

Ferromagnetically correlated clusters in semimetallic Ru₂NbAl Heusler alloy and its thermoelectric properties

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In this work, we report the structural, magnetic, electrical and thermal transport properties of the Heusler-type alloy Ru₂NbAl. From the detailed analysis of magnetization data, we infer the presence of superparamagnetically interacting clusters with a Pauli paramagnetic background, while short-range ferromagnetic interaction is developed among the clusters below 5 K. The presence of this ferromagnetic interaction is confirmed through heat capacity measurements. The relatively small value of electronic contribution to specific heat γ (~ 2.7 mJ mol⁻¹ K⁻²) as well as the linear nature of temperature dependence of the Seebeck coefficient indicate a semimetallic ground state with a pseudogap, which is also supported by our electronic structure calculations. The activated nature of resistivity is reflected in the observed negative temperature coefficient and has its origin in the charge carrier localization due to antisite defects, inferred from magnetic measurements as well as structural analysis. Although the absolute value of thermoelectric figure of merit is rather low ($ZT = 5.2 \times 10^{-3}$) in Ru₂NbAl, it is the largest among all the reported nondoped full Heusler alloys.

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I. INTRODUCTION

Since their discovery in 1903, Heusler alloys, having a general formula X₂YZ (*X/Y* are transition metals, *Z* = *p*-block elements), have constantly drawn the attention of the researchers due to their remarkable magnetic and transport properties [1–3]. The Heusler alloys crystallize in the L2₁ structure (space group: $Fm\bar{3}m$), which consists of four interpenetrating *fcc* sublattices where the *X* atoms are located at $(\frac{1}{4}\frac{1}{4}\frac{1}{4})$ and $(\frac{3}{4}\frac{3}{4}\frac{3}{4})$ positions, whereas the *Y* and *Z* atoms are at $(\frac{1}{2}\frac{1}{2}\frac{1}{2})$ and (0 0 0) positions, respectively [3,4]. This family of compounds includes weak ferromagnets, antiferromagnets, ferrimagnets, half-metallic ferromagnets, metals, semimetals, as well as semiconductors [3]. The valence electron count (VEC) per formula unit of these alloys has a great influence in determining the wide variations in physical properties. For example, the total magnetic moment (*M*) per unit cell depends on VEC and is generally estimated to be $M(\mu_B) = |\text{VEC} - 24|$ (Slater-Pauling rule) [5]. Many members of this class established the validity of the Slater-Pauling rule, e.g., Mn₂VAl (VEC 22) has a moment of $1.94 \mu_B/\text{f.u.}$ at 5 K [6], whereas Co₂FeSi (VEC 30) exhibits a moment of $5.97 \mu_B/\text{f.u.}$ at 5 K [7]. Thus Heusler alloys with VEC 24 are expected to be nonmagnetic with a vanishing total magnetic moment per unit cell. Several materials having VEC 24 that have been discovered till now, e.g., Fe₂VAl, Fe₂VGa, Fe₂TiSn, etc. [8–10], are indeed found to be nonmagnetic. Interestingly, in all these compounds having VEC 24, a narrow gap or pseudogap has been found in the vicinity of the Fermi level

and hence they exhibit semiconducting or semimetallic behavior [8,10,11]. However, various inconsistencies are also reported in the experimental measurements of magnetic properties of these alloys. As for example, in spite of having VEC 24, cluster glass behavior has been reported in Fe₂VAl [12]. Such discrepancies arise primarily due to the presence of antisite defects and disorders introduced during the synthesis and annealing process [13–16]. In the case where the atoms on the (0 0 0) and $(\frac{1}{2}\frac{1}{2}\frac{1}{2})$ positions are fully exchanged, the Heusler alloy then adopts the averaged B2 structure type whereas in the extreme case where all the sites are randomly occupied by all the atoms, the alloys adopt the A2 structure type [3]. Several kinds of antisite defects have been reported at low concentration in Heusler alloys: in Fe₂VAl, for instance, Fe_V and Fe_{Al} are experimentally known to occur [16,17]. According to a theoretical study [18], V_{Al} antisite defects influence neither the magnetic properties nor the transport properties whereas the Fe_V and Fe_{Al} defects bear a magnetic moment ($\sim 4 \mu_B$) and give rise to electronic states in the pseudogap. Having a narrow gap/pseudogap in the vicinity of the Fermi level, these compounds are considered to be suitable for thermoelectric applications. The efficiency of a thermoelectric device varies like the Carnot efficiency and the dimensionless figure-of merit of its constituting materials, $ZT = \frac{S^2 T}{\rho \kappa}$, where *S* is the Seebeck coefficient, and ρ and κ are the electrical resistivity and thermal conductivity, respectively. For a thermoelectric material, a value of *ZT* close to or larger than 1 is generally considered to be large

enough to give rise to applications. The highest value of ZT at room temperature (RT) has been found in the compound Bi_2Te_3 ($ZT \sim 1$) [19]. However, Te is toxic and expensive, which makes Bi_2Te_3 commercialized only in niche markets like localized or silent cooling. Pristine Heusler alloys display $ZT \sim 10^{-3}$ at RT whereas careful doping, leads, for instance, to $ZT \sim 0.2$ in $\text{Fe}_2\text{V}_{0.9}\text{W}_{0.1}\text{Al}$ [20]. Heusler alloys with VEC 24 are also considered for applications such as the magnetic information storage where they could play the role of a thin nonmagnetic buffer layer sandwiched between two ferromagnetic thin layers of Heusler alloy acting as a spin polarizer in a recording head [21,22].

Since Ru is isoelectronic to Fe, some attempt have also been made to study and compare the properties of Ru-based full Heusler alloys (VEC 24) with Fe_2VAl and similar other materials. We have earlier reported the successful synthesis of two new compounds: Ru_2VAl and Ru_2VGa [23,24]. Thermoelectric properties of Ru_2NbGa [25], Ru_2TaAl [26], and $\text{Ru}_2\text{VAl}_{1-x}\text{Ga}_x$ [27] have also been investigated recently. In the present work, we report a detailed study of the structural, magnetic, and transport properties of the Heusler alloy Ru_2NbAl , whose crystal structure has only been reported so far [28]. Band-structure calculations have also been performed for better understanding of the ground-state properties. Our experimental data and calculations suggest that this compound is a semimetal. We have also measured $ZT = 5.2 \times 10^{-3}$ as a value of the thermoelectric figure of merit in Ru_2NbAl at RT. This value, though relatively small, is found to be one of the largest among the nondoped Heusler alloys reported in the literature.

II. EXPERIMENTAL AND COMPUTATIONAL METHODS

Ru_2NbAl was prepared by a melting process taking stoichiometric amounts of the constituent elements Ru (>99.9%), Nb (>99.9%), and Al (>99.9%) in an arc furnace on a water cooled copper hearth under a flowing Ar atmosphere. The resultant ingot was melted several times, flipped after each melting, to promote homogeneity. The weight loss during the whole process was found to be less than 0.5%. Following the postsynthesis sample treatment procedure reported earlier in Fe_2VAl [29], we have also annealed the as-cast ingot of Ru_2NbAl at 1273 K for 48 hours in a vacuum sealed quartz tube and then quenched in ice water. After cleaning the surface of the sample, it was again annealed at 1223 K for 12 hours following the same procedure. The sample was then cut in appropriate shapes and polished. The appropriately shaped sample was again annealed for 2 hours at 1173 K using a similar procedure to remove any surface strain that could have developed due to the mechanical stress in the process of cutting and polishing, as some Heusler alloys are indeed found to be highly prone to cold work [29,30]. The elemental composition of the annealed material had been estimated by the wavelength dispersive spectroscopy based electron probe microanalysis (EPMA) technique [Model: SX 100, Cameca, France]. An essentially single phase nature of Ru_2NbAl was identified by powder x-ray diffraction (XRD) technique at room temperature using $\text{Cu K}\alpha$ radiation in a powder diffractometer having a rotating anode x-ray source at 9 kW [Model: TTREX III, Rigaku, Japan]. The XRD

