

1 **EFFECTS OF BIAXIAL CONFINEMENT IN MORTARS EXPOSED TO EXTERNAL**
2 **SULFATE ATTACK**

3

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15

16 **ABSTRACT**

17

18 Research on external sulfate attack (ESA) is usually performed on small scale specimens under

19 free expanding conditions. However, most field structures cannot expand freely due to

20 confinement induced by the ground or other elements from the structure. As a result, ESA

21 usually develops in confined conditions. This work aims to assess the interaction of gradual

22 biaxial compression stresses generated by confinement with the ESA. Visual appearance, mass

23 and ultrasonic velocity were monitored to characterize the macro-scale behavior of free and

24 restrained mortar samples. Changes on phase composition and crystal morphology induced by
25 confinement were evaluated by X-Ray diffraction and scanning electron microscopy. The
26 confining stresses generated were estimated during the attack. Results indicate that ESA is not
27 developed equally in free and confined specimens. The confinement limits sulfate availability,
28 reduce the amount of ettringite precipitated and might induce changes on crystal morphology
29 that reduce the degradation caused by the ESA.

30
31 Keywords: Concrete (E); Durability (C); Sulfate attack (C); Ettringite (D); Confinement;

32 33 **1. INTRODUCTION**

34
35 External sulfate attack (ESA) is a degradation process that affects concrete structures. It is
36 caused by the interaction between the reactive phases of the cement paste and sulfate ions from
37 an external source. The continuous sulfate exposure may lead to cracking, spalling, softening and
38 disintegration. Fortunately, in typical service conditions the attack usually develops during
39 decades before causing high degrees of damage.

40
41 The majority of common methods to investigate the resistance of cement-based materials
42 exposed to sulfates are based on accelerated tests to obtain representative results in a reasonable
43 time (e.g. ASTM C1012 or ASTM C452). These test methods assess the sulfate resistance by
44 length change measurements of unconfined specimens submerged in sulfate rich solutions. As a
45 result, most research carried out in this field use free expansions as the main degradation
46 parameter. However, typical elements exposed to ESA, such as foundations or retaining walls,

47 can rarely expand freely during sulfate exposure. Instead, these elements are subjected to a wide
48 variety of external loads and to different degrees of confinement due to interactions with other
49 elements of the structure and the soil.

50

51 Most studies dealing with the coupled action of external loads and ESA apply a constant flexural
52 or compressive load since sulfate exposure [1-9]. In general, flexural loading applied together
53 with the sulfate exposure resulted in negative effects on the durability against the attack,
54 especially when the loading exceeded 40-60 % of the maximum flexural load [7,8]. R. Gao et. al
55 [7] reported more serious deterioration of the face subjected to tensile stresses than the one
56 subjected to compressive stresses. According to the authors [7], the tensile stresses might
57 accelerate the sulfate attack due to micro-cracks that promote sulfate penetration.

58

59 Fewer studies are available in the literature dealing with the combined action of sulfate attack
60 and compressive loading [1-3,9]. This is probably caused by the higher complexity of the
61 experimental set up. In general, studies report favorable effects on the durability against the
62 attack for low stress levels, as it might slow down the sulfate ingress into concrete. However,
63 compressive stresses seems to accelerate the sulfate attack when the stress is set above a certain
64 threshold value, estimated between the 30-60 % of the ultimate compressive strength. This
65 acceleration is attributed to the generation of micro-cracks that promotes sulfate penetration [1-
66 3,9].

67

68 In all studies presented above, the load was applied from exposure and remained constant until
69 the end of the test. Although this configuration might simulate the effects of underground water,

70 rocks, overlaying soil or dead loads from the superstructure, it does not represent the effects of
71 confinement that might appear in indeterminate structures. In this case, the load rises as a
72 consequence of the expansions generated by the ESA, thus increasing gradually along the attack.
73 Figure 1 illustrates this situation with a group of end bearing piles joined at the top by a pile cap.
74 Due to the heterogenic characteristics of the groundwater level and the distribution of gypsum
75 veins in the soil, the expansions generated by the attack (ϵ_{ESA}) evolve at different rates at each
76 pile. However, highly indeterminate structures act as a single entity prior to failure.
77 Consequently, the least affected elements (pile 2 and 3) restraint the expansions and confine the
78 concrete of pile 1 by applying a gradual compressive load (F_c) in the whole section.

