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## A PARTICLE TRACKING TECHNIQUE FOR BEDLOAD MOTION

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### ABSTRACT

The advances made in scientific visualization techniques have enhanced our capabilities of tracking sediment and measuring sediment rates. The focus of this study is to provide a new experimental approach to determine the displacement speed of particles rolling atop a well packed layer of spheres and provide a formula that describes the average displacement speed of particles as a function of the particles geometry and weight, settling velocity, and the frictional characteristics of flow. This study presents the measurements of the displacement speeds of three different sized spherical particles under varying flow conditions and bed roughness. The particles, ranging in size from 1.6 cm to 2.5 cm in diameter, primarily experienced motion due to rolling. The displacement speed information is required for the prediction of sediment fluxes, which can be used to model local sediment entrainment in natural gravel streams. A laboratory flume was used to perform 30 experimental runs. The tests were repeated 15 times, or until repeatability was established. Velocity profiles, shear stress, discharge, and bulk velocity were acquired for each run. An ADV and Swoffer were used to obtain the velocity profiles. Sediment motion was monitored using a plan view from a digital camera mounted above the flume. Individual frames depicting a particle's motion were produced using Asymetrix DVP and Adobe Photoshop 4.0. Data translation software combined the individual frames to calculate the displacement speed of sediment motion. The results are compared with values predicted by bed load formulas developed by Sekine and Lee. Values observed in this experiment are greater than the values predicted by Sekine and less than the values predicted by Lee.

### 1. INTRODUCTION

Several methods are commonly used to measure sediment transport, including detention ponds, various observation methods, and the use of both portable and stationary samplers.

A detention pond can be utilized for capturing sediment for measurement by routing a stream through a pond. All material moved as either bedload or in suspension is effectively trapped by the stilling effects of the pond (Leaf, 1970; Troendle, et al., 1996). Each fall, after runoff from

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snowmelt recedes, the ponds are drained and the accumulated sediment is excavated. The total sediment volume is calculated using surveyed data of the difference in bed elevation (Ryan and Troendle, 1997). This method yields an annual transport and can be correlated with flow conditions for that year.

Bed load measurements can also be made by observation of tracer particles before and after a flow event. There are two basic methods of observation. The first is known as "seeding," where individual particles are gathered, painted, and replaced with their positions marked during low flow. After a flow event, any movement of the particles from their original marked location is considered particle transport (Ryan and Troendle, 1997). The second is the "painted area" method. An exposed portion of the bed is painted and photographed while the stream is at a low stage. After a flow event, the painted area is again photographed. Non-colored particles inside the painted region are considered to be transported bedload (Ryan and Troendle, 1997). Recently, other tracer particles have been used as predictors of bedload transport. Specifically, "spy cobbles" have been developed that are equipped with a geographic positioning system (GPS) to track the pathway of bedload particles in natural streams and their traveling (displacement) distances. Also, in the laboratory, advancements in video imaging have eased the process of tracking particle displacement to determine the displacement velocity of particles and relate it to bedload (Papanicolaou et al., 1999).

Probably the most common means of sampling is by portable sampler. Bedload estimates are made from portable samplers, such as the Helley-Smith sampler (Figure 1). The sampler is placed on the bed of the channel and sediment is collected and analyzed.

Stationary samplers are samplers designed to be placed and left in place for operation. They come in several forms. The traditional sediment trap is an example of a stationary sampler where bedload falls or rolls into a trap that extends across the bottom of the channel. A more recent development is the magnetic tracer technique, which makes use of the naturally magnetic pebbles and cobbles of the riverbed. When a magnetic pebble crosses the detector log, a voltage peak is induced according to the Faraday inductive principle (Bunte, 1992). The sediment is then collected in sampling net behind the sensor.

