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2017

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Zawistowski, Matthew; Sussman, Jeremy B.; Hofer, Timothy P.; Bentley, Douglas; Hayward, Rodney A.; and Wiitala, Wyndy L., "Corrected ROC analysis for misclassified binary outcomes" (2017). *U.S. Department of Veterans Affairs Staff Publications*. 99. <https://digitalcommons.unl.edu/veterans/99>

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Corrected ROC analysis for misclassified binary outcomes

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Creating accurate risk prediction models from Big Data resources such as Electronic Health Records (EHRs) is a critical step toward achieving precision medicine. A major challenge in developing these tools is accounting for imperfect aspects of EHR data, particularly the potential for misclassified outcomes. Misclassification, the swapping of case and control outcome labels, is well known to bias effect size estimates for regression prediction models. In this paper, we study the effect of misclassification on accuracy assessment for risk prediction models and find that it leads to bias in the area under the curve (AUC) metric from standard ROC analysis. The extent of the bias is determined by the false positive and false negative misclassification rates as well as disease prevalence. Notably, we show that simply correcting for misclassification while building the prediction model is not sufficient to remove the bias in AUC. We therefore introduce an intuitive misclassification-adjusted ROC procedure that accounts for uncertainty in observed outcomes and produces bias-corrected estimates of the true AUC. The method requires that misclassification rates are either known or can be estimated, quantities typically required for the modeling step. The computational simplicity of our method is a key advantage, making it ideal for efficiently comparing multiple prediction models on very large datasets. Finally, we apply the correction method to a hospitalization prediction model from a cohort of over 1 million patients from the Veterans Health Administration EHR. Implementations of the ROC correction are provided for Stata and R. Published 2017. This article is a U.S. Government work and is in the public domain in the USA

Keywords: misclassification; ROC analysis; risk prediction modeling; electronic health records; precision medicine

1. Introduction

Predicting a binary outcome using a set of covariates is common practice in many areas of research [1, 2]. Typically, this involves fitting a predictive model on observed data, then assessing how accurately prediction probabilities from that model discriminate cases from controls. A standard metric for quantifying prediction accuracy is AUC, the area under the receiver operating characteristic (ROC) curve [3]. The ROC curve plots the sensitivity (true positive) and specificity (true negative) of the prediction model at potential discrimination thresholds and the AUC is the probability that a randomly chosen case has a higher predictive score than a randomly chosen control. Implicit in the prediction modeling and subsequent ROC analysis is the assumption that the observed binary outcomes are measured without error. In practice, this assumption may not hold, meaning samples that are recorded as cases are in truth controls and vice versa. Random error or systematic bias can produce measurement error in a binary variable that is often referred to as misclassification [4]. Examples of this phenomenon are widespread in research, including epidemiology [5–7], genetics [8, 9], and studies involving administrative claims outcomes [10].

Ignoring misclassification when modeling binary outcomes with logistic regression is well known to result in biased effect size estimates [4, 11]. Numerous methods have been proposed to obtain bias-corrected, although less efficient, regression parameters estimates, including a modified likelihood

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equation [11], Bayesian estimation [12], the expectation–maximization algorithm [13], simulation [14], and multiple imputation [15]. These papers focused primarily on parameter estimation and did not consider the predictive accuracy of the resulting estimates. Thus, the effect of misclassified outcomes on ROC analysis of risk prediction models has not been well described.

Analysis of misclassified outcomes is receiving renewed interest because of the emergence of research using Electronic Health Record (EHR) data. The promise of precision medicine rests in part on the ability to leverage Big Data resources such as EHRs that track vast clinical, demographic and genetic data into accurate prediction tools for individual patient risk [16–18]. Already, clinical information recorded in EHRs has been used to develop risk models for a wide range of conditions; examples include cardiovascular disease [19, 20], hospital readmission [21], acute kidney injury [22], and postoperative complications [23]. The clinical research potential of EHRs is immense; however, EHRs are imperfect and highly susceptible to missing and inaccurate diagnoses and behavioral information [24–26]. In practice, the presence of specific diagnosis or procedural billing codes (e.g., ICD9 codes) in a patient’s EHR are often used to identify case samples. Control samples are then defined as patients lacking the codes of interest. There are many reasons that a patient EHR might contain incorrect or missing information, making outcomes extracted from EHRs particularly prone to the problem of misclassification [27]. For example, a code can be erroneously entered in a patient EHR as the result of an incorrect diagnosis, typographical mistake, or ambiguous and heterogeneous use of codes. In addition, because EHRs are rarely shared between hospitals or health systems, whereas patients most certainly are, EHR-based records can be incomplete as patients move between health systems. While statistical methods to create error-adjusted prediction models from misclassified EHR outcomes do exist, the methods to properly assess the prediction accuracy of these models are lacking.

Evaluating diagnostic measurements in the absence of gold standard outcomes is a well-appreciated statistical problem (see [28] for an excellent review). Previous studies have examined ROC analysis for scenarios that include multiple non-gold standard diagnostic tests [29], partial outcome verification leading to missing outcomes [30], prediction based on multiple biomarkers [31] and even no observed outcomes [32]. In this paper, we focus on the specific problem of ROC analysis on risk prediction scores developed from and tested on outcomes subject to misclassification, a scenario commonly encountered in EHR research. Because the risk prediction scores are generated using the misclassified outcomes, they are themselves subject to bias [4, 11, 13, 14]. Even if the prediction model is properly corrected using one of the aforementioned methods, one is left with the dilemma of how to use the imperfect outcomes when performing the ROC analysis.

Here, we report that using misclassified outcomes in a standard ROC analysis leads to biased AUC estimates. The AUC bias exists regardless of whether the predictive model fit on the misclassified outcomes was properly corrected. The extent of the AUC bias depends on multiple factors including the composition of true cases and controls in the dataset and the specific rates at which each are misclassified. We present an intuitive and computationally simple correction to the standard ROC analysis that accounts for the misclassification inherent in the data. In particular, when computing the coordinates of the ROC curve, we replace the observed and potentially misclassified binary outcomes with a quantitative measurement: the probability that a sample is in truth a case conditional on their predictor covariates, observed outcome, and the likelihood that their observed outcome is misclassified. We show, through simulation, that this ROC correction produces nearly the same AUC value that would have been obtained in the absence of misclassification. Our method builds on the likelihood-based model for correcting logistic regression parameter estimates originally proposed by Neuhaus [11] and likewise assumes that probabilities defining the misclassification mechanism are known or can be estimated. Similar to regression parameter estimation in the presence of misclassification, the AUC estimates suffer from a loss of efficiency compared with AUC based on the true outcomes. However, the AUC bias correction remains effective even in the presence of high rates of misclassification.

