MIXED HYBRID AND ELECTRIC BUS DYNAMIC FLEET MANAGEMENT IN URBAN **NETWORKS: A MODEL PREDICTIVE CONTROL APPROACH** Marco Rinaldi, Ph.D.* Post-doctoral researcher Faculty of Science, Technology and Communication, University of Luxembourg, 6 Av. de la Fonte, L-4364, Esch-Sur-Alzette, Luxembourg Email: marco.rinaldi@uni.lu Erika Picarelli M.Sc. Student Department of Engineering Roma Tre University, Italy Email: eri.picarelli@stud.uniroma3.it **Georgios Laskaris** Ph.D. Candidate Faculty of Science, Technology and Communication, University of Luxembourg, 6 Av. de la Fonte, L-4364, Esch-Sur-Alzette, Luxembourg Email: georgios.laskaris@uni.lu Francesco Viti, Ph.D. Associate Professor Faculty of Science, Technology and Communication, University of Luxembourg, 6 Av. de la Fonte, L-4364, Esch-Sur-Alzette, Luxembourg Email: francesco.viti@uni.lu * Corresponding author Word count: 5817 words text + 2 tables x 250 words (each) = 6317 words Submission Date 15/11/2018

ABSTRACT

1 2

3 Reducing pollutant emissions and promoting sustainable mobility solutions, including Public Transport, are 4 increasingly becoming key objectives for policymakers worldwide. In order to jointly achieve these goals, 5 careful consideration should be put on the operational cost and management of PT services, in order to 6 promote the adoption of green mobility solutions and advanced management techniques by operators. In 7 this work we develop a dynamic fleet management approach for next generation Public Transportation 8 systems, considering the instance of mixed electric / hybrid fleet. Our objective is that of investigating to 9 what extent electrification, coupled with optimal fleet management, can yield operational cost savings for 10 PT operators, explicitly considering real-time disturbances, including delays, service disruptions etc. We 11 propose a Mixed Integer Linear Program to address the problem of optimal scheduling of a mixed fleet of 12 electric and hybrid / non-electric buses, and employ it as predictor in a Model Predictive Control approach. 13 Test results based upon a real-life scenario showcase how the proposed approach is indeed capable of 14 yielding a sizable reduction in operational costs, even when considerable disturbances arise from the 15 underlying system.

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18 Keywords: Dynamic bus fleet management, e-bus charging scheduling, MILP, MPC

INTRODUCTION

3 The last four decades have witnessed the rapid and widespread adoption of private transport, due to 4 significant advancements in technology. While yielding considerable gains at the individual level, this has 5 resulted in negative externalities, both in terms of network inefficiencies (ever-increasing congestion 6 causing delays, productivity loss, ...) and in terms of pollutant emissions. To counteract these effects, 7 developing advanced solutions for sustainable urban Public Transport (PT) is becoming of paramount 8 importance for policymakers, practitioners and researchers worldwide. In order to become an attractive 9 alternative to the comfort and flexibility offered by private transport solutions, next generation PT services 10 must however meet very demanding criteria both in terms of service performance and quality (minimal 11 delays, high frequency, high resilience, ...). Next to these ambitious performance goals, researchers and 12 practitioners are also actively investigating whether the adoption of greener vehicles (hybrid electric and/or 13 full electric buses) can vield both reduced pollutant emissions and operational costs, representing therefore 14 a win-win situation for both policymakers and PT operators.

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Adopting fully electric vehicles isn't however straightforward from the tactical/operational perspective: e-16 17 buses exhibit shorter driving ranges compared to hybrid and conventional combustion alternatives, 18 requiring within-day recharging operations, which poses extra constraints to the state-of-the-art problem of 19 transit scheduling (1). Solutions to this problem must be developed with care, as a clear trade-off exists 20 between exploiting the available full-electric fleet to serve scheduled trips at a reduced operational cost 21 (compared to either internal combustion or hybrid buses), and the cost of recharging operations. Indeed, 22 while recent technological advancements have substantially reduced the time required to fully recharge an 23 e-bus battery, this comes at a considerable cost in terms of energy prices, due to the required peak current.

24

In the Luxembourgish national context, recent policies adopted by the government are supporting the capital's main PT operators towards widespread electrification (2). By the end of 2018, all buses operated by Autobus Ville de Luxembourg are indeed expected to be plug-in hybrid electric. Furthermore, a small number of opportunity charging stations has been equipped in selected terminals around the city, to encourage further adoption of full electric vehicles in the coming ten-year period. In collaboration with the main national stakeholders, the University of Luxembourg is investigating the conditions under which this shift can be optimal, both from the strategic and tactical/operational perspective.

