# Kent Academic Repository Full text document (pdf)

### **Citation for published version**

Orlandi, Fabio and Aza, Eleni and Bakaimi, Ioanna and Kiefer, Klaus and Klemke, Bastian and Zorko, Andrej and Ar on, Denis and Stock, Christopher and Tsibidis, George D. and Green, M.A. and Manuel, Pascal and Lappas, Alexandros (2018) Incommensurate atomic and magnetic modulations in the spin-frustrated -NaMnO2 triangular lattice. Physical Review Materials, 2 (7). 074407.

# DOI

https://doi.org/10.1103/PhysRevMaterials.2.074407

# Link to record in KAR

http://kar.kent.ac.uk/67281/

# **Document Version**

Author's Accepted Manuscript

### Copyright & reuse

Content in the Kent Academic Repository is made available for research purposes. Unless otherwise stated all content is protected by copyright and in the absence of an open licence (eg Creative Commons), permissions for further reuse of content should be sought from the publisher, author or other copyright holder.

### Versions of research

The version in the Kent Academic Repository may differ from the final published version. Users are advised to check http://kar.kent.ac.uk for the status of the paper. Users should always cite the published version of record.

### Enquiries

For any further enquiries regarding the licence status of this document, please contact: **researchsupport@kent.ac.uk** 

If you believe this document infringes copyright then please contact the KAR admin team with the take-down information provided at http://kar.kent.ac.uk/contact.html





#### PHYSICAL REVIEW MATERIALS 00, 004400 (2018)

Incommensurate atomic and magnetic modulations in the spin-frustrated  $\beta$ -NaMnO<sub>2</sub> 2 triangular lattice З Fabio Orlandi,<sup>1</sup> Eleni Aza,<sup>2,3</sup> Ioanna Bakaimi,<sup>2,\*</sup> Klaus Kiefer,<sup>4</sup> Bastian Klemke,<sup>4</sup> Andrej Zorko,<sup>5</sup> Denis Arčon,<sup>5,6</sup> 4 Christopher Stock,<sup>7</sup> George D. Tsibidis,<sup>2</sup> Mark A. Green,<sup>8</sup> Pascal Manuel,<sup>1</sup> and Alexandros Lappas<sup>2,†</sup> 5 <sup>1</sup>ISIS Facility, Rutherford Appleton Laboratory, Harwell Oxford, Didcot OX11 0QX, United Kingdom 6 <sup>2</sup>Institute of Electronic Structure and Laser, Foundation for Research and Technology–Hellas, Vassilika Vouton, 71110 Heraklion, Greece 7 <sup>3</sup>Department of Materials Science and Engineering, University of Ioannina, 451 10 Ioannina, Greece 8 <sup>4</sup>Department Sample Environment and CoreLab Quantum Materials, Helmholtz-Zentrum Berlin für Materialien und Energie GmbH, g D-14109 Berlin, Germany 10 <sup>5</sup>Jozef Stefan Institute, Jamova c. 39, 1000 Ljubljana, Slovenia 11 <sup>6</sup>Faculty of Mathematics and Physics, University of Ljubljana, Jadranska c. 19, 1000 Ljubljana, Slovenia 12  $^{7}$ School of Physics and Astronomy, University of Edinburgh, Edinburgh EH9 3JZ, United Kingdom 13 <sup>8</sup>School of Physical Sciences, University of Kent Canterbury, Kent CT2 7NH, United Kingdom 14 (Received 1 April 2018; published xxxxx) 16 The layered  $\beta$ -NaMnO<sub>2</sub>, a promising Na-ion energy-storage material, has been investigated for its triangular 17 lattice capability to promote complex magnetic configurations that may release symmetry restrictions for the 18 coexistence of ferroelectric and magnetic orders. The complexity of the neutron powder diffraction patterns 19 underlines that the routinely adopted commensurate structural models are inadequate. Instead, a single-phase 20 superspace symmetry description is necessary, demonstrating that the material crystallizes in a compositionally 21 modulated  $\mathbf{q} = (0.077(1), 0, 0)$  structure. Here Mn<sup>3+</sup> Jahn-Teller distorted MnO<sub>6</sub> octahedra form corrugated 22 layer stacking sequences of the  $\beta$ -NaMnO<sub>2</sub> type, which are interrupted by flat sheets of the  $\alpha$ -like oxygen 23 topology. Spontaneous long-range collinear antiferromagnetic order, defined by the propagation vector  $\mathbf{k} =$ 24 (1/2, 1/2, 1/2), appears below  $T_{\rm N1} = 200$  K. Moreover, a second transition into a spatially modulated proper-25 screw magnetic state ( $\mathbf{k} \pm \mathbf{q}$ ) is established at  $T_{N2} = 95$  K, with an antiferromagnetic order parameter resembling 26 that of a two-dimensional (2D) system. The evolution of <sup>23</sup>Na NMR spin-lattice relaxation identifies a magnetically 27 inhomogeneous state in the intermediate T region ( $T_{N2} < T < T_{N1}$ ), while its strong suppression below  $T_{N2}$ 28 indicates that a spin gap opens in the excitation spectrum. High-resolution neutron inelastic scattering confirms that 29 the magnetic dynamics are indeed gapped ( $\Delta \sim 5 \text{ meV}$ ) in the low-temperature magnetic phase, while simulations 30 on the basis of the single-mode approximation suggest that Mn spins residing on adjacent antiferromagnetic 31 chains, establish sizable 2D correlations. Our analysis points out that novel structural degrees of freedom promote 32 cooperative magnetism and emerging dielectric properties in this nonperovskite type of manganite. 33

DOI: 10.1103/PhysRevMaterials.00.004400

34

35

#### I. INTRODUCTION

Devising cost-efficient chemical routes for multiferroic 36 magnetoelectric compounds that foster coupling between spins 37 and other electron degrees of freedom is a fascinating problem 38 of both fundamental and technological interest [1]. Engineer-39 ing the materials' structure to accommodate unusual coordi-40 nations of interacting neighbors offers one such viable but 41 challenging avenue. The perturbation of exchange interactions 42 that emerge from competition due to magnetic frustration [2-4] 43 can select complex spin arrangements that release symmetry 44 restrictions and realize the long-wanted coupling of otherwise 45 mutually exclusive ferroelectric and magnetic orders. In this 46 context, the nonperovskite, two-dimensional (2D) Na-Mn-O 47 oxides are investigated as a testing ground for such a kind of 48

\*Present address: Ioanna Bakaimi, Department of Chemistry, University of Southampton, Southampton SO 171 BJ, UK.

<sup>†</sup>Corresponding author: lappas@iesl.forth.gr

2475-9953/2018/00(0)/004400(14)

004400-1

66

AUTHOR Orlandi

magnetoelectricity. These are rock-salt derivatives of the fam- 49

ily  $A^+Me^{3+}O_2$  (A = alkali metal, Me = 3*d* transition metal) 50

delafossites [5,6] that have attracted considerable interest 51

due to their physical and chemical properties. They include, 52

transparent conducting oxides, such as the CuAlO<sub>2</sub> [7], super- 53

conductors, like the hydrated variant Na<sub>0.3</sub>CoO<sub>2</sub>  $\cdot$  1.3H<sub>2</sub>O [8] <sub>54</sub>

of the P2-Na<sub>v</sub>CoO<sub>2</sub> bronzes [9], multiferroics as AFeO<sub>2</sub> (A = 55

Na, Ag) [10,11], and cathodic materials for high-capacity Na- 56

ion rechargeable batteries, like P2-Na<sub>y</sub>Mn<sub>1-x</sub>M<sub>x</sub>O<sub>2</sub> ( $x, y \leq 1$ , 57

M = Ni, Mg, Li) [12]. Such intercalation materials show high <sub>58</sub>

structural flexibility upon alkali metal insertion or extraction 59

and give rise to a rich phase diagram [13]. The crystal chemistry 60

of AMeO<sub>2</sub> allows for polymorphism due to oxygen-layer 61

gliding processes [14]. Consequently, their performance is 62

mediated by phase transitions between nearly degenerate 63 structural types [e.g., designated as O3- (3*R*; *R*-3*m*) and P2- $(P6_3/mmc)$ ] [12,15], while extended defects (e.g., stacking 65 faults) formed between various crystal domains, render the

apparently simple  $A_x MeO_2$  bronzes metastable. Therefore, 67

new insights on the impact of their inherent compositional 68

<sup>69</sup> variation are sought in order to explain their complicated <sup>70</sup> sequences of electronic and structural processes.

Core concepts of materials science point out that when 71 near-degenerate energy states are involved, compositional modulation [16] often emerges as a naturally evolving process 73 that relieves frustration by satisfying the cation-anion chemical 74 requirements, as, for example, in ferroelectrics [17] and shape 75 memory alloys [18,19]. Then, alternatives to traditional crys-76 tallographic approaches are necessary in order to understand 77 how subtle structural modulations in correlated transition metal 78 oxides (e.g., cation order and tilting of metal-oxygen coordina-79 tion polyhedral, etc.) entangle their electron degrees of freedom 80 and lead to novel behavior, extending from heterogeneous 81 82 catalysis and spin-induced ferroelectricity to high-temperature 83 superconductivity. The ability to control such functional properties, often emerging in the framework of broken symmetries 84 (as in TbMnO<sub>3</sub> and Ni<sub>3</sub>V<sub>2</sub>O<sub>8</sub> magnetoelectric materials) [20], 85 relies on understanding the role of residual disorder governing 86 the modulation of atomic positions and magnetic moments. 87 The superspace formalism, previously implemented for the 88 description of modulated chemical crystal structures [21], has 89 grown as a powerful method especially when nuclear and mag-90 netic modulations intertwine in the same phase [22]. Diverse 91 structural types, ranging from perovskites (CaMn<sub>7</sub>O<sub>12</sub> [23], 92 Pb<sub>2</sub>MnWO<sub>6</sub> [24]) to wolframite-type (MnWO<sub>4</sub> [25]) modu-93 lated structures, which all display symmetry-allowed coupling of electric polarization and magnetization, are illustrative examples of the importance of a robust and efficient treatment 96 97 of the symmetry of nuclear and magnetic modulations.

