

Global ocean heat transport dominated by heat export from the tropical Pacific

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Effective Ocean Heat Transport Revealed

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1 **One of the primary mechanisms by which oceans regulate Earth’s climate is**
2 **through redistribution of heat. However, interpretation of ocean heat trans-**
3 **port (OHT) has been obscured by internal heat loops that are confined within**
4 **the ocean and are not directly relevant to Earth’s energy budget. Here we elim-**
5 **inate these internal heat loops to reveal the net effects of OHT as part of the cli-**
6 **mate system, the effective OHT. Our result challenges the previous paradigm,**
7 **which emphasized global conveyor belt concepts, by highlighting that pole-**
8 **ward OHT within the Pacific is four times as large as any inter-oceanic or**
9 **inter-hemispheric OHT. This shift in interpretation implies that efforts aimed**
10 **at monitoring and estimating OHT changes in the Pacific should be priori-**
11 **tized. Furthermore, our analysis framework bridges a gap between direct es-**
12 **timation of OHT from oceanic measurements and indirect estimation of OHT**
13 **via atmospheric energy budgets. It provides means to calibrate otherwise in-**
14 **consistent OHT estimates, which will allow for more meaningful model-data**
15 **comparisons.**

16 The Ocean plays an important role in redistributing heat within the evolving climate sys-
17 tem (1). Perhaps most importantly, it transports heat from the equator, where oceans take up
18 heat in excess, towards higher latitudes where heat gets released to the atmosphere. This is
19 clearly seen in observational estimates of global meridional ocean heat transport (OHT) which
20 is directed poleward in both Hemispheres (2, 3). However, interpretation of measurements can
21 be more complicated when looking at individual ocean basins since seawater can loop around
22 land masses. This difficulty has lead to highly uncertain depictions of regional OHT contribu-
23 tions in the scientific literature (4), but the analysis presented here provides a framework to help
24 reconcile previous estimates.

25 The two following examples illustrate how regional OHT contributions may, or may not
26 play a role in Earth's energy budget. First, consider the case of OHT converging into an ocean
27 basin to balance out heat release to the Atmosphere. Such OHT contributions play an important
28 role in Earth's energy budget (5, 6). Second, consider a situation where seawater parcels loop
29 around a land mass with unchanged temperatures in the ocean interior – e.g., around Australia
30 in the counterclockwise direction. The seawater parcels would transport their internal energy
31 northward in the Pacific only to return it southward in the Indian. Owing to internal cancellation
32 between northward and southward OHT contributions within the ocean, such mass fluxes have
33 no direct impact on Earth's energy budget.

34 Mass fluxes can thus obscure the most relevant, convergent or divergent OHT contributions.
35 Furthermore, any oceanic section is potentially affected by this issue in ways that are not easy to
36 predict given the complex, present-day arrangement of land masses. Freshwater may also tem-
37 porarily leave the Ocean via evaporation to re-enter it elsewhere via precipitation, and closing
38 such ocean-atmosphere loops (7) can, in and of itself, introduce non-zero mass fluxes through
39 any oceanic section. Consequently, OHT through any oceanic section is a priori sensitive to
40 the choice of an energy reference level (ERL; i.e., conditions of temperature, pressure, etc.,

41 at which energy is defined as zero by convention) which often requires careful treatment, for
42 example to ensure energy conservation in climate models (8).

43 The need to adequately account for mass fluxes has long been recognized in the oceano-
44 graphic literature, where various approaches have been proposed to treat non-zero mass fluxes
45 across OHT sections (9, 10). One method is to adjust the net mass flux through each section to
46 near zero (11, 12). Another approach is to pair sections with one another, aiming to cancel out
47 non-zero mass flux contributions, and focus on OHT convergence between sections. This is of-
48 ten done by pairing various sections with Bering strait or the Indonesian Through Flow (4, 13).
49 Alternatively, in cases such as Drake Passage where simply adjusting to zero mass flux is not
50 sensible and there isn't an obvious pairing section, one may opt to introduce a distinctive tem-
51 perature transport scale sometimes denoted as 'PWT' (4, 13). These heterogeneous treatments
52 of OHT can render comparison amongst estimates difficult and contribute to large uncertainties
53 and unexplained differences between estimates (4, 6).

54 **Methods And Data** Progress in understanding OHT can be made, instead, through a system-
55 atic decomposition of OHT over the global ocean into divergent and rotational components as
56 done here using a gridded data product (supplementary material, SPM, sections 1-2). In prac-
57 tice, this simply involves computing the vertical integral and lateral divergence of the gridded
58 OHT estimate and then solving a Poisson equation. Similar Helmholtz decomposition technics
59 have been used in the atmospheric and oceanic literature to decompose various fluxes (14–16).
60 Here we present a novel application of this approach to a recent observational estimate of OHT
61 over the 1992-2011 period. This gridded OHT estimate is part of a global ocean state estimate
62 that agrees, within expected uncertainty ranges, with the bulk of available ocean observations
63 collected between 1992 and 2011, including millions of Argo profiles and complementary satel-
64 lite data, as well as with atmospheric re-analysis estimates (17–24).

65 The ocean state estimate includes global vector fields of OHT associated with dynamically
66 consistent heat budgets, which is crucial for our purpose. This allows us, for instance, to readily
67 verify that the divergence of OHT balances out regional air-sea heat fluxes to a good approxi-
68 mation while the other terms, from heat storage and the divergence of mass fluxes, are compara-
69 tively small on average over 20 years (SPM section 3). Hereafter, we denote the divergent OHT
70 component, which approximately balances out air-sea heat fluxes, as effective OHT (effOHT).
71 It will be compared with raw ocean heat transport (rawOHT) which also includes the rotational
72 OHT component ($\text{rawOHT} = \text{effOHT} + \text{rotOHT}$). We come back to rotOHT and its interpretation
73 later on in the paper. By convention, ERL is set to the energy of liquid water at 0°C. Importantly,
74 effOHT, unlike rotOHT or rawOHT, is insensitive to this choice (SPM section 4).

75 **Transport Maps** Values of effOHT and rawOHT are coarsely charted in Fig. 1 and tabulated
76 in SPM. By construction, effOHT and rawOHT yield the exact same divergence field, shown
77 as contours in Fig. 1. For example, 1.46 PW diverges from the tropical Pacific while 0.11 PW
78 converges into the Atlantic for both the red and the blue charts in Fig. 1. They are also identical
79 when integrated all the way around the globe (e.g., black curve in Fig. 2). Nevertheless, effOHT
80 and rawOHT provide fundamentally different perspectives on regional influences, due to the
81 prominence of internal oceanic heat loops in rawOHT, as evidenced by Fig. 1. The rawOHT
82 values generally fit well within the range of previously published “direct” estimates (4, 11–13,
83 25), whereas effOHT rather corresponds to “indirect” estimates (3–6).

84 Owing to the presence of the Atlantic Meridional Overturning Circulation (AMOC), which
85 brings relatively warm water into the Northern Hemisphere and returns colder water back into
86 the Southern Hemisphere, Atlantic OHT is northward across the Equator and in both Hemi-
87 spheres (13, 26, 27) as seen in Figs. 1-2. In the Pacific, large amounts of heat enter the Ocean
88 through the sea surface in the Tropics (black contours in Fig. 1). Based on rawOHT, most of

89 this heat uptake (1.20 PW out of 1.46 PW) appears to be transferred to the Indian ocean via
90 the Indonesian Through Flow (ITF). The Southern Ocean also stands out for its large eastward
91 rawOHT, with values ranging between about 1 and 2 PW seen around Antarctica. But, these
92 values are highly sensitive to ERL choices, so much so that setting ERL to 3.5°C, the approxi-
93 mate global mean ocean temperature, instead of 0°C suffices to reverse the direction of rawOHT
94 over the Southern Ocean (SPM section 4). This is not the case for effOHT which is much less
95 affected by non-zero mass fluxes (SPM sections 3-4).