32

In this paper we develop models and algorithms to support this paradigm shift, specifically addressing two research questions which we believe of both theoretical and practical relevance:

- 1) The problem of optimal scheduling and dispatching of a *mixed* fleet of electric and plug-in hybrid vehicles, bearing different recharging requirements, has received little attention in literature;
- 36 37 38
- 2) In high frequency services operating in congestion-sensitive networks, operational disturbances such as delays, bunching etc. might arise; Model-based dynamic fleet management approaches might be useful to reduce loss of performance without resorting to deadheading.
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43 In what follows we propose a mixed-integer linear programming formulation of the single-depot vehicle 44 scheduling problem (SDVSP), which explicitly considers the additional constraints deriving from the inclusion of electric vehicles and their discharging/recharging dynamics. This formulation, based upon our 45 46 recent work (3), is accompanied by a time-window decomposition solution scheme, which allows both to 47 i) tackle large scale problems at a minor loss in optimality and ii) employ the model as predictor in a Model 48 Predictive Control framework. By basing ourselves upon the real-life scenario of Luxembourg City, we 49 showcase both how relevant appropriate modelling is when computing an offline daily plan for the 50 dispatching of a mixed plug-in hybrid and electric fleet, and, most importantly, how robust the proposed model is when employed in real-time fleet management applications. 51

The rest of the paper is organized as follows. The next section provides a literature review of fleet management operations, highlighting both the existing works dealing with electrification and those focusing on operational research driven approaches to solve the dispatching problem optimally. Later we discuss the methodological contribution of this paper, focusing on the proposed model and its solution schemes, both for offline and online purposes. Experimental results will be presented next, evaluating and comparing how different dispatching techniques perform in terms of operational costs, both in offline and online instances. Finally, some conclusions and pointers for future research are drawn.

8 9

LITERATURE REVIEW

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Vehicle scheduling problems in the context of public transportation have been studied extensively as part of the "full operational planning process", as defined in (4). From a mathematical / operations research perspective, this problem is known as the Single/Multi-Depot Vehicle Scheduling Problem (SDVSP/ MDVSP), for which several algorithms, both exact and heuristic in nature, have been developed (5). Indeed, exhaustive literature reviews concerning different algorithmic approaches for these problems can be found (6,7).

17

18 Concerning the expected benefits of PT electrification in the urban context, works such as (8-11) have 19 investigated the problem both from a technological perspective and from an economic standpoint, 20 highlighting the benefits of different categories of hybrid-electric and full-electric buses. Few works have 21 so far dealt with extending or reformulating the SDVSP or the MDVSP with explicit consideration of the 22 additional needs stemming from the inclusion of charging/recharging constraints, either from the modelling 23 perspective (12) or from the algorithmic solution development perspective (13-15). These approaches 24 showcase how proper fleet management, under the assumption of homogeneous electric fleet, vields 25 reduced operational costs for the PT operator while, at the same time, reducing overall pollutant emissions.

26

Most recently, in (16), the authors discuss in details the implications of introducing electrification in the operational planning process for transit systems. Among others, they propose an extension to the MDVSP to consider a homogeneous fleet of electric vehicles operating in a network with multiple charging points, which guarantees that all trips from/to different depots in the network pass through a sufficient amount of

charging points, where e-buses will be fully charged. In a different model they also consider a fleet requiring
 overnight charging only.

33

To the authors' knowledge, explicitly modelling PT operations consisting of a *mixed* fleet of full-electric buses - requiring within-day charging at a capacitated infrastructure - and either conventional or plug-in hybrid buses - for which instead no operational charging constraint is present - has so far been neglected.

hybrid buses - for which instead no operational charging constraint is present - has so far been neglected. We believe this to be a considerable can in literature; the shift from internal combustion floats towards

37 We believe this to be a considerable gap in literature: the shift from internal combustion fleets towards 38 more sustainable alternatives will certainly be gradual in nature, and ontimal management in mixed fleet

38 more sustainable alternatives will certainly be gradual in nature, and optimal management in mixed fleet 39 conditions might yield considerable reductions in operational costs, whereas a less-than-careful approach -

40 as will be shown later in the results section - could be detrimental to the operator's performance.

