal communication, 2001) stated that this soil seems to be better modeled without cracking tendencies and, from personal observations, Wright (personal communication, 2001) stated that although the portion of a Portneuf silt loam furrow that is saturated usually does crack on drying, the cracking is typically only about 0.05 m deep. The surface soil that is wetted by soaking in between the furrows usually does not crack on drying.

was used. A larger value for  $Z_e$  and a two stage simulation was used for the Portneuf soil during Series 2. Table 8 shows the specific soil parameters used in the Series 1 simulations.

### Simulation Series 2: Scientist-Reported Soil Parameters

For this series of simulations, the FAO-56 Model used REW and TEW<sub>2</sub> soil parameters that were developed from detailed soils data provided by the scientists that conducted the specific field evaporation studies. Specific soils data for the Houston black clay were not available. The  $Z_e$  parameter for the Portneuf silt loam

was changed to 0.15 m, as recommended by Allen (personal communication, 2001) and Wright (personal communication, 2001). For the other soils,  $Z_e$  was left at 0.1 m. The Portneuf silt loam soil simulation was run without Stage 3 evaporation in the Series 2 simulations. Table 9 shows the specific soil parameters used in the Series 2 simulations.

### Simulation Series 3: Best-Fit Soil Parameters

Simulation Series 3 modified soil parameters from the Series 2 simulations. REW, TEW<sub>2</sub>, TEW<sub>3</sub>, and  $K_{r2}$  evaporation coefficients were altered manually to obtain the best fit between the

**Table 10.** Simulation series 3 soil Parameter Values Altered to Produce the Best Comparison Between Measured and FAO-56-style Simulated Evaporation.

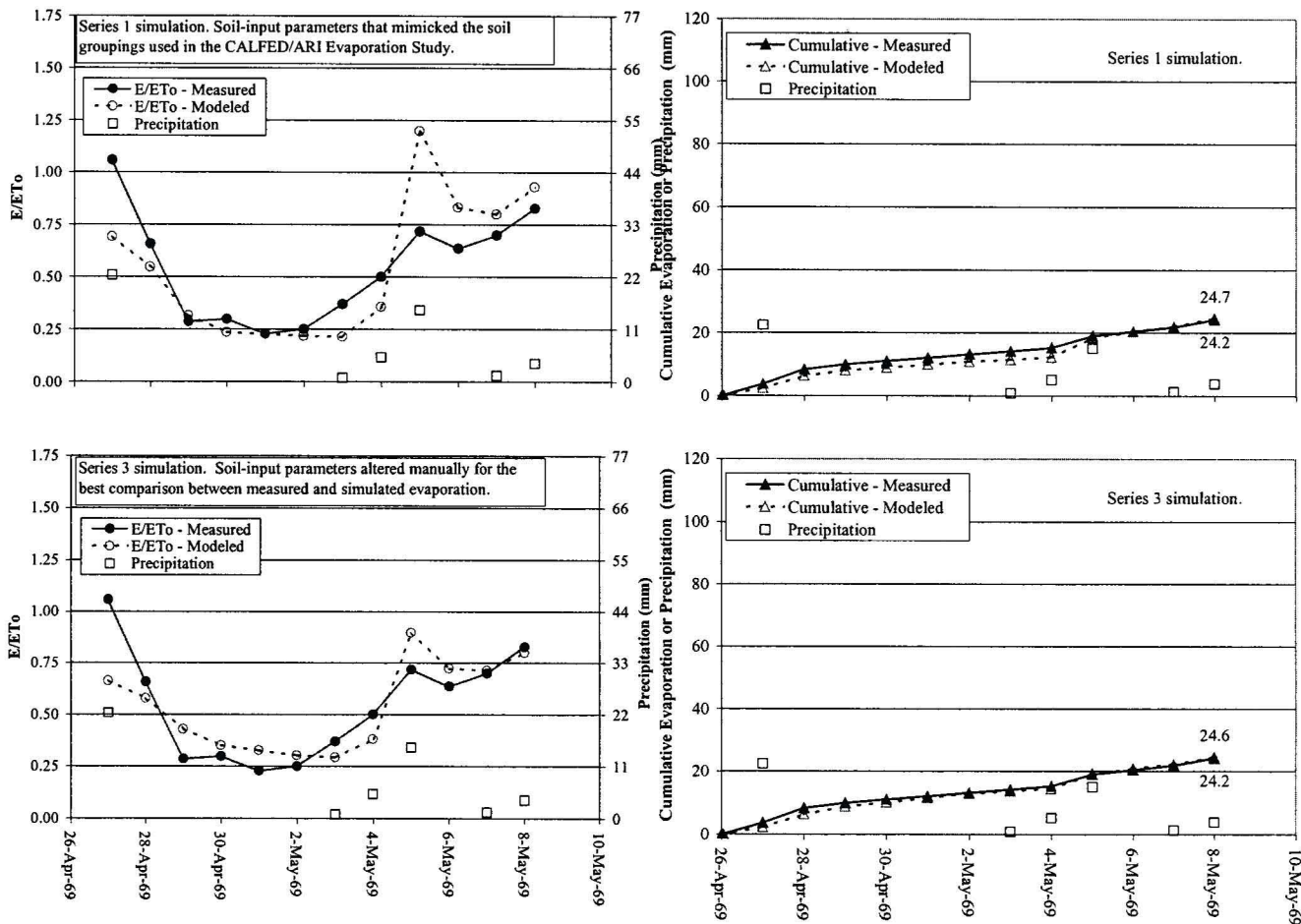
	Houston black clay	Yolo clay loam	Pullman clay loam	Portneuf silt loam	Kim loam/sandy clay loam
Source	Ritchie (1972)	Parlange et al. (1992)	Howell et al. (1995)	Wright personal communication, (2001)	Farahani and Bausch (1995)
Stage 1 REW (mm)	7	2	7	13	10
Stages 1 and 2 TEW <sub>2</sub> (mm) <sup>a</sup>	30	6	22	40	25
Stages 1,2, and 3 TEW <sub>3</sub> (mm) <sup>b</sup>	50	18	45	—	—
Evaporation Coefficient at end of Stage 2 <sup>b</sup>	0.3	0.35	0.2	—	—
Z <sub>e</sub> or the effective depth of soil evaporation layer (m) <sup>a</sup>	0.115	0.032	0.096	0.16	0.12
Cracking nature of simulated soil <sup>c</sup>	Yes	No	Yes	No	No