The focus here is on two particular polymorphs in the Na-Mn-O system which crystallizes in distorted variants of the O3-NaFeO<sub>2</sub> structure (3R polytype, R-3m) [26]. In these 100 layered compounds the spontaneous deformation of the MnO<sub>6</sub> 101 octahedra is caused by the Jahn-Teller effect, inherent to 102 the high-spin Mn<sup>3+</sup> cations  $(t_{2g}^3 e_g^1; S = 2; \mu_{eff} \cong 4.9 \mu_B)$ . 103 Because of this distortion,  $\alpha$ -NaMnO<sub>2</sub> becomes monoclinic 104 (C2/m), with flat [27] MnO<sub>6</sub> sheets [Fig. S1(a) in the Sup-105 plemental Material] [28], while  $\beta$ -NaMnO<sub>2</sub> appears to adopt 106 an orthorhombic cell (*Pmmn*), entailing zigzag [29] MnO<sub>6</sub> 107 sheets [Fig. S1(b)] [28]. The latter polytype is similar to the 108 thermodynamically stable lithiated analog  $\beta$ -LiMnO<sub>2</sub> [30], an 109 important precursor phase for cathode materials in solid-state 110 Li-ion batteries [31]. Moreover, specific challenges facing the 111 Mn-containing systems are governed: (a) by the very similar 112 free-energies of the  $\alpha$ - and  $\beta$ -NaMnO<sub>2</sub> polymorphs [32], 113 which suggest that intermediate phases with compositional 114 modulations could be formed at a very low energy cost, and 115 (b) by the Mn topology (see Fig. S1 in the Supplemental 116 Material) [28] that maps out a triangular lattice [33], inferring 117 some degree of spin frustration that renders these polymorphs 118 sensitive to small perturbations. 119

In view of the former characteristic, transmission electron 120 microscopy and synchrotron x-ray powder diffraction have 121 shown that on the basis of superspace formalism, planar defects 122 could act as a structure-directing mechanism in the cation-123 ordered rock-salt-type AMeO<sub>2</sub> structures, and in particular, 124 the  $\alpha$  and  $\beta$  phases of NaMnO<sub>2</sub> can be gradually transformed 125 into each other by changing the density of the involved twin 126 planes [33]. Interestingly, the presence of local intergrowths 127 of  $\beta$ -polymorph and stacking faults within the lattice of 128

the parent  $\alpha$ -NaMnO<sub>2</sub> phase is shown to be controlled in 129 single-crystals grown under optimal conditions [34]. This 130 apparent energy degeneracy between  $\alpha$ - and  $\beta$ -type oxygen coordinations seems to play an important role in determining the particularly high charge capacity ( $\sim 190 \text{ mA h g}^{-1}$ ) 133 of polycrystalline  $\beta$ -NaMnO<sub>2</sub> as an earth-abundant Na-ion 134 cathode [35]. As of the second inherent feature, neutron 135 powder diffraction has shown that despite the considerable spin 136 frustration in  $\alpha$ -NaMnO<sub>2</sub>, Néel order sets in at 45 K [36]. With <sup>137</sup> this concomitant symmetry breaking, a spin gap due to lead-138 ing quasi-one-dimensional interactions (with a predominant 139 nearest-neighbor exchange interaction of  $J_1 \sim 72$  K [37] and 140 frustrated  $J_2 \cong 0.44 J_1$  [38]; Fig. S1(a) [28]) describes the low-141 energy magnetic dynamics, while a peculiar magnetostructural 142 inhomogeneity emerges as a consequence of the system's tendency to remove magnetic degeneracy due to spin frustration 144 [39,40]. On the other hand, the magnetic ground state of 145  $\beta$ -NaMnO<sub>2</sub> is less well understood from the experimental point 146 of view. Theoretical calculations, though, predict that a spin 147 model with two-dimensional couplings  $[J_1 \sim 70 \,\mathrm{K}$  nearest 148 neighbor and  $J_3 \sim 57 \,\mathrm{K}$  next nearest neighbor; Fig. S1(b)] <sup>149</sup> [28] and a weaker frustrated interaction ( $J_2 \sim 13$  K) are likely 150 to describe the experimental magnetic susceptibility. This 151 material also manifests an abundant quasiperiodic arrangement 152 of defects [33]. Moreover, room-temperature <sup>23</sup>Na solid-state 153 nuclear magnetic resonance (NMR) spectra supported by 154 first-principles DFT computations identified a wealth of local 155 structural rearrangements, entailing a trade-off between the 156 majority  $\beta$ -type nanodomains and those of the  $\alpha$ -like phase 157 upon electrochemical cycling of sodium [41]. 158

The present contribution provides a powerful neutron 159 powder diffraction insight on  $\beta$ -NaMnO<sub>2</sub>, highlighting that 160 this challenging material is stabilized by near equivalent 161 in energy lattice conformations. The strength of superspace 162 formalism has been utilized to describe the structure on the 163 basis of a single-phase model, entailing an incommensurate 164 compositional modulation. The latter is depicted as a coherent 165 intergrowth of two types of NaMnO<sub>2</sub> layers, reflecting the 166  $\alpha$ - and  $\beta$ -type oxygen coordinations, and is shown to de-167 termine the material's physical properties. We illustrate the 168 implications of the modified lattice topology, with its intrinsic 169 extended defects, on the successive magnetic phase transitions. 170 Furthermore, temperature-dependent <sup>23</sup>Na NMR and inelastic 171 neutron scattering experiments point out that the magnetic 172 dynamics are gapped, while the influence of the magnetic order 173 on the electric dipole order is also reflected in the temperature- 174 and field-dependent magnetocapacitance studies. 175

#### **II. EXPERIMENTAL METHODS**

176

Polycrystalline  $\beta$ -NaMnO<sub>2</sub> samples were synthesized by 177 a high-temperature solid-state chemistry protocol reported 178 before [33], while phase identification was undertaken by 179 x-ray powder diffraction (XRPD) experiments carried out 180 on a Rigaku D/MAX-2000H rotating Cu anode diffractome-181 ter.  $\beta$ -NaMnO<sub>2</sub> specimens were air sensitive and all post-182 synthesis handling was carried with the aid of an Ar-circulating 183 MBRAUN anaerobic glove box. 184

Dc magnetic susceptibility as a function of temperature  $_{185}$  (5  $\leqslant$   $T\leqslant$  300 K) was measured on 20 mg batches of powder  $_{186}$ 

samples with a superconducting quantum interference device 187 (SQUID) magnetometer (Quantum Design, MPMS-XL7) un-188 der a moderate magnetic field (H = 20 mT). Heat capacity (C) 189 was measured at zero field on a cold-pressed pelletized powder 190 sample by means of the relaxation technique, utilizing a phys-191 ical property measurement system (Quantum Design, PPMS). 192 NMR measurements on the <sup>23</sup>Na nucleus (nuclear spin 193 = 3/2) were performed on a powder sample sealed in 194 pyrex sample holder. <sup>23</sup>Na NMR spectra and spin-lattice а 195 relaxation rate  $1/T_1$  were recorded between 50 and 300 K 196 in a magnetic field of 8.9 T using a solid-echo and inversion 197 recovery pulse sequences, respectively. Wide-line <sup>23</sup>Na NMR 198 powder data were obtained as sums of individual spectra 199 acquired by changing the measurement frequency in 50 kHz 200 steps over  $\pm 3$  MHz around the <sup>23</sup>Na reference frequency, 201  $v_0 = 100.5234 \text{ MHz}$ , which was determined from a 0.1 M 202 NaCl solution. The spin-lattice relaxation rate measurements 203 were performed at the position of the central line. 204

Neutron powder diffraction data were collected on the 205 WISH diffractometer [42], operating at the second target sta-206 tion (TS2) at the ISIS pulsed neutron source in the UK. WISH, 207 with its high brilliance, is particularly optimized for providing 208 high resolution at long d spacing required for magnetic studies. 209 For this purpose, a 2.7 g polycrystalline sample was loaded 210 in a 8 mm V-can, which was then sealed with indium wire 211 inside a high-quality, He-circulating anaerobic glove box. An 212 213 Oxford Instrument liquid helium cryostat was used for the temperature dependent diffraction experiments. Data analysis 214 was performed by using the Jana2006 software [43] for the 215 Rietveld refinements, whereas the group theory analysis was 216 performed with the help of the ISODISTORT software [44]. 217

Inelastic neutron scattering work was performed on the 218 MARI direct geometry chopper spectrometer (ISIS, UK) and 219 also on the DCS spectrometer (NIST, USA). Experiments on 220 MARI used incident energies  $E_i = 85$  and 150 meV, with 221 a Gd Fermi chopper spun at 300 and 450 Hz, respectively. 222 Measurements on DCS were done with an incident energy of 223  $E_i = 14.2 \text{ meV}$ . A 7.3 g of a powder sample was loaded in an 224 annular aluminum sachet that was placed inside a cylindrical 225 Al-can for the ISIS experiment, while a 5 g sample was loaded 226 in V-can for the NIST experiment. In either case the cans 227 were sealed with indium wire and they were cooled at low 228 temperatures with a top-loaded closed-cycle refrigerator. All 229 data has been corrected for background and also phonons from 230 the structural lattice. For the MARI data, the background plus 231 phonon contribution to the scattering at each energy transfer 232 was estimated from the high angle detector banks where 233 magnetic scattering is suppressed owing to the Mn<sup>3+</sup> form 234 factor. We have fit the high angle and high momentum detectors 235 at a fixed energy transfer to the form  $L(Q) = L_0 + L_1 Q^2$ , with 236  $L_0$  capturing the background and  $L_1$  providing an estimate 237 of the phonon scattering. L(Q) was then used to estimate 238 the background and phonon scattering at low momentum 239 transfers and then it was subtracted. For data taken on DCS, 240 the background was estimated by using the requirement for 241 detailed balance as discussed previously [45]. 242

The dielectric permittivity of ~3 mm pellets of pressed polycrystalline samples, without electrodes attached on the two flat surfaces, was studied at the CoreLab for Quantum Materials in the Helmholtz-Zentrum, Berlin, with a 14 T



FIG. 1. Temperature dependent (a) zero-field cooled dc magnetic susceptibility  $\chi(T)$  (right axis) under an applied field of 20 mT, and the heat capacity C(T) (left axis) of  $\beta$ -NaMnO<sub>2</sub>. The red line over the C(T) data is the calculated phonon contribution to the specific heat  $C_{\rm ph}(T)$  (see text). (b) The heat capacity remaining after subtracting the  $C_{\rm ph}(T)$  contribution from the experimental C(T) depicts two anomalies assigned as  $T_{\rm N1}$  and  $T_{\rm N2}$ .

