1	Population type influences the rate of ageing
2	Overall ADJ ^{1*} & Faragher RGA ¹
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4	1. School of Pharmacy & Biomolecular Sciences, Huxley Building, University of Brighton, Brighton,
5	East Sussex, BN2 4GJ, UK
6	
7	* Corresponding author
8	+441273 642099
9	a.d.j.overall@brighton.ac.uk
10	
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13	
14	Data archiving
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16	along with GNU public license details.
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ABSTRACT

Mutation accumulation is one of the major genetic theories of ageing and predicts that the frequencies of deleterious alleles that are neutral to selection until post-reproductive years are influenced by random genetic drift. The effective population size (N_e) determines the rate of drift and in age-structured population and is a function of generation time, the number of newborn individuals and reproductive value. We hypothesise that over the last 50,000 years, the human population survivorship curve has experienced a shift from one of constant mortality and no senescence (known as a Type-II population) to one of delayed, but strong senescence (known as a Type-I population). We simulate drift in age-structured populations to explore the sensitivity of different population 'types' to generation time and contrast our results with predictions based purely on estimates of N_e. We conclude that estimates of N_e do not always accurately predict the rates of drift between populations with different survivorship curves and that survivorship curves are useful predictors of the sensitivity of a population to generation time. We find that a shift from an ancestral Type-II to a modern Type-I population coincides with an increase in the rate of drift unless accompanied by an increase in generation time. Both population type and generation time are therefore relevant to the contribution mutation accumulation makes to the genetic underpinnings of senescence.

1 Introduction

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3 The survivorship curve is a useful visualisation of the frequency distribution of the age-classes of a population (Rauschert, 2010) and is calculated as $l_x = n_x/n_0$, where n_x is the number of individuals 4 5 in the study population who survive to the beginning of age category *x* and *n*₀ is the number of 6 newborns. If the population is stable, then survivorship curves describe how the numbers of 7 individuals of a cohort decline with time. When the logarithm of the number of survivors is plot 8 against age, then three distinct, idealized "types" are distinguished (Type-I, Type-II and Type-III 9 (Deevey, 1947); Figure 1A). Survival curves, by deduction, give some indication of the rate at 10 which mortality increases with age and, therefore, the rate of senescence of the population. It has 11 also been stated that variation in survival curves reflects species sensitivity to the genetic and 12 environmental factors that have shaped their evolutionary history (Demetrius, 2013). The 13 survival curve of modern humans is described as a classic "Type-I", where the probability of 14 survival is high until relative old age, whereby it then declines rapidly, which is typical of many large mammals. A Type-I survival curve is also typical of pre-industrial human populations (e.g., 15 16 the 1751 Swedish population in Figure 1A) and ancient societies, such as hunter-gatherer, forager-17 horticulturalist and acculturated hunter-gatherer societies, a modern example being the 18 indigenous Hadza population of Tanzania (Gurven & Kaplin, 2007, Figure 1A). Our closest living 19 relative species, the Chimpanzee, has a survivorship curve that is variable, depending on whether 20 the population is wild or captive (Thompson et al., 2007), but the wild examples are arguably 21 closer to a Type-II (Hill et al., 2001; Bronikowski et al., 2016), which is described by a constant 22 proportion of individuals dying over time. For illustrative purposes we generated an example 23 Type-II population with a 10% probability of mortality from one age class to the next, which aligns 24 closely with the chimpanzee population (Figure 1A). Ancestral human populations studied from 25 archaeological specimens, for example the Libben site skeletal sample, which is radiocarbon dated 26 to between 800 - 1100 CE, have been described as Type-II populations (Lovejoy et al., 1977). 27 However, the remains from such sites are not always representative of the total population 28 (Howell, 1982); hence, survivorship curves derived from archaeological specimens are not 29 considered in this study. By comparison, Type-III populations display very high mortality at young 30 ages, but those that do survive to adulthood go on to have a relatively long life expectancy, which 31 is typical of tree and insect species. The difference between the Type-I survivorship curves of 32 hunter-gatherer and pre-industrial populations and the Type-I survivorship curve of modern

industrial populations is difficult to quantify and identifies a limitation of this approach when
 considering the evolutionary demography of a species.