79

80 *<Insert Figure 1>*

81

82 Previous research on the interaction between constant compressive loads and ESA [1-3,9]
83 suggests that the effects of confinement will probably depend on the stress level. Therefore, for a
84 precise assessment of this phenomenon, it is necessary to link the different behavior of confined
85 and free specimens with the stress level applied. The monitoring of the confining stresses
86 generated during the attack requires complex experimental set ups. Only one study was found in
87 the literature able to capture this phenomenon [10]. Mullauer et. al [10] applied different degrees
88 of confinement to thin-walled mortar cylinders exposed to sulfates by a specially constructed
89 stress cell. Even though the main objective was to estimate the stresses generated during the
90 attack, it indirectly pointed some possible positive effects of confinement on the durability.
91 Evolution of the phase composition with and without confinement showed that both ettringite
92 and gypsum were partially suppressed at late stages of the attack by increasing the degree of

93 confinement. Unfortunately, other potential effects of stresses generated by confinement remain
94 practically unexplored and are ignored during the assessment of the ESA. The present work aims
95 to shed light on this phenomenon and identify which processes (ionic transport, phase
96 composition or crystal morphology) might be altered by the confining stresses.

97

98 One of the key aspects to study this phenomenon is the experimental set up adopted to generate
99 the confinement. In this work, the confinement is achieved by casting mortar specimens in the
100 shape of flattened cylinders within metallic rings. To increase the representativeness of this
101 study, 6 mortar compositions with different expansive potentials are considered to induce
102 varying magnitudes of confining stresses. Stresses are estimated by the monitoring of expansions
103 in restrained specimens throughout the attack. Visual appearance, mass and ultrasonic velocity
104 variations are used to characterize the macro-scale behavior of free and restrained samples.
105 Changes on phase composition and crystal morphology are evaluated by X-Ray diffraction with
106 Rietveld refinement and scanning electron microscopy with energy dispersive X-ray analysis,
107 respectively.

108

109 This study describes how the confined conditions in which ESA usually develops reduce the
110 deleterious effects associated to the attack. The understanding of the positive effects of
111 confinement could lead to more realistic assessments of the ESA and contribute to explain the
112 large difference between the damage developed in small-scale free-expanding laboratory
113 specimens and the one observed in real structures.

114

115 **2. EXPERIMENTAL PROGRAM**

116

117 2.1 MATERIALS AND MIXTURE CHARACTERISTICS

118

119 Materials and mixture characteristics were defined to obtain mortars with different expansion
120 rates to assess the effects of confinement over a wide range of confining stresses. Two different
121 Portland cements were used as binders: ordinary CEM I 52.5R (OPC) and sulfate-resisting CEM
122 I 42.5 R-SR5 (SRPC). Moreover, a low-calcium fly ash (ASTM C618 class F) and the air-
123 entrainer MasterAir 100 were incorporated in some dosages. Table 1 shows the chemical and
124 mineralogical composition of the binders and summarizes the physical properties. Chemical
125 composition was determined by XRF spectrometry and mineralogical composition was estimated
126 by Bogue equations. Data provided by Bogue equations is only used qualitatively to classify the
127 cements. Due to the presence of ferromagnetic particles, the elemental composition of the fly ash
128 was determined by ICP-MS. Deionized water and siliceous sand following the specifications of
129 UNE-EN 196-1:2005 were used in all mortars. Commercial superplasticizer GLENIUM ACE
130 456 was added to the mixtures.

131

132

Table 1. Properties of binders.

	OPC ^a	SRPC ^b		FA ^c
<i>Chemical comp. [% bcw^d]</i>			<i>Elemental comp. [%]</i>	
SiO ₂	19.50	20.80	Si	23.56
Al ₂ O ₃	5.90	4.00	Al	8.74
Fe ₂ O ₃	1.70	4.00	Fe	6.92
CaO	63.10	62.70	Ca	3.70
MgO	2.10	1.70	Mg	0.50
SO ₃	3.50	3.02	S	0.20
K ₂ O	0.78	0.55	K	0.55
Na ₂ O	0.35	0.24	Na	-
Cl ⁻	0.02	0.01	P	0.11
MnO	-	-	Mn	0.01

TiO ₂	-	Ti	0.28
<i>Physical prop.</i>			
Spec. surf. area (BET) [m ² /g]	1.10	1.16	1.56
d ₁₀ [μm]	0.58	0.57	2.08
d ₅₀ [μm]	6.88	7.29	8.97
d ₉₀ [μm]	31.84	34.92	29.21
<i>Phase comp. [% bcw^d]</i>			
C ₃ S	65.4	62.1	
C ₂ S	10.6	15.6	
C ₃ A	12.3	4.1	
C ₄ AF	5.6	13.6	

133 ^a: Ordinary Portland cement, ^b: Sulfate-resisting Portland cement, ^c: Fly ash and ^d:By cement weight.

