

Axial acoustic field barrier for fluidic particle manipulation

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An acoustic field barrier integrated within a flow tubing system to achieve high-throughput separation of particles in fluid is reported in this work. We investigate the axial acoustic field of a piezo-tube with an inside diameter 34mm, length 25mm and operating frequency 1.15MHz. Energy concentrates within the tube and leakage at the ends provides a sharp monotonic acoustic pressure field within a fluidic circuit. This process is not the conventional standing wave mechanism; instead the geometry produces a spatially stable filtering action without fouling. This powerful filtering action is confirmed theoretically via a COMSOL simulation and demonstrated experimentally by concentrating suspensions of 5 μ m proteoglycan tracer particles at a flow rate of 20mL/min: The corresponding acoustic contrast factor is 0.243 and trapping force is 11pN. This tube geometry tackles the limitations of microfluidic standing wave based acoustic concentrators, namely complex extraction, low-throughput and distributed focus, by harnessing a stable monotonic field profile.

Keywords: acoustophoresis, acoustic, focussing, microparticle, trapping, piezoelectric, piezo

Acoustic pressure fields offer non-contact manipulation opportunities, with levitation in air receiving attention recently with stable single beam levitation¹, mid-air trapping and control², single axis levitation³ and non-spherical particles in artificial field profiles⁴. Levitation of microparticles in liquids has also emerged within advanced healthcare, biotechnology research, and industrial applications such as cell culturing⁵, early diagnosis of diseases⁶, biomass harvesting⁷ and food quality control⁸. These standing wave pressure fields have high particle concentration efficiency, rapid processing and maintenance of cell viability⁹. The primary advantage is access to physical forces that localise particles at an equilibrium point in a similar fashion as acoustic tweezers¹⁰. The most successful application is miniaturised lab-on-a-chip geometries⁹ with standing wave patterns in submillimetre sized channels¹¹. Particle separation is well controlled for half-wavelength standing wave gaps with two monotonic pressure field profiles straddling a focussing point¹².

Widening standing wave gaps to increase throughput produces polytonic regions (FIG.1.(a)) with distributed focus. This loss of focus and potential de-tune indicates standing waves in larger structures have an Achilles' heel, *i.e.* particles don't move to a single equilibrium point. Whereas living organisms sticking together via acoustic pressure waves improves harvesting^{13,14} and throughput¹⁵. Nevertheless filtration, centrifugation, flocculation, sedimentation¹⁶ remain attractive options.

We present a piezo-tube method to create monotonic pressure profiles with single focussing action (FIG.1.(b)). It patches the Achilles' heel of the standing wave microfluidic filtration devices¹⁷. Here we use the piezo-tube end to pass or capture particle collectives reproducing porous filter or chromatographic medium character¹⁸. COMSOL simulations and tests of proteoglycan accumulation within a monotonic force field are described below.

The piezo-tube is excited by a radio frequency signal and generates a monotonic pressure gradient at its end. The oscillations of the electric field induce the mechanical vibrations in the wall. This energy transfers axially within the adjoining walls between the piezo-tube and adjacent elastomer coupled glass tubes and radially as an internal pressure wave. Energy along the tube walls is governed by the equations of mechanical displacement field \mathbf{U}_S and the electric displacement field \mathbf{D}_{El} :

$$\begin{aligned}\nabla \cdot \mathbf{T}_S &= -\rho_S \omega^2 \mathbf{U}_S \\ \nabla \cdot \mathbf{D}_{El} &= 0\end{aligned}\quad (1)$$

where ρ_S is the mass density of the solid, ω is the angular frequency of the applied voltage and \mathbf{T}_S is the mechanical stress tensor induced within the solid.

In a piezoelectric solid, \mathbf{T}_S and \mathbf{D}_{El} are coupled by the linear piezoelectric constitutive matrix. The stress-charge form of these relations can be expressed as:

$$\begin{bmatrix} \mathbf{T}_S \\ \mathbf{D}_{El} \end{bmatrix} = \begin{bmatrix} c_E & -e^T \\ e & \epsilon_S \end{bmatrix} \begin{bmatrix} \nabla \mathbf{U}_S \\ -\nabla V_S \end{bmatrix}\quad (2)$$

where V_S is the electric potential field within the solid, c_E is the elasticity matrix of the material, e is the electromechanical coupling matrix of the material, and ϵ_S is the electric permittivity matrix of the material. While in a non-piezoelectric material of the flow tubing, the electromechanical coupling matrix e is absent, so the two energy fields can be expressed as:

$$\begin{bmatrix} \mathbf{T}_S \\ \mathbf{D}_{El} \end{bmatrix} = \begin{bmatrix} c_E & 0 \\ 0 & \epsilon_S \end{bmatrix} \begin{bmatrix} \nabla \mathbf{U}_S \\ -\nabla V_S \end{bmatrix}\quad (3)$$

