

Hydrogen Recombination And Dimer Formation On Graphite From Ab Initio Molecular Dynamics Simulations

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Abstract

We studied Eley-Rideal molecular hydrogen formation on graphite using *ab initio* molecular dynamics, in the energy range relevant for the chemistry of the interstellar medium and for terrestrial experiments employing cold plasma (0.02-1 eV). We found substantial projectile steering effects which prevent dimer formation at low energies, thereby ruling out any catalytic synthetic pathways that form hydrogen molecules. *Ortho* and *para* dimers do form efficiently thanks to preferential sticking, but only at energies which are too high to be relevant for the chemistry of the interstellar medium. Computed reaction cross sections and ro-vibrational product populations are in good agreement with available experimental data and capable to generate adsorbate configurations similar to those observed with scanning tunneling microscopy techniques.

The interaction between hydrogen atoms and graphitic materials has been widely studied in the last decade, mainly because its many applications in materials science and astrochemistry. After exposing semi-metallic graphene to a cold hydrogen beam it is possible to induce a band gap¹ forming either disordered²⁻⁴ or locally crystalline hydrogenated phases such as graphane^{5,6} or C₄H polymers.^{7,8} At present H atom patterning is a very promising route to produce semiconducting graphene, and much effort has been devoted to study methods to design and control hydrogenation of this material.

In astrochemistry, molecular hydrogen is considered to be a key ingredient of the interstellar medium (ISM), since it is involved in both the formation of complex chemicals and the dynamics of the clouds. It was noticed that the star formation rate is related to the abundance of molecular gas, and in particular of H₂.^{9,10} Hydrogen molecules are important cooling agents during the gravitational collapse of the clouds, despite the lack of a permanent dipole moment. H₂ is indeed by far the most abundant molecule present in the interstellar clouds that radiative cooling through weak quadrupole transitions is the main process allowing the collapse to continue till star ignition.

H₂ is found abundantly in both the *dense* and the *diffuse* molecular clouds of the ISM,

therefore an efficient route for H₂ production must be operative at the temperatures and densities typical of the ISM. Whereas gas phase synthesis of H₂ is considered to be poorly efficient, a number of gas-surface pathways have been invoked that lead to a value of the recombination rate consistent with astronomical observations.¹¹

The dust grains composition has been debated for long time, and many different models were proposed.¹² Among those models, structures based on silicate cores and sp² polycyclic aromatic hydrocarbons (PAH) should be good candidates and fit many observations, at least in warm environments, where icy mantles would quickly evaporate.^{13,14} Therefore, many theoretical and experimental studies have focused on the H₂ recombination on graphitic surfaces for both physisorbed and chemisorbed H atoms. As physisorbed H atoms diffuse easily on the graphite surface, they may efficiently undergo Langmuir-Hinshelwood (LH) recombination, provided that the surface temperature (T_s) is lower than the desorption threshold (~ 40 K according to the physisorption well depth E_b ~40 meV, as obtained experimentally¹⁵ and confirmed theoretically¹⁶). No chemisorption is expected in this regime, since H atoms need to overcome a barrier ~0.2 eV high in order to form a covalent bond, as a consequence of the re-hybridization of the C atom valence orbitals from sp² to sp³.^{17,18} In warmer areas of the ISM, such as photon dominated (PDR) or shocked regions, the (gas) temperature ranges between 100 and 10000 K, and only chemisorbed H atoms can be found. These species are immobile on the surface and do not suit to LH kinetics, thus foreshadowing a completely different scenario for hydrogen recombination. Sticking is difficult because of the above mentioned adsorption barrier – though tunneling^{19,20} and quantum fluctuations of the lattice²¹ might help in this context – but is interesting because it is accompanied by some profound changes into the substrate. Indeed, formation of a CH bond leaves one unpaired electron on the lattice (a radical) that localizes mostly in the *ortho* and *para* positions, as a consequence of the aromaticity of the substrate.²² This is the reason for the preferential sticking mechanism forming *ortho* and *para* dimers on the carbon surface²³ (for a recent review see Ref. 24). Thus, in this case the possible recombination pathways are the Eley-Rideal (ER) abstraction

between a chemisorbed H atom and a gas phase H atom, a ‘hot-atom’ recombination and the associative desorption of the H dimers.²⁵ Experimentally, the abstraction cross-section was found to have the same remarkably large value of about 4 \AA^2 both in the high T_s and in the high coverage limit,^{26,27} *i.e.* in conditions where hot-atom contributions are negligible. The thus estimated value of the ER cross section is much larger than that found for similar processes on semiconducting²⁸ and metallic²⁹ surfaces. This found a qualitative agreement with previous theoretical studies which, being mostly based on reduced models including only few degrees of freedom, were unable to account for the competing dimer formation process and for the energy transferred to the lattice.

In this work we studied the Eley-Rideal recombination of chemisorbed H atoms by means of *ab initio* molecular dynamics (AIMD), improving and extending our recent findings.³⁰ This approach allows us not only to quantify the cross section for the ER recombination, but also that of the competing formation of many different dimer structures without the limitation of a static structureless substrate lattice. Differently from our previous investigation, we have extended the collision energy range investigated, the time scales considered, and we have tightened the simulation parameters. In addition, we analyzed the energy transfer to the surface, the effect of dispersion forces on the dynamics, and included different isotopic combinations for the target and projectile H atoms.

We found that at low energy steering of the projectile atom gives an important contribution to the recombination, preventing dimer formation despite the favorable (barrierless) energetics. Only at higher energies *para* and *ortho* dimers are found to form abundantly, at the expense of the reaction yield. Computed cross sections and ro-vibrational H_2 populations are in good agreement with existing thermal desorption and molecular beams studies,²⁶ as well as with theoretical results obtained with different dynamical models.³¹⁻³³

Theoretical Methods

Ab initio (first principles) molecular dynamics simulations were performed using the VASP package.^{34,35} Exchange and correlation were treated at the generalized gradient approximation (GGA) level, with the PW91 functional³⁶ in its spin polarized form. Core electrons were represented by ultra-soft pseudopotentials and the plane wave basis set was limited at 300 eV. The Brillouin zone was integrated on a $3\times 3\times 1$ Γ -centered k points mesh and a 0.05 eV Gaussian smearing was used to ensure a fast electronic convergence. The graphite surface was modeled by a 3×3 single-layer graphene supercell consisting of 18 carbon atoms, and a vacuum layer 10 Å thick was introduced between periodic images to minimize their interaction. This setup was chosen to reproduce the energetics of a single H atom chemisorbed on graphite obtained in Ref. 22, but requires much less computational effort. Table 1 reports a comparison with literature data and shows that our setup allows a reasonable description of binding energies, chemisorption barriers and C-H bond lengths (“puckering” height of the C atom out of the surface plane). In details, the ER minimum energy path in this setup is barrierless, in agreement with recent studies,³⁷ while the formation of *para* dimers, also known to be barrierless,³⁸ is weakly activated (~ 20 meV). However, since in the following we shall limit ourselves to collision energies higher than 20 meV this spurious barrier is irrelevant for the reaction dynamics.