134

135 The composition of the 6 matrices used in this study are listed in Table 2. The composition of the
136 OPC_0.45 intends to simulate the typical composition of the mortar that surrounds the coarse
137 aggregate in a conventional concrete applied in foundations. Mortars with high expansive
138 potentials were produced by using OPC with varying water/cement ratios (from 0.38 to 0.55) and
139 the use of an air-entrainer to promote sulfate penetration. Fly ash was incorporated in one
140 composition to obtain a highly refined pore network. Volumetric variations caused by the
141 different water/cement ratios considered and the use of fly ash were fully compensated by a
142 reduction of sand, maintaining a constant amount of cement in all compositions. The slight
143 increase of volume produced by the air-entrainer was not taken into account. On the other hand,
144 a dosage with SRPC was designed to assess the behavior of low expansive mortars under
145 confined conditions. The nomenclature adopted for each composition follows the pattern ‘cement
146 type’_‘water/cement ratio’. Mortars with air-entrainer or fly ash have the term ‘AE’ or ‘FA’ after
147 the cement type, respectively.

148

149 The mixing procedure defined in UNE-EN 196-1:2005 was adopted. In the case of the
150 composition with fly ash, the latter was first thoroughly mixed with cement prior to water

151 addition. The air-entrainer was added at the end of the mixing procedure and mixed at high speed
 152 for 60 s. To assure similar surface finish qualities and workability amongst the different
 153 compositions, superplasticizer was mixed with the deionized water to obtain flow extents of 20
 154 cm \pm 0.5 cm.

155

156 Table 2. Compositions and mass attenuation coefficient (MAC) of the mortars.

Material	OPC_0.38	OPC_0.45	OPC_0.55	OPC+AE_0.45	OPC+FA_0.45	SRPC_0.45
Cement [kg/m ³]	580	580	580	580	580	580
Sand [kg/m ³]	1425	1325	1180	1325	1140	1330
Water [kg/m ³]	220	261	319	261	261	261
Water/cement ratio	0.38	0.45	0.55	0.45	0.45	0.45
Air-entrainer [% bcw]	-	-	-	0.3	-	-
Fly ash [% bcw]					30	
Superplasticizer [% bcw]	1.00	0.35	-	0.25	0.55	0.20
MAC [cm ² /g]	48.11	48.01	47.84	48.01	49.15	48.98

157

158 2.2 EXPERIMENTAL PROCEDURE

159

160 2.2.1 SPECIMEN PREPARATION

161

162 Specimens traditionally used for the assessment of the ESA consist of slender prisms with low
 163 volume to surface ratios to maximize sulfate ingress and facilitate measurement of expansions.

164 However, the generation of confinement in samples with such geometric characteristics

165 submerged in aggressive solutions requires complex devices with limited accuracy and

166 replicability [1-3,9].

167

168 In this work, mortars specimens of 78 mm of diameter and 17 mm of height were used. This
169 configuration allows easier expansion restraint by casting the sample within a metallic ring. The
170 dimensions of the mortar specimens were defined to maintain similar exposed surface-volume
171 ratio than other studies that showed good balance between test duration and representativeness
172 [11]. Steel rings were laser cut from a duplex stainless steel 2205 (EN 1.4462) seamless pipe of
173 3" SCH. 40s. This material was used for its high strength and resistance to local and uniform
174 corrosion in aggressive environments. Thickness and material properties of the steel ring were
175 chosen to obtain high degrees of restraint in order to maximize the confining stresses applied to
176 the mortar and to avoid onset of inelastic deformations on the steel. In practice, such degrees of
177 confinement may not be representative of the soil action, but it could be representative of other
178 situations such as the one depicted in Figure 1.

179
180 Figure 2a and 2b depicts a schematic representation of the molds and the casting process
181 adopted. The molds were composed by a PE rigid base with 4 fixed PVC or steel molds with the
182 same inner diameter and a moving PE rigid cover. The mortar (represented in light hatching) was
183 poured inside the PVC or steel molds and compacted with 15 jolts in the flow table (ASTM
184 C1437) at a rate of 1 jolt per second to eliminate air pockets. 5 bolts were used to guide the cover
185 into the base during assembly (Figure 2b). In order to ensure adequate surface finish quality, the
186 molds were then vibrated during 10 seconds at the vibration table. Notice that these molds
187 allowed the casting of both free and restrained specimens by following the same procedure. By
188 that, mortars in both configurations reached similar initial mixture properties and surface finish
189 qualities.

190

191 Specimens were demolded 24 hours after casting. Specimens in free conditions were extracted
192 from the PVC molds and their lateral faces were water sealed with the flexible epoxy coating
193 MasterSeal M 338 to ensure similar penetration of the sulfate ions than in restrained specimens
194 and to avoid corner spalling (Figure 2c). Specimens in restrained conditions were not coated
195 since the steel ring surrounding the mortar prevents the sulfate ingress from the lateral faces of
196 the specimen (Figure 2d).