41

42 When considering online responsiveness to disturbances such as delays, bunching etc., dynamic fleet 43 management approaches in literature focus on optimally allocating deadheading trips (17,18), in order to 44 achieve better reliability. Real-time reaction / prediction in terms of scheduling is however virtually unheard 45 of, at least in transit literature, and has been recognized as a very challenging problem in fields such as city 46 logistics (19).

47

48 In the private transport literature, rejection of real-time disturbances is often achieved by means of Model

49 Predictive Control (MPC) (20–23). Employing predictive modelling allows, in principle, to optimally

50 redistribute the available fleet in real-time, without resorting to deadheading additional rolling stock from

other terminals or depots. In this work, we will assess whether such a framework can be successfully applied

52 to the instance of dynamic fleet management for transit operations.

METHODOLOGY

We begin this section by quickly introducing the main idea behind Model Predictive Control, motivating this framework's choice for dynamic mixed fleet management, and framing the contribution within our chosen case study. We then introduce the developed prediction model, together with the assumptions and modifications required to solve it efficiently, and finally introduce the underlying bus simulation approach, which we employ as "plant model", to represent reality.

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Model Predictive Control for dynamic fleet management

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11 MPC has been successfully employed as a control technique for non-linear systems for the last two decades, 12 ranging in applications from early industrial processes (chemical plants, manufacturing) to vehicular technology and transportation. The rationale behind this success is that the MPC framework (24) allows to 13 14 apply standard optimisation techniques based upon a white-box prediction model in order to determine the 15 best possible control action, while at the same time retaining the desirable properties of feedback control, in terms of real-time responsiveness and rejection of disturbances. The standard MPC framework, 16 17 summarised in Figure 1, entails three main components: a prediction model, which is a sufficiently faithful 18 representation of reality, an optimisation approach, which minimises a chosen objective function leveraging

- 19 the model itself and, finally, a connection to the system being controlled, in terms of sensing/actuation.
- 20



21 Figure 1: MPC framework description, between parenthesis specific components considered in this work

22

In the standard Rolling Horizon (RH) approach, the MPC controller operates by, at each time step t, optimizing its control decisions subject to the predictions obtained for a certain future duration of time (the prediction horizon, N_p), applying the control decision for the current time t and moving forward to the next time step, where the process is repeated. Depending on the goodness of the chosen prediction model, the length of the prediction horizon and the non-linearity of the underlying phenomenon, the MPC approach might result more or less computationally intensive and more or less successful in controlling the given system.

31 In this work, we employ as prediction model a Mixed-Integer Linear Programming formulation of the

vehicle scheduling problem for the specific instance of electric vehicles, subdivided in time windows in order to correctly represent the Rolling Horizon approach. The chosen optimization approach is the branch-

- 3 and-cut approach of IBM's ILOG CPLEX, version 12.7.
- 4
- 5 <u>The Single Depot Electric Vehicle Scheduling Problem with Time Decomposition (SDEVSP-TD)</u> 6
- 7 We formulate the problem of scheduling a mixed fleet of electric (e-) and hybrid (h-) buses $I = \{1, ..., i\}$
- 8 following a set of scheduled trips $J = \{1, ..., j\}$, each comprising a desired departure time $D_j = \{1, ..., d_j\}$
- 9 [min], cycle (terminal 1 to terminal 1) duration $T_j = \{1, ..., t_j\}$ [min] and total energy required $U_j = \{1, ..., u_j\}$
- 10 [kWh]. For each trip, decision variables $y_{i,j}^t$ and $z_{i,j}^t$ describe respectively whether trip j is initiated at time
- 11 period t by electric or hybrid bus i. In order to both allow solving large scale scenarios and correctly
- 12 represent MPC's Rolling Horizon, we introduce a time window decomposition, so that the full time scale
- 13 of the problem $T = \{1, ..., t\}$ is decomposed in $L_f = \{l_1, ..., l_f\}$ time windows, each bearing its own (possibly

14 heterogeneous) duration. The optimization problem is solved separately and sequentially for each time

15 window, with specific constraints ensuring that correct information flows between the separate problems.

