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Scaling Relationships of Gas-Solid Spouted Beds

Jian Xu[*]   Ye Ji[†]   Weisheng Wei[‡]

Xiaojun Bao[**]   Wei Du[††]

[*]China University of Petroleum, xujian@cup.edu.cn

[†]China University of Petroleum

[‡]China University of Petroleum

[**]China University of Petroleum, baoxj@cup.edu.cn

[††]China University of Petroleum

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Jian Xu, Ye Ji, Weisheng Wei, Xiaojun Bao[*], Wei Du
The Key Laboratory of Catalysis, China National Petroleum Co.,
China University of Petroleum, Beijing 102249, China
Corresponding author. Email:baoxj@cup.edu.cn. Fax: (8610)89734979.

ABSTRACT

An additional parameter, the particle-particle coefficient of restitution was added to the scaling relationship of spouted beds proposed by He et al. ([4]) by granular kinetic theory analysis of the particle movements in both spout and annulus regions. The experimental verification was conducted in two spouted beds with 80 and 120 mm ID. It has been found that good similarity could not be obtained when the coefficients of restitution were not matched.

INTRODUCTION

Spouted bed technology has been widely used for a variety of applications, such as drying, coating, granulation, and chemical reactors ([1]). Although many equations based on small-scale spouted beds (D_c < 0.3 m), most of which were operating at ambient conditions, are available for predicting the hydrodynamic properties of spouted beds, the information on large scale vessels, especially those operating at elevated temperature and pressure, is inadequate ([2]). Therefore, scaling-up studies of spouted beds are of great importance.

The most straightforward method to derive the correct scaling relationships is the nondimensionalization of the governing equations. The scaling relationships for spouted bed were developed based on scaling relationship proposed by Glicksman ([3]) for fluidized beds. By analysis of the force balance on particles in the annulus region of a spouted bed, He et al. ([4]) added two dimensionless parameters, the internal friction angle (φ) and the loose packed voidage (ε_0), to the scaling relationship of Glicksman ([3]). Their experimental verifications conducted in columns of different sizes at atmospheric and elevated temperatures and pressures demonstrated that the full set of modified scaling parameters are valid for spouted beds when all dimensionless parameters are matched between a prototype and a model bed. For the scaling relationship of a two-dimensional spouted bed, Costa and Tarano ([5]) found that the parameters of Glicksman ([3]) were adaptable. For the scaling relationship of a rectangular spouted bed with a draft tube, Shirvanian and Calo ([6]) added two parameters, the coefficient of restitution and internal friction angle, to the parameters of Glicksman ([3]) to account for the effect of particle-particle interactions.

However, in the scale-up study of He et al. (4), only considering the motion of the
particles in annulus is inadequate, because the flow in the spout region is also
significantly different from that in a fluidized bed. The flow of gas and particle phases
in the spout zone is dominated by gas turbulence and particle-particle collisions.
Therefore, the effective stress tensor relationships for both the spout region and the
annulus region should be taken into account. It has been found that the granular
kinetic theory was suitable for describing the particle-particle stresses in spouted
beds, e.g. (7, 8). In the present study, a new scaling relationship of spouted beds
was proposed and was experimentally verified with the data obtained in two spouted
beds.

SCALING RELATIONSHIP FOR SPOUTED BED

By nondimensionalizing the continuity and momentum equations for the fluid and
solid phases along with the boundary conditions, together with the consideration of
the stress tensor by using the kinetic theory of granular flow, the full set of the
scaling parameters were obtained as follows. The derivation detail was not
presented in this paper due to the space limitation, see (4, 7-8) for reference.

$$\begin{cases} \dfrac{gd_p}{U^2}, \dfrac{\rho_s d_p U}{\mu}, \dfrac{\rho_g}{\rho_s}, \dfrac{H}{d_p}, \dfrac{D_c}{d_p}, \phi_s, \varphi, \varepsilon_0, e_{ss}, \text{dimensionless particle} \\ \text{size distribution, and dimensionless bed geometry} \end{cases} \tag{1}$$

Comparing Eq. (1) with the scaling relationship of He et al. (4) shows that an
additional parameter, the coefficient of restitution of particles, e_{ss}, is introduced in the
present study. It is well known that e_{ss} is a measure of the elasticity of the collision
between two particles, and relates to how much of the kinetic energy of the colliding
particles before the collision remains after the collision. It has been shown that the
flow dynamics of gas-solids systems, such as the bed expansion ratio, particle
velocities were sensitive to e_{ss} (9). Huilin et al. (7) and Du et al. (8) showed that e_{ss}
could greatly affect the CFD simulation results of the spouted beds. However, in their
validation experiments, the particles used in different cases by He et al. (4) are same
or have close e_{ss}, the possible effect of e_{ss} on the scaling of spouted bed is therefore
undetectable.