Finally, we use the proposed ROC correction to assess a prediction model for inpatient hospitalization among patients in the Veteran’s Health Administration (VHA). We extracted clinical and demographic predictors as well as instances of inpatient hospitalization from the VHA EHR for a cohort of over 1 million samples. However, it is possible that a hospitalization event is not recorded in the VHA EHR if the patient received the care outside of a VHA facility, leading to misclassification of patients with true hospitalizations in our cohort. Ignoring the misclassified hospitalization events results in an underestimate of the true predictive capacity of the model. We show that the misclassification rates can be estimated using an internally validated ‘gold standard’ subset created from Medicare data that captures hospitalization events missing from the VHA EHR and incorporated into our corrected ROC procedure.

2. Methods

2.1. Binary misclassification model

We will adapt the basic notation for misclassified binary outcome data used by Neuhaus [11]. Let T be a binary outcome variable and assume that the probability of event T depends on a set of covariate variables $\mathbf{X} = X_1, \dots, X_p$ and effect size parameters $\beta = \beta_0, \beta_1, \dots, \beta_p$ through the standard logistic model

$$\text{logit}[P(T = 1|\mathbf{X}, \beta)] = \log\left(\frac{P(T = 1|\mathbf{X})}{1 - P(T = 1|\mathbf{X})}\right) = \beta_0 + \beta_1 X_1 + \dots + \beta_p X_p = \mathbf{X}'\beta. \quad (1)$$

We assume however that the true outcome variable T is not observed. Instead, we observe Y , a realization of the outcome variable subject to misclassification according to the following functions:

$$\gamma_0(\mathbf{X}) = P(Y = 1|T = 0, \mathbf{X}) \text{ and } \gamma_1(\mathbf{X}) = P(Y = 0|T = 1, \mathbf{X}). \quad (2)$$

The observed outcome variable Y is then related to the covariates \mathbf{X} through the likelihood equation

$$\begin{aligned} P(Y = 1|\mathbf{X}, \beta) &= \sum_{t=0}^1 P(Y = 1|\mathbf{X}, T) \times P(T|\mathbf{X}) \\ &= \{1 - \gamma_1(\mathbf{X}) - \gamma_0(\mathbf{X})\} \times P(T = 1|\mathbf{X}) + \gamma_0(\mathbf{X}) \\ &= \{1 - \gamma_1(\mathbf{X}) - \gamma_0(\mathbf{X})\} \times \frac{\exp(\mathbf{X}'\beta)}{1 + \exp(\mathbf{X}'\beta)} + \gamma_0(\mathbf{X}) \end{aligned} \quad (3)$$

We assume that the misclassification parameters satisfy $\gamma_0(\mathbf{X}), \gamma_1(\mathbf{X}) \leq 0.5$, indicating that observed values are no worse than chance. Moreover, the constraint $\gamma_0(\mathbf{X}) + \gamma_1(\mathbf{X}) \leq 1$ is required for numerical estimation of the β values.

2.2. Estimation of regression parameters

Assume a dataset consisting of covariate values and binary outcomes is generated using the model described previously. We will define three estimates for the effect size parameters β . First, let $\hat{\beta}^T$ be the maximum likelihood estimates for Equation (1) had the true observations been observed (i.e., $\mathbf{Y} = \mathbf{T}$). The $\hat{\beta}^T$ are then the standard log odds ratios obtained from logistic regression. Next, let $\hat{\beta}^I$ denote parameter estimates obtained by ignoring the misclassification and performing a standard logistic regression of the misclassified outcome Y on the covariates X . That is, $\hat{\beta}^I$ is computed by maximizing the incorrectly specified likelihood function $\text{logit}[P(Y = 1|\mathbf{X})] = \mathbf{X}'\beta$. The $\hat{\beta}^I$ estimators are biased, with the amount of bias determined by the misclassification functions in Equation (2) [11].

Finally, let $\hat{\beta}^M$ be the misclassification-adjusted log odds ratio estimates obtained by maximizing the corrected likelihood function based on Equation (3). We assume that the misclassification parameters $\gamma_0(\mathbf{X})$ and $\gamma_1(\mathbf{X})$ are known. The resulting $\hat{\beta}^M$ are consistent estimators of β provided the maximum likelihood regularity conditions are satisfied.

2.3. Prediction probabilities

After fitting a logistic regression, the effect size estimates can be used in the inverse logit function $\phi(\mathbf{x}, \mathbf{b}) = \exp(\mathbf{x}'\mathbf{b}) / (1 + \exp(\mathbf{x}'\mathbf{b}))$ to create a prediction model for the binary outcome. Here, we define prediction models based on the three different effect size estimators. Let $\hat{P}^T(X) = \phi(X, \hat{\beta}^T)$ denote the risk prediction model that uses the effect size parameter estimates $\hat{\beta}^T$ obtained when the true outcomes are observed. Likewise, let $\hat{P}^I(X) = \phi(X, \hat{\beta}^I)$ and $\hat{P}^M(X) = \phi(X, \hat{\beta}^M)$ be risk prediction models based on the parameter estimates $\hat{\beta}^I$ and $\hat{\beta}^M$, respectively. In the presence of misclassified outcomes, $\hat{P}^I(X)$ is a naive risk prediction model for the true outcome T based on the biased parameter estimates $\hat{\beta}^I$. Risk scores obtained from this model are in fact prediction values for the misclassified outcome Y rather than the true outcome T . The risk model $\hat{P}^M(X)$ gives prediction probabilities for the true, unobserved outcome by incorporating the bias-corrected parameter estimates $\hat{\beta}^M$.