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- 4

5 Figure 1

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7 An early approach to quantifying the information contained within survivorship curves was to use its logarithm, for example Keyfitz's entropy, $H = \frac{-\int_0^\infty (lnl_x)l_x dx}{\int_0^\infty l_x dx} = -\frac{e^+}{e_0}$ (Keyfitz, 1978, Goldman & 8 9 Lord, 1986), described as the ratio of life expectancy lost due to death (e^{\dagger}) to that of life 10 expectancy (e_0) . This more quantitative approach to describing age-distributions has recently 11 been developed to distinguish between the 'pace' and 'shape' of change of populations as they age 12 (Baudisch, 2011; Baudisch et al, 2013). The 'pace' of life, or how fast populations age, can be 13 measured as life expectancy (*e*₀), which captures the average length of life, or the tempo at which 14 organisms survive and reproduce, placing organisms on a fast/slow continuum of ageing 15 (Baudisch, 2011; Colchero et al, 2016). On the other hand, the 'shape' describes the direction and degree of change in mortality (Wrycza et al, 2015) and hence captures the rate at which a species 16 17 senesces (Baudisch, 2011). There are various ways of measuring the 'shape' of ageing, all of which 18 are highly correlated (Wrycza et al, 2015). Figure 1B and 1C illustrate two methods of measuring 19 'shape'; one is generally referred to as life table entropy (sometimes lifespan equality), which can 20 be calculated as *ln*(1/Keyfitz's entropy) (Wrycza, 2015, Colchero, 2016). Another is the ratio of 21 longevity (Ω)/life expectancy (e_0), where Ω is the age at which, for example, 95% of the adults 22 have died. Although there are many measures (Wrycza et al, 2015), we present these two as they 23 have previously been used for cross-species comparisons (Baudisch, 2011; Colchero et al, 2016). 24 As can be seen from Figure 1, there is some correspondence between these pace/shape metrics 25 and the survivorship curves: the wild chimpanzee population clusters with the Type-II example; 26 the pre-industrial/hunter-gatherer Type-I populations cluster together and the modern US Type-I 27 population stands apart from all of these. For the populations considered here, life expectancy 28 increases from Type-III to Type-II to Type-I, as expected, and shows that population Type 29 corresponds more obviously with notions of the 'pace' of life. There are, however, some important 30 subtleties. For example, the distinct Type-II and Type-III survivorship curves presented in Figure 31 1A have similar 'shape' (Figure 1B and 1C). Because Type-II populations show constant mortality 32 with age, they are representative of populations that show negligible senescence. Baudisch (2011)

1 points out that long-lived species typically present negligible senescence, for example, long-lived 2 trees and marine invertebrates mostly show Type-III survivorship. For this reason Type-II and 3 Type-III populations should cluster on the 'shape' axis. However, there are clear exceptions to this 4 rule, modern human populations being one as, although they are long-lived, they have a shape 5 score indicative of strong senescence. As helpful as pace and shape are at capturing important 6 aspects of a species life-history, we believe they do not lend themselves so readily to visual 7 comparisons of survival/mortality with age where the corresponding reproductive distribution is 8 being studied. Here we explore the influence of the reproductive distribution, specifically 9 generation time, on the rate of genetic drift for human populations, with current and hypothetical 10 ancestral survival curves. The aim is to identify the influence of population 'type' and generation 11 time on mutation accumulation and, as a consequence, the corresponding changing role of 12 mutation accumulation on the senescence of these populations.

13

14 The current longevity that modern humans experience came late in human evolution, where for first time during the Upper Palaeolithic (~ 50,000 to 10,000 years ago) there are a larger number 15 16 of older adults amongst the deceased than there are younger adults (Caspari & Lee, 2004). 17 Evidence from throughout the late Archaic up to the Upper Palaeolithic also indicates that 18 mortality patterns for young (pre- 40 years) versus old (post- 40 years) did not alter during this 19 period and that older individuals would have been rare (Trinkaus, 2011). If the wild 20 chimpanzee/Type-II survivorships are indicative of our common *ancestral* type, then judging by 21 modern hunter-gatherer societies and the evidence from Upper Palaeolithic humans (Caspari & 22 Lee, 2004}, it seems reasonable to assume that the Type-I distribution is generally reflective of 23 human populations since the Neolithic period (~ 500 generations ago). This has implications for 24 the evolution of ageing in human populations as well as the laboratory models used to study it. We 25 hypothesise that a Type-II survivorship curve displaying a constant mortality rate and relatively 26 few older reproductive adults describes the majority of our ancestral demography, up until the 27 Palaeolithic. A Palaeolithic, demographic shift towards the modern Type-I survivorship curve 28 would then have followed this, with the older, parental age-classes now numerically better 29 represented. The greatest shift in modern human evolution may not simply be one of increasing 30 population size, but rather a change in the survivorship curve (Type-II to Type-I), which has 31 implications for the genetic drift of deleterious mutations, and hence mutation accumulation. 32

1 Standard population genetics theory tells us that the allele frequencies of mutations entering small 2 populations will drift to a greater degree (greater stochasticity) than those entering large 3 populations, as genetic diversity is lost at a rate proportional to $1/2N_e$, where N_e is the effective 4 population size. A mutation with a negative impact on the fitness of the homozygous genotype 5 (e.g., *aa*) relative to the wild-type homozygote (e.g. *AA*), measured as *s*, is effectively removed by 6 natural selection whenever $s > 1/2N_e$, else drift dominates the rate of loss (Hartl & Clark, 2007). If 7 we consider a snapshot of a population with overlapping generations, then we expect to see a 8 monotonic decline in the number of individuals with increasing age due to the unavoidable causes 9 of mortality that individuals encounter with the passing of time. This then leads to a proportional 10 decline in the effectiveness of selection with age due to the relatively few individuals of older age 11 contributing to the genetics of future generations, known as Hamilton's principle (Hamilton, 12 1966). Because selection removes mutations more effectively when they have a detrimental 13 phenotypic effect early on in life compared with mutations that only affect older individuals, 14 detrimental mutations accumulate (Medawar, 1952; Charlesworth & Williamson, 1975). 15 Importantly, the negative affect of these mutations may persist in post-reproductive ages, 16 contributing to the ageing phenotype.