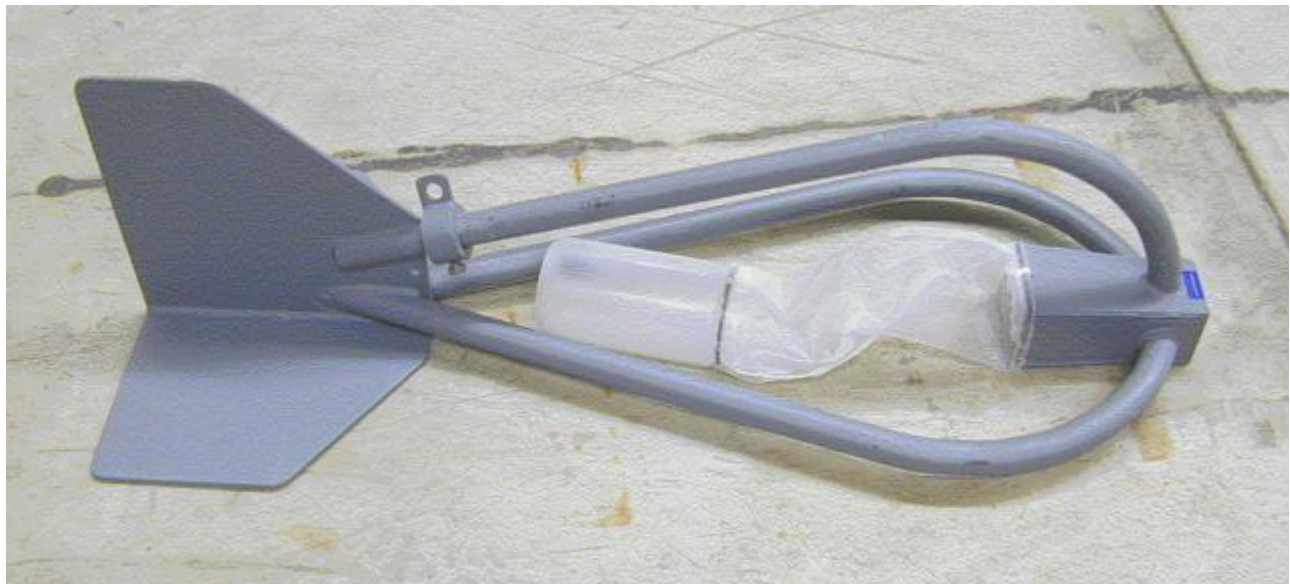


Figure 1 Helley-Smith bed load sampler.

***Limitations of existing devices:*** Each of these methods of measurement has serious limitations. Detention ponds only yield an annual flux of sediment and are therefore not able to differentiate between suspended load and bedload, nor can they measure the bedload rate during a single flow event. Also, it may take many years to build up a sufficient database (Ryan and Troendle, 1997).

When particles are removed and replaced, as in the case of seeding, the particles become more susceptible to movement. Bed material tends to orient itself into the most stable form possible. This will most likely cause the seeded particles to move to a more stable position and can lead to an overestimation of bedload rate. Another limitation is the recovery rate of particles after movement. Ryan and Troendle (1997) found that the recovery rate for their study was less than 30%. One of the major disadvantages of the painted area method is that part of the bed must be exposed in order to paint the particles. Because of this, the most representative section of bed over which movement is occurring might not be tested. Particle sizes may also be distorted by overlaying particles or by the orientation of the picture plane (Church et al., 1987).

With portable samplers, the size of the particles that can be sampled is limited by the opening of the sampler. In gravel streams, this often leads to truncation of the upper size fractions in the distribution of the bed load. Helley-Smith samplers openings are typically  $7.62 \times 7.62$  cm (3 in  $\times$  3 in). According to the USGS Office of Surface Water Technical Memorandum No. 90.08 (1990), nozzle opening should be two or more times larger than the grain size of interest (Ryan and Troendle, 1997). This limits samples to a very small size range. In order to get accurate measurements, the samplers must also be placed on a flat bed, which is rarely the case in steep gravel streams. If not placed correctly, the nozzle can dive down and cause scouring of the bed and an overestimation of bed load rate (Ryan and Troendle, 1997). Also, such devices can become unmanageable in high flow conditions and many require the use of tether lines, boats, or beams (Ryan and Troendle, 1997). Because of the limitations on sizes that can be sampled and the requirement of a flat bed, the Helley-Smith is best utilized only in sand bed rivers.

Sediment traps cannot be moved and must be excavated when they fill. The magnetic tracer technique employed by Bunte (1992) is a good improvement on being able to capture the largest size fractions and being less intrusive, but it is not without drawbacks. The sample only covers portions of the active channel and takes at least three people to collect (Bunte, 1992). This means that a good understanding of where the bed load is occurring in the channel is vital in correctly placing the device the first time. The tracer is also constricted to a short sampling duration and is unable to capture particles less than 10mm (Bunte, 1992).

All of these techniques lack the ability to make local measurements, i.e. transport induced from a pier, fish passage culverts, large particle, or bedform. Portable samplers such as a Helley-Smith are non-applicable to steep mountain streams where the bed is dominated by non-uniform gravel. The development of an accurate, portable, non-intrusive instrument is vital in order to have a better understanding of the hydraulic, morphologic, and sedimentation processes in gravel rivers for preservation and restoration of these natural resources.

## **2. GRAVEL TRANSPORT SENSOR (GTS)**

The Gravel Transport Sensor (GTS) (Figure 2) was developed by John Downing of D & A Instruments in Port Townsend, WA. It is an acoustic device that detects moving sediment particles as they impact a steel pipe, accumulates a count of impacts, and stores a record of the impacts at a regular interval.