2.4. ROC analysis

2.4.1. *Standard ROC analysis.* We will first develop notation for computing the standard ROC curve for an arbitrary set of binary outcomes $\mathbf{B} = B_1, B_2, \dots, B_N$ and corresponding risk prediction scores $\mathbf{q} = q_1, q_2, \dots, q_N$. The ROC curve is defined as the true positive and false positive rates over a range of potential prediction score cutpoints. The coordinates of the ROC curve for outcomes \mathbf{B} and prediction scores \mathbf{q} at a given cutpoint α are defined as $ROC(\alpha, \mathbf{B}, \mathbf{q}) = (FP(\alpha, \mathbf{B}, \mathbf{q}), TP(\alpha, \mathbf{B}, \mathbf{q}))$ where

$$TP(\alpha, \mathbf{B}, \mathbf{q}) = \frac{\sum_{i=1}^N I(B_i = 1) \times I(q_i > \alpha)}{\sum_{i=1}^N I(B_i = 1)} \tag{4}$$

$$FP(\alpha, \mathbf{B}, \mathbf{q}) = \frac{\sum_{i=1}^N I(B_i = 0) \times I(q_i > \alpha)}{\sum_{i=1}^N I(B_i = 0)} \tag{5}$$

are the true positive and false positive rates, respectively, and $I()$ is the indicator function. The area under the ROC curve is defined to be $AUC(\mathbf{B}, \mathbf{q}) = \int_{\alpha} ROC(t, \mathbf{B}, \mathbf{q}) dt$ and can be computed numerically using, for example, Riemann Sums or Monte Carlo methods. Using this notation, let $AUC(\mathbf{T}, \hat{P}^T)$ be the AUC for an ROC analysis of the true outcomes T ; $AUC(\mathbf{Y}, \hat{P}^I)$ be the AUC value for an ROC analysis of the biased risk scores and the observed outcomes \mathbf{Y} ; and $AUC(\mathbf{Y}, \hat{P}^M)$ the AUC value for the unbiased risk scores and the observed outcomes \mathbf{Y} .

2.4.2. *Misclassification-adjusted ROC analysis.* In the presence of misclassification, there is uncertainty regarding the observed outcomes, meaning that cases and controls can be incorrectly tallied in Equations (4) and (5). To account for this uncertainty, we propose replacing the observed and potentially misclassified outcome Y in the computation of the true and false positive rates with the ‘conditional predictive probability’ that a sample is in truth a case (i.e., $T = 1$). This predictive probability incorporates information from the observed outcome Y , the bias-corrected prediction probability $\hat{P}^M(X)$, and the misclassification values $\gamma_0(X)$ and $\gamma_1(X)$. As with the misclassification-adjusted regression, we assume that $\gamma_0(X)$ and $\gamma_1(X)$ are either known or can be estimated and have previously been used in the model building step to obtain the bias-corrected parameter estimates $\hat{\beta}^M$.

The conditional predictive probability that the unobserved outcome is in truth a case is

$$\begin{aligned} \hat{P}(T = 1|Y, X, \hat{\beta}^M) &= \frac{P(Y|T = 1, X) \times \hat{P}(T = 1|X, \hat{\beta}^M)}{\hat{P}(Y|X, \hat{\beta}^M)} \\ &= \begin{cases} \frac{[1 - \gamma_1(X)] \times \hat{P}^M(X)}{[1 - \gamma_1(X) - \gamma_0(X)] \times \hat{P}^M(X) + \gamma_0(X)} & Y = 1 \\ \frac{\gamma_1(X) \times \hat{P}^M(X)}{1 - [1 - \gamma_1(X) - \gamma_0(X)] \times \hat{P}^M(X) + \gamma_0(X)} & Y = 0 \end{cases} \tag{6} \\ &= \frac{[\gamma_1(X) - Y \times (2\gamma_1(X) - 1)] \times \hat{P}^M(X)}{(1 - Y) + (-1)^{1-Y} \left\{ [1 - \gamma_1(X) - \gamma_0(X)] \times \hat{P}^M(X) + \gamma_0(X) \right\}} \end{aligned}$$

where the denominator in the first line comes from Equation (3). After computing the conditional predictive probability in Equation (6) for each sample in the discrimination dataset, we define the misclassification-adjusted ROC curve to be $ROC_M(\alpha) = (FP_M(\alpha), TP_M(\alpha))$ where

$$TP_M(\alpha) = \frac{\sum_{i=1}^N \hat{P}(T_i = 1|Y_i, X_i, \hat{\beta}^M) \times I(\hat{P}^M(X_i) > \alpha)}{\sum_{i=1}^N \hat{P}(T_i = 1|Y_i, X_i, \hat{\beta}^M)} \tag{7}$$

$$FP_M(\alpha) = \frac{\sum_{i=1}^N \hat{P}(T_i = 0|Y_i, X_i, \hat{\beta}^M) \times I(\hat{P}^M(X_i) > \alpha)}{\sum_{i=1}^N \hat{P}(T_i = 0|Y_i, X_i, \hat{\beta}^M)} \tag{8}$$

and the corresponding misclassification-adjusted AUC, $AUC_M = \int_{\alpha} ROC_M(t)dt$, can be computed in the typical manner.

3. Simulation results

We present simulation results that describe the behavior of various strategies for assessing prediction models in the presence of misclassified binary outcomes. We simulated data according to the binary misclassification model described in Section 2.1 using R software. For each dataset, we fixed the effect sizes β and misclassification functions $\gamma_0(X)$ and $\gamma_1(X)$. Covariate values X were drawn from standard normal distributions, and true binary outcomes T were simulated based on the logistic model in Equation (1). We then created an observed version Y of the outcome by changing true cases ($T = 1$) to observed controls ($Y = 0$) with probability $\gamma_1(X)$, and true controls ($T = 0$) to observed cases ($Y = 1$) with probability $\gamma_0(X)$. We partitioned each dataset into training and testing cohorts. The bias-corrected regression parameter estimates $\hat{\beta}^M$ were computed on training samples only using an iteratively weighted least squares maximization of the logistic regression based on Equation (3) [11]. ROC computations were performed only on the testing samples. Results presented in this paper are for datasets of 5000 training samples and 5000 testing samples. The reported AUC and bias values are averaged over 500 simulated realizations with fixed parameter settings.