PPMS system. The home-made setup is tailored for dielectric 247 constant measurements in a capacitorlike arrangement. It gives 248 the possibility to select between an AH 2700A ultraprecision 249 capacitance bridge, for relatively low frequencies (50 Hz– 250 20 kHz) or a Solatron 1260 impedance/gain phase analyzer, 251 for the high-frequency region up to 32 MHz; the latter is 252 being used together with a 1296A dielectric interface system 253 in order to cope with ultralow capacitance levels. A Lakeshore 254 370 temperature controller was utilized to cover a broad 255 temperature range (5  $\leq T \leq$  180 K). 256

#### III. RESULTS AND DISCUSSION

#### A. Macroscopic properties

257 258

The temperature dependent magnetic susceptibility  $\chi(T)$  <sup>259</sup> of the different NaMnO<sub>2</sub> polymorphs qualitatively appears <sup>260</sup> similar, with exception of the presence of a broad maximum <sup>261</sup> (~200 K for  $\alpha$ -polytype) [36], which apparently shifts to <sup>262</sup> higher temperature in the  $\beta$  phase [Fig. 1(a)]. Such a broad <sup>263</sup> feature is a general characteristic of low-dimensional antiferromagnetic systems. However, from  $\chi(T)$  data alone no evidence <sup>265</sup> for a transition to a long-range ordered state is observed. <sup>266</sup>

On the other hand, the heat capacity C(T) measured in 267 zero magnetic field displays several very weak anomalies 268 (Fig. 1), possibly of magnetic origin. In order to highlight 269 these features, we first estimated the phonon contribution to the 270 specific heat  $C_{\rm ph}(T)$  and subtracted it from the experimentally 271 measured heat capacity. Here  $C_{\rm ph}(T)$  assumes a sum of Debye 272 contributions (2 < T < 280 K), following the procedure used 273

<sup>274</sup> before for other low-dimensional spin systems [46,47]:

$$C_{\rm ph}(T) = 9R \sum_{i=1}^{2} C_i \left(\frac{T}{\theta_D^{(i)}}\right)^3 \int_0^{x_D^{(i)}} \frac{x^4 e^x}{(e^x - 1)^2} dx, \quad (1)$$

with R (8.314 J mol<sup>-1</sup> K<sup>-1</sup>) the gas constant,  $\theta_D^{(i)}$  is the Debye 275 temperature, and  $x_D^{(i)} = \theta_D^{(i)}/T$ , while fitting was based on 276 an optimization approach using the minimum number of 277 free parameters. In our case, the  $C_{\rm ph}(T)$  was approximated 278 by two Debye functions, addressing the relatively different 279 atomic masses of the constituent element-coupled vibrations 280 (cf. Na-O and Mn-O) in the  $\beta$ -NaMnO<sub>2</sub>. This yielded the fitting 281 parameters  $C_1 = 0.55(2)$ ,  $C_2 = 2.0(2)$  and  $\theta_D^{(1)} = 287(22)$  K, 282  $\theta_D^{(2)} = 510(15)$  K [Fig. 1(a)]. The vanishingly small magnitude 283 of C(T) at very low temperatures, in accord with the  $\beta$ -284 phase insulating nature, agrees well with the  $\propto T^3$  term that 285 corresponds to phonons [Eq. (1)]. 286

The outcome of the subtraction of  $C_{\rm ph}(T)$  from the total heat 287 capacity is shown in Fig. 1(b). As the corresponding anomalies 288 in the differential C(T) are very small, pointing to some 289 sensitivity to the defects in the lattice structure (vide infra), 290 and the estimated phonon part uncertainties are high, they 291 render further analysis to assess the differential C(T) as a likely 292 magnetic contribution  $\Delta S_{\text{mag}} = \int \frac{C_{\text{mag}}(T)}{T} dT$ , unfavorable at this stage. The identification, though, of the two fairly broad 293 294 humps centered at  $\sim$ 95 ( $T_{N2}$ ) and  $\sim$ 200 K ( $T_{N1}$ ), would suggest 295 that  $\beta$ -NaMnO<sub>2</sub> undergoes two transitions. These qualitative 296 C(T) characteristics therefore require further study to inquire 297 about the role of magnetic interactions in such phase changes. 298

#### 299

#### B. <sup>23</sup>Na NMR dynamics near the transitions

A critical aspect of many macroscopic thermodynamic 300 properties is the role of the material's microscopic dynamical 301 response. Techniques capable of detecting spin dynamics on 302 a local scale, such as solid-state <sup>23</sup>Na NMR, can therefore be 303 helpful to understand the complex behavior of  $\beta$ -NaMnO<sub>2</sub>. 304 The <sup>23</sup>Na NMR powder spectra of  $\beta$ -NaMnO<sub>2</sub> were measured 305 between room temperature and 50 K, where they become very 306 broad and, consequently, the signal becomes very weak and 307 difficult to measure [Fig. 2(a)]. At 300 K, the spectrum has 308 a characteristic powder line shape for a quadrupole I = 3/2309 nuclei with the quadrupole asymmetry parameter of  $\eta \approx 0$ . A 310 closer inspection of the satellite  $(\pm 3/2 \leftrightarrow \pm 1/2)$  transitions 311 of the 300 K spectrum terminated around  $\pm v_{\rm O} = \pm 1.28$  MHz 312 from the narrow central transition  $(1/2 \leftrightarrow -1/2)$  line [upper 313 inset to Fig. 2(a)] shows that the expected singularity is 314 rounded, which is consistent with a high degree of Na local 315 site disorder. Here  $v_Q$  is the <sup>23</sup>Na quadrupole frequency. On 316 cooling below  $T_{N1}$ , there is almost no change of the central 317 transition line. However, a close inspection of the <sup>23</sup>Na NMR 318 satellite line reveals that a shoulder starts to gradually broaden 319 well beyond  $\pm v_0$ . This is clearly seen as a growth of the 320 NMR signal intensity on both sides of the satellite shoulder 321 [lower inset of Fig. 2(a)]. As the positions of the satellite 322 shoulder remain nearly at the same frequency, the quadrupole 323 frequency must also remain the same through the transition 324 at  $T_{\rm N1}$ . This suggests that no structural deformation takes 325 place in the vicinity of the Na site, corroborating that the high 326



FIG. 2. (a) Normalized <sup>23</sup>Na NMR powder spectra of  $\beta$ -NaMnO<sub>2</sub> revealing two different magnetic regimes that evolve with temperature lowering. The spectra are shifted vertically for clarity. The insets point to a specific part of the spectra, where the quadrupolar frequency is indicated by the vertical dashed line. (b) The temperature dependence of the <sup>23</sup>Na NMR central line intensity multiplied by temperature for  $\beta$ -NaMnO<sub>2</sub>. The arrows indicate the two transition temperatures  $T_{\rm N1}$  and  $T_{\rm N2}$ .

temperature transition  $(T_{N1})$  is magnetic in origin. Moreover, 327 below  $T_{\rm N1}$  the intensity of the sharp central peak multiplied 328 by temperature (to counterbalance the changing Boltzmann 329 population) starts to progressively decrease with decreasing 330 temperature below  $T_{\rm N1}$  [Fig. 2(b)]. The broadening of the NMR 331 line beyond the satellites can thus be attributed to growing 332 internal magnetic fields at certain Mn ion sites, while the 333 gradual wipeout of the central line below  $T_{\rm N1}$  [Fig. 2(b)] reveals that the high-temperature paramagneticlike signal vanishes 335 only gradually, as it remains present at all temperatures below 336  $T_{\rm N1}$ . This leads us to the important conclusion that the magnetic 337 state below  $T_{\rm N1}$  is inhomogeneous. On further cooling below 338  $T_{\rm N2}$ , the <sup>23</sup>Na NMR line shape broadening becomes really <sup>339</sup> pronounced as the spectrum becomes completely dominated 340 by the broad distribution of internal (hyperfine) magnetic 341 fields and the sharp central peak almost disappears. These line 342 shape changes verify that  $\beta$ -NaMnO<sub>2</sub> indeed undergoes two <sup>343</sup> successive transitions to magnetically ordered states, at  $\sim 200$ 344 and  $\sim$ 95 K, in agreement with the assignment of subtle peaks 345 in the differential C(T) as magnetic transitions [Fig. 1(b)]. 346

Additional information about the two magnetic transitions <sup>347</sup> is deduced from the <sup>23</sup>Na spin-lattice relaxation rate  $1/T_1$ , <sup>348</sup> which was determined from fitting of <sup>23</sup>Na magnetization <sup>349</sup> recovery curves [Fig. 3(a)] to the magnetic-relaxation model <sup>350</sup> for I = 3/2 [48], <sup>351</sup>

$$M(t) = M_0 \Big[ 1 - s \Big( 1/10e^{-\left(\frac{t}{T_1}\right)^a} + 9/10e^{-\left(\frac{6t}{T_1}\right)^a} \Big) \Big].$$
(2)

352

Here s < 1 accounts for imperfect inversion of <sup>23</sup>Na nuclear magnetization after the initial  $\pi$  pulse, while  $\alpha$  stands for the initial  $\pi$  pulse,  $\pi$  stands for  $\pi$  stands for the initial  $\pi$  pulse,  $\pi$  pulse,  $\pi$  stands for the initial  $\pi$  stands



FIG. 3. (a) Normalized magnetization-recovery curves at a few selected temperatures. The data sets are shifted vertically for clarity. The solid lines are fits of a stretched single-component magnetic-relaxation model for I = 3/2 [Eq. (2), see text], while the dashed line corresponds to the fit with two such components. Please note that significantly different stretching exponent  $\alpha$  is found for temperatures above  $T_{N1}$  and below  $T_{N2}$ . (b) The temperature dependence of the spin-lattice relaxation rate for  $\beta$ -NaMnO<sub>2</sub>. The arrows indicate the two transition temperatures. A double-component fit is needed in the intermediate temperature regime  $T_{N2} < T < T_{N1}$ . The solid lines indicate a critical type of behavior for  $T > T_{N2}$  and an activated one for  $T < T_{N2}$  (see text for details).

(AFM) insulator in the paramagnetic phase. The stretching 359 exponent is  $\alpha = 0.88$  [Fig. 3(a)]; a value slightly below 1 360 implying a small distribution of relaxation rates expected in 361 experiments on powder samples. The transition to the magnetic 362 state at  $T_{N1}$  is accompanied by a sizable steplike increase in 363 the  $1/T_1$  value to  $1/T_1 = 66(5) \text{ s}^{-1}$  and a gradual reduction 364 of the stretching exponent [Fig. 3(a)]. The latter indicates that 365 the distribution of the spin-lattice relaxation times suddenly 366 starts increasing below  $T_{N1}$  thus indicating growing magnetic 367 inhomogeneity between  $T_{N1}$  and  $T_{N2}$  which is in accord 368 with the line shape changes [Fig. 2(a)]. In fact, as two-step 369 magnetization-recovery curves are clearly observed below  $T_{N1}$ 370 [e.g., measurement taken at 100 K shown in Fig. 3(a)], the 371 fit of the magnetization recovery curves in the  $T_1$  experiment 372 is significantly improved if two relaxation components are 373 included. Here the relative intensity of one of the components 374 (AFM1) increases at the expense of the second PM component, 375 the latter in close analogy to the wipeout effect of the narrow 376 central line [Fig. 2(b)]. 377