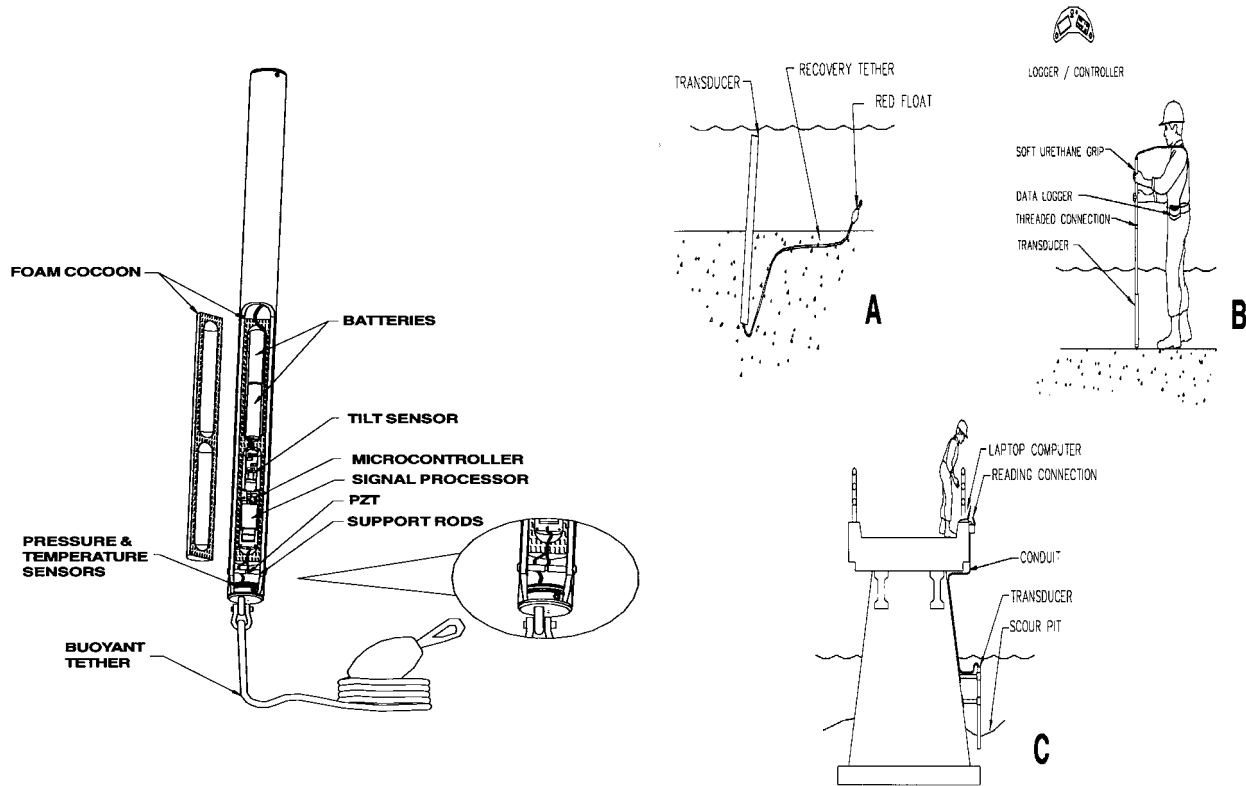


Figure 2 A sketch of the GTS system and its different uses (after Downing, 1999).

The GTS is able to detect particles ranging from 10 mm to 128 mm in size moving as bedload, i.e., rolling, sliding, or bouncing (Downing, 1999). The GTS has the potential to become a useful tool in measuring bedload in gravel bed streams and rivers, gravel beaches, and gravel talus slopes (Downing, 1999). The GTS can have sampling periods and duration times downloaded to it from a computer and then be placed in the active layer or attached to a pier and left for up to 5 months at a time. The recorded information can then be downloaded to the computer for data analysis.

In operation, moving particles strike the GTS cylinder and excite damped vibrations in the cylinder that are picked up by a piezoelectric vibration sensor (PZT). The electrical signal produced by the PZT is detected, amplified, and produces a signal. The first part of the signal is a high frequency, rapidly decaying ping that is followed by resonant ringing of the cylinder (Downing, 1999). In order to avoid masking a new impact, an 8<sup>th</sup> order high pass filter is used to remove the ringing. An analog circuit processes the signals, rejects flow and bedload noise, and uses an adaptive filter to a comparator to output logic pulses for counting (Downing, 1999).

### 3. OBJECTIVE

The objective of this research was two-fold. First, it was designed to test the ability of the GTS to accurately detect moving particles in a streambed under a variety of flow conditions. The second objective was to develop an equation that provides the velocity of individual particles and use this equation to estimate the flux of sediment particles impinging the GTS.

### 3.1 Testing of the GTS

Tests were performed in a 0.5 m wide and 15 m long water-recirculating flume. The prototype GTS cylinder was 59 and 567 mm in diameter and length respectively. All tests used uniform spherical glass particles, which eliminated any variance that might arise due to the shape of the particles or composition of the bed and allowed the study to focus on the ability of the GTS to detect particles. An artificial bed of well-packed 8 mm glass beads was used to provide a uniform roughness and eliminate hiding and embeddedness effects over the test section. These particles were glued in place around the cylinder to prevent scour. Three particle sizes, 25.4, 22.2, and 15.9 mm in diameter (1, 7/8, and 5/8 in), were tested over six different flow conditions. Particles were placed at a distance of 4.5 to 6 particle diameters apart. This was to prevent “grouping” of particles during the tests, even though this may not represent the bed conditions in the stream at all times. Figure 3 shows a setup of the test section. Velocity measurements were made along the vertical axis with a Swoffer 2100 current meter, and flow rates were measured with a sharp crested weir. A video camera was mounted above the GTS to monitor particle behavior around the cylinder.