197

198 *<Insert Figure 2>*

199

200 2.2.2 EXPOSURE CONDITIONS

201

202 All specimens were cured in water at $25\text{ }^{\circ}\text{C} \pm 1\text{ }^{\circ}\text{C}$ for one day to ensure full saturation of the
203 samples prior to sulfate exposure. Two days after casting, specimens were exposed to two
204 different sodium sulfate solutions (3 and 30 g of $\text{Na}_2\text{SO}_4/\text{l}$). The sulfate concentration of 3 g/l
205 corresponds to the upper limit of the moderately aggressive class of exposure defined in EN 206-
206 1, whereas 30 g/l corresponds to 10 times the typical values found in the field conditions [12].
207 The early exposure was adopted to reproduce the conditions of structures build *in situ* and to
208 accelerate the attack [12]. The age of sulfate exposure is considered as day 0 in the analysis of
209 the results. The solution was renewed weekly during the first month and every other week until
210 the end of the test at 365 days. The volumetric ratio of sulfate solution to mortar was 12.

211

212 Water pumps were used at low speed to ensure a continuous flow from the bottom to the top of
213 the container in order to minimize concentration gradients. The containers were filled up to the

214 top and covered to reduce contact with the air, thus limiting CO₂ dissolution and carbonation.
215 Reference samples of each composition with and without confinement rings were exposed to
216 non-aggressive curing with water without sulfates for comparative purposes.

217

218 2.2.3 TEST METHODS

219

220 - *Expansions and confining stresses*

221

222 A MICROMASTER electronic micrometer with a precision of ± 0.001 mm was used to measure
223 the expansions of free and restrained specimens (Figure 3). A metallic platform braced with the
224 micrometer was used to fix the specimen and measured points. Several vertical strips were
225 introduced to facilitate the measuring and to guarantee a similar position of the specimens
226 (Figures 2c and 2d). Prior to the start of the experimental program, the precision of the
227 equipment was evaluated on free and restrained specimens during a series of over 500
228 measurements. Both free and restrained specimens showed a variability of the measurements of
229 ± 0.002 mm. Measurements were taken weekly during the first month and every other week until
230 the end of the study. For each specimen, 3 radial directions were measured at each time (Figure
231 3a and 3b). Since 3 replicas were considered, each expansion value presented in this study is the
232 average of 9 measurements.

233

234 <Insert Figure 3>

235

236 - *Macrostructural monitoring*

237

238 Characterization of the macro-scale behavior relies upon measurements of ultrasonic velocity
239 and mass variation and visual inspection of the specimens. Ultrasonic pulse velocity between the
240 two exposed faces was measured at 500 kHz sampling frequency with a PUNDIT PL-200. A
241 high frequency transducer was selected due to the low thickness of the specimens (17 mm). A
242 zero-crossing algorithm was used to calculate the travelling time of the ultrasonic signal. The
243 measurements were performed immediately after extraction from the solution tanks to ensure
244 similar saturation conditions. A sample holder was used to fix the position of the measured
245 location (the center of the specimen). Mass evolution was controlled with a precision balance of
246 ± 0.01 g. In this case, surface water of the samples was dried before weighting. Measurements
247 were taken weekly during the first month and every other week until the end of the study. The
248 values of ultrasonic pulse velocity and mass presented in this study represent the average of three
249 specimens.

250

251 - *X-ray diffraction (XRD)*

252

253 Differences on phase composition between free and restrained specimens were investigated by
254 XRD at 90, 180 and 365 days. Samples for XRD were core drilled from the center of the exposed
255 faces of the original specimens using a column drill equipped with a diamond drill bit cooled
256 with water (14 mm of diameter). For each dosage, samples were extracted from the same
257 specimen to reduce the variability of the results. Due to the symmetric sulfate exposure
258 conditions, each sample was divided in two. One half was crushed and the powder was pressed
259 in cylindrical standard sample holders of 16 mm of diameter and 2.5 mm of height. The other

260 half was discarded. XRD measurements were made using a PANalytical X'Pert PRO MPD
261 Alpha1 $\Theta/2\Theta$ diffractometer in reflection Bragg Brentano geometry of 240 mm of radius. $\text{CuK}_{\alpha 1}$
262 radiation ($\lambda=1.5406 \text{ \AA}$) and X'Celerator detector with active length of 2.122° were used. Work
263 power was set to 45 kV – 40 mA. $\Theta/2\Theta$ scans from 4 to $80^\circ 2\Theta$ with a step size of $0.017^\circ 2\Theta$ and
264 a measuring time of 50 seconds per step were performed. Sample holders were spun at 2
265 revolutions per second.