VALIDATION OF THE SCALING RELATIONSHIP

Figure 1 is a schematic of the experimental setup. The spouted beds studied were
two plexiglass cylindrical columns with conical steel bases. The internal diameters of
the cylindrical sections are 120 mm and 80 mm, respectively, and both are 2.0 m in
height. The conical bases have an internal angle of 60º. Two gas orifices with
diameters of 10 and 6.7 mm were used. The two columns are in geometrical
similarity. On the top of each column, a pressure valve is installed to pressurize the
system to the desired pressure. Length rules are blazed on the outside of the
columns to measure the bed height and the fountain height.

Air, as spouting gas, was provided by an air compressor, controlled by a pressure
regulator and measured by rotameters. Narrow size-distributed alumina and silica
gel particles were used as bed materials. Their properties can be found in Table 1.
The coefficients of restitution were measured by the method of Zhang and Vu-Quoc
(10). In this method, a particle in a closed box was freely dropped at height H_0 and

its rebounding height H_1 is recorded by a high speed video camera, then the
coefficient of restitution can be determined by $e_{ss} = \left(H_1 / H_0 \right)^{1/2}$. It should be noted
that the close box in this measurement is not vacuum. Since additional forces, such
as the drag force should be accounted for in order to get the true coefficient of
restitution, the e_{ss} measured in this study can rather be served as a relative
comparison of the coefficient of restitution of different particles. Bed voidage was
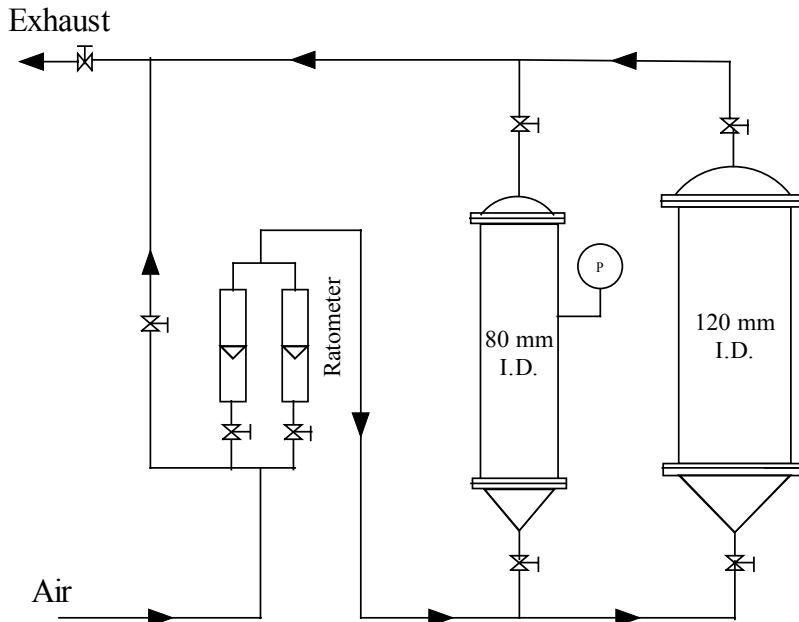measured by an optical fiber system.

Fig. 1. Schematic of experimental setup

To verify the new scaling relationships proposed in the present investigation, several
cases were designed. Test conditions are listed in Table 1, the gas is air in all the
cases. Case A was conducted in the 120 mm column with 1.5 mm silica gel particles
spouted at ambient conditions; Case C is conducted in the 80 mm column with 0.96
mm silica gel particles, the pressure was increased to 130 kPa to match all the
scaling parameters with Case A, except for the slight difference in U^2/gd_p; Case E is
also conducted in the 80 mm column with 1.08 mm alumina particles at room
temperature and 170 kPa pressure, and was designed to have the coefficient of
restitution mismatch with Case A; Cases B and D are the test cases with only the
coefficient of restitution mismatched with each other. Case B is conducted in the 120
mm column with 1.51 mm silica gel particles spouted at ambient conditions, while
Case D is conducted in the 80 mm column with 1.08 mm alumina particles spouted
at room temperature and 136 kPa. Here, Cases A and B are designed as the
prototype beds and the others as the model beds for comparison. For all the cases
designed, the following geometric criteria for stable spouting were satisfied ([4], [12]):

