



The cost of toxin production in phytoplankton: the case of PST producing dinoflagellates

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1 **Title of the paper: The cost of toxin production in phytoplankton: the case of**
2 **PST producing dinoflagellates**

3 **Running title: Cost of toxin production**

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19 **Abstract**

20 Many species of phytoplankton produce toxins that may provide protection from
21 grazing. In that case one would expect toxin production to be costly; else all species
22 would evolve toxicity. However, experiments have consistently failed to show any
23 costs. Here, we show that costs of toxin production are environment dependent but
24 can be high. We develop a fitness optimization model to estimate rate, costs, and
25 benefits of toxin production, using PST (paralytic shellfish toxin) producing
26 dinoflagellates as an example. Costs include energy and material (nitrogen) costs
27 estimated from well-established biochemistry of PSTs, and benefits are estimated
28 from relationship between toxin content and grazing mortality. The model reproduces
29 all known features of PST production: inducibility in the presence of grazer cues, low
30 toxicity of nitrogen-starved cells, but high toxicity of P- and light-limited cells. The
31 model predicts negligible reduction in cell division rate in nitrogen replete cells,
32 consistent with observations, but >20% reduction when nitrogen is limiting and
33 abundance of grazers high. Such situation is characteristic of coastal and oceanic
34 waters during summer when blooms of toxic algae typically develop. The investment
35 in defense is warranted, since the net growth rate is always higher in defended than in
36 undefended cells.

37 **Key words**

38 Defense; Trade-off; Environment-dependent cost

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42 **Introduction**

43 Many phytoplankton species produce substances that are toxic to humans, hence we
44 consider such phytoplankton ‘toxic algae’, but the evolution and functional role of
45 these secondary metabolites remain unclear. They may be released into the
46 environment and have allelochemical effects to combat competitors [1, 2] or grazers
47 [3], they may be mainly intracellular and have toxic and/or deterrent effects on
48 grazers [4, 5], or in mixotrophic species they may have offensive roles, functioning as
49 a venom towards prey [6–8]. Some toxic algae may also form dense blooms,
50 potentially promoted by their toxicity and consequent grazer deterrent effects, and a
51 defensive role of toxin production is thus often assumed [4, 9]. This interpretation is
52 supported by the observations that algal toxins often have a deterrent rather than a
53 toxic effect on grazers [10–15], and that toxin production may be upregulated in the
54 presence of grazers or their cues, as demonstrated in dinoflagellates, *Alexandrium*
55 spp. [13, 16, 17], and in diatoms, *Pseudo-nitzschia* spp. [18]. The latter observation
56 also suggests that toxin production comes at a cost – why else regulate the production
57 in response to the need? Optimal defense theory, well founded in terrestrial plant
58 ecology, predicts that inducibility of defense should evolve only when the defense is
59 costly and variable in time [19]. However, experiments have generally been unable to
60 demonstrate such costs in toxic phytoplankton, and the growth rates of grazer-induced
61 and un-induced cells, or of toxic and nontoxic strains of the same phytoplankton
62 species appear to be similar [3, 13, 16, 18], and model exercises have similarly
63 suggested costs to be trivial [20]. However, if defense via toxin production is both
64 effective and costless, one would expect most phytoplankton to be toxic, which is far
65 from being the case [19]. Also, the promotion of phytoplankton diversity in the ocean
66 due to grazing and consequent evolution of defense mechanisms, as demonstrated in

67 both theoretical models and considerations [21–23] and whole-community
68 experiments [24], functions only if the defense comes at a cost.

69 One of the most studied groups of toxic phytoplankton is the dinoflagellate
70 *Alexandrium* spp. since the toxins it produces, Paralytic Shellfish Toxins (PSTs), have
71 serious effects on humans. The main potential grazers of dinoflagellates are copepods.
72 While the toxin production may be induced by grazer (copepod) cues [13], the
73 production also depends on the nutrient status of the algae. Specifically, when
74 nitrogen or carbon (light) is limiting the PST production is reduced, while nutrient
75 balanced or P-limited cells may produce PSTs at a high rate (growth of P-limited cells
76 decreases while the production of toxins continues) [25, 26]. PSTs contain large
77 amounts of nitrogen, and so this dependency suggests that the costs of PST
78 production only become obvious when N or light is limiting, and may become
79 manifest either as a reduction in growth rate because part of the assimilated N goes
80 towards PST production; or as a cessation of the production of PSTs in favor of a
81 higher growth rate with a consequent loss of the defense; or a combination of the two.

82 Here, we explore by means of a simple resource allocation model the costs of
83 chemical defense in phytoplankton, using PST producing dinoflagellate *Alexandrium*
84 spp. as an example. We consider both energy and material costs of PST production,
85 their dependency on environmental conditions, and the reduction in mortality that is
86 achieved by the defense investments. Through fitness optimization we demonstrate
87 that costs can be substantial, leading to > 20% reduction in cell division rate, when
88 grazer abundance is high and nitrogen availability is low. We also examine the
89 conditions under which the production of toxins provides maximum benefit to the
90 toxin producing species.

91 **Model description:**

92 The model is based on a resource allocation optimization model modified from Berge
93 *et al.* [27]. The division rate of phytoplankton depends on the acquisition of three
94 resources, viz. carbon (via photosynthesis), nitrogen (as nitrate), and phosphorous (as
95 phosphate), as well as on metabolic expenses. The cells may invest some of their
96 assimilated nitrogen into toxin production and combust some of their fixed organic
97 carbon to cover costs of toxin synthesis, and in return experience reduced grazing
98 mortality. We search for the investment that maximizes the fitness of the cells,
99 defined as the difference between cell division rate and mortality rate (= net growth
100 rate). We use the model to explore the dependency of division rate, net growth rate,
101 and toxicity on the environmental resource availability and predation risk.

102 Uptake of carbon, nitrogen and phosphorous to the cell is described by the symbol J_i
103 (mass flows i being carbon via light-dependent photosynthesis (C), nitrogen (N) or
104 phosphorous (P) in units of μg per day; see Table 1 for central symbols and
105 parameters), and are combined to synthesize new biomass (Fig. 1). Respiratory costs,
106 R_C (units of μg C per day), include costs of biomass synthesis (incl. transport) and
107 maintenance of the structure. Toxin is produced at a rate, T_r , and implies an additional
108 respiratory cost, R_T . Biomass synthesis rate, J_{tot} , is constrained by the stoichiometric
109 balance between carbon, nitrogen and phosphorous. Finally, we assume that toxins
110 and structure have constant but different stoichiometry.

111 *Uptake of carbon, nitrogen, and phosphorous*

112 The potential uptake J_i of resource i (C, N, P) is governed by a standard saturating
113 functional response:

$$J_i = M_i \frac{A_i Y_i}{A_i Y_i + M_i}, (1)$$

114 where A_i is the affinity for resource i , Y_i resource concentration ($\mu\text{g L}^{-1}$), and M_i is
 115 the maximum uptake rate.

116 *Costs*

117 Respiratory costs include costs of both uptake and mobilization of resources for
 118 synthesis through each pathway, and the maintenance of the structure. This metabolic
 119 cost is assumed to be 30% of the total carbon budget [28] plus a constant basal
 120 respiration (R_0) independent of J_C , i.e.,

$$R_C = 0.3J_C + R_0. (2)$$

121 *Rate and cost of toxin production*

122 Let θ be the fraction of nitrogen uptake that a toxic phytoplankton cell devotes to
 123 toxin production. Then the potential rate of toxin production is (units of $\mu\text{g N d}^{-1}$):

$$124 \quad T_{pot}(\theta) = \theta J_N. \quad (3)$$

125 As the toxin production needs carbon both for building the toxin molecules and to
 126 fuel the respiratory costs of toxin production, the actual toxin production rate may be
 127 limited by the available carbon to:

$$128 \quad T_r(\theta) = \min[T_{pot}(\theta), (J_C - R_C)/(n_T + r_T)], (4)$$

129 where n_T is the mass of carbon need per mass of nitrogen in the toxin, and r_T is the
 130 respiratory cost per nitrogen synthesized into toxins (units of g C (g N)^{-1}).