<sup>a</sup>In the Series 3 simulation, values were determined for  $Z_e$  to produce the value shown for TEW<sub>2</sub> based on Eq. 73 from Allen et al. (1998):  $TEW = 1,000(FC - 0.5WP)Z_e$  where field capacity (FC) and wilting point (WP) were reported by the scientist and are listed in Table 1.

<sup>b</sup>Stage 3 evaporation methods for three-stage FAO-56 model were based on information from the following report: Water Study Team. Imperial Irrigation District Water Use Assessment for the Years 1987–1996 (1998). Received via Freedom of Information Act.

<sup>c</sup>Relative to the Series 2 simulations, only the Yolo clay loam simulation was altered to include Stage 3 evaporation in the best fit simulations.





**Fig. 2.** Comparison of daily bare soil  $E/ET_o$  ratios and of cumulative bare soil evaporation for lysimeter measurements in 1990 at Temple, Tex.—Houston black clay—reported by Ritchie (1972) and FAO-56 model results. Simulation results for two variations on the soil parameter definitions. Scientist reported soil parameter values were not available for this soil. Therefore it was not simulated during Series 2.

measured and simulated evaporation events. During Simulation Series 3, the Yolo clay loam was altered to include Stage 3 evaporation. The  $Z_e$  parameters were modified from those used in the Series 2 simulations to create values for  $TEW_2$  as shown in Table 10. Table 10 summarizes the specific soil parameters used in the Series 3 simulation.