We stress that no obvious critical fluctuations leading to 378 diverging  $1/T_1$  could be detected at  $T_{N1}$ . The likely reason is 379 the nature of magnetic fluctuations, which according to the ex-380 pression  $\frac{1}{T_1} = \frac{2\gamma_n^2 k_B T}{(\gamma_e \eta)^2} \sum_{q^\rho} A_q^\rho A_{-q}^{\rho} \frac{\chi_{\perp}^{''}(q^\rho, \omega)}{\omega}$  (where  $A_q$  denotes the hyperfine coupling of the <sup>23</sup>Na nuclei with the electronic 381 382 magnetic moments,  $\chi''$  is the imaginary part of the dynamical 383 susceptibility, and  $\omega$  is the Larmor frequency), could be 384 filtered out in the  $1/T_1$  measurements for highly symmetric Na 385 (octahedral) sites. On the other hand, on approaching the lower 386 transition temperature at  $T_{N2}$ , the  $1/T_1$  of the paramagnetic PM 387 component is rapidly enhanced, suggesting the onset of critical 388

fluctuations. A phenomenological fit of the critical model 389  $1/T_1 = A + B(T - T_{N2})^{-p}$  to the PM data in the temperature 390 range between  $T_{N2}$  and 110 K, yields the critical exponent p = 3910.45(10) for  $A = 66(5) \text{ s}^{-1}$  and  $T_{N2} = 95.0(5) \text{ K}$  [Fig. 3(b)]. 392 Such critical enhancement demonstrates that the magnetic 393 fluctuations that govern the transition at  $T_{N2}$  cannot be filtered 394 out anymore at the Na site. This is also consistent with the 395 observed dramatic <sup>23</sup>Na NMR line shape changes [Fig. 2(a)]. 396 The temperature dependence of the other component (AFM1), 397 which we attribute to the already magnetically ordered regions 398 in the sample, is much more subtle [Fig. 3(b)]. Finally, at 399  $T < T_{\rm N2}$ , the two components in the magnetization recovery 400 curves are not obvious anymore [Fig. 3(a)], so we resort 401 back to a single-exponential fit [Eq. (2)]. However, a very 402 low stretching exponent of 0.34 has to be employed. Such a 403 strikingly low value of  $\alpha$  indicates an extremely broad distri-404 bution of relaxation times, hence a broad distribution of local 405 magnetic environments below  $T_{N2}$ . At the same time  $1/T_1$  is 406 strongly suppressed below  $T_{\rm N2}$  and exhibits an activated type of 407 dependence  $[1/T_1 \propto T^2 \exp(-\Delta/T), \text{ Fig. 3(b)}]$ , indicating the 408 opening of an excitation gap  $\Delta$  in the low-temperature phase. 409

#### C. Crystallographic structure

410

Critical to understanding such transformations is the way 411 magnetic ions are arranged in the underlying lattice structure 412 that establishes nearest-neighbor exchange terms and stabilizes 413 nondegenerate ground states. High quality data collected on 414 the WISH diffractometer enables the analysis of the crystallo- 415 graphic structure of  $\beta$ -NaMnO<sub>2</sub>. The main reflections of the 416 neutron powder diffraction (NPD) pattern are consistent with 417 the *Pmmn* space group, with cell parameters  $a_0 = 4.7851(2)$  Å, <sup>418</sup>  $b_0 = 2.8570(8)$  Å,  $c_0 = 6.3287(4)$  Å, at 300 K. The Rietveld 419 refinement of the main nuclear reflections (300 K), with the 420 *Pmmn* model [29] [Mn1 in 2b position z = 0.617(5), Na1 in 421 2b z = 0.125(4), O1 in 2a z = 0.365(6), and O2 in 2a z = 4220.872(6)], suggests a significant degree of "antisite" defects 423 between the Mn and Na sites that leads to an average occu- 424 pation of  $\sim$ 80:20 (see Fig. S2, Supplemental Material) [28]. 425 Moreover, the refinement points to an unexpectedly large value 426 for the oxygen thermal parameter  $[U_{\rm iso} \sim 0.038(2) \,\text{\AA}^2]$ . The  $_{427}$ use of anisotropic temperature factors in the refinement results 428 in a clear elongation of the thermal ellipsoids along the c direction (see Fig. S2) [27] indicating strong positional disorder. 430 Following this suggestion we spilt the two oxygen positions 431 along the c axis and the refinement converged to a splitting 432 of  $\sim 0.5$  Å and  $\sim 70:30$  occupancy of the resultant sites, with  $_{433}$ normal isotropic thermal parameters  $[U_{\rm iso} \sim 0.015(2) \,{\rm \AA}^2]$ . It 434 is worth stressing that the split and especially the occupancy 435 of O1 and O2 resemble the antisite occupancy of the Mn and 436 Na atoms; in particular, as shown in Fig. S2 this distortion is 437 needed to satisfy the coordination requirements of the Na and 438 Mn cations. 439

A crucial feature of the 300 K NPD pattern, in association 440 with the above analysis, is the presence of additional reflections 441 that could be ascribed to a nuclear modulation (Fig. 4). In 442 support of this comes earlier transmission electron microscopy 443 (TEM) work on  $\beta$ -NaMnO<sub>2</sub> [33], where it was pointed out that 444 formation of planar defects establishes short-ranged ordered 445



FIG. 4. Rietveld plot at 300 K for the  $\beta$ -NaMnO<sub>2</sub> structure in the *Pmmn*( $\alpha$ 00)000 superspace group. Inset: Zoom of the low *d*-spacing region inferring that stacking faults and defects give rise to a peculiarly broadened profile function. In both panels observed (black crosses), calculated (red line), and difference (blue line) patterns are shown. The tick marks indicate the calculated position of the main (black ticks) and satellite reflections (green ticks). The asterisk marks the main reflection from the  $\alpha$ -NaMnO<sub>2</sub> impurity, whereas the hashtags indicate, for example, two satellite peaks that are slightly off with respect to the calculated Bragg position indicating the possibility of the other two components of the modulation vector to be different from zero (see text for details).

regions that locally (i.e., on the length scale of a few unit cells) 446 follow the stacking sequence of NaMnO2 layers characteristic 447 of either the  $\alpha$  or the  $\beta$  phases. Importantly, long-period stack-448 ing sequences, with a modulation vector  $\boldsymbol{q} = (\alpha 00)\alpha \approx 0.1$ 449 (consistent with the cell choice reported in the present work), 450 were also required for indexing the additional satellite peaks 451 observed in both electron and synchrotron x-ray diffraction 452 data. From a LeBail fit of the WISH data we obtained an 453 optimal modulation vector q = (0.077(1), 0, 0), accounting for 454 satellites up to the second order in the NPD pattern. Some small 455 satellite reflections, however, are sliding off the calculated 456 position (Fig. 4), suggesting that the other two components 457 of the modulation vector may be slightly different from zero. 458 Refinements where the other two components of q were 459 allowed to vary proved unstable and did not lead to reasonable 460 results. The obtained value of q is near the commensurate 1/13461 position, which explains why the 1/6 value used before in 462 the synchrotron x-ray diffraction patterns indexed well a large 463 number of satellite peaks. 464

The observation of the satellite reflections in both NPD and 465 'EM measurements and the refinement of the average nuclear 466 structure indicate the possibility of a compositional modulation 467 in the structure that can be modeled through the superspace 468 formalism [49,50]. The theory of (3 + D) superspace groups, 469 introduced by de Wolff (1974, 1977) [51,52], is widely used to 470 describe the symmetry of commensurate and incommensurate 471 modulated structures. In order to understand the NPD pattern 472

#### PHYSICAL REVIEW MATERIALS 00, 004400 (2018)

of WISH we therefore used a (3+1)-dimensional superspace 473 approach considering an occupational modulation for all the sites in the average nuclear structure. In order to derive the possible superspace groups we performed group symmetry 476 analysis with the help of the ISODISTORT Software Suite [44] 477 starting from the refined average structure and the propagation 478 vector  $\boldsymbol{q} = (\alpha 00)$ . Having taken into account the observed 479 reflection conditions and the symmetry properties of the modulation vector, the symmetry analysis led to the *Pmmn*( $\alpha 00$ )000 superspace group as the best solution, corresponding to the  $\Sigma_1$  irreducible representations (IRs), with order parameter 483 direction (OPD)  $P(\sigma, 0)$  [53].

To account for the compositional modulation a steplike 485 (Crenel) function is introduced for every site in the structure. 486 The Crenel function is defined as [54] 487

$$p(x_4) = 1 \in \langle x_4^0 - \Delta/2, x_4^0 + \Delta/2 \rangle,$$
  

$$p(x_4) = 0 \notin \langle x_4^0 - \Delta/2, x_4^0 + \Delta/2 \rangle,$$
 (3)

where  $x_4$  is the internal (fourth) coordinate in the (3+1)D 488 approach and  $\Delta$  is the width of the occupational domain 489 centered at  $x_4^0$  ( $\Delta$  corresponds also to the average fractional 490 occupancy of the site). The modulation functions on the same 491 cation site are constrained to be complementary, meaning 492 that in every point of the crystal the site is occupied (this 493 results in the equations  $\Delta[Mn_i] + \Delta[Na_i] = 1$  and  $x_4[Mn_i] =$ 494  $1 - x_4$ [Na<sub>i</sub>] for each cation site). For the split oxygen positions 495 we introduce a similar constraint, imposing that in any position 496 in the crystal we have the superposition of the two split sites. 497 Regarding the origin along the fourth axis, the superspace 498 group constrains this value to two equivalent values: 0 and 499 0.5, thus making the choice trivial. Moreover, an additional constraint is introduced regarding the two Mn/Na sites. The 501 electron diffraction measurements, reported by Abakumov 502 et al. [33], suggest that the quasiperiodic stacking sequences 503 of the NaMnO<sub>2</sub> layers entail coherent stacking faults, a feature 504 which points out that their modeling can be reduced to the 505 alternation sequence of the Na and Mn cations. We followed 506 a similar approach for the modeling of the NPD pattern 507 assuming that the steplike functions were constrained to have 508 in every NaMnO<sub>2</sub> plane the right Mn/Na ordering, that is 509 to say, when one site switches from Mn to Na the other 510 changes from Na to Mn. The crystallographic model built in 511 this way was employed for qualitative Rietveld refinements. 512 Broad, asymmetric reflections throughout the NPD pattern, 513 mainly due to defects (e.g., stacking faults) and strain, make 514 such analysis hard to optimize, raising the agreement factors 515 and making a quantitative refinement difficult. The Rietveld 516 plot, over a wide *d*-spacing range, is shown in Fig. 4 and the 517 associated reliability factors are  $R_p = 8.81\%$ ,  $R_{wp} = 12.73\%$ , 518  $R_{\text{main}} = 9.96\%, R_{\text{sat}} \pm 1 = 15.41\%, R_{\text{sat}} \pm 2 = 14.79\%. \text{ De-} 519$ spite the apparent reflection broadening, our model shows good 520 agreement for the modulated parts of the profile, especially 521 obvious in the relatively short *d*-spacing region of the pattern 522 (inset in Fig. 4). The crystallographic parameters of the compositionally modulated  $\beta$ -NaMnO<sub>2</sub> at 300 K, on the basis of a 524 (3+1)D Rietveld analysis with the *Pmmn*( $\alpha$ 00)000 superspace 525 group  $[a = 4.7852(4) \text{ Å}, b = 2.85701(8) \text{ Å}, c = 6.3288(4) \text{ Å}, {}_{526}$  $\alpha = 0.077(1)$ ], are compiled in Table S1 [28]. 527



FIG. 5. Projection of the structure in the *ac* plane, depicting the refined incommensurate compositional modulated structure; two types of stacking changing between the NaMnO<sub>2</sub> polymorphs are shown. The violet atoms represent the Mn, the yellow ones the Na, and the red spheres the oxygen atoms. The small rectangle indicates the unit cell of the average *Pmmn* structure (see Fig. S1).