96 Eliminating internal oceanic heat loops reduces inter-ocean exchanges to second-order terms
97 in effOHT (red chart in Fig. 1); hence, the Pacific merely provides 0.2 PW to each of the
98 Atlantic, Arctic, and Indian. The direction of effOHT in the South Pacific is reversed as com-
99 pared with rawOHT (poleward instead of equatorward) while poleward effOHT is much smaller
100 than rawOHT would suggest in the Indian (0.23 versus 1.33 PW at 30°S; a factor ≈ 6 re-
101 duction). These differences are linked to an anticlockwise loop of ocean circulation around
102 Australia (13, 28) which is here estimated to contribute ≈ 1.1 PW rawOHT with a 0°C ERL.
103 Omitting this heat loop reveals that the net effect of the tropical connection between Pacific and
104 Indian, the ITF, is only a small contribution to Earth's energy balance (0.10 PW effOHT).

105 In the Southern Ocean, at all longitudes, effOHT is again much smaller than rawOHT, due
106 to the omission of a ≈ 1.3 PW heat loop around Antarctica. This shift reveals that heat loss to
107 the atmosphere in the southern Pacific sector is sustained by heat uptake in the tropical Pacific
108 rather than by heat sources in the southern Indian sector as might have been inferred from
109 rawOHT (29, 30). In fact, westward effOHT from the southern Pacific is found to sustain heat
110 loss in the southern Indian – not the other way around. There is virtually no effOHT between the
111 Indian and the Atlantic (0.01 PW). Finally, westward effOHT from the southern Pacific to the
112 Atlantic via Drake Passage explains about half of the heat convergence into the South Atlantic;
113 the other half is provided locally by heat uptake from the atmosphere.

114 **Meridional Transports** The respective roles played by the Atlantic, Pacific, and Indian in
115 transporting heat poleward also need to be revisited (Fig. 2). Estimates of rawOHT indeed
116 suggest that only the Indian Ocean transports heat poleward in the Southern Hemisphere (e.g.,
117 see blue chart in Fig. 1). On the contrary, poleward effOHT in the South Pacific (0.69 PW at
118 30°S) overpowers that in the Indian (0.23 PW at 30°S) as is clearly seen in Fig. 2. Furthermore,
119 inter-hemispheric symmetry becomes evident in the Pacific based on effOHT, with poleward
120 transport ≈ 0.7 PW at 30°N and 30°S, and near zero cross-equatorial transport (0.02 PW).

121 Another noteworthy shift occurs in the Northern Hemisphere where poleward effOHT is
122 larger in the Pacific than in the Atlantic (Fig. 2) whereas rawOHT would suggest the opposite
123 according to our estimate (Fig. 1 and SPM). This shift reflects the omission of a ≈ 0.2 PW heat
124 loop which is directed northward throughout the Atlantic, crosses the Arctic, and comes back
125 southward in the Indo-Pacific. As a result, the Pacific is found to account for two-thirds of heat
126 converging into the Arctic (0.20 PW out of 0.29 PW) where it can participate in melting Arctic
127 sea ice (31).

128 The most relevant gauge for AMOC-related OHT is provided by effOHT at the equator
129 where wind-driven OHT is expected to be small. This yields an estimate of 0.39 PW for the
130 AMOC-related OHT which approximately balances out (a) 0.27 PW atmospheric heat uptake
131 in the southern Atlantic sector plus 0.19 PW provided by the Pacific and (b) 0.34 PW heat loss
132 to the Atmosphere in the North Atlantic plus 0.09 PW diverging to the Arctic. Such small inter-
133 hemispheric and inter-oceanic OHT magnitudes (< 0.4 PW) challenge the notion that AMOC-
134 related OHT must play a crucial role in regulating the global climate system (1). Poleward heat
135 transport within the Pacific is a much bigger term (> 1.6 PW in total).

136 Subtracting 0.39 PW from effOHT throughout the Atlantic in turn yields an estimate of
137 0.33 PW (resp. 0.30 PW) for the northern (resp. southern) subtropical wind-driven cells, which
138 is consistent with previous findings that the inter-hemispheric AMOC only represents $\approx 50\%$

139 of the peak OHT in the Atlantic (13, 27). Interestingly, 0.30–0.33 PW is also $\approx 50\%$ of the
140 corresponding value for the Pacific subtropical wind-driven cells (0.7 PW). Such proportionality
141 is hypothesized to reflect that the Pacific is about twice as wide as the Atlantic along the Equator
142 where oceanic heat uptake is concentrated. Hence, the gyre systems of the Pacific and Atlantic
143 appear to redistribute tropical heat uptake with approximately the same efficiency.

144 **Heat Loops** The rotational OHT component estimate ($\text{rotOHT}=\text{rawOHT}-\text{effOHT}$) provides a
145 global mapping of internal oceanic heat loops (grey contours in Fig. 3). By construction, it is
146 divergence-free and yields zero global meridional transport. When ERL is set to 0°C as in Fig. 3,
147 the patterns of rotOHT highlight familiar features of the wind-driven ocean circulation that can
148 connect and even shape up regions of air-sea heat uptake and loss (16, 28, 32). Subtropical
149 gyres and the associated shallow overturning circulations notably set up the global hemispheric
150 pattern of poleward OHT (27) and are clearly reflected in rotOHT (Fig. 3). This provides an
151 interpretation for the westward orientation of effOHT at mid-latitudes (recall that the divergent
152 component of a vector field is orthogonal to the scalar potential; effOHT thus goes from red
153 to blue contours in Fig. 3) as a result of subtropical gyres releasing heat received in the tropics
154 primarily via their western boundary currents and associated mode water formation sites (33).

155 **Perspectives** Our analysis bridges the gap between two contrasting depictions of OHT which
156 tend to emerge either from an atmospheric perspective (3) or from an oceanic perspective (2).
157 By deriving both of them, effOHT and rawOHT, from the same gridded data product we show
158 that apparent conflicts amongst earlier estimates may in part reflect comparison of apples with
159 oranges (see Fig. 1 and Tables in SPM). The Helmholtz decomposition methodology provides
160 a framework to resolve such differences. The underlying Poisson equation approach alleviates
161 uncertainty associated with arbitrary boundary condition and ERL choices in previous studies
162 (see SPM section 4). Applying it to full oceanic heat budgets notably shows that inferring

163 effOHT from air-sea fluxes implies an uncertainty of $\pm 0.3PW$ associated with mass fluxes and
164 heat storage variations (SPM section 3).

165 A remaining challenge, however, is the lack of practical methods to accurately quantify OHT
166 uncertainties that derive from limited ocean data coverage, uncertain air-sea fluxes, and imper-
167 fect estimation methods. Progress on this issue could be made by leveraging the Helmholtz
168 decomposition methodology employed here to analyze OHT differences amongst ocean data
169 assimilation products (34). From a sea-going oceanography perspective, the availability of ro-
170 tOHT estimates may also help circumvent the fact that, due to the fundamentally global nature
171 of Earth's energy budget, effective OHT cannot be observed locally by an individual section.
172 Subtracting, for example, the rotOHT estimate shown in Fig. 3 from ship-based OHT estimates
173 would indeed provide a systematic method to convert them into effOHT estimates – a promis-
174 ing alternative to the heterogeneous and sometimes ad-hoc treatments of non-zero mass fluxes
175 found in the oceanographic literature.