17

18 The effect of drift on late-acting deleterious mutations is one of potential inflation of their 19 frequencies, where older age-classes suffer a greater loss of health relative to the younger age-20 classes and hence where smaller populations age at a faster rate than larger populations. Lohr et 21 *al.*, (2014) explicitly tested this hypothesis using *Daphnia magna* and, consistent with other recent 22 work (Jones et al., 2008) identified a correlation with age at first reproductive output and rate of 23 ageing across numerous wild and model organisms, which is consistent with the expectation that 24 populations with low genetic diversity have accelerated ageing. The main conclusion of Jones et 25 al., (2008) is that the onset and rate of senescence in both survival and reproduction are 26 associated with generation time, an aspect that is not usually considered with the 'pace' or 'shape' 27 of ageing in populations. Given that generation time influences N_e (Waples, 2007), where generally $N_e \propto N_{nb}T$, where N_{nb} is the number of newborns arriving in each generation and T is the 28 29 generation time (mean age of parents), then we expect effective population size to decline with 30 shorter generation times. It then becomes conceivable that the age of sexual maturity, as well as 31 the survivorship and reproductive span of a species, have consequences for the role of mutation 32 accumulation in ageing phenotypes.

1 The phenotypic effect of a mutation entering a population is dependent upon when the gene is 2 expressed, which can be age-specific (e.g., developmental genes, genes associated with sexual 3 maturity and female menopause), although not always, as when a gene's influence can be 4 cumulative (e.g., IL1RAP and its influence on amyloid plaque accumulation (Ramanan et al., 5 2015)). When the mutation has an age-specific expression, its survival depends upon the size of 6 this age-class. As a population declines in size, the age-classes that are large enough for selection 7 to dominate drift (i.e., $s > 1/2N_e$) will shift towards the younger classes. Mutations that have a 8 detrimental effect on survival and reproduction are therefore more likely to persist in the older 9 age-classes.

10

11 According to traditional ecology theory, population density governs the optimal age of maturity 12 (Macarthur & Wilson, 1967), distinguishing *r*-selected species (typically small organisms 13 producing many offspring, with early maturity and with short lifespans) from *K*-species 14 (reproduce slowly at later ages and with longer life-spans) (Pianka, 1970). Most primate species, 15 including humans, are *K*-species. This *r*/*K* categorisation can be quite sensitive to environmental 16 factors. For example, an increase in environmental stochasticity can select for an *r*-type strategy 17 (Engen & Saether, 2016). Although this *r*/*K* categorisation of life histories persists in some of the 18 ageing literature (e.g., Reichard, 2016), there is now a preference for placing species on a fast-slow 19 continuum, or tempo, of life history. One method is to use the ratio of fertility rate to age at first 20 reproduction, which among other factors is less sensitive to environmental stochasticity (Oli, 21 2004). Which of these r/K strategies, or position on the fast-slow continuum, a species adopts may 22 be highly constrained by their environment and evolutionary history. Nevertheless, we 23 hypothesise that there will have been situations, e.g., during the Neolithic period and modern 24 industrialization, where the change in culture, environment and reproductive patterns on human 25 survival would have been of sufficient magnitude that the species survivorship curve shifted, 26 resulting in consequent changes in both the 'pace' and 'shape' of their life history. The 27 consequence is that, once a modern-industrialised life-history strategy emerged, the older 28 reproductive age-classes once poorly represented in a Type-II population and potentially subject 29 to the consequences of mutation accumulation, become numerically better represented in a Type-I 30 population. Using simulations, we explore the significance of this shift on the rate of genetic drift 31 and the contribution mutation accumulation is likely to make to the ageing, or senescence, of the 32 population. The value in doing so is that any insights relating to the magnitude of influence past

1 demographic shifts have had on the present evolution of ageing in the human population would

2 better inform the choice of model organism employed in its study.