The frequency domain of the acoustic pressure field p_L in the liquid can be expressed by Helmholtz equation:

$$(\nabla^2 + k^2)p_L = 0\quad (4)$$

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where $k = \omega/c_L$ is the angular wave number, and c_L is the velocity of sound in the liquid.

The levitating pressure field in the fluid affects a particle's path: Generally the glass tubes vibrate with a weak non-uniform energy that interferes with the standing wave fields of the piezo-tube. The overall pressure field of the piezo-tube at frequencies where radial vibrations dominate over axial vibrations, leads to negligible end radiation and a sharp pressure gradient of significant force.

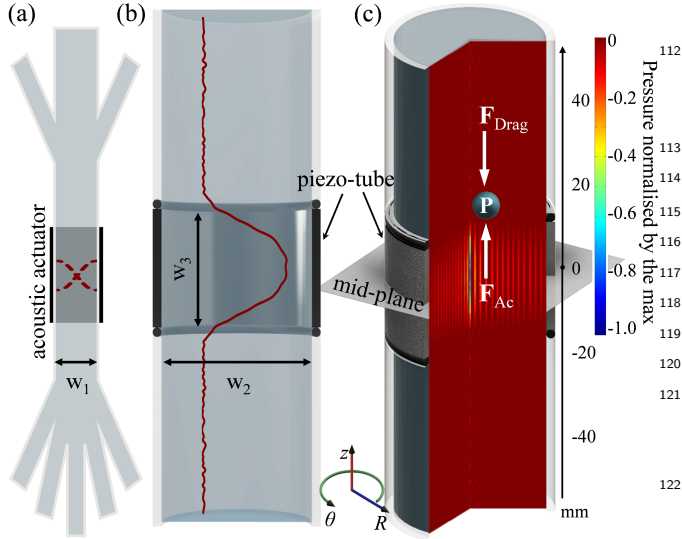


FIG. 1. The pressure gradient profiles in (a) a typical lab on-a-chip acoustic separation setup with multiple inlets and outlets (---), where w_1 is usually hundreds of microns and (b) the reported high-throughput acoustic filter (—), where w_2 and w_3 are 34mm and 25mm respectively. A COMSOL simulation of the axial acoustic pressure distribution is demonstrated on (c). The acoustic pressure field is symmetric about the mid-plane perpendicular to z -axis. It is at its strongest at $z=0$ and decreases along the z -axis to both the positive and negative directions until the pressure approaches a minimum value in liquid within the glass tubes. The tubing geometry is consisted in the sequence of glass tube, O-ring, piezo-tube, O-ring and glass tube.

This z -axis pressure profile is confirmed by a COMSOL simulation: In FIG.1.(c) an axisymmetric model in a cylindrical co-ordinate system is developed. Equations (1), (2), (3) and (4) are solved simultaneously. The pressure field in the liquid is driven by continuity conditions of stress and pressure at the tube inner wall. Plane wave radiation conditions are imposed at the upper and lower walls of the geometry to model energy leakage outside the piezo-tube into the flow tubing system.

The particle forces from the non-periodic monotonic gradient of its ends are determined as follows. If the diameter of the particle, d_P is smaller than the acoustic wavelength, the particle is subject to a time averaged acoustic radiation force \mathbf{F}_{Ac} , according to Gorkov's equation¹⁹ as:

$$\mathbf{F}_{Ac} = -\frac{\pi}{6}d_P^3(0.5f_1\beta_L\nabla \langle p_L^2 \rangle - 0.75f_2\rho_L\nabla \langle v_L^2 \rangle) \quad (5)$$

where β_L and ρ_L are respectively the isothermal compressibility and the mass density of the liquid, v_L is the medium molecular velocity. The coefficients f_1 and f_2 can be defined as functions of the liquid and particle compressibilities and densities respectively^{19,20}:

$$f_1 = 1 - (\beta_P/\beta_L) \quad (6)$$

$$f_2 = \frac{2[(\rho_P/\rho_L) - 1]}{2(\rho_P/\rho_L) + 1}$$

where β_P and ρ_P respectively represent the particle compressibility and mass density