Table 1: Binding energies (E_{bind}), chemisorption energy barriers (E_{barr}) and bond lengths (d_{puck}) for H chemisorbed on different graphene models.

Cell	E_{bind} (eV)	E_{barr} (eV)	d_{puck} (Å)	Ref
2×2	0.67	0.20	0.36	18
coronene	0.57	0.16	0.35	17
3×3	0.77	0.20	0.42	22
3×3	0.84	0.20	0.50	this work
4×4	0.91	-	-	39
5×5	0.84	0.20	0.59	22

Dynamical simulations were performed by sampling the micro-canonical (NVE) ensemble with classical trajectories. Hellmann-Feynman forces were computed on-the-fly with DFT while the Newton equations of motion were integrated using a Verlet algorithm, as implemented in VASP, with a time step dependent on the initial collision energy (E_{coll}): 0.40 fs for $E_{coll} < 0.5$ eV, 0.25 fs for $0.5 \leq E_{coll} \leq 0.8$ eV and 0.08 fs for $E_{coll} > 0.8$ eV.

At the beginning of each trajectory the projectile atom was placed at 5 Å above the surface plane with (monochromatic) initial velocity directed along the surface normal. Only syn-facial adsorption was included in our simulation. The aiming points were generated by a uniform Monte Carlo sampling in a symmetry-irreducible sector $\theta = \pi/6$ of the circular area ($r_{max}=3.55$ Å) centered around the target H atom. The surface initial conditions were not sampled in our calculations, instead each carbon atom and the target H were initially set at rest at their equilibrium positions and left free to move during the whole simulation. The only exceptions are the carbon atoms farthest away from the target which were kept fixed along the axis normal to the surface plane to prevent block translations of the whole system after the impact with the projectile, thereby limiting the dynamical degrees of freedom (N) to $N=59$. These initial conditions thus describe a surface initially at $T_s = 0$ K which is appropriate for typical ISM conditions (*e.g.* $T = 5-100$ K in the interstellar clouds, and typically $T_s < T$); notice though that the Eley-Rideal reaction is expected to be little influenced by the surface temperature³² and by the vibrational excitation of the target H atom.^{40,41}

For each collision energy, we ran 500 trajectories, equivalent to 3000 trajectories on the whole circular area surrounding the target. The number of trajectories was increased to 1000 (per irreducible area) when computing rovibrational populations at selected energies and isotopic substitutions. The reactive channels considered in the molecular dynamics simulations were: the Eley-Rideal recombination (ER), dimer formation (DF), and collision-induced desorption. A dimer was considered as formed when the projectile H atom was found oscillating at a C site for at least seven vibrational periods. For the recombination channel, each product

molecule was assigned to a rotational and vibrational state, based on standard binning into the rovibrational spectrum of the H₂ (HD) molecule, as obtained with the help of a discrete variable representation (DVR) Hamiltonian⁴² on a Morse potential energy curve fit to data computed with the same DFT setup.

It is worth mentioning at this point that collisions on the underlying adiabatic potential, which is dominated by the H-H interaction, result in a ER reaction only if the projectile and target atom spins are coupled as a singlet, triplet pairs experience a fully repulsive interaction.⁴³ Therefore, in our AIMD calculations we set the initial spins of the colliding pair (H-graphene and the gas-phase H atom) anti-parallel, in order to help the system to follow the (ground state) singlet adiabatic surface, and scaled reactive AIMD cross sections by a spin statistical factor 1/4. Similarly for formation of *ortho* and *para* pairs, which occurs barrierless only in the (ground) singlet state.

Results and Discussion

Eley-Rideal H₂ recombination

Eley-Rideal recombination (abstraction) and dimer formation cross sections from AIMD simulations are shown in Figure 1 in the collision energy range 0.02-1.20 eV. At low energy the abstraction cross sections are quite large (3.5 Å²), and then decrease steadily to reach a plateau of 2.5 Å² at $E_{coll}=0.9$ eV with a slight increase at higher energies. The ER-AIMD results can be compared with other classical and quantum studies performed on reduced-dimensionality models, to study the influence of the surface corrugation on the recombination dynamics. In the left panel of Figure 1 we show the quantum results obtained with a time dependent wave packet method on a three-dimensional model, corresponding to a *flat* and *rigid* graphite surface in two distinct dynamical regimes.³¹ One is known as the “sudden” approximation, and keeps the binding C atom frozen at its puckered position; this is expected