131 The total cost of toxin production in terms of carbon then becomes ($\mu\text{g C d}^{-1}$):

132
$$R_T(\theta) = (n_T + r_T)T_r(\theta). \quad (5)$$

133 *Synthesis and growth rate*

134 The assimilated carbon, nitrogen and phosphorous are combined to synthesize new
135 structure. We assume constant C:N mass ratio, Q_{CN} (units of $\mu\text{g C } (\mu\text{g N})^{-1}$) and C:P
136 mass ratio, Q_{CP} (units of $\mu\text{g C } (\mu\text{g P})^{-1}$) of the cell. The total available carbon for
137 growth is then $J_C - R_C - R_T$ where J_C represents the total uptake of carbon through
138 photosynthesis, and R_C and R_T represent the costs of maintenance and biomass
139 synthesis, and costs of toxin production, respectively. The carbon required to
140 synthesize biomass from nutrients is $Q_{CN}(J_N - T_r)$ and $Q_{CP}J_P$ for nitrate and
141 phosphate, respectively. The growth rate is constrained by the limiting resource
142 (Liebig's law of the minimum) such that the total flux of carbon (and nutrients)
143 available for growth J_{tot} is:

$$J_{\text{tot}}(\theta) = \min[J_C - R_C - R_T(\theta), Q_{CN}(J_N - T_r(\theta)), Q_{CP}J_P]. \quad (6)$$

144 Synthesis is not explicitly limited by a maximum synthesis capacity; limitation of
145 synthesis is taken care of by the limitation of uptake of carbon, nitrogen and
146 phosphorous in the functional responses (Eq. 1). The division rate μ of the cells (d^{-1})
147 is the total flux of carbon divided by the carbon mass of the cell (w_X):

148
$$\mu(\theta) = J_{\text{tot}}(\theta)/w_X. \quad (7)$$

149 Further subtracting the predation mortality (m_p) yields the net growth rate (r):

150
$$r(\theta) = \mu(\theta) - m_p(\theta). \quad (8)$$

151 We assume that predation mortality increases linearly with zooplankton biomass (Z),
152 and due to the toxin production, zooplankton reduces its grazing pressure on toxic
153 cells exponentially as:

$$154 \quad m_p(\theta) = m_{p,0} Z e^{-\beta T(\theta)}, \quad (9)$$

155 where $m_{p,0}$ is a mortality constant, T is the cellular toxin content ($\mu\text{g N cell}^{-1}$)
156 estimated as the toxin production rate divided by the cell division rate ($= T_r/\mu$), and
157 β represents the strength of toxic effect.

158 The resulting population growth rate, $r(\theta)$, is a measure of the fitness of the
159 phytoplankton and we assume that the cell has the ability to optimize its growth rate
160 by regulating its resource allocation to toxin production such that it maximizes its
161 fitness. The optimal proportion of assimilated N devoted to toxin production then
162 becomes:

$$163 \quad \theta^* = \operatorname{argmax}_{\theta} \{r(\theta)\}. \quad (10)$$

164 **Model parameterization**

165 Calibration of parameters is based on laboratory measurements on the dinoflagellates
166 *Alexandrium minutum* and *A. tamarense* as the toxic species, and the copepods
167 *Acartia clausi* and *A. tonsa* as the grazer zooplankton. To calibrate the basic grazing
168 parameters, we use data for non-toxic strains of *A. minutum*.

169 *Parameters related to phytoplankton division rate (μ):*

170 We use experimental observations reported in the literature for cell division rate (μ)
171 of *A. minutum* as a function of light intensity (L) and nutrient concentrations (N and

172 P) to estimate parameter values for maximum uptake rates (M_i) and affinities (A_i)
173 (Fig. 2a-c). While calibrating these parameters a non-toxic strain of *A. minutum* was
174 considered, and as a result, no cost is deducted. For calibration, we adjust the
175 parameters manually to fit the curves with data and keep them close to the existing
176 values of the parameters from other studies (when available). Due to Liebig's
177 minimum law for synthesis (eq. 6), the synthesis is limited by one of the resources
178 (either C or N) and further growth cannot materialize in spite of the availability of
179 other non-limiting resource. As a result, growth cannot increase any further.

180 We use a constant value $1.07 \times 10^{-4} \mu\text{g C d}^{-1}$ for the basal respiration rate (R_0) taken
181 from the range reported in Frangoulis *et al.* [29].

182 *Parameters related to the cost of toxin production:*

183 To estimate the two parameters related to the cost of toxin production (n_T , r_T), we
184 consider the stoichiometry of PSTs and the biochemistry of PST synthesis. PSTs
185 produced by *Alexandrium* spp. (and other organisms) consist of saxitoxin and
186 multiple derivatives; they are cyclic nitrogenous compounds that are synthesized from
187 amino acid precursors. Here we consider the synthesis of saxitoxin, one of the
188 dominating toxins, from the amino acid glutamate via arginine to estimate the
189 approximate costs of toxin production. The costs are two-fold; i.e. the metabolic cost
190 of biosynthesis, r_T , and the cost in terms of material invested in the toxin, n_T .

191 *Material investment (n_T):* The molecular formula of saxitoxin is $\text{C}_{10}\text{H}_{17}\text{N}_7\text{O}_4$, that is
192 10 moles of carbon per 7 moles of nitrogen, or $n_T = (10 \times 12) / (7 \times 14) = 1.23 \mu\text{g C} (\mu\text{g}$
193 $\text{N})^{-1}$.

194 *Metabolic expenses* (r_T): Saxitoxin is synthesized from arginine [30], which in turn is
195 typically synthesized from glutamate that in phytoplankton has to be synthesized *de*
196 *novo*. The metabolic cost of converting glutamate to arginine is 12 mol ATP per mol
197 of arginine, and the synthesis of arginine precursors (i.e. glutamate and carbamoyl-P)
198 requires another 32 mol of ATP, i.e. a total of 44 mol ATP per mol of arginine [31].
199 We have no estimate of the cost of synthesizing saxitoxin from arginine (e.g.,
200 necessary transcripts and translation to enzymes) as well as costs due to actual or
201 potential autotoxicity (hence we ignore it), but it takes 3 mol of arginine to synthesize
202 one mol of saxitoxin. Therefore, it requires at least 132 mol of ATP to synthesize 1
203 mol of saxitoxin. The respiratory equivalent of ATP synthesis is about 0.235 mol ATP
204 synthesized per liter of oxygen consumed; or about 2 g of organic carbon combusted
205 per mol of ATP synthesized [32]. Thus, 2x132 g of organic carbon is respired per mol
206 of toxin synthesized. With 7x14 g N per mol toxin yields an estimate of $r_T = 2.7 \mu\text{g C}$
207 $(\mu\text{g N})^{-1}$.

208 *Parameters related to zooplankton feeding:*

209 The parameters related to reduction in feeding on toxic cell (β) was calibrated from
210 Teegarden & Cembella [12] who quantified the feeding rate on a toxic strain of *A.*
211 *minutum* by *A. tonsa* as a function of cellular toxin content ($\mu\text{g N cell}^{-1}$). We fit Eq. 9
212 to the experimental data to estimate β (Fig. 2d). We use $8.95 \times 10^{-4} \mu\text{g C}$ as the
213 cellular carbon content of *A. minutum* [28], and chose the value of the mortality
214 constant ($m_{p,0}$) as $0.008 \text{ L } (\mu\text{g C})^{-1} \text{ d}^{-1}$ based on the clearance rate of *A. tonsa* [34].