All tests were conducted under uniform flow conditions. The GTS recorded 20 samples per output with an interval of 5 seconds. Data for bedload rate, velocity profile, flow depth, flow rate, recorded impacts by GTS, and actual impacts on GTS were collected for each test.

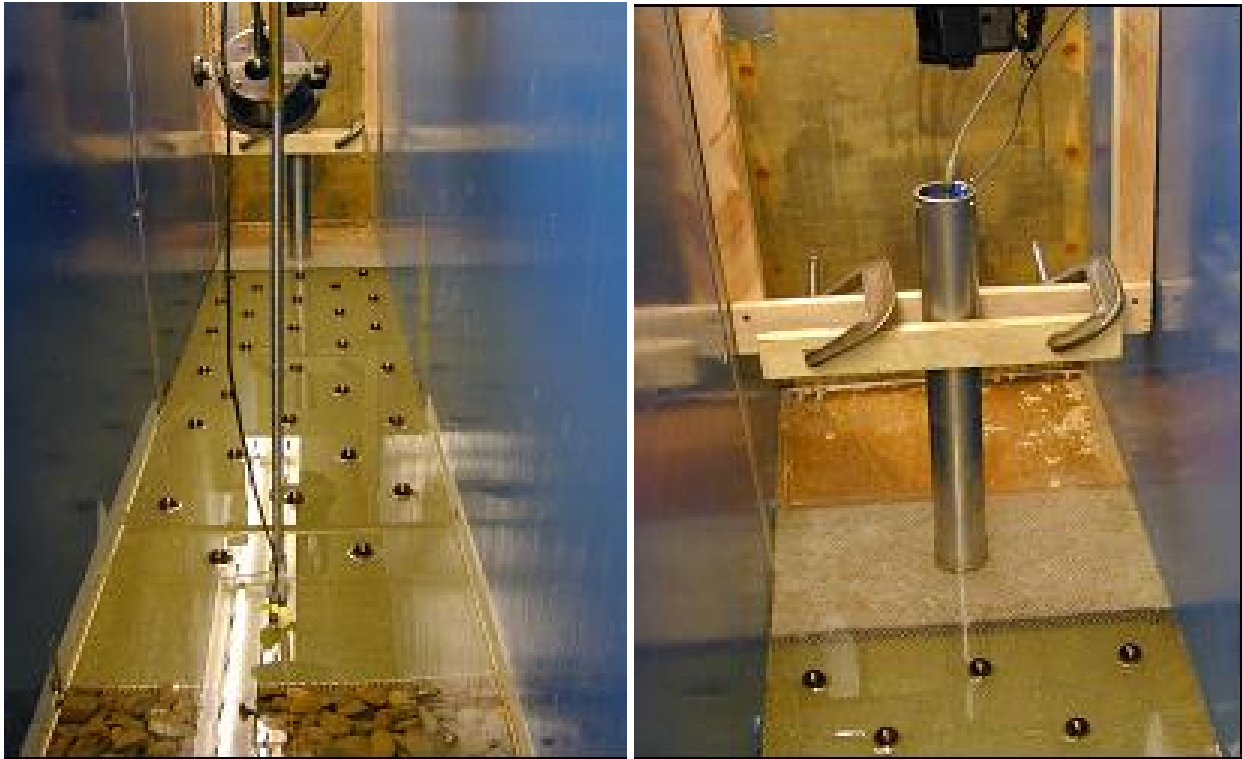


Figure 3 Test section and GTS setup.

Preliminary analysis of uniformly sized sediment experiments has clearly shown that a linear correlation exists between the ping rate (expressed in Hz) and sediment flux (expressed in Kg/m/s) (Figure 4). These tests were conducted six times, each time using different size spheres, and they are only applicable to uniform sized gravel.

In the present study, this limitation was removed by performing experiments with different-sized gravel. The major thrust of this project was the development of a method that converts sediment momentum measurements to sediment flux measurements when sediment particles of different sizes are transported and hitting the GTS. Once the correlation between the pings rates and the momentum of the particles colliding with the GTS is determined, we will utilize the momentum equation along with the fluid velocity (assuming a zero time lag between fluid and particle motion) in order to determine the masses of the particles.

To convert momentum to sediment flux, the theory of fractional sediment transport was considered. According to this theory, if there are  $i$ -different gravel sizes present atop a stream bed with diameter  $d_i$ , then  $F_i$  denotes the fraction of sediment found atop the stream having diameter  $d_i$ ,  $m_i$  is the mass of an individual grain with size  $d_i$ , and  $Y_i$  is a mobility coefficient. The total mass of sediment with size  $d_i$  will be equal to

$$M_i = \sum (m_i \frac{F_i}{d_i^2} Y_i) \quad (1)$$

and the momentum  $J_i$  of each  $i$ -fraction will be

$$J_i = \sum M_i U_i \quad (2)$$

where  $U_i$  is the particle velocity. The momentum  $J_i$  is provided by the GTS while the particle velocity is determined in the second phase of the project.