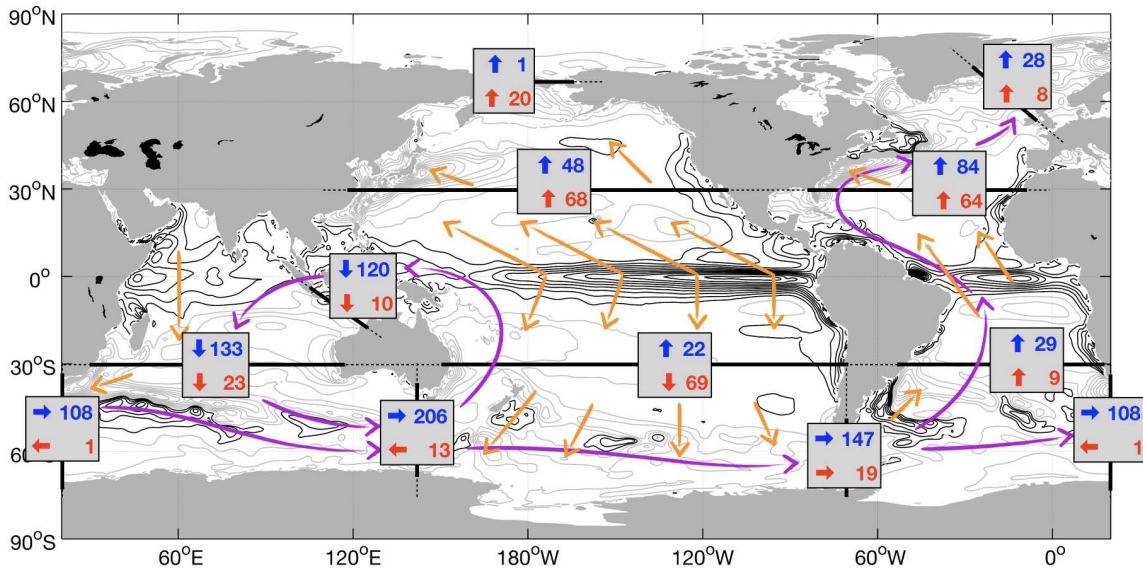


Figure 1: Ocean heat transport (OHT in 0.01 PW; 1 PW= 10¹⁵ W) as estimated through gates that separate ocean basins and through meridians that delimit the tropics (thick black lines) for the 1992-2011 time mean. Raw OHT (rotational+divergent components) and effective OHT (divergent component only) values are charted in, respectively, blue and red. Thin lines with arrow heads are a schematic of the main internal oceanic heat loops (purple) and effective OHT patterns (orange). Black contours (resp. grey contours) represent the rate of ocean heat divergence (resp. convergence) which reflects the rate of heat uptake from (resp. heat release to) the atmosphere. These rates are contoured every 15 W/m² intervals starting from ±5 W/m².

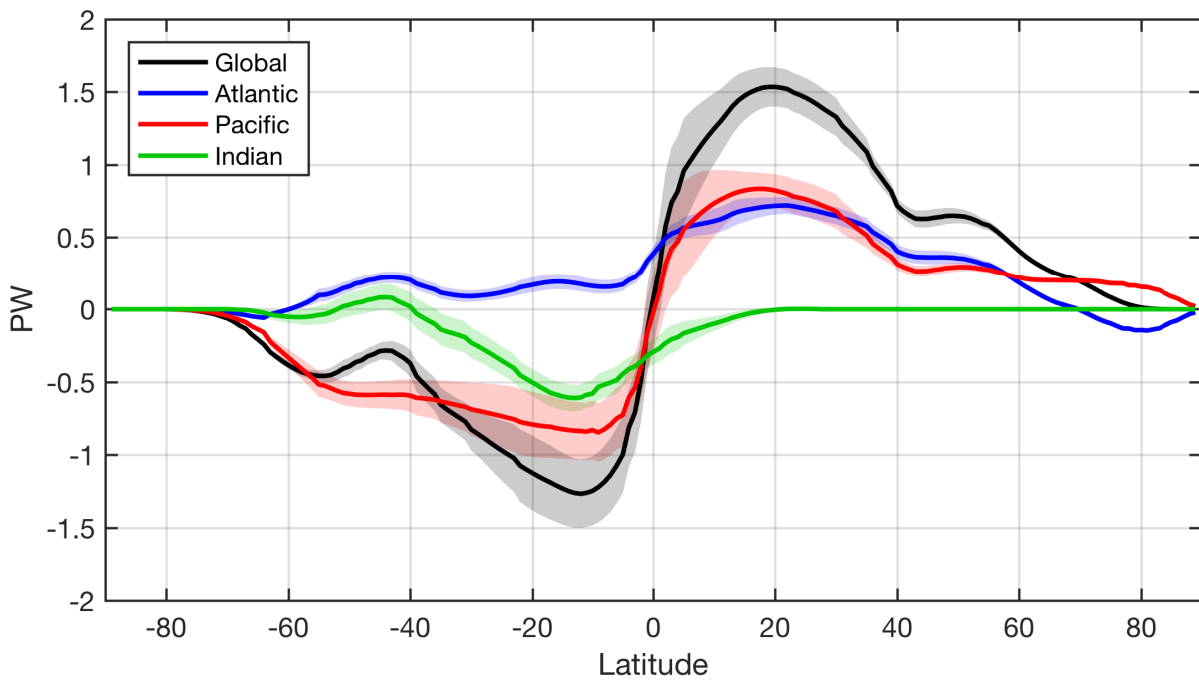


Figure 2: Meridional ocean heat transport (OHT; in PW) for the global ocean is depicted in black. Also shown: meridional effective OHT for the Atlantic (blue), Pacific (red), and Indian (green) sectors. Thick lines denote the 1992-2011 mean and shaded ranges reflect ± 1 standard deviation amongst annual means.

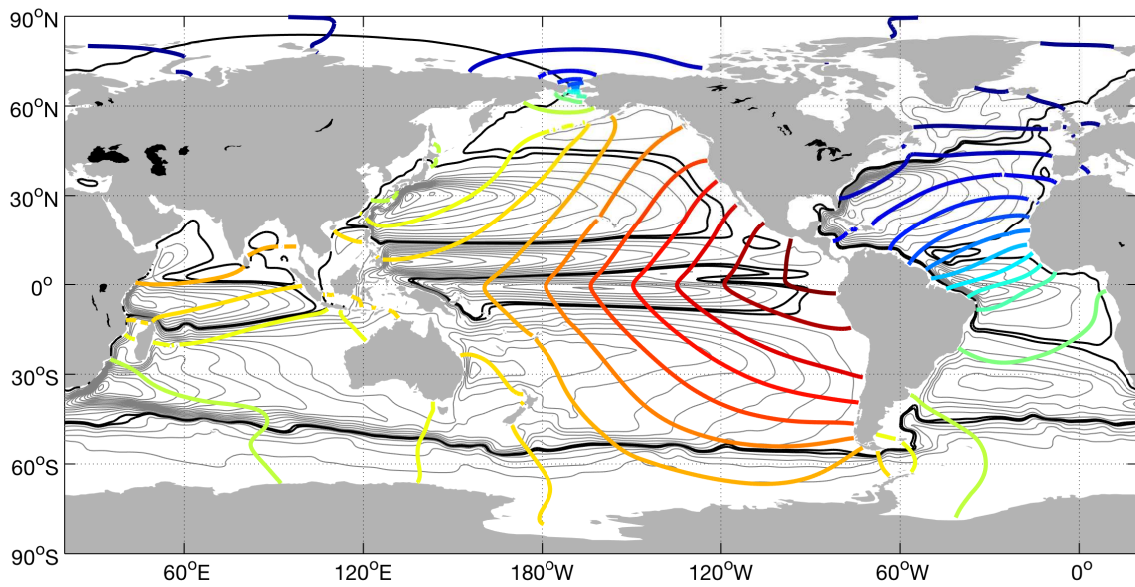


Figure 3: Scalar potential (colored contours; in 0.2 PW intervals) and vector potential (black and grey contours; in 0.05 then 0.2 PW intervals) as derived from the global vector field of rawOHT averaged over 1992-2011. The scalar and vector potentials determine, respectively, effOHT and rotOHT (see SPM, section 2). Each contour of the vector potential can be thought of as a heat loop confined within the ocean. In contrast, effOHT is oriented perpendicularly across contours of the scalar potential and directed from red to blue contours.

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Supplementary Material For *Effective Ocean Heat Transport*

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1 Ocean State Estimate

2 Our analysis is based on the ECCO version 4 release 2 gridded data product (1, 2). The ECCO v4
3 ocean state estimate agrees, within expected uncertainty ranges, with the bulk of available ocean
4 observations as well as with atmospheric re-analysis data over 1992-2011. It includes a full set
5 of optimized transport estimates across the sea surface and in the ocean interior along with
6 recent estimate of geothermal heat fluxes (3) applied at the sea floor. The chosen, adjoint-
7 based estimation methodology does not rely on *assimilation increments* (4) but rather optimizes
8 surface forcing fields and internal model parameters (1, 5, 6). As a result, the ECCO v4 product
9 offers closed heat budgets where the convergence of transports matches the ocean state evolution
10 to machine precision.