For each simulated misclassification dataset, we computed the following four measures of area under the ROC curve:

- (1) True outcome ROC analysis: This scenario assumes the true outcomes are observed ($Y = T$). A logistic regression model is fit on the observed/true outcomes and a standard ROC analysis is performed. For this scenario, we report $AUC(\mathbf{T}, \hat{P}^T)$, which we treat as the true predictive value when assessing the performance of the next three ROC strategies.
- (2) Misclassified outcome ROC analysis: This scenario assumes that misclassified outcomes are observed, but the misclassification is ignored in both the model fitting and subsequent ROC analysis. Biased parameter estimates \hat{B}^I are used for the prediction model and a standard ROC analysis of the observed outcomes is performed, giving $AUC(\mathbf{Y}, \hat{P}^I)$.
- (3) Corrected predictions, standard ROC analysis: This scenario assumes that misclassified outcomes are observed and that the misclassification is accounted for in the regression model but ignored in the ROC analysis. Therefore, bias-corrected parameter estimates \hat{B}^M are used for the prediction model but a standard ROC analysis of the observed outcomes is performed, resulting in $AUC(\mathbf{Y}, \hat{P}^M)$.
- (4) Misclassification-adjusted ROC analysis: This scenario assumes that misclassified outcomes are observed, and that the misclassification is accounted for in both the regression model and the ROC analysis. That is, the bias-corrected parameter estimates \hat{B}^M are used for the prediction model, conditional predictive probabilities (Equation 6) are computed and incorporated into the ROC analysis, leading to AUC_M .

The goal of the misclassification-adjusted ROC analysis for a given dataset is to reproduce the AUC value that would have been observed had there been no misclassification of outcomes. Therefore, we define AUC bias for the aforementioned naive or corrected ROC analyses as the difference between the AUC from true outcome ROC analysis, $AUC(\mathbf{T}, \hat{P}^T)$, and the AUC from the respective strategies ($AUC(\mathbf{Y}, \hat{P}^I)$, $AUC(\mathbf{Y}, \hat{P}^M)$ or AUC_M). In the following, we report the mean value of bias across realizations of datasets from the same underlying model parameters.

3.1. Bias in area under the curve of misclassified outcomes

We first show the results of standard ROC analysis performed on true and misclassified versions of simulated binary outcome data (scenarios 1 and 2 shown earlier) to establish the existence of AUC bias and to determine conditions that are most problematic. Table I gives the mean AUC values from an ROC analysis of true outcomes $AUC(\mathbf{T}, \hat{P})$ and from a naive ROC analysis of the misclassified outcomes $AUC(\mathbf{Y}, \hat{P}^I)$. To allow insight, we simulated outcomes with only a single covariate and constant misclassification at combinations of realistically low and high parameter values for the outcome-covariate model (β_0 and β_1) and the misclassification model (γ_0 and γ_1).

Misclassification leads to bias in the estimate of AUC for all parameter combinations. When the effect size β_1 is small, the true AUC value is already relatively low and any misclassification introduces only a small bias in AUC. When the effect size is larger ($\beta_1 = 1.0$), misclassification produces a greater bias in

Table I. Bias in area under the ROC curve for misclassified outcomes in a population cohort in which controls outnumber cases.

| Baseline risk $e^{\beta_0} / (1 + e^{\beta_0})$ | Effect size β_1 | False positive rate γ_0 | False negative rate γ_1 | True outcome ROC $AUC(T, \hat{P})$ | Misclass. outcome ROC $AUC(Y, \hat{P}^I)$ | Mean bias (% change) | | |
|--|--------------------------|-----------------------------------|-----------------------------------|---------------------------------------|---|-------------------------|-------|-------|
| 0.01 | 0.1 | 0.05 | 0.05 | 0.511 | 0.499 | 1.60 | | |
| | | | 0.2 | 0.511 | 0.500 | 1.31 | | |
| | 1.0 | 0.05 | 0.05 | 0.511 | 0.499 | 1.56 | | |
| | | | 0.2 | 0.511 | 0.500 | 1.27 | | |
| | | 0.2 | 0.05 | 0.758 | 0.560 | 26.07 | | |
| | | | 0.2 | 0.758 | 0.552 | 27.16 | | |
| 0.2 | 0.1 | 0.05 | 0.05 | 0.527 | 0.522 | 0.95 | | |
| | | | 0.2 | 0.527 | 0.520 | 1.28 | | |
| | | | 0.2 | 0.527 | 0.513 | 2.61 | | |
| | 1.0 | 0.05 | 0.05 | 0.05 | 0.527 | 0.510 | 3.10 | |
| | | | | 0.2 | 0.743 | 0.704 | 5.21 | |
| | | | | 0.2 | 0.743 | 0.688 | 7.42 | |
| | | 0.2 | 0.05 | 0.2 | 0.05 | 0.743 | 0.641 | 13.72 |
| | | | | | 0.2 | 0.743 | 0.617 | 16.87 |
| | | | | | 0.2 | 0.743 | 0.617 | 16.87 |

The table shows the area under the curve (AUC) for standard receiver operating characteristic (ROC) analysis of true and misclassified outcomes simulated at low and high values for each model parameter. The bias in AUC is greatest for very rare events with large effect covariates. In this scenario, misclassifying controls as cases (false positives) has a greater impact on AUC bias than does misclassifying true cases. Table S1 shows the result when cases are more prevalent in the cohort.

AUC, particularly for very rare events (baseline risk of 0.01). For example, misclassifying rare events, even at low false positive (γ_0) and false negative (γ_1) rates of 5%, leads to a 26% reduction in AUC value, from 0.758 down to 0.560. Misclassifying true controls as cases has a more dramatic effect on AUC bias. Whereas increasing the false negative rate to $\gamma_1 = 20\%$ in the prior scenario leads to only a slight increase in AUC bias (from 26% to a 27.2% reduction), increasing the false positive rate to $\gamma_0 = 20\%$ results in an AUC value that is reduced by 31.6% from the true value.