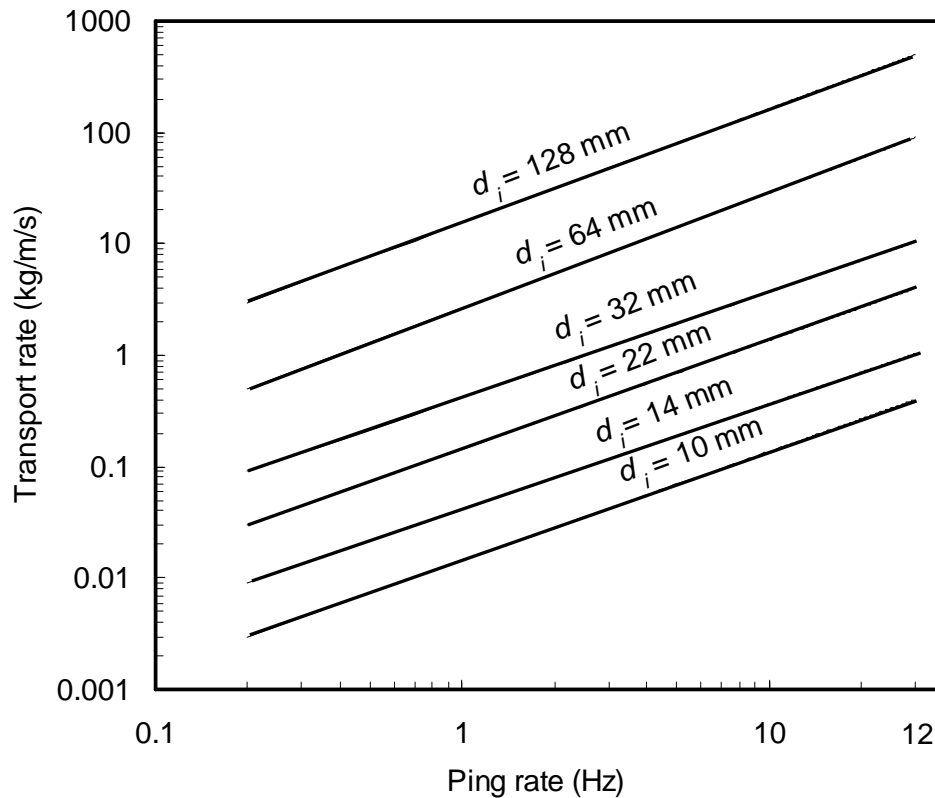


Figure 4 Sediment flux versus "ping" rate.

### 3.2 Determination of the Particle Velocity

The majority of the particle monitoring was performed in the same flume (15 m long and 0.5 m wide) with a stationary slope of zero. Complementary runs were also conducted in a larger tilting flume that is 21 m long and 0.91 m wide. The rolling motion of four groups of spherical particles with diameters of 8mm, 15.9 mm, 22.2 mm, and 25.4 mm was monitored for varying flow conditions and bed roughness. The flow conditions ranged from the incipient condition to flows causing general sediment motion. Bed roughness conditions were simulated by using spheres with diameters of 8 mm and 19 mm and a gravel bed with a median sediment size of 6.5 mm. The thickness of the simulated roughness bed was about 3.5 cm. The bed was flattened to avoid protrusion effects and was well compacted to allow the unimpeded transport of the entrainable spheres.

Four major initial testing conditions were examined throughout the tests: initial condition B1 corresponds to an 8 mm spherical bed with a zero slope, B2 is a 19.05 mm spherical bed with zero slope, B3 is a 6.36 mm average diameter gravel bed with a slope of 0.005, and B4 is an 8 mm spherical bed with a slope of 0.002. Overall, a total of 40 tests were run with multiple particles being displaced in each test.

An Acoustic Doppler Velocimeter (ADV) and a Swiffer 2100 current meter were used to obtain the velocity profiles throughout the water depth and flow rates were measured with a sharp crested weir. The velocity profiles were used in conjunction with the Clauser method to determine the friction velocity. The Clauser method was necessary since the shear velocity expression

$$U_* = \sqrt{gRS} \quad (3)$$

where  $g$  is the gravitational acceleration,  $R$  is the hydraulic radius and  $S$  is the bed slope, cannot be used with a slope of zero that was present in some of the bed conditions. Incipient flow conditions were determined based on a trial and error method and were defined as the conditions corresponding to the dislodgment of individual particles from their initial position (Papanicolaou et al., 2002).

A digital camera captured the particle movement over a flat bed. The camera was mounted above the flume in order to obtain a plan view of the bed. Individual pictures depicting particle motion were obtained using Asymetrix DVP and Adobe Photoshop 4.0. Two frames showing the displacement of a particle over a known time span were combined using image analysis software developed by Data Translation. The displacement was measured in pixels, and those pixels were converted to a distance by comparison to a known distance in pixels. With this information, the average displacement velocity of the particle could be determined. To obtain the virtual velocity from the average displacement velocity, the only additional information needed was the average resting period of particles as they were transported downstream. The average displacement distance was divided by the sum of the average displacement time and the resting period to calculate the virtual velocity. Error encountered using the image analysis software and the repeatability of the results was less than 6-8%. The same technique has been used by Papanicolaou et al. (1999) to define displacement of particles.