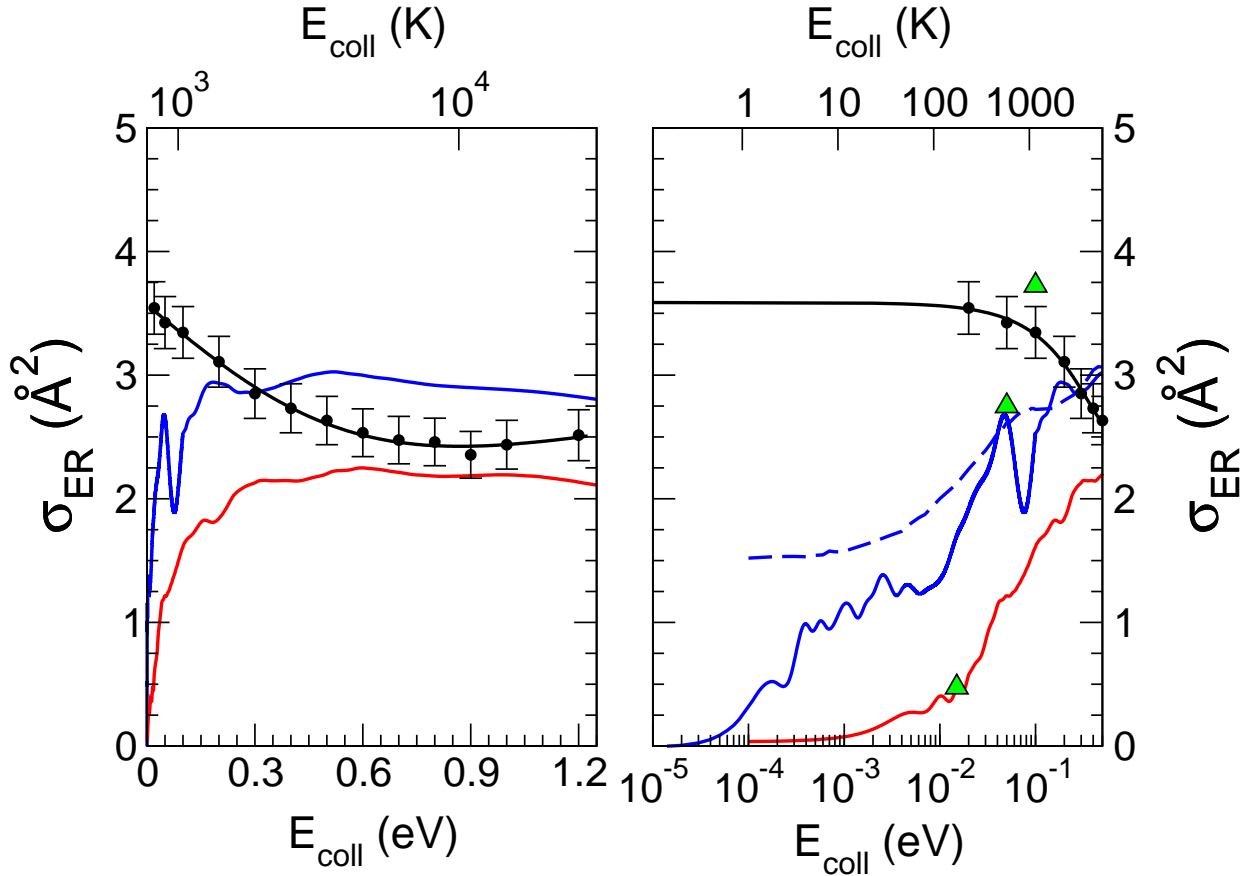


Figure 1: Left panel: Cross sections for ER recombination from AIMD (black dots with error bars) and from quantum calculations within the adiabatic (blue) and sudden (red) rigid, flat-surface models.³¹ Right panel: the same graph shown in the low collision energy regime. Dashed line represents classical results obtained for the rigid, flat-surface adiabatic PES, and green triangles are for classical results on a Brenner-like potential.⁴⁴

to be appropriate at high collision energies, where the product molecule moves back to the gas phase on a time-scale faster than the relaxation of the surface atom. The other is the so-called “adiabatic” approximation, and takes the relaxed C atom height above the surface plane for each position of the two H atoms; this is expected to be more accurate at low collision energies where the carbon atom adjusts its position during the supposedly slow reaction dynamics.¹⁸ Here we note that classical and quasi-classical results obtained from the same potentials give qualitatively the same results in regimes where quantum effects become negligible.⁴⁰

It looks clear that at moderately high collision energies ($E_{coll} > 0.6$ eV) the AIMD results lay

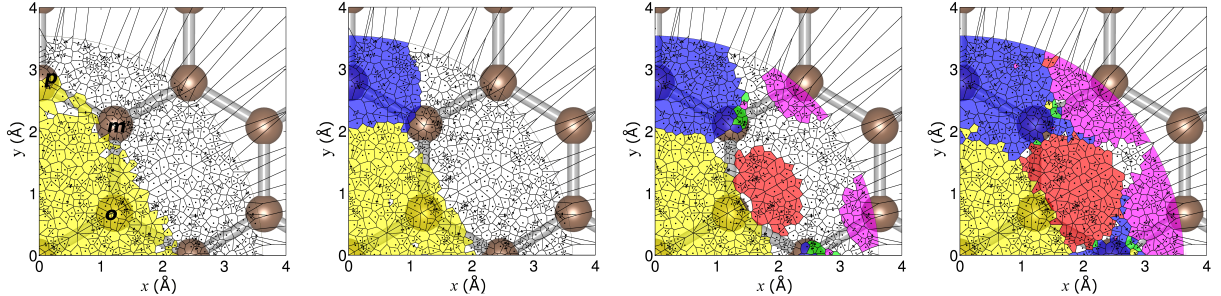


Figure 2: Aiming points location for AIMD trajectories at (from left to right) $E_{coll}=0.02$, 0.2, 0.4 and 0.8 eV. The area around each aiming point was colored to match trajectories for ER (yellow), *ortho* dimer (red), *meta* dimer (green), *para* dimer (blue), and other dimers (magenta). The target H atom is located at the origin of the axes and the *ortho* (o), *meta* (m) and *para* (p) positions are indicated in the leftmost panel.

in between the two curves obtained for the quantum reduced models, approaching the sudden results at $E_{coll} \sim 0.8-0.9$ eV. At low energy, instead, a marked difference is observed. Two main factors contribute to this discrepancy. On the one hand, at vanishing collision energies the quantum cross-sections vanish due to a quantum reflection effect, which occurs when the projectile de Broglie wavelength gets larger than the spatial variations of the attractive CH-H potential³¹ (see *e.g.* Ref. 45 for a surface science example). Classical calculations (either AIMD or QCT) are unable to account for this quantum effect, and indeed show a reaction cross-section which levels off at some finite value when reducing the projectile energy. On the other hand, AIMD calculations include the effects of surface corrugation, and show an increasing cross-section at small collision energies. The flat, rigid-surface model underestimates reaction at low energies even in the classical limit (see the dashed line in the right panel of Figure 1). The same holds for the more accurate analytic representation of the interaction developed by Bachelier *et al.*,⁴⁴ who used a Brenner-like potential model and included the lattice dynamics in their classical calculations. Both these models fail in describing the influence of the spin density excess localized on *ortho* and *para* positions with respect to the target atom, thereby suggesting that the *ortho-para* orientation effect plays a role not only in the formation of dimers, but also in the ER recombination dynamics at low energies. This is made clear in Figure 2, which shows the location of the reactive aiming

points at different values of E_{coll} . As is evident in that figure, at the lowest energy considered ($E_{coll}=20$ meV, or 232 K), the aiming points of those trajectories leading to reaction are not isotropically distributed around the target atom, but form a three-fold shape protruded toward the *para* positions. This is a sign that the attractive well generated by the unpaired electron is accelerating and *steering* the projectile atom toward the target atom, which then captures the projectile forming an H_2 molecule. This effect is less important at higher collision energies, where the projectile momentum becomes large compared to the attractive potential, and the ER reactive area gets progressively more isotropic.