215

216 **Results**

217 *Optimal allocation strategy*

218 The optimal allocation of nitrogen to toxin production is the one that yields the
219 highest population growth rate (Fig. 3). The optimal allocation of N to toxin
220 production increases with decreasing environmental nitrogen availability and
221 increasing concentration of zooplankton (Fig. 3). As a result, the investment in
222 defense - toxin production - in toxic dinoflagellates varies with both N-availability
223 and grazing pressure, with implications to cell division rate, grazing mortality rate,
224 and population growth rate (Fig. 4, Fig. 5, Fig. 6 and Fig. 7).

225 *Toxin production, grazing mortality, and cost of defense*

226 At high N concentrations, the cells produce toxin whenever zooplankton is present but
227 production ceases in the absence of grazers (Fig. 4a). Note that for simplicity we
228 assume that toxin production rate becomes zero when there is no grazer. In contrast,
229 at low N, phytoplankton produce toxins only when zooplankton biomass exceeds a
230 threshold concentration, and the cellular toxin content increases with the biomass of
231 the zooplankton (Fig. 4a, 6b).

232 Defended cells experience lower grazing mortality than undefended cells especially
233 when nitrogen availability is high and zooplankton concentration is low (Fig. 4d) as
234 cellular toxin content remains high (Fig. 4a). Taken together the grazing mortality
235 increases with zooplankton density and decreases with availability of nitrogen.

236 The cost of the defense can be quantified as a reduction in the cell division rate of
237 defended relative to undefended cells. This cost is significant only at high
238 zooplankton biomass and/or low nitrogen availability (Fig. 4b, Fig. 5a) and increases
239 with increasing zooplankton biomass and decreasing nitrogen concentration (Fig. 6c,

240 d). At realistically high zooplankton biomass and realistically low nitrogen
241 availability, cell division rate may be reduced by more than 20%. At high nitrogen
242 concentrations, the cells produce toxins from the excess nitrogen (not used for
243 growth) and therefore the costs are, of course, unmeasurably low (Fig. 6d). The net
244 outcome of the defense investment is that defended cells have similar or higher
245 population growth rates (fitness) than undefended cells under all nutrient conditions
246 (Fig. 4c). The absolute enhancement is largest at high N (Fig. 6e) whereas the relative
247 advantage is most pronounced at low N and high zooplankton biomass (Fig. 6f).

248 *Effects of P and light limitation*

249 If phosphate or light rather than nitrogen limit cell growth, N is in excess and the
250 excess N can be allocated to toxin production and the cells consequently become well
251 defended. Figs. 7a and b display the effects of light limitation on toxin production and
252 cellular toxin contents, respectively. There are two regions in this parameter space:
253 the left region where light is limiting and toxin production increases with light
254 intensity while toxin content decreases with light intensity; and the right region,
255 where nitrogen is limiting and both toxin production and cellular toxin content are
256 independent of light intensity. Toxin production and cellular contents similarly vary
257 in the nitrogen-phosphorous parameter space, between phosphorous limitation at low
258 P and nitrogen limitation at high P (Fig. 7c, d). Under all conditions, cellular toxin
259 contents increase with decreasing ambient P.

260 *Sensitivity analysis of β and r_T*

261 Since the parameter β was calibrated based on only four available data points (Figure
262 2d), we perform a sensitivity analysis by varying β , which represents the reduction in

263 zooplankton grazing due to cellular toxin (see supplementary material fig. A1).
264 Overall, the qualitative patterns described above are robust to changes in β . When
265 nitrogen concentrations are high, there is no observable change in cellular toxin
266 concentration with varying β as organisms produce toxins at their maximum rate and
267 consequently division rates remain same. However, due to the increase in predation
268 pressure with decreasing β , population growth rate decreases. On the other hand, with
269 decrease in nitrogen concentrations, organisms produce more toxin with decrease in
270 β , leading to reduction in division rates as well as growth rates.

271 Similarly, varying the parameter r_T , representing the metabolic cost of synthesizing
272 toxin, does not lead to observable changes in the system dynamics (see supplementary
273 material fig. A2).

274 **Discussion**

275 Experiments have demonstrated that PST producing dinoflagellates become less toxic
276 when N-starved, that toxin content is high in exponentially growing cells in N:P
277 balanced environments, and that the cells become most toxic when P-limited [20, 26,
278 35–37]. Light-limited cells also accumulate more toxins [38] and toxin production is
279 enhanced in the presence of grazer cues [13]. Our model qualitatively reproduces all
280 these observations.

281 The model further conforms with the experimental observation that the cost of toxin
282 production, quantified as a reduction in cell division rate of toxin-producing cells
283 compared to cells or strains that produce less or no toxins, is negligible when
284 resources, mainly N and light, are plentiful [3, 13]. However, when light or nitrogen
285 are limiting cell growth, and when grazers are abundant, we predict that the cost of

286 investing in toxin production may be substantial and lead to > 20% reduction in cell
287 division rate. There is evidence for other defense mechanisms in phytoplankton where
288 the cost of the defense only materializes when resources are limiting [39–41].
289 However, the prediction of costs of toxin production still remains to be tested
290 experimentally. The costs of the investment are two-fold: (i) the cells need nitrogen to
291 build toxin molecules, and this requirement compete with the nitrogen investment in
292 cell structure and growth. While the nitrogen requirement for toxin production is
293 small in absolute terms, leading John and Flynn [20] to consider it trivial, it becomes
294 significant when nitrogen is limiting, and may eventually lead to a total shut down of
295 toxin production. (ii) The cells further need energy for the synthesis of toxins, and this
296 energy eventually comes from photosynthesis. This is why toxin production rate
297 increases with light intensity when light is the limiting resource. In this situation, cell
298 division rate increases faster than toxin production rate with increasing light, and
299 therefore cellular toxin content decreases with increasing light, an effect and a
300 mechanism in agreement with experimental observations [38].

301 The environmental conditions that promote cell toxicity, i.e., high grazer biomass,
302 actually coincide with the time of the year when nitrogen is the most limiting resource
303 in temperate shelf regions. Thus, zooplankton (copepod) biomass is at its seasonal
304 maximum during summer and may easily exceed 10-100 $\mu\text{g C L}^{-1}$ [42], which will
305 impose a high predation mortality and thus induce high cell toxicity. At this time of
306 the year, concentrations of inorganic nitrogen in surface waters in temperate shelf
307 regions are low, typically below 1-10 $\mu\text{g N L}^{-1}$ [43, 44], and under these conditions
308 the model predicts that the cost of toxin production is substantial, leading to > 20%
309 decrease in cell division rate. However, the investment in defense pays off since
310 defended cells experience lower grazing mortality, and may consequently have net

311 growth rates up to twice or more of that of undefended cells (e.g. Fig. 6f). If the toxins
312 have deterrent rather than toxic effects, i.e., preventing the toxic cells from being
313 consumed rather than killing grazers that do consume the cells [10, 11, 45], then the
314 toxic cells may have a competitive advantage and a monospecific bloom may
315 develop. Indeed, blooms of toxic algae typically occur during summer [46], which is
316 consistent with these considerations.

317 Furthermore, the toxic species can also gain growth advantage under high nitrogen
318 and high grazer biomass, as growth rates can be doubled due to the benefit provided
319 by toxin production at a negligible production cost (Fig. 6d, f). Such situations are
320 comparable with many coastal areas where N:P ratios remain considerably high due
321 to erratic input of nitrogen from human activities, and can consequently result in toxic
322 blooms [47]. Thus, potentially toxic species can also become toxic when exposed to
323 high N regime caused by eutrophication.

324 The success of toxic bloom formation also depends on the evolutionary history of
325 zooplankton grazer and toxic species [40]. Evidence from both fresh- and marine
326 waters shows that grazers can evolve full or partial resistance against the toxic algae
327 [48, 49]. Our results suggest that cellular toxin content will increase in the presence of
328 toxin-resistant grazers as will the costs (see supplementary material fig. A1).
329 However, if the benefits in terms of reduced grazing mortality vanish due to grazer
330 resistance, the possibility of success of the toxic species in terms of forming bloom
331 will be reduced or disappear.