$$D_i / d_p < 25 - 30 \qquad (2)$$

$$D_c / D_i > 3 - 12 \qquad (3)$$

Table 1. Dimensions, properties and dimensionless groups in experimental tests

Case	A	C	E	B	D
D_c(m)	0.12	0.08	0.08	0.12	0.08
$D_i \times 10^3$ (m)	10	6.7	6.7	10	6.7
L(m)	2	2	2	2	2
H(m)	0.25	0.158	0.179	0.25	0.179
T(K)	298	298	298	298	298
P(kPa)	101	130	170	101	136
Particle	Silica gel	Silica gel	Al_2O_3	Silica gel	Al_2O_3
$d_p \times 10^3$ (m)	1.50	0.96	1.08	1.51	1.08
ρ_s(kg/m^3)	1231	1557	2061	1528	2061
ρ_g(kg/m^3)	1.21	1.54	2.03	1.21	1.63
$\mu \times 10^5$ (Pa·s)	1.81	1.81	1.81	1.81	1.81
U(m/s)	0.368	0.392	0.307	0.448	0.445
Scaling group					
Φ_s	1	1	1	1	1
α(°)	21	21	20	21	20
ε_0	0.57	0.59	0.54	0.58	0.54
H/d_p	165.6	165.4	165.7	165.6	165.7
D_c/d_p	79.5	83.3	74.1	79.5	74.1
ρ_s/ρ_g	1017.3	1011.2	1014.8	1252.1	1264.2
$\rho_g d_p U/\mu$	37.1	32.02	37.2	45.2	43.3
U^2/gd_p	9.2	16.3	8.9	13.0	18.7
$\rho_s d_p U/\mu$ (10^{-3})	37.79	32.38	37.75	57	54.7
e_{ss}	0.84	0.82	0.70	0.84	0.70

RESULTS AND DISCUSSION

Table 2 gives the dimensionless fountain heights measured in the different cases. It can be seen that comparing with Case A, the dimensionless fountain height of Case C is 23% higher and that of Case E is 34% higher. As can be seen in Table 1, e_{ss} is the main difference in the scaling parameters among Cases A, E and C, suggesting the importance of e_{ss}. This can be further confirmed by the much larger difference in the dimensionless fountain heights of Cases B and D that have almost the same values of the scaling parameters except for their different e_{ss}.

Table 2. Fountain heights obtained in the different cases listed in Table 1

Case	Bed height (mm)	Fountain height H_f (mm)	Dimensionless fountain height H_f/D_c	Deviation relative to Case A (%)
A	250	145	1.21	-
E	179	130	1.62	+34
C	158	120	1.50	+23
B	250	180	1.50	-
D	179	220	2.75	+83

It is known from practice that with lower values of the coefficient of restitution the particles loose a considerable amount of their momentum during the collisions. This leads to a very different bed behavior (i.e. much more clustering of particles) ([13], [14]). The differences in fountain height may be related to the increased tendency to clustering and thus more irregular bed behavior.

Table 3 shows the spout diameters measured in the different cases. It can be seen that the dimensionless spout diameters of Cases A and C are very close, with only a deviation of 0.4%. For Cases A and E, however, a large deviation (20.1%) emerges; the dimensionless spout diameter difference of Cases B and D is more obvious, about 53.7%. These results further emphasize that the e_{ss} significantly affect the scaling of spouted beds. By considering the force balance and solid stresses in the annulus, Bridgewater and Mathur ([11]) concluded that the spout diameter depended on the gas flowrate, column diameter and particle bulk density, which was further confirmed by He et al. ([4]). The recent CFD studies ([7], [8]) revealed that by affecting the solid stresses in the spout, e_{ss} could greatly impact the flow patterns in spouted beds and thus can be considered as an important parameter in describing solid stresses in the spout.