11 The underlying configuration of the MIT general circulation model (1, 7) uses the “real
12 freshwater flux” formulation, accounting for mass fluxes across the sea surface associated with
13 precipitation, evaporation, run off, and sea ice freezing and melting. However, as commonly

14 done in climate modelling, the model makes the Boussinesq approximation and neglects spe-
 15 cific heat capacity variations (1, 5). In practice, this means that for any given volume element
 16 V the corresponding heat content is simply given by $H = \rho_c C_p \theta V$ where ρ_c is the constant
 17 Boussinesq density, C_p the constant specific heat capacity, and θ the potential temperature av-
 18 eraged over V . Accordingly, if \mathbf{U} denotes a volume flux across the sea surface or in the ocean
 19 interior then the corresponding mass flux is given by $\mathbf{M} = \rho_c \mathbf{U}$. In this paper, we follow
 20 common oceanographic usage by referring to $\rho_c C_p \theta \mathbf{U}$ simply as *heat transport* rather than as
 21 *approximation of total energy transport* which would be more rigorous (8, 9).

22 All variables needed for the presented analyses are permanently archived (10, 11) and readily
 23 available for download via the ECCO website (<http://ecco-group.org/>).

24 **2 Computation of the divergent and rotational transports**

25 First, we sum up all monthly-averaged advective and diffusive transports of potential tempera-
 26 ture (10), multiply them by $\rho_c C_p$, integrate vertically, and form annual averages from 1992 to
 27 2011. The resulting vector fields are referred to as rawOHT in this article and as \mathbf{F} in equations
 28 reported below. As is classically done in Helmholtz decomposition, we then separate \mathbf{F} into a
 29 divergent component, \mathbf{F}_{div} , and a rotational component, \mathbf{F}_{rot} :

$$\mathbf{F} = \mathbf{F}_{div} + \mathbf{F}_{rot} \quad (1)$$

30 satisfying:

$$\nabla \times \mathbf{F}_{div} = 0 \text{ and } \nabla \cdot \mathbf{F}_{rot} = 0 \quad (2)$$

31 These components are associated with a scalar potential, \mathcal{P} , and a streamfunction, \mathcal{S} , such that:

$$\mathbf{F}_{div} = \nabla \mathcal{P} \quad (3)$$

$$\mathbf{F}_{rot} = \nabla \times \mathcal{S}. \quad (4)$$

32 In practice, the scalar potential, \mathcal{P} , is computed by solving, over the global ocean, the Pois-
33 son equation:

$$\nabla^2 \mathcal{P} = \nabla \cdot \mathbf{F} \quad (5)$$

34 obtained by taking the divergence of Eq. (1) and using Eqs. (2-3). The divergent component,
35 \mathbf{F}_{div} , is then readily derived from \mathcal{P} using Eq. (3); it is referred to as effOHT in this article.
36 Finally, the rotational component is computed as the remainder, $\mathbf{F}_{rot} = \mathbf{F} - \mathbf{F}_{div}$, and integration
37 of its transverse component along grid line paths readily gives \mathcal{S} .

38 The Poisson equation is formulated such that \mathbf{F}_{div} obeys a zero normal flow boundary condi-
39 tion at the coastline over the global Ocean. This choice makes the most immediate physical and
40 practical sense as argued by (12). It is indeed consistent with the underlying zero normal flow
41 boundary condition for \mathbf{F} in the ocean model, so that the rotational component, $\mathbf{F}_{rot} = \mathbf{F} - \mathbf{F}_{div}$,
42 also satisfies a zero normal flow boundary condition. Hence, \mathbf{F} , \mathbf{F}_{div} , and \mathbf{F}_{rot} all are tangential
43 to the coastline, and the decomposition of \mathbf{F} as $\mathbf{F}_{div} + \mathbf{F}_{rot}$ yields a simple extension of the
44 familiar notion of meridional transports bounded by coastlines (Fig. S1).

45 The 20-year mean \mathcal{P} and \mathcal{S} are depicted in Fig. 3 as, respectively, colored and grey contours.
46 The raw and effective transports reported in Figs. 1 - 2 and Tabs. S1 - S4 are computed by
47 integrating the transverse component of either \mathbf{F}_{div} or \mathbf{F} following grid line paths that are shown
48 in Fig. S2. Algorithmic detail is provided in appendix C of (1). When computing pole to pole
49 meridional transports for the Atlantic, Pacific, and Indian oceans, the Arctic is split into two
50 sectors along the 80°W and 100°E meridians, the Southern Ocean is split into three sectors
51 along Drake Passage, 147°E, and 20°W, and marginal seas are attached to neighboring oceans
52 as reflected by the color coding in Fig. S2.

3 Underlying physical Processes

To evaluate uncertainties associated with our interpretation of effOHT, it is useful to consider the various terms of the temperature equation computed at constant volume (11). The underlying heat budget can be written for a time-variable volume element, V , as

$$\frac{dH}{dt} = \rho_c C_p \left(\theta \frac{dV}{dt} + \frac{d\theta}{dt} V \right) \quad (6)$$

where $\rho_c \frac{dV}{dt}$ is the rate of mass flux convergence and $\frac{d\theta}{dt}$ is the rate of temperature change within the selected volume element. Detailed equations are provided in (1).

The temperature equation computed at constant volume, which by construction is free of any mass-flux convergence, expresses the second term on the right hand side of Eq. (6) as

$$\rho_c C_p V \frac{d\theta}{dt} = h_{tend} = h_{adv} + h_{dif} + h_{forc} \quad (7)$$

where h_{adv} represents the advective heat flux convergence, h_{dif} the diffusive heat flux convergence, h_{forc} the external forcing due to air-sea and geothermal heat flux convergence, and h_{tend} the temperature tendency term. Any term in Eq. (7), once its global mean has been removed, can be substituted with $\nabla \cdot \mathbf{F}$ on the right-hand-side of the Poisson equation (5) to translate it into a divergent vector field associated with a scalar potential like in Eq. (3).

A close approximation to effOHT is obtained by applying this approach to $h_{adv} + h_{dif}$ (e.g., compare Fig. S3 with Fig. 2) since the impact of non-zero mass fluxes on effOHT is generally small (SPM section 4). The residual (i.e., the difference between Fig. S3 and Fig. 2) shows little interannual variability and time-mean values of the order of ± 0.1 PW in terms of meridional transports (Fig. S4; left) with patterns that resemble those seen in net mass transports (2).

Further unpacking the terms in Eq. (7) reveals that effOHT primarily reflects a balance between advection and air-sea fluxes (top panels in Fig. S5). Lateral diffusion contributes ± 0.2 PW in the time mean with negligible interannual variability (bottom left) while temporal variations in ocean temperature translate into negligible effOHT for the 20-year average

75 along with ± 0.2 PW interannual variability in the tropics (bottom right). As a result, indi-
76 rect estimates of annual-mean meridional heat transports based on air-sea flux maps can only
77 approximate effOHT at best within ± 0.3 PW. Such uncertainty levels are unfortunately compa-
78 rable to the magnitude of effective inter-ocean heat transports (Tab. S1).

79 **4 Sensitivity Tests**

80 The approach introduced in SPM sections 1-2-3 has noteworthy advantages as compared with
81 previous methods. Unlike earlier estimations of the divergent OHT component in (13) and simi-
82 lar studies, it [a] addresses also the non-divergent OHT component, [b] readily filters out global
83 imbalances which may come from atmospheric data assimilation schemes or anthropogenic heat
84 uptake (4, 14), [c] ensures strict consistency between air-sea fluxes, ocean heat content changes,
85 and OHT (1, 2), and [d] avoids ad-hoc integration method or boundary condition choices in
86 deriving meridional transports. As compared with ship-based estimations, our approach fur-
87 ther [e] alleviates uncertainty associated with energy reference level choices and non-zero mass
88 fluxes (15, 16). Issues [d] and [e] remain to be illustrated, which is done below.

89 **4.1 Sensitivity to the integration method**

90 First, we replicate the method of (13) to infer meridional OHTs by cumulatively integrating $\nabla \cdot \mathbf{F}$
91 from the North pole to the South pole over the Atlantic, Pacific, and Indian. Similar methods
92 have been used to infer meridional OHTs from air-sea flux maps going back at least as far as
93 the 1950's (17). Closely following the methodology of (13) facilitates comparison with their
94 Fig. 3. Their methodological choices imply that OHTs through the Indonesian Archipelago and
95 through the Southern Hemisphere passages between the Atlantic, Pacific, and Indian are set to
96 zero. Still following (13), the whole Arctic is attached to the Atlantic in this computation, which
97 de facto also sets OHT through Bering Strait to zero. The result of this computation is hereafter

98 denoted by infoOHT and is depicted in Fig. S6 (dashed curves).