332 Many phytoplankton species have evolved what is supposed to be defense
333 mechanisms to avoid or reduce predation, ranging from hard shells and spines, to
334 evasive behaviors and toxin production, and such defenses may have significant

335 implications on predator-prey interactions, population dynamics, and diversity of
336 phytoplankton communities [50]. However, the trade-offs are rarely quantified and
337 often not even documented. While there is increasing evidence that toxin-production
338 in many cases provides partial protection from grazing in dinoflagellates, the costs
339 have hitherto not been properly quantified. The currencies of benefits and costs are
340 growth and mortality. Here, we have shown that the costs are not only strongly
341 dependent on the concentration of grazers but also on the resource availability, and
342 that the realized costs in nature are typically highest during summer when the defense
343 is most needed. The delicate balance between costs, benefits, and resource availability
344 not only explains why the defense is inducible but also has implications for the timing
345 of toxic algal blooms. Further studies on costs and benefits of toxin production are
346 needed to experimentally test our model predictions (e.g., toxin production and
347 growth under sufficient and deficient resources), and for deeper understanding of the
348 mechanisms and evolution of inducible toxin production. At present, very little is
349 known about the consequences of inducible toxin production on the community level
350 in complex communities. Future work should be devoted towards investigating the
351 complex integrated ecological issues of inducible toxin production, species diversity,
352 and food web structure.

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357 **Conflict of interest**

358 The authors declare that they have no conflict of interest.

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530 **Table 1.** Central symbols and general parameters. Index i refers to carbon (C) via
 531 light-dependent photosynthesis where light intensity is measured in units of
 532 $\mu\text{E m}^{-2}\text{s}^{-1}$, nitrogen (N) in units of $\mu\text{g N L}^{-1}$ or phosphorous (P) in units of $\mu\text{g P L}^{-1}$.
 533 Calibration of parameters is based on data from laboratory measurements and
 534 provided in the ‘Model parameterization’ section.

Symbol	Description	Value	Unit	Reference
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L	Light flux in the environment	-	$\mu\text{E m}^{-2}\text{s}^{-1}$	-
N	Concentration of nitrogen in the environment	-	$\mu\text{g N L}^{-1}$	-
P	Concentration of phosphorous in the environment	-	$\mu\text{g P L}^{-1}$	-
w_X	Cellular mass of toxic algae	8.95×10^{-4}	$\mu\text{g C}$	[28]
Z	Biomass of zooplankton	-	$\mu\text{g C L}^{-1}$	-
Functional responses				
J_i	Flux of assimilated substance		$\mu\text{g C d}^{-1}, \mu\text{g N d}^{-1}, \text{ or } \mu\text{g P d}^{-1}$	Eq. (1)
A_L	Affinity for light	3.1×10^{-5}	$\mu\text{g C } (\mu\text{E m}^{-2}\text{s}^{-1})^{-1} \text{ d}^{-1}$	Calibrated
A_N	Affinity for nitrogen	3×10^{-6}	L d^{-1}	Calibrated
A_P	Affinity for phosphorous	3×10^{-7}	L d^{-1}	Calibrated
M_L	Max. uptake rate of C through photosynthesis	9.5×10^{-4}	$\mu\text{g C d}^{-1}$	Calibrated
M_N	Max. uptake rate of N	1.1×10^{-4}	$\mu\text{g N d}^{-1}$	Calibrated
M_P	Max. uptake rate of P	1.3×10^{-5}	$\mu\text{g P d}^{-1}$	Calibrated
Costs and toxin production				
R_C	Total metabolic cost	-	$\mu\text{g C d}^{-1}$	Eq. (2)
R_0	Basal respiration rate	1.07×10^{-4}	$\mu\text{g C d}^{-1}$	[29]
θ	Fraction of N devoted to toxin	-	-	Eq. (10)
T_{pot}	Potential toxin production rate	-	$\mu\text{g N d}^{-1}$	Eq. (3)
T_r	Actual toxin production rate	-	$\mu\text{g N d}^{-1}$	Eq. (4)
T	Cellular toxin content	-	$\mu\text{g N cell}^{-1}$	-
R_T	Cost of toxin production	-	$\mu\text{g C d}^{-1}$	Eq. (5)
n_T	Material cost of toxin production	1.23	$\mu\text{g C } (\mu\text{g N})^{-1}$	Calibrated
r_T	Metabolic cost of synthesizing toxin	2.7	$\mu\text{g C } (\mu\text{g N})^{-1}$	Calibrated
Predation				
m_p	Predation mortality	-	d^{-1}	Eq. (9)

$m_{p,0}$	Mortality constant	0.008	$L (\mu\text{g C})^{-1} \text{d}^{-1}$	[34]
β	Reduction in grazing due to toxin	1.147×10^5	$\text{cells } (\mu\text{g N})^{-1}$	Calibrated
Synthesis and growth				
J_{tot}	Total available C flux	-	$\mu\text{g C d}^{-1}$	Eq. (6)
μ	Division rate of algae	-	d^{-1}	Eq. (7)
r	Growth rate of algae	-	d^{-1}	Eq. (8)
Q_{CN}	C:N mass ratio	5.68	$\mu\text{g C } (\mu\text{g N})^{-1}$	[51]
Q_{CP}	C:P mass ratio	41	$\mu\text{g C } (\mu\text{g P})^{-1}$	[51]