16 This decomposition scheme does however impact optimality: since time lapses are limited in length in order

- 17 to keep memory requirements at bay, each independent MILP is solved with no knowledge on future trips,
- 18 whose departures lay beyond the duration of the individual decomposed problem. This implies that
- 19 decisions taken in time lapse f, especially those related to trips departing in its latter time steps, might be
- 20 sub-optimal from the perspective of the full problem's timetable.
- Table 1 introduces the full problem variables' meaning as well as their domain.
- 22

23 Table 1: Problem variables and parameters and their explanation

Var.	Domain	Explanation		
${y}_{\scriptscriptstyle i,j}^t$	$\{0,1\}$	1 if trip j is initiated by e-bus i at time t , 0 otherwise		
$z_{i,j}^t$	$\{0,1\}$	1 if trip j is initiated by h-bus i at time t , 0 otherwise		
$\gamma_{\scriptscriptstyle i,j}^t$	$\{0,1\}$	1 if e-bus <i>i</i> has sufficient energy ε_i^t to perform trip <i>j</i> at time <i>t</i> , 0 otherwise		
$x_{\scriptscriptstyle i,m}^t$	$\{0,1\}$	1 if e-bus i is being recharged at charging station m at time t , 0 otherwise		
ε_i^t	$\leq E, \in \Re^+$	Total energy in kWh that e-bus <i>i</i> has at time <i>t</i>		
$u_{_j}$	\Re^+	Total energy in kWh required to perform trip <i>j</i>		
$d_{_j}$	\Re^+	Preferred departure time for trip <i>j</i>		
t_{j}	\Re^+	Duration of trip <i>j</i> in time steps		
s_i^t	\Re^+	+ Slack variable, necessary to ensure that constraint (11) does not violate the domain of ε_i^t		
E	\Re^+	Total battery capacity in kWh for all electric buses		
A_i^t	$\{0,1\}$	1 if e-bus i is not available to perform any trip of the current window problem at time t , 0 otherwise		
H_i^t	$\{0,1\}$	1 if h-bus <i>i</i> is not available to perform any trip of the current window problem at time <i>t</i> , 0 otherwise		

25 The formulation's objective function, in Eqn. (1), is that of minimizing the total operational cost.

$$\min \sum_{t} \sum_{i} \sum_{j} y_{i,j}^{t} \cdot c + r \cdot (t - d_{j}) + \sum_{t} \sum_{i} \sum_{j} z_{i,j}^{t} \cdot \hat{c} + r \cdot (t - d_{j}) + \sum_{m} \sum_{i} \sum_{t} q_{i}^{t} \cdot x_{i,m}^{t} - \chi \cdot \sum_{t} \sum_{i} \varepsilon_{i}^{t}$$

$$(1)$$

- Cost vectors c and \hat{c} are computed as shown in Eqn. (2), considering average cost rates per kWh of energy components η_1 and η_2 for e-buses and h-buses respectively.
- 4 $c = \eta_1 \cdot [u_j]$ $\hat{c} = \eta_2 \cdot [u_j]$ (2)
- A penalty term r [EUR] is applied to trips being performed later than their preferred departure time, in order to evaluate trade-offs between schedule adherence and operational performance. We consider M = {1,...,m} charging stations available at the selected bus terminal, and explicitly take into account the time dependent cost q^t_i of recharging bus *i* at time *t* as part of the operational cost needing minimization.
 System dynamics are captured by constraints (3-19). The last summation term of Eqn. (1), with χ chosen appropriately small, is necessary to complement the slack variables introduced in constraint (11).

11
$$\sum_{j} y_{i,j}^{t} \leq 1 - A_{i}^{t} \quad \forall i,t$$
 (3)

12
$$\sum_{j} z_{i,j}^{t} \leq 1 - H_{i}^{t} \,\forall i,t \tag{4}$$

13
$$\sum_{t \ge d_j} \sum_{i} y_{i,j}^t + z_{i,j}^t = 1 \quad \forall j$$
 (5)

14
$$\sum_{i} x_{i,m}^{t} \le 1 \ \forall m, t \tag{6}$$

15
$$\sum_{m} \sum_{\overline{t} > t} x_{i,m}^{\overline{t}} \ge 1 - \sum_{j} \gamma_{i,j}^{t} \quad \forall i,t$$
 (7)

16
$$y_{i,j}^t - \gamma_{i,j}^t \le 0 \ \forall i, j, t$$
(8)

17
$$\frac{\varepsilon_i^t}{u_j} - \gamma_{i,j}^t \ge 0 \ \forall i, j, t$$
 (9)

18
$$\frac{\varepsilon_i^t}{u_j} - E \cdot \gamma_{i,j}^t < 1 \ \forall i, j, t$$
 (10)