This single-phase structural model, despite the presence 528 of low intensity reflections ascribable to a small amount of 529 the  $\alpha$  phase and MnO (Fig. 4), takes into account almost 530 all the satellites present in the NPD pattern of the  $\beta$  phase, 531 as compared to the two-phase description on the basis of 532 the  $B2/m(\alpha\beta 0)00$  superspace group derived before from the 533 analysis of the synchrotron x-ray powder diffraction data [33]. 534 The nuclear structure model obtained here is shown in Fig. 5. 535 This is consistent with the one proposed by Abakumov et al. 536 [33], entailing coherent intergrowth of stacking sequences of 537 NaMnO<sub>2</sub> layers along the  $\mathbf{a}_0$  axis, characteristic of the  $\alpha$ - and 538  $\beta$ -polytypes. It may be considered as good approximation to 539 540 the real chemical phase, as planar defects, seen by electron microscopy, could violate the idealized Crenel-type function 541 used in the present analysis of the NPD data. In this model, the 542 MnO<sub>6</sub> octahedra throughout the structure display strong Jahn-543 Teller distortion (see Fig. S3 [28], for oxygen-cation distances 544 in the (3+1)D approach), with four short bonds below 2 Å 545 and two long ones around 2.4 Å, in a fashion analogous to the 546  $\alpha$ -NaMnO<sub>2</sub> [36]. On the other hand, while Na is also octahe-547 drally coordinated to oxygen, the distances involved are longer 548 due to its larger ionic radius. Moreover, in an effort to visualize 549 the degree of compositional modulation in the  $\beta$ -NaMnO<sub>2</sub> 550 structure, Fourier maps of the observed structure factor (Fig. 6) 551 involving the atomic sites in the  $zx_4$  plane were computed on 552 the basis of the observed NPD intensities and the calculated 553 phases. Figure 6(a) shows the complementary occupation of 554 the cation sites without any particular modulation of the z555 coordinate. On the contrary, from the Fourier maps centered 556 at the oxygen positions [Fig. 6(b)], it is inferred that the site 557 splitting observed in the average structure is needed in order to 558 satisfy the coordination requirement of the Mn<sup>3+</sup> Jahn-Teller 559 active cation. In fact, it is noted that when the Na and Mn swap 560 sites (cf. compositional modulation), the same happens in the 561

#### PHYSICAL REVIEW MATERIALS 00, 004400 (2018)



FIG. 6. Fourier maps of the observed structure factor ( $F_{obs}$ ) depicting the crystallographic cation sites (a) and oxygen positions (b). The solid colored lines represent the calculated position of the atoms showing no positional modulation along the  $x_4$  for the Mn/Na but its presence for the oxygen sizes (violet Mn, green Na, red oxygen, and blue the primed oxygen position). The black continuous lines indicate the positive density isosurface and the dashed lines the negative isosurface (the neutron scattering length for the Mn atoms is negative). The isosurface contours correspond to two scattering density units (Å<sup>-2</sup>) in all the plots.

oxygen split positions so that the bonding requirements are restored as depicted in Fig. S3 [28]. Our approach demonstrates that having taken advantage of the superspace formalism to describe the compositional modulation of the Mn and Na sites in a single-phase atomic configuration, the incommensurate  $\beta$ -NaMnO<sub>2</sub> structure can be depicted as a coherent intergrowth of two types of NaMnO<sub>2</sub> layers, reflecting the  $\alpha$ - and  $\beta$ polytype oxygen coordinations (Fig. 5).

#### D. Magnetic structure evolution 570

In view of the complex nuclear modulated structure ob-  $_{571}$  served in the NPD profiles of  $\beta$ -NaMnO<sub>2</sub>, it is challenging to  $_{572}$ 



FIG. 7. (a) A long *d*-spacing section of the neutron powder diffraction patterns as a function of temperature, showing the complex nature of the magnetic contribution to the pattern. Color map: The neutron scattering intensity. (b) Integrated intensity versus temperature for the main magnetic reflections with propagation vector  $\mathbf{k} = (1/2, 1/2, 1/2)$ , and for the satellites with propagation vector  $\mathbf{k} + \mathbf{q}$ , where  $\mathbf{q} = (0.077(1), 0, 0)$ . The lines over the data points depict the fit to the critical region (see text).

<sup>573</sup> evaluate the correlation between the crystal and magnetic struc<sup>574</sup> tures as the sample temperature is lowered. The temperature
<sup>575</sup> evolution of the diffraction pattern demonstrates the presence
<sup>576</sup> of two magnetic transitions (Fig. 7).

First, below  $T_{\rm N1} \sim 200$  K there is an intensity increase at 577 magnetic Bragg peak positions corresponding to a propagation 578 vector  $\mathbf{k} = (1/2 1/2 1/2)$  with respect to the *Pmmn* orthorhom-579 bic average structure. These reflections grow quickly below the 580 magnetic transition temperature and their broad Lorentzian-581 like profile is an indication that the magnetic domain is sensi-582 tive to the strain and defects present in the nuclear structure 583 (refer to Fig. 6), complying with the broadening of <sup>23</sup>Na 584 NMR spectra [inset, Fig. 2(a)]. Moreover, below about 100 K 585 the diffraction patterns show the development of additional 586 reflections [Fig. 7(a)]. This new set of peaks can be indexed 587 assuming the combination of the magnetic propagation vector 588 k and the nuclear one q, giving magnetic intensity at the 589 positions  $hkl \pm [\mathbf{k} \pm \mathbf{q}]$ . It is worth noting that the temperature 590 dependence of the integrated intensity [Fig. 7(b)] of these 591

#### PHYSICAL REVIEW MATERIALS 00, 004400 (2018)

two sets of reflections possesses different critical behavior, <sup>592</sup> thus suggesting that the two magnetic orders likely fall into <sup>593</sup> different universality classes. In particular, the fit of the 1/2 <sup>594</sup> 1/2 1/2 reflection with power law  $I = I_0[1 - (T/T_N)]^{2\beta}$  gives <sup>595</sup> a critical exponent of  $\beta = 0.33(4)$ , indicating interactions of <sup>596</sup> a 3D nature, instead, the **k±q** satellites possess an exponent <sup>597</sup> of  $\beta = 0.15(8)$ , which is more consistent with 2D interactions <sup>598</sup> the presence of some additional low intensity reflections that <sup>600</sup> are not indexed with the previous propagation vectors. These <sup>601</sup> extra reflections are ascribed to a small content of MnO <sup>602</sup> impurity and the  $\alpha$ -polymorph.

Let us first discuss the important changes in the NPD 604 pattern that were observed below 200 K. In order to establish 605 the possible magnetic space group we performed magnetic 606 symmetry analysis with the help of the ISODISTORT software 607 [44]. The NPD patterns show that no clear magnetic inten-608 sity is observed on the nuclear satellite reflections, therefore 609 pointing out that the magnetic structure is not strongly related 610 to the nuclear modulation at least in the  $100 < T < 200_{611}$ K temperature range. For this reason, magnetic symmetry 612 analysis was initiated on the basis of parent average Pmmn 613 nuclear structure (Fig. S1, Table S1) [28] and the propagation 614 vector  $\mathbf{k} = (1/2 \, 1/2 \, 1/2)$ . The results of the symmetry analysis 615 are reported in Table S2 [28]. The best agreement between 616 observed and calculated patterns was obtained for the mR1 617 representation, with order parameter direction (OPD) P1(a,0), 618 corresponding to the magnetic space group  $C_a 2/c$ , with a 619 change in the unit cell with respect to the parent structure 620 described by the transformation matrix (0, -2, 0, 0, 0, 2, -1, 1, 0). 621 It is worth underlining that the space group  $C_a 2$  also gives 622 a reasonably good result (Table S2), but with an increased 623



FIG. 8. Rietveld plot at 100 K of the  $\beta$ -NaMnO<sub>2</sub> structure in  $C_a 2'/c'(\alpha 0\gamma)00$  superspace group, with cell parameters a =5.7108(2) Å, b = 12.6394(9) Å, c = 5.5397(4) Å,  $\beta = 120.96(7)^{\circ}$ , and  $\mathbf{q} = (0, 0, 0.078(1))$ . Observed (black crosses), calculated (red line), and difference (blue line) patterns are reported. The tick marks indicate the calculated position of the main (black ticks) and satellite reflections (green ticks).



FIG. 9. Sketch of the magnetic structure below 200 K, (a) along the Mn zigzag chain typical of the  $\beta$ -polymorph ( $\mathbf{a}_0$  direction) and (b) in the same projection as for Fig. 6 (top panel). The black rectangle depicts the unit cell of the average *Pmmn* structure [ $a_0 = 4.7851(2)$  Å,  $b_0 = 2.85699(8)$  Å,  $c_0 = 6.3287(4)$  Å], while the red rectangle indicates the unit cell of the average low temperature monoclinic structure [ $a_m = 5.7112(2)$  Å,  $b_m = 12.6388(9)$  Å,  $c_m = 5.5365(4)$  Å,  $\beta = 120.97(7)^\circ$ ]; please note that the  $\mathbf{c}_m$  axis is inclined by ~60° out of the plane.

number of refinable variables, thus suggesting the higher 624 symmetry option  $C_a 2/c$  as the best solution. Combining the 625 mR1 P1(a,0) IRs with the compositional modulated structure, 626 the  $C_a 2'/c'(a0\gamma)00$  magnetic superspace group is obtained. 627 With the latter we then carried out Rietveld refinements, with 628 the representative 100 K profile. The Rietveld plot is shown 629 in Fig. 8, and the refined parameters are compiled in Table S3 630 [28]. The associated reliability factors are  $R_{Fobs} = 8.46\%$  for 631 the nuclear reflections and  $R_{Fmag} = 12.50\%$  for the magnetic 632 ones, while  $R_P = 13.88\%$ . Their values are rather on the high 633 side, due to pronounced hkl-dependent broadening, likely aris-634 ing from the presence of planar defects. The magnetic structure 635 is drawn in Fig. 9, projected in the same plane as the nuclear 636 one (Fig. 5, top panel). It entails antiferromagnetically coupled 637 Mn chains running down the  $\mathbf{b}_0$  axis ( $\mathbf{a}_0$ ,  $\mathbf{b}_0$ , and  $\mathbf{c}_0$  setting 638 is with respect to the orthorhombic Pmmn unit cell), stacked 639 in a zigzag fashion when viewed in an  $a_0c_0$ -plane projection 640 Fig. 9(a) that gives rise to antiferromagnetically coupled, 641 corrugated MnO<sub>2</sub> layers [Fig. 9(b)]. A similar collinear spin 642 model has been utilized before for the description of the 643 magnetic state in the isomorphous  $\beta$ -LiMnO<sub>2</sub>, where three-644 dimensional long-range order is established at  $T_{\rm N} \sim 260 \, {\rm K}$ 645 [55]. 646