Choice of this equation is based on the necessity to calculate the force based on pressure gradients at discrete locations within the tube. This can be contrasted with conventional standing wave forces which are induced in a spatially periodic 1-D sinusoidal field. Under the influence of such a field, Equation (5) can be simplified²⁰ to:

$$\mathbf{F}_{Ac} = kVE_{Ac}\Phi_{Ac}\sin(2kx) \quad (7)$$

where V is the particle volume and E_{Ac} is the peak energy density dependent on the amplitude of the sinusoidal acoustic pressure field. Φ_{Ac} is the acoustic contrast factor which is a function of the densities and compressibilities of the particle and the liquid (Equation (6)). For a 1-D acoustic field the contrast factor becomes²⁰:

$$\Phi_{Ac} = f_1 + 1.5f_2 \quad (8)$$

Here, the energy density multiplied by a sinusoidal profile gives a force periodicity less than 1mm. Whereas the piezo-tube, with its non-periodic, monotonic acoustic pressure field as predicted by the COMSOL simulation, generates monotonic gradients separated by the piezo-tube length matching the form of Equation (5). This gradient behaviour is consistent with a fraction of acoustic energy leaking out of the ends of the piezo-tube. This profile overlays the underlying radial component of the Bessel field within the fluid volume²¹. This hybrid acoustic force structure supports a particle concentration mode via the tube end geometry as the force determining variable.

The uniqueness of the present work lies in the physics of the tube-end pressure gradient for trapping particles and against a co-linear fluid flow. Whereas the remaining terms involving fluid pressure acting on the particle is based on known physics, *i.e.* the diameter of the particle d_P to the 3rd power, the energy density of the acoustic field E_{Ac} and finally the acoustic contrast factor Φ_{Ac} .

Overall transiting particles experience a significant net force field \mathbf{F}_{Total} , which is a vector sum of the acoustic radiation force \mathbf{F}_{Ac} upwards and the Stokes' drag force \mathbf{F}_{Drag} downwards due to the flow rate \mathbf{u}_L , *i.e.*:

$$\begin{aligned}\mathbf{F}_{Total} &= \mathbf{F}_{Ac} + \mathbf{F}_{Drag} \\ \mathbf{F}_{Drag} &= 3\pi\eta_L d_P \mathbf{u}_L\end{aligned}\quad (9)$$

where η_L is the dynamic viscosity of the liquid.

Thus particle paths resulting in concentration or leakage processes, is significantly influenced by the field \mathbf{F}_{Total} which needs to exceed zero to concentrate particles. For flow rates sufficiently strong or for weak acoustic powers, \mathbf{F}_{Drag} dominates over \mathbf{F}_{Ac} and the particles flow along without being manipulated. As one keeps increasing the particle diameter or power, the acoustic trapping forces increase more strongly (cubic scaling) than the fluid flow-induced drag forces (linear scaling). Hence for a given acoustic wave power and a fluid flow rate, one would have a critical particle diameter below which the acoustic forces are too weak to trap particles against the drag forces.

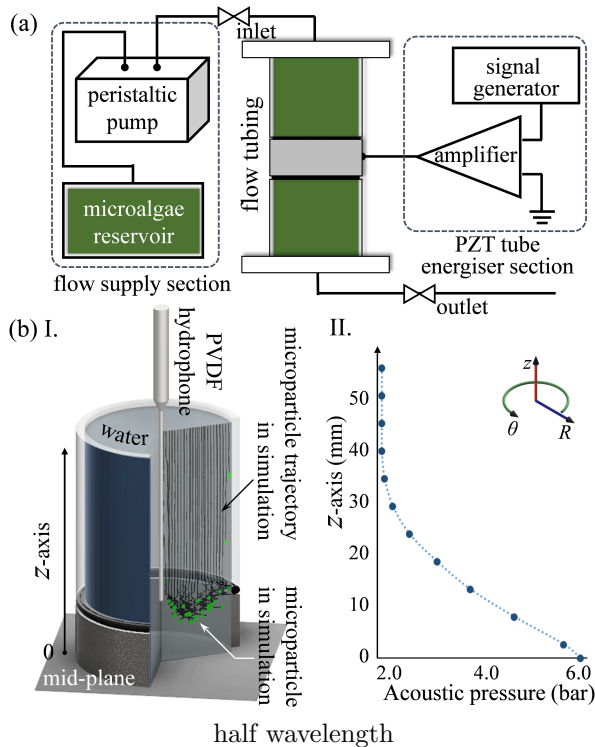


FIG. 2. (a) The high-throughput particle concentration experimental setup: Acoustic filter configuration based on a flow tubing system with passive/active tubes, piezo-tube energiser section and a flow supply system. (b) A COMSOL simulation predicts particle (\bullet) trajectory (—) in a flow tubing system coming to a halt near the piezo-tube entrance (I). A PVDF hydrophone placed between active and passive tubes helps confirm the pressure variations of the barrier plane (II).