19
$$E \cdot \sum_{m} x_{i,m}^{t} - \sum_{j} y_{i,j}^{t} \cdot u_{j} + \varepsilon_{i}^{t} - s_{i}^{t} = \varepsilon_{i}^{t+1} \quad \forall i, t$$
(11)

20
$$\begin{cases} \varepsilon_{i,0}^{0} = E \ \forall i \\ \varepsilon_{i,f}^{0} = \varepsilon_{i,f-1}^{l_{(f-1)}} \forall i, f \end{cases}$$
(12)

21
$$\sum_{j} y_{i,j}^{t} + \frac{s_{i}^{t}}{E} \le 1 \quad \forall i,t$$
 (13)

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$$\frac{1}{E} \cdot s_i^t - \frac{1}{E} \varepsilon_i^t \le 0 \ \forall i, t$$
(14)

$$y_{i,j}^t + \sum_m x_{i,m}^t \le 1 - A_i^t \,\forall i, j, t \tag{15}$$

3
$$y_{i,j}^{t} + k_{1} \sum_{\bar{t}=t+1}^{t+t_{j}-1} \sum_{\bar{j}} y_{i,\bar{j}}^{\bar{t}} \le 1 \ \forall i,t \ \forall j:t_{j} > 1$$
(1)

4
$$k_1 = \frac{1}{t_j - 1}$$
 (17)

$$y_{i,j}^{t} + k_{2} \sum_{\bar{i}=t+1}^{t+j-1} \sum_{m} x_{i,m}^{\bar{t}} \le 1 \ \forall i, t \ \forall j: t_{j} > 1$$
(18)

6)

Constraints (3-4) ensure that no bus (electric or hybrid) can perform more than one trip at a time. Constraint
(5) guarantees that all trips must (eventually) be performed by either kind of bus, that trips are not performed
more than once, and that trips cannot be performed before their respective preferred departure time.

10 Constraint (6) implies that an e-bus can be charged at only one charging station at any given time, and,

11 implicitly through the set *M*, that the maximum amount of concurrent recharging buses is limited by the

12 total charging stations available. Constraint (7) ensures that, if an e-bus has no charge left to perform any

13 trip, it will be recharged at a future time. Constraint (8) guarantees that an e-bus will not perform a trip

unless it has sufficient energy to do so. Constraints (9-10) describe the characteristics of variable $\gamma_{i,i}^t$ in

15 relation to the current available bus energy ε_i^t and the required energy to perform trip u_j . Constraint (11)

16 captures the discharging/recharging dynamics: if an electric bus is performing a trip *j* at time *t*, its available

17 charge at time t+1 will be reduced by u_i . Conversely, if the electric bus is being recharged at time t, its

18 available charge at time t+1 will be equal to the total battery capacity E. The slack variables s_i^t absorb any

19 leftover energy ε_i^t , in order to guarantee that the maximum battery capacity is not violated. Constraint (12)

20 implies that all e-buses begin operations fully charged at the beginning of the simulations, and that between

21 contiguous time windows f, f+1 the amount of available energy is conserved for each bus. Constraints (13-

14) ensure that slack variables can only be utilized during recharging operations. Constraint (15) ensures

that an e-bus cannot be recharging and operating simultaneously. Constraints (16-19) ensure that an e-bus

24 performing a trip *j* whose duration in time steps is greater than one cannot be used to perform any other trip

25 nor recharged until trip j has been completed.

Finally, cross-problem coupling equations (20-23) ensure that the availability of buses whose trips' duration

- exceeds the length of the current time window f is safeguarded and correctly represented in time window f+1. These values are computed once the problem of time window f has been solved, and produce inputs
- for the problem of time window f+1.

$$A_{i}^{t}\Big|_{f} = A_{i}^{t+l_{(f-1)}}\Big|_{f-1} + \lambda_{i}^{t}\Big|_{f-1} \forall i, f, t$$
(20)

$$H_{i}^{t}\Big|_{f} = H_{i}^{t+l_{(f-1)}}\Big|_{f-1} + \zeta_{i}^{t}\Big|_{f} \,\forall i, f, t$$
(21)