## Results and Discussion

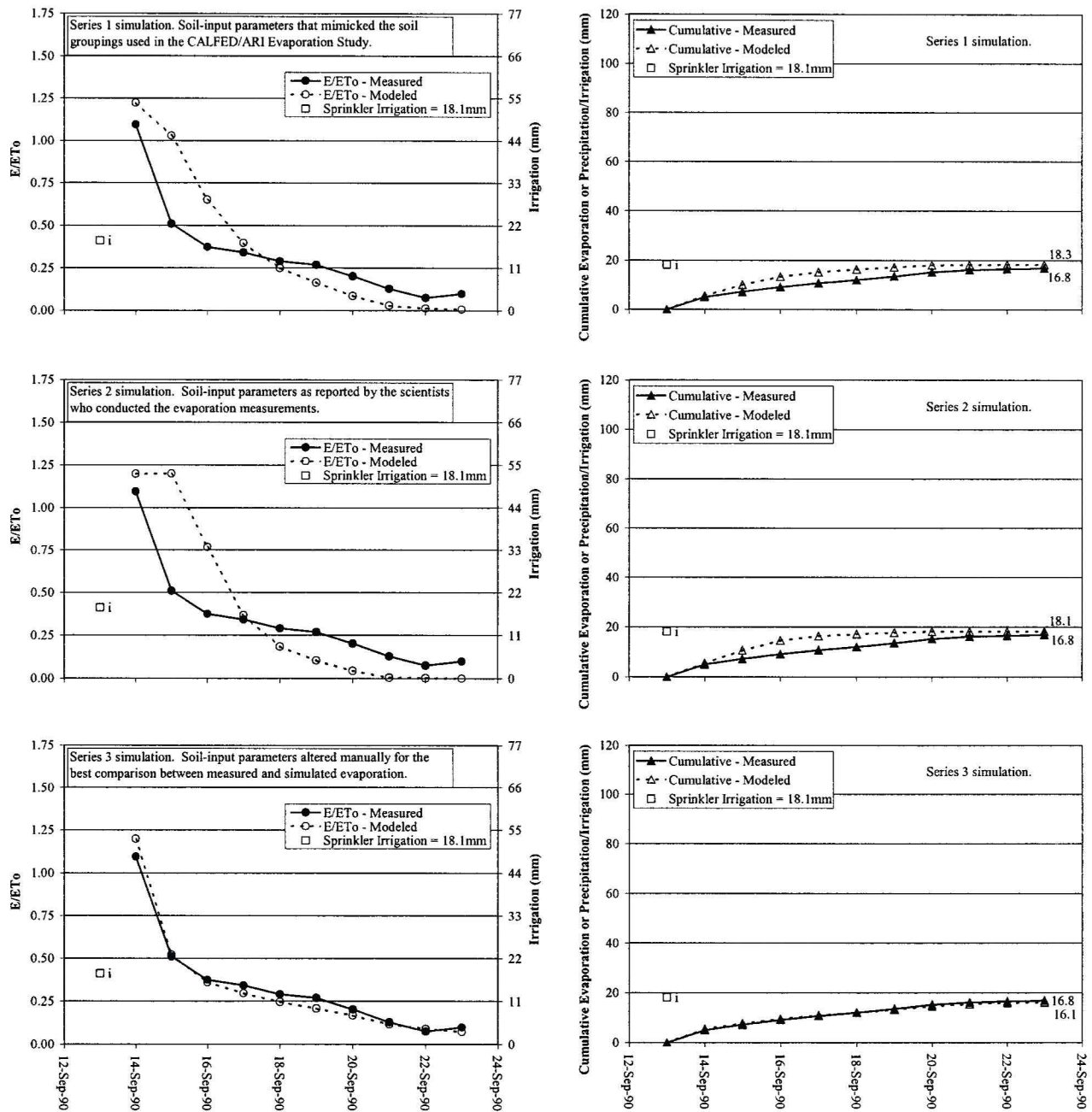
The figures in this section display the measured and simulated  $E/ET_o$  versus time, and cumulative evaporation versus time, for five of the seven bare soil evaporation data sets used to evaluate the model. The results from these five data sets demonstrate key points learned from this evaluation. Each figure includes measured and simulation comparisons for the three variations (Series 1, 2, and 3) used for defining the soil parameters.

### General Observations about the Figures of $E/ET_o$ and Cumulative $E$

1. The measured and simulated  $E/ET_o$  and cumulative bare soil evaporation trends (Figs. 2–6) were similar among the three simulation series that used different approaches to define soil parameters. This indicates that the FAO-56 evaporation

model is generally valid for predicting evaporation from bare soil and that the general soil values published in FAO-56 are sufficient for general prediction work.

2. The similarity between predicted and measured evaporation values offers confidence as to the capability of the two-stage and three-stage FAO-56 model to provide good prediction of bare soil evaporation when there is sound weather data.
3. Following large precipitation or irrigation events, the FAO-56 simulated ratios of  $E/ET_o$  were similar to measured ratios of  $E/ET_o$  (Figs. 2–6). Maximum measured  $E/ET_o$  often exceeded 1.2, which contrasts with findings by Snyder et al. (2000), who found that maximum  $E/ET_o$  measurements following soil wetting ranged from 0.8 to 1.0 in Imperial Valley, Calif.
4. The response of  $E/ET_o$  to small precipitation or irrigation events occurring several days after a large irrigation event as simulated by the FAO-56 model tended to be smoother and of lower magnitude than the measured  $E/ET_o$  response (Figs. 2–6). This is due to the dampening caused by the water balance conducted for the entire surface soil layer (of depth  $Z_e$ ) in the FAO-56 model, so that small wetting events increase the average water content of the entire layer by a small amount and consequently the predicted ratio  $E/ET_o$  may not change significantly. In reality, small events will rehydrate the skin of the soil surface and will generally shift



**Fig. 3.** Comparison of daily bare soil  $E/ET_o$  ratios and of cumulative bare soil evaporation for lysimeter measurements in 1990 at Davis, Calif.—Yolo clay loam—reported by Parlange et al. (1992) and FAO-56 model results. Simulation results for three variations on the soil parameter definitions.

the evaporation process temporarily into Stage 1 drying. Allen et al. (2005) have expanded the FAO-56 method to conduct two separate water balances of the surface soil layer to account for skin wetting. Their expansion of the method was not tested in this study.