99 The ECCO estimate of infoOHT (Fig. S6; dashed curves) is in good agreement with the
100 result shown in Fig. 3 of (13), which is based on a combination of top-of-atmosphere radiation
101 estimates with atmospheric and oceanic reanalyses products. However, comparison between
102 our infoOHT (Fig. S6; dashed curves) and our effOHT (Fig. S6; solid curves), both based on the
103 exact same ECCO estimate of $\nabla \cdot \mathbf{F}$, reveals biases in infoOHT.

104 Starting from the North Pole, the *closing* of Bering Strait leads to a northward OHT bias in
105 the Atlantic and a corresponding southward OHT bias in the Pacific. In turn, the ITF closing
106 induces a northward OHT bias in the Indian while adding southward OHT bias south of $\sim 10^\circ\text{S}$
107 in the Pacific. Additional compounding of OHT bias occurs further South as a result of closing
108 Drake Passage and the section between Australia and Antarctica.

109 Once integration has reached the coast of Antarctica, the end result is an unbalanced OHT
110 of 0.39, -0.62, and 0.22 PW for the Atlantic, Pacific, and Indian respectively. These large
111 imbalances are consistent with those reported in (13), and result from introducing artificial
112 boundaries of integration between oceanic basins. As already pointed out by (13), this clearly
113 argues in favor of a more objective approach such as the one introduced in this paper.

114 **4.2 Sensitivity to the Energy Reference Level**

115 Now, we assess the sensitivity of OHT estimates to arbitrary ERL choices, which can be a major
116 concern in the case of ship-based OHT estimates due to non-zero mass fluxes (15, 16). To assess
117 the impact of ERL choices, we subtract $\rho_c C_p \theta_0 \mathbf{U}$, where θ_0 is a uniform temperature value and
118 $\rho_c \mathbf{U}$ is the ECCO mass-transport estimate, from \mathbf{F} and recompute \mathbf{F}_{div} and \mathbf{F}_{rot} via Eqs. 3-4-5.
119 It should be noted that $\rho_c \mathbf{U}$ itself includes both rotational and divergent components. Results
120 shown previously in Figs. 1 to 3, Figs. S2 to S6, and Tabs S1 to S4 correspond to $\theta_0 = 0^\circ\text{C}$.
121 Here we test two other reasonable choices for θ_0 : 3.5°C and 18.5°C which correspond to setting

122 the ERL approximately to, respectively, the global mean ocean temperature and the global mean
123 sea surface temperature.

124 Comparing results from the 3.5°C and 18.5°C cases reveals that rawOHT is often very sen-
125 sitive to ERL choices whereas effOHT is much more robust (e.g., compare Tabs. S5 with S6).
126 This contrast in sensitivity between rawOHT and effOHT reflects that rotational mass flux mag-
127 nitudes associated with gyres, the Antarctic Circumpolar Current, etc. vastly exceed divergent
128 mass flux magnitudes associated with evaporation and precipitation ($I, 2$). As a result, the OHT
129 streamfunction \mathcal{S} associated, per Eq. (4), with the rotational flux \mathbf{F}_{rot} differs wildly between the
130 two panels of Fig. S7 as well as between Fig. S7 and Fig. 3. In contrast, the OHT scalar potential
131 \mathcal{P} is remarkably insensitive to the choices of ERL: effOHT changes by less than 0.01-0.02 PW
132 in these tests, an effect well below other sources of uncertainties (Tabs. S5 and S6).

133 In conclusion, even the sign and order of magnitude of rawOHT should be interpreted with
134 great caution as they are essentially predicated on an arbitrary ERL choice. As a consequence,
135 heterogeneous treatment of non-zero mass fluxes can, in and of itself, greatly complicate OHT
136 estimate inter-comparisons.

Table S1: Effective and raw ocean heat transports (in PW; 1 PW= 10^{15} W) computed through passages that separate the main oceanic basins (red sections in Fig. S2). The top four values (resp. bottom five) are counted positive northward (resp. eastward). Reported values are for the 1992-2011 mean \pm 1 standard deviation amongst annual means.

effective transport effOHT	raw transport rawOHT	section name
-0.13 \pm 0.06	+2.06 \pm 0.03	Australia–Antarctica (147°E)
+0.19 \pm 0.07	+1.47 \pm 0.02	Drake Passage
-0.01 \pm 0.06	+1.08 \pm 0.03	South Africa–Antarctica (19.5°W)
-0.10 \pm 0.11	-1.20 \pm 0.10	Indonesian Through Flow (negative values = westward transport)
+0.20 \pm 0.02	+0.01 \pm 0.00	Bering Strait
-0.01 \pm 0.00	+0.01 \pm 0.00	Davis Strait
+0.02 \pm 0.00	+0.01 \pm 0.00	Denmark Strait
+0.06 \pm 0.01	+0.26 \pm 0.02	Iceland–Scotland
+0.01 \pm 0.00	-0.00 \pm 0.00	Scotland–Norway

Table S2: Effective and raw ocean heat transports (in PW) across meridians over the Indian Ocean (green sections in Fig. S2). All values are counted positive northward. Reported values are for the 1992-2011 mean \pm 1 standard deviation amongst annual means.

effective transport effOHT	raw transport rawOHT	Latitude
-0.00 ± 0.01	-0.00 ± 0.01	20 °N
-0.10 ± 0.05	-0.10 ± 0.05	10 °N
-0.29 ± 0.09	-0.33 ± 0.08	Equator
-0.58 ± 0.09	-1.04 ± 0.10	10 °S
-0.50 ± 0.09	-1.60 ± 0.13	20 °S
-0.23 ± 0.11	-1.33 ± 0.09	30 °S
$+0.02 \pm 0.10$	$+0.34 \pm 0.08$	40 °S
$+0.03 \pm 0.08$	-1.79 ± 0.08	50 °S
-0.05 ± 0.04	-0.26 ± 0.01	60 °S

Table S3: Same as Table S2 but for the Pacific Ocean (blue sections in Fig. S2).

effective transport effOHT	raw transport rawOHT	Latitude
$+0.16 \pm 0.02$	-0.01 ± 0.00	80 °N
$+0.20 \pm 0.02$	$+0.00 \pm 0.00$	70 °N
$+0.22 \pm 0.02$	$+0.02 \pm 0.00$	60 °N
$+0.29 \pm 0.03$	$+0.10 \pm 0.02$	50 °N
$+0.31 \pm 0.04$	$+0.12 \pm 0.03$	40 °N
$+0.68 \pm 0.12$	$+0.48 \pm 0.11$	30 °N
$+0.82 \pm 0.11$	$+0.63 \pm 0.10$	20 °N
$+0.73 \pm 0.23$	$+0.54 \pm 0.24$	10 °N
-0.02 ± 0.27	-0.18 ± 0.29	Equator
-0.83 ± 0.20	-0.56 ± 0.17	10 °S
-0.79 ± 0.22	$+0.11 \pm 0.14$	20 °S
-0.69 ± 0.18	$+0.22 \pm 0.08$	30 °S
-0.59 ± 0.11	$+0.30 \pm 0.06$	40 °S
-0.58 ± 0.08	$+0.37 \pm 0.10$	50 °S
-0.33 ± 0.06	-0.17 ± 0.03	60 °S
-0.05 ± 0.00	-0.05 ± 0.00	70 °S

Table S4: Same as Table S2 but for the Atlantic Ocean (yellow sections in Fig. S2).

effective transport effOHT	raw transport rawOHT	Latitude
-0.14 ± 0.02	$+0.02 \pm 0.00$	80 °N
-0.01 ± 0.02	$+0.19 \pm 0.02$	70 °N
$+0.18 \pm 0.02$	$+0.38 \pm 0.02$	60 °N
$+0.35 \pm 0.04$	$+0.55 \pm 0.03$	50 °N
$+0.40 \pm 0.05$	$+0.60 \pm 0.04$	40 °N
$+0.65 \pm 0.06$	$+0.84 \pm 0.06$	30 °N
$+0.72 \pm 0.06$	$+0.91 \pm 0.07$	20 °N
$+0.61 \pm 0.08$	$+0.81 \pm 0.09$	10 °N
$+0.39 \pm 0.05$	$+0.58 \pm 0.06$	Equator
$+0.16 \pm 0.05$	$+0.36 \pm 0.06$	10 °S
$+0.17 \pm 0.05$	$+0.36 \pm 0.06$	20 °S
$+0.09 \pm 0.04$	$+0.29 \pm 0.04$	30 °S
$+0.20 \pm 0.04$	-1.01 ± 0.06	40 °S
$+0.16 \pm 0.04$	$+1.03 \pm 0.03$	50 °S
-0.00 ± 0.02	$+0.04 \pm 0.01$	60 °S
-0.02 ± 0.00	-0.02 ± 0.00	70 °S

Table S5: Transports as in Tabs. S1 to S4 (in PW) but with the Energy Reference Level (ERL) set to the global mean ocean temperature (3.5°C). See SPM section 4 for detail.

effective transport effOHT	raw transport rawOHT	section name
-0.13 ± 0.06	-0.34 ± 0.03	Australia–Antarctica (147°E)
+0.19 ± 0.07	-0.70 ± 0.04	Drake Passage
-0.01 ± 0.06	-1.10 ± 0.05	South Africa–Antarctica (19.5°W)
-0.10 ± 0.11	-0.98 ± 0.09	Indonesian Through Flow
+0.20 ± 0.02	-0.01 ± 0.00	Bering Strait
-0.29 ± 0.09	-0.33 ± 0.08	Equator (Indian)
-0.23 ± 0.11	-1.12 ± 0.09	-30 N (Indian)
+0.68 ± 0.12	+0.47 ± 0.11	+30 N (Pacific)
-0.01 ± 0.27	-0.19 ± 0.29	Equator (Pacific)
-0.69 ± 0.18	-0.02 ± 0.08	-30 N (Pacific)
+0.65 ± 0.06	+0.86 ± 0.06	+30 N (Atlantic)
+0.39 ± 0.05	+0.60 ± 0.06	Equator (Atlantic)
+0.09 ± 0.04	+0.30 ± 0.04	-30 N (Atlantic)

Table S6: Transports as in Tabs. S1 to S4 (in PW) but with the Energy Reference Level (ERL) set to the global mean sea surface temperature (18.5°C). See SPM section 4 for detail.

effective transport effOHT	raw transport rawOHT	section name
-0.12 ± 0.06	-10.62 ± 0.20	Australia–Antarctica (147°E)
+0.19 ± 0.07	-10.01 ± 0.19	Drake Passage
-0.00 ± 0.06	-10.47 ± 0.20	South Africa–Antarctica (19.5°W)
-0.08 ± 0.11	-0.05 ± 0.07	Indonesian Through Flow
+0.20 ± 0.02	-0.07 ± 0.02	Bering Strait
-0.29 ± 0.09	-0.31 ± 0.08	Equator (Indian)
-0.24 ± 0.11	-0.21 ± 0.08	-30 N (Indian)
+0.70 ± 0.12	+0.43 ± 0.11	+30 N (Pacific)
+0.02 ± 0.26	-0.23 ± 0.28	Equator (Pacific)
-0.71 ± 0.18	-1.01 ± 0.12	-30 N (Pacific)
+0.66 ± 0.06	+0.94 ± 0.06	+30 N (Atlantic)
+0.40 ± 0.05	+0.67 ± 0.06	Equator (Atlantic)
+0.07 ± 0.04	+0.35 ± 0.04	-30 N (Atlantic)

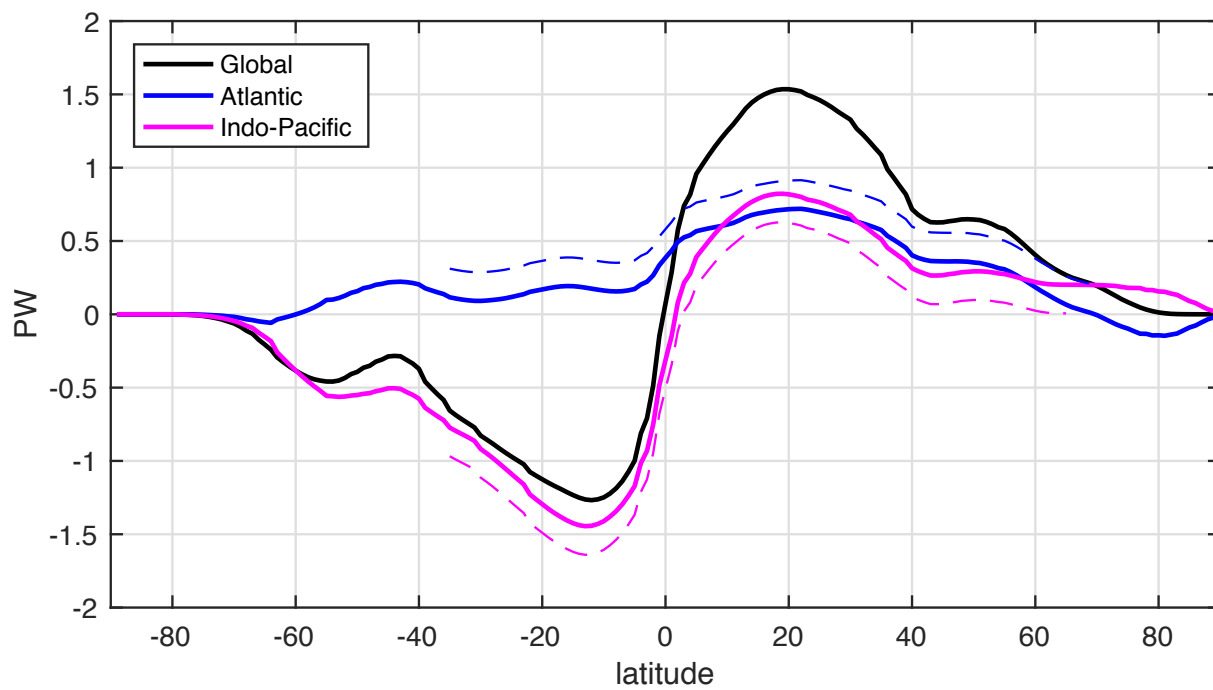


Figure S1: Meridional ocean heat transport (in PW; 1 PW= 10^{15} W) on average over 1992-2011 for the Atlantic (blue) and the Indo-Pacific (red) based on either F_{div} (solid) or F (dashed). Net meridional transports integrated around the Globe are the same in both cases (black).

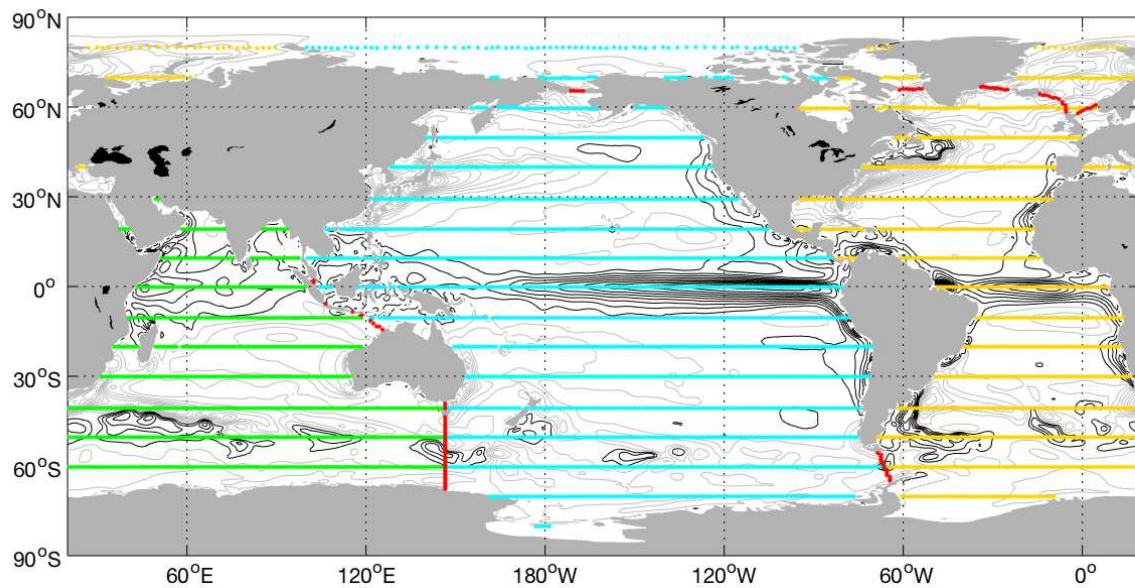


Figure S2: Transects through which heat transport estimates are reported in Tab. S1 (red transects), Tab. S2 (green transects), Tab. S3 (blue transects), and Tab. S4 (yellow transects). Black contours (resp. grey contours) represent the rate of ocean heat divergence (resp. convergence) which reflects the rate of heat uptake from (resp. heat release to) the atmosphere.