The increased sensitivity of AUC bias to false positive misclassification rate (γ_0) in the previous simulations stems from the fact that controls far outnumber cases in those datasets, as often occurs in population cohort studies. Because the vast majority of samples are true controls, the false positive rate has a larger influence on the actual number of outcomes that will be misclassified. We repeated this analysis using β_0 values in which cases are more prevalent than controls (Table S1). As expected, in that scenario, it is the false negative misclassification rate (γ_1) that has the greater effect on AUC bias. Thus, the prevalence of the outcome in the dataset is critical in determining which type of misclassification will have the greater effect on AUC bias.

3.2. Area under the curve correction

3.2.1. Constant misclassification. Initially, we assume the misclassification functions $\gamma_0(X)$ and $\gamma_1(X)$ are known and constant across all samples. Figure 1 shows the distribution of AUC values for the four ROC procedures based on datasets simulated with effect sizes of $\beta_0 = -1, \beta_1 = 1$ at reasonably large constant misclassification rates of $\gamma_0 = 0.2$ and $\gamma_1 = 0.3$.

The first boxplot shows the distribution of $AUC(T, \hat{P})$, the AUC values that would be obtained if the true outcomes were observed, and therefore provides the true distribution that we wish to recover. The dotted line at 0.741 marks the mean $AUC(T, \hat{P})$ value for the true outcome ROC analysis. The second boxplot shows the distribution of $AUC(Y, \hat{P}^I)$, an analysis that ignores misclassification in both the model fitting and ROC procedure. As expected, this naive analysis produces biased underestimates of true AUC (mean bias = 0.129). The third boxplot shows values of $AUC(Y, \hat{P}^M)$ based on a standard ROC analysis of misclassification-corrected prediction estimates. Interestingly, these AUC values are virtually identical to those from the previous ROC analysis that completely ignored the misclassification. Therefore, accounting for misclassification in the modeling step had little effect on AUC computation when the misclassified outcomes were still used in a standard ROC analysis.

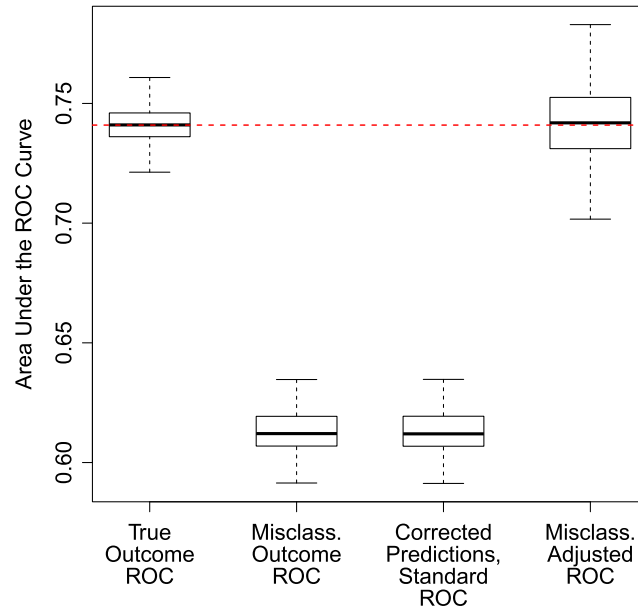


Figure 1. Distribution of area under the curve (AUC) values for four strategies of performing receiver operating characteristic (ROC) analysis in the presence of misclassified binary outcomes. (1) The distribution of AUC values when the true outcomes are observed. (2) Ignoring misclassification in both the regression prediction model and ROC analysis leads to a biased, underestimate of the true AUC. (3) The AUC bias remains when accounting for the misclassified outcomes during the modeling step, but ignoring them in ROC computation. (4) The misclassification-adjusted ROC procedure gives nearly unbiased AUC estimates (bias = -0.001) but larger variance than the true outcome AUC. Results are shown for 500 simulated datasets of 5000 training and 5000 testing samples with model effect sizes of $\beta_0 = -1, \beta_1 = 1$ and constant misclassification parameters $\gamma_0 = 0.2, \gamma_1 = 0.3$. [Colour figure can be viewed at wileyonlinelibrary.com]

Finally, the fourth boxplot shows AUC_M , the AUC values based on our misclassification-adjusted ROC method. The distribution for AUC_M is centered over the mean of the true AUC values (dotted line), and the ROC adjustment has removed nearly all bias introduced by the misclassification (mean bias = -0.001). The AUC_M estimates do, however, have a larger variance than the $AUC(T, \hat{P})$ from the true model. This is expected because the bias-corrected parameter estimates $\hat{\beta}^M$ are themselves known to be less efficient than estimates based on the true data $\hat{\beta}^T$ [11].

We computed confidence intervals for the corrected AUC_M estimator using a bootstrap technique. We created bootstrapped training datasets by randomly drawing samples with replacement from the training cohort only, recomputing the $\hat{\beta}^M$ and prediction model for each bootstrapped set and calculating the corresponding AUC_M in the original testing data. Assuming that AUC_M is an estimator for $AUC(T, \hat{P})$, the true AUC value that would have been observed in the absence of misclassified outcomes, we find that these bootstrap-based confidence intervals have accurate coverage probabilities when the underlying misclassification rates are known. For example, 90% confidence intervals for the AUC_M values shown in Figure 1 (based on 300 bootstraps of the training data) contained the true AUC in the testing data for 89% of the 500 simulated realizations.

Figure 2 shows mean bias and associated standard errors for AUC values obtained using a standard ROC analysis of misclassified outcomes and the misclassification-adjusted ROC analysis across a range of misclassification rates (also Figure S1). As expected, bias in the standard AUC computation increases with increasing levels of misclassification. The adjusted ROC procedure removes nearly all bias in AUC, although the standard error on these corrected estimates does increase with increasing misclassification. We observed similar results for simulations with multiple predictor variables (Figure S2).