32
$$\lambda_{i}^{t}\Big|_{f} = \begin{cases} 1 \quad \forall i, t : \exists j, \overline{t} : y_{i,j}^{\overline{t}}\Big|_{f} = 1 \land \left(l_{f} < t \leq \overline{t} + t_{j}\right) \\ 0 \quad otherwise \end{cases}$$
(22)

$$\zeta_{i}^{t}\Big|_{f} = \begin{cases} 1 \quad \forall i, t : \exists j, \overline{t} : z_{i, j}^{\overline{t}}\Big|_{f} = 1 \land \left(l_{f} < t \le \overline{t} + t_{j}\right) \\ 0 \quad otherwise \end{cases}$$
(23)

2 <u>MATLAB Bus Corridor Simulation software</u>

3

4 The proposed prediction model is linked to a bus simulation model that mimics all the characteristics of 5 real time operation and replicates the different phenomena that may occur at a mesoscopic level. The bus 6 simulation model is coded using Mathworks[™] MATLAB[®]. The inputs of the model are the number of 7 stops with the corresponding demand, per each line, the number of trips and the scheduled riding times 8 between stops. Passenger demand is based on historical data and it is given as input in terms of arrival rates 9 per hour per OD pair. The sources of stochasticity of the model are the dispatching times, the travel times 10 and, consequently, passenger demand. The variability of all three during simulation is modelled by sampling from the probability distribution that best fits with the nature of each variable. By setting the parameters of 11 each distribution, the simulator can be tuned appropriately. Analytically, dispatching times are sampled by 12 13 Gamma distribution. It is worth mentioning that, for the purposes of this study, only the dispatching times 14 of the trips of the first hour are sampled (based also on the fleet size chosen). For the remainder of the 15 simulation, the dispatching times for the remaining trips are obtained as coupling input from the SDEVSP-TD prediction model. An e-bus or h-bus is assigned based on the availability and the cost. Actual riding 16 times are sampled by lognormal distribution, using as average the scheduled riding time and a 20% standard 17 18 deviation for the shape and the scale of the distribution. The number of boarding passengers at stops follow 19 Poisson distribution, given the arrival rate and the actual headway at each stop. Since the simulation is 20 stochastic, several replications are conducted with different random seeds.

21

22 During simulation, each trip initiates at its dispatching time, which coincides with the arrival at the first 23 stop of the route. For the rest of the stops, the arrival time of the bus is calculated as the sum of the departure 24 time of the vehicle from the previous trip and the actual riding time, as sampled. The difference between 25 the last registered arrival time and the arrival time of the current trip constitutes the actual headway. This is 26 then employed together with the arrival rate at the stop to calculate the number of passengers generated at 27 each stop. The number of boarding passengers is the sum of all passengers originated at the current stop. 28 travelling downstream. The alighting passengers are the passengers on board that were generated upstream 29 and had as destination the current stop. Once the occupancy of the bus is updated, dwell time is calculated 30 as the sum of the products of the boarding and alighting passengers with the corresponding rates as retrieved 31 by (25). After the completion of dwell time, the trip departs from the stop. To appropriately consider the 32 full travel time of each trip as it returns to the terminal from where it was dispatched (in this work we 33 consider circular terminal 1 - terminal 2 - terminal 1 trips), one intermediate stop works as the terminal of 34 the one-way route. At that stop, all remaining passengers are instructed to alight and the trip departs from 35 stop after a predefined time corresponding to its scheduled arrival.

36

After the completion of each replication, results are generated for the full trajectory of each trip, togetherwith travel and passenger related performance measurements.

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40 **EXPERIMENTAL RESULTS**

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In this section we first describe the experimental setup, focusing on the chosen case study in the city of Luxembourg. We then showcase two sets of test results: a first set of tests evaluates the impact of additional e-buses in terms of fleet size on two different dynamic management techniques (our proposed model and a simpler Just-In-Time approach), assuming exact information and no disturbances. The second set of tests focuses instead on assessing whether the proposed model is indeed robust when employed as predictor in

an MPC framework.

- 48
- 49 <u>Experimental setup</u>

As discussed earlier, we consider a real-life case study arising from Luxembourg City, specifically comprising of five urban bus lines, all radiating from the city's central station (Gare Centrale), as highlighted in Figure 2.



Figure 2: Schematic of Luxembourg City's public transport lines, case study shown in coloring.