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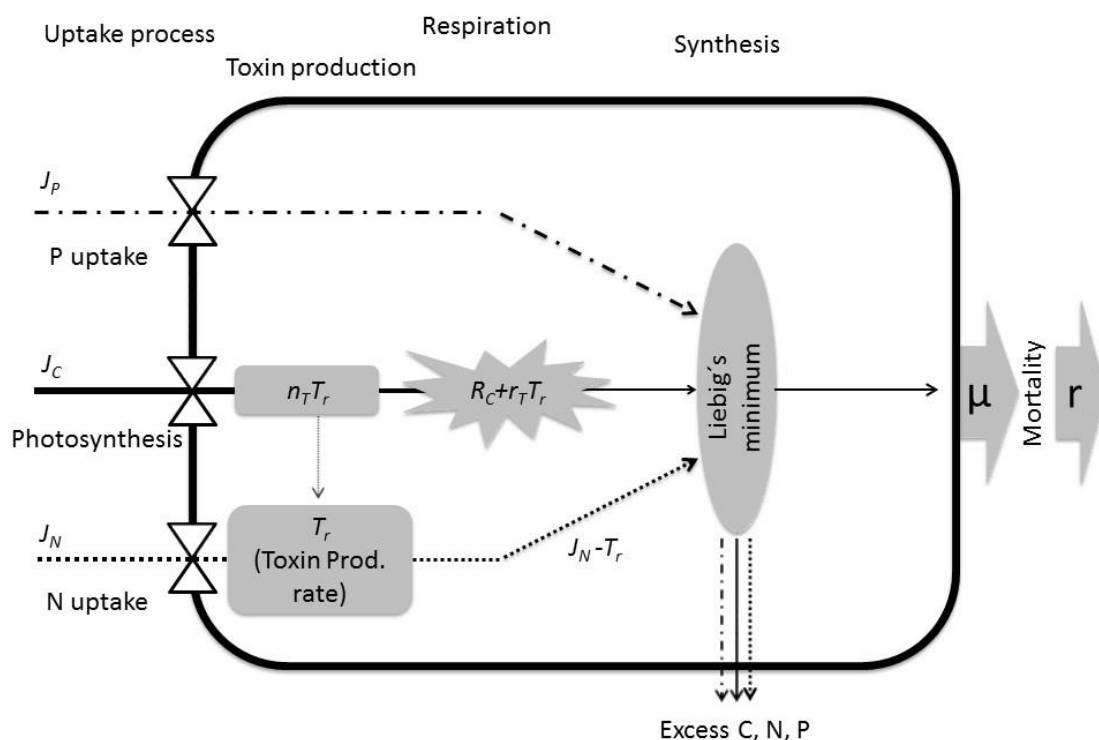
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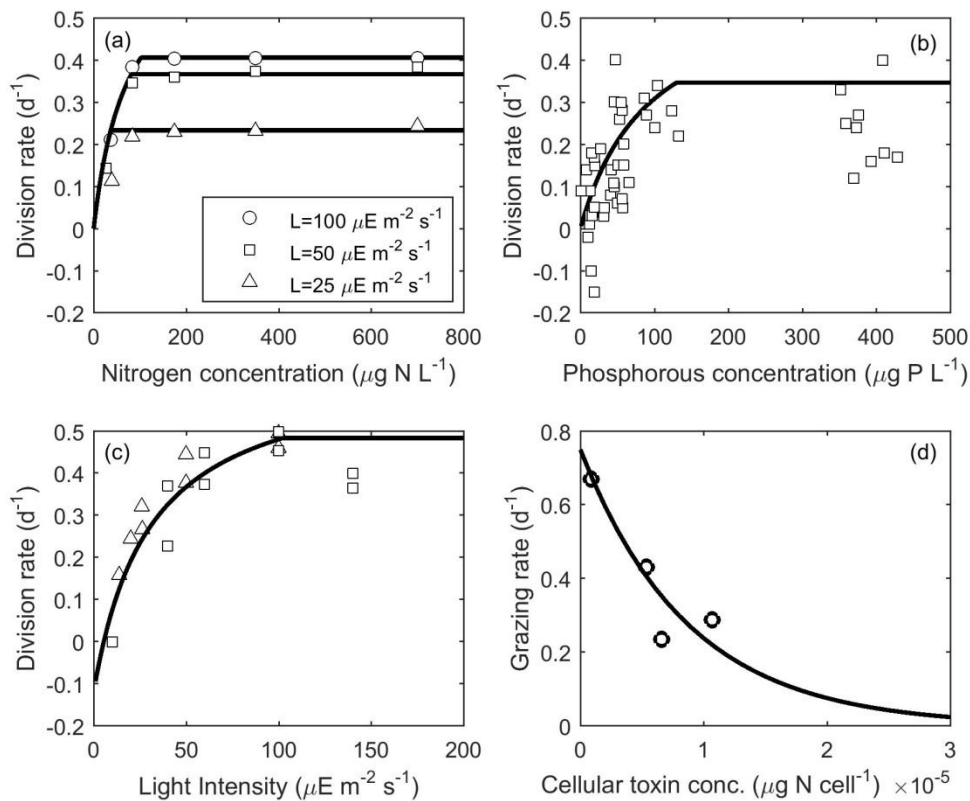
542 **Figures**



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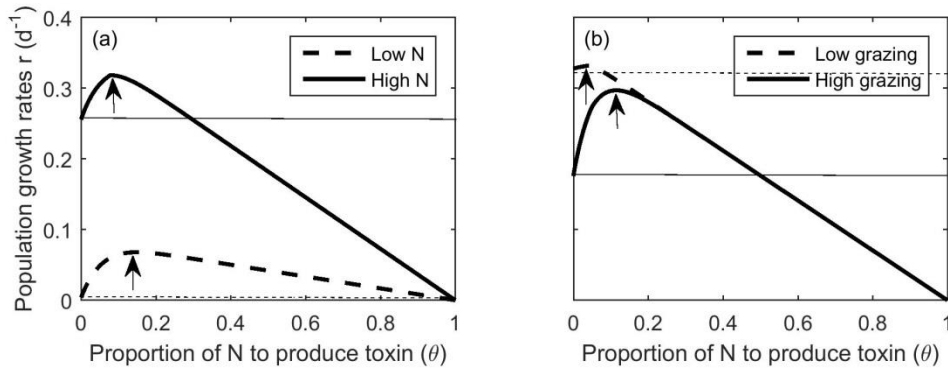
544 **Figure 1.** Schematic representation of the model showing how fluxes of nitrogen
 545 (dotted), carbon (solid) and phosphorous (dash-dot) are lost through respiration (gray
 546 explosion) and toxin production (gray rectangles), and combined (gray ellipse) to
 547 determine growth rate. White triangle symbols represent the functional responses for
 548 the uptake mechanisms. R_C represents the respiratory cost that includes the costs of
 549 both uptake and mobilization of resources for synthesis and the maintenance of
 550 structure. The rate at which toxin is synthesized from C and N is $n_T T_r$, and the
 551 respiratory cost of toxin production is $r_T T_r$ where T_r is the toxin production rate. The
 552 ellipse represents synthesis of biomass from the available C, N and P following
 553 Liebig's law of the minimum and constrained by the Redfield ratio ($\mu\text{g C } (\mu\text{g N})^{-1}$
 554 $=5.68$, $\mu\text{g C } (\mu\text{g P})^{-1}=41$) [51]. In our steady state consideration, the excess amounts
 555 of assimilated C, N or P are assumed lost as excess resources. μ represents the

556 division rate, and r is the population growth rate after subtracting predation mortality
 557 from μ .



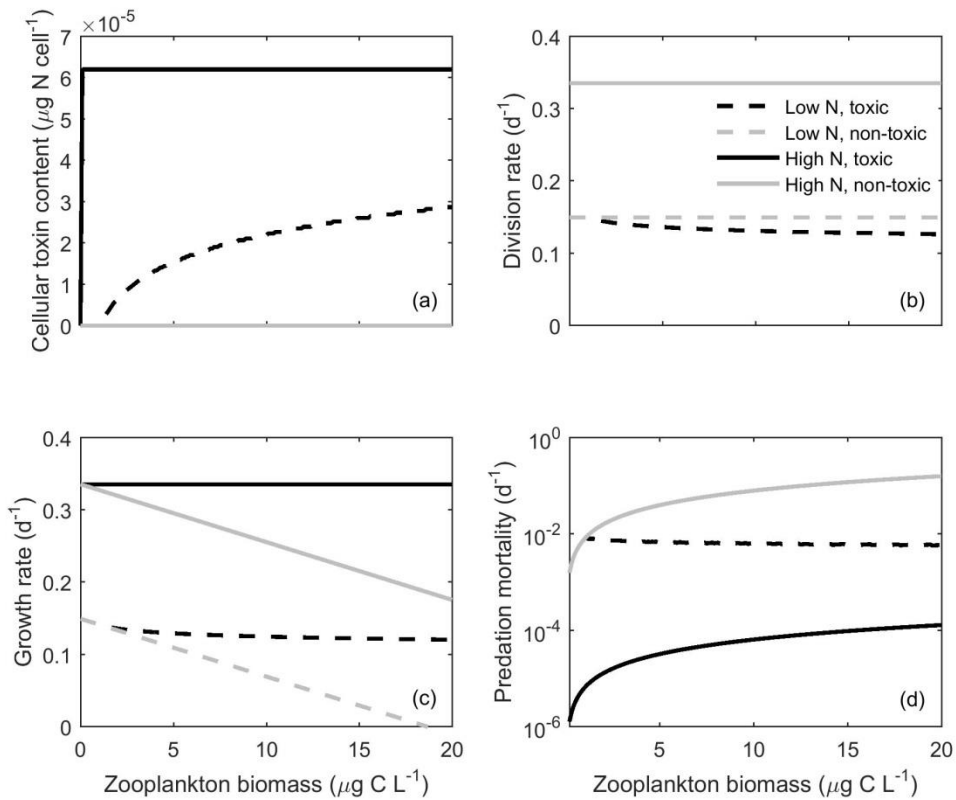
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559 **Figure 2.** Comparison of division rates (μ) between available data and model
 560 outcome with the calibrated parameters by varying (a) nitrogen ($P = 200 \mu\text{g P L}^{-1}$)
 561 (at three different light intensities
 562 $L = 100 \mu\text{E m}^{-2}\text{s}^{-1}, 50 \mu\text{E m}^{-2}\text{s}^{-1}, 25 \mu\text{E m}^{-2}\text{s}^{-1}$) [52], (b) phosphorous ($L =$
 563 $45 \mu\text{E m}^{-2}\text{s}^{-1}, N = 200 \mu\text{g N L}^{-1}$) [53], and (c) light ($N = 6000 \mu\text{g N L}^{-1}, P =$
 564 $400 \mu\text{g P L}^{-1}$) [52, 54]. Grazing rate at different toxin concentrations (d). Data for
 565 grazing on toxic *A. tamarensis* strain CCMP 115 by *A. tonsa* were used [12].



