PHYSICAL REVIEW B 99, 041402(R) (2019)

Rapid Communications

Editors' Suggestion

Bulk properties of the van der Waals hard ferromagnet VI₃

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(Received 13 November 2018; revised manuscript received 28 November 2018; published 7 January 2019)

We present comprehensive measurements of the structural, magnetic, and electronic properties of layered van der Waals ferromagnet VI_3 down to low temperatures. Despite belonging to a well-studied family of transition-metal trihalides, this material has received very little attention. We outline, from high-resolution powder x-ray diffraction measurements, a corrected room-temperature crystal structure to that previously proposed and uncover a structural transition at 79 K, also seen in the heat capacity. Magnetization measurements confirm VI_3 to be a hard ferromagnet (9.1 kOe coercive field at 2 K) with a high degree of anisotropy, and the pressure dependence of the magnetic properties provide evidence for the two-dimensional nature of the magnetic order. Optical and electrical transport measurements show this material to be an insulator with an optical band gap of 0.67 eV—the previous theoretical predictions of d-band metallicity then lead us to believe VI_3 to be a correlated Mott insulator. Our latest band-structure calculations support this picture and show good agreement with the experimental data. We suggest VI_3 to host great potential in the thriving field of low-dimensional magnetism and functional materials, together with opportunities to study and make use of low-dimensional Mott physics.

DOI: 10.1103/PhysRevB.99.041402

I. INTRODUCTION

Two-dimensional van-der-Waals (vdW) magnetic materials have in recent years become the subject of a wide range of intense research [1]. While a large portion of research into two-dimensional materials has centered on graphene, the addition of magnetism into such a system leads to many interesting fundamental questions and opportunities for device applications [2–6]. Particularly for future spintronics applications, semiconducting or metallic materials which exhibit ferromagnetism down to monolayer thickness are an essential ingredient. This has led to a large volume of recent publications on two-dimensional honeycomb ferromagnet CrI₃ [7–12]. CrI₃ and VI₃ belong to a wider family of MX₃ transition metal trihalides with X = Cl, Br, I, which were synthesized in the '60s [13,14] but have since seen little interest until recently [15].

 VI_3 is an insulating two-dimensional ferromagnet with a Curie temperature, T_c , given as 55 K and reported to have the layered crystal structure of BiI₃ with space group R3 [16–18]. As shown in a recent review [15], there is very little available information on VI_3 other than the structure and the expected

S=1 from the $3d^2$ configuration of the vanadium sites. Calculations using density functional theory, which additionally yield the exchange constants, have suggested VI₃ to not only remain ferromagnetic down to a single crystalline layer, but to also exhibit Dirac half-metallicity, of interest for spintronic applications [19].

In these vdW materials, hydrostatic pressure forms an extremely powerful tuning parameter. Given the weak mechanical forces between the crystal planes, the application of pressure will dominantly have the effect of pressing the *ab* planes together, and gradually and controllably push the system from two- to three-dimensionality. Additionally, first-principles calculations have suggested in-plane strain and compression to stabilize both antiferromagnetic phases and spin reorientation in CrI₃ [20] and both VBr₃ and VCl₃ are antiferromagnetic [18].

II. RESULTS

A. Crystal structure

Finding the correct crystal structure is crucial for accurate *ab initio* calculations of a new material's behavior and for general insight into its properties. The structure of VI₃ has not been previously outlined beyond its basic crystallographic family [13,16,18,21]. This earlier work assigned VI₃

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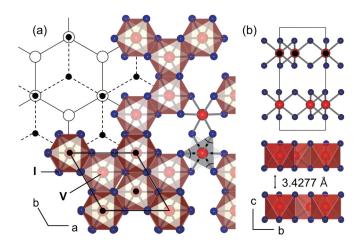


FIG. 1. Views of the room-temperature crystal structure of VI_3 along (a) the c axis and (b) the a axis. Additional projections are shown in the SM (Figs. S4 and S5).

as belonging to the BiI_3 type R3 structure, but no detailed crystallographic results are available nor any description of temperature dependence. Here we present the crystal structure of VI_3 from refined powder x-ray diffraction data and find a transition to an alternative structure at low temperature.

The results show good agreement between the high-resolution x-ray diffraction (HR-XRD) measurement and refined data (see Supplementary Material (SM) [22], Figs. S2-S5 and Table S1. The FULLPROF, GSAS-II, and VESTA software suites were employed [23–25]). Contrary to previous reports, we find the room temperature structure to be fitted better with the space group of P31c than R3. Even though both structures show very similar simulation results, several peaks were missing from the R3 simulations, and peak shapes and ratios are better fit by the P31c (SM, Fig. S3). The P31c structure at room temperature is shown in Fig. 1. The unit cell has an ideal honeycomb bilayer of V formed of $[VI_6]^{3-}$ octahedra, separated by a clear van der Waals gap. All the shortest V-V and V-I bonds have the same lengths.