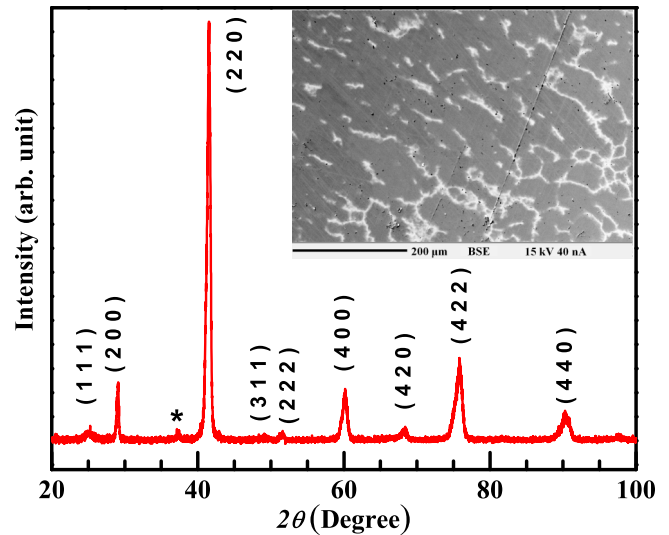


FIG. 1. Powdered x-ray diffraction pattern of Ru_2NbAl , measured at room temperature and indexed considering the $L2_1$ crystal structure, with a weak extra peak marked by an asterisk. (Inset) Back scattered electron image of Ru_2NbAl .

spectra had also been collected in various temperatures ($12 \leq T \leq 300$ K) using the same powder diffractometer. The XRD patterns had been analyzed by the Le Bail refinement method using the FULLPROF software [31]. Thermal transport [$\rho(T)$, $S(T)$, $\kappa(T)$], magnetic [$M(T, H)$], and heat capacity (in the absence of external magnetic field) measurements were performed in the temperature range 2–300 K using commercial set ups [Models: SQUID-VSM and PPMS Evercool-II, Quantum Design Inc., USA].

Electronic structure calculations were carried out using a full potential linearized augmented plane wave (FP-LAPW) method as implemented in WIEN2K package [32,33]. Since the traditional exchange functionals like LDA and GGA might underestimate the band gap, we have cross checked the band profile with the Tran-Blaha modified Becke-Johnson (TB-mBJ) functional [34,35]. Spin-orbit coupling has been incorporated using a second variation scheme [36]. Transport coefficients such as Seebeck coefficient (thermopower) (S in $\mu\text{V/K}$) and electrical conductivity scaled by relaxation time (σ/τ in $\Omega^{-1}\text{m}^{-1}\text{s}^{-1}$) were calculated using the BOLTZTRAP code [37] with a dense k mesh of the order of $50 \times 50 \times 50$ k points. The BOLTZTRAP code is based on the rigid band approximation [38–40] and the constant scattering time approximation, and these approximations have been successfully applied earlier for several thermoelectric materials [41–45].

III. RESULTS AND DISCUSSION

A. Structural details

The room temperature XRD pattern of Ru_2NbAl is presented in Fig. 1. Except a peak of negligible intensity (<2% of most intense peak) at $\sim 37^\circ$, all the other peak positions could be indexed by the $L2_1$ crystal structure (space group: $Fm\bar{3}m$) (Fig. 1) as suggested in the literature [28] and the lattice constant is found to be $6.1504(8)$ Å. The peak at $\sim 37^\circ$ has, however, been found in many Ru-based Heusler alloys and

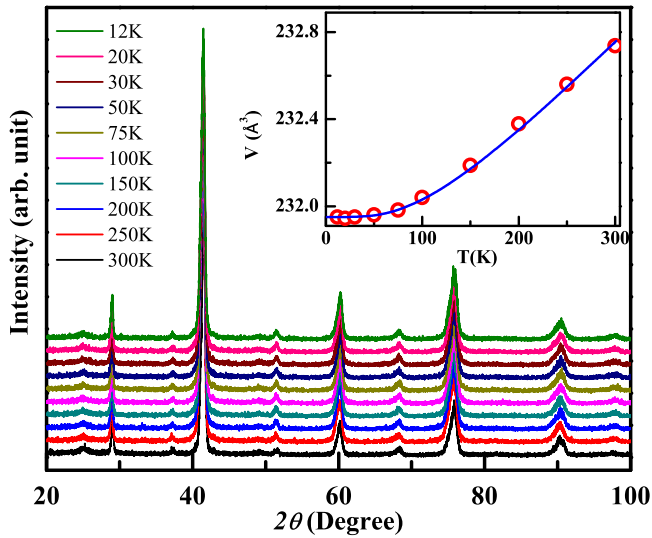


FIG. 2. Low-temperature XRD pattern of Ru_2NbAl down to 12 K. (Inset) Temperature dependence of unit-cell volume of Ru_2NbAl . Solid line represents a fit to Eq. (1).

generally assigned to unreacted Ru [25,46]. It has also been found that the presence of this minor phase in the material hardly influences its transport and magnetic properties [25,46]. The EPMA measures a composition $\text{Ru}_{2.08(1)}\text{Nb}_{0.88(3)}\text{Al}_{1.04(3)}$ for the main Heusler phase and $\text{Ru}_{65}\text{Nb}_{33}\text{Al}_2$ for the other phase(s), distributed at the grain boundaries (Fig. 1, inset). Examination of the Nb-Ru phase diagram [28] suggests that $\text{Ru}_{65}\text{Nb}_{33}\text{Al}_2$ is the spatially averaged composition of a eutectic which mixes the NbRu and Ru phases, in agreement with XRD. The slightly nonstoichiometric composition of the main Heusler phase suggests the occurrence of Ru_{Nb} and Al_{Nb} antisite defects.

The low temperature XRD patterns taken in the range of 12–300 K do not show any significant change suggesting the invariance of crystal structure down to 12 K, the lowest temperature attainable in our diffractometer (Fig. 2). The lattice parameter gradually decreases as the temperature decreases. The unit-cell volume as a function of temperature [$V(T)$] is plotted and fitted (Fig. 2, inset) using the equation

$$V(T) = \gamma U(T)/K_0 + V_0, \quad (1)$$

where V_0 is the unit-cell volume at $T = 0$ K, K_0 represents the bulk modulus, and γ is the Grüneisen parameter. $U(T)$ is the internal elastic energy, generally expressed according to the Debye approximation as

$$U(T) = 9NK_B T \left(\frac{T}{\Theta_D} \right)^3 \int_0^{\frac{\Theta_D}{T}} \frac{x^3}{e^x - 1} dx, \quad (2)$$

where N is the number of atoms per unit cell. Using this approximation, a Debye temperature $\Theta_D = 410$ K and a Grüneisen parameter $\gamma = 1.8$ have been estimated for Ru_2NbAl . This value of Debye temperature is consistent with the value further derived from heat capacity measurements ($\Theta_D = 418$ K) (discussed later). This value is smaller than that reported for Fe_2VAl ($\Theta_D = 540$ K) [47], most likely due to the heavier atomic mass of the chemical elements constituting Ru_2NbAl .