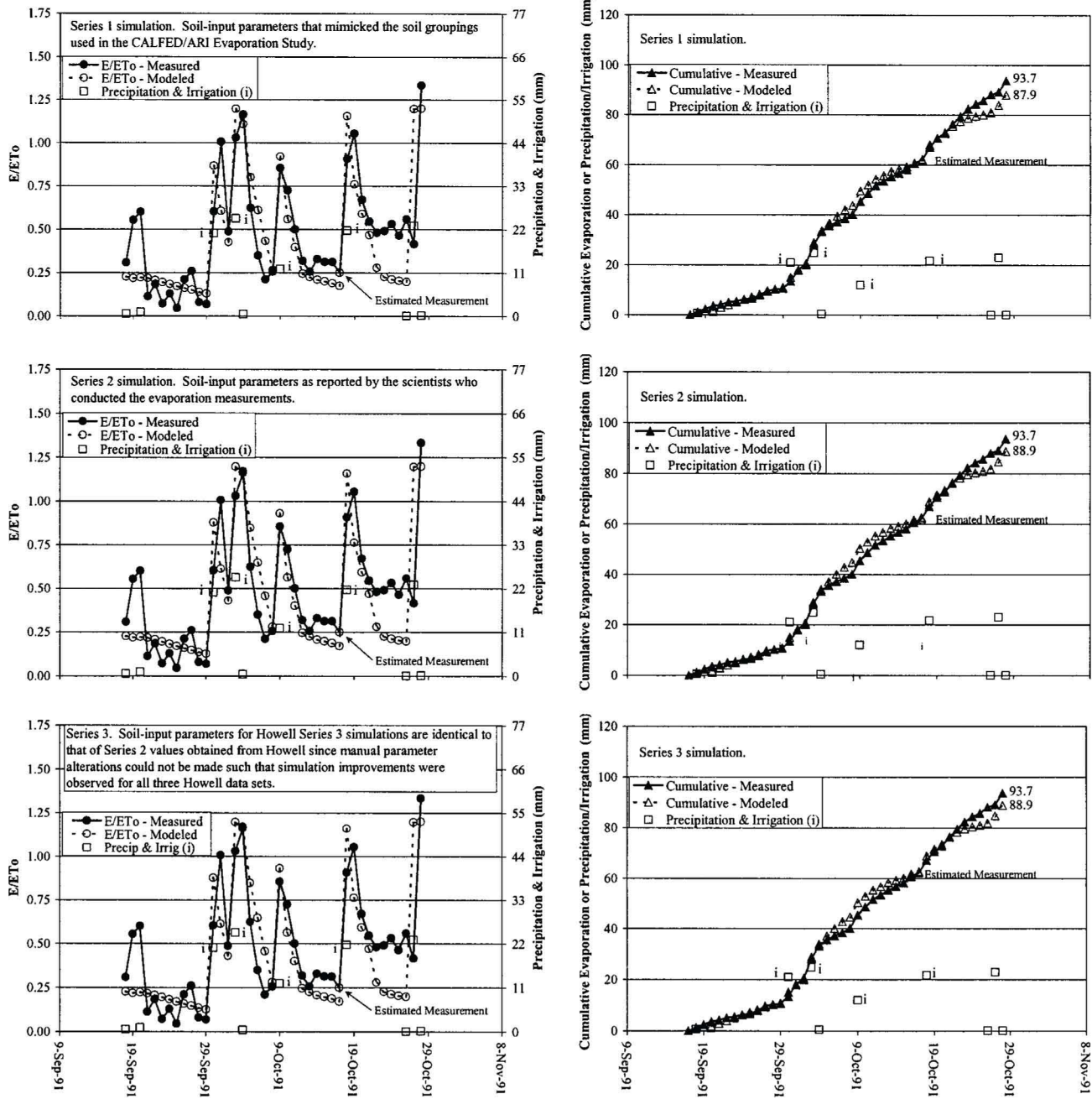
- Occasionally, the upper limit on the evaporation and transpiration component ( $K_{c\ max}=1.20$ ) in the Modified FAO-56 model was reached and even exceeded (Figs. 2–6). It should be noted that  $K_{c\ max}$  is intended for cropped surfaces, but in the CALFED/ARI Evaporation Study this limit was included in the bare soil evaporation as well. The value of 1.20 is to account for impacts of lower albedo of wet soil relative to grass, coupled with heat storage in the soil surface layer prior to wetting (Allen et al. 1998). The impact of allowing  $K_{c\ max}$

to limit the rate of bare soil evaporation appears to be minimal since it was only occasionally exceeded by measured data and, over time, the simulated cumulative evaporation was very similar to the measured value for all three series of simulations (Figs. 2–6).