7 Lines 9 and 14 are already being served exclusively through plug-in hybrid buses, with others soon to follow, and two opportunity charging stations have been equipped in the terminal area of Gare Centrale. Starting 8 9 from this ideal testing ground, we investigate the effect of introducing a mixed fleet including fully electric 10 buses, which will exert a stronger demand on the two charging stations. This allows us to both evaluate whether the existing infrastructure would be sufficient, and to assess the overall impact of electrification in 11 12 terms of operational costs. We focus on the weekly morning schedule, which consists of 119 trips for these five lines, from 5am until 1pm, extracted from the openly available GTFS dataset provided within the 13 14 nation's online data portal (26). The lines operate at an average frequency of about 15 minutes, although 15 some irregularities do arise both within-line and between lines, as shown in Figure 3 (trips have been colored following the same scheme as the schematic in Figure 2). Due to these irregularities, computing the 16 17 optimal fleet scheduling is considerably challenging. Following our model's formulation, we discretise time 18 considering intervals of 5 minutes.

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Figure 3: Complete schedule for the five lines considered

2 In order to faithfully represent reality, we collected average consumption rates for both h-buses and e-buses 3 based both on available literature (10) and on technical sheets provided by Volvo Bus corporation, which supplies the current generation of h-buses to the city of Luxembourg. Specifically, we consider a 4 5 consumption rate of 1.7 kWh/km for e-buses and 2.3 kWh/km for h-buses (including the internal 6 combustion powertrain). In order to monetise these values, we consider for both a generalised cost of 0.277 EUR/kWh, which includes, on top of the cost of electricity itself, an estimation of all costs concerning 8 operational aspects of buses, such as maintenance etc. We assume battery capacity for e-buses to be set at 9 100kWh, and we apply the current national average price of electricity of 0.15 EUR/kWh when considering 10 recharging. Even though this assumption is rather conservative compared to peak pricing policies, we will show in what follows that recharging already plays a dominant role in the proposed scenario, and that fleet 11 management should be performed accordingly. For the first set of tests, the possibility of dispatching a trip 12 13 at a departure time later than the planned value is excluded entirely $(r = \infty)$, whereas a value of r = 514 EUR is selected for the second, online scenario.

16 Case Study 1: Fleet size and operational costs

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In this first case study we evaluate the impact of gradually expanding the fleet size allocated to the five lines above, by adding extra e-buses to an otherwise *large enough* set of h-buses (we suppose availability of h-buses not to be an issue to the feasibility of the problem at hand, in order to isolate the impact of ebuses). We compare the full operational cost in terms of the objective function value (Eqns. 1-2), across three different fleet management techniques: our proposed model (Eqns. 3-19), a Just-In-Time approach and a reference solution obtained employing solely hybrid buses.

24

We consider a naïve Just-In-Time implementation, which attempts to maximise utilisation of the cheaperto-run electric fleet, disregarding the wider impact that such a policy might have on the overall operational costs in terms of recharging, which instead is used speculatively whenever any e-bus exhibits a charge lower than what is necessary.

3 The Just-In-Time approach operates according to the following simple rules:

- 4 at a given time instant *t*: if any e-bus *i* is available and has sufficient charge to perform any trip 5 $u_i: d_i = t$, bus *i* is assigned to trip *j*. Otherwise, an h-bus will be used.
- 6 at a given time instant *t*: if any e-bus *i* is available but does not have sufficient charge to perform any 7 trip $u_i: d_i = t$, it is recharged, as long as at least one charging station is available.

For each trip, a scheduling decision is taken by either model in terms of which bus (electric/hybrid) is going
to be used to serve it, ensuring that all availability constraints are satisfied.

10

1

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11 The results of this first case study are presented in Figure 4.

12





Figure 4: Variation of operational cost with respect to total e-bus fleet size.

14 Our proposed model performs very well, progressively reducing operational costs as the available e-bus 15 fleet size increases, as is expectable, and reaching substantial savings (ranging from 10% to over 20% reduction in total operational cost) when the e-bus fleet size exceeds 14 buses. The naïve just-in-time 16 approach however only achieves smaller operational gains for larger fleet sizes, due to its recharging policy, 17 18 and is instead worsening overall costs compared to utilising all hybrid buses for fleets ranging between 12 19 and 14. These results hint at the fact that, indeed, in mixed fleet conditions a myopic approach that tries to 20 maximise the usage of the cheaper running cost alternative is far from ideal, and that instead greater care 21 must be taken in scheduling charging operations. 22

23 Case Study 2: dynamic fleet management

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Having verified that our model captures the desired dynamics to a satisfactory level, and that it is indeed capable of yielding substantial gains in terms of objective function under ideal conditions, in this second set of tests we investigate whether it can be used in operational conditions, where disturbances such as
 delays and bunching arise due to variability in demand.