3.2.2. Differential misclassification. Next, we relaxed the assumption of constant misclassification, allowing the misclassification rates to be functions of the covariate and thus vary between samples. Figure 3 shows distributions of AUC values for two extreme scenarios of covariate-dependent differential misclassification. Again, we set $\beta_0 = -1$ and $\beta_1 = 1$ and modeled misclassification using logistic functions of the covariate X as follows: $\text{logit}[\gamma_0(X)] = \theta_0 + \theta_1 X$ and $\text{logit}[\gamma_1(X)] = \sigma_0 + \sigma_1 X$. We fixed

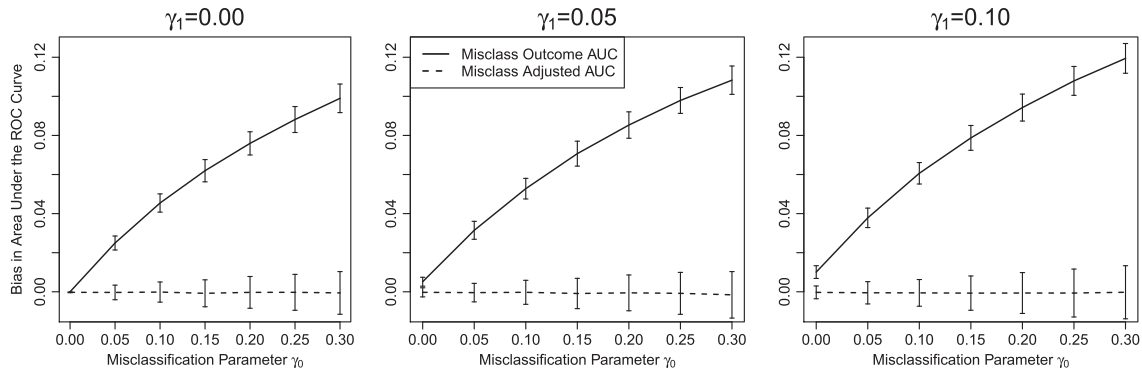


Figure 2. Bias in area under the curve (AUC) for standard and misclassification-adjusted receiver operating characteristic (ROC) analysis over a range of constant misclassification rates ($\beta_0 = -1, \beta_1 = 1$). Mean bias in AUC for a standard ROC analysis of misclassified outcomes (solid lines) increases with increasing amount of misclassification. The misclassification-adjusted ROC procedure (dashed lines) has bias of nearly zero over all combinations of false positive and false negative misclassification rates. Standard error on the misclassification-adjusted AUC estimates (vertical bars) increases with increasing rates of misclassification.

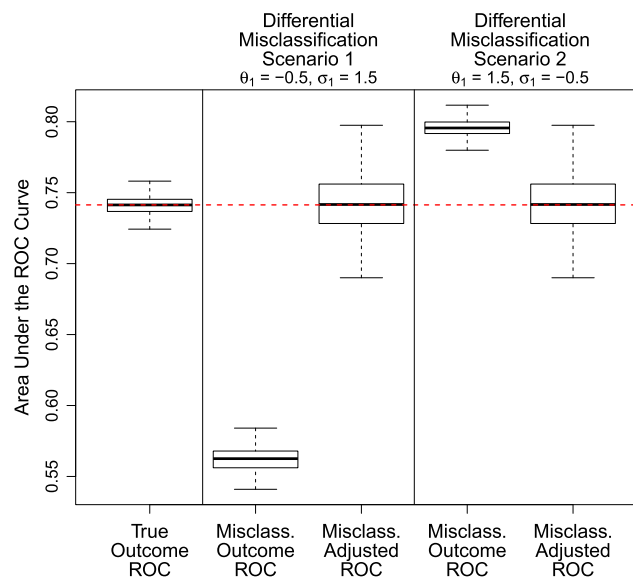


Figure 3. Distribution of area under the curve (AUC) values for covariate-dependent differential misclassification. In the first scenario, the differential misclassification reduces the true association between covariate and outcome, leading to an underestimate of the true AUC. In the second scenario, the misclassification rates inflate the covariate-outcome association in the prediction model, and lead to an overestimate of the true AUC. In both cases, the misclassification-adjusted receiver operating characteristic (ROC) procedure removes nearly all bias in AUC estimates. [Colour figure can be viewed at wileyonlinelibrary.com]

$\theta_0 = \sigma_0 = -1.386294$ to give $\gamma_0(0) = \gamma_1(0) = 0.2$. Then, in the first scenario, we set $\theta_1 = -0.5$ and $\sigma_1 = 1.5$ so that false positive rate increases with the probability of being a control and false negative rate increases with the probability of being a case (Figure S3). AUC values from the misclassified outcome ROC analysis severely underestimate of the true AUC (mean bias = 0.179). The AUC_M values from the adjusted ROC analysis have a mean bias of only -0.001 , indicating that the correction method has removed virtually all bias induced by misclassification.

In the second scenario, we reversed the relationship between misclassification rates and event probability. We set $\theta_1 = 1.5$ and $\sigma_1 = -0.5$ so that the false positive rate increases with the probability of being a case and the false negative rate increases with the probability of being a control (Figure S4). Here, the misclassified outcome ROC analysis actually overestimates the true AUC value (mean bias = -0.054). Again, the misclassification-adjusted ROC procedure yielded nearly unbiased AUC estimates (mean bias = -0.001).

This differential misclassification example highlights the fact that AUC bias can actually occur in both directions. In the first scenario, the noise introduced by misclassification weakened the regression association between the covariate and the outcome and ultimately led to a lower estimated predictive capacity. Underestimation of the true AUC is the more frequent scenario, also occurring for constant misclassification as well as when $\gamma_0(X)$ and $\gamma_1(X)$ have the same direction of effect (Figure S5). In the second scenario, the misclassification systematically strengthened the perceived association between the covariate and the outcome leading to an inflated estimate of the predictive ability of the covariate. In each case, however, the ability to recover bias-corrected parameter estimates in the modeling step allows the misclassification-adjusted ROC procedure to substantially reduce the AUC bias.