3

4 Methods

Felsenstein's method of estimating the effective population size of an age-structured population
(Felsenstein, 1971, equation 10) was used to measure the influence of generation time on the rate
of drift across populations with Type-I and Type-II survival curves:

9
$$N_e = \frac{N_{nb}T}{1 + \sum_{x=1}^{k} l_x s_x d_x v_{x+1}^2}$$
 (Eq.1)

10

11 where, for *k* age classes, *N*_{nb} is the number of newborns, $d_x = l_x - l_{x+1}$ and *v* the reproductive value: 12 $v_x = \sum_{i=1}^k l_i m_i / l_x$

13

14 Because our focus was the hypothetical shift in population type during human evolution, Type-III 15 populations were not considered in any further detail. Following convention, we consider the 16 female constituents of a population of parents and offspring. The number of females of each age 17 (x) is denoted as n_x (equivalent to the number of females that survive each age-class, s_x), with the fecundity of each age-class denoted as *m_x*. The probability of surviving *to* each age-class from birth 18 19 is l_x , which is simply $l_x = n_x/n_0$. The probability of surviving each age x is $P_x = l_x/l_{x-1}$. By convention, 20 $l_0 = 1$. For simplicity, we consider sampling the number of recruits for the next generation post-21 breeding. With a birth-pulse model, the effective fecundity of females of age *x* is $f_x = P_{x-1} . m_x$. The net reproductive rate of the population, per generation, is $R_0 = \sum l_x m_x$. Importantly, R_0 is the 22 change in population size by *generation*, *T*, where $T = \frac{\sum_{x=0}^{k} x l_x m_x}{\sum_{x=0}^{k} l_x m_x}$, and where *k* is the total number 23 of age-classes. Hence, the intrinsic rate of population growth is $r = \frac{lnR_0}{T}$. Importantly for this 24 discussion, this shows clearly that as *T* increases, the intrinsic rate of population growth (*r*) 25 26 decreases, hence, for population sizes to remain stable, as they do for our simulations, a change in 27 T requires a compensatory change in m_x .

28

29 In order to discriminate between the effect of young and old breeders on the loss of genetic

30 diversity, we explicitly explore the influence of generation time and survivorship by employing a

31 Leslie matrix approach. We use three example survivorship curves to illustrate the influence they

32 may have on the rate of genetic drift. Life history data was obtained from 1) the US female

1 population census from 2000 (Templeton, 2006), considered to be typical of a Type-I population 2 where there is high survival until late in life. 2) The Hadza female population (modelled by 3 Blurton-Jones, 2016) and, for comparison, 3) a fictional population representative of a typical Type-II population with a constant 10% mortality rate over yearly age-classes: $l_{x+1} = 0.9 \times l_x$, 4 5 designed to be similar to a wild chimpanzee population (Figure 1A). The age classes (x) are one year apart. A Type-III population was also generated for comparison in Figure 1 as $l_x = x^{-2.126}$. The 6 7 fecundity schedule, which is the tabulation of birth rates (m_x) , is manipulated similarly to Ryman 8 (Ryman, 1997), where the fecundity of each age-class of each population is adjusted such that $\sum l_x m_x = 1$. Here our focus is on the variability in survival curves, so the fecundity trajectories for 9 10 Hadza and Type-II populations are a manipulation of the US female trajectory. The US female 11 fecundity schedule is taken from Templeton (2006) and simulated as a normal distribution with 12 mean = 27 years and variance = 7 years. The simulated populations have stable age-structure and 13 constant size.

14

Assuming the age-specific survival and fecundity probabilities remain constant across generations (*t*), we track the number of females (n_x), starting with age-class x + 1, by multiplication with a Leslie matrix for 100 generations to reach a stable age distribution. We then track the frequency of two alleles, *A* and *B*, at a single locus over a 1000 year time period by multiplying our Leslie matrix L, by a mating matrix **M**, such that $\mathbf{n}(t+1) = \mathbf{LMn}(t)$ (Roughgarden, 1998):

- 20
- 21

$\langle n_{t+1,x,AA} \rangle$		$(f_{x,AA})$	١	f_{x} ,	AB	f_{i}	x, BI	f_x	+1, <i>A</i>	A	$f_{x+1,AB}$		$f_{k-1,BB}$	١
$n_{t+1,x,AB}$		0 0				0		0		0		0		
$n_{t+1,x,BB}$		0		(0		0		0		0		0	
$n_{t+1,x+1,AA}$	=	$P_{x,AA}$	4A 0		0			0		0		0		
$n_{t+1,x+1,AB}$		0		P_{x}	AB		0		0		0		0	
÷		÷					÷		÷		÷	·	:	
$\left(n_{t+1,k-1,BB}\right)$		0	0 0			0		0		0	$P_{k-1,BB}$	0	J	
		$\int p^2$	2	0	0	0	0		0)		$(n_{t,x,AA})$			
		2p	pq	0	0	0	0		0		$n_{t,x,AB}$			
		q^2	2	0	0	0	0		0		$n_{t,x,BB}$			
		× 0)	0	0	1	0		0	×	$n_{t,x+1,AA}$			
		0		0	0	0	1		0		$n_{t,x+1,AE}$	3		
		:		÷	÷	÷	÷	۰.	÷		:			
		(0)	0	0	0	0		1)		$n_{t,k-1,BE}$,)		

1 2

> As described in detail in (Roughgarden, 1998), the number of newborn females at time *t*+1 is $b_{t+1} = \sum_{x,ij} f_{x,ij} n_{t,ij}$ for alleles *i*, *j*. The allele frequencies amongst the newborn are simply the result of Mendelian segregation:

7
$$p_{t+1} = \frac{\sum_{x} f_{x,AA} n_{x,AA} + (1/2) \sum_{x} f_{x,AB} n_{x,AB}}{b_{t+1}}$$

8

6

9 This describes the random union of gametes between parents across all age-classes and maintains
10 Hardy-Weinberg genotypic ratios among the newborn, presented in the mating matrix M. We
11 performed all calculations and iterations of the matrices in *R* (R Development Core Team, 2008).
12 The R Script and input data are available from https://github.com/AndyOverall/DriftAgeStruct,
13 along with GNU public license details.