The backbone of this methodology is based on the consideration that the lower limit for bedload motion is the incipient motion and the upper limit is saltation. Based on this consideration, the functional dependence of particle velocity on fluid, flow, and sediment bed parameters can be determined through the use of dimensional analysis (the Buckingham  $\pi$  theorem). This analysis yields six dimensionless  $\pi$  terms described in the following equation:



$$F(U_p^*) = F_1 \left( \frac{w}{kU_*}, \frac{k_s}{d_i}, \frac{H}{d_i}, \frac{U_*^2}{gd_i \left( \frac{\rho_s}{\rho} - 1 \right)}, \frac{U_* d_i}{\nu}, \left( \frac{\rho_s}{\rho} - 1 \right) \right) \quad (4)$$

where  $F(U_p^*)$  is a function of the dimensionless particle velocity,  $g$  is the gravitational acceleration,  $H$  is the average water depth,  $U_*$  is the friction velocity,  $\kappa$  is the von Karmen constant,  $d_i$  is the diameter of the test material,  $k_s$  is the bed roughness,  $w$  is the fall velocity,  $\rho_s$  is the density of the test materials,  $\rho$  is the water density, and  $\nu$  is the kinematic viscosity of water.

The first term on the right hand side of eq. 4 denotes the Rouse number, which is indicative of the mode of sediment motion. The second term in eq. 4 is the relative roughness term. The remaining terms are the relative submergence, the dimensionless bed shear stress  $\tau_*$ , known as the Shields parameter, the particle Reynolds number  $Re_*$ , and the non-dimensional submerged weight of the test material. Equation 4 can be further simplified if we account for the dependency of the dimensionless bed shear stress  $\tau_*$  on the particle Reynolds number  $Re_*$ ; combine the Rouse number with the dimensionless bed shear stress, and neglect the non-dimensional submerged weight of the test material, since it is already included in the shear stress term.

The simplified version of equation (4) is:

$$G(U_p^*) = F_2 \left( \frac{w}{kU_*}, \frac{k_s}{d_i}, \frac{H}{d_i}, \frac{U_*^2}{gd_i \left( \frac{\rho_s}{\rho} - 1 \right)} \right) \quad (5)$$

This functional dependence will be experimentally explored at flows varying between threshold conditions and conditions representing general motion for the displacement speed tests and for the virtual velocity tests. A comparison of the dimensionless formula proposed here with that of Sekine and Kikkawa (1992) will be provided. The Sekine and Kikkawa formula was developed to describe the mechanics of saltating grains and provided a function of particle velocity as function of the friction velocity and fall velocity. The Sekine and Kikkawa formula is expressed as:

$$U_p^* \frac{U_p}{\sqrt{\frac{\rho_s - \rho}{\rho} g d_i}} = \frac{U_*}{w} \sqrt{1 - \frac{U_*}{w}} \quad (6)$$

#### 4. RESULTS

To validate the velocity profile obtained from the Swoffer current meter, depth-averaged velocity was calculated from the velocity profile and checked against the depth-averaged velocity calculated from the flow rate and depth. The two compared well with each other (Figure 5).

Velocity profiles were well represented by the Log-Law

$$\frac{U}{U_*} = \frac{1}{\kappa} \ln\left(\frac{y}{k_s}\right) + B \quad (7)$$

where  $U$  is the average velocity at a distance,  $y$ , from the bed,  $U_*$  is the shear velocity,  $\kappa$  is the von Karmen constant taken to be 0.4,  $k_s$  is the equivalent sand grain bed roughness, and  $B$  is a constant of integration. The Log-Law velocity profiles were plotted linearly to determine  $U_*$  from the slope of the profile based on the Clauser method (1956) (Figure 6).

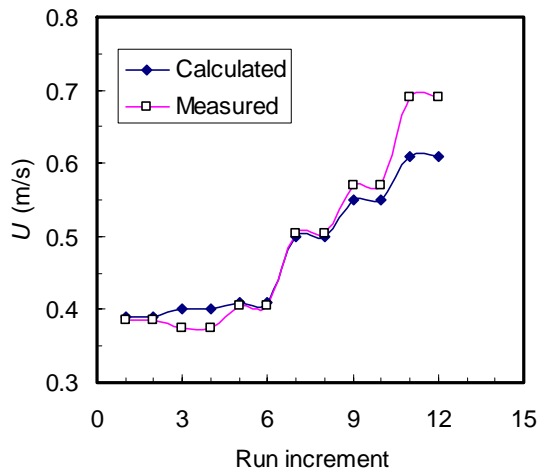


Figure 5 Depth averaged velocities.