### General Observations about the Statistical Evaluation of the Bare Soil Evaporation Simulations

There are several possibilities that could be used as a basic evaluation of how well the two-stage FAO-56 model and enhancement to a three-stage model performed in simulating soil evaporation. The method that seemed most appropriate was to compare the evaporation weighted average percent difference between the





**Fig. 4.** Comparison of daily bare soil  $E/ET_o$  ratios and of cumulative bare soil evaporation for lysimeter measurements in 1991 at Bushland, Tex.—Pullman clay loam—reported by Howell et al. (1995) and three-stage FAO-56 model results. Simulation results are for three variations on the soil parameter definitions.

measured and the simulated cumulative bare soil evaporation. The evaporation weighted average was a straightforward method of minimizing bias that could be introduced by the variation in the time of year, the geographical location, and length of evaluation period for the seven data sets.

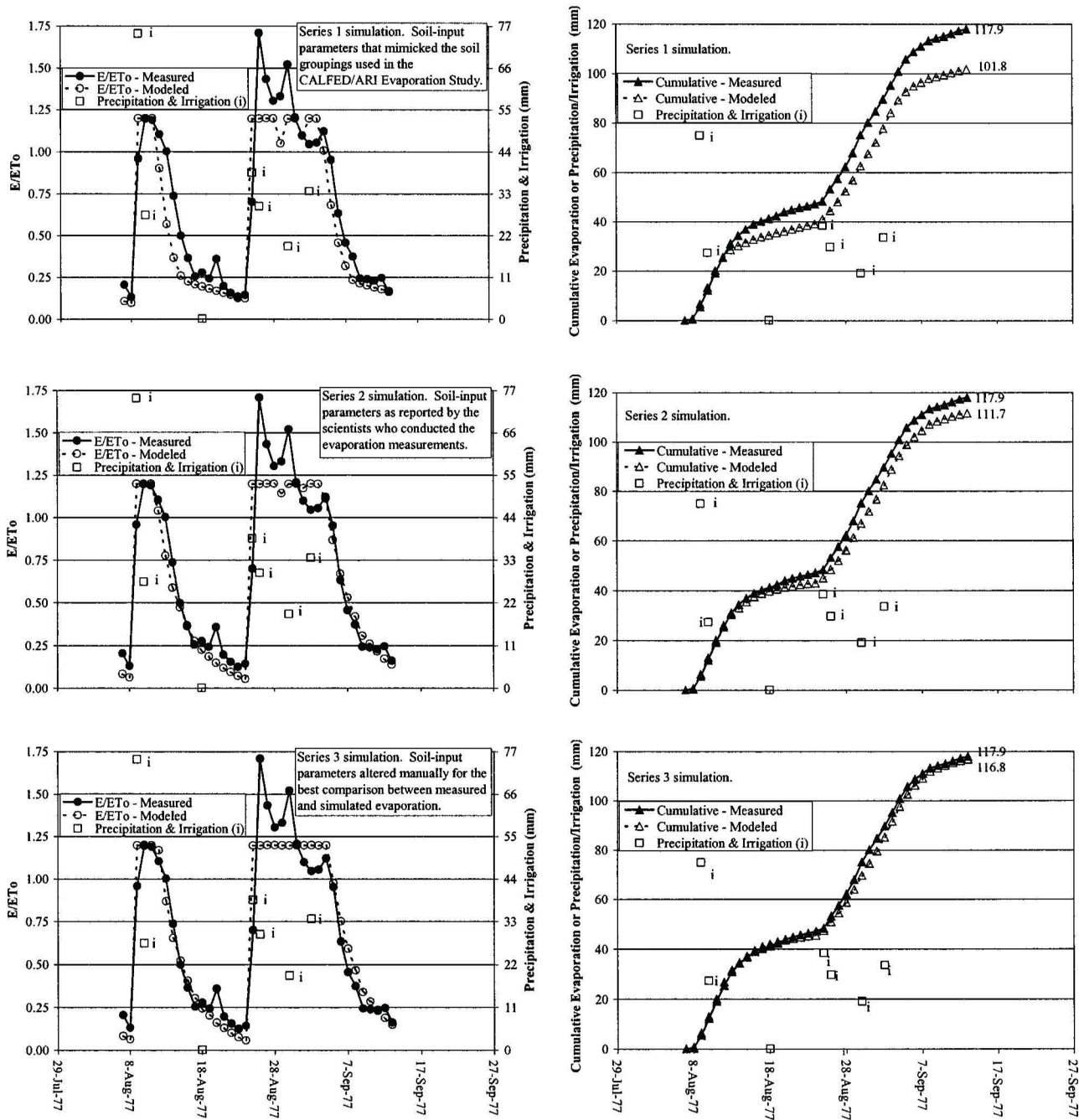
The evaporation weighted average percent difference between the measured and FAO-56 simulated cumulative evaporation was negative for all three methods of defining the simulation parameters for all soils (Tables 11–13). As one might expect, the general method for defining the soil parameters (Series 1 simulations) resulted in more average evaporation weighted error than when

the scientist-reported (Series 2) or best-fitted (Series 3) soil parameters were used:  $-7.3$ ,  $-4.2$ , and  $-3.1\%$ , respectively, when the Ritchie data set is not included.