14

15 The simulation of genetic drift is a two-stage process. The first deals with the random union of 16 gametes to generate the newborn class. The second models the random culling of alleles with time 17 such that the allele frequency distribution in the breeder's age-class (e.g., $n_{t=20,x=20}$) is a random 18 subsample of the allele frequency distribution of the age class when they were newborns ($n_{t=1,x=1}$). 19 The number of newborn individuals is kept constant and takes the value of the first age-class of 20 the stable age-distribution (i.e., the one resulting from 100 iterations of the Leslie matrix 21 multiplication: $\mathbf{n}(t = 100) = \mathbf{Ln}(t = 99)$). For example, considering the US Female population, where $\sum_{x=1}^{k} n_{100,x} = 1000$, the number of newborns (age-class *x*=1) = $n_{100,1} = 13$, with the numbers 22 of genotypes being in accord with Hardy-Weinberg proportions: *n*_{100,1,AA}+*n*_{100,1,AB}+*n*_{100,1,BB} = 13. The 23 24 simulation of random genetic drift involves the random sampling of these 13 genotypes using the 25 *R* function **rmultinom**, **rmultinom**(n, size, prob). If *X* is a random variable such that *X* = 26 { n_{AA} , n_{AB} , n_{BB} }, then **X** = **rmultinom** (1, 13, $n_{AA}/13$, $n_{AB}/13$, $n_{BB}/13$) regenerates the newborn's genotypes subsequent to drift and from these genotypes the new allele frequencies are 27 28 obtained. These frequencies then feed directly into the mating matrix **M**. If P_x and m_x remain 29 constant, iterations of this procedure simulate the frequency of the alleles under the influence of 30 drift. The simulation included 1000 repeats, to model 1000 reproductive events, each iterated 31 1000 times to correspond with the passage of 1000 years.

In addition to allele frequency stochasticity occurring in the generation of newborn's genotypes, there is a random cull of genotypes between age-classes over generations. For example, with neutral alleles, the number of genotypes of age-class x=2 in generation 1 ($n_{1,2,AA}$; $n_{1,2,AB}$ and $n_{1,2,BB}$) each has a probability (P_x) of surviving to the next generation ($n_{2,2,AA}$; $n_{2,2,AB}$ and $n_{2,2,BB}$). This is simulated, in this example, by $n_{2,2,ij} = P_1 \times n_{1,2,ij}$. Then, P_x % of $n_{2,2,ij}$ remain the same genotypes, with the remaining 1 - P_x % being randomly drawn using the same R function **rmultinom**.

7

8 The simulation of selection involved a modification of the survival probability. For example, for 9 neutral alleles, the survival of the genotypes from one age-class (*x*) to the next is equal (e.g., $P_{x,AA} =$ 10 $P_{x,AB} = P_{x,BB}$). Negative selection for individuals that are homozygous for recessive alleles is 11 simulated as $P_{x,BB} < P_{x,AA}$, $P_{x,AB}$.

12

13 Figure 2 illustrates the survival curves for the three populations where the total population size is 14 *N*=1000. The middle dashed curve shows the reproductive distribution for the US female 15 population (where the y-axis frequency scale is arbitrary), which corresponds to a generation time $T = \frac{\sum_{x=0}^{k} x l_x m_x}{\sum_{x=0}^{k} l_x m_x} = 27$. Shifting the reproductive distribution either towards younger or older age-16 17 classes modified the generation times. For example, the dashed curve of Figure 2 furthest to the left shows the reproductive distribution shifted 20 years younger and, for the US females, T = 8.818 19 (referred to as T-20). When shifted 20 years towards the more elderly individuals, shown by the 20 dashed curve to the right, T = 46.8 (referred to as T+20). This manipulation separates out the 21 influence of young versus older breeders, whilst acknowledging that the corresponding 22 plausibility of such an early/late age of reproduction may be unrealistic.

- 23
- 24 Figure 2
- 25

26 Results

27

Setting N=1000 for each of the three populations, Felsenstein's estimate of N_e (Eq.1) results in a simple linear increase in N_e with generation time (T) for both Type-I populations (US and Hadza

30 females), but plateaus for the Type-II (Figure 3). This comes as no surprise for both Type-I

- 31 populations as the survivorship curve barely changes over the age-range considered here (10 60
- 32 years), and so $N_e \propto T$, as the other parameters in Eq.1 change very little with increasing *T*.