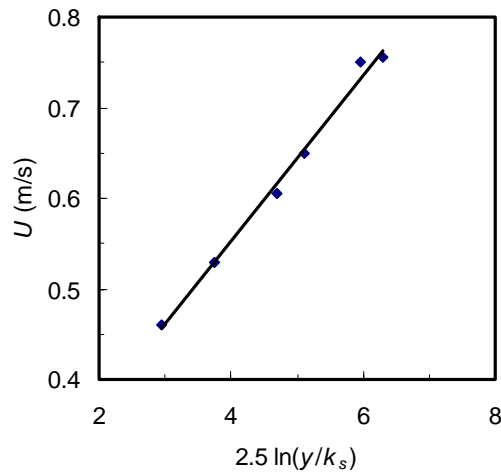


Figure 6 Velocity profile.

To add consistency and validity to the test, measured bedload rate was nondimensionalized as:

$$q_{s*} = \frac{q_s}{\sqrt{(\rho_s / \rho - 1)gd_i^3}} \quad (8)$$

and plotted against dimensionless bed shear stress  $\tau_*$

$$\tau_* = \frac{U_*^2}{(\rho_s / \rho - 1)gd_i} \quad (9)$$

where  $q_s$  is volumetric bedload rate per unit width. For the three different particles sizes tested, it was found that  $q_{s*} \propto \tau_*^{2.50}$  (Figure 7). This agrees with Paintal's (1971) data for bed load with

relatively high shear stress values. The actual values of  $\tau_*$  are lower than would be expected in the present study because of the well-packed uniform bed that the test particles were placed on.

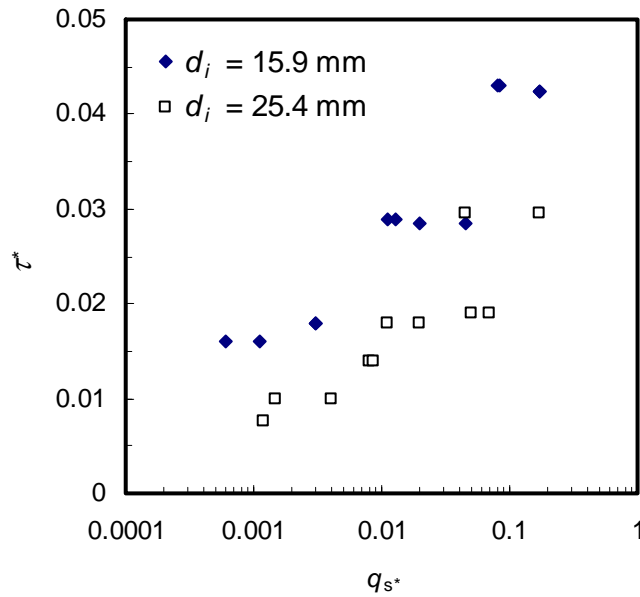


Figure 7 Variation in bed load with shear stress.

Video tape was analyzed to determine the number of times a particle actually hit the cylinder per run, actual hits, and how many times the flow around the cylinder influenced the particle to go around the cylinder instead of hitting it. The term theoretical hits is used to describe the sum of actual hits and the number that were influenced by the flow around the cylinder. Measured bedload was compared to the predicted bedload from the recorded impacts as well as the theoretical impacts to assure that a representative portion of the bedload was passing through the occupied cylinder area (Figure 8). The measured and theoretical bed load rates compare well to each other, showing that the number of particles on path to hit the cylinder area can be applied to the rest of the bed.

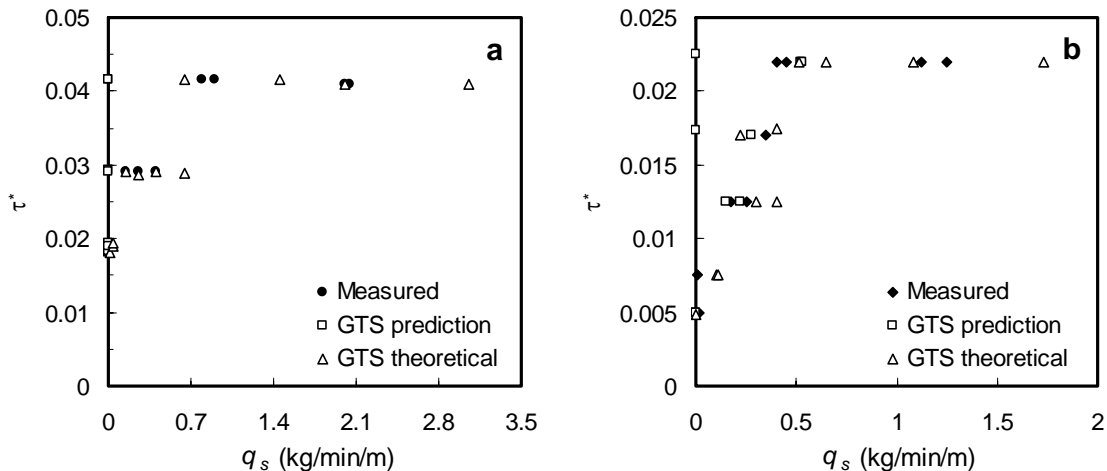


Figure 8 Comparison of theoretical and measured bed load: a)  $d_i = 15.9$  mm; b)  $d_i = 25.4$  mm.