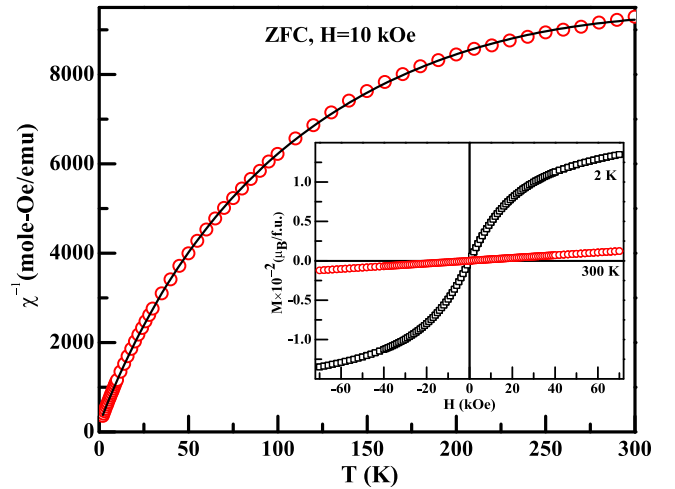


FIG. 3. Temperature dependence of inverse magnetic susceptibility of Ru_2NbAl measured in a 10 kOe applied magnetic field under ZFC configuration. (Inset) Isothermal magnetization at 2 and 300 K of the same sample.

B. Magnetic properties

1. Magnetic susceptibility

To understand the magnetic properties of Ru_2NbAl , magnetic susceptibility (χ) measurements have been carried out under both zero field cooled (ZFC) and field cooled (FC) configurations at $H = 10$ and 70 kOe. The magnetic susceptibility exhibits no thermoremanence behavior between ZFC and FC protocol for both the magnetic fields. The absence of any anomaly in the magnetic susceptibility suggests the compound remains essentially paramagnetic down to the lowest measured temperature, 2 K (Fig. 3). The dominance of temperature independent Pauli paramagnetic behavior is evident as the magnetization changes very slowly in the temperature range 300–100 K. On further lowering of the temperature below 100 K, the magnetization starts to increase at a faster rate, particularly below 20 K. This behavior indicates the presence of a small localized paramagnetic contribution over a Pauli paramagnetic background.

To estimate this localized paramagnetic contribution, we have plotted the inverse susceptibility (χ^{-1}) as a function of temperature in Fig. 3. In case of localized magnetic spins, $\chi^{-1}(T)$ is known to exhibit a linear Curie-Weiss behavior. The inverse susceptibility of Ru_2NbAl could thus be very well fitted with a modified Curie-Weiss law,

$$\chi(T) = \chi_0 + \alpha T^2 + \frac{C}{T - \theta_p}, \quad (3)$$

where χ_0 represents temperature independent Pauli paramagnetic or diamagnetic contributions, while αT^2 is the temperature dependent higher order contribution to Pauli paramagnetism, generally not considered in the zero-order approximation [48]. The third term describes the standard Curie-Weiss expression. The fit of $\chi^{-1}(T)$ for $H = 10$ kOe yields $\chi_0 = 6.76(4) \times 10^{-5} \text{ emu mol}^{-1} \text{ Oe}^{-1}$, $\mu_{\text{eff}} = 0.27(2) \mu_B$, $\theta_p = -1.61(7) \text{ K}$, and $\alpha = 1.08(4) \times 10^{-10} \text{ emu mol}^{-1} \text{ Oe}^{-1} \text{ T}^{-2}$. The fitted parameters remain essentially the same for the $H = 70$ kOe measurement

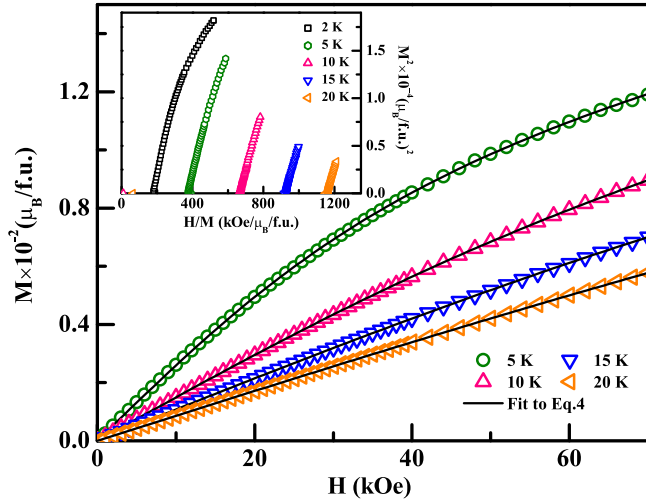


FIG. 4. Isothermal magnetization data at various temperatures for Ru_2NbAl . The solid lines represent the fit of the data using Eq. (4). (Inset) Arrott plots (M^2 versus H/M) for Ru_2NbAl at different temperatures.

as well. Such small values of μ_{eff} and θ_p point towards the very weak nature of the localized spins in this compound. One may note here that the observation of such small local moment in Ru_2NbAl is not at all unusual despite the fact that all the constituent atoms in this material are generally considered to be nonmagnetic in nature. We may point out here that magnetic order has earlier been reported in many similar compounds, viz. Cu_2VAl [49], Pd_2TiAl [50], SrRuO_3 [51], etc. Even theoretically, it has been predicted that Ru_2VZ ($Z = \text{Si, Ge, Sn}$) series of compounds, if could be formed in a single phase, should order ferromagnetically [52].

2. Isothermal magnetization

The isothermal magnetization [$M(H)$] curve of Ru_2NbAl at 300 K is linear (Fig. 3, inset), as expected for a paramagnetic material. Interestingly, the $M(H)$ curve at 2 K deviates from linearity and magnetization slowly approaches towards a saturationlike behavior at a field higher than 70 kOe but does not exhibit any hysteresis (Fig. 3, inset). We have also measured $M(H)$ at 5, 10, 15, and 20 K in the field range 0–70 kOe (Fig. 4). As temperature increases, the nonlinearity in the isothermal magnetization gradually gets weakened, becoming almost linear above 20 K. This is at variance with the absence of any signature of long-range interactions down to 2 K as the $\chi(T)$ curve of Ru_2NbAl does not show any anomaly in this temperature range. This is also confirmed by the heat capacity measurement (discussed later) and the Arrott plot (M^2 versus H/M) that fails to exhibit any spontaneous magnetization (Fig. 4, inset) even at 2 K. Generally, in systems that exhibit no long-range ferromagnetic ordering, such S-shaped anhysteretic $M(H)$ curve (at 2 K) could have its origin in short range ferromagnetic (FM) interactions or a superparamagnetic (SPM) state, or a combination of both [12,53]. This additional magnetic interaction appears to develop only below 20 K, where the magnetic isotherms start to deviate from a linear behavior.

TABLE I. Parameters extracted from the fit of magnetic isotherms of Ru_2NbAl to Eq. (4) for temperature range 5–20 K and SPM fit parameters from RA + SPM fit of 2 K data using Eq. (7) + $M_S L(x)$.

T (K)	μ (μ_B)	M_S ($\mu_B/\text{f.u.}$)	χ ($\mu_B/\text{f.u.}$)	M_S/μ (/f.u.)	N (/mol)
2	3.883	0.00422	0	0.00108	0.65×10^{21}
5	4.348	0.01080	5.372×10^{-4}	0.00248	1.49×10^{21}
10	4.515	0.01032	4.570×10^{-4}	0.00228	1.37×10^{21}
15	4.721	0.00938	4.193×10^{-4}	0.00198	1.19×10^{21}
20	4.675	0.00920	3.767×10^{-4}	0.00196	1.18×10^{21}

In order to investigate the origin of the saturationlike behavior observed at low temperatures, in our first attempts, the magnetic isotherms were analyzed considering short range FM interactions through the Néel-Brown (NB) [54] and the micromagnetic (MM) [55] models. However, none of the isotherms, not even at 2 K, could be analyzed with either the NB or MM model, forcing us instead to consider the presence of an SPM phase in this compound. We obtained reasonably a good fit for all the $M(H)$ curves, except that taken at 2 K, by considering the equation

$$M(H) = M_S L(x) + \chi H, \quad (4)$$

where $x = \frac{\mu H}{k_B T}$, M_S represents the saturation magnetization, μ is the average magnetic moment per cluster, $L(x) = \coth(x) - 1/x$ is the Langevin function, and χ is the paramagnetic (PM) susceptibility [12,53]. The first term in Eq. (4) denotes the magnetic behavior of the SPM component, while the second term arises from the paramagnetic phase present in this material. The results of these fits are listed in Table I. It can be seen from the table that for all the temperatures from 5 to 20 K, the magnetic moment of an SPM cluster is thus estimated to be $\sim 4 \mu_B$. The value of the saturation magnetization and the number of clusters per mole (N) are nearly $0.01 \mu_B/\text{f.u.}$ and $\sim 10^{21}$, respectively, and remain closely constant throughout the temperature range 5–20 K. However, the magnetic isotherm at 2 K still does not yield a good fit and will be discussed later.