Figure 2 shows the radial voidage profiles of Cases A, C and E. In the upper section of the bed, the voidage profiles of Cases C and E distinctly deviates from that of Case A, with that of the latter more significantly lower than that of Case A; in the middle section of the bed (Fig. 2b), this deviation becomes less for both Cases C and E; in the lower section of the bed (Fig. 2c), the voidage profiles of Cases A and C approach to each other, except near the spout axis, while that of Case E shows a larger deviation from that of Case A. As seen in Table 1, the scaling parameters of Cases C and E are close to those of Case A except for the apparent difference of the e_{ss} between Case E and Cases A and C. Therefore, the large deviation of the voidage profile of Case E from that of Case A than that of Case C signifies that e_{ss} plays very important role in the scaling relationship. The somewhat complexity of voidage distribution in the middle section may be caused by the measurement errors. Our CFD simulation work ([8]) has also shown that the influence of e_{ss} on bed voidage could not be neglected. The results show that a larger coefficient of restitution give higher voidage in the spout region, which is coincident with the CFD simulation results of Huilin et al. ([7]). Fig. 2 also shows that in the annulus the radial porosity profiles are nearly flat, suggesting that the interaction between the wall and the particles is small, meaning that the particle-wall collision can be neglected in the scaling relationship.

Table 3. Spout diameters measured for the different cases

Case	Dimensionless spout diameter (D_s/D_c)			Average	Deviation relative to Case A (%)
	Upper section	Middle section	Lower section		
A	0.300	0.278	0.290	0.289	-
E	0.207	0.246	0.24	0.231	-20.1
C	0.293	0.282	0.282	0.286	-0.4
B	0.280	0.290	0.280	0.283	-
D	0.440	-	0.430	0.435	+53.7

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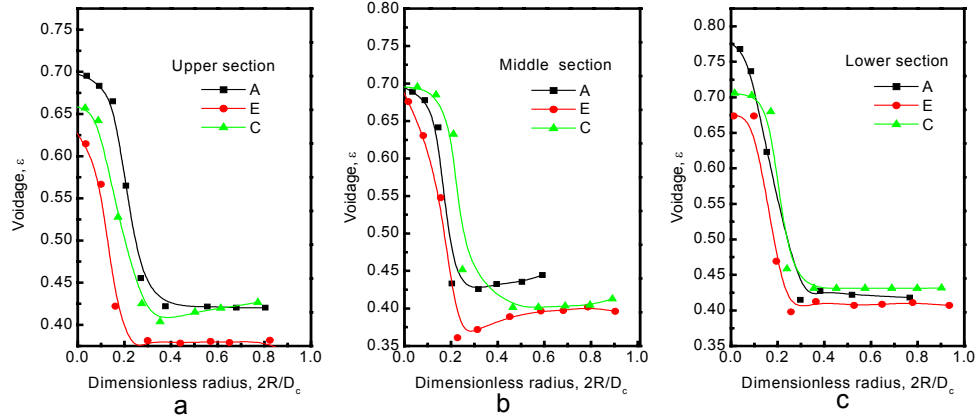

Fig. 2. Radial voidage profiles of Cases A, C and E

CONCLUSION

A new set of scaling relationship of spouted beds including the coefficient of restitution of particles was proposed and was experimentally verified in the present investigation. The results of the experimental verification show that the hydrodynamic parameters such as the fountain height, spout diameter, and voidage profile are closely related to the coefficients of restitution. When the coefficients of restitution of two systems do not match, their similarity can not be satisfied.

ACKNOWLEDGEMENT

NOTATION

D_c	Bed diameter, m
D_i	Orifice diameter, mm
d_p	Particle diameter, mm
D_s	Spout diameter, mm
e_{ss}	Coefficient of restitution of particles
H	Packing bed height, m
H_0	Initial height, m
H_1	Rebounding height, m
H_f	Fountain height, mm
H_m	Maximum spouting height, mm
L	Length of the vessel, m
P	Pressure, kPa
r'	Dimensionless radius

T	Temperature, K
U	Superficial gas velocity, m/s
U'	Dimensionless gas velocity
α	Particle inner friction angle
ε_0	Solids volume fraction at loose packing state
μ	Gas viscosity, Pa s
ρ_g	Gas density, kg m^{-3}
ρ_s	Particle density, kg m^{-3}
Φ_s	Particle sphericity

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