266

267 Rietveld analysis using external standard method was performed with the XRD results for the
268 quantitative study of the crystalline phases. The external standard method was used for
269 quantification instead of the more common internal standard method to avoid homogenisation
270 problems and further dilution of the cement paste in the analyzed sample [13-15]. The adopted
271 methodology is similar to earlier works [13-15]. Phase weight fractions were calculated from
272 phase scale factors by comparison to the scale factor of the external standard (Al_2O_3), measured
273 under identical diffractometer conditions. The values of density and volume of the unit cell of
274 each phase were obtained from data sets from ICSD. Mass attenuation coefficients (MAC) of the
275 different compositions used were calculated from the MAC of each component, including the
276 water content and considering the weight fraction of all components. Final MAC of the different
277 mortars used are listed in Table 2.

278

279 All Rietveld refinements were done with X'Pert High Score Plus software package by
280 PANalytical using the structures listed in Table 3. Small peaks of Fe-substituted ettringite
281 formed as a result of the reaction between sulfate ions and the ferroaluminate phases were
282 detected in some mortars at late stages of the attack. Since its crystalline structure for Rietveld

283 refinement was not available it was not considered during quantification. The global variables
 284 refined were the background polynomial with 4 coefficients (1st, 2nd, 3rd and 5th) and the zero
 285 shift. For all phases detected, individual scale factors and lattice parameters were refined. A
 286 pseudo-Voigt function was chosen to model the peak shape. The phase profile width (w) was
 287 refined for quartz, ettringite, portlandite and gypsum. For quartz and portlandite, the profile
 288 parameters U , V and the peak shape were also refined. Preferred orientation corrections were
 289 applied when necessary for gypsum (0 2 0), portlandite (0 0 1), ettringite (1 0 0) and quartz (1 0
 290 1) as long as the phase content was above 2 %.

291

292

Table 3. Phase structures used for Rietveld refinement.

Phase	Chemical composition	ICSD Code	Reference
Alite	Ca ₃ SiO ₅	94742	[16]
Belite_o	Ca ₂ SiO ₄	81097	[17]
Portlandite	Ca(OH) ₂	15471	[18]
Calcite	CaCO ₃	79673	[19]
Ettringite	Ca ₆ Al ₂ (SO ₄) ₃ (OH) ₁₂ 26H ₂ O	155395	[20]
Gypsum	CaSO ₄ 2H ₂ O	15982	[21]
Ferrite	Ca ₂ AlFeO ₅	9197	[22]
Quartz	SiO ₂	200721	[23]
Mullite	Al _{4,74} Si _{1,25} O _{9,63}	66448	[24]
Corundum	Al ₂ O ₃	73725	[25]

293

294 - *Scanning electron microscopy (SEM)*

295

296 Morphology of the hydrates precipitated during sulfate exposure at the end of the test were
 297 examined by SEM (Jeol J-6510) using backscattered and secondary electrons at the voltage of 20
 298 kV. Chemical composition was determined by energy disperse X-ray spectroscopy (EDS).

299 Sections of the samples extracted were cut with an end-cutting plier perpendicular to the exposed

300 surfaces. Fractured samples were frozen in liquid nitrogen, dried in vacuum during 48 hours and
301 coated with carbon.

302

303 2.2.4 CONFINING STRESSES PROVIDED BY THE STEEL RING

304

305 In this work, the strain evolution measured in free and restrained specimens were used to
306 estimate the theoretical and real confining stresses generated during the attack. In free expanding
307 conditions, stresses generated by ESA are released in the form of strains. However, when the
308 strains are restrained due to the steel ring only a fraction of the stresses generated by the attack
309 are released in the form of expansions, while the other fraction confines the mortar with
310 compressive stresses (σ_c). This situation is depicted in Figure 4a, where free, restrained and steel
311 expansions are denoted as ε_f , ε_r and ε_s , respectively. The term D corresponds to the diameter of
312 the specimen.

313

314

<Insert Figure 4>

315

316 Figure 4b shows the ideal stress distribution assumed to estimate the confining stresses (σ_c). As
317 depicted, compressive stresses are balanced by tensile stresses in the steel ring (σ_s). By imposing
318 equilibrium in the steel ring, it is possible to relate the increase of confining stresses applied to
319 the mortar with the increment of strains measured in the steel ring between t_n and t_{n+1} (Eq. 1).
320 In Eq. 1, E_s and e refers to the elastic modulus and the thickness of the steel ring, while R
321 represents the radius of the mortar specimen (Figure 4b). Eq. 1 assumes a linear behavior of the
322 steel, which is verified in Section 3 by the low stresses developed.