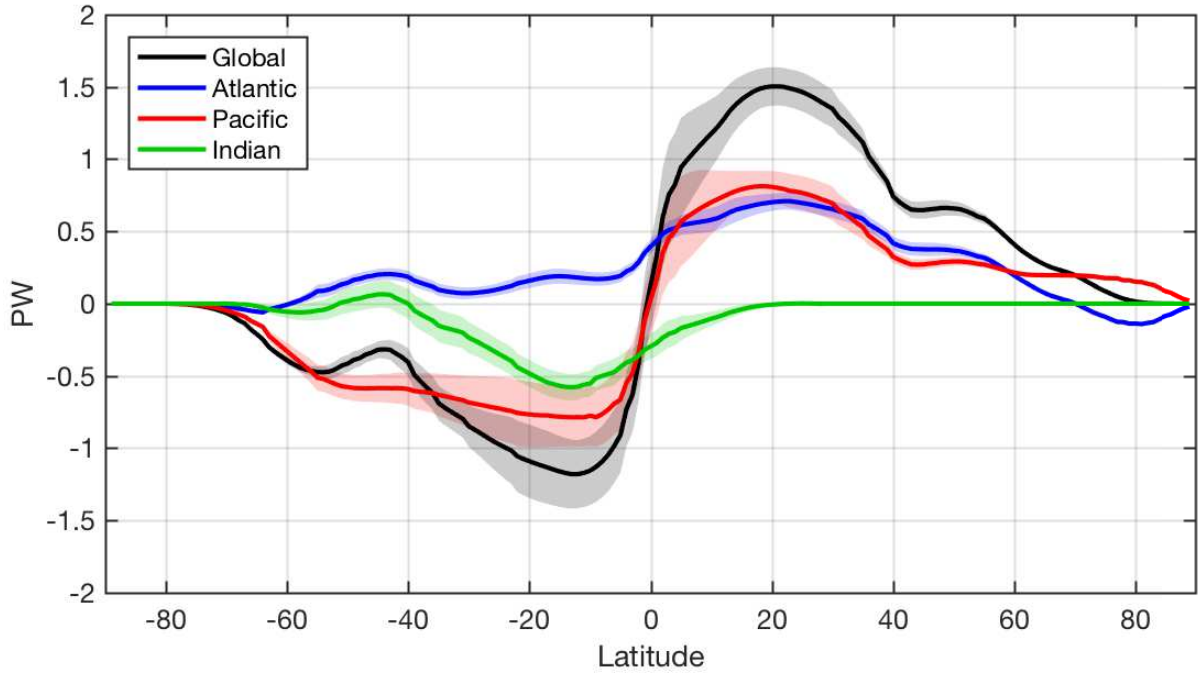


Figure S3: Implied meridional ocean transports (in PW) computed from the convergence of advective and diffusive fluxes ($h_{adv} + h_{dif}$ in Eq. (7)) for the global ocean or separately for the Atlantic, Pacific, and Indian sectors. Unlike in Fig. 2, these results are based on the temperature tendency equation computed at constant volume: $h_{adv} + h_{dif} = h_{tend} - h_{forc}$ where h_{tend} and h_{forc} respectively represent the tendency and external forcing terms. Implied transports are computed from $h_{adv} + h_{dif}$ by subtracting the global mean value and then solving a Poisson equation as done before for effOHT (Fig. 2). Thick lines denote the 1992-2011 mean and shaded ranges reflect ± 1 standard deviation amongst annual means.

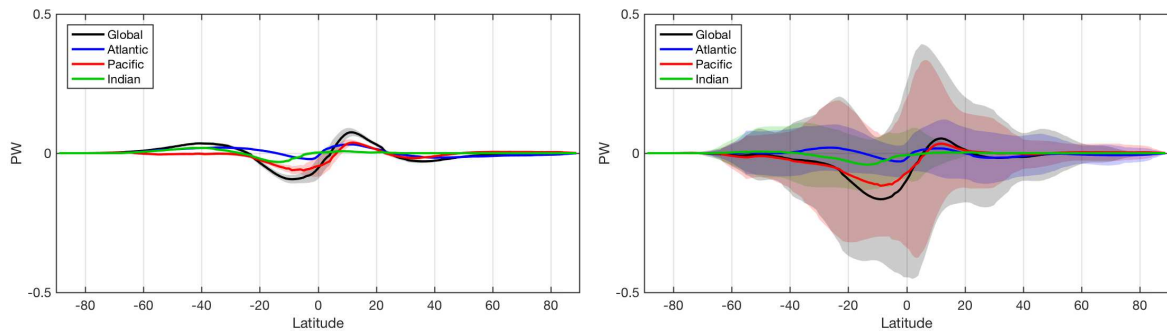


Figure S4: Left: difference between effOHT (Fig. 2) and meridional heat transports implied by $h_{adv} + h_{dif}$ in Eq. (7) (Fig. S3); this gives the residual contribution of convergent mass fluxes associated with the interplay of evaporation, precipitation, and runoff to effOHT. Right: difference between effOHT (Fig. 2) and meridional heat transports implied by $-h_{forc}$ in Eq. (7) (top right panel of Fig. S5); this corresponds to errors that would result from using air-sea heat fluxes as an estimate of ocean heat transport convergences. Thick lines denote the 1992-2011 mean and shaded ranges reflect ± 1 standard deviation amongst annual means.

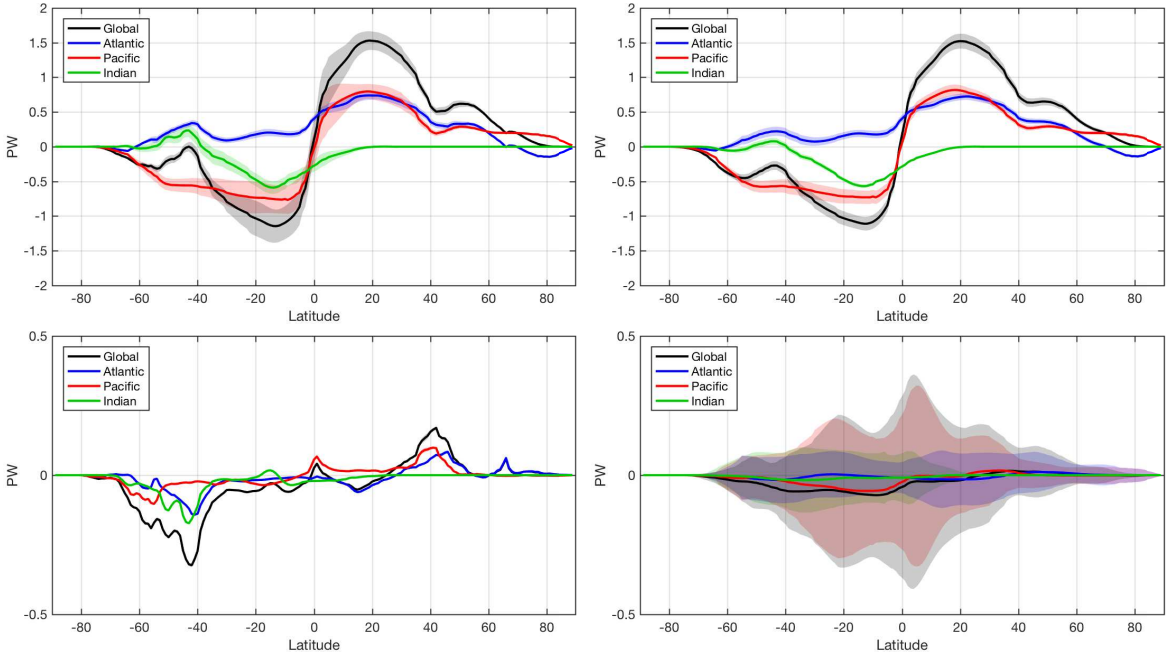


Figure S5: Implied meridional ocean heat transports (in PW) for each term of the temperature equation computed at constant volume (Eq. (7)). In each case, implied transports are computed by subtracting the global mean value and then solving a Poisson equation: (top left) the advective flux convergence h_{adv} , (bottom left) the diffusive flux convergence h_{dif} , (top right) the vertical divergence of heat fluxes through the sea surface and sea floor $-h_{forc}$, and (bottom right) the tendency term h_{tend} . Note that, by construction, the sum of the left panels ($h_{adv} + h_{dif}$) is equal to the sum of the right panels ($h_{tend} - h_{forc}$). Thick lines denote the 1992-2011 mean and shaded ranges reflect ± 1 standard deviation amongst annual means.