Besides the direct abstraction of the target H atom we found other possible mechanisms for H_2 recombination. One is the abstraction by a projectile that is moving away from the surface after scattering off the repulsive potential of *e.g.* a *meta* site, as shown in Figure 3. This “rebound” mechanism is different from that reported before for the flat and rigid model in which the abstraction takes place from below the target,⁴⁰ irrespective of the impact site. The other mechanism is the associative desorption from a metastable dimer pair in which the projectile atom sticks on the *para* site in a highly excited vibrational state and, after few vibrations, captures the target before dissipating its excess energy to the lattice. This mechanism was postulated in a recent study⁴⁶ and found in our AIMD trajectories only at $E_{coll} > 0.7$ eV. Unfortunately, the number of reactive trajectories is not large enough to provide the relative weight of each recombination mechanism with confidence, however we estimate these last two pathways to be less than 10% of the total number of reactive trajectories.

At last, we note here that in the energy range considered here we found no exchange of the two H atom, nor any collision induced desorption, in agreement with previous studies.⁴⁰

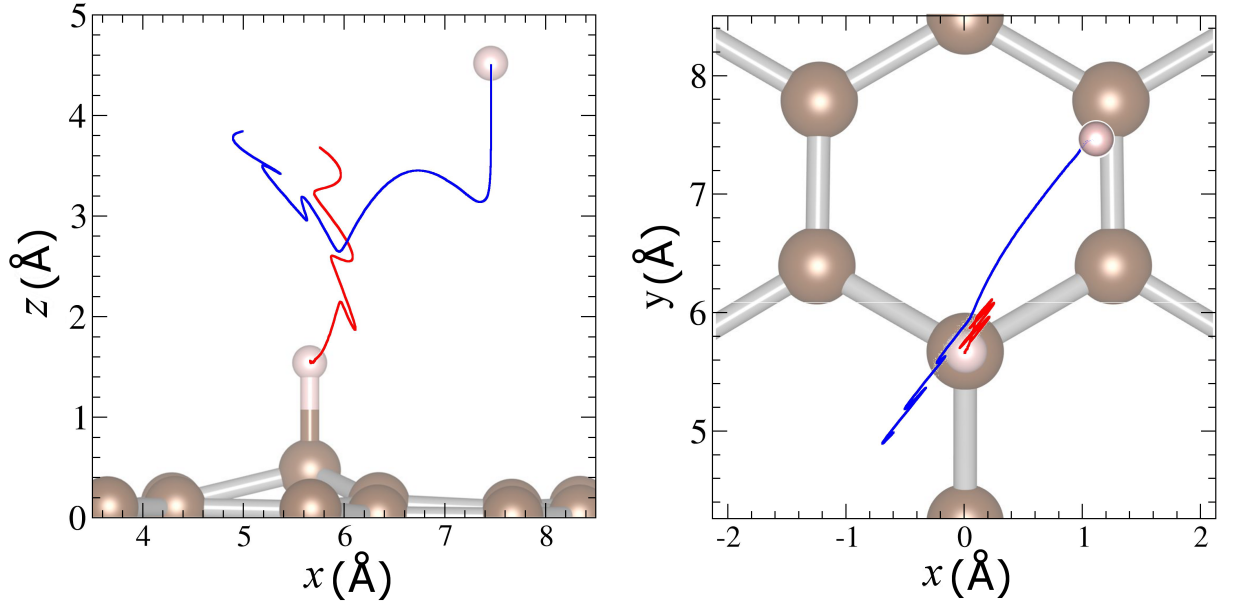


Figure 3: Typical “rebound” reactive trajectory in which the projectile H atom is first scattered by the repulsive potential of the meta C site, and then stirred toward the target H atom by its attractive potential.

Dimer formation

The most important DF cross sections are shown in Figure 4 as functions of E_{coll} , divided in *ortho*, *meta* and *para*¹. As already visible in Figure 2, at low energy the attractive potential of the target H atom hinders dimer formation in favor of reaction. Only increasing the collision energy some of the reactive trajectories turn into dimer formation, thereby determining a decrease of the ER recombination. DF cross sections rise slowly with energy till collisions get so fast that the projectile leaves the interaction region before the C atom has the time to move out from the surface plane and bind the projectile into a dimer.

The channels for the formation of H pairs open at different collision energies because of their different activation barrier, which in turn depends on the amount of spin density localized on the lattice site.²² *Meta* dimers have a formation barrier comparable to that found when adsorbing a hydrogen atom on a fresh surface, and their cross sections are much smaller than the *ortho* and *para* one, despite the larger number of sites (six *vs.* three) and the favorable

¹Since the ground-state *meta* dimers are in a *triplet* state and our AIMD trajectories follow the lowest energy adiabatic surface, we used a different spin statistical factor (3/4) for this dimer configuration.