To confirm the presence of an SPM state, a more rigorous check has been carried out by drawing a universal plot of reduced magnetization (M/M_S) as a function of H/T , where the magnetization at any particular temperature is normalized with respect to the saturation magnetization at the same temperature [12]. Since $M(H)$ in Ru_2NbAl exhibits both superparamagnetic as well as paramagnetic contributions, we have subtracted the estimated paramagnetic contribution from the experimentally obtained isothermal magnetization data [$M(H) - \chi H$] and normalized with respect to the saturation magnetization at the same temperature [$(M(H) - \chi H)/M_S$], which has been finally plotted as a function of H/T in Fig. 5. All the isothermal curves up to 20 K, except that measured at 2 K, follow a single universal curve (Fig. 5). These results confirm the presence of a superparamagnetic state along with a paramagnetic state in the temperature range 5–20 K, thus suggesting the existence of noninteracting magnetic clusters in a PM matrix. The effect of intercluster interactions, if any,

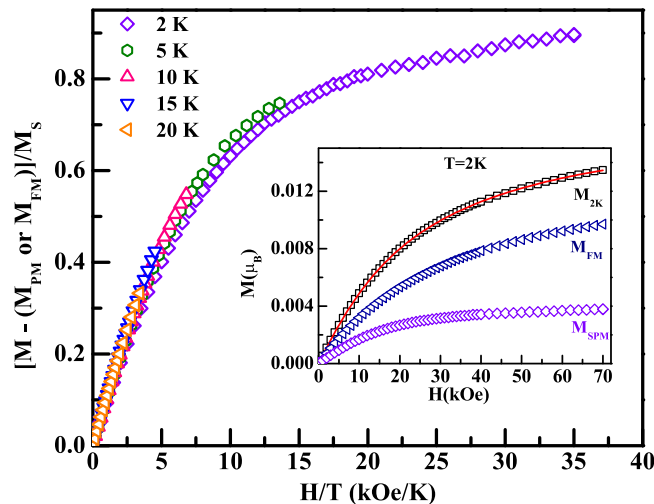


FIG. 5. Normalized magnetic isotherms corresponding to SPM contributions follow universal curve at low temperatures. (Inset) Isothermal magnetization data at 2 K and the fit using Eq. (7) together with $M_S L(x)$. The individual FM and SPM components are also shown.

must be quite weak and masked by the SPM effect in this temperature region, $5 \text{ K} \leq T < 20 \text{ K}$.

As already discussed above, a deviation from Eq. (4) is observed in the $M(H)$ curve measured at 2 K. The increase in both the magnetization value and the curvature of the magnetic isotherm at 2 K, can be attributed either to the blocking of SPM clusters or to the presence of interacting clusters that might have grown in strength below 5 K. Since there is no cusp observed in the ZFC curve down to 2 K (Fig. 3), the idea of the blocking of the SPM clusters can be ruled out, which indicates that the noninteracting SPM clusters start to interact or that some new interacting clusters develop at temperatures below 5 K. Existence of FM clusters at low temperature has also been reported in isostructural Heusler alloys, like Fe_2VAl and $\text{Fe}_2\text{V}_{1-x}\text{Cr}_x\text{Al}$ [15,17,56]. In Fe_2VAl , based on density functional theory (DFT) calculations [18,57], these ferromagnetic clusters were ascribed to Fe_V and Fe_{Al} antisite defects. To investigate the origin of interactions among clusters in our case, we have used the random anisotropy (RA) model [58], and analyzed the $M(H)$ curve at 2 K. This model deals with the ground-state configuration of magnetic materials having random anisotropy for a wide range of anisotropy strengths as well as experimentally applied magnetic fields. In case of weak anisotropy, three different regimes can be identified depending upon the relative strength of applied field (H). A parameter H_s is used to gauge the relative strength of H and is expressed as

$$H_s = H_r^4 / H_{ex}^3, \quad (5)$$

where H_r and H_{ex} are the anisotropic field and exchange field, respectively. For low-field region, $H < H_s$, one gets a correlated spin glass having large susceptibility. The intermediate-field regime, $H_s < H < H_{ex}$, is called the ferromagnet with wandering axis where the spins are nearly aligned. Any random anisotropy present in such system causes the directions of the magnetization of locally correlated regions to vary. In

this regime, the magnetization approaches saturation as

$$M(H) = M_S^{\text{FM}} \left[1 - \frac{1}{15} \left(\frac{H_s}{H} \right)^{\frac{1}{2}} \right], \quad (6)$$

where M_S^{FM} is the saturation magnetization for ferromagnetic component. For high-field region, $H > H_{ex}$, all spins are virtually aligned with the field, differing only by a small tipping angle that arises due to the random anisotropy. In such case, $M(H)$ would gradually approach towards M_S^{FM} as

$$M(H) = M_S^{\text{FM}} \left[1 - \frac{1}{15} \left(\frac{H_r}{H + H_{ex}} \right)^2 \right]. \quad (7)$$

The $M(H)$ data at 2 K could be well fitted with Eq. (7) after considering an additional SPM contribution [$M_S L(x)$, $x = \frac{\mu H}{k_B T}$] (Fig. 5, inset). The fitted parameters obtained for the RA contribution are $M_S^{\text{FM}} = 0.0124 \mu_B$, $H_r = 236.9 \text{ kOe}$, and $H_{ex} = 61.0 \text{ kOe}$. The value of H_r is larger than H_{ex} , which reveals that in our material the strength of the anisotropy is strong [58]. But surprisingly H_r also exceeds the maximum applied field, i.e., $H = 70 \text{ kOe}$. Here it may be noted that the usage of the prefactor $1/15$ in Eq. (7), which was calculated for $H_r \ll H_{ex}$ [58], can be applied only when the magnetization has reached over 93% of its saturation value [59]. However, in the present case, the saturation value of $M(H)$ at 2 K and at 70 kOe field appears to be substantially lower. As a result, using the same prefactor of $1/15$ is unlikely to be appropriate in our system that has much higher level of anisotropy and therefore requires a more suitable correction. A similar situation in case of $\text{Dy}_x\text{Y}_{1-x}\text{Al}_2$ [59], GdAl_2 [60], and $\text{Co}_{58.5}\text{Ga}_{41.5}$ [61] compounds had earlier been dealt by considering the prefactor to be of the order of 1. Accordingly, by considering a prefactor of order unity, H_r reduces to 61.2 kOe, although interestingly H_{ex} remains the same. The reduced value of H_r and H_{ex} are less than the maximum applied field (70 kOe) and thus fulfills the condition for materials having strong anisotropy as demanded by Eq. (7). The presence of such strong anisotropy would lead to make the system as speromagneticlike, where the local magnetizations generally follow the local anisotropy axis [58]. However, in our case, the occurrence of speromagneticlike state is forbidden as $H_r \leq H_{ex}$. Rather the system is more likely to have ferromagnetically correlated regions (clusters), whose magnetization directions are pinned or frozen by random anisotropy, as in a correlated glassy system.