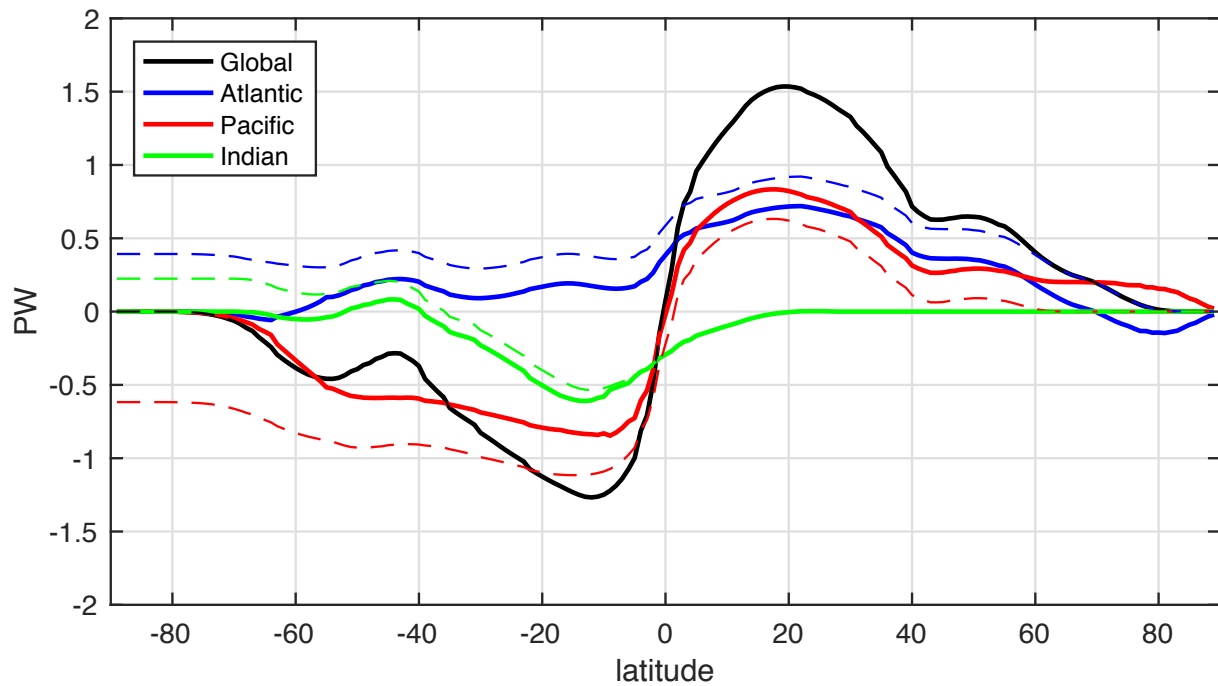


Figure S6: Meridional effOHT (solid curves; in PW) over the Globe (black), Atlantic (blue), Pacific (red), and Indian (green) sectors. Corresponding dashed curves are estimated from the same OHT convergence but based on the method of (13) (namely, infoHT). Net meridional transports integrated around the Globe are the same in both cases (black curve). See SPM section 4.1 for computational details.

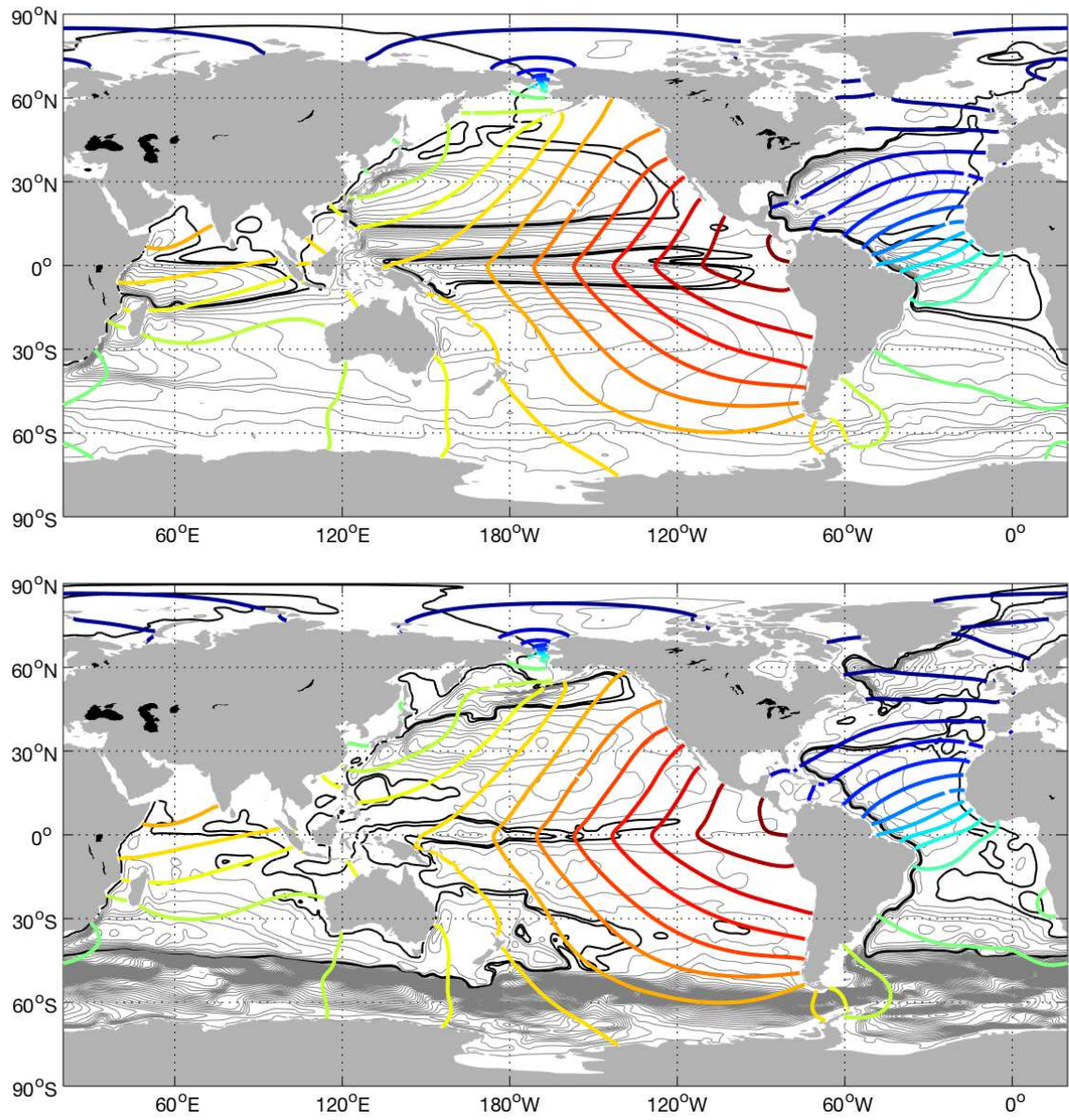


Figure S7: Same as Fig. 3 but after resetting the Energy Reference Level (ERL) to approximately the global mean ocean temperature (3.5°C; top) and the global mean sea surface temperature (18.5°C; bottom). See SPM section 4.2 for detail.

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