<sup>647</sup> The derived spin configuration for  $\beta$ -NaMnO<sub>2</sub>, though, <sup>648</sup> indicates a commensurate ordering only for the Mn2 site, as a <sup>649</sup> similar ordering on the Mn1 site would have generated strong <sup>650</sup> magnetic intensity at the nuclear satellite reflections, a case

#### PHYSICAL REVIEW MATERIALS 00, 004400 (2018)

that is not supported by the NPD data. In this compositionally 651 modulated nuclear structure, between 100 < T < 200 K, only 652 the NaMnO<sub>2</sub> layer stacking sequences characteristic of the 653  $\beta$ -polytype carry a net magnetic moment. Such a magnetically 654 inhomogeneous state is consistent with the wipeout of the 655 central <sup>23</sup>Na-NMR line [Fig. 2(b)] and the two-component 656 nuclear spin-lattice relaxation in the same temperature range. 657 The magnetic moment of Mn2 sites has been computed as 658  $\mu \cong 2.38(10)\mu_{\rm B}$  at 100 K, but as the observed NPD profile 659 shows fairly broad magnetic peaks, the attained staggered 660 moment may be an underestimate (cf. the full moment for 661 spin-2 Mn<sup>3+</sup> is expected to be 4  $\mu_{\rm B}$ ). 662

When temperature is lowered below  $T_{\rm N2} \sim 100$  K, the incommensuratelike magnetic ordering appears to be described 664 with a combination of the magnetic  $\mathbf{k}$  and nuclear  $\mathbf{q}$  propagation vectors suggesting that the second transition takes place because longer-range magnetic correlations are established in 667 the alphalike stacking sequence(s). Assuming that the same 668 superspace group defines also the magnetic order at T < T669 100 K and taking into account a Mn1-site spin configuration 670 similar to that of the Mn2 site, magnetic scattering is calculated 671 only for the  $\mathbf{k} + \mathbf{q}$  satellite positions. However, its relative 672 intensity does not match the experimentally observed one, 673 pointing out that additional spin modulation of the existing 674 structure is required in order to adequately reproduce the 675 observed magnetic NPD pattern. Rietveld refinements of the 676 magnetic structure confirmed that the magnetic phase below  $T_{\rm N2}$  can be described by a proper-screw component, with 678 propagation vector  $\mathbf{k} + \mathbf{q}$  for both Mn1 and Mn2 sites, while 679 refinements assuming a spin-density wave type of structure 680 produced worse agreement factors and unphysical moment 681 size for the Mn1 site. The corresponding Rietveld refined 5 682 K NPD profile is shown in Fig. 10, with the refined magnetic 683 parameters compiled in Table S4 [27]. The associated reliabil-684 ity parameters are  $R_{Fobs} = 8.41\%$  for the nuclear reflections 685 and  $R_{Fmag} = 9.4\%$  for the magnetic ones, while  $R_P = 16.6\%$ 686 is relatively poor again due to the extreme peak broadening. 687 The magnetic structure below  $T_{\rm N2}$  is depicted in Figs. 11(a) 688 and 11(b). 689

To a first approximation the spin configuration is similar 690 to the commensurate one that develops below  $T_{\rm N1}$ , but at 691 the "boundary" of the  $\alpha$ - and  $\beta$ -like stacking sequences 692 (Fig. 5), as the ordering at the Mn1 site ( $\alpha$ -NaMnO<sub>2</sub> layer 693 stacking sequence) acts as a perturbation to the Mn2 site, 694 the Mn spins start to rotate away from the commensurate 695 structure type [Fig. 9(a)]. Within this modulated behavior, the 696 Mn<sup>3+</sup> magnetic moment takes the lowest values within the 697 NaMnO<sub>2</sub> layers characteristic of the  $\alpha$ -polytype (likely due 698 to their higher degree of spin frustration), while it grows in 699 magnitude as we move within the  $\beta$ -like stacking sequences, 700 reaching a maximum  $\mu \cong 3.5(10)\mu_B$  at their midpoint (see 701 Fig. S4) [28]. Such a nontrivial magnetic order is in line 702 with very broad distribution of spin-lattice relaxation times 703 found by NMR below  $T_{N2}$  (cf. low value of the stretching 704 exponent), implying a broad distribution of local environ-705 ments. This complexity might be an outcome of the sys-706 tem's effort to relieve competing interactions among neigh-707 boring spins in the  $\beta$ -NaMnO<sub>2</sub> modulated nuclear structure, 708 therefore requiring further insights on the role of geometric 709 frustration. 710



FIG. 10. Rietveld plot at 5 K for the  $\beta$ -NaMnO<sub>2</sub> structure in  $C_a 2'/c'(\alpha 0\gamma)00$  superspace group, with cell parameters a =5.7112(2) Å, b = 12.6388(9) Å, c = 5.5365(4) Å,  $\beta = 120.97(7)^{\circ}$ , and q = (0, 0, 0.081(1)). Observed (black crosses), calculated (red line), and difference (blue line) patterns are shown. The tick marks indicate the calculated position of the main (black ticks) and satellite reflections (green ticks). The asterisk marks the main nuclear and magnetic reflections from the  $\alpha$ -NaMnO<sub>2</sub> impurity phase, whereas the diamond indicates the main MnO magnetic reflection.

**E. Parametrization of magnetic excitations** 

<sup>712</sup> Since the NPD and the NMR resolved two magnetic <sup>713</sup> regimes, the magnetic fluctuations of  $\beta$ -NaMnO<sub>2</sub> were <sup>714</sup> studied by inelastic neutron scattering (INS). An overview



FIG. 11. (a) Schematic of the  $\beta$ -NaMnO<sub>2</sub> modulated magnetic structure at 5 K, projected at the same plane as the nuclear structure shown in Fig. 6 (top panel). (b) Sketch of the incommensurate part of the magnetic structure depicting a proper-screw order propagating along the (-110) direction with respect to the average *Pmmn* unit cell. In both panels the axes directions with subscript 0 indicate the average orthorhombic *Pmmn* cell (black rectangle), whereas the axes with subscript m indicate the direction of the low-temperature monoclinic structure (red rectangle).

#### PHYSICAL REVIEW MATERIALS 00, 004400 (2018)



FIG. 12. (a) The powdered averaged magnetic scattering in  $\beta$ -NaMnO<sub>2</sub> and (b) the corresponding single mode approximation (SMA) heuristic model, with two-dimensional (2D) interactions. The background subtraction method to remove phonon scattering and instrument background are described in the text. Color map: The powder average scattering intensity  $\bar{I}(\vec{Q},\hbar\omega)$  (see text for details).

of the measured INS response, well within the magnetically 715 ordered state (5 K), is shown in Fig. 12(a) for experiments on 716 the MARI spectrometer. A complementary insight on the low 717 energy magnetic dynamics was offered with higher resolution 718 through the DCS spectrometer (Fig. 13). At low temperatures 719 (1.5 and 75 K) the DCS spectra show clearly the presence of a 720 spin gap in the excitation spectrum, with little change in the gap 721 energy,  $\Delta \sim 5$  meV. A pronounced change is observed at 100 K 722 with a filling of the gap, yet with the presence of significant 723 magnetic scattering even at  $T > T_{N1}$  (see Fig. S5) [28]. 724

As the measured neutron scattering cross section is proportional to the structure factor  $S(\vec{Q}, \hbar\omega)$ , for a powder 726 material, the measured, momentum integrated neutron intensity is proportional to the following average at a fixed  $|\vec{Q}|$ , 728  $\bar{I}(\vec{Q},\hbar\omega) = \int \frac{d\Omega S(\vec{Q},\hbar\omega)}{d\Omega Q^2}$ . Obtaining microscopic exchange interactions that form the basis of the magnetic Hamiltonian 730 from powder neutron data are rather difficult owing to the averaging over all reciprocal space directions  $|\vec{Q}|$ . However, 732 applying sum rules allows information to be obtained about 733 the interactions and correlations in a general way which is 734 independent from the microscopic Hamiltonian. We outline 735 this method in the following. 736



FIG. 13. The temperature dependence of the low-energy magnetic fluctuations in  $\beta$ -NaMnO<sub>2</sub>, measured on the high-resolution DCS spectrometer. All data has been corrected for a temperature independent background using the detailed balance relation. Color map: The powder average scattering intensity.

In the absence of a full theory for the magnetic exchange 737 interactions in  $\beta$ -NaMnO<sub>2</sub>, and lack of single crystal data, we 738 have parametrized the dispersion  $E(\vec{Q})$  with a phenomenolog-739 ical expression which satisfies the periodicity of the lattice and 740 hence Bloch's theorem. One possible form of the dispersion, 741 consistent with lattice periodicity, can be written as a Fourier 742 series  $E^2(\vec{Q}) = \Delta + \sum_d B_d \sin^2(\vec{Q} \cdot \vec{d})$ , where  $\vec{d}$  is a bond vec-743 tor connecting nearest-neighbor (NN) spins,  $B_d$  are coefficients 744 in this series expansion, and  $\Delta$  is the magnitude of the spin 745 gap. Because the magnetic excitations appear relatively sharp 746 in energy (Figs. 12 and 13), we could utilize the single mode 747 approximation (SMA) which states that the structure factor, 748 which is proportional to the neutron cross section, is dominated 749 by a single resonant mode. 750

The problem of deriving a parametrization of the neutron 751 cross section  $S^{\alpha\alpha}(\vec{Q},\hbar\omega) = S(\vec{Q})\delta[\hbar\omega - E(\vec{Q})]$  (delta func-752 tion being numerically approximated by a Lorentzian with the 753 energy resolution width), is reduced to finding an expression 754 for S(Q). To do this, we apply the Hohenberg-Brinkmann first 755 moment sum rule [56], which applies to the case of isotropic 756 exchange and is closely related to the ground state magnetic 757 energy. Effectively the first moment sum relates S(Q) to the 758 dispersion E(Q) through the following expression: 759

1

$$\begin{split} \tilde{S}(\vec{Q}) &= \frac{\hbar \, \omega}{E(\vec{Q})} \\ &= -\frac{1}{3} \frac{1}{E(\vec{Q})} \sum_{\vec{d}} \mathbf{J}_d \langle \vec{S}_0 \cdot \vec{S}_d \rangle [1 - \cos(\vec{Q} \cdot \vec{d})]. \end{split}$$
(4)

In view of this, the single-mode approximation and parametrization of the dispersion  $E(\vec{Q})$  allows us to characterize which correlations are important and also determine the dimensionality of the excitations. In particular, the energy gap in a powder averaged constant-Q scan is sensitive to the dimensionality of the interactions. This fact was previously 765 used to show that  $\alpha$ -NaMnO<sub>2</sub> is dominated by one-dimensional 766 magnetic correlations [37]. 767