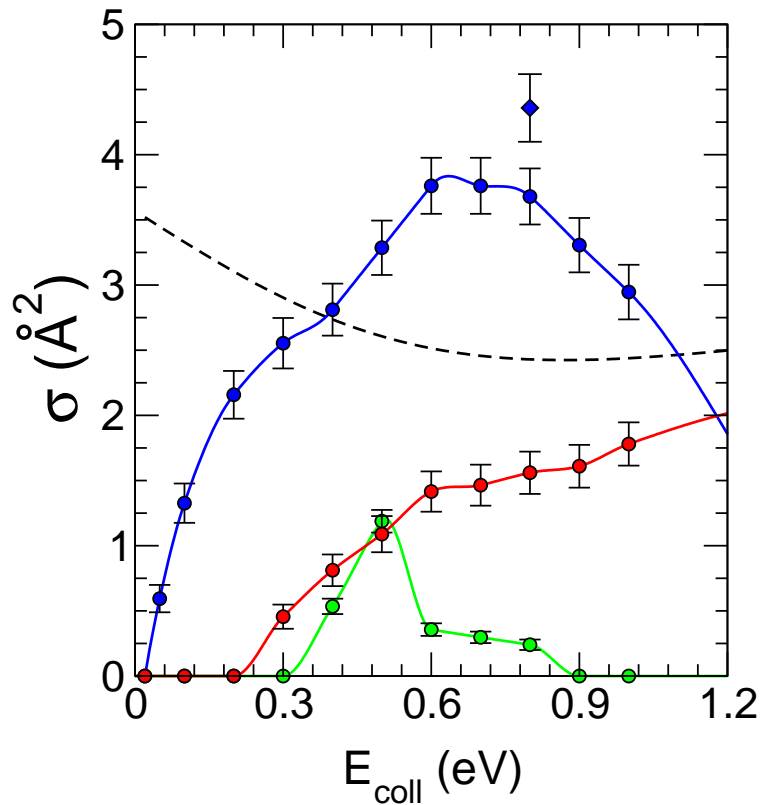


Figure 4: AIMD cross sections for the formation of H dimers: for the *ortho* (red), *meta* (green) and *para* (blue) dimers. The blue diamond shows the *para* dimer value obtained by doubling the sampled area (see text), and lines are guides to the eye. The dashed line is the ER cross section, set as a reference.

spin statistics (triplet *vs.* singlet). *Ortho* and *para* dimers have favorable energetics and present either a barrierless (*para*) or a weakly activated (*ortho*) path to their formation.²² Dynamical results do confirm that their formation is favored, but also show that the dynamical threshold is larger than the adsorption barrier. The reason for this behavior, as mentioned above, is the competing reaction: the target atom lies about 2 Å above the surface plane and captures low energy projectiles (forming H₂) more efficiently than the *ortho* or *para* sites do.

Overall, *para* dimers are roughly twice as abundant than any other in the energy range considered, and at $E_{coll} < 0.2$ eV (2320 K) they are the only ones we found. From Figure 2 it is possible to notice that the sampled area is not large enough to enclose the whole *para*-forming region already at $E_{coll}=0.2$ eV. The same holds of course for dimers lying further away from the nearest benzene ring, therefore our σ_{DF} cross sections are best considered as lower bounds to the true values. To have a better estimate of the *para* cross section we doubled the sampled area and the number trajectories at $E_{coll}=0.8$ eV, where the DF reaches its maximum. We obtained an increase of 0.7 \AA^2 in σ_{DF} which is likely to be the error arising from truncating the sampled area to $r_{max}=3.55 \text{ \AA}$.

Ortho dimers are the second most abundant species, and their cross section is the only one still increasing at $E_{coll}=1.2$ eV. Curiously, their aiming points are not centered on-top to the *ortho* C atom, instead they protrude toward the center of the adjacent benzene ring. This is a consequence of the shape of the interaction potential which forces the two atoms of the *ortho* dimer quite far from each other because steric effects.^{22,38,47}

Results from van der Waals-corrected AIMD

When computing first principles AIMD trajectories the results naturally reflect the lack of dispersive forces which standard DFT suffers. In the H-graphene system van der Waals corrected functionals have shown to improve the description of physisorption on graphene. In particular, it was recently shown that even the weak (~ 40 meV) physisorption well of H

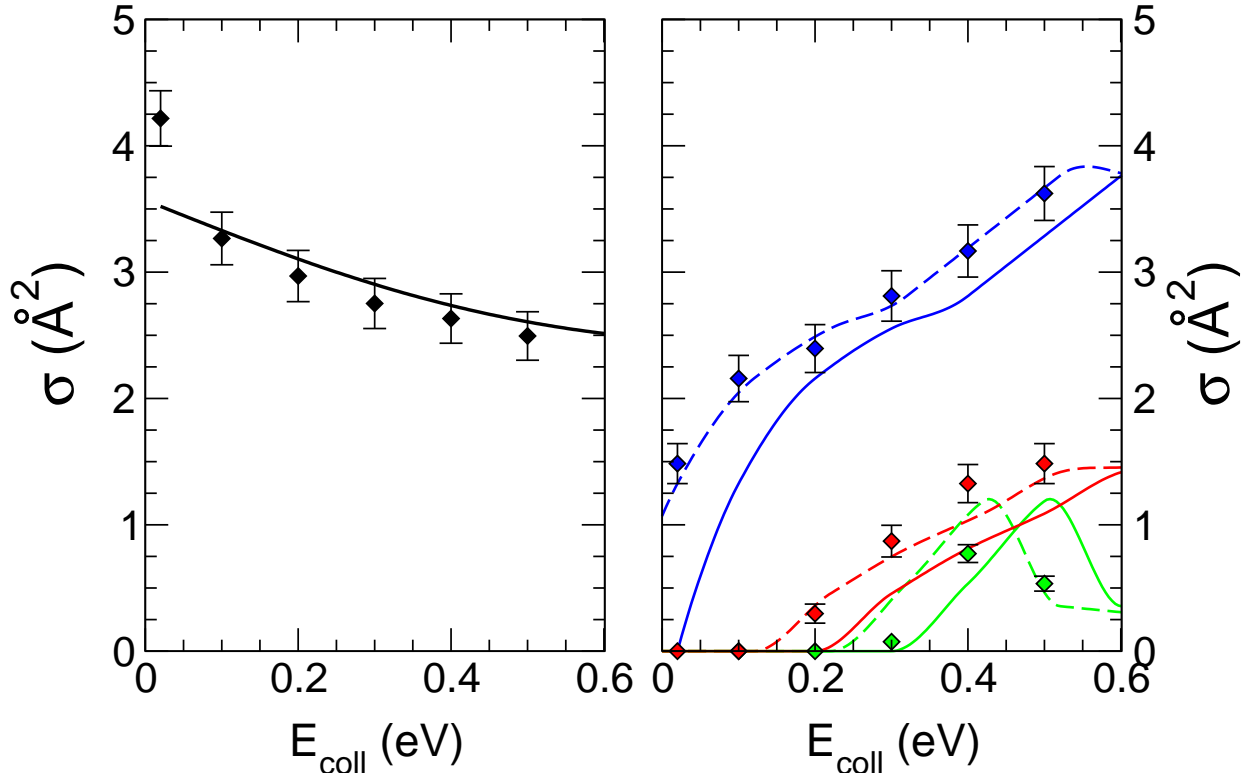


Figure 5: Effect of the van der Waals corrections to cross sections at low energies on ER (left panel) and DF (right) cross sections. Results for ER and for *ortho*, *meta* and *para* DF are given in black, red, green and blue, respectively. Diamonds show the vdW-corrected AIMD results, full lines show the AIMD results of Fig.1 and 4, dashed lines show the same results shifted by -80 meV.

atoms on PAHs could be reasonably reproduced by including simple corrections to the DFT functionals.^{38,48} Therefore we further ran AIMD trajectories using the PW91 functional with the additional Grimme’s DFT-D2 van der Waals parametric corrections⁴⁹ in the range $0.02 \text{ eV} < E_{\text{coll}} < 0.5 \text{ eV}$. The results of these calculations are shown in Figure 5.