323

$$\Delta\sigma_c(t_{n+1}, t_n) = \frac{\Delta\varepsilon_s(t_{n+1}, t_n)E_s e}{R} \quad (\text{Eq. 1})$$

324

325 By introducing the strain evolution measured in confined specimens (ε_s), Eq. 1 provides the real
326 confining stresses developed in these samples. Additionally, the experimental set up designed
327 measures the strain of its corresponding sample in free expanding conditions (ε_f). To estimate
328 the theoretical confining stresses developed for a given ε_f , it is necessary to consider the strains
329 relation described in Eq. 2 and the constitutive law of mortar. According to Figure 4a, for any
330 given time interval expansions generated in free specimens (ε_f) are the sum of the expansions
331 measured in confined specimens (ε_s) and the ones restrained by the presence of the steel ring (ε_r)
332 (Eq. 2). Eq. 3 shows the mortar constitutive law assumed, which is described in the Spanish
333 building code EHE-08 for concrete structures. Notice that this equation takes into account the
334 second order effects of structurally indeterminate specimens (creep and potential cracking).

335

$$\Delta\varepsilon_f(t_{n+1}, t_n) = \Delta\varepsilon_s(t_{n+1}, t_n) + \Delta\varepsilon_r(t_{n+1}, t_n) \quad (\text{Eq. 2})$$

$$\Delta\sigma_c(t_{n+1}, t_n) = \left(\Delta\varepsilon_r(t_{n+1}, t_n) - \sum_{i=1}^{i=n-1} \frac{\Delta\sigma_c(t_i)}{E_{c,28}} (\varphi_c(t_{n+1}, t_i) - \varphi_c(t_n, t_i)) \right) \cdot \frac{E_c(t_n)}{1 + \frac{E_c(t_n)}{E_{c,28}} \varphi_c(t_{n+1}, t_n)} \quad (\text{Eq. 3})$$

336

337 In Eq. 3, the terms $E_c(t_n)$ and $E_{c,28}$ represent the elastic modulus of mortar at a certain time and
338 at 28 days, respectively. Potential cracking caused by high compressive stresses generated in the
339 mortar due to the expansions restrained is considered by a degradation of the elastic modulus
340 ($E_c(t_n)$), initiating a plastic behavior of the material for stresses higher than 80 % of the
341 compressive strength. The effects of creep are considered in Eq. 3 by the creep coefficients φ_c ,

342 which are calculated according to the equations provided in the Spanish building code EHE-08.
343 This expression is valid as long as the stresses remain below the 45 % of the mortar compressive
344 strength. The theoretical confining stresses and strains generated over time in restrained
345 specimens are estimated from Eqs. 1, 2 and 3, considering that at $t = 0$ the influence of creep
346 and cracking is null.

347
348 Due to the importance of the Young Modulus of the steel rings for the assessment of the
349 confining stresses generated (real and theoretical), two tensile coupon tests were performed to
350 precisely determine this parameter. Coupon dimensions and loading configuration are depicted in
351 Figure 5. Strain gauges were placed on each face of the coupon specimen to measure the
352 longitudinal tensile strains. The amplitude of the cycles depicted in Figure 5 was defined to cover
353 the expected stress levels reached during the attack. The Young Modulus (E_s) was calculated
354 from the slope of the strain-stress curves obtained during the 10 loading cycles. The average
355 value obtained considering both strain gauges was 178769 MPa with a standard deviation of
356 10294 MPa.

357
358 *<Insert Figure 5>*

359
360 The Young Modulus of the mortar at 28 days ($E_{c,28}$) was indirectly estimated from ultrasonic
361 pulse velocity measurements. The dynamic modulus of elasticity was calculated for each
362 composition from the pulse velocity measured at 28 days according to ASTM C 597-02. Density
363 and dynamic Poisson's ratio of 2150 kg/m^3 and 0.2 were assumed, respectively. The Static
364 modulus of elasticity was estimated by considering that the dynamic modulus is 1.2 times the

365 static modulus [26]. Values obtained for all compositions ranged between 16492 and 19595
366 MPa.

367

368 **3. RESULTS AND DISCUSSION**

369

370 **3.1 EXPANSIONS AND CONFINING STRESSES**

371

372 Figure 6 depicts the evolution of free and restrained expansions for specimens stored in 30 and 3
373 g/l. Traditionally, the expansions presented by most researchers correspond to the difference
374 between the expansions measured in aggressive and non-aggressive conditions to isolate the
375 effects of sulfates from dimensional variations caused by normal cement hydration processes.
376 However, in this work expansions are used to assess the theoretical and actual confining stresses
377 generated in the restrained specimens. For that, the discrimination of the contribution of sulfates
378 and normal cement hydration on the expansions measured is not appropriate since all expansions
379 contribute to generate stresses, regardless of its origin. Due to the large number of measuring
380 points at each curve, +1/-1 standard deviation bars are only depicted at 28, 90, 180, 270 and 365
381 days, being $3.97 \cdot 10^{-5}$ and $2.68 \cdot 10^{-5}$ the mean standard deviation for free and restrained expansion
382 measurements, respectively. For clarity, the standard deviation bars of expansion measurements
383 in restrained specimens are not included in Figure 6b and Figure 6d. Instead, the corresponding
384 standard deviations are represented in Figure 7.