#### **Specific Findings from This Evaluation of Soil Water Evaporation Predicted by the Two- or Three-Stage FAO-56 Model**

Specific findings from this evaluation of soil water evaporation predicted by the two- or three-stage FAO-56 model are

1. The FAO-56 style soil water evaporation model, patterned



**Fig. 5.** Comparison of daily bare soil  $E/ET_o$  ratios and of cumulative bare soil evaporation. Lysimeter measured (in 1977 at Kimberly, Id.—Portneuf silt loam—reported by Wright personal communication, 2001) and FAO-56 model results. Simulation results are for three variations on the soil parameter definitions.

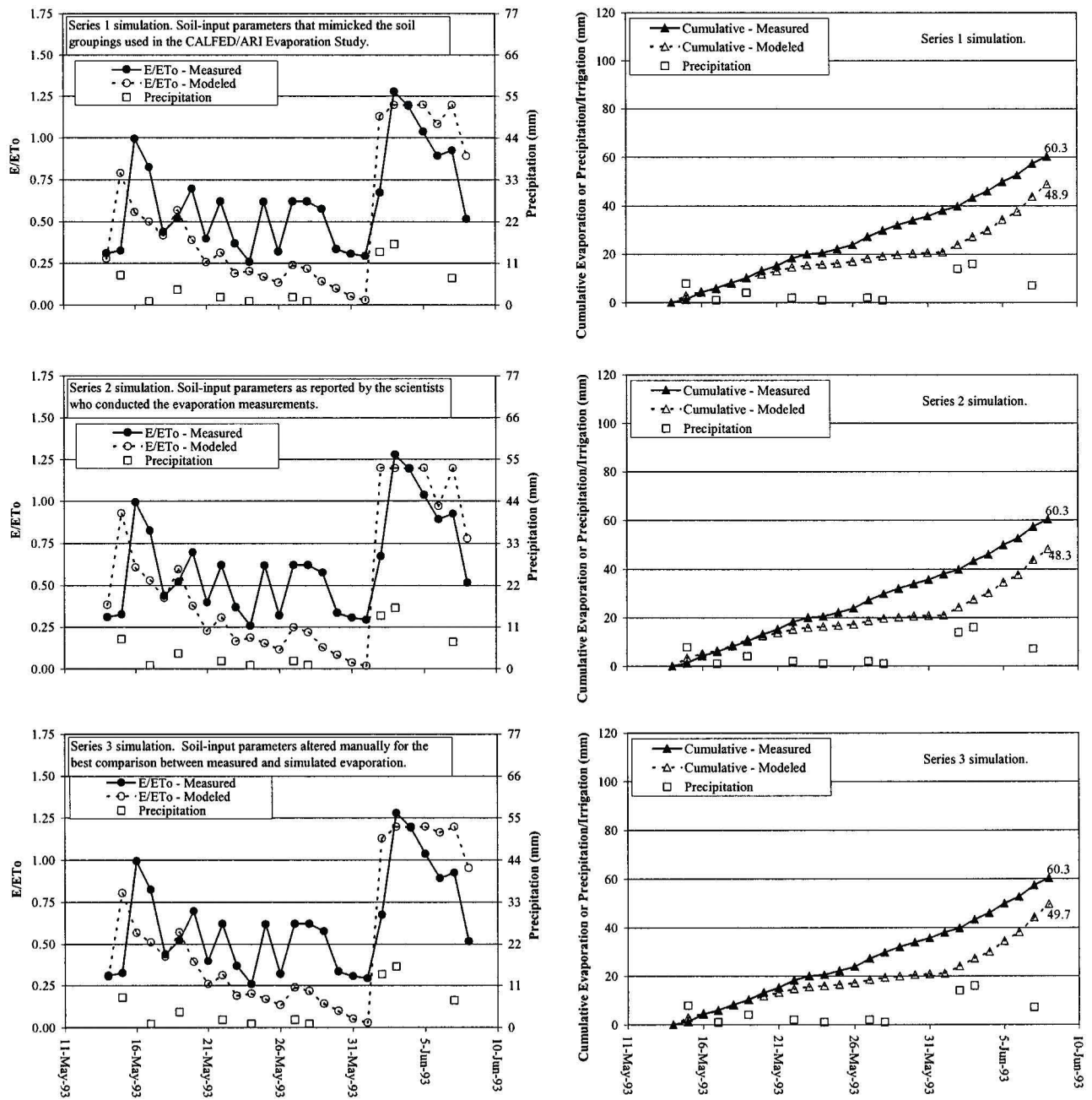
after Ritchie (1972), provided a good physical structure for simulating evaporation from bare soil. The use of a daily soil water balance and the use of two or three stages of drying in the model appears to be sound. There is a tendency for a small to modest improvement in model results when scientist-reported soil parameters (Series 2) are used in simulations, rather than general parameters from FAO-56 whose values are based on general textural classes (Series 1).