Comparison of the powder averaged spectra for  $\beta$ -NaMnO<sub>2</sub> 768 against its closely related  $\alpha$ -NaMnO<sub>2</sub> system (see Fig. S6) [28] 769 points to several key differences. First, the spectral weight in 770  $\alpha$ -NaMnO<sub>2</sub> is concentrated at low energies near the energy 771 gap edge, while it is much more evenly distributed in energy 772 in the case of the  $\beta$ -NaMnO<sub>2</sub> variant. The scattering is also 773 much more strongly peaked [56] in momentum for  $\beta$ -NaMnO<sub>2</sub>, 774 which is indicative of the higher (cf. than the quasi-1D of the 775  $\alpha$  phase) dimensionality of the associated spin correlations. 776 In addition, considerable spectral weight is located at the 777 top of the excitation band and the scattering is much more 778 well defined in momentum than in the  $\alpha$ -polytype. Such 779 qualitative observations suggest that  $\beta$ -NaMnO<sub>2</sub> may be more 780 two dimensional than the  $\alpha$  phase. We have therefore simulated 781 the powder averaged spectra by considering the case of the 782 two-dimensional spin exchange, with dominant correlations 783 along the  $\mathbf{b}_0$ -crystal axis. We have taken the dispersion relation 784 to have the following phenomenological expression: 785

$$E^{2}(\vec{Q}) = B_{0} + B_{1}\sin^{2}(\pi K) + B_{2}\sin^{2}(\pi H) + \dots + B_{3}\{\sin^{2}[\pi(K+H)] + \sin^{2}[\pi(K-H)]\}, (5)$$

which is consistent with the periodicity of the lattice (*Pmmn* <sup>786</sup> symmetry) and gives a minimum at half-integer positions, <sup>787</sup> relating the observed magnetic Bragg peaks. We have chosen <sup>788</sup>  $B_0 = 25 \text{ meV}^2$  to account for the spin-gap ( $\Delta$ ),  $B_1 = B_2 =$  <sup>789</sup> 625 meV<sup>2</sup> and  $B_3 = 400 \text{ meV}^2$ . <sup>790</sup>

To extract an estimate for the exchange constants, we have put the inelastic magnetic response on an absolute scale using the internal incoherent elastic line as a reference. The absolute calibration combined with the first moment sum rule afforded an estimate of  $J_d \langle S_0 \cdot S_d \rangle$ . Combined with the collinear magnetic structure, we have estimated a strong exchange along the **b**<sub>0</sub>,  $J_1 = 5.0 \pm 1.0$  meV, and a weaker one along **a**<sub>0</sub>,  $J_3 =$  $1.5 \pm 1.0$  meV (Fig. S1) [28].

The total integrated spectral weight (elastic and inelastic) 799 is constrained by the zeroth moment sum rule which can be 800 summarized as follows: 801

$$\frac{\int d^3q S(\dot{Q},\hbar\omega)}{\int d^3q} = S(S+1). \tag{6}$$

Integrating the INS data by using the elastic incoherent 802 scattering of the vanadium as an internal standard gives 803 the inelastic contribution to the above integral being 1.8(3). 804 Including the ordered moment in the elastic channel and noting 805 that there are two Mn<sup>3+</sup> ions per unit cell gives a total integral 806 of 4.7(4) for this sum. Given the expected value for S = 2807 is 12, this indicates that more than half of total moment 808 resides elsewhere in momentum and energy. One possibility 809 is for a large fraction residing in diffuse scattering, which 810 maybe resulting in a low-energy contribution that is beyond 811 the resolution of the spectrometer, while it is in agreement with 812 the broad shape of the magnetic reflections in the diffraction 813 data and with the high density of structural defects present in 814 the material. 815

816

#### F. Incommensurate structure and frustration

We have seen that the magnetic long-range order of 817  $\beta$ -NaMnO<sub>2</sub> is strongly correlated with its structural com-818 plexity, which is established through the relief of frustration. 819 Importantly, competing interactions between spins and their 820 complex magnetic orders are known to motivate spectacular 821 cross-coupling effects that lead to improper ferroelectricity 822 in frustrated magnets [57]. Establishing cross control of the 823 magnetic and ferroelectric polarizations challenges scientific 824 endeavors as striking new multiferroic device concepts may 825 be realized [58]. A key question then is whether the compo-826 sitionally modulated nuclear structure and magnetic order in 827  $\beta$ -NaMnO<sub>2</sub> may also stimulate competing degrees of freedom 828 that can become cross correlated through the symmetries [59] 829 of the associated magnetic and nuclear orderings. Preliminary 830 evidence for such a type of behavior in  $\beta$ -NaMnO<sub>2</sub> was 831 first reported by Bakaimi et al. who demonstrated that the 832 temperature-dependent dielectric permittivity  $\varepsilon'(T)$  displays 833 two small anomalies, near the  $T_{N1}$  and  $T_{N2}$  transitions discussed 834 here [60]. Since the explanation of possible magnetoelectric 835 coupling needs the understanding of the crystal and magnetic 836 symmetries, these early findings remained unexplored. Now 837 that these structures are known, through the current work, it is 838 worth revisiting the coupling of the aforementioned properties. 839 Let us now glance through the dielectric response of 840  $\beta$ -NaMnO<sub>2</sub> and compare it to that of  $\alpha$ -NaMnO<sub>2</sub>. Bearing in 841 mind that the magnitude of the dielectric permittivity anoma-842 lies in  $\beta$ -NaMnO<sub>2</sub> becomes larger with the application of an 843 intense electric field [60], here instead we utilized a progres-844 sively stronger external magnetic field, hoping for enhanced 845 changes in the  $\varepsilon'(T)$ . Our dielectric permittivity experiments, 846 however, identified only small anomalies in  $\varepsilon'(T, H)$  curves 847 that coincide with the onset of antiferromagnetic orders taking 848 place in the bulk  $\alpha$  ( $T_{\rm N} = 45$  K) and  $\beta$  ( $T_{\rm N2} = 95$  K) phases. 849 In  $\beta$ -NaMnO<sub>2</sub>, no other low-temperature  $\varepsilon'(T,H)$  signature is 850 observed that could indicate contributions from  $\alpha$ - and  $\beta$ -type 851 structural domains, as local probes have resolved before [41]. 852 Moreover, the magnetoelectric coupling must be weak in both 853 NaMnO<sub>2</sub> materials, as very little changes are brought about 854 despite the strength of the externally applied magnetic field 855 (Fig. 14). Having taken into account the symmetry-imposed 856 constraints for the free-energy [61] in the  $\alpha$ - and  $\beta$ -magnetic 857 phases, it is conferred that the spatial inversion symmetry is not 858 violated, excluding the possibility of improper ferroelectricity 859 in the magnetically ordered states (see Sec. S7, Supplemental 860 Material). In this respect, it is postulated that the observed 861 small anomalies in the dielectric constant are likely related 862 to the nonlinear, higher order terms (e.g., biquadratic term 863  $\sim E^2 H^2$ ) that are operative in chemically diverse systems, 864 ranging from planar magnets [62,63] and three-dimensional 865 magnetoelectric perovskites (AMnO<sub>3</sub>, A = Y, Bi) [64,65] to 866 quantum paraelectrics (EuMeO<sub>3</sub>) [66,67]. 867

#### IV. SUMMARY AND CONCLUSIONS

868

The present work entails a thorough study of the crystallographic and dynamical properties of  $\beta$ -NaMnO<sub>2</sub>. The proposed single-phase nuclear structure model takes advantage of the superspace formalism to describe the incommensurate compo-



FIG. 14. Temperature dependent dielectric permittivity  $\varepsilon'(T)$  as a function of the applied magnetic field for  $\alpha$ -NaMnO<sub>2</sub> (a) and  $\beta$ -NaMnO<sub>2</sub> (b).

sitional modulation [propagation vector,  $\mathbf{q} = (0.077(1), 0, 0)$ ] <sup>673</sup> of the Mn and Na sites that can be depicted as an intergrowth  $\alpha$ - and  $\beta$ -like oxygen coordinations. This peculiar topology strongly influences the physical and chemical properties of the material and underlines the role of the nearly degenerate in energy  $\alpha$  and  $\beta$  layer stacking sequences. The remarkable flexibility of  $\beta$ -NaMnO<sub>2</sub> to adapt its lattice topology is likely at the basis of the particular high charge capacity of the system as a Na-ion cathode material [35], but also may corroborate to the stability of the various nonstoichiometric phases [41] accessible through its electrochemical Na-intercalation/removal [68].

Moreover, the magnetic structure of  $\beta$ -NaMnO<sub>2</sub> was solved 885 on the basis of time-of-flight neutron powder diffraction data 886 and found to be strongly mediated by the material's inherent 887 lattice topology. First, below  $T_{\rm N1}$  (200 K), a collinear com-888 mensurate antiferromagnetic state, involving only the  $\beta$ -like 889 stacking sequences, develops with a propagation vector  $\mathbf{k} =$ 890 (1/2 1/2 1/2). Then, a second magnetic transition is observed 891 at  $T_{\rm N2}$  (95 K), marked by new satellite reflections ascribed 892 to the interaction of  $\mathbf{k}$  with the compositional modulation 893 vector **q**. The new magnetic ordering is due to the relief 894 of the magnetic frustration in the  $\alpha$ -like sheets that in turn 895 influences the ordering in the  $\beta$ -like stacking sequences, and 896 instigates a cooperative proper-screw magnetic state. Here the 897 lattice topology of the Jahn-Teller active Mn<sup>3+</sup> cation drives 898

the original 3D spin correlations ( $T < T_{N1}$ ) to become 2D in character. Inelastic neutron scattering and <sup>23</sup>Na NMR provide evidence that a spin gap ( $\Delta = 5 \text{ meV}$ ) opens in the excitation spectra, in line with the 2D nature of the magnetic interactions at  $T < T_{N2}$ .

