

# On the Universality of Hawking Radiation

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## Abstract

A physically consistent semi-classical treatment of black holes requires universality arguments to screen late-time Hawking radiation from ultra-short distance near-horizon effects. We evaluate three families of such arguments in comparison with Wilsonian renormalization group universality arguments found in the context of condensed matter physics. Particular emphasis is placed on the quality whereby the various arguments are underpinned by ‘integrated’ notions of robustness and universality. Whereas the principal strength of Wilsonian universality arguments can be understood in terms of the presence of such integration, the principal weakness of all three universality arguments for Hawking radiation is its absence.

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*Universality*. . . is the slightly  
pretentious way in which physicists  
denote identical behaviour in different  
systems.

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— M.V. Berry (1987, p.185)

## 1 Introduction

Back in ancient Miletus, the fashion amongst philosophers was to posit that everything was made of a single, primal substance (water, air, *apeiron*). For the Milesians, the manifold diversity of the phenomenal world was underpinned by a single type of stuff: macro-diversity despite micro-uniformity. These days, most philosophers are reluctant to endorse such a unitary reductionism. Some even insist that the relationship in question is, in some cases, the other way around: macro-uniformity despite micro-diversity. A scientific foundation to support instances of such a remarkable reversal has been firmly established in the study of phase transitions within condensed matter systems. From the nineteen-sixties onwards, revolutionary work by Wilson, Kadanoff and others provided physical arguments to understand the basis by which systems that are very different at a micro-level, like fluids and magnets, can display the same *universal phenomena* at a macro-level. Wilsonian-style universality arguments are based upon renormalization group techniques and are already the subject of a burgeoning philosophical literature.<sup>1</sup>

A very different area of physics where one also finds appeals to universality arguments is in the study of thermal properties of black holes. In this context also, arguments have been developed aimed at showing that systems that are very different at a micro-level can display the same phenomena at a macro-level. The particular issue that these arguments are invoked to resolve is related to Hawking's famous prediction that black holes produce thermal radiation (Hawking 1975). As was recognised soon after Hawking's original paper (Gibbons 1977), the derivation of Hawking radiation makes essential use of a breakdown in the separation between micro- and macro-scales. In particular, due to an exponential redshift, the Hawking radiation that is detected far away from the black hole, at relatively large wavelengths and late times, is sensitive to the near horizon physics at ultra-short wavelengths — even much smaller than the Planck scale of  $10^{-35}$  m! This 'trans-Planckian problem' is not just a curious side-note. Rather it implies that quantum spacetime effects can be amplified such that they undermine the semi-classical framework for modelling black holes. Various arguments have been put forward to screen Hawking radiation from this sensitivity to trans-Planckian physics. The focus of our analysis is arguments related to: i) the Unruh effect and equivalence principle (Agullo et al.

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<sup>1</sup>See for example (Batterman 2000; Batterman 2002; Mainwood 2006; Butterfield 2011; Ruetsche 2011; Franklin 2017; Palacios 2017; Fraser 2018; Shech 2018; Saatsi and Reutlinger 2018).

2009; Wallace 2017, §4.2); ii) horizon symmetries (Birmingham et al. 2001; Banerjee and Kulkarni 2008; Iso et al. 2006b); and iii) modified dispersion relations (Unruh and Schützhold 2005; Himemoto and Tanaka 2000; Barcelo et al. 2009). What all three sets of arguments have in common is that they aim to establish that the same phenomenon of Hawking radiation is suitably ‘universal’, whatever the micro-physics at and beyond the Planck scale may be. We will argue below that in each case the extent to which this aim is achieved is limited in important respects. The comparison between the Hawking radiation universality arguments and Wilsonian universality arguments will prove instrumental in both isolating these limitations and establishing possible avenues for them to be overcome.

At first sight, the Wilsonian and Hawking radiation universality arguments appear rather different, and it is thus not immediately clear that the comparison is apposite. Most obviously, whereas the principal conclusion supported by the Hawking radiation universality arguments is the insensitivity of a single phenomenon (Hawking radiation) under a token-level variation with respect to one aspect of the possible micro-physics of a single type of system (black holes), the Wilsonian universality arguments most vividly establish the insensitivity of a range of critical phenomena under a variation between different types of systems (e.g., magnets and fluids). This difference in emphasis notwithstanding, as we will argue at length below, both cases of universality arguments crucially rely upon the combination of single-type token-level insensitivity with inter-type insensitivity. The first form of insensitivity will be identified as ‘robustness’. The second form of insensitivity will be identified as ‘universality’ proper.

This observed conceptual similarity between the two sets of universality arguments is the starting point for the present analysis. Our goal is then to establish a framework through which the similarity can be rigorously assessed. Our framework is based upon six qualities:

1. *Degree of Robustness*. The range of single-type token-level variation across which the robustness can be established;
2. *Physical Plausibility*. The applicability of the robustness arguments to de-idealised target systems;
3. *Degree of Universality*. The range of inter-type variation across which the universality can be established;
4. *Comprehensiveness*. The size of the set of observables over which the robustness argument can be applied;
5. *Empirical Support*. Experimental evidence supporting instantiation of effects in different types and/or relevant methods of approximation;
6. *Integration*. Feature whereby the theoretical basis behind the invariance found in the universality arguments and the robustness arguments is the same.

Our main focus is to provide a diagnosis of *why* the Hawking universality arguments fail to measure up to their Wilsonian counterparts. This diagnosis will be in terms of the relationship between the qualities. In particular, it will be argued that much of the strength of the Wilsonian arguments is predicated upon their integration. Wilsonian universality arguments are able to combine such a high degree of robustness and universality because the theoretical basis behind the invariance in each case is the same. Furthermore, it is this combination that allows the arguments to also be highly physically plausible.<sup>2</sup> The converse of these relationships will be argued to hold in the Hawking case: the universality arguments that do well on degree of robustness do poorly on degree of universality and physical plausibility, and arguments that do well on degree of universality do poorly on degree of robustness. We argue that the lack of integration found in these arguments is a plausible reason for the existence of these trade-offs between the relevant subset of qualities. This negative conclusion provides a possible basis for future scientific research aimed at developing integrated universality arguments for Hawking radiation.

## 2 Hawking Radiation and the Trans-Planckian Problem

### 2.1 What is Hawking Radiation?

In quantum field theory on curved spacetime the ground state of a free quantum field can evolve into a state with excitations when the geometry of the background spacetime is non-trivial. In an asymptotically flat spacetime, this means that there can be a flux of ‘out-particles’ at future-null infinity  $\mathcal{I}^+$  even if there is no flux of ‘in-particles’ at past-null infinity  $\mathcal{I}^-$  (Jacobson 2005, §5). Most famously when the spacetime in question features a black hole, this flux can have a characteristic thermal form that depends only upon intrinsic properties of the black hole spacetime (Kay and Wald 1991). This thermalised flux is the Hawking radiation of a black hole.

The original treatment of Hawking (1975) proceeds as follows. Model an astrophysical black hole spacetime as the formation of a Schwarzschild black hole from the collapse of a matter shell.<sup>3</sup> The conformal diagram for the spacetime exterior to the collapsing matter is given in Fig 1. Within the spacetime assume that there is a free quantized Klein-Gordon field  $\hat{\phi}$ .