4 We utilise our proposed model as predictor in an MPC framework, as discussed earlier: at each time step *t*,

5 the approach predicts $N_p = 30$ minutes into the future, assuming that both dispatching times and trip

6 durations are exactly aligned to the schedule of Figure 3. Once the model reaches optimality, the scheduling

- 7 decisions for time step *t* are implemented, both in terms of dispatching time and type of bus utilised 8 (electric/hybrid), and the dispatching information is forwarded to the underlying plant model, which
- 9 performs the trip(s) accordingly. The exact amount of available rolling stock at time t is obtained in real-
- 10 time as a derived output from the previous time step's status of the plant model, in terms of trip arrivals.
- 11

Passenger demand is simulated along the five lines, in terms of stochastic arrivals, considering a uniform spatial distribution along the lines' stops, and three different levels of total demand (300 pax/h/line, 500 pax/h/line, 700 pax/h/line). As demand increases, the elongated boarding/alighting times cause delays at the line level, with longer lines running the risk of bus bunching under high demand conditions. The actual complete trip durations become known to the prediction model only upon trip completions themselves, meaning that considerable mismatching can occur between the predicted completion times and the realised ones.

19

We simulate and compare three different fleet management techniques: our proposed model predictive controller, the previously mentioned just-in-time approach and an "oracle" version of our model, computed

22 ex-poste, where exact trip duration and dispatching time information are assumed known at all time steps,

23 providing therefore a "best case" comparison. These results are summarised in Table 2, in terms of percental

24 difference between the realised objective function value and that of an all-hybrid solution.

25

Table 2: Case Study 2 results. Percental variations compared to an all-hybrid operational cost of 957 EUR.

	Just-In-Time	MPC	Oracle
Demand: 300 pax/h/line	-1.76%	-3.38%	-12.71%
Demand: 500 pax/h/line	-0.2%	-8.99%	-11.84%
Demand: 700 pax/h/line	+1.45%	-8.49%	-12.77%

27

As expectable, the "oracle" model performs best in all scenarios, while the chosen just-in-time approach is 28 29 clearly unsuitable for the given problem. The online MPC approach shows promising results, especially 30 when its reference trip completion times are underestimations compared to the realised ones (that is, for 31 higher demand levels). Conversely, when trips are consistently completed earlier than what is anticipated, 32 the advantage obtained by using a complex prediction model is quickly eroded, reducing from -12.71% to 33 -3.38%. In the "plant" model we assumed that no regularising control (e.g. holding) is active, meaning that 34 in very undersaturated conditions trips can indeed be systematically completed ahead of schedule. In future 35 research we will assess the combined effect of both MPC-based dynamic fleet management and line-wise 36 or system-wise holding strategies. Over all scenarios, the average computational time necessary for CPLEX 37 to optimize the prediction instances of the SDEVSP-TD model was 11.2 seconds, with a standard deviation 38 of 2 seconds, well within the ideal requirements for real-time applicability.

39

40 CONCLUSIONS

41

In this paper we develop an approach for dynamic mixed electric/hybrid bus fleet management, leveraging a Model Predictive Control framework. After validating the prediction model's capabilities in terms of

44 minimising operational costs in a real-life case study, we assess its online performances considering

45 stochastic trip completion times as arising from a mesoscopic bus simulator approach. All tests conducted

46 are based upon a real-life case study situated in the city of Luxembourg. Test results show that, indeed, the

proposed model is suitable for a dynamic fleet management application based upon model predictive control, retaining a very solid level of performance even when facing considerable disturbances and delays. Future research includes, first and foremost, the extension of the obtained results to a multi-depot scenario, in order to consider larger instances and case studies. Further investigation will also be performed in evaluating the relationship between charging station location / density and peak electricity pricing by grid operators, framing the latter's dynamic pricing schemes in game theoretical terms and focussing on establishing whether a gain can be found by switching from competition to cooperation.

8 9

AUTHOR CONTRIBUTION STATEMENT

10

The authors confirm contribution to the paper as follows: study conception and design: M. Rinaldi; model(s)
 formulation and implementation: E. Picarelli, M. Rinaldi, G. Laskaris; analysis and interpretation of results:
 M. Rinaldi, E. Picarelli. F. Viti; draft manuscript preparation: M. Rinaldi. G. Laskaris, F. Viti. All authors

14 reviewed the results and approved the final version of the manuscript.

15

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17

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