Overall, structure and dynamics point that the incommen-904 surate  $\beta$ -NaMnO<sub>2</sub> structure can relay a magnetocapacitance 905 effect in the low-temperature magnetic state. Such a structural 906 complexity inquires whether controlled engineering of coher-907 ent defects may impart the material with novel technological 908 capabilities. In view of this, it is worth considering that in the 909 compositionally modulated  $\beta$ -NaMnO<sub>2</sub>, domain-wall (DW)-910 like phenomena [69] associated with the abundance of the  $\alpha$ 911 and  $\beta$  interfaces (Figs. 6 and 12), rather than extended domains 912 themselves, may be the active element in promoting some 913 degree of topologically correlated (related to DW), cooperative 914 magnetic and electric dipole arrangements. The way electronic 915 structure changes at such interfacial regions could be relevant 916 in order to manipulate the magnetoelectric response [70] even 917

- W. Eerenstein, N. D. Mathur, and J. F. Scott, Nature (London) 442, 759 (2006).
- [2] T. Kimura, T. Goto, H. Shintani, K. Ishizaka, T. Arima, and Y. Tokura, Nature (London) 426, 55 (2003).
- [3] T. Goto, T. Kimura, G. Lawes, A. P. Ramirez, and Y. Tokura, Phys. Rev. Lett. 92, 257201 (2004).
- [4] M. Pregelj et al., Phys. Rev. Lett. 103, 147202 (2009).
- [5] J. P. Parant, R. Olazcuag, M. Devalett, C. Fouassie, and P. J. Hagenmul, Solid State Chem. 3, 1 (1971).
- [6] M. A. Marquardt, N. A. Ashmore, and D. P. Cann, Thin Solid Films 496, 146 (2006).
- [7] H. Kawazoe, M. Yasukawa, H. Hyodo, M. Kurita, H. Yanagi, and H. Hosono, Nature (London) 389, 939 (1997).
- [8] K. Takada, H. Sakurai, E. Takayama-Muromachi, F. Izumi, R. A. Dilanian, and T. Sasaki, Nature (London) 422, 53 (2003).
- [9] C. Delmas, J. J. Braconnier, C. Fouassier, and P. Hagenmuller, Solid State Ionics 3–4, 165 (1981).
- [10] N. Terada, Y. Ikedo, H. Sato, D. D. Khalyavin, P. Manuel, A. Miyake, A. Matsuo, M. Tokunaga, and K. Kindo, Phys. Rev. B 96, 035128 (2017).
- [11] N. Terada, D. D. Khalyavin, P. Manuel, Y. Tsujimoto, K. Knight, P. G. Radaelli, H. S. Suzuki, and H. Kitazawa, Phys. Rev. Lett. 109, 097203 (2012).
- [12] R. J. Clement, P. G. Bruce, and C. P. Grey, J. Electrochem. Soc. 162, A2589 (2015).
- [13] C. Fouassier, G. Matejka, J. M. Reau, and P. Hagenmuller, J. Solid State Chem. 6, 532 (1973).
- [14] J. M. Paulsen, R. A. Donaberger, and J. R. Dahn, Chem. Mater. 12, 2257 (2000).
- [15] C. Delmas, C. Fouassier, and P. Hagenmuller, Physica B & C 99, 81 (1980).
- [16] A. Janner and T. Janssen, Phys. Rev. B 15, 643 (1977).
- [17] N. Choudhury, L. Walizer, S. Lisenkov, and L. Bellaiche, Nature (London) 470, 513 (2011).
- [18] L. Righi, F. Albertini, L. Pareti, A. Paoluzi, and G. Calestani, Acta Mater. 55, 5237 (2007).

in this class of nonperovskite compounds and warrants further exploration. 919

#### ACKNOWLEDGMENTS

We thank the Science and Technology Council (STFC) for <sup>921</sup> the provision of neutron beam time at ISIS Facility. Access to <sup>922</sup> DCS was provided by the Center for High Resolution Neutron <sup>923</sup> Scattering, a partnership between the National Institute of <sup>924</sup> Standards and Technology and the National Science Foundation under Agreement No. DMR-1508249. This work was <sup>926</sup> partly funded by the Carnegie Trust for the Universities of <sup>927</sup> Scotland, the Royal Society, and the EPSRC. Partial funding <sup>928</sup> was also secured through the framework of the Heracleitus <sup>929</sup> II project (Grant No. 349309.WP1.56) co-financed by the <sup>931</sup> European Social Fund, European Union (Operational Program <sup>932</sup> "Education and Lifelong Learning" of the National Strategic <sup>933</sup> Reference Framework, NSRF, 2007–2013).

- [19] L. Righi, F. Albertini, E. Villa, A. Paoluzi, G. Calestani, V. Chernenko, S. Besseghini, C. Ritter, and F. Passaretti, Acta Mater. 56, 4529 (2008).
- [20] T. Kimura, Annu. Rev. Mater. Res. 37, 387 (2007).
- [21] J. M. Perez-Mato, G. Madariaga, and M. J. Tello, Phys. Rev. B 30, 1534 (1984).
- [22] J. M. Perez-Mato, J. L. Ribeiro, V. Petricek, and M. I. Aroyo, J. Phys-Condens Matter 24, 163201 (2012).
- [23] W. Slawinski, R. Przenioslo, I. Sosnowska, M. Bieringer, I. Margiolaki, and E. Suard, Acta Crystallogr. Sect. B 65, 535 (2009).
- [24] F. Orlandi, L. Righi, C. Ritter, C. Pernechele, M. Solzi, R. Cabassi, F. Bolzoni, and G. Calestani, J. Mater. Chem. C 2, 9215 (2014).
- [25] I. Urcelay-Olabarria, J. M. Perez-Mato, J. L. Ribeiro, J. L. Garcia-Munoz, E. Ressouche, V. Skumryev, and A. A. Mukhin, Phys. Rev. B 87, 014419 (2013).
- [26] Y. Takeda, J. Akagi, A. Edagawa, M. Inagaki, and S. Naka, Mater. Res. Bull. 15, 1167 (1980).
- [27] M. Jansen and R. Hoppe, Z. Anorg. Allg. Chem. 399, 163 (1973).
- [28] See Supplemental Material at http://link.aps.org/supplemental/ 10.1103/PhysRevMaterials.xx.xxxxx for additional figures and tables with crystallographic information.
- [29] R. Hoppe, G. Brachtel, and M. Jansen, Z. Anorg. Allg. Chem. 417, 1 (1975).
- [30] I. J. Davidson, R. S. Mcmillan, J. J. Murray, and J. E. Greedan, J. Power Sources 54, 232 (1995).
- [31] A. R. Armstrong and P. G. Bruce, Nature (London) **381**, 499 (1996).
- [32] O. I. Velikokhatnyi, C. C. Chang, and P. N. Kumta, J. Electrochem. Soc. 150, A1262 (2003).
- [33] A. M. Abakumov, A. A. Tsirlin, I. Bakaimi, G. Van Tendeloo, and A. Lappas, Chem. Mater. 26, 3306 (2014).
- [34] R. Dally et al., J. Cryst. Growth 459, 203 (2017).

FQ

920

3

0

- [35] J. Billaud, R. J. Clement, A. R. Armstrong, J. Canales-Vazquez, P. Rozier, C. P. Grey, and P. G. Bruce, J. Am. Chem. Soc. 136, 17243 (2014).
- [36] M. Giot, L. C. Chapon, J. Androulakis, M. A. Green, P. G. Radaelli, and A. Lappas, Phys. Rev. Lett. 99, 247211 (2007).
- [37] C. Stock, L. C. Chapon, O. Adamopoulos, A. Lappas, M. Giot, J. W. Taylor, M. A. Green, C. M. Brown, and P. G. Radaelli, Phys. Rev. Lett. **103**, 077202 (2009).
- [38] A. Zorko, S. El Shawish, D. Arcon, Z. Jaglicic, A. Lappas, H. van Tol, and L. C. Brunel, Phys. Rev. B 77, 024412 (2008).
- [39] A. Zorko, O. Adamopoulos, M. Komelj, D. Arcon, and A. Lappas, Nat. Commun. 5, 3222 (2014).
- [40] A. Zorko, J. Kokalj, M. Komelj, O. Adamopoulos, H. Luetkens, D. Arcon, and A. Lappas, Sci. Rep.-Uk 5, (2015).
- [41] R. J. Clement, D. S. Middlemiss, I. D. Seymour, A. J. Ilott, and C. P. Grey, Chem. Mater. 28, 8228 (2016).
- [42] L. C. Chapon, P. Manuel, P. G. Radaelli, C. Benson, L. Perrott, S. Ansell, N. J. Rhodes, D. Raspino, D. Duxbury, E. Spill, and J. Norris, Neutron News 22, 22 (2011).
- [43] V. Petricek, M. Dusek, and L. Palatinus, Z. Krist-Cryst. Mater. 229, 345 (2014).
- [44] B. J. Campbell, H. T. Stokes, D. E. Tanner, and D. M. Hatch, J. Appl. Crystallogr. 39, 607 (2006).
- [45] C. Stock, E. E. Rodriguez, and M. A. Green, Phys. Rev. B 85, 094507 (2012).
- [46] N. S. Kini, E. E. Kaul, and C. Geibel, J. Phys.-Condens. Matter 18, 1303 (2006).
- [47] K. M. Ranjith, R. Nath, M. Majumder, D. Kasinathan, M. Skoulatos, L. Keller, Y. Skourski, M. Baenitz, and A. A. Tsirlin, Phys. Rev. B 94, 014415 (2016).
- [48] A. Suter, M. Mali, J. Roos, and D. Brinkmann, J. Phys.-Condens. Matter 10, 5977 (1998).
- [49] J. M. Perez-Mato, M. Zakhour-Nakhl, F. Weill, and J. Darriet, J. Mater. Chem. 9, 2795 (1999).
- [50] V. Petricek, A. Vanderlee, and M. Evain, Acta Crystallogr. Sect. A 51, 529 (1995).

#### PHYSICAL REVIEW MATERIALS 00, 004400 (2018)

- [51] P. M. D. Wolff, Acta Crystallogr. Sect. A A33, 493 (1977).
- [52] P. M. De Wolff, Acta Crystallogr. Sect. A A30, 777 (1974).
- [53]  $\sigma$  is the allowed direction of the order parameter in the distortion vector space defined by the irreducible representations within ISODISTORT suite.
- [54] S. v. Smaalen, *Incommensurate Crystallography* (Oxford University Press, New York, 2007).
- [55] J. E. Greedan, N. P. Raju, and I. J. Davidson, J. Solid State Chem. 128, 209 (1997).
- [56] P. C. Hohenberg and W. F. Brinkman, Phys. Rev. B 10, 128 (1974).
- [57] S. W. Cheong and M. Mostovoy, Nat. Mater. 6, 13 (2007).
- [58] Y. H. Chu *et al.*, Nat. Mater. 7, 478 (2008).
- [59] M. Fiebig, J. Phys. D Appl. Phys. 38, R123 (2005).
- [60] I. Bakaimi, A. Abakumov, M. A. Green, and A. Lappas, in SPIE OPTO (SPIE, Bellingham, WA, 2014), p. 7.
- [61] G. A. Smolenskii and I. E. Chupis, Usp Fiz Nauk 137, 415 (1982).
- [62] D. L. Fox, D. R. Tilley, J. F. Scott, and H. J. Guggenheim, Phys. Rev. B 21, 2926 (1980).
- [63] G. A. Samara and J. F. Scott, Solid State Commun. 21, 167 (1977).
- [64] T. Katsufuji, S. Mori, M. Masaki, Y. Moritomo, N. Yamamoto, and H. Takagi, Phys. Rev. B 64, 104419 (2001).
- [65] T. Kimura, S. Kawamoto, I. Yamada, M. Azuma, M. Takano, and Y. Tokura, Phys. Rev. B 67, 180401 (2003).
- [66] V. V. Shvartsman, P. Borisov, W. Kleemann, S. Kamba, and T. Katsufuji, Phys. Rev. B 81, 064426 (2010).
- [67] R. Saha, A. Sundaresan, M. K. Sanyal, C. N. R. Rao, F. Orlandi, P. Manuel, and S. Langridge, Phys. Rev. B 93, 014409 (2016).
- [68] A. Mendiboure, C. Delmas, and P. Hagenmuller, J. Solid State Chem. 57, 323 (1985).
- [69] M. Daraktchiev, G. Catalan, and J. F. Scott, Phys. Rev. B 81, 224118 (2010).
- [70] J. Seidel *et al.*, Nat. Mater. **8**, 229 (2009).

4