Further assume that there is no back-reaction between the quantum field and the background spacetime. The asymptotic flatness of the spacetime before and after the collapse selects unique ground state vacua and Fock representations for the Klein-Gordon field on  $\mathcal{I}^\pm$ . Assuming that there is no incoming radiation from  $\mathcal{I}^-$ , Hawking showed that the evolution of such a state would appear, to first order, as a thermal state at the *Hawking temperature*  $T_H = \frac{\hbar\kappa}{2\pi}$  for an

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<sup>2</sup>Batterman (2000, 2002) makes a similar point.

<sup>3</sup>See (DeWitt 1975) for the Kerr case.

observer near  $\mathcal{I}^+$  at asymptotically late times – i.e., near future time-like infinity  $i^+$  – where  $\kappa$  is the surface gravity of the black hole horizon.

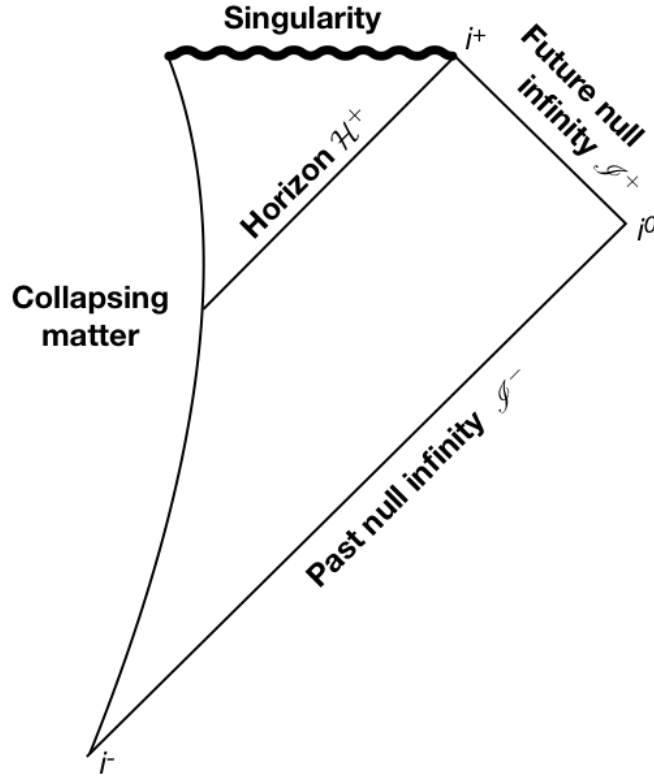


Figure 1: The conformal diagram of a spacetime external to a spherically symmetric distribution of collapsing matter.

Various proposals have been made to provide a local physical mechanism for the production of Hawking radiation. The different proposals vary significantly in terms of where and how the thermal radiation is produced and are largely mutually inconsistent. The most significant possible mechanisms include: splitting of entangled modes as the horizon forms (Unruh 1977; Gibbons 1977); tidal forces pulling apart virtual particle-anti-particle pairs (Hawking and Israel 1979; Adler et al. 2001; Dey et al. 2017); entangled radiation quantum tunnelling through the horizon (Parikh and Wilczek 2000); the effects of non-stationarity of the background metric field (Fredenhagen and Haag 1990; Jacobson 2005) and anomaly cancellation (Banerjee and Kulkarni 2008). The formal rigour of these proposals varies greatly, and none is entirely satisfactory from a physical perspective.

Ideally, we like is to find a relationship between the way in which the gravitational degrees of freedom interact with  $\hat{\phi}$  during the evaporation process and the production of the radiation itself. An explicit such demonstration is currently lacking for most, if not all, of the putative mechanisms.<sup>4</sup> At the very least, to be physically plausible, a mechanism for Hawking radiation must be explicitly demonstrated to be generalisable from the highly idealised cases of eternal

<sup>4</sup>See (Curiel 2018) are references therein.

black holes to physically realistic astrophysical models in which time translation symmetry is broken by the collapse phase leading up to the formation of the horizon (Hollands and Wald 2015).

Notwithstanding this lack of unique physically plausible mechanism or region of origin associated with Hawking radiation, it is certainly significant that the formal expression for Hawking flux has proved ‘remarkably robust’ under the inclusion of various complicating factors (Leonhardt and Philbin 2008; Thompson and Ford 2008) and formal clarifications (Freidenhagen and Haag 1990). As noted by Wallace (2017), such consistency between various theoretical derivations strongly suggests that Hawking radiation really is a consequence of semi-classical gravity and not simply an artefact of a particular (potentially flawed) argument. That said, robustness of an effect between different theoretical models offers little comfort if there is a problematic feature that all the various derivations share.

## 2.2 Red-Shift and Robustness

An important insight into the physics behind Hawking radiation, which is independent of the mechanism of production, can be obtained by considering the possible equilibrium states of the quantum field long after the collapse process has taken place. By this time we can assume that the geometry will have effectively reached Schwarzschild form (assuming zero angular momentum). Since this geometry is not maximally symmetric, there is no unique ground state singled-out by the global symmetries. To resolve this underdetermination, a variety of physically motivated principles can be appealed to. These principles are used to argue for different choices of privileged observers who are required to see the quantum field in a ground state. One choice, the *Boulware vacuum* (Boulware 1975), is a ground state as seen by the static observers of the exterior Schwarzschild geometry. In this state no fluxes are observed and there is thus no Hawking radiation. The Boulware vacuum is irregular on the horizon and generally regarded not to be a physically viable description of the vacuum state of a collapsed black hole. Two vacua that are regular on the horizon are the *Hartle–Hawking vacuum* (Hartle and Hawking 1976) and the *Unruh vacuum* (Unruh 1976; Dappiaggi, Moretti, Pinamonti, et al. 2011).

The Hartle–Hawking vacuum is a ground state as seen by in- and out-going null observers of the entire maximally-extended Schwarzschild geometry. When restricted to the exterior geometry, this state appears as a thermal state near future time-like infinity  $i^+$  for modes out-going from near the horizon (Kay and Wald 1991). Under similar conditions, the Unruh vacuum also appears as a thermal state on  $i^+$  but differs from the Hartle–Hawking vacuum away from  $i^+$  (Dappiaggi et al. 2011). The Unruh vacuum is defined to be a ground state for null out-going observers on the past horizon  $\mathcal{H}^-$  of maximally-extended Schwarzschild and for static observers near  $\mathcal{I}^-$ . It is justifiably regarded as being more physically motivated than the Hartle–Hawking vacuum as a description of the vacuum state of a collapsed black hole since any state evolving on a background that becomes Schwarzschild at late times will approach the Unruh

vacuum near  $i^+$ , provided that the state satisfies certain regularity conditions in the ultraviolet limit and has no in-coming radiation from near spatial infinity  $i^0$  (Fredenhagen and Haag 1990; Hollands and Wald 2015). In this sense, the Hawking spectrum is seen to be insensitive to the details of the collapse process and to the initial state of  $\hat{\phi}$  on  $\mathcal{I}^-$  (but away from  $i^0$ ). The main constraint on the state can be formulated, for example, in terms of the Hadamard condition (Hollands and Wald 2015) or via a scaling limit in the ultraviolet (Fredenhagen and Haag 1990). These constraints amount to regularity conditions in the ultraviolet limit and can be understood intuitively as enforcing high-energy modes to be effectively in a ground state. This avoids non-local divergences in the 2-point functions (Wald 1994; Hollands and Wald 2015). Furthermore, in conventional effective field theory treatments (Candelas 1980), which assume no unusual effects in the UV due to quantum-gravity, violation of the regularity conditions can be shown to lead to pathological behaviour near the horizon.

To better understand the role of the regularity conditions in establishing the robustness of the thermal spectrum we can analyse the relative frequency shift between the Killing frequency and affine frequency of a particular Hawking mode as seen respectively by static and null-geodesic observers (Jacobson 1996). The Killing frequency, which is constant along geodesics, is particularly useful for describing the frequency of free-falling modes of  $\hat{\phi}$  as they approach future time-like infinity  $i^+$ , where the static observers become inertial. The affine frequency is suitable for describing the frequency of free-falling  $\hat{\phi}$  modes near the horizon, where the affine coordinates describe a local patch of Minkowski space. A key formal property of the Schwarzschild geometry, which can be generalized to arbitrary Killing horizons (Kay and Wald 1991), is that the affine frequency is exponentially related to the Killing frequency near the horizon. Given the properties outlined above, this fact implies that free-falling modes near the horizon will be red-shifted exponentially as they approach  $i^+$ . Furthermore, if the Killing modes of  $\hat{\phi}$  are expanded in terms of in-going and out-going affine components, then as the horizon is approached more and more of the in-going affine modes will disappear behind the horizon, which provides a causal barrier to their escape. Thus a static detector approaching  $i^+$  will observe both an exponentially red-shifted spectrum and one entirely dominated by the out-going components. This means that the extreme red-shift combined with the presence of the horizon erases all information about how the horizon itself was formed and the details of the initial state of the radiative mode. The extreme red-shift further implies that in studying a moderate frequency mode at late times a static observer is effectively probing the ultraviolet structure of the 2-point functions of the mode near the horizon.

It is in this context that the regularity conditions imposed on the 2-point function in the ultraviolet become vitally important. As noted above, the conditions require that the modes observed near  $i^+$  be in their ground state near the horizon. Locally, this ground state is approximately the vacuum of Minkowski space split by the horizon into right and left Rindler-like regions. Tracing out the in-going modes (which disappear behind the horizon) therefore leaves the characteristically thermal state expected of the Rindler vacuum. The robustness of the ther-



mal spectrum detected by late-time observers thus results from three ingredients. First, the exponential red-shift, which implies that late-time observers probe ultra-high frequency modes near the horizon. Second, the regularity conditions, which enforce that a state in the ultraviolet is approximately a Minkowski vacuum state. Third, the horizon, which creates a causal barrier between the in-going modes and the observers confined to the exterior region and therefore modifies the character of the state of the UV modes from ‘Minkowski-like’ to ‘Rindler-like’.

## 2.3 Ultraviolet Catastrophe

With some irony, the mechanisms that are responsible for the ‘remarkable robustness’ of Hawking radiation are simultaneously a cause for scepticism. As we have just seen, the exponential red-shift implies that the spectrum of radiation at late times is dominated by the characteristics of the state of the field near the horizon at energies that well exceed the Planck scale. It can be shown that the modes in question are those whose energy is that of an arbitrary time-like particle no more than a Planck time before falling through the horizon (Helfer 2003). This is precisely the regime where quantum gravity effects, such as those due to entanglement with the horizon, would be expected to be relevant and thus the semi-classical framework no longer be valid. We have run into the trans-Planckian problem.<sup>5</sup> As was aptly put by Jacobson (2005), the trans-Planckian problem amounts to ‘a breakdown in the usual separation of scales invoked in the application of effective field theory’ (p.79).<sup>6</sup> In response to this breakdown, and in particular the role played by back-reaction and the evaporation process, Fredenhagen and Haag (1990) conclude that ‘a full understanding of the [Hawking] phenomenon including a self-consistent description of the causal structure needs some elements of a quantum theory of gravity’ (pp.282-3). As noted by Unruh (2014), in typically robust fashion, ‘if one examines Hawking’s original calculation, there are some severe problems with his derivation. While mathematically unimpeachable, they are nonsense physically’ (p.533). To highlight the significance of the scales involved Unruh estimates that the ‘frequencies which are needed to explain the radiation produced even one second after a solar mass black hole forms, correspond to energies which are  $e^{10^5}$  times the energy of the whole universe.’ (Unruh 2014, p.533).

An influential attempt to resolve the trans-Planckian problem is the ‘nice slice’ argument due to Polchinski (1995). The argument has been recently endorsed in the philosophy literature by Wallace (2017) and is also popular amongst string theorists. Polchinski defines a particular slicing of a black hole spacetime that is ‘nice’ in the sense that the slices are smooth, have small extrinsic curvature, and are such that in-falling particles are seen to have modest velocities. Due to the small extrinsic curvature the geometry of the slices changes slowly from slice to slice. Polchinski then argues that the adiabatic theorem should apply to modes in this slice and

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<sup>5</sup>See (Gibbons 1977; Unruh 1981; Jacobson 1991; Jacobson 1993; Unruh 1995; Brout, Massar, Parentani, and Spindel 1995; Helfer 2003). Accessible introductions are give in (Jacobson 2005, §7) and (Harlow 2016, pp.36-8).

<sup>6</sup>For a more general argument that effective field theory methods may breakdown near horizons see (Burgess et al. 2018).

therefore that only very low-energy degrees of freedom can be excited from their ground state in the Hawking emission process (by whatever mechanism it takes place). According to this argument, the entire process can be described using local low-energy physics near the horizon and will therefore be independent of Planck scale effects.

The ‘nice slice’ argument is unconvincing as a response to the trans-Planckian problem as we have formulated it. In particular, the assumption that the relevant modes are in a genuine ground state is precisely the assumption that is in question. As emphasised by Jacobson in the quote above, the trans-Planckian problem occurs precisely because we have good reasons to expect the separation of energy scales to breakdown. Thus, whether the adiabatic theorem, or local arguments from effective field theory in general, should apply to near-horizon modes, which may be entangled or even interacting with the geometric degrees of freedom of the horizon, is exactly the issue at hand. Plausibly, some form of non-linear gravity-matter interaction is required for the evaporation process to take place at all. Furthermore, as noted by [Harlow \(2016\)](#), the adiabatic theorem applies only to the global conserved energy not to the centre of mass energy of localized excitations. Finally, the nice-slice argument does nothing to ameliorate the exponential redshift: ‘it does not get rid of the fact that projecting onto possible final states of the late-time Hawking radiation produces states with a genuine high energy collision in the past’ ([Harlow 2016](#), p.37-38). Thus, *pace* Wallace, Polchinski’s argument offers no definitive means to rebut the force of the trans-Planckian problem.<sup>7</sup>

A different response to the trans-Planckian problem is based upon the inconsistency of Hawking radiation *not* existing. The argument is that the physics of the Planck scale cannot alter the Hawking spectrum since to do so would violate the semi-classical field equations ([Candelas 1980](#); [Sciama et al. 1981](#)). However, once more, such a line of response is based upon an assumption that is itself in question. We might reasonably assume that due to the relatively mild curvature, the semi-classical field equations must apply to any local observers description of vacuum fluctuations near the horizon of an astrophysical black hole. However, in order for us to extend this assumption to near-horizon fluctuations as seen by a late-time observer, due to the exponential red-shift, we must assume that the semi-classical field equations continue to hold up to and beyond the Planck scale. However, it is at precisely at the Planck scale that we expect violations of the semi-classical field equations to occur.

What we take to be the essential lesson is that absent a well-trusted theory of quantum gravity, any derivation of Hawking radiation as a phenomena that depends on near-horizon physics must be supplemented with an argument for the insensitivity of the effect to ultra short-distance physics.<sup>8</sup> This supplement may take the form of an additional argument or a modification of the

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<sup>7</sup>The possibility for quantum gravity effects to undermine the nice slice argument is in fact acknowledged in the original paper ([Polchinski 1995](#), §2) and, for example, in subsequent discussions regarding firewalls ([Almheiri, Marolf, Polchinski, and Sully 2013](#)).

<sup>8</sup>To keep our discussion within reasonable constraints we have chosen to excluded approaches to Hawking radiation that do not feature near horizon sensitivity. See ([Parentani 2010](#); [Giddings 2016](#); [Hod 2016](#); [Dey, Liberati, and Pranzetti 2017](#)).

derivation. In either case, the insensitivity is required to be at a token-level, since we need to establish the insensitivity of the effect to different possible ultraviolet physics for a given type of system, and type-level, since to justify our idealisations, we need to establish the insensitivity of the effect to the type of black hole being considered. In the terminology introduced above we need an argument for both the *robustness* and *universality* of Hawking radiation. Before we consider examples of such arguments, it will prove instructive to first examine the structure of Wilsonian universality arguments found in the context of condensed matter physics.

### 3 Universality Arguments in Condensed Matter Systems

#### 3.1 The Wilsonian Approach to Critical Phenomena

A phase transition occurs when there is an abrupt change in the macroscopic parameters that uniquely specify the equilibrium states of a system. A first-order phase transition is characterized by the existence of discontinuities in the first derivatives of the free energy. Continuous phase transitions, in contrast, involve divergence of the response functions. An important feature of continuous phase transitions is that in the vicinity of the critical point measurable quantities depend upon one another in a power-law fashion. For example, in the ferromagnetic-paramagnetic transition, the net magnetization,  $M$ , the magnetic susceptibility,  $\chi$ , and the specific heat,  $C$ , all depend upon the reduced temperature  $t = \frac{T-T_c}{T_c}$  (the temperature of the system with respect to the critical temperature  $T_c$ ) as:

$$M \sim |t|^\beta, C \sim |t|^{-\alpha}, \chi \sim |t|^{-\gamma}, \quad (1)$$

where  $\beta$ ,  $\alpha$ ,  $\gamma$  are the *critical exponents*. Another remarkable feature of these phenomena is the existence of cooperative behaviour at the transition or critical point, which means that the correlations between particles extend to very large distances even if the microscopic interactions between them remain short range. This implies the divergence of the correlation length  $\xi$ , which is a quantity that measures, for example, the distance over which spins in are correlated. The divergence of the correlation length is perhaps the most important feature of continuous phase transitions. In particular, it involves the loss of a characteristic scale at the transition point and thus provides a basis for the explanation of universal behaviour. That is, the divergence of the correlation length explains why system types with physically distinct micro-structure, such as ferromagnets, antiferromagnets and fluids, display the same macro-behaviour.

Landau's theory of continuous phase transitions ([Landau 1936](#)) was one of the first attempts to give a rigorous explanation for the behaviour of physical variables close to the critical point and anticipated the development of renormalization group approaches. In this theory, physical variables, such as magnetization, are replaced by their average values and non-linear fluctuation contributions are neglected. One can then use Landau theory to estimate the importance of

fluctuations close to the critical point. For space dimension  $d > 4$ , the theory makes adequate predictions of the order parameter and the critical exponents. Unfortunately, for  $d \leq 4$ , the Landau's theory of continuous phase transitions predicts strong infrared singularities in the lowest order fluctuation contributions, which means that fluctuations dominate the behaviour close to the critical point (Goldenfeld 1992, §6).

In analogy with the trans-Planckian problem, the problem of infrared singularities requires us to find a means to screen observable quantities in our theory from a breakdown in the separation of scales. One strategy is to explicitly renormalize the ultraviolet divergences, which involves expressing the weight of fluctuation contributions (amplitudes), in terms of physical coupling constants without assuming any particular cut-off in the calculation. Wilson (Wilson 1971; Wilson and Kogut 1974) suggested a different strategy, now called momentum shell renormalization group (RG), that consists in integrating out short-range wavelength modes up to a finite cut-off in momentum  $\Lambda$ .<sup>9</sup> In this approach, one starts by defining a field theory in which the degrees of freedom are represented in terms of Fourier modes,  $S(q)$ . The partition function is then expressed as an integral over the full range of Fourier components. Each field theory, as defined by a particular local Hamiltonian (or Lagrangian), will then be characterized by the set of coupling constants  $g_i$  that measure the strength of the various interactions. The core idea of RG approach is to examine how the coupling constants change as one varies the length scale of interest, which is achieved by changing the value of the cut-off  $\Lambda$ . For continuous phase transitions one is interested in the limit of large length scales thus, for such theories, one analyses the behaviour of the coupling constants as the length scale increases.

This RG procedure involves the following three steps: First, one carries out the partition integral over all Fourier components  $S(q)$  with wave vectors residing in the momentum shell  $\Lambda/b \leq |q| \leq \Lambda$ , where  $b > 1$ . This step effectively eliminates the short-wavelength modes and thus corresponds to a coarse graining. Second, one relabels the control parameters by performing a scale transformation:  $x \rightarrow x' = x/b$  and  $q \rightarrow q' = bq$ . Third, one relabels the field degrees of freedom by performing a scale transformation:

$$S(x) \rightarrow S'(x') = b^\zeta S(x), S(q) \rightarrow S'(q') = b^{\zeta-d} S(q), \quad (2)$$

where  $\zeta$  must be chosen so as to assure that the rescaled residual Hamiltonian recovers the original form. The three steps result in an 'effective' Hamiltonian, which has different values of coupling constants than the original Hamiltonian but in successful cases has the same form. The RG transformations, given by repeated application of the three steps, are associated with a flow on theory space that tells us how the coupling constants change. Depending on their behaviour under repeated iterations of the coarse graining transformations, the coupling constants can be classified as:

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<sup>9</sup>Kadanoff's real-space renormalization approach has been neglected for reasons of space. Plausibly our analysis will apply mutatis mutandis. See (Fisher 1998; Goldenfeld 1992; Mainwood 2006; Franklin 2017).

- i *relevant coupling constants*, which grow and ultimately tend to infinity as the number of iterations tends to infinity. These parameters allow one to define the *critical surface*;
- ii *irrelevant coupling constants*, which ultimately approach zero in the RG procedure and do not affect the critical behaviour;
- iii *marginal coupling constants*, which approach an infrared-stable fixed point that is associated to scale-invariant behaviour.

The disappearance of the irrelevant couplings and the existence of non-trivial infrared fixed points is precisely what resolves the problem of infrared singularities in the RG approach. Crucially for our analysis, it is also this feature that establishes both the robustness and universality of the critical phenomena.

The Wilsonian RG argument for universality takes the following form. Given the disappearance of the irrelevant couplings and the existence of a non-trivial infrared fixed point, the critical behaviour will depend only on the spatial dimension and the symmetries of the original Hamiltonians and not on the strength of the nonlinear couplings or other non-universal parameters. All distinct Hamiltonians whose trajectories converge toward the same infrared fixed point, i.e., the basin of attraction of the fixed point, will then exhibit identical behaviour at the critical point. This establishes universality since the critical phenomena in question have been shown to be insensitive to a inter-type variation between systems described by the set of distinct Hamiltonians (i.e., variation across the relevant universality class). Furthermore, the same arguments also establish robustness. This is because the critical phenomena in question have been shown to be insensitive to a variation between possible microphysical realisations of a single type of system as described by distinct Hamiltonians. It is thus the very same mathematical properties of the basin of attraction of the fixed point that establish both robustness and universality. The difference between robustness and universality in the case of the RG approach is merely one of interpretation. It amounts to the choice as to whether we understand the distinct Hamiltonians as representing different possible physics of the same type of system, or different possible system types. The implications of this close connection between robustness and universality will be important in the next section.

### 3.2 The Six Qualities

Drawing upon the Wilsonian exemplar we can identify six key qualities of a successful universality arguments. First, the degree of robustness, which is the range of single-type token-level variation across which the robustness can be established. A Wilsonian treatment of RG transformations comes with a well-defined set of restrictions regarding the type of possible micro-interactions that can be shown to be irrelevant, and these limitations restrict the degree of robustness that the arguments can establish. Most importantly, the theory space contains only theories within the broad framework of quantum field theory. When we are dealing with

discrete systems, this assumption can obscure the connection to the microphysics of the systems. Further restrictions are then imposed within the family of field theories. In particular, the interactions must be short range (Wilson and Kogut 1974, p. 161) and expressible in terms of a convergent set of constants and differential operators. Finally, in constructing theory space one is required to make assumptions about the number of spacetime dimensions and the irrelevance of, as yet unknown, fundamental spacetime structure. Not least in assuming a smooth  $3 + 1$  spacetime model we are implicitly also assuming that we can rule out macro-level effects that have their origin in an unknown number of compactified extra dimensions or even fundamental dimensional heterogeneity (Täuber 2012) due for example to quantum modifications to the spectral dimension of spacetime. That said, we have good reason to expect that the ‘separation of scales’ should mean that even if spacetime is fundamentally dimensionally heterogeneous or matter is not described by a quantum field theory, these assumptions will not undermine the effectiveness of the RG approach. These limits on the degree of robustness are thus very mild when considered in the relevant context.

The next two qualities on our list are closely connected to the first. The second quality is physical plausibility, which is the applicability of the robustness arguments to de-idealised target systems. The Wilsonian framework does particularly well on this front. By design, the arguments coarse-grain out physically irrelevant detailed information. This means that they are particularly suitable for modelling real systems. What is shown by these arguments is the robustness of certain features with regard to different possible microphysics *and* different possible complicating factors, both micro and macro.<sup>10</sup> The third quality on our list is the degree of universality. This is the range of inter-type variation across which the universality can be established. This is one of the core virtues of Wilsonian renormalization group methods. In particular, the Wilsonian approach provides a means to characterise both quantitative and qualitative aspects of the ‘universal phenomena’ across a wide range of system types such as fluids, ferromagnets, and antiferromagnets.

The fourth quality we isolated was comprehensiveness. This is the size of the set of observables over which the robustness argument can be applied. At criticality the arguments apply to all relevant observables and so this quality is again very strong. The fifth quality was empirical support. It is possible to use this framework to calculate explicit values of the critical exponents by linearizing around the fixed points and these values are found to be in good agreement with experimental results – see for example, (Ahlers, Kornblit, and Guggenheim 1975). Thus, the arguments are directly supported by experimental evidence in the relevant range of physically instantiated types. Furthermore, the methods of approximation that underlie the Wilsonian approach are also justified by the fact that they successfully reproduce empirically observed phenomena.<sup>11</sup>

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<sup>10</sup>For more on the relationship between idealisations and RG universality arguments see (Batterman and Rice 2014; Palacios 2017).

<sup>11</sup>See (Blum and Joas 2016) for analysis of a historical case study focusing on the interplay between experimental evidence, approximations techniques and ‘emergent entities’ in the context of RG techniques.

The sixth quality, crucial to our analysis, is integration. Integration is the quality whereby the theoretical basis behind the invariance found in the universality arguments and the robustness arguments is the same. Wilsonian arguments are clearly integrated since, as noted above, it is the very same mathematical properties of the basin of attraction of the fixed point that establish both robustness and universality. The irrelevance of the micro-details of a given system and the irrelevance of the micro-details of different systems are established by the same means. Integration means that the high degree of robustness established by Wilsonian arguments automatically underpins a similarly high degree of universality (Batterman (2002, p.13) also notes this connection).

In general terms, we can expect integration to obtain whenever the robustness argument that establishes token-level insensitivity is applicable to multiple different system types. In such situations, the universality argument is constituted by the robustness argument together with some general commonality conditions between the types. In the Wilsonian case these are the spatial dimension and the symmetries of the original Hamiltonian. Furthermore, given an argument with a high degree of robustness, we can expect integration to imply both high physical plausibility and a high degree of universality. This is because such an argument allows us to use insensitivity under token-level variations between different possible micro-physics to show insensitivity under: i) de-idealisation, which means that the same predictions will also hold for de-idealised models; <sup>12</sup> and ii) re-interpretation, which means that we can re-interpret the system type by adding details that characterize particular models. Conversely, given an argument with a high degree of universality, we can expect integration to imply both high physical plausibility and a high degree of robustness on a similar basis. Without integration we have no expectation for these qualities to be so linked. Plausibly, integration is the *sine qua non* of a genuinely successful universality argument.

## 4 Universality Arguments for Hawking Radiation

### 4.1 Arguments from the Equivalence Principle

Our first example is best understood as an independent universality argument for Hawking radiation, rather than an alternative derivation. It is based upon a heuristic argument that runs as follows. Through the equivalence principle, Einstein taught us that gravitation and acceleration are locally indistinguishable. This means that we should expect to be able to translate the local physics experience by a stationary observer in a region outside the event horizon of a black hole spacetime into equivalent physics experienced by a constantly accelerating Rindler observer in a Minkowski spacetime. A translation scheme based upon the equivalence princi-

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<sup>12</sup>It is important to note that this is not equivalent to the claim that one can find fixed-point solutions in a de-idealised model, which is still matter of controversy in the philosophical literature (Batterman and Rice 2014; Palacios 2017; Saatsi and Reutlinger 2018).



ple would instruct us to identify the Hawking radiation detected by some stationary observer in the black hole spacetime with the Unruh radiation detected by a Rindler observer with the same acceleration. In particular, a simple argument – see e.g. (Wallace 2017, pp.23-4) – can be used to numerically identify the Hawking temperature of a black hole with the Unruh temperature of a near-horizon observer red-shifted to infinity.<sup>13</sup> Next, one shows that the Unruh effect is suitably robust under some class of possible ultraviolet modifications (i.e. quantum gravity effects). Using the translation scheme for near-horizon observers one then infers that the Hawking effect should also be robust to ultraviolet modifications. Such reasoning suggests that we were wrong to ever think of Hawking radiation and the Unruh effect as two separate phenomena, just as it would be wrong to distinguish gravitational and inertial mass. Rather, the equivalence principle argument implies the two effects to be instances of single universal phenomenon of Unruh/Hawking radiation connected to acceleration/gravitation. Although suggestive, and to an extent physically insightful, in this section we will isolate the various senses in which such a line of argument is unreliable. We start by analysing the evidence for the robustness of the Unruh effect.

The most physically salient starting point is the ‘detector approach’ to describing Unruh radiation (Unruh 1976; Unruh 1975; Crispino, Higuchi, and Matsas 2008). In this approach, a particle detector is made to follow a constantly accelerating path through Minkowski spacetime. In the simplest case, a scalar field in its vacuum state is coupled to the detector in such a way that the detector will count any sufficiently localized particle that enters the detector. The quantum field theoretic calculation can be done rigorously. In particular, the thermal spectrum can be obtained as the result of a particular branch cut in the relevant integrals over the divergent part of the 2-point functions. Two important factors therefore determine the thermal form of this spectrum: the Lorentz invariance of the procedure, which controls the periodicity of the domain of the analytically continued integrals, and the precise form of the ultraviolet divergences of the 2-point functions (Agullo et al. 2009). The physical mechanism behind the particle production in the Unruh effect can be understood in terms of the physical force responsible for the detector’s sustained acceleration. The ‘energy reservoir’ for the pair production is then seen to arise from whatever source is producing the energy to maintain this force.

Given these insights, it is possible to investigate whether trans-Planckian modifications due to gravitational physics should have a noticeable effect on the spectrum observed by the detector via its response function. In this context, different kinds of ultraviolet modifications have been considered in the literature and all point to a limited degree of robustness of the thermal Unruh spectrum. In (Agullo et al. 2009) the effect of introducing a Lorentz-invariant ultraviolet cutoff for the scalar field modes on the detector response function is considered. It is found that the thermal Unruh spectrum is insensitive to the introduction of this particular cutoff provided it is Lorentz-invariant. Contrastingly, it is also shown that non-Lorentz invariant cutoffs ruin

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<sup>13</sup>The red-shifting here is important because it regularizes the proper acceleration of a stationary observer on the horizon which is formally divergent.



the thermal properties of the spectrum by introducing a time-dependent damping effect on the detection rate of Unruh modes. We thus see that the Unruh effect should not be expected to be robust with respect to effects due to violations of Lorentz invariance in the ultraviolet. In more general terms, it can be explicitly shown via non-perturbative Functional Renormalization Group methods that, even in the case of Unruh radiation, the thermality of the spectrum can be ruined by a variety of quantum gravity effects (Alkofer et al. 2016). Such effects are unlikely to improve in the Hawking case, and could even be compounded by non-linear effects during the evaporation process.

Certain features of Unruh radiation can thus be seen to be robust under certain limitations. On such a basis one might plausibly attempt to construct an argument for the universality of Hawking radiation based upon the equivalence principle along the lines of the heuristic argument presented above. Agullo et al. (2009) do this as follows. First, reason that a small detector near the horizon is locally indistinguishable from a Rindler observer in Minkowski space provided the detector is much smaller than the Schwarzschild radius of the black hole. Next, assert that such a detector will have a response rate identical to the one computed in the Unruh case. Finally, use the robustness of the Unruh effect to reason that the response function of the detector *in the black hole spacetime* will be invariant under arbitrary Lorentz-invariant modifications.

There are good reasons to be sceptical regarding this line of reasoning. As we have seen already, one must be cautious about using a local argument concerning the behaviour of a detector near a horizon to make inferences regarding the behaviour of a late-time detector far away from the horizon. While particle detection is itself a local process, the parameters of the Hawking spectrum, such as its temperature, depend functionally on global properties of the spacetime, such as its ADM mass. This is ultimately because the Hawking spectrum is determined in terms of an integrated effect of the field over its entire history. Moreover, as argued in detail by Helfer (2010), the cis-Planckian Hawking modes detected by a stationary detector near the horizon of a black hole can contribute only a negligible proportion of the total Hawking flux detected at late times. Thus, almost all the late-time Hawking fluxes must stem from thermal modes that are trans-Planckian for the near-horizon inertial observers. It is therefore clear that universality arguments for Unruh radiation are completely ill-suited to provide a response to the trans-Planckian problem. They can only show insensitivity of near horizon cis-Planckian thermal spectrum to unknown trans-Planckian physics. By construction, they are silent regarding the properties of (almost all of) the late-time Hawking radiation.

Equivalence principle based universality arguments thus do badly on the qualities of both degree of robustness and physical plausibility. The idealisation that the entire class of observers can be represented by near-horizon detectors limits the argument in terms of both the token-level insensitivity established and applicability to de-idealised token system. In fact, it can be shown that repeating the above argument using *any* observer other than one infinitesimally close to the horizon leads to the wrong answer (Singleton and Wilburn 2011) for the pre-

dicted radiation near  $i^+$ .<sup>14</sup> This puts into the question the consistency of the entire approach. The score on degree of universality is better since two fairly different system types (Rindler and black hole spacetimes) are included. Contrastingly comprehensiveness is low since only a single observable is covered. Empirical support is completely lacking. Furthermore, and most problematically, the argument is worryingly unintegrated. The theoretical basis for universality (the equivalence principle) is not just different to, but in tension with, the theoretical basis for robustness (effective field theory arguments applied to the Unruh effect). Plausibly, it is precisely the lack of integration that renders this an argument almost without qualities.

## 4.2 Arguments from Horizon Symmetries

Our next candidate universality argument is best understood as a new derivation of Hawking radiation as a universal phenomena based upon the symmetries of the black hole event horizon. The argument relies upon the cancellation of anomalies of the effective event horizon symmetries to establish robust properties of the resulting Goldstone bosons. These Goldstone bosons are then interpreted as Hawking fluxes which suggests that Hawking radiation is itself robust.

A good starting point is to observe that in general there exists an expansion of the d'Alembertian (in terms of the radial tortoise coordinate) near a fairly general class of horizons within which the leading order term is conformal and the angular contributions can be integrated out. This means that a Klein-Gordon theory reduces to an effective 1 + 1 conformal field theory near such a horizon (Birmingham et al. 2001; Carlip 2005). These simplifications allow, under fairly general assumptions, for the near-horizon Klein-Gordon modes to be written as representations of a chiral Virasoro algebra whose quantization is well-known. In 1 + 1 dimensions, there is a conformal anomaly that can be expressed in terms of the topological invariants of the horizon geometry. This quantum mechanically broken conformal symmetry can be seen to lead to the generation of Goldstone bosons that must be present to cancel the anomaly. It is these Goldstone bosons that are interpreted as Hawking fluxes. Two formal observations support this interpretation. First, a state-counting of the Goldstone bosons generated by such an anomaly can be found to exactly reproduce the Bekenstein–Hawking entropy that one would expect for a black hole (Carlip 2005). Second, if one computes the emission rate of the Goldstone bosons from the horizon, the response rate at infinity reproduces a thermal Hawking spectrum (Banerjee et al. 2010; Banerjee and Kulkarni 2008).<sup>15</sup>

Arguably, further justification is needed to identify the generation of Goldstone bosons from a broken conformal symmetry with genuine Hawking fluxes. However, given such an identification, the argument from horizon symmetries shows precisely why we should expect Hawking radiation to have a degree of robustness comparable to the Wilsonian approach. In particular, that the anomalies in the near-horizon field theory are related to topological invari-

<sup>14</sup>This is effect is most extreme for static observers near  $i^+$  who see no Unruh radiation at all.

<sup>15</sup>See also (Iso, Umetsu, and Wilczek 2006a; Iso, Umetsu, and Wilczek 2006b).

ants of the horizon geometry means they can be expected to be invariant under a wide range of possible micro-physics. This is because any ultraviolet modifications that preserve the relevant symmetries without disrupting the topological properties of the horizon will produce the same spectrum of Goldstone bosons. This approach thus allows us to demonstrate invariance of the Hawking spectrum under any ultraviolet modifications that are due to quantum gravity effects that preserve the horizon symmetries without disrupting the topological properties of the horizon. Such assumptions are natural in string theory where conformal symmetry of the  $1 + 1$  dimensional string worldsheet plays a vital role in the expected ultraviolet finiteness of the theory. However, the assumption that the horizon is smooth and has a definite position – even when probed by arbitrarily high energy modes – requires further justification in the context of quantum gravity. Moreover, it is certainly not clear that physically realistic horizons, such as the event horizons of astrophysical black holes, can indeed be effectively described using Virasoro methods, since there is no proof that the reduction to  $1 + 1$  dimensions can adequately encode the physics of collapse. This notwithstanding, given we have justification of the identification of Goldstone bosons as Hawking fluxes, we can take arguments from Horizon symmetries to imply a fairly wide range of token-level insensitivity of Hawking radiation within the idealised system type that they describe. The arguments are thus moderately robust.

A further advantage of these methods is in terms of their comprehensiveness. It is known that, for CFTs in  $1 + 1$ , all observables (i.e.,  $n$ -point functions) can be computed directly from the symmetry considerations of the Virasoro algebra. This means that the arguments apply to all measurable processes rather than a restricted class of observables. With regard to the quality of comprehensiveness the horizon symmetry approach to black holes is comparable to the Wilsonian approach to condensed matter.

To what extent can we think of these arguments for horizon symmetries as universality arguments? Since only quite general properties of the horizon geometry and the Klein-Gordon operator are required to derive the Hawking flux, one might expect that the arguments will be applicable regardless of the type of physical system in question. Clearly this depends upon the extent to which the relevant features of the horizon geometry and the conformal expansion of the Klein-Gordon operator are instantiated in a wide range of physically plausible models. At present the Goldstone bosons and their entropies have only been computed for the a restricted class of horizons where back-reaction and evaporation effects are ignored. As noted above, such models are highly idealised. Most significantly, they assume both that the horizon can be treated as a boundary with fixed location even for the highest of trans-Planckian modes and that the equilibrium state of these modes is independent of the details of the non-stationary collapse process itself. It is an interesting open question whether the numerical coincidence between the Goldstone bosons and Hawking modes can be given a plausible physical basis in non-stationary and evaporating black hole models. However, it is certainly not a matter beyond all conjecture; if Hawking radiation really does causally depend upon the creation of the horizon and the violation of time translation invariance, perhaps due to some non-linear quantum back-

reaction between the background quantum geometry and the trans-Planckian modes (or some other effect), then the physical basis behind this approach will be undermined. We thus find that both the physical plausibility and degree of universality of these arguments is severely limited. Empirical support is obviously also lacking.

Finally, we find arguments for the universality of Hawking radiation based upon horizon symmetries are not integrated. Unlike in the Wilsonian approach, the robustness arguments in question do not also function as theoretical underpinnings for universality arguments – they are highly type sensitive. It is natural to diagnose the weakness with regards to degree of universality and physical plausibility, despite high robustness, as stemming from this lack of integration. Thus although arguments from horizon symmetries do provide a remarkably robust and comprehensive derivation of Hawking radiation, that establishes the effect as originating from very general features of anomaly cancellation, since they are unintegrated, these arguments do not establish the effect as universal and also there are also doubts regarding their physical plausibility.

### 4.3 Arguments from Modified Dispersion Relations

Our final example of a universality argument for Hawking radiation takes the form of a general strategy for modifying derivations of Hawking radiation such that ultra-short distance effects are factored in. The key idea is that quantum gravity corrections to the Hawking spectrum can be modelled in terms of their effects on the propagation of the scalar field. In particular, the corrections are characterised in terms of a set of possible modifications to the dispersion relation of the high-energy Hawking modes. The late-time flux of Hawking modes is then computed with the modified dispersion relations using a straightforward generalisation of Hawking’s original derivation. Provided the modifications to the dispersion relation satisfy a number of criteria the Hawking spectrum can be shown to be insensitive to the modifications.

The original idea behind the modified dispersion relation approach comes from numerical studies of analogue black holes<sup>16</sup> which indicate that one can use a modified dispersion relation to understand the ‘ultraviolet’ breakdown of continuous fluid models due to atomic effects (Jacobson 1991; Jacobson 1993; Unruh 1995). Various generalisations of this approach to the gravitational case have now been achieved but, for our purposes, the most physically enlightening will prove to be that of Unruh and Schützhold (2005).<sup>17</sup>

The universality argument of Unruh and Schützhold (2005) can be reformulated to make the comparison with Wilsonian universality arguments as follows.<sup>18</sup> First, take the family

<sup>16</sup>See (Unruh 1981; Garay et al. 2000; Philbin et al. 2008; Belgiorno et al. 2010; Unruh and Schützhold 2012; Liberati et al. 2012; Nguyen et al. 2015; Jacquet 2018).

<sup>17</sup>See also (Brout et al. 1995; Corley 1998; Himemoto and Tanaka 2000; Barcelo et al. 2009; Coutant et al. 2012; Schützhold and Unruh 2013).

<sup>18</sup>Two particular differences in our formulation are that in their analysis condition (ii) is left implicit and condition (iv) is reformulated in a mathematically equivalent way (see its use in Equation (16) of (Unruh and Schützhold 2005)).

of modified dispersion relations to be parametrized by a single function,  $F$ , on momentum space. This function can be interpreted as representing a (non-Lorentz invariant) 3-momentum-dependent mass term for the Klein-Gordon field. In terms of the function  $F$ , the modified Klein-Gordon equation then takes the local form:

$$(\square + F(\hat{p}^2)) \phi = 0, \quad (3)$$

where  $\square$  is the Klein-Gordon operator in the exterior Schwarzschild spacetime and  $\hat{p}^2$  is some differential representation of the 3-momentum operator in a first quantized Casimir Klein-Gordon theory. In momentum space,  $F$  can be taken to be some function of the eigenvalue  $k^2$  of the linear momentum Casimir operator satisfying four criteria:

- (i) *Analyticity*:  $F(s^2)$  has an analytic continuation in terms of some convergent power series expansion in  $s$ , for  $s \in \mathbb{C}$ .
- (ii) *Vanishing in the infrared*:  $F(k^2) \rightarrow 0$  when  $k \rightarrow 0$  so that the dispersion relation is unmodified for the low energy modes.<sup>19</sup>
- (iii) *Sub-luminal*:  $F(k^2) \leq k^2$  so that all modes travel slower than the speed of light.
- (iv) *Scaling limit*:  $F(k^2) \rightarrow \tilde{F}_\infty k^2$  for  $0 < \tilde{F}_\infty < 1$  when  $k \rightarrow \infty$  so that the dimensionless mass term,  $\tilde{F}(k^2) = \frac{F(k^2)}{k^2}$ , flows to a constant,  $\tilde{F}_\infty$  in the ultraviolet.

The relevant limits of  $k$  above are defined relative to the Planck scale so that the infrared and ultraviolet limits represent the sub- and trans-Planck limits respectively. It is worth noting that, aside from the sub-luminal assumption, the above criteria are remarkably similar to those found in the Wilsonian renormalization framework. In particular, plausibly we can understand  $F(k^2)$  as representing a running coupling in a particularly simple truncation of the Klein-Gordon theory space. The reasoning of this approach is to assume that  $F(k^2)$  could be obtained from an honest Wilsonian treatment of the coupled Klein-Gordon and quantum-gravity system. But without a concrete proposal for quantum gravity, the specific form of  $F(k^2)$  is left free (up to the restrictions mentioned above). Moreover, in the context of the Hawking set-up where the WKB approximation applies to the Hawking modes, the classical (effective) Green's function contains most of the information of the full quantum mechanical 2-point function. Thus criterion (iv) formally accomplishes many of the same things as requiring the Klein-Gordon state to be Hadamard or to have a scaling limit.<sup>20</sup> Using (3) it is possible to explicitly compute the spectrum of Hawking fluxes by essentially following Hawking's original procedure. The exponential nature of the red-shift between near-horizon Killing and affine modes drowns out

<sup>19</sup>A rapidity of convergence condition could also be applied here.

<sup>20</sup>For the former, criterion (iv) in equation (16) of (Unruh and Schützhold 2005) guarantees that all divergences of the Green's function are local. For the latter, the fixed point requirement of  $\tilde{F}(k^2)$  is just equivalent to a scaling limit.

any contributions coming from the power-series expansion of  $F(k^2)$ , and a thermal spectrum is straightforwardly recovered.

The great strength of the modified dispersion relation approach is its physical plausibility. In fact, we take this style of approach to be the most physically plausible derivation of Hawking radiation available since, like the original Hawking calculation, we incorporate core physical features of astrophysical black holes whilst attempting to address certain aspects of the trans-Planckian problem. Since they are adapted from Hawking’s original treatment of astrophysical black holes, modified dispersion relation approaches are embedded in a physically plausible context for Hawking radiation. Furthermore, as could be expected given its origin, the modified-dispersion approach is readily applicable to a huge range of physical systems and thus also has a high degree of universality. In fact, any system to which a Hawking-style derivation can be applied can be supplemented with a corresponding modified dispersion relation treatment. This includes a wide variety of analogue black hole systems.

With regard to empirical support there is increasing cause for confidence. There are a large number of potential analogue realisations of the Hawking effect compatible with the modified dispersion relation argument. Examples include: phonons in superfluid liquid helium, ‘slow light’ in moving media, traveling refractive index interfaces in nonlinear optical media and laser pulses in nonlinear dielectric medium (Philbin et al. 2008; Belgiorno et al. 2010; Unruh and Schützhold 2012; Liberati et al. 2012; Nguyen et al. 2015; Jacquet 2018). Furthermore, in some such cases the physical reliability of the techniques has been evaluated experimentally (Weinfurtner et al. 2013; Steinhauer 2014; Steinhauer 2016; de Nova et al. 2018).<sup>21</sup> Thus, although the arguments are not supported by experimental evidence for the full range of physically instantiated types, the methods of approximation that underlie the modified dispersion relation approach are (at least in part) justified by the fact that they successfully reproduce empirically observed phenomena in some system types.

What we gain in physical reasonableness and degree of universality it appears, unfortunately, we have lost in degree of robustness. In particular, whilst the modifications considered are consistent with known microphysics of the analogue systems (for example the Bogoliubov theory of BECs (Recati et al. 2009)), they are highly restrictive with regard to the class of possible ultraviolet modifications to the physics of black holes. It is reasonable to identify this weakness in terms of a lack of integration. In particular, the same features that imply that the modified dispersion relations argument can be applied in a wider range of physical situations, are those that limit its robustness in the specific context of black hole physics. A particular concern is whether sub-luminal modified dispersion relations really are sufficient to model quantum gravity effects. Most significantly, the truncation used in the ‘Klein-Gordon theory space’ is of a very special type. In particular, a  $k$ -dependent sub-luminal mass term

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<sup>21</sup>For discussion of the problem of making inferences about black holes based upon universality arguments combined with such ‘analogue experiments’ see Dardashti et al. (2017), Dardashti et al. (2018), Thébault (2019). For other examples of analogue experiments combined with universality arguments see Thouless (1989), Prüfer et al. (2018), Erne et al. (2018), Eigen et al. (2018).



with a scaling limit in the ultraviolet is only the simplest example of how an effective quantum geometry could affect the propagation of Hawking modes across spacetime. Many quantum gravity proposals exhibit some sort of dimensional reduction or enhancement or non-locality in the ultra-violet where even a smooth local parameter such as  $k$  (let alone an analytic expansion in terms of it) may not be defined. The space of all such effects cannot plausibly be modeled in such a limited truncation.<sup>22</sup> The arguments also do not do well on comprehensiveness since they only apply to the occupation number of the Hawking modes.

In summary, the modified dispersion relation approach can legitimately be treated as a universality argument since it has the three qualities of robustness, physical plausibility and universality to a non-trivial degree. The arguments also have some empirical support. Modified dispersion relation arguments are, however, highly limited in their comprehensiveness. Moreover, with regard to black holes in particular, the arguments have only a low degree of robustness since there is only a very limited degree to which a modified dispersion relations approach can show the gravitational Hawking effect to be robust. Our diagnose of the cause of this issue is again a lack of integration since the basis behind robustness and universality are very different, the degree of token level insensitivity can vary to a high degree from type to type.

## 5 Conclusion

The principal strength of Wilsonian universality arguments is their integration. Since the basis for the invariance found in the universality arguments and the robustness arguments is the same, these arguments are able to combine a high degree of robustness, physical plausibility and universality. What is more the arguments are also comprehensive and empirically supported. Universality arguments for Hawking radiation fail to consistently measure up to their Wilsonian counterparts in terms of our six qualities. Arguments based on the equivalence principle do poorly on both degree of robustness and physical plausibility. Arguments based on horizon symmetry do well on degree of robustness, but do poorly on degree of universality and physical plausibility. Arguments based on modified dispersion relations do well on degree of universality and physical plausibility, but do poorly on degree of robustness. We have isolated the lack of integration found in these arguments as a plausible reason for these trade-offs between the relevant subset of the qualities. Given that the trans-Planckian problem threatens to undermine the entire semi-classical framework for modelling black holes, it is significant that none of the available universality arguments offer an entirely convincing means of response to it.

A natural way forward drawn from the analysis above would be to attempt to combine the horizon symmetry and modified dispersion relation arguments for the universality of Hawking

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<sup>22</sup>This can be seen explicitly in the quantum gravitational analysis of the Unruh effect mentioned above in (Alkofer, D’Odorico, Saueressig, and Versteegen 2016).

radiation. However, the coherence of such a combined approach is yet to be seen. In particular, the stationarity idealization used in the anomaly cancellation approach is not compatible with a Hawking-style derivation where the (non-stationary) process of the formation of the horizon plays an important role. There is, as yet, no smooth limit in which the original Hawking derivation can be seen to lead to the context in which the anomaly cancellation arguments are based. A significant challenge is to show that anomaly cancellation arguments can be successfully applied to a more realistic model of a collapsing black hole. In particular, there is no existing universality argument or analogue model that deals explicitly with how quantum fluctuations and back-reaction of the horizon, which should dominate the physics of the trans-Planckian modes, could impact the thermality of the Hawking spectrum. If that could be achieved, then it is plausible that a suitably integrated universality argument for Hawking radiation could be established based upon the combination of the modified dispersion relation and horizon symmetry approaches.

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