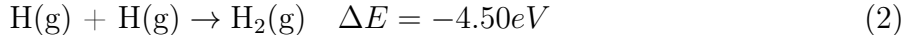
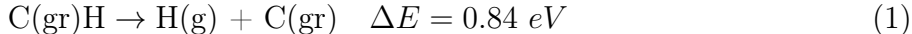
For the case of the ER reactive channel, the van der Waals corrected results are significantly different from the non-corrected ones only at $E_{\text{coll}}=0.02 \text{ eV}$, for which σ_{ER} is increased by 0.67 \AA^2 . This is consistent with recent kinetic Monte Carlo simulations, which estimated the effect of steering in the abstraction process in about 1 \AA^2 of the cross-section⁵⁰ (once corrected for the spin statistics). The enhanced reactivity comes from an enlargement of the capture radius of the target H atom, which follows from the increased interaction of the projectile with the surface.

In contrast, the DF cross sections increase in the whole energy range considered, and their thresholds move toward lower energy, eventually disappearing (see the case of the *para* dimers in Figure 5). This effect is due to the lowering of the chemisorption barriers and the increased attractive potential due to the DFT-D2 contribution. At a closer inspection it is possible to notice that the van der Waals corrected results can be reproduced by shifting toward low energies the uncorrected ones by 80 meV. Therefore we can infer that the correction has the effect of accelerating the projectile by this amount.

It should be noted though that the effect of the vdW forces is likely to be overemphasized with the adopted correction. Although necessary for reproducing the physisorption well far from the surface the effect of Grimme’s D2 correction extends indeed to much smaller values of the height of the projectile above the surface. The vdW correction reduces the adsorption barrier and increases the chemisorption energy,²⁰ at odds with the long range nature of the vdW interactions. Particularly important is the effect on the barrier to sticking, since the latter already suffers from a general underestimation due to the use of a semilocal functional⁵¹ and is likely to be better reproduced without such correction. Better results are expected from the use of vdW-functionals, which though are not yet practical for AIMD if a good statistics is required.

Energy Budget

The reaction enthalpy for the recombination process is:



$$\Delta E_{\text{react}} = 0.84 \text{ eV} - 4.50 \text{ eV} = -3.76 \text{ eV} \tag{3}$$

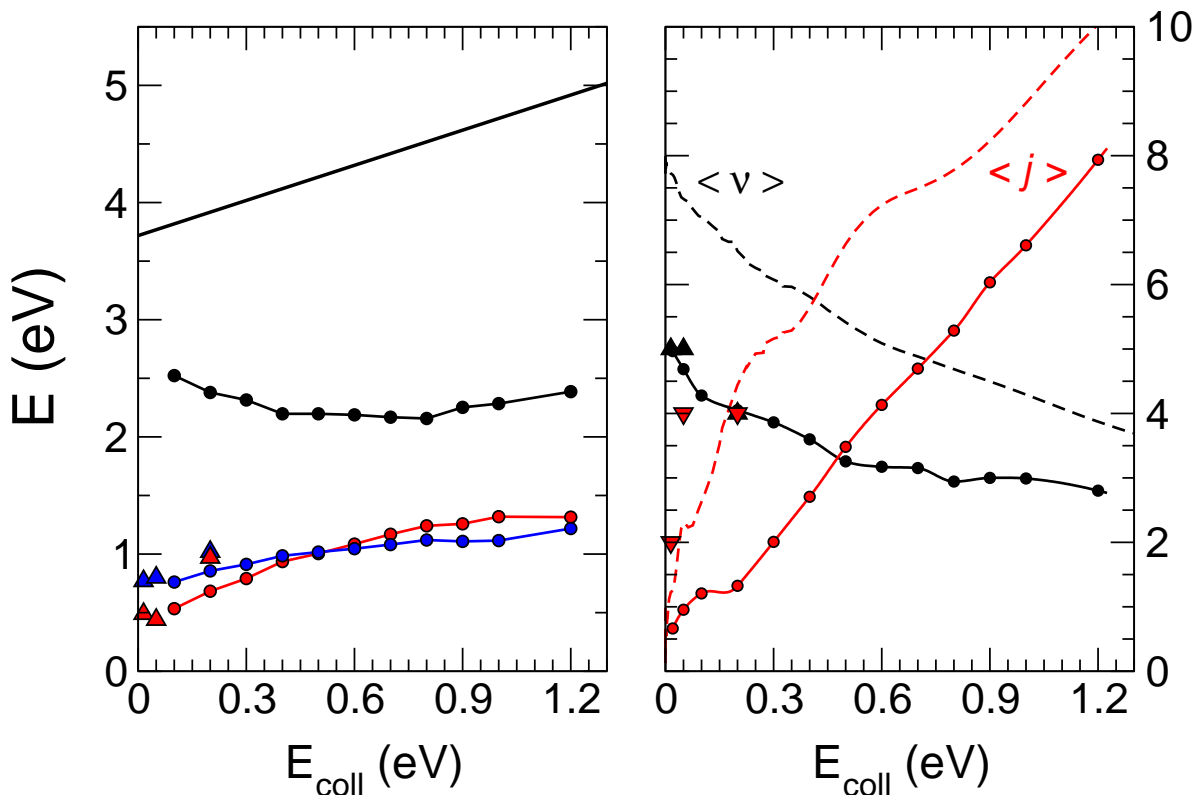


Figure 6: Left panel: Partitioning of the reaction energy into surface degrees of freedom (blue), H₂ center of mass (red) and H₂ internal (black) motion. The black line shows the total energy of the system ($\Delta H_{react} + E_{coll}$). Right panel: average H₂ vibrational (black) and rotational (red) quantum number as obtained from AIMD (dots-full lines) and quantum (dashed lines) calculations. Triangles are classical trajectory results from Ref.,⁴⁴ color codes follow those of AIMD data.