- 1 However, for the Type-II population, after an initial increase in N_e with T, the relationship plateaus
- 2 and N_e becomes largely independent of generation time as a corresponding increase in

3 reproductive value (v_x) balances the increase in N_e with T (results not shown).

4

5 Figure 3

- 6
- The expected loss of heterozygosity (*H*) over time is a function of N_e , e.g., $H_{t+1} = H_t \left(1 \frac{1}{2N_t}\right)$ 7 8 (Gillespie, 2004). However, for age-structured populations, the number of newborns (N_{nb}) and 9 reproductive values (*v_x*), as well as generation time influence estimates of *N_e*. Although Felsenstein 10 (and others, e.g., (Hill, 1972) have formulated estimates of *N*^{*e*} for age-structured populations, it is 11 not immediately obvious how this translates to a loss of heterozygosity over time. For *N*=1000, the 12 estimate of *N_e* is larger for the Type-II population than Type-I populations across the generation 13 times considered here (Figure 3), leading to the expectation that drift would proceed at a slower 14 rate for the Type-II population. Figure 4A shows the decline in mean heterozygosity over time for 15 populations of early (T-20) and late (T+20) breeding individuals across the three populations. 16 Figure 4B presents notched boxplots to summarise the distribution of heterozygosity values at the 17 final time point (Time = 1000) for 1000 replicates. The "notch" of the

18 boxplots span the 95% confidence interval of the median and the box itself spans the interquartile 19 range. Informally, if the notches do not overlap, then it is considered that the medians differ with 20 95% confidence. These plots show that for the Type-I populations, the earlier breeding 21 populations lose heterozygosity, on average, at a markedly greater rate than later breeding 22 populations and that these earlier breeding populations are highly variable in the rate of this loss. 23 However, for Type-II populations, the distribution of heterozygosity values for populations with 24 early breeders is indistinguishable from that of late breeding populations. For early breeding 25 populations (T-20), the rate of loss is consistent with the Felsenstein N_e estimates presented in 26 Figure 3: the smaller the *N_e*, the greater the rate of loss of heterozygosity. However, Figure 4A 27 shows that for later breeding populations this is not the case and in fact the rate of drift is not 28 accurately predicted from estimates of *N_e*, with US females drifting the least and Type-II the most. 29

- 30 Figure 4
- 31

1 With the introduction of negative selection into the simulations, we expect to see heterozygosity 2 lost at a greatest rate in populations where $s > 1/2N_e$ and to be independent of population type 3 when s >> $1/2N_e$. When the recessive mutation reduces the survival of breeding individuals 4 homozygous for this mutation ($P_{x,BB}$) by 0.1% (s), the rate at which heterozygosity is lost is not 5 altered noticeably (result not shown). However, Figure 5A shows the decline in heterozygosity 6 when s = 1% for early (T-20) and late (T+20) breeding populations where, as predicted, 7 population type is still having some influence, more noticeably for the T+20 populations where the 8 distribution of heterozygosity values at time point *t*=1000 are distinct between Hadza and Type-II 9 (Figure 5B).

10

11 Figure 5

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14 **Discussion**

The two main genetic causes of senescence, antagonistic pleiotropy and mutation accumulation, 15 16 have different expectations with regard to the frequency distribution of mutations that are 17 deleterious to the older age-classes of a species (Rodriguez et al., 2016). Here we considered the 18 consequence of population 'type' on the rate of drift in light of this influence on mutation 19 accumulation. We hypothesised that the human survivorship curve has shifted relative to pre-20 industrialised and hunter-gatherer populations and possibly further back in time from ancestral 21 populations that had survivorship curves more akin to chimpanzees. The literature on the theory 22 underpinning estimates of *N_e*, the rate-determining parameter of drift, is extensive (e.g., Engen et 23 al., 2005), but there has been little attention paid towards the influence of population type (e.g., 24 those that fit the ecological Type-I, II and III survivorship ideals). The potential importance of this 25 lay in the fact that most ageing studies have an understandable bias towards human ageing, but 26 the industrial-age human population type is unusual in being an extreme example of Type-I (see 27 Figure 1). Not only is this shift in population type likely to have consequences for the rate of 28 mutation accumulation, there are also consequences relating to the appropriate choice of 29 organism used to model the ageing of human populations. For example, a model organism's 30 evolutionary history shapes its life history, including its survivorship. Ancestral population type 31 may then contribute to the genetic causes of the model organism's senescence, which may be at 32 variance with the evolutionary history of humans.

33

1 When Type-I and Type-II age-structured populations are of comparable size (e.g., *N*=1000), then 2 the number of newborns (N_{nb} , age-class x=1) in Type-I populations are fewer than the N_{nb} of Type-II populations (Figure 2). The relationship: $N_e \propto N_{nb}T$ (Felsenstein, 1971) predicts that Type-I 3 4 populations will drift at a greater rate than Type-II populations. Figure 3 shows the results of 5 applying Felsenstein's estimate of N_e to the three population types showing that Type-I and Type-6 II populations differ in how sensitive these estimates of *N*_e are to changes in generation time, with 7 the allele frequencies in Type-II populations drifting almost independently of generation time 8 throughout the majority of the age range considered here. The reason for this is that the 9 reproductive value of the breeding individuals (v_x in the denominator of Eq.1) differs markedly 10 between the young and elderly of a Type-II population relative to that of a Type-I. For the 11 scenarios presented here, where populations are constrained to remain at a constant population 12 size (e.g., *N*=1000), an elderly breeder in a Type-II population is required to make a much greater 13 contribution to the next generation in terms of offspring number, relative to an elderly breeder in 14 a Type-I population. Hence, the increase in the reproductive value in Type-II populations balances 15 the increase in N_e expected as a consequence of an increase in generation time (numerator of 16 Eq.1), which is why the relationship between these two parameters (T and N_e) weakens (Figure 3).

17

18 Figure 4 shows the results of drift simulations for the populations presented in Figure 3 (modern 19 US females, Hadza females and a Type-II population). For the populations with an early generation 20 time (T-20, solid lines, Figure 4A) the rate of drift corresponds with estimates of *N*_e presented in 21 Figure 3. However, for the populations with a later generation time (T+20, dashed lines, Figure 4), 22 the mean rates of drift are the opposite of expectations based purely on the relative magnitudes of 23 *N_e* (Type-II > Hadza females > US females), although the distributions of 1000 simulations 24 performed here do overlap (Figure 4B). It is not obvious what the cause of this reversal of mean 25 heterozygosity value is. However, the ordering of the populations in terms of their rates of drift 26 does appear to correspond with the number of breeders (*N*_{Breeders}), indicated by the overlapping 27 reproductive distributions in Figure 2. For example, considering the T-20 populations, the number 28 of breeders throughout the reproductive distribution (dashed lines, Figure 2) is ordered as Type-II 29 > Hadza females > US females. However, the number of breeders throughout some of the T+20 30 population's reproductive distribution shows a reversed ordering. Taken together, the plots in 31 figures 3 and 4A illustrate the magnitude of difference that population types have on the rate of 32 drift and indicate a few subtleties that may be difficult to predict directly from Felsenstein's 33 estimate of *N_e*. This outcome appears to be a simple consequence of the fact that, despite having

equal census sizes (*N*), populations with differing N_{nb} / $N_{breeders}$ ratios will drift at differing rates and that population 'type' captures this ratio.

3

4 For mutations that are selectively neutral with regards to the breeding individual's probability of 5 survival (i.e., those implicated in mutation accumulation), a shift in survivorship from a Type-II to 6 a Type-I, all else being equal, will correspond with an increase in the rate of drift unless this shift also corresponds with an increase in generation time (Figure 4A). A corresponding increase in 7 8 generation time reduces the rate of drift for Type-I populations. Going from a Type-II to Type-I 9 population, the 'pace' of life decreases as life expectancy increases, but the 'shape' steepens 10 indicating an increase in the strength of ageing (Baudisch, 2011, see Figure 1B & 1C). This shift in 11 population from Type-II to Type-I, therefore, corresponds to an increase in senescence. With 12 Type-I populations, unlike Type-II, the contribution that mutation accumulation makes to 13 senescence does appear to be sensitive to generation time. It follows that Type-I populations with 14 younger generation times will experience drift at a greater rate than those with older generation 15 times and hence a greater contribution of mutation accumulation to senescence is expected. 16 Considering the transition from a pre-industrial / hunter-gatherer human population to a modern 17 industrialised population, this also results in a shift towards slower pace and steeper shape 18 (Figure 1). However, the drift simulations suggest that, in terms of the rate of the heterozygosity 19 loss, this shift does not correspond to a marked change in the contribution mutation accumulation 20 may make to senescence. Although the pace/shape metrics used to tease apart how fast and how 21 strongly populations senesce indicate an almost linear change from Type-II to pre-22 industrial/hunter-gatherer to modern populations (Figure 1B & 1C), our results suggest that the 23 contribution of mutation accumulation to senescence is dependent upon population type and, for 24 Type-I populations, this is also dependent upon generation time. Modern human populations may 25 have 'pace' and 'shape' metrics distinct from pre-industrial/hunter-gatherer populations, but both 26 Type-I populations drift at similar rates and are equally sensitive to generation time (Figure 4). 27

The relationship $s > 1/2N_e$ describes the conditions required for selection to dominate drift in allele frequency evolution. However, as we have shown, the relative rates of drift between agestructured populations do not always correspond to the relative effective sizes. Figure 5A shows that when negative selection (*s*=0.01) is experienced, the rate at which the mutation is lost from the populations still bears the hallmarks of the differential rates of drift between population types. For the older breeding populations (T+20), the Type-II and Hadza populations have noticeably distinct distributions of heterozygosity values at time point t=1000 (Figure 5B). With strong selection (e.g., s=0.1), as predicted, selection dominates the loss of heterozygosity and all three populations evolve at a similar rate and with similar sensitivity to generation time (result not shown). Hence, unless selection is strong relative to $1/2N_e$, population type will continue to influence the allele frequency distribution of detrimental alleles.