Following the powder-diffraction patterns down to low temperature additionally reveals a phase transition to a new low-temperature structure below $T_{\rm s}=79.0(5)$ K. Figures 2(a) and 2(b) show heat capacity and details of the x-ray diffraction patterns as a function of temperature. A clear peak at 79 K in the heat capacity and the peak splitting in the XRD patterns demonstrate the existence of a sharp structural phase transition at this temperature.

As one can see from the long debates about the low-temperature structure of α -TiCl₃ [26], the overlap of many peaks via symmetry breaking at low temperature gives multiple potential solutions to the structure. Among the possible candidates, we obtained the best results for a C2/c structure, a subspace group of the room temperature structure. Contrary to MoCl₃ [27] and α -TiCl₃ [15] undergoing dimerization of the transition metal ions at low temperature, the V atoms here stretch in a single direction from their perfect honeycomb—antidimerization [see Fig. 2(c)]. The short bonding length is 3.92(5) Å and the long 4.12(11) Å. Furthermore, accompanying the antidimerization of V honeycomb atoms, the VI₆ octahedra experience an off-center distortion when the low-

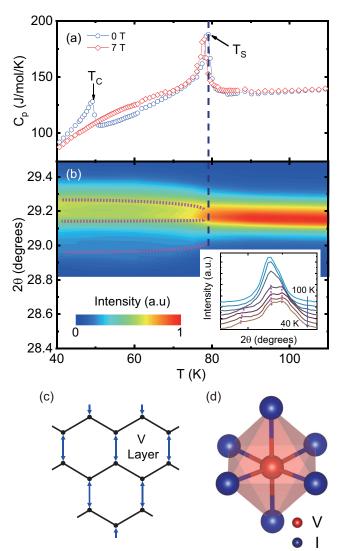


FIG. 2. (a) Heat capacity of a VI₃ single crystal, in 0 and 7 T fields. The structural transition at $T_{\rm s}=79~{\rm K}$ is unaffected by magnetic field, unlike the ferromagnetic transition at $T_{\rm c}=50~{\rm K}$. (b) Detail of temperature–dependent x-ray powder diffraction patterns showing peak splitting at $T_{\rm s}$. (c), (d) Illustrations of the antidimerization of the V sites and the distortion of the VI₆ octahedra in the low-temperature phase.

temperature structure is entered. Figure 2(d) illustrates the structural deformation of the VI_6 octahedra at low temperature. Plots of the refinement results and structural parameters at 40 and 300 K are given in the SM (Figs. S2 and S3, Table S1).

The peak seen in the heat capacity at 50 K (T_c) we identify as the ferromagnetic transition from the broadening of peak width in an applied 7 T of magnetic field. All measurements were reproducible over multiple thermal cycles, which rules out the effect of sample degradation on the results. Like other transition-metal halides with vdW gaps such as CrI₃ and α -RuCl₃, VI₃ is easily exfoliated by the common Scotch tape method [28] (SM, Fig. S7), placing it as a valuable system for studying two-dimensional physics and applications.

B. Magnetic properties

We next explore the magnetic properties of single crystal VI₃. The results of measurements are shown in Fig. 3 and additional data given in the SM (Fig. S6). Measurements were carried out with the magnetic field both parallel and perpendicular to the crystallographic *c* axis, which is easily identified as perpendicular to the *ab* crystal planes this two-dimensional material forms. Orientation-dependent magnetic susceptibility is shown in Fig. 3(a), measured during warming after cooling to 2 K with the measurement magnetic field of 100 Oe applied, i.e., field-cooled (FC). Similarly to the previous result of Wilson *et al.* [18] we find VI₃ to be ferromagnetic with T_c of 50.0(1) K, defined from the derivative of the susceptibility.

As shown in Fig. 3(a), there is a strong anisotropy in the susceptibility—magnetic field applied in-plane $(H \perp c)$ leads to magnetization roughly half that found when it is applied out of plane $(H \parallel c)$. We can conclude that VI₃ has Ising-type spins with the easy axis along c. A small kink in the magnetic susceptibility as well as a change in slope in the paramagnetic state at 79.3 K was observed, corresponding to the structural transition temperature T_s . A structural-phase transition accompanies similar features in the susceptibility of CrI₃ and α -TiCl₃ [7,29]. The kink was not seen when the field was applied in-plane, but was clearly present with the field along the easy axis, implying the coupling of the structural phase transition and the magnetism and a link to the magnetic anisotropy.

Zero-FC data are presented in the SM (Fig. S6)—a linear Curie-Weiss fit to these data above T_s allows us to extract an effective moment $\mu_{\rm eff} = 2.08(20)~\mu_B$. Wilson *et al.* reported a value of $2.22~\mu_B$, which agrees with our fit within error, and our *ab initio* calculations (SM) give a moment of $2~\mu_B$. The extrapolated Curie temperature from the fit is 64.5(5) K, which differs from the observed T_c as the structural transition at T_s alters the slope of the susceptibility and destabilizes magnetic order.