The partitioning of the reaction energy *plus* the collision energy into surface and molecular degrees of freedom is shown in Figure 6. Most of the reaction energy is stored in the product internal (vibrational and rotational) degrees of freedom, *i.e.* product molecules are rovibrationally hot, consistently with many previous findings.^{31-33,40}

The energy transfer to the surface is about 20% of the available energy, in agreement with the findings of Ref. 44. It changes only slowly with increasing E_{coll} and is generally larger than that found in other studies which limited somewhat the surface atoms motion.^{52,53} Interestingly, the amount of energy left on the surface (~ 0.9 - 1.0 eV) compares rather well with the puckering energy, *i.e.* the energy needed to move the C atom out of the pristine

surface at a height it has when binds a hydrogen atom. This shows that reaction is close to the sudden limit: the molecular product is formed on a time scale shorter than the one needed for surface relaxation, the carbon atom remains essentially frozen in its puckered configuration and only at later times, when H_2 is far away from the surface, it releases its excess energy. The slight increase with collision energy is just caused by the additional energy transfer due to the impulsive collision of the projectile.

Importantly, the energy transferred to the lattice is significant, and the formation of hydrogen molecules considerably heats the interstellar grains. Using the low temperature Debye expression of the specific heat $c_v = 12\pi^4/5 \times n \times k_B \times (T/\Theta_D)^3$, where $n \sim 4/35.3 \times 10^{30} \text{m}^{-3}$ is the number density of carbon atoms in graphite, and $\Theta_D \sim 400 \text{K}$ is its Debye temperature⁵⁴ – we estimate that formation of a *single* H_2 molecule on a grain $1\mu\text{m}^3$ -sized at $T = 5 \text{K}$ increases its temperature by $2.2 \times 10^{-4} \text{K}$.

The internal energy of the product molecule initially decreases and then increases from around 0.6 eV. This behavior may be understood by looking at the average vibrational and rotational quantum numbers of the nascent H_2 . At low collision energies the product is mostly vibrationally hot and rotationally cold. At higher energies rotational excitation increases quickly as the vibrational one decreases, as more large-impact-parameter trajectories rebounding on the repulsive potential of the surface gets captured by the target (see Fig.3 and sec. "Eley-Rideal H_2 recombination"). The values for $\langle v \rangle$ and $\langle j \rangle$ are significantly smaller than those obtained with quantum calculations in the rigid surface approximation,³¹ though present similar dependence on the collision energy. This effect could be anticipated, since the graphite surface dissipates part of the reaction energy by exciting phonons. Nevertheless our AIMD results for the average rotational quantum number of H_2 are also smaller than those obtained using the Brenner-like potential,⁴⁴ thereby suggesting that the attractive well localized on the para site affects not only the cross section but also the detailed dynamics of molecular formation.

Comparison with experiments

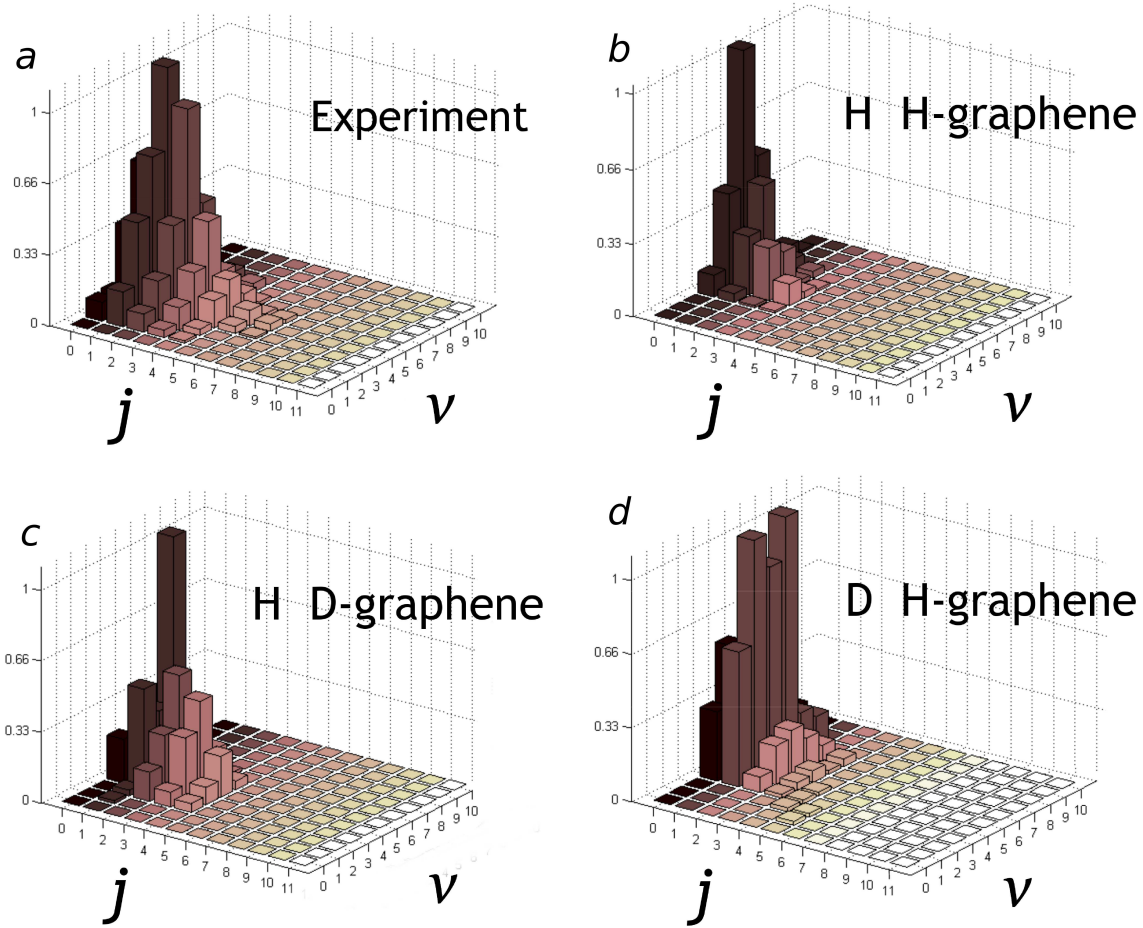


Figure 7: Relative ro-vibrational population for the product molecule. *a*: Experimental results from Ref. ⁵⁵ for the recombination of H and D beams ($T_{gas}=300$ K) on HOPG kept at $T_{surf}15$ K. *b – d*: AIMD results at $E_{coll}=20$ meV (~ 230 K) for H impinging on chemisorbed H, H on D and D on H respectively.