As mentioned above, in addition to the contribution from the correlated magnetic clusters, the $M(H)$ data at 2 K also contains an additional contribution from SPM clusters (Fig. 5, inset). The SPM component obtained by subtracting the RA part, when normalized by M_S and plotted against H/T , follows the same universal curve discussed earlier (Fig. 5). The resulting parameters correspond to SPM state at 2 K are also tabulated in Table I. Although the magnetic moment per cluster remains near-about same, the value of M_S and number of SPM clusters are reduced significantly. The reduction of these superparamagnetically interacting clusters affirms that FM interaction develops among the rest of the clusters. The above analysis suggests that in case of Ru_2NbAl , although the

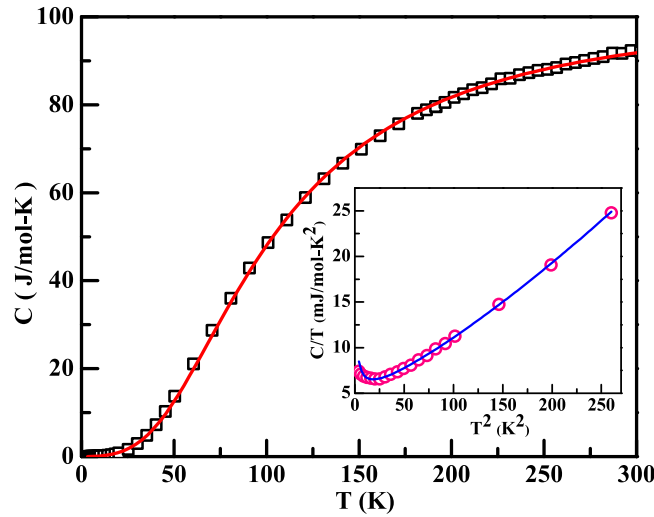


FIG. 6. Specific heat as a function of temperature of Ru_2NbAl . Solid line represents the fit to Eq. (8). (Inset) C/T vs T^2 plot at low temperature along with a fit to Eq. (10).

SPM component exists down to 2 K whereas, FM interactions becomes prevalent below 5 K. Above 20 K, the magnetization is dominated by the Pauli paramagnetic component.

C. Heat capacity

In order to verify the presence of magnetic clusters in Ru_2NbAl using another independent experimental probe, we have carried out heat capacity [$C(T)$] measurement in the temperature range 2–300 K in absence of any external magnetic field (Fig. 6). No peak could be observed in the $C(T)$ curve (Fig. 6) in the measured temperature range, which is also an indication of the absence of any long range magnetic order, similar to that inferred from magnetic susceptibility measurements.

Generally, the heat capacity of a metallic system can be written as

$$C(T) = \gamma T + 9nR \left(\frac{T}{\Theta_D} \right)^3 \int_0^{\frac{\Theta_D}{T}} \frac{x^4 e^x}{(e^x - 1)^2} dx, \quad (8)$$

where the first term represents the electronic specific heat and the second term comes from the lattice/phonon contribution. $\gamma = \frac{1}{3}\pi^2 D(E_F)k_B^2$, is the Sommerfeld coefficient, where $D(E_F)$ is the density of states at the Fermi level E_F . n is the number of atoms per formula unit (for Ru_2NbAl : $n = 4$), Θ_D is the Debye temperature and $x = \hbar\omega/k_B T$. The standard Debye model, discussed above, could explain the heat capacity data very well in the temperature range 25–300 K, by considering $\gamma = 3.7 \text{ mJ mol}^{-1} \text{ K}^{-2}$ and $\Theta_D = 418 \text{ K}$, in agreement with the value derived from the lattice parameter measurements as a function of temperature. The low-temperature data, however, deviates from the standard behavior.

In the low-temperature region, Eq. (8) can be simplified as

$$C(T) = \gamma T + \beta T^3 + \delta T^5 + \dots, \quad (9)$$

where β , δ are the coefficients. Below $\sim \Theta_D/50$, δT^5 and other higher-order terms could be neglected [62] and the heat

capacity behavior in the representation of C/T versus T^2 is expected to show a linear dependence: this is indeed the case above 5 K (Fig. 6, inset). We may mention here that a linear behaviour of C/T vs T^2 plot had earlier been reported in other Ru-based Heusler compound Ru_2TaAl in the temperature range 2–5 K [26]. However, an upturn observed in C/T versus T^2 (Fig. 6, inset) plot of Ru_2NbAl below 5 K, suggests the presence of additional contribution to the heat capacity given in Eq. (9). It may be noted here that in Ru_2NbAl , the development of ferromagnetically interacting clusters below 5 K was inferred from the isothermal magnetic measurements. Therefore, the additional contribution to heat capacity in Ru_2NbAl appears to have originated from the inter/intra-clusters interactions.

Such upturn in the low-temperature heat capacity has also been found in Fe_2VAl [63], Fe-V [64], TiFe alloys [65] where oscillation of small FM clusters have been argued to be responsible for this behavior. In those compounds, it was claimed that the system having ferromagnetic clusters in nonferromagnetic matrix normally rests in a position of minimum energy and the potential energy of the system gets enhanced when the direction of the magnetization vector of the clusters are altered due to the application of any force. The enhanced energy is generally stored in the system through the local elastic deformation of the clusters and the matrix as well as in magnetostriction energy [65]. So, due to thermal excitation, each cluster makes oscillation about a direction determined by its crystallographic anisotropy energy and absorbs $k_B T$ amount of thermal energy. This gives rise to an extra constant term $C_0 \sim 2k_B N$ to the total specific heat [63,64], where N is the number of such oscillating magnetic clusters. However, to satisfy the third law of thermodynamics, which requires the heat capacity to be zero at $T = 0 \text{ K}$, it is argued that this additional contribution, C_0 , gradually loses its strength below a certain temperature, called the Einstein temperature, $T_E = 2\beta H/k_B$, where H is the magnetic field needed to produce the same torque as the crystal anisotropy energy [64]. T_E is generally found to be very low, $< 1 \text{ K}$ in most of the materials [64,66]. So, by considering the cluster interaction term, Eq. (9) gets modified to

$$C(T) = \gamma T + \beta T^3 + \delta T^5 + C_0 + \dots. \quad (10)$$

This modified equation could reproduce quite well the experimentally observed specific heat data of Ru_2NbAl in the temperature range 2–20 K (Fig. 6, inset). We have included the δT^5 term in the fit so as to cover the extended temperature range beyond $\Theta_D/50$. The estimated values of the parameters from this fit are $\gamma = 2.7 \text{ mJ mol}^{-1} \text{ K}^{-2}$, $\beta = 0.067 \text{ mJ mol}^{-1} \text{ K}^{-4}$, $\delta = 6 \times 10^{-5} \text{ mJ mol}^{-1} \text{ K}^{-6}$, and $C_0 = 11.04 \text{ mJ mol}^{-1} \text{ K}^{-1}$. Using the value of C_0 we have calculated the number of ferromagnetic clusters as $N \sim 4 \times 10^{20}$ per mol. This number matches quite closely to the number of FM clusters ($\sim 8 \times 10^{20}$) estimated earlier from the magnetization data at 2 K (Table I).