6

7 Our treatment of life-table, actuarial senescence is possibly naive in that it simply relates to the 8 increased mortality with age, but is nevertheless consistent with a large body of literature drawn 9 upon for this study (e.g., Baudisch, 2011; Wrycza, 2015; Colchero et al., 2016). More sophisticated 10 analyses of senescence, based upon detailed life history data, have arisen that move away from 11 this traditional life-table approach where, for example, generation time was identified as capturing 12 the 'speed of living' and to be tightly associated with the onset and rate of senescence (Jones et al, 2008). One explicit metric of this is the ratio of fertility rate to age at first reproduction (F/ α). 13 14 Because *α* is proportional to generation time (*T*), this 'pace of life' metric slows with increasing *T*. 15 This result is consistent with ours, although we consider this in terms of the rate of drift. Metrics 16 such as F/α are valuable in predicting the rate of senescence, but they do not tease apart the 17 genetic underpinnings of senescence. We show that a population's sensitivity to drift and 18 generation time is a function of its 'type', which in turn relates to the relative importance of 19 mutation accumulation as a cause of senescence.

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21 Our focus in this paper has been on the contrast between Type-I and Type-II survivorship curves. 22 It remains to be explored how variation in the reproductive distribution (other than just 23 generation time) influences drift. Although the reproductive distribution employed throughout 24 this manuscript corresponds well with modern and pre-industrialised human populations, the 25 chimpanzee reproductive distribution is quite different as it spans their entire adult life 26 (Bronikowski et al., 2016). Fitting a modern reproductive distribution to a Type-II population is 27 likely to be an unrealistic contrivance and in need of further investigation. Nevertheless, the 28 general principle that manipulating survivorship and generation time can influence the relative 29 contribution of mutation accumulation to senescence opens up the possibility of laboratory 30 investigations that could have some bearing on the evolution of human senescence. 31

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4

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23 Figure Legends

- 24
- 25 **Figure 1**
- 26 A. Comparison of survivorship curves for six populations. The US females from 2000 (black,
- 27 Templeton, 2006) represent a Type-I population. The Swedish females from 1751 (orange, Human
- 28 Mortality Database (http://www.mortality.org)) and Hadza females (blue, Blurton-Jones, 2016) represent

1 Type-I populations prior to the increased longevity seen in modern populations. The wild

- 2 Chimpanzee (purple, Bronikowski et al, 2016) represents our closest living species. The Type-II
- 3 population (red, simulated (see Methods for details)) is used as a close approximation of the
- 4 chimpanzee population and the Type-III population (green, simulated (see Methods for details)) is
- 5 used for completion as a comparator at the other end of the 'type' spectrum. B. A continuum of
- 6 lifespan equality $(\ln(1/H))$ and life expectancy in six populations presented in A. C. A comparison
- 7 of 'pace' (life expectancy) and 'shape' (ratio of longevity to life expectancy) for six populations in A.
- 8

9 Figure 2

10 Survivorship curves for three populations: US Female population from 2000, Hadza females and a

11 Type-II population with survivorship of $l_{x+1} = 0.9 \times l_x$. Age (x) is in years. Central dashed curve

12 shows the reproductive distribution of the US female population, where the frequency scale on the

13 y-axis is arbitrary. Left hand curve shows the reproductive distribution shifted 20 years earlier (T-

- 14 20) and the right hand curve shows the reproductive distribution shifted 20 years later (T+20).
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16 **Figure 3**

17 The change in N_e with generation time for three population types: US Female population from

18 2000, Hadza females and a Type-II population with survivorship of $l_{x+1} = 0.9 \times l_x$. Each population

19 has a total population size of *N*=1000. Generation = generation time calculated as $T = \frac{\sum_{x=0}^{k} x l_x m_x}{\sum_{x=0}^{k} l_x m_x}$.

20

21 **Figure 4**

A. Mean decline in heterozygosity from 1000 age-structured simulations where the starting

frequency is $P_B = 0.5$, N = 1000, where reproductive distributions have been shifted towards the

young (T-20, solid lines) and the old (T+20, dashed lines). Time is in years. B. Notched boxplots

- summarising each of the 1000 simulations run for each population. The black, blue and red dots
 indicate the means for the US, Hadza and Type II populations respectively.
- 27
- 28 Figure 5
- A. Mean decline in heterozygosity from 1000 age-structured simulations where the starting
- 30 frequency is $P_B = 0.5$, N = 1000, where reproductive distributions have been shifted towards
- 31 the young (T-20, solid lines) and the old (T+20, dashed lines). Homozygous individuals
- 32 (*BB*) have a reduced survival probability (*s*=0.01). Time is in years. B. Notched boxplots

1	summarising each of the 1000 simulations run for each population. The black, blue and red
2	dots indicate the means for the US, Hadza and Type II populations respectively.
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Figure 1A





1 Figure 1B



1 Figure 1C









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1 Figure 4



1 Figure 5