The effect of applied hydrostatic pressure on the FC susceptibility in a 1000 Oe field applied along c is shown in Fig. 3(b). Along with the evolution of several bumps in the data, most likely due to domain dynamics, the key result shown in the inset is the behavior of T_c . The effect of pressure on a vdW material such as VI₃ will be predominately to continuously decrease interlayer spacing, increasing interplanar exchange and tuning toward a three-dimensional system. At pressures up to around 7 kbar, however, no change in T_c was observed, but at higher pressures it begins to rapidly increase. We interpret this as evidence of the true two-dimensional nature of the magnetic order in VI₃. Bringing the planes closer together has zero effect on stabilizing the magnetic order to higher temperatures-interplanar interactions are unaffected and hence are presumed to be negligible to begin with. Only above 8 kbar does changing interlayer spacing lead to easier formation of magnetic order—at this point, the dimensionality is starting to tune away from two. The only prior pressure study, to our knowledge, on the MX₃ materials to date is the work of Yoshida et al. [30], which reports a continuous decrease in the value of T_c with increasing pressure—the opposite effect to our observations.

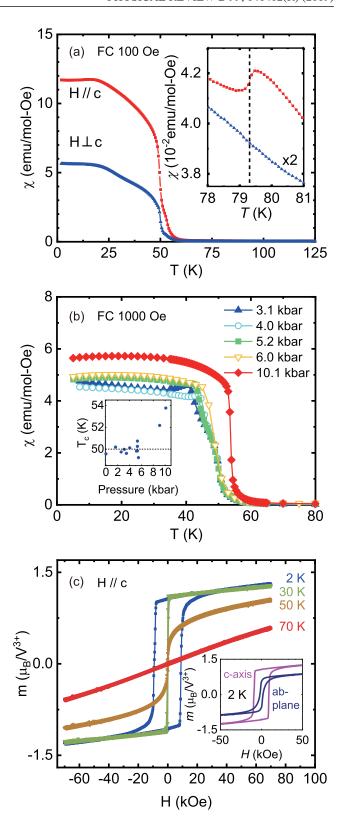


FIG. 3. (a) Field-cooled magnetic susceptibility of VI₃ with applied 100 Oe field parallel and perpendicular to the crystallographic c axis. Inset shows detail around $T_{\rm s}$, where a kink is visible in the data taken with field along c. (b) Pressure dependence of the field-cooled data, measured with 1000 Oe along the c direction. Inset shows extracted values of $T_{\rm c}$. (c) Field-dependent ionic magnetic moment, showing clear ferromagnetic hysteresis loops below $T_{\rm c}$ —inset shows the orientation dependence at 2 K.

Characteristic ferromagnetic hysteresis loops of the magnetic moment with applied field along the c axis are shown in Fig. 3(c) for several temperatures (more in the SM). As temperature is increased, the coercive field is exponentially decreased (SM, Fig. S6) and above T_c the hysteresis loops close and the system reverts to paramagnetic linear behavior. At the maximum applied field of 70 kOe (7 T) and at 2 K, the magnetic moment was found to be $1.3(1) \, \mu_B/f.u.$, which is smaller than the expected saturated moment of a V^{3+} ion, $gS = 2\mu_B/f.u.$ The moment is not fully saturated at 70 kOe, but clearly cannot reach this predicted value. The reason for this disagreement is not currently clear.

The orientation dependence of the magnetization is illustrated in the inset of Fig. 3(c). The field-in-plane curves show coercivity of 1.8 kOe, smaller than that of out-of-plane (9.1 kOe), which again suggests the easy axis to lie along the c axis, from the Stoner-Wohlfarth model [31]. This simple model, it should be noted, while offering valuable insight into the overall behavior strictly applies only to a singledomain crystal—more complex treatments [32] may prove more suitable for these data going forward. One thing to note here is its huge coercive field at 2 K-9.1 kOe, in contrast to other vdW ferromagnets such as CrBr₃ [33], CrI₃ [7], Fe₃GeTe₂ [34], and Cr₂Ge₂Te₆ [35]. To our knowledge, all other such ferromagnets are soft, contrary to this hard vdW ferromagnet VI₃. Understanding the physical origin of the hard-ferromagnetic behavior and the comparison of otherwise similar systems VI₃ and CrI₃ forms a rich opportunity for low-dimensional magnetism going forward and may help in designing future magnetic materials for specific applications. Interestingly, Chang et al. [36] reported in their comparison of V- and Cr-doped Sb₂Te₃ that the V-doped samples show much higher coercive fields than the Cr-doped systems. The Stoner-Wohlfarth model describes that a small saturated moment, M_S , and/or a large total magnetic anisotropy K lead to larger coercive fields. The smaller saturated moment in V³⁺ driven by the smaller number of d-orbital spin and the larger anisotropy coming from the partially filled t_{2g} d-band of the V³⁺ ion, unlike the fully filled Cr³⁺ orbitals, could contribute the large anisotropy, and, in turn, coercive field.