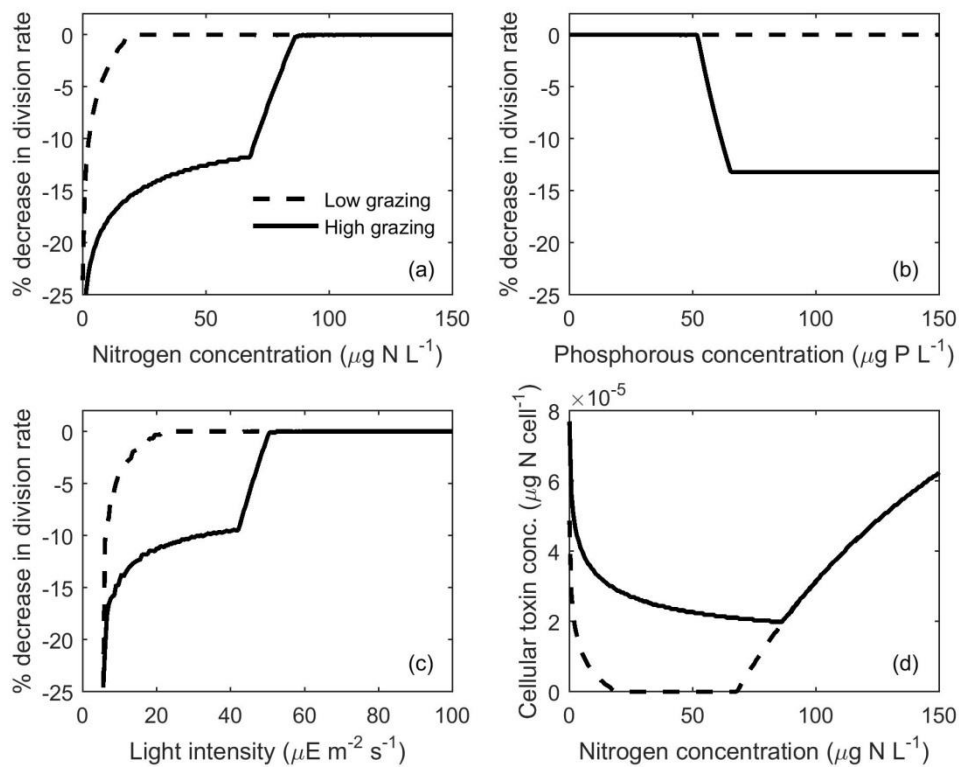
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567 **Figure 3.** Population growth rate as a function of the fraction of assimilated nitrogen
 568 that is allocated to toxin production (a) at low and high environmental concentration
 569 of N ($N=80 \mu\text{g N L}^{-1}$ and $10 \mu\text{g N L}^{-1}$ with concentration of grazer $Z = 10 \mu\text{g C L}^{-1}$),
 570 and (b) at high and low concentration of zooplankton ($Z = 20 \mu\text{g C L}^{-1}$ and
 571 $1 \mu\text{g C L}^{-1}$ with $N = 75 \mu\text{g N L}^{-1}$). The maximum of the curves shows the optimal
 572 allocation strategy (θ^*) (marked by arrows). Thin lines represent growth rates in the
 573 absence of toxin production. Other resources are phosphate (P) = $120 \mu\text{g P L}^{-1}$, light
 574 intensity (L) = $150 \mu\text{E m}^{-2}\text{s}^{-1}$, and phytoplankton biomass (X) = $90 \mu\text{g C L}^{-1}$.



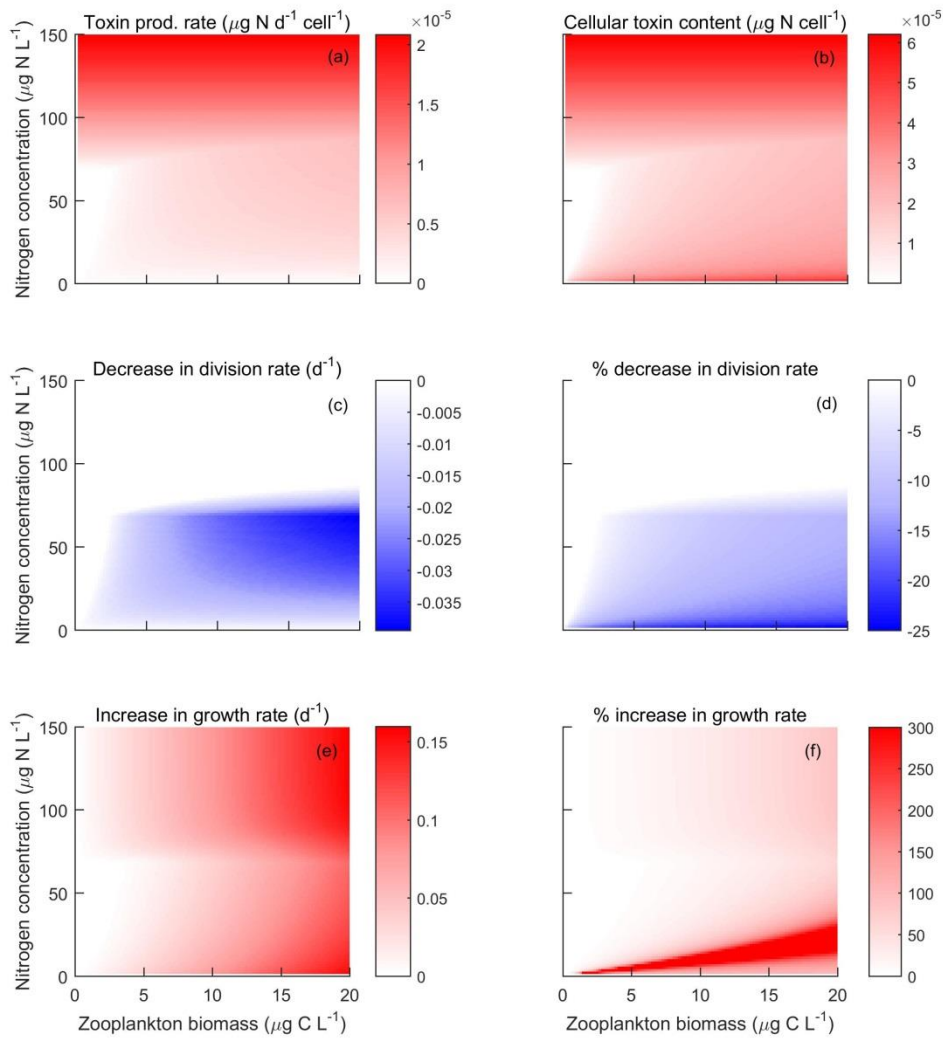
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576 **Figure 4.** Optimal cellular toxin content (a), cell division rate (b), population growth
 577 rate (c), and predation mortality (d) as a function zooplankton biomass at low ($N=20$
 578 $\mu\text{g N L}^{-1}$) and high ($N=150 \mu\text{g N L}^{-1}$) N concentrations of defended (toxin producing)
 579 and undefended cells (non-toxic strain). Curves of division rates for defended and
 580 undefended cells under high N concentration lie on top of each other. Light intensity
 581 $L = 150 \mu\text{E m}^{-2}\text{s}^{-1}$ and phosphorous concentration $P = 120 \mu\text{g P L}^{-1}$ in all plots.



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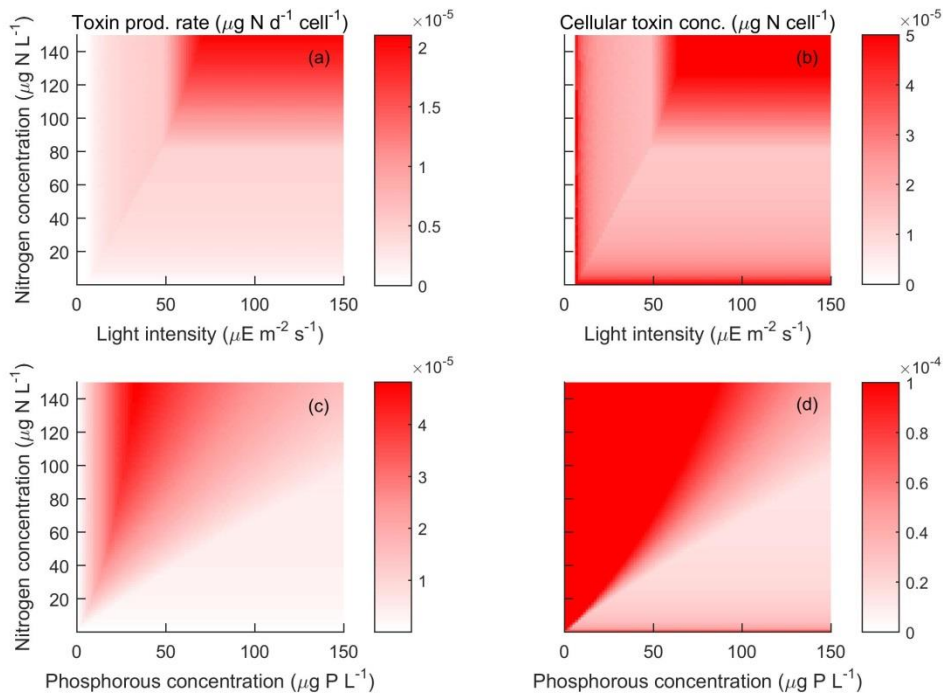
583 **Figure 5.** Relative reduction in cell division rate as a function of nitrogen
 584 concentration ($L=150 \mu\text{E m}^{-2}\text{s}^{-1}$, $P=120 \mu\text{g P L}^{-1}$) (a), phosphorous concentration
 585 ($L=150 \mu\text{E m}^{-2}\text{s}^{-1}$, $N=40 \mu\text{g N L}^{-1}$) (b), and light intensities ($N=120 \mu\text{g N L}^{-1}$,
 586 $P=120 \mu\text{g P L}^{-1}$) (c) at high ($Z=20 \mu\text{g C L}^{-1}$) and low ($Z=1 \mu\text{g C L}^{-1}$) zooplankton
 587 biomasses. Cellular toxin content as a function of N at high and low zooplankton
 588 biomasses (d).



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590 **Figure 6.** Surface plots of toxin production rate (a), and cellular toxin content (b), as
 591 well as absolute and relative changes in cell division rate ($\mu(\theta^*) - \mu(\theta = 0)$) and
 592 $(\mu(\theta^*) - \mu(\theta = 0)) \times 100 / \mu(\theta = 0)$ (c, d), and population growth rates
 593 $(g(\theta^*) - g(\theta = 0))$ and $(g(\theta^*) - g(\theta = 0)) \times 100 / g(\theta = 0)$ (e, f) of defended relative
 594 to undefended cells as a function of N-availability and zooplankton biomass. Light
 595 intensity $L = 150 \mu\text{E m}^{-2}\text{s}^{-1}$ and phosphorous concentration $P = 120 \mu\text{g P L}^{-1}$ in
 596 all plots.

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599 **Figure 7.** Surface plots of toxin production rate (a), and cellular toxin content (b) as a
 600 function of N-availability and light intensity. Zooplankton biomasses $Z=10 \mu\text{g C L}^{-1}$,
 601 and phosphorous concentration $P=120 \mu\text{g P L}^{-1}$ in both plots. Surface plots of toxin
 602 production rate (c), and cellular toxin content (d) as a function of N and P-availability.
 603 Zooplankton biomasses $Z=10 \mu\text{g C L}^{-1}$, and light intensity $L=150 \mu\text{E m}^{-2} \text{s}^{-1}$ in both
 604 plots.

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611 **Supplementary material**

612 **Appendix A. Sensitivity analysis**

613 Fig. A1 shows the color plot with continuous variations in both N concentration and
614 the benefit from toxin production (β). The toxin production rate is high when the
615 benefit from toxin production remains within certain range. However, it decreases at
616 very high benefit range as organisms receive large benefit by producing small amount
617 of toxin (Fig. A1b). As a result, benefits of toxin production in terms of population
618 growth rate remains high when benefits are high and also N concentration is high.

619 Fig. A2 shows the color plot with continuous variations in both N concentration and
620 the metabolic cost of synthesizing toxin (r_T). When the cost is relatively low, an
621 increase in N concentration increases toxin production (Fig A2b), as organisms get
622 more benefit from toxin production rather than increasing division rate. However,
623 when the toxin production is costly and N is sufficient in the system, organisms invest
624 their energy in increasing division rate rather than production of costly toxin.
625 Although, since low N does not support high growth, organisms produce toxin to
626 increase their population growth rate in spite of their high cost.

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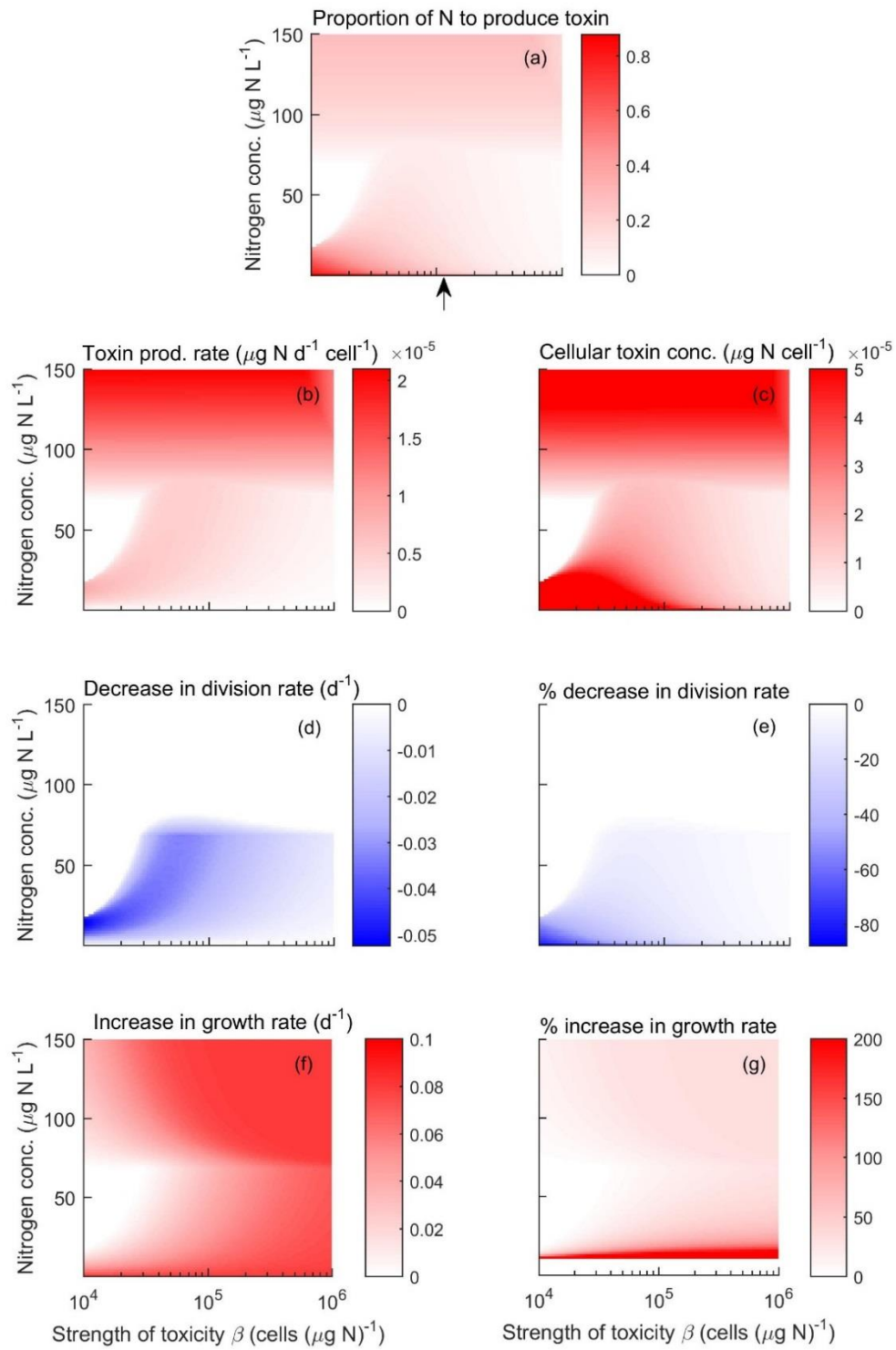
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635 **Figure legends**