The AIMD cross sections can be compared with those obtained experimentally by integrating the peaks of thermal desorption spectroscopy (TDS) profiles. In these experiments, an atomic beam of hydrogen atoms is directed toward a HOPG (highly oriented pyrrolytic graphite) surface which has been previously exposed to D atoms, at different coverages. In these conditions, other reaction mechanisms cannot be excluded *a priori*, in particular hot-atoms (HA) recombination was found to be efficient for H on metals and should be expected for graphite as well. ⁵⁶ Indeed TDS data for HOPG²⁶ are similar to those for the Cu(111)

surface, in which HD formation rate does rise linearly with the coverage (as expected for an ER process) but because of formation of HAs with a preference for reaction over sticking. Graphite has a physisorption well of about 40 meV^{15,16} which may host fast diffusing projectiles. In this scenario, a HA mechanism cannot be excluded and may also explain the detection of D₂ molecules.²⁶ To remove the HA fraction from the experimental cross-sections we take as a reference the (same) limiting value observed either at high surface temperatures or at a high D coverage.²⁷ In these conditions HAs cannot contribute to the reaction either because they desorb before encountering their reaction partner or because the crowd of H atom makes ER much more likely. At saturation D pre-coverage ($\Theta=0.4$ ML) the recombination cross-section gets independent on the surface temperature²⁶ and levels off at the same value obtained at a high T_s value (400 K),²⁷ about 3.75 \AA^2 for a hyperthermal beam at $T \sim 2000$ K. We compare this value with that obtained with AIMD at a collision energy of 0.2 eV, the closest to the corresponding maximum of the Maxwell-Boltzmann distribution of the experimental H sources. At the surface coverage of the simulation ($\theta=1/18$ ML \simeq 0.055 ML) after running 1000 trajectories per irreducible area we obtain $\sigma_{ER}=3.77 \pm 0.15 \text{ \AA}^2$ for H impinging on H, $\sigma_{ER}=3.92 \pm 0.15 \text{ \AA}^2$ for H impinging on D, and $\sigma_{ER}=3.99 \pm 0.15 \text{ \AA}^2$ for D impinging on H. The agreement is rather good, despite the simulated conditions are not exactly the same as the experimental ones.

Some more experimental data are available for the population of ro-vibrational states of the nascent molecular product.^{55,57,58} In this series of studies, a H atoms beam with mean energy of 300 K recombines with pre-dosed D atoms on a graphite surface at 15 K and product HD internal state are probed with laser spectroscopy. A comparison of experimental and AIMD results at $E_{coll}=20$ meV is shown in Figure 7. Experiments found most of the products in a low-lying rotational state, while they have a significant vibrational excitation. Our simulations reproduce semi-quantitatively this behavior, and show rather peaked distributions with dominant contributions from the state $\nu=5, j=1$ for H on D and from $\nu=5, j=0$ for H on H. For D impinging on chemisorbed H, on the other hand, we found a much

broader distribution, though still peaked at a low rotational and at high vibrational quantum numbers ($(j, \nu) = (1, 4 - 6)$). Overall, our results are in rather good agreement with the experiments, with only minor deviations from the experimentally determined rovibrational distributions.^{55,57,58} This suggests that, under the above described experimental conditions, ER recombination dominates over LH: if reaction followed Langmuir-Hinshelwood kinetics H₂ product molecules would be rotationally hot.^{59,60} Hence, the low surface temperature used in the experiment prevents physisorbed species to desorb but cannot preclude trapping in (facile) chemisorption sites where direct ER recombination with a gas phase atom can occur.

Quantitative data for dimer formation are still lacking, although some information may be inferred from STM experiments and vibrational spectroscopy. From our AIMD results we expect that Eley-Rideal recombination dominates at low energy, where *para* DF cross section is found to be much smaller than the ER one. This is in qualitative agreement with recent experiments in which a HOPG surface pre-covered with D atoms is observed to form dimers and clusters only when irradiated with highly energetic H atoms,⁶¹ while at low energy ($E_{coll}=25$ meV) only ER abstraction occurs.⁶² These data also suggest that the use of van der Waals interaction in the AIMD does not improve the quality of the simulations, since it promotes dimer formation even at very low collision energies. Unfortunately, in our simulations formation of *ortho* dimers was found to be efficient only at $E_{coll} \geq 0.3$ eV, while in experiments such dimers were found to be already abundant at this energy. Hence, in this case the vdW corrections would improve the AIMD simulations, thereby contradicting the previous case. This finding signals the need of a higher correlation level in the simulations which can overcome the limits of the semilocal functionals and of an empirical vdW correction.

The AIMD results have also an important application for the chemistry of the ISM, where H₂ probably forms *via* recombination of chemisorbed species. Since *para* DF is a barrier-

less process, in principle it may initiate a catalytic cycle on the graphitic dust grains. In this process a chemisorbed H atom firstly pairs with a H atom to form a *para* dimer *via* barrierless adsorption, then it undergoes ER abstraction (also barrierless) to produce H₂ and returns to the original configuration.²³ This efficient synthetic pathway would explain the high abundance of H₂ molecules in diffuse clouds, but our results clearly show that at the gas temperatures relevant for the ISM clouds (10-100 K, *i.e.* 10⁻⁴ – 0.01 eV) no dimer formation occurs. Therefore, this suggestive hypothesis is only plausible at the higher temperatures of PDR or shocked regions where DF can effectively compete with ER abstraction.

Summary and conclusions

We studied the dynamics of H atoms on a graphene surface including the full lattice corrugation and its motion with the help of *ab initio* molecular dynamics. We computed cross sections for Eley-Rideal recombination and for the competing dimer formation channel, showing that at low collision energies the H₂ formation is a very efficient process due to projectile steering. At energies larger than 0.3 eV the formation of H dimers dominates, and *para* dimers are found to form twice as much as any other dimer species. We critically analyzed the role of vdW corrections, and determined the energy transferred to the lattice. Our findings suggest that molecular formation *via* ER recombination considerably heats the interstellar grains, releasing the puckering energy initially stored in the surface when chemisorbing the target atom. We further computed detailed ro-vibrational distributions at selected energies for different isotopic combinations, and compared our results with existing experiments. Reaction cross-sections and product H₂ ro-vibrational populations were found in good agreement with experimental results, proving that AIMD is a reliable method to study complex reactions at surfaces, where most often many competing channels need to be taken into account.

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