Specifically, the improvement in the straight percent difference between the measured and modeled cumulative bare soil evaporation ranged from 1 to 2% for 4 of the 6 comparable data sets.

Results were worse for Series 2 as compared to Series 1 for a fifth data set [the 1992 lysimeter data from Howell et al. (1995) found in Tables 11 and 12].

The sixth Series 2 simulation [using Wright (personal communication 2001) data] that had scientist-reported soil data for the Portneuf silt loam soil in Kimberly, Id. resulted in the most significant improvement over the Series 1 simulation, by increasing the depth of the evaporation zone ( $Z_e$ ) from 0.1 m to the reported value of 0.15 m and using a two-stage process rather than three-stages. The Series 2 simulation brought the cumulative evaporation 8.4% closer to the measured cumulative value (Fig. 5 and





**Fig. 6.** Comparison of daily bare soil  $E/ET_o$  ratios and of cumulative bare soil evaporation for Bowen Ratio measurements in 1999 at Fort Collins, Colo.—sandy clay loam—reported by Farahani and Bausch (1995) and FAO-56 model results. Simulation results for three variations on the soil parameter definitions.

Tables 11 and 12). This improvement occurred even though the total evaporative water (TEW) for the two series was essentially the same (TEW<sub>3</sub> in Series 1 was 40 mm and TEW<sub>2</sub> in Series 2 was 38 mm). The two-stage series allowed water to be depleted more quickly between wetting events.

This information indicates that if a bare soil evaporation simulation using the FAO-56 model is conducted for an individual soil, it is generally best to use scientist-reported soil parameters if they are available. However, when a bare soil evaporation simulation is conducted for many soil types simultaneously, for example, in computing water consumption for a large area, the expedience of using generalized soil parameters will likely result in only a modest reduction in the overall prediction accuracy. The best value for  $Z_e$ , the soil depth parameter for the FAO-56 model,

is not well defined for specific soils, but a general value of 0.1 m worked well for three of the five soils in this evaluation. The Portneuf and Colorado soils required a 0.15 m depth for accurate simulation with the two-stage evaporation model.

2. To obtain the best fit between the measured and simulated bare soil evaporation (Series 3, Table 13), the REW parameter (Table 10) was altered to a value outside of the typical range for this parameter, as listed in Table 7. For example, the best-fit REW for the Yolo clay loam data set was 2 mm, although the typical REW range for a silt loam soil listed in Table 7 is 8–11 mm. (Note that Table 7 does not list clay loam. Therefore average silt loam parameters were used to define the clay loam soils in the Series 1 simulations.) Further, the best fit required a third stage of evaporation for the

**Table 11.** Measurements of Bare Soil Evaporation Compared to FAO-56 Simulated Bare Soil Evaporation. Simulation Series 1.

	Ritchie (1972)	Parlange et al. (1992)	Howell et al. (1995)			Wright (personal communication, 2001)	Farahani and Bausch (1995)
Soil type	Clay	Clay loam	Clay loam			Silt loam	Sandy Clay loam
Year measurements were collected	1969	1990	1989	1991	1992	1977	1993
Measurement method	Lysimeter	Lysimeter	Lysimeter			Lysimeter	Bowen ratio
Number of days from start to end of evaluated period	12	10	31	41	40	37	25
Rain or irrigation during period (mm)	48.4	18.1	74.0	104.8	95.7	223.8	56.1
Measured cumulative bare soil evaporation (mm)	24.2	16.8	52.8	93.7	81.2	117.9	60.3
Modified FAO-56 modeled cumulative bare soil evaporation (mm)	24.7	18.3	51.5	87.9	84.4	101.8	48.1
Percent difference between measured and modeled cumulative <i>E</i> (%)	2.1	8.9	-2.4	-6.1	3.9	-13.7	-20.2
Evaporation-weighted average percent difference between measured and modeled cumulative bare soil evaporation (%)						Without Ritchie -7.3	All data sets -6.3

**Table 12.** Measurements of Bare Soil Evaporation Compared to FAO 56 Simulated Bare Soil Evaporation. Simulation Series 2.

	Ritchie (1972)	Parlange et al. (1992)	Howell et al. (1995)			Wright (personal communication, 2001)	Farahani and Bausch (1995)
Measured cumulative bare soil evaporation (mm)	—	16.8	52.8	93.7	81.2	117.9	60.3
Modified FAO-56 modeled cumulative bare soil evaporation (mm)	—	18.1	52.5	88.9	85.6	111.7	48.3
Percent difference between measured and modeled cumulative <i>E</i> (%)	—	7.9	-0.6	-5.1	5.4	-5.3	-19.9
						Without Ritchie	—
Evaporation-weighted average percent difference between measured and modeled cumulative bare soil evaporation (%)						-4.2	—

**Table 13.** Measurements of Bare Soil Evaporation Compared to FAO 56 Simulated Bare Soil Evaporation. Simulation Series 3.