D. Transport properties

1. Seebeck coefficient

To study the thermoelectric properties of Ru_2NbAl , we have carried out Seebeck coefficient (thermopower),

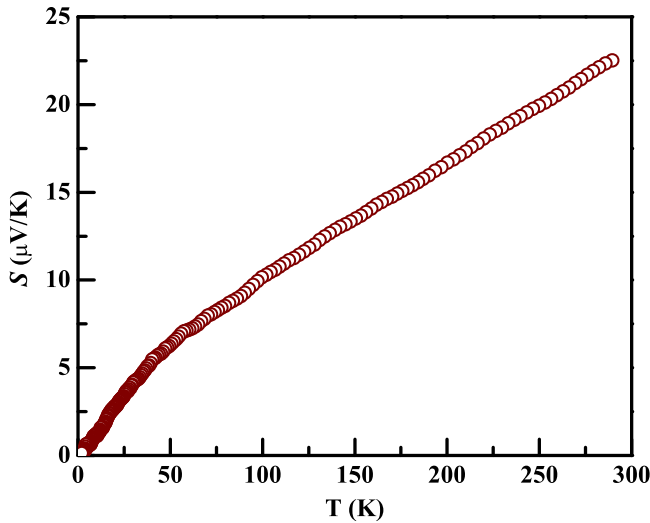


FIG. 7. Temperature dependence of Seebeck coefficient of Ru_2NbAl in the absence of magnetic field. Application of magnetic field of 80 kOe (not shown in the figure) does not have noticeable influence in the $S(T)$ behavior.

resistivity and thermal conductivity measurements in the absence ($H = 0$) and presence of a 80 kOe magnetic field. The magnetic field is found to have very insignificant impact on all the three measurements. The temperature dependent Seebeck coefficient $S(T)$ of Ru_2NbAl at $H = 0$ is only shown in Fig. 7. The measured value of S remains positive in the entire temperature range under investigation suggesting that the dominant carriers in thermoelectric transport are holes in this compound. The Seebeck coefficient at 300 K is equal to $22 \mu\text{V/K}$, a value comparable to those reported for other Heusler alloys like Fe_2VAl ($\sim 35 \mu\text{V/K}$), Fe_2VGa ($\sim 30 \mu\text{V/K}$), and Ru_2NbGa ($\sim 20 \mu\text{V/K}$) [67–72]. Such a moderate value at room temperature, combined with the linear increase from ~ 50 to 300 K is a characteristic of metallic state and suggests the possibility of a semimetallic ground state for Ru_2NbAl , in agreement with dominant Pauli paramagnetism above 20 K and the nonzero value of Sommerfeld coefficient $\gamma = 2.7 \text{ mJ mol}^{-1} \text{ K}^{-2}$. Moreover, as will be further reported below, $S_{300 \text{ K}} = 22 \mu\text{V/K}$ is also consistent with the value obtained by DFT calculations, which also conclude that Ru_2NbAl is a semimetal.

2. Resistivity

The electrical resistivity as a function of temperature [$\rho(T)$] of Ru_2NbAl , studied in the temperature range 2–300 K at $H = 0$ is shown in Fig. 8. There is no significant change in the data in presence and absence of a magnetic field, not even exhibiting any thermal hysteresis behavior. The value of resistivity is $452 \mu\Omega \text{ cm}^{-1}$ at room temperature, whereas it is found to be $\sim 538 \mu\Omega \text{ cm}^{-1}$ at 2 K, indicating that this quantity varies within a narrow range of values. These values are rather characteristic of Ru_2NbAl being a semimetal or a degenerate semiconductor, but surprisingly, the $\rho(T)$ curve exhibits a negative temperature coefficient of resistivity (TCR), characteristic of a semiconductor. Such activated behavior for the resistivity has also been reported

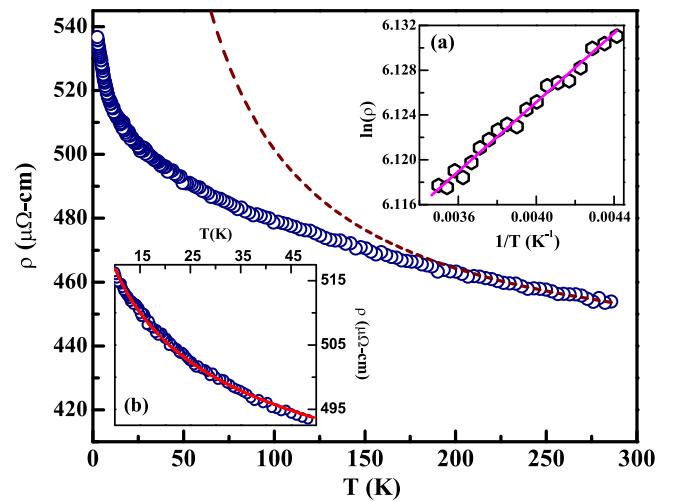


FIG. 8. The temperature dependent resistivity behavior for Ru_2NbAl at $H = 0$. [Inset (a)] $\ln(\rho)$ vs $1/T$ plot at temperature range 225–300 K. Solid line depicts a linear fit. [Inset (b)] Resistivity data below 60 K with a fit to Eq. (11).

in other Heusler alloys having VEC 24, viz. Fe_2VAl [8], Ru_2NbGa [25], Ru_2TaAl [26], etc. A plot of $\ln(\rho)$ versus $1/T$ reveals that the linear region is only found in the temperature range 225–300 K [Fig. 8, inset (a)]. The value of activation energy (Δ), estimated from the slope of the curve as $\Delta \sim 5.3 \text{ meV} \sim 63 \text{ K}$. This small value cannot be ascribed to the intrinsic band gap, which would otherwise manifests itself by a nonmonotonous variation of the Seebeck coefficient at low temperature (minority carrier effect).

The resistivity data at lower temperature ($T < 225 \text{ K}$) increases at a much slower rate than that expected (Fig. 8, dashed line) for an activated behavior. Such deviation may be attributed to the temperature dependence of carrier mobility [20]. Alternatively, negative TCR at low temperature can also be explained by variable range hopping (VRH) conduction proposed by Mott [73]. In this mechanism, electrons hop to energetically closed and localized states and conduction law of VRH can be expressed as

$$\rho(T) = \rho_0 + A \exp \left[\left(\frac{T_0}{T} \right)^{1/4} \right], \quad (11)$$

where A is a constant and T_0 is the activation temperature that depends on the localization length (ξ) as ξ^{-3} [73]. Using the above equation, the resistivity data of Ru_2NbAl can be fitted below 60 K [Fig. 8, inset(b)]. The analysis yields T_0 to be 0.25 K, a similar value (0.063 K) of the activation temperature was earlier found in $\text{Fe}_2\text{V}_{1-x}\text{Nb}_x\text{Al}$ [74]. These results are rather suggestive of localization effects of the charge carriers by structural disorder rather than of a true semiconducting ground state, as already discussed in the literature on Fe_2VAl [17,56]. The exact scenario of such localization remains currently elusive but both EPMA and magnetic measurements indicate the occurrence of structural defects in Ru_2NbAl . The latter technique shows the existence of $\sim 10^{21}$ superparamagnetic (SPM) clusters. It was reported earlier that the Fe_y and Fe_{Al} type of antisite defects in Fe_2VAl introduce localized and resonant d states into the band gap, resulting a magnetic

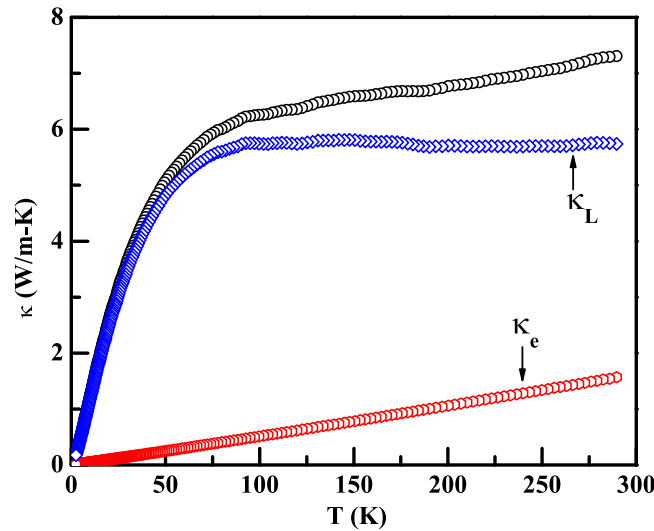


FIG. 9. Temperature variations of the total thermal conductivity κ , lattice thermal conductivity κ_L , and electronic thermal conductivity κ_e for Ru_2NbAl at $H = 0$.