The theoretical and actual impacts, or pings, were then compared to the number of impacts recorded by the GTS (Figure 9). As a general trend, as the velocity of the fluid increased, the ability of the GTS to detect particles heading towards it decreased. Its ability to detect the particles also decreased with particle size. Figure 10 shows that with a decrease in particle size, theoretical hits increased while recorded hits decreased. It is worth noting that for the smallest size tested,  $d_i = 15.9$  mm (5/8 in), the GTS did not detect any particles.

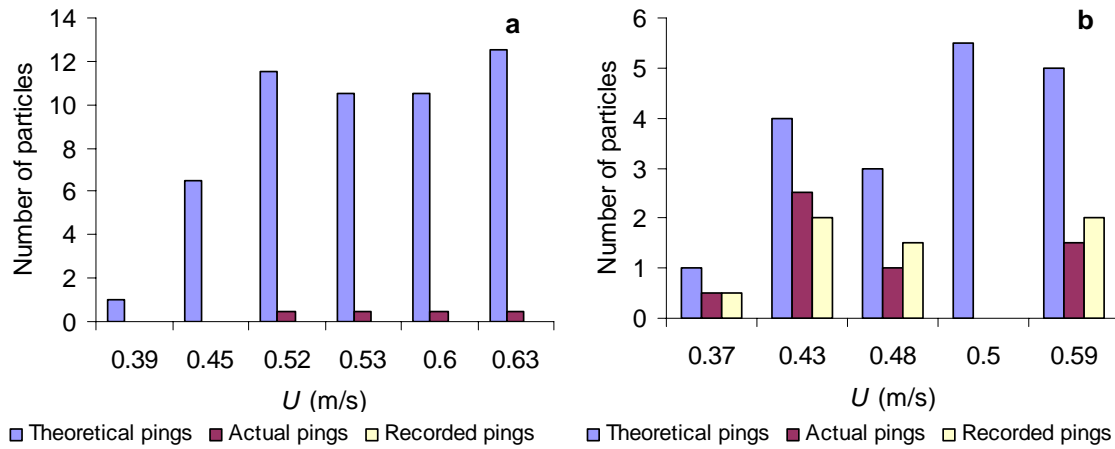


Figure 9 Comparison between theoretical, actual, and recorded pings: a)  $d_i = 15.9$  mm; b)  $d_i = 25.4$  mm

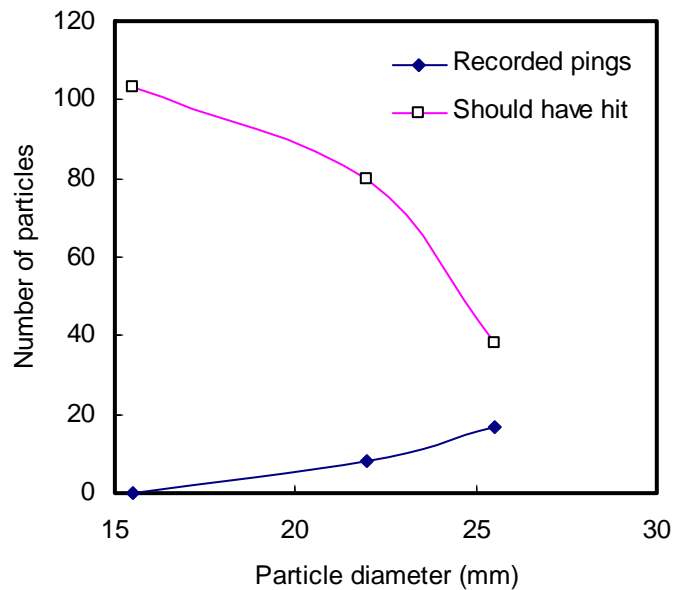


Figure 10 Comparison between theoretical and recorded pings.

## 5. CONCLUSIONS

The development of the GTS is a necessary step to better understand sediment transport in gravel bed channels, especially for low flow conditions. Its ability to make unattended local measurements, record data over long periods of time, capture the larger size fractions, and the ease of instrument movement are all advantages that the GTS has over other techniques.

Testing on the prototype model showed that the ability of the GTS to make accurate measurements increases as particle size increases. The presence of the cylinder in the flow can have a large effect on the smaller sized particles and cause them to follow the streamlines around the cylinder rather than impacting it. Further testing should be conducted to find particle velocity under varying flow conditions and relate its momentum to the detection rate of the GTS. The prototype GTS is only in its first stages. Further development of the GTS will allow for a correlation between the momentum of a particle and the acoustic output signal. This will allow the GTS to record particle momentum to account for non-uniformity in the bed material.

The developed particle velocity equations have great potential for bedload applications and the instantaneous particle velocity equation can be used to calibrate the GTS. Also, the virtual velocity relation can be used to develop a bedload transport equation. The study showed that the virtual velocity is a function of more than just an excess shear term. The size of the entrained particle versus the size of the bed is a key factor in the resting period that affects the overall movement of a particle. Future work on the virtual velocity and the excess shear correction is warranted.

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