4. Application to Electronic Health Record hospitalization data

We present a proof of principle example using data from the Veteran's Health Administration (VHA) Electronic Health Record (EHR) and Centers for Medicare and Medicaid Services (CMS). This example serves as an application of our proposed ROC correction on real EHR data as well as a description of how the misclassification functions can be estimated using an internally validated 'gold standard' subset. The binary outcome of interest is the occurrence of an inpatient hospitalization in veteran patients aged 65 or older during a 3-year followup period from 1/1/2007 through 12/31/2009. We wish to know how well hospitalization events can be predicted using demographic (age and sex), behavioral (smoking), medication (hypertension prescription), and comorbidity (diabetes, chronic heart failure, chronic obstructive pulmonary disease, atrial fibrillation, and depression) information collected at baseline. We defined a nationwide cohort of $N = 1,037,428$ VHA healthcare patients between the ages of 65 and 80 at the start of 2006 and with at least two outpatient appointments within the VHA system during 2006. We partitioned the dataset into a training cohort of 750,000 samples for model building and the remaining $\sim 250,000$ samples to a testing cohort for the ROC analysis. Full description of the cohort and specific diagnosis and procedural codes used for comorbidities are given in the appendix.

4.1. Misclassification of hospitalization events

Patients in our cohort may be eligible for medical care through non-VHA sources, meaning that hospitalizations either occurring outside of VHA facilities or not billed to the VHA may not be recorded in the VA EHR. This inevitable gap in recording leads to the clear potential to misclassify patient outcomes when using only VHA EHR data, a common problem for any health care system. We therefore extracted Medicare records from CMS for patients in our cohort to identify additional hospitalization events not appearing in the VHA EHR. We treated the combined set of hospitalization events from the VHA EHR and CMS as the 'true' outcomes (T) and pose the question of how using only 'observed' VHA EHR outcomes (Y) would affect our prediction modeling. Under this scenario, patients with a hospitalization event in CMS but not in their VHA EHR would be misclassified as non-events.

We purposefully chose inpatient hospitalizations in Medicare-eligible patients ≥ 65 years of age to create an example in which total event capture should be nearly complete between the VA EHR and CMS. Inpatient hospitalizations are typically medically intensive and expensive, leading to a large number of procedural and billing codes that leave a substantial trail in the patient medical record, be it the VHA EHR or CMS, which is unlikely to be missed.

In total, 130,876 patients (12.6%) had an inpatient hospitalization during the 3-year followup recorded in their VHA EHR. In comparison, 320,697 patients (30.9%) had a hospitalization event based on the combined VHA and CMS records, indicating the extent of false negative misclassification for hospitalization events. We make the simplifying assumption that all hospitalization events are real. Although this may not hold in practice, the number of false positive events is likely much smaller than false negative events. Then, by construction, the false positive misclassification function is $\gamma_0(X) = 0$, and the false negative function $\gamma_1(X)$ is non-zero and unknown but there is evidence that it is covariate dependent (Figure S6).

4.2. Standard receiver operating characteristic analysis

Figure 4 shows ROC curves for predicting 3-year hospitalization events. First, we used the true (VHA + CMS) outcomes in the regression model with standard ROC analysis (black curve) to establish the 'true' AUC value in the absence of misclassification. This analysis yielded an AUC of 0.669 in the testing cohort. Next, we determined the effect of ignoring misclassification by fitting the logistic

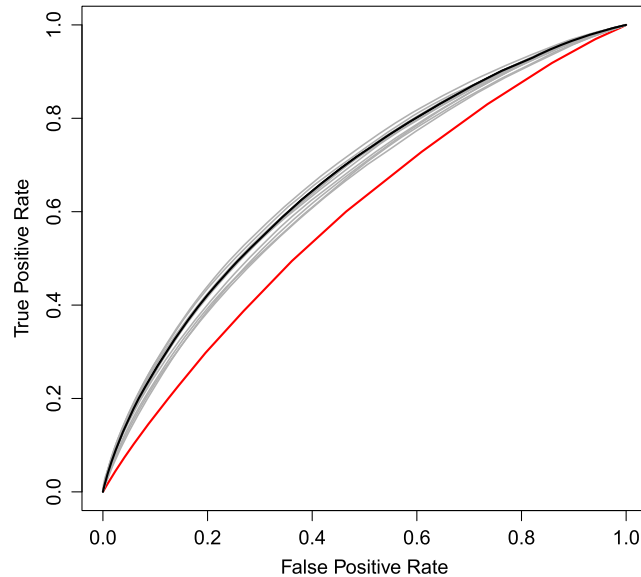


Figure 4. Receiver operating characteristic (ROC) curves for prediction of hospitalization events in Veteran's Health Administration (VHA) patients. The ROC curve (black) obtained when the true outcomes are observed has area under the curve (AUC) = 0.669. Using only hospitalization events recorded in the VHA EHR leads to misclassified outcomes. A standard ROC analysis of only VHA outcomes (red curve) has AUC = 0.592, an underestimate of the true predictive capability. We applied the misclassification-adjusted ROC procedure to the data using 'gold standard' subsets with validated outcomes to model outcome misclassification in the VHA-only data. The gray lines show the misclassification-adjusted ROC curve for realizations of the gold standard subset. The mean AUC value from the misclassification-adjusted ROC curves was 0.658, meaning the combination of a small gold standard subset and adjusted ROC procedure dramatically improved AUC estimation.

prediction model on the observed (VHA-only) outcomes and using the subsequent biased prediction values in a standard ROC analysis with the observed outcomes (red line). The AUC for this analysis was 0.592. As expected, the missed hospitalizations in the VHA-only outcome led to a biased AUC that lowered the perceived predictive value of the covariates. The 11.5% drop in AUC is consistent with simulation results in Table I for fairly common outcomes with low false positive and high false negative rates.

4.3. Estimation of misclassification rates

In order to apply our ROC procedure, we require an estimate of the misclassification function $\gamma_1(X)$. To do this, we randomly selected a subset of the training samples to serve as internally validated 'gold standard' outcomes. That is, for these samples, we revealed the true (VHA + CMS) hospitalization outcome and fit the following logistic regression model on true hospitalization cases:

$$\text{logit}[P(Y = 1|T = 1, X)] = \text{logit}[1 - \gamma_1(X)]. \quad (9)$$

where T is the VHA + CMS outcome, Y is the VHA-only outcome, and X is the same set of covariates used for predicting hospitalizations. We used the regression parameter estimates from Equation (9) to compute a covariate-dependent estimate of false negative misclassification $\hat{\gamma}_1(X)$ for each sample in the dataset. Using the $\hat{\gamma}_1(X)$ values and the VHA-only hospitalization outcomes Y , we computed AUC_M using our misclassification adjusted ROC procedure.