moment of $\sim 4 \mu_B/\text{defect}$ [18]. V_{Al} type of defect, however, remain nonmagnetic. Since EPMA analysis of Ru_2NbAl also indicate the presence of both the Ru_{Nb} as well as Al_{Nb} type of defects, it is expected that while Ru_{Nb} defects would introduce localized moments, the magnetic contribution to Al_{Nb} would be minimal. The additional d states in the gap caused by the Ru_{Nb} defects are expected to change both the magnetic as well as the transport properties of Ru_2NbAl significantly. While the magnetic influence is manifested in the SPM behaviour, the semiconducting-like nature of the electrical resistivity may also arise from these defects.

3. Thermal conductivity

To further evaluate the thermoelectric performance of Ru_2NbAl , thermal conductivity (κ) is measured between 2–300 K, shown in Fig. 9. At low temperatures, κ increases rapidly with temperature which is typical for solids as thermal scattering by mass defects (isotopes, impurity, etc.) increases with temperature [75]. Above 50 K, the rate of increment has been slowed down and the value of κ reaches $7.3 \text{ W m}^{-1} \text{ K}^{-1}$ at 300 K (Fig. 9). In general, the total thermal conductivity of metals and semimetals is defined by a sum of electronic (κ_e) and lattice (κ_L) contributions. The electronic thermal conductivity can be estimated using the Wiedemann-Franz law $\kappa_e \rho / T = L_0$, where ρ is the measured electric resistivity and $L_0 = 2.45 \times 10^{-8} \text{ W } \Omega \text{ K}^{-2}$ is the Lorenz number. The lattice thermal conductivity, κ_L , thus can be evaluated by subtracting κ_e from the observed κ . The value of κ_e thus found to be very small, suggesting that the thermal conductivity of this compound is necessarily due to κ_L (Fig. 9). At low temperatures, κ_L increases with temperature and a maximum appears between 50 and 100 K due to the reduction in thermal scattering at low temperatures. The κ_L value of Ru_2NbAl at 300 K is estimated to be $5.6 \text{ W m}^{-1} \text{ K}^{-1}$ (Fig. 9), which is much lower than those found in Fe_2VAl ($\sim 28 \text{ W m}^{-1} \text{ K}^{-1}$) and Fe_2VGa ($\sim 17 \text{ W m}^{-1} \text{ K}^{-1}$) [69–72]. This reduction may be attributed to phonon scattering caused

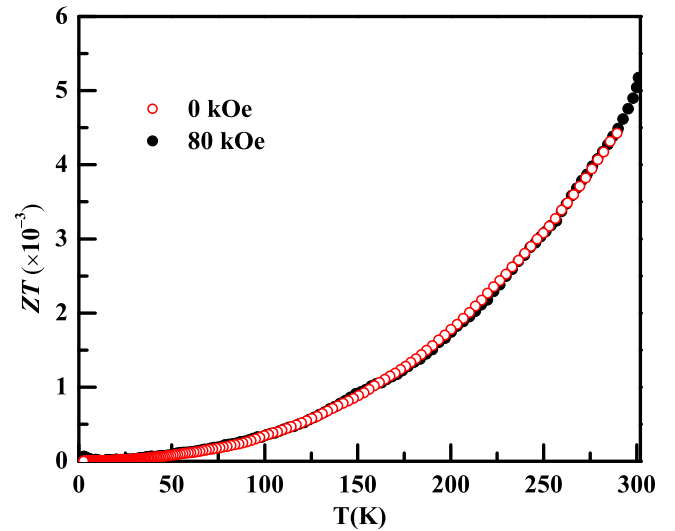


FIG. 10. ZT value as a function of temperature for Ru_2NbAl in the absence ($H = 0$) and presence ($H = 80 \text{ kOe}$) of magnetic field.

by the elemental substitution by heavier Ru and Nb atoms in the place of Fe and V in Fe_2VAl [20,26]. Antisite defect arising from the elemental substitutions is strongly related to crystal lattice strain and may also be responsible for the reduction of κ_L in Ru_2NbAl . This low value of κ observed in Ru_2NbAl , makes it a potential candidate for thermoelectric applications.

4. Figure of merit

Since Ru_2NbAl exhibits a smaller thermal conductivity and a comparable power factor (S^2/ρ) to other full Heusler alloys, its dimensionless figure of merit $ZT = 5.2 \times 10^{-3}$ (Fig. 10) is larger at room temperature than that in those alloys. Nonetheless, it is still several orders of magnitude smaller than that of the state-of-the-art thermoelectric material at 300 K, Bi_2Te_3 , which displays $ZT = 1$. Doping, to adjust the charge carrier concentration and maximize the power factor and substitution, to further decrease the thermal conductivity, will be required to improve ZT in Ru_2NbAl .

E. Electronic structure calculations

The experimental structure parameters were optimized, and further calculations are performed using those optimized parameters. We have performed the electronic structure calculations using several exchange functionals like LDA, GGA, and TB-mBJ, and the calculated band structure using the TB-mBJ functional is presented in Fig. 11. Spin-orbit coupling has been included in the calculations due to the presence of heavy elements. From the band structure, it is evident that the compound possesses semimetallic character, as argued from our experimental observations and also from an earlier reported theoretical calculation [76]. The bands cross the Fermi level around Γ and X high-symmetry points. Similar crossover behavior of the bands was earlier reported in the electronic structure of prototype Ru-based compounds viz. Ru_2NbGa [25], Ru_2TaAl [26], and $\text{Ru}_2\text{VGa}_{1-x}\text{Al}_x$ [77]. In Ru_2NbAl , the conduction and valence bands are found to

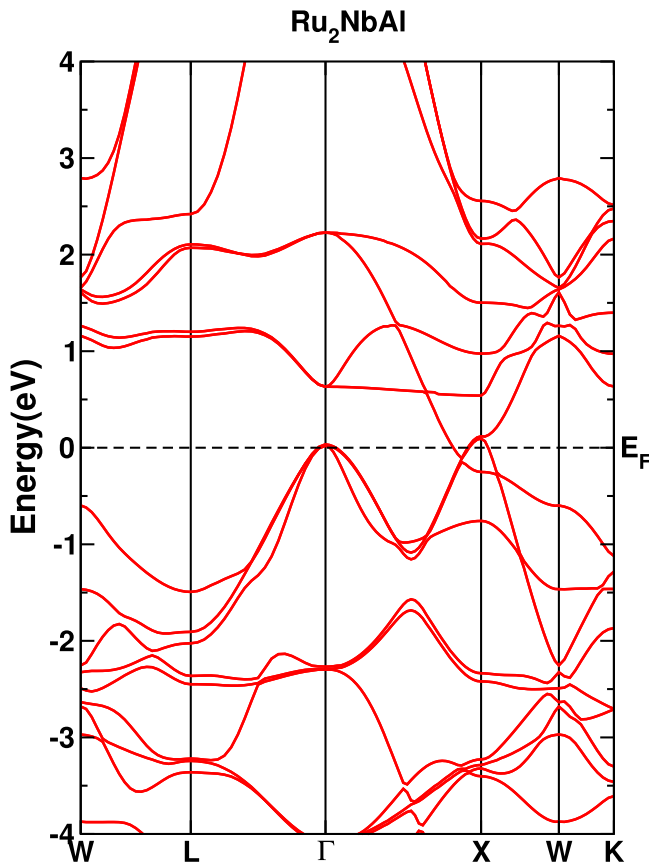


FIG. 11. Calculated band structure using TB-mBJ functional.