C. Electronic properties

To investigate the electronic properties, we measured the band gap by optical transmittance and the temperature dependence of the bulk resistivity. Figure 4(a) shows the transmittance at room temperature as a function of incident photon energy, from which we can extract the optical band gap. The dependence of the absorption coefficient α on incident photon energy is given by the expression $\alpha E \propto (E-E_g)^m$, where $E=h\nu$ is the incident photon energy, E_g is the optical band gap, and for a direct allowed transition the exponent can be taken as m=1/2. For $E < E_g$, the material cannot absorb photons so the band gap is found from extrapolating $(\alpha h \nu)^2$ vs $h\nu$ to zero (inset). The obtained direct optical band-gap value for VI₃ was 0.67(1) eV.

The temperature dependence of the in-plane resistivity, ρ , of a bulk single crystal of VI₃ is plotted in Fig. 4(b) from room temperature down to the point where the resistance becomes too high to measure on our setup. The increasing resistivity as

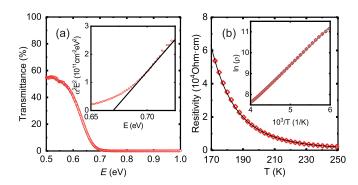


FIG. 4. (a) Optical transmittance of VI_3 at room temperature with inset showing the accompanying Tauc plot and linear fit to extract the optical band gap. (b) Resistivity, with good agreement to the Arrhenius insulating temperature dependence shown in the inset.

temperature was lowered shows clear insulating behavior. The resistivity can be fitted well by an Arrhenius type exponential function: $\rho \propto e^{E_a/k_BT}$, where E_a is the activation energy and k_B Boltzmann's constant. The inset illustrates the standard $\ln(\rho)$ vs 1/T plot—the straight line proves good agreement to Arrhenius-type thermally activated transport. The extracted activation energy E_a was 0.16 eV, giving an electrical band gap of 0.32 eV—significantly smaller than the measured optical band gap. The reason for this (common) mismatch is not immediately clear in this material; a potential explanation is the presence of some form of impurity band within the gap or denaturing of the surface contact—iodine deficiency or the effect of exposure to oxygen or moisture may be possible candidates.

Sister compound CrI_3 is a Mott insulator [7], with all the rich electronic correlation that implies. Previous results from *ab initio* calculations [19] predict VI_3 to be metallic, rather than the observed insulating behavior—giving a hint that VI_3 is also a Mott-insulating system. Our band structure calculations (SM, Fig. S1) implemented in the Quantum ESPRESSO package [37–42], which use our updated crystal structure parameters and include the effects of a Hubbard U, suggest a ground state that is indeed Mott insulating, rather than metallic, with a \sim 1 eV band gap in good agreement with observed data. Reducing the on-site Coulomb interaction leads to half metallicity in our calculations.

III. DISCUSSION

We have presented an overview of the basic properties of near-unexplored van der Waals ferromagnet VI₃. We suggest an updated crystal structure—crucial for accurate *ab initio* calculations—and a transition into a distorted alternative structure at low temperature. A key result is a coercive field far higher than in any other vdW ferromagnet system, setting VI₃ apart as a hard vdW ferromagnet and raising several questions worthy of further exploration. Optical and electrical transport measurements show this material to be an insulator with an optical band gap of 0.67 eV. In contrast to previously published studies, our band-structure calculations yield an insulating ferromagnetic ground state when an on-site Coulomb interaction is included, leading us to believe VI₃ to be a correlated Mott insulator. This evidence of Mott physics evokes potential for band-gap tuning and the emergence of

exotic states due to strong electron correlations in this 2D ferromagnetic system.

ACKNOWLEDGMENTS

The authors would like to thank Sanghyun Lee, S. E. Dutton, Inho Hwang, and Y. Noda for their generous help and discussions. We would also like to acknowledge support from Jesus College of the University of Cambridge, IHT Kazatomprom, and the CHT Uzbekistan Programme.

The work was carried out with financial support from the Ministry of Education and Science of the Russian Federation in the framework of Increase Competitiveness Program of NUST MISiS (No. K2-2017-024). The work of D.Kh. was supported by the German research Project No. SFB 1238 and by Köln University via the German Excellence Initiative. This work was supported by the van der Waals Materials Research Center NRF-2017R1A5A1014862 and the Institute for Basic Science of the Republic of Korea (Grant No. IBS-R009-G1).

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