4.4. Misclassification-adjusted receiver operating characteristic analysis

Because of the sampling variation inherent in drawing an internal validation cohort, we created 20 realizations of 5000 randomly selected gold standard samples. The gray curves in Figure 4 show the misclassification-adjusted ROC curves based on the different realizations of the internal validation cohorts. The true ROC curve (black) is roughly centered within the distribution of misclassification-adjusted ROC curves. The AUC_M values ranged from 0.626 to 0.692, with an average value of 0.658, providing a much closer estimate of the AUC value of 0.669 from the true outcome ROC analysis.

Coverage of the bootstrap-based confidence intervals suffered (only two of the 20 90% confidence intervals covered the true AUC) because of the misclassification rates being estimated rather than known exactly (Figure S7). However, none of the confidence intervals covered or were below the naive AUC estimate of 0.592, only two intervals overestimated the true AUC, and, in many cases, the distance between the bounds of the confidence intervals and the true AUC were negligible (e.g., < 0.01). Thus, the combination of a small internally validated subset ($< 0.5\%$ of the full cohort) and our proposed ROC correction were able to sufficiently estimate unknown EHR misclassification rates and provide a much improved estimate of the predictive accuracy for hospitalization events.

5. Discussion

Building accurate predictive models based on EHR data is a critical step toward the goal of personalized medicine. Analysis of misclassified outcome data is therefore only likely to increase as EHR research becomes more prevalent. Properly accounting for inevitable misclassification in Big Data resources is required in both the statistical model building step as well as for determining prediction accuracy. Ignoring outcome misclassification when fitting a regression model leads to biased parameter estimates. Numerous methods have been proposed to correct that bias. Here, we have shown that simply correcting the effect estimates in the regression model is not sufficient for performing a valid ROC analysis. Using the misclassified outcomes, even with accurate risk prediction scores, leads to biased estimates of AUC. We have introduced a correction procedure in which the ROC curve incorporates quantitative likelihoods for the outcome into the definitions of true and false positive rates in place of the observed potentially misclassified outcome (Equations 7 and 8). This adjustment leads to more accurate estimates of true and false positive rates for any fixed cutoff α that in turn substantially reduces the bias in area under the ROC curve.

A major advantage of our correction method is that it is computationally simple, requiring only one additional value (Equation 6) be computed beyond the standard ROC analysis. Computational efficiency is essential in the era of Big Data in which datasets can be on the order of thousands of variables in millions of samples, thereby placing a premium on algorithms that can obtain the desired result without iterating through the data many times or requiring repeated draws of random variables. While the AUC bias could potentially be corrected using simulation, imputation, or more complex Bayesian methods, our closed-form equation is substantially faster. It is therefore ideal for quickly and accurately comparing the predictive value of competing models in very large datasets or determining the predictive value of individual model covariates.

Analyzing misclassified data requires some knowledge of the underlying misclassification mechanism. Unfortunately, this mechanism can be very complicated and unintuitive. Nevertheless, we have assumed that misclassification probabilities are either known or can be estimated. Because the misclassification probabilities are typically needed for correction in the model building step, we do not require additional information for our ROC correction. Estimates of misclassification rates can come from external diagnostic data or potentially even inferred from summary analyses of the observed data. In this paper, we showed how covariate-dependent misclassification probabilities can be estimated from an internally validated subset in which the true outcome is known. We used Medicare records to obtain the true outcome for hospitalization events, but other applications may require validation techniques such as medical chart review or molecular-based diagnosis (e.g., biopsy). The feasibility of this strategy is dependent on the cost (both financial and time) of obtaining true validated outcomes. It is important to note that although the actual causal mechanism leading to the misclassification in our data example remained unclear, the sample-level estimates of misclassification were sufficiently accurate to improve AUC estimation.

In practice, it may be unclear how extensive the misclassification is or how accurately it has been estimated. Our results in Tables I and S1 provide a means for determining how large the misclassification rates must be for different scenarios in order to have a major impact on AUC estimates. In some cases, the misclassification may be judged low enough that the effect on AUC is negligible. When fitting models and performing ROC analysis on misclassified outcomes, we recommend a sensitivity analysis in which AUC is computed for a range of misclassification parameter values to understand how changes in the misclassification probabilities affect inference. Similar sensitivity analyses have already been recommended for misclassification in the model building step [33].

There are many analytic considerations in prediction modeling and discrimination analysis. Throughout, we have assumed that the misclassification rates are the same in the testing and training cohorts, as expected when a single dataset is partitioned; however, this is not required. Provided the misclassification rates from the training data are used for the model building step and the misclassification rates from

the testing data are used in the misclassification-adjusted ROC analysis, the correction method remains valid. We have also used logistic regression throughout as our prediction model, but the prediction scores used in the ROC analysis can come from any type of classification model [2]. We simply assume that the risk scores have been properly corrected for the misclassification. Finally, sample size plays an important role in analysis of misclassified outcome data. Of course, larger sample sizes improve precision of effect size parameter estimates. But, more importantly, small sample sizes can lead to difficulty in convergence when trying to obtain maximum likelihood estimates for the misclassification-adjusted effect sizes $\hat{\beta}^M$. Here, we used the iteratively weighted least squares approach to solve for the $\hat{\beta}^M$ in training cohorts of 5000 samples. Smaller sample sizes may require alternative maximization procedures.

Implementations of the ROC correction and sample usage in R and Stata can be downloaded from the online Supplementary Material section.

Acknowledgements

We thank Tom Braun, Sebastian Zöllner, and Phillip Boonstra for providing valuable feedback on the initial manuscript and the three reviewers for constructive criticisms that improved the manuscript.

This work was supported by VA IIR 11-088. Support for VA/CMS data is provided by the Department of Veterans Affairs, Veterans Health Administration, Office of Research and Development, Health Services Research and Development, VA Information Resource Center (Project numbers SDR 02-237 and 98-004).

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Supplementary material

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