Also some permeability/leakage is anticipated as there

TABLE I. A comparison list of density ρ_P , compressibility β_P ²², acoustic contrast factor Φ_{Ac} and the maximum acoustic force $|\mathbf{F}_{Ac}|_{max}$ of selected particles. $|\mathbf{F}_{Ac}|_{max}$ is calculated assuming the particle with a unit size, *i.e.* 1 μ m, in an acoustic field introduced by a piezo-tube energised with 30V_{pp} input at approximately 1.15MHz. $|\mathbf{F}_{Ac}|_{max}$ can be scaled as a function of the particle sizes by multiplying d_P^3 .

particle	ρ_P kg/m ³	β_P Pa ⁻¹	Φ_{Ac}	$ \mathbf{F}_{Ac} _{max}$ ^a pN
Microphyte ²²	1100	3.83×10^{-10}	0.243	0.088
WBC ²³ ^b	1090	3.59×10^{-10}	0.287	0.119
Fused silica ²⁴	2210	1.00×10^{-11}	1.648	0.577
Polystyrene ²⁵	1050	2.49×10^{-10}	0.495	0.263
Gold ²⁶	19300	5.56×10^{-12}	2.374	0.584

^a COMSOL predicted numbers

^b White blood cell

are loci where the axial trapping force can vanish. These permeable regions are expected to occur along inner cylindrical planes representing the pressure nodes of the field.

Concentration or leakage is also dependent on particle contrast factors when suspended in water as shown in TABLE I. This presents the estimated traction forces in the centre of the tubular geometry according to particle type. This demonstrates dense rigid particles such as gold and fused silica are entrained by significantly higher forces, whilst biological cells have the least effect. Distinguishing from standing waves, it is important to note the axial forces are not periodic along the fluid flow direction. This results in an advantageous single concentration phase.

Particle flow rate, according to Poiseuille/laminar flow (Reynolds number for the flow rate and tube ID used in this work is 12.482), is expected to vary from the centre to the edge. At the centre it is likely to be flowing faster but also working against a stronger field (Bessel function distribution), hence there is a degree of compatibility between the flow rate and force field distribution. Overall choice of different particles of β_P , ρ_P result in different Φ_{Ac} , together with d_P lead to a variation in the \mathbf{F}_{Ac} . The larger the $|\mathbf{F}_{Ac}|$ is, the easier it is to manipulate the particle. TABLE. I indicates that biological cells suspended in water are the most difficult particle to capture with acoustic waves, hence for our initial experiments we have selected a biological particle; microphyte as the most challenging test for the system.

An experimental setup for demonstrating the anticipated field-particle coupling of a suspension comprising proteoglycan tracer particles (microphytes d_P of 5 μ m) is shown in FIG.2.(a). The flow tubing geometry consists of a piezo-tube with an OD 38mm, ID 34mm and height 25mm (APC International *Ltd.*, Type I) co-linear with two 40mm glass tubes of the same OD and ID positioned above and below. To minimise acoustic transmis-

208 sion an O-ring is inserted between adjoining active and 266
 209 passive tubes. The outer ends of the glass tubes are sand-267
 210 wiched between two customised acrylic sheets with liquid-268
 211 inlet (top) and outlet (bottom) respectively. A sinusoidal-269
 212 signal from the signal generator (Agilent 33120A Func-270
 213 tion/Arbitrary Waveform Generator) drives the piezo-271
 214 tube at its radial mode resonant frequency and ampli-272
 215 fied by a power amplifier (EIN 310L) to approximately-273
 216 $30V_{pp}$. The flow of the particle suspension is driven by-274
 217 a peristaltic pump (Masterflex). The glass tubes allow-275
 218 visualisation of the particle concentration effect. 276