	Ritchie (1972)	Parlange et al. (1992)	Howell et al. (1995)			Wright (personal communication, 2001)	Farahani and Bausch (1995)
Measured cumulative bare soil evaporation (mm)	24.2	16.8	52.8	93.7	81.2	117.9	60.3
Modified FAO-56 modeled cumulative bare soil evaporation (mm)	24.6	16.1	52.5	88.9	85.6	116.8	49.7
Percent difference between measured and modeled cumulative <i>E</i>	1.6%	-4.0%	-0.6%	-5.1%	5.4%	-0.9%	17.6%
						Without Ritchie	All data sets
Evaporation-weighted average percent difference between measured and modeled cumulative bare soil evaporation						-3.1%	-2.8%



Yolo clay loam soil, with a  $TEW_2$  of 6 mm, as opposed to the  $TEW_2$  range of 18–25 mm for silt loam soil in Table 7.

Although not tested, it may have been possible to obtain best-fit parameters for the Series 3 simulations closer to expected ranges in value had the  $Z_e$  parameter, representing the depth of drying in the profile at the end of stage 2, been allowed to vary more. However, what seems crucial is that the overall benefit of using best-fit soil parameters (Table 13), rather than general (Table 11) or scientist-reported (Table 12) soil parameters, appears to be rather modest. Furthermore, in order to identify best-fit soil parameters, one must have a complete bare soil evaporation data set for optimizing the specific FAO-56 model soil parameters. If such a data set is not readily available, it is likely that the potential improvement in simulation would likely be overshadowed by the cost and effort required to obtain the data.

3. The average evaporation weighted errors indicate that the model underestimates bare soil evaporation by about 7% (Tables 11–13). This said, the relatively sparse number of bare soil evaporation data sets that were available for this evaluation does not allow one to conclude a bias for the FAO-56 evaporation model to overestimate or underestimate bare soil evaporation using the published model parameters.
4. To assess a 95% confidence interval containing model error may result in an erroneous measure of the model accuracy, simply due to the limited number of available data sets. Instead, it may be better to look at the nonevaporation weighted percent differences and to use observed errors to generalize the potential model accuracy.

The Series 1 simulations (using soil parameters defined in Table 7 and the CALFED/ARI Evaporation Study method for grouping the soil types) can be used as an approximation of expected error. Some percent differences between the measured and modeled cumulative bare soil evaporation were high (8.9%) and some were low (–20.2%). From this range, we estimate the general accuracy of the FAO-56 model, when applied with general estimates of soil parameters, to be about  $\pm 15\%$ .

## Conclusions

The measured and the two- and three-stage FAO-56 simulated  $E/ET_o$  and cumulative bare soil evaporation trends and values were similar for each of the three methods used for defining soil simulation parameters. All other things being equal, the Series 2 simulation using measured soil parameters tended to give similar results to the Series 1 simulation that used generalized soil parameters. The Series 3 simulation indicated that the soil parameters can be varied from general or measured values to obtain somewhat better correlations—even though there may not be a logical justification for individual parameter values except to obtain better correlations. Specifically, the average evaporation weighted percent difference between the measured and the simulated cumulative evaporation was –4.2% for the Series 2 simulations and –7.3 and –3.1% for the Series 1 and Series 3 simulations, respectively, for data sets that were directly comparable.

The tendency for the model to underestimate bare soil evaporation for the data sets in this evaluation by 7% does not necessarily mean that the FAO-56 model will always underestimate evaporation since the number of possible data sets evaluated (7) was relatively small. Simulations of some of the data sets resulted in an overestimate and some resulted in an underestimate of the cumulative evaporation measurements. Therefore this evaluation

does not conclusively indicate that the FAO-56 model has a bias when simulating bare soil evaporation.

Rather than identifying the statistical accuracy of the model for predicting bare soil evaporation using the relatively sparse number of identified data sets, the accuracy may be best estimated by general comparison of the measured and simulated evaporation. For the simulations that used the general soil parameters published in FAO-56 (Series 1), it appears that the model is accurate to about  $\pm 15\%$  based on the largest overestimate and the largest underestimate of the cumulative bare soil evaporation.

For bare soil evaporation simulations, it seems reasonable that if one has good site-specific soil parameter information for use in the FAO-56 model, the results will tend to have a modest improvement over a simulation that uses generally defined soil parameters. For broad scope evaluations of bare soil evaporation, use of generalized soil parameters seem to be dependable. The effort to obtain the site specific parameters will tend to be rewarded by only modest improvements in the evaporation estimate.

The simulations using best-fit soil parameters (Simulation Series 3) were for comparison purposes only to find the most improvement possible in model accuracy. The Series 3 simulation is artificial in nature, as the optimized parameter values tended to be outside the normal ranges expected for soils. The results were only slightly better than for the other two simulation series.

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