touch around the X point, and preserve a gap in all other points in the Brillouin zone. Figure 12(a) shows the density of states (DOS) of the investigated compound, together with the partial density of states. Highly competing Ru and Nb “ d ” states are found near the Fermi level, as shown in Fig. 12(a). A total of four bands are crossing the Fermi level, and among these bands three are found to be of holelike nature and the other one is found to possess electronlike nature. One may note here that our Seebeck coefficient measurements have also suggested that the majority charge carriers are holes. The merged Fermi surface plot of the investigated compound is represented in Fig. 12(b). As mentioned before, there are pockets in the Fermi surface around Γ and X points. The density of states variations above and below the Fermi level are almost similar, indicating the possibility of both hole and electron carriers for thermoelectric applications, which certainly attracts device applications, but it is to be mentioned that the DOS is steeply rising for hole carriers and we base our discussion only on holes in this work.

The mechanical properties are examined, and the calculated parameters are listed in Table II. The high value of bulk modulus indicates the stiffness of the compound. The calculated Debye temperature is found to be little higher than the experimental value.

Thermoelectric coefficients like the Seebeck coefficient, electrical conductivity scaled by relaxation time, and power factor are calculated by combining the semiclassical Boltzmann transport equation with density functional theory. The

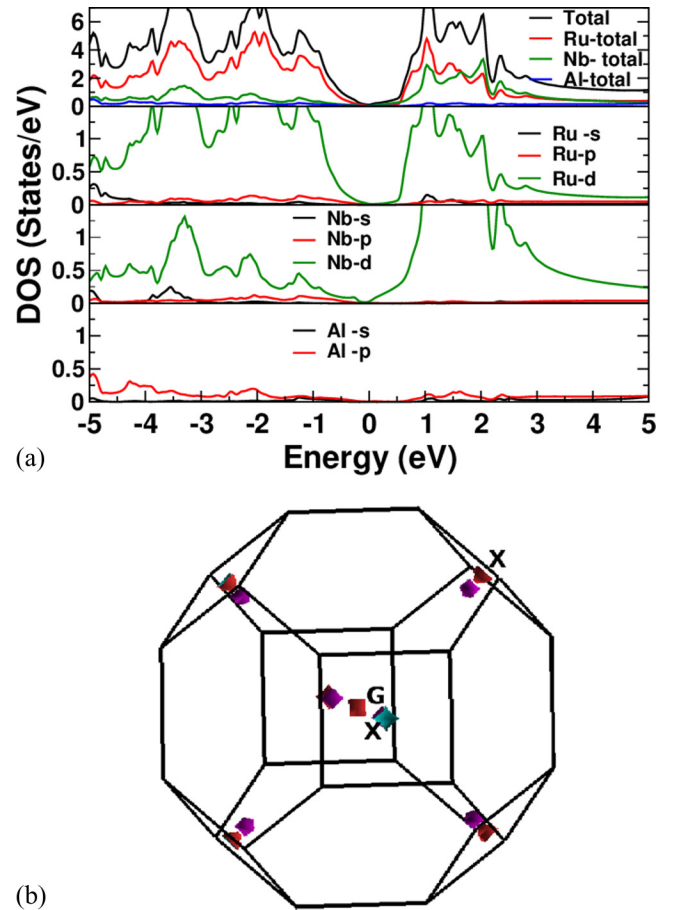


FIG. 12. Calculated (a) density of states (b) merged Fermi surface.

calculated Seebeck coefficient as a function of holes and electrons is given in Figs. 13(a) and 13(b). For both holes and electrons, carrier concentrations around $5 \times 10^{19} \text{ cm}^{-3}$ secure the maximum value of Seebeck coefficient. The temperature dependent Seebeck coefficient for a hole concentration around $1 \times 10^{18} \text{ cm}^{-3}$ is represented in Fig. 14. The trend is in agreement with the experiment. In addition, we have deduced the electrical conductivity scaled by relaxation time, and its carrier concentration dependence is also represented in Figs. 13(c) and 13(d). Using the calculated Seebeck coefficient and electrical conductivity scaled by relaxation time, we have analyzed the power-factor value. The experimental resistivity value has been adapted to find the conductivity value, and we have decoupled the relaxation time. The estimated relaxation time turned out to be around $1 \times 10^{-14} \text{ s}$. The calculated figure of merit around 300 K is 4.29×10^{-3} , which is in good agreement with the experimental value.

TABLE II. Calculated mechanical properties.

C_{11} (GPa)	405.86
C_{12} (GPa)	152.81
C_{44} (GPa)	96.84
Bulk modulus (GPa)	237.40
Debye temperature (K)	535.917

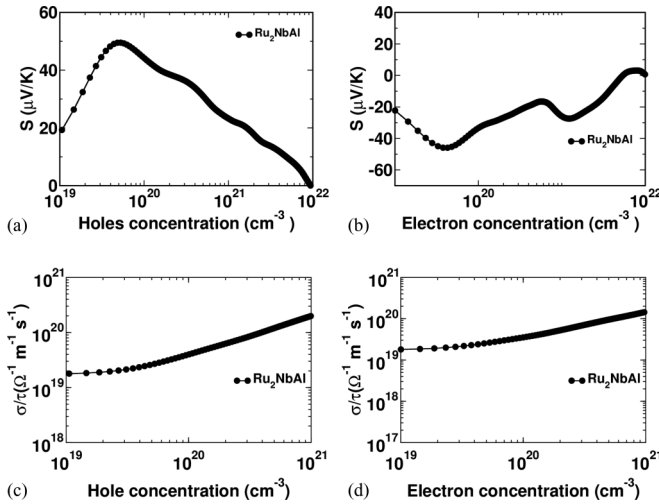


FIG. 13. Variation of Seebeck coefficient [(a) and (b)] and electrical conductivity [(c) and (d)] as a function of hole and electron concentrations.

IV. CONCLUSION

The magnetic properties of Ru_2NbAl are dominated by intrinsic Pauli paramagnetism and superparamagnetism of magnetic defects below ~ 20 K. These magnetic defects as well as the conduction electrons ($\gamma = 2.7 \text{ mJ mol}^{-1} \text{ K}^{-2}$) are found to have discernible contribution to the specific heat at low temperature. The Seebeck coefficient displays moderate positive values and linearly increases with temperature. All these experimental results suggest a semimetallic ground state for Ru_2NbAl , in agreement with the DFT calculations.

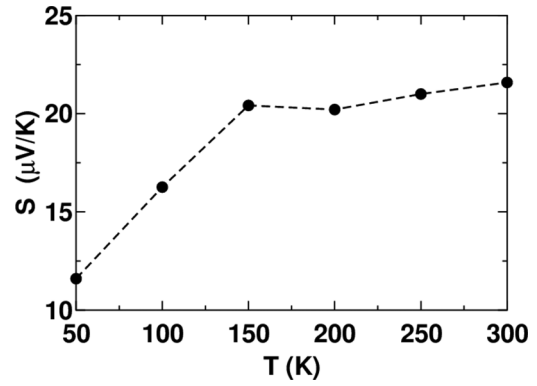


FIG. 14. Calculated temperature dependent Seebeck coefficient value.

In this context, the activated behavior of the electrical resistivity would thus arise from charge carrier localization due to structural antisite defects, detected by both magnetic measurements and EPMA. Ru_2NbAl displays a thermal conductivity smaller than that found in other full Heusler alloys and could, after suitable doping, display a larger thermoelectric figure of merit.

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