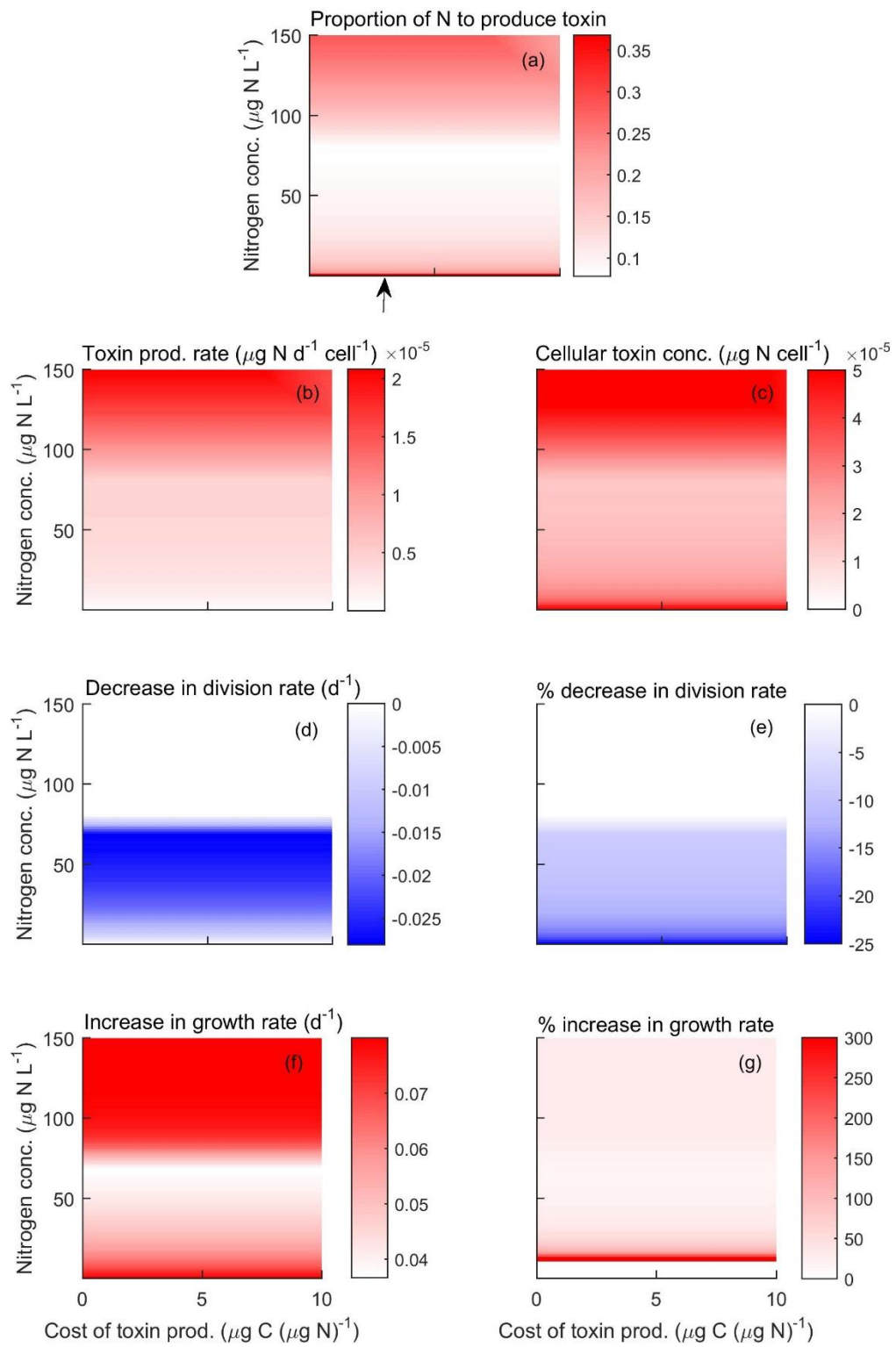
636 **Figure A1.** Surface plots of optimal allocation of N to toxin production (a), toxin
637 production rate (b), and cellular toxin content (c), as well as absolute and relative
638 changes in cell division rate ($(\mu(\theta^*) - \mu(\theta = 0))$ and $(\mu(\theta^*) - \mu(\theta = 0)) \times 100 / \mu(\theta =$
639 $0))$) (d, e), and population growth rates ($(g(\theta^*) - g(\theta = 0))$ and $(g(\theta^*) - g(\theta =$
640 $0)) \times 100 / g(\theta = 0))$) (f, g) of defended relative to undefended cells as a function of N-
641 availability and the strength of toxicity (β). The position of arrow indicates the value
642 of β used for other figures. The phytoplankton biomasses $X=90 \mu\text{g C L}^{-1}$,
643 zooplankton biomasses $Z=10 \mu\text{g C L}^{-1}$, light intensity $L=150 \mu\text{E m}^{-2}\text{s}^{-1}$, and
644 phosphorous concentration $P=120 \mu\text{g P L}^{-1}$ in all plots.

645 **Figure A2.** Surface plots of optimal allocation of N to toxin production (a), toxin
646 production rate (b), and cellular toxin content (c) as well as absolute and relative
647 changes in cell division rate ($(\mu(\theta^*) - \mu(\theta = 0))$ and $(\mu(\theta^*) - \mu(\theta = 0)) \times 100 / \mu(\theta =$
648 $0))$) (d, e) and population growth rates ($(g(\theta^*) - g(\theta = 0))$ and $(g(\theta^*) - g(\theta =$
649 $0)) \times 100 / g(\theta = 0))$) (f, g) of defended relative to undefended cells as a function of N-
650 availability and the cost of toxin production (r_T). The position of arrow indicates the
651 value of r_T used for other figures. The phytoplankton biomasses $X=90 \mu\text{g C L}^{-1}$,
652 zooplankton biomasses $Z=10 \mu\text{g C L}^{-1}$, light intensity $L=150 \mu\text{E m}^{-2}\text{s}^{-1}$, and
653 phosphorous concentration $P=120 \mu\text{g P L}^{-1}$ in all plots.



654

655 Figure A1



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657 Figure A2

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