219 These demonstration experiments are setup to col-277
 220 lect acoustic and optical data from the tubes via a hy-278
 221 drophone and camera respectively: For measuring the-279
 222 pressure field a PVDF hydrophone (Dr Mueller Instru-280
 223 ments, Müller-Platte Needle Probe) was placed at the-281
 224 tubes axial centre (FIG.2.(b).I.) and the sampled signal-282
 225 amplified by a voltage amplifier (Dr Mueller Instruments, 283
 226 MVA 10). The result is displayed on an oscilloscope-284
 227 (Hantek, DSO5102P) revealing the corresponding plot-285
 228 shown in FIG.2.(b).II. and confirming the acoustic pres-286
 229 sure falls significantly outside the piezo-tube. 287

230 Under the same conditions we pass the tracer parti-288
 231 cle suspension through the energised piezo-tube to get-289
 232 the concentration effect. Of note is the pumps flow rate, 290
 233 which is significantly greater than typical lab-on-chip de-291
 234 vice process by 1000 to 10000 times *i.e.* at 20mL/min. 292
 235 As the tube shape and depth prevent straightforward-293
 236 concentration measurements, the signature chromatic co-294
 237 ordinate (Sg_{cc}) technique was chosen based on its suc-295
 238 cess with assessing green foliage levels from satellite-296
 239 images^{27,28} and the potential to profile a smaller photo-297
 240 synthetic system. Here the Sg_{cc} carries the RGB colour-298
 241 information of an image correlated with the concentra-299
 242 tion process. A 75s video is converted into an image se-300
 243 quence; and a consistent region of interest (ROI) is anal-301
 244 ysed frame by frame. The RGB information is recorded-302
 245 and the Sg_{cc} is calculated, ratioing the signature colour-303
 246 digit number over the sum of the red, green and blue-304
 247 digit numbers. The green colour is the most represen-305
 248 tative parameter, as long as the lighting levels remain-306
 249 fixed. 307

250 At this stage we observe a concentration effect which-308
 251 agrees with the form of the theoretical prediction, 309
 252 thus making it a suitable candidate geometry for high-310
 253 throughput solid-liquid separation. A detailed COMSOL-311
 254 simulation also confirms the trajectory of microparticles-312
 255 in the flow tubing, which shows the same accumulation-313
 256 behaviour of the particles at the entrance of the piezo-314
 257 tube as expected (FIG.2.(b).I). 315

258 Particle concentration and other motional effects were-316
 259 also observed: Particles influenced by the piezo-tube in-317
 260 either on-state or off-state is presented in FIG.3.(a). This-318
 261 shows the on-state creates a particle concentration ef-319
 262 fect as indicated by the relative concentrations via ROI-320
 263 Sg_{cc} data collected from a vertically oriented tube with-321
 264 downward flow. Here frames are taken of four quad-322
 265 rants: above and below an active tube, above and be-323

low an inactive tube (referred as on_above, on_below, 324
 325 off_above and off_below). Interpreting FIG.3.(b), there 326
 327 is a slight difference between baselines relating to small 328
 329 background differences in the first few frames. For the 330
 331 off-state as time progresses, the green and brown dashed 332
 333 lines indicate matching contrast above and below the 334
 335 tube. Whereas the on-state results in an increasing dif- 336
 337 ference: The solid green line confirms that the particles 338
 339 accumulate above the piezo-tube, *i.e.* unable to enter 340
 341 the piezo-tube. Around frame 40 a minor leakage is visi- 342
 343 ble, which indicates partial percolation of tracer particles 344
 345 through the field.

346 Leakage and streaming were minor relative to the trap- 347
 348 ping effect observed. For the former permeability of the 349
 350 field is associated with particle trajectories along the ra- 351
 352 dial nodal planes, where the axial forces are weak. We 353
 354 hypothesise that the leakage is encouraged when the axial 355
 356 radiation pressure depletes along the nodal planes. As a 357
 358 result, we expect the leakage to be positively correlated 359
 360 to the number of the radial modes, although no tests 361
 362 were done to confirm this. However it was observed that 363
 364 leakage operates uniformly over the width, but is difficult 365
 366 to quantify due to agglomeration effects. Outside of the 367
 368 tube, streaming had minimal contribution to the motion 369
 370 of either entrant or leaked particles. From the gradient 371
 372 of the ROI Sg_{cc} the accumulation rate in the active tube 373
 374 beyond frame 70 (where the count is most accurate) is 375
 376 doubled, further confirming the trapping effect.