385

386 Free specimens under high aggressive conditions reach a wide variety of expansions depending
387 on the mixture composition (Figure 6a). The expansions obtained at the end of the period

388 assessed varies between $2.8 \cdot 10^{-3}$ and $6.6 \cdot 10^{-4}$. Mortars with fly ash and water/cement ratio of
389 0.55 (OPC+FA_0.45 and OPC_0.55) present the highest expansions while mortars with air-
390 entrainer and sulfate-resisting cement (OPC+AE_0.45 and SRPC_0.45) show the lowest
391 expansions throughout the attack. On the other hand, in low aggressive curing conditions the
392 expansions developed by free specimens presented maximum values below $5.0 \cdot 10^{-4}$ at 365 days
393 (Figure 6c).

394

395 *<Insert Figure 6>*

396

397 Results obtained for restrained specimens (Figures 6b and 6d) show expansions below $2 \cdot 10^{-4}$ for
398 all compositions in both aggressive environments. Additionally, these figures include the
399 evolution of theoretical steel expansions estimated by the mechanical model described in section
400 2.2.4, depicted as dotted lines of the same color as the corresponding composition. The domain
401 covered by the theoretical expansions is highlighted by grey hatching. Due to the lack of
402 experimental data, a mortar compressive strength of 40 MPa was assumed for this calculation,
403 which is consistent with typical values reported in the literature for this material [27]. However,
404 a parametric analysis performed indicates that the compressive strength of the material is not a
405 critical parameter of the model, since a 25 % increase of the compressive strength only induces a
406 3 to 6 % increase of the expansion obtained at the end of the test. As shown in Figure 6b, there is
407 a significant difference between the theoretical and measured expansions for the high aggressive
408 environment. Final expansions measured at 365 days are between 1.4 and 8.5 times lower than
409 the theoretical expansions. For low aggressive conditions, measured and theoretical expansions
410 are similar.

411
412 Figure 7 presents the real and theoretical evolution of confining stresses in restrained specimens
413 based on the theoretical and measured expansions depicted in Figure 6b and 6d for high and low
414 aggressive conditions. Real and theoretical stresses for each composition are represented with
415 solid lines with markers and dotted lines, respectively, following the same color pattern. The
416 envelop domain covered by the theoretical stresses is depicted in grey. Based on the mechanical
417 contribution of the steel rings and the free expansions measured, the confining stresses applied to
418 the restrained specimens should reach values between 3.8 and 16.8 MPa at the end of the test in
419 high aggressive conditions. However, as shown in Figure 7a, the actual confining stresses
420 generated at 365 days are significantly lower, varying between 1.9 and 4.9 MPa. As expected
421 from Figure 6d, theoretical and actual confining stresses are similar for low aggressive
422 conditions.

423
424 *<Insert Figure 7>*
425

426 The large difference between theoretical and measured stresses are observed in all mortars.
427 Therefore, it seems that the composition of the different matrices considered had minor effects
428 on the confining stresses generated. Due to the low values measured, the influence of
429 water/cement ratio, cement, air-entrainer or fly ash is not clear. In most cases, the differences
430 observed amongst these compositions are relatively close to the average variability of the
431 measurements (+1/-1 mean standard deviation of +0.67/-0.67 MPa).

432

433 These results might be partially influenced by several factors. First, the mechanical model used
434 assumes several simplifications on the consideration of the second order effects. However, for
435 the values of stresses predicted (below the 45 % of the compressive strength), the model
436 described in section 2.2.4 should remain valid. On the other hand, the presence of the steel ring
437 might promote the release of strains in the non-restrained plane. Special considerations were
438 taken during the design stage of the samples to minimize this phenomenon. Due to the geometric
439 characteristics of the specimens, strains developed in the horizontal plane are about 4 times the
440 strains in the vertical plane. Therefore, it is unlikely that the large difference between the
441 theoretical and measured stresses depicted in Figure 7a is entirely explained by a transfer of
442 strains from the restrained plane to the free direction.

443

444 The results obtained indicate that only a small fraction of the expansions restrained by the steel
445 ring are translated into stresses. This unexpected behavior suggests the presence of an additional
446 phenomenon: There might be an interaction between the confining stresses caused by restraint
447 and processes associated with the ESA that define the expansive forces generated during the
448 attack.

449

450 3.2 MACROSTRUCTURAL EFFECTS OF EXPANSION RESTRAINT

451 3.2.1 VISUAL ASPECT OF SAMPLES

452

453 Figure 8 and Figure 9 allows the comparison of the external surface of free and restrained
454 specimens for OPC+FA_0.45, OPC_0.45, SRPC_0.45 and OPC+AE_0.45 in non-aggressive
455 conditions (0 g/l) and high aggressive conditions (30 g/l) at the end of the test. These mixtures

456 are selected to cover different free expansions depicted in Figure 6a. The visual aspect of the
457 specimens submerged in non-aggressive conditions are included here to be able to distinguish the
458 effects of confinement on the ESA phenomenon from the normal hydration processes. Figure 8
459 shows no difference on the visual aspect of the external surface of free and restrained specimens
460 in non-aggressive conditions.

461

462 *<Insert Figure 8>*

463

464 No major failure in the form of generalized spalling of the external surface, cracking due to
465 compressive stresses or tensile splitting is observed in any composition submerged in the
466 aggressive solution (Figure 9). Restrained and free OPC+FA_0.45 and OPC_0.45 specimens
467 present a thin dense layer covering most of the surface. In both cases, samples experienced
468 similar degrees of localized spalling (highlighted with a red circle) in locations within the region
469 covered by the dense layer. This layer is not observed in SRPC_0.45 or OPC+AE_0.45. The
470 similar visual appearance between free and restrained specimens of each composition may be
471 caused by the low confining stresses developed during the attack (below 5 MPa). Compressive
472 stresses of this magnitude should not cause additional damage.

473

474 *<Insert Figure 9>*

475

476 Figure 10 presents the visual aspect of OPC_0.45 in the low aggressive solution (3 g/l) at 365
477 days. As described for 30 g/l, the external surface of free and restrained mortars are in similar
478 conditions and do not present any form of major failure. As expected, specimens show lower

479 levels of degradation than the same composition stored in 30 g/l (Figure 9b). Figure 10 depicts
480 the beginning of the formation of a thin layer of precipitated product covering a small fraction of
481 the exposed surface. At the end of the test, no local spalling is detected in any configuration.

482

483 *<Insert Figure 10>*

484

485 3.2.2 MASS VARIATION

486

487 Figure 11 shows the influence of confinement on the evolution of the relative mass variation
488 over time for all mortars stored in 30 and 3 g/l. In order to isolate the effects related to sulfate
489 exposure from the phenomena of absorption, hydration and leaching experienced by all samples
490 in both configurations (free and restrained), this figure represents the differences between
491 exposed and control specimens. The relative mass variation is calculated as the ratio between the
492 mass variation and initial mass for each composition. The envelopes covered by the relative mass
493 variation curves measured in all compositions considered for free and restrained specimens
494 (without considering the weight of the steel ring) are represented with green and grey domains,
495 respectively. To isolate and highlight the effects of confinement, Figure 11 includes relative
496 mass variation curves corresponding to the difference between restrained and free specimens for
497 each composition (represented in solid lines with markers). Curves with positive values indicate
498 that confinement reduces the relative mass loss whereas negative values suggest that confined
499 conditions promote mass loss. The standard deviation of the curves depicted in Figure 11 range
500 from 0.015 to 0.021 %, being the +1/-1 mean standard deviation of +0.017/-0.017 %.

501

502 Prior to cracking, mass variation in saturated conditions can be related to the mobility of ions
503 between the pore and the external solution. On one hand, mortars exposed to ESA might
504 experience positive mass changes caused by sulfate uptake from the external solution. On the
505 other hand, negative mass changes are associated to leaching. The domains depicted in Figure 11
506 depict negative relative mass variations for free and restrained specimens during sulfate
507 exposure. These results indicate that leaching overrides the sulfate uptake phenomenon in both
508 aggressive conditions evaluated.

509

510 The curves corresponding to the difference between relative mass variation of restrained and free
511 specimens shows positive values for most compositions. Based on the assumption of full
512 saturation and the similar cracking state between free and restrained mortars (Figure 9 and 10),
513 these results indicate lower leaching rates in confined specimens. This phenomenon might be
514 explained by the mechanical action of the steel rings over the mortar sample. Confinement could
515 potentially limit the appearance of micro-cracks and partially close or reduce pore channels
516 connecting the inner layers of the matrix with the external media. Consequently, the ionic
517 movement between the pore and external solution is indirectly reduced. This observation is in
518 agreement with several studies that report that low or moderate compressive stresses reduce the
519 availability of sulfates [1-3,9].

520

521 *<Insert Figure 11>*

522

523 Mortars OPC_0.55, OPC_0.45, SRPC_0.45 and OPC+AE_0.45 show the highest influence of
524 restrained conditions on the mass variation. The restrained configuration of these compositions

525 presