

International Handbook of Mathematical Learning Difficulties

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Pekka Räsänen
Editors

International Handbook of Mathematical Learning Difficulties

From the Laboratory to the Classroom

Foreword by Brian Butterworth

 Springer

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