377 We believe this is the first demonstration of a particle 378
 379 trajectory arrested by an acoustic barrier derived from a 380
 381 large scale monotonic field. The sample flowing within 382
 383 this tubing system is subject to a dominant localising 384
 385 effect, where it concentrates at a significant volume and 386
 387 flow rate of 20mL/min alongside the supernatant phase. 388
 389 These experiments demonstrate that low contrast bio- 390
 391 particles can be filtered, the most challenging case, which 392
 393 bodes well for entities of higher contrast. A clear focal 394
 395 point is produced at the tube end. We no longer need 396
 397 to depend on the characteristics of the standing wave 398
 399 alone, which can become problematic at small scales and 400
 401 high frequencies as the particle distorts the wavefront and 402
 403 leads to tuning variabilities.

404 The membrane like filter action is the most promi- 405
 406 nent characteristic of the profile leading to an accessible 407
 408 accumulation which is relatively straightforward to tap. 409
 410 Batch type fluidic operations can immediately be applied 411
 412 and is amenable for series or parallel operation, with the 413
 414 opportunity to boost very low concentrations.

415 Applications include plant cell collection, animal cell 416
 417 purification, bioreactor systems, geological separations, 418
 419 agricultural processing and sensing enhancement due to 420
 421 the concentration factor. The approach is especially use- 422
 423 ful for particles with high acoustic contrast. Here high 424
 425 throughput retrofitted systems benefit from less tuning 426
 427 than standing wave approaches. Thus it can work within 428
 429 micro- or macro-liquid processing systems and support 430
 431 low maintenance, non-clogging and low power applica- 432
 433 tions. These are powerful foundations for processing bio-

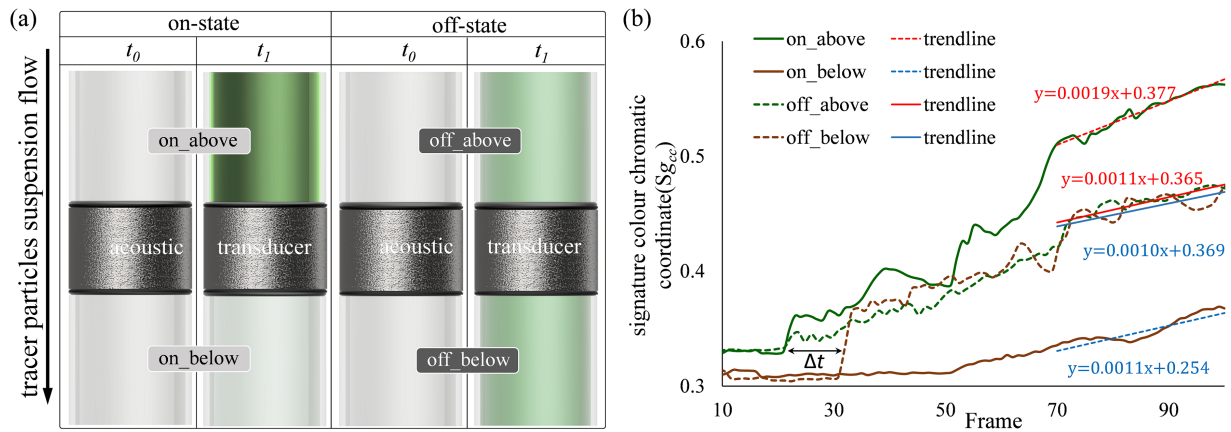


FIG. 3. Visualisation of the filtration action for a tracer particle suspension: Two sets of experiments are utilised, one with the acoustic transducer active (on-state) and the other with it idle (off-state). (a) Images taken at initial t_0 and endpoint t_1 (after 60s) show the on-state inhibits particle flow, against a fluid flow of 20mL/min. (b) Video frames capture an image sequence for dynamics of the filtration process, with relative concentration obtained from RGB digit numbers of the selected ROI. The number of frames for the tracer particle to transit the acoustic transducer is indicated by Δt . In the off-state, the marginal difference between the green and brown dashed lines indicates no particle trapping. Whereas, in the on-state, increasing differences between green and brown solid lines indicate a particle concentration effect.

- 324 ological molecules including protein and DNA and live³⁶⁴
 325 cells where high-throughput sorting is available to meet³⁶⁵
 326 industrial scale throughput requirements.³⁶⁶
 327
 328 The authors gratefully acknowledge funding from the³⁶⁷
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 330 Dr Devaki Bhatta and Dr William Nock for the helpful³⁶⁹
 331 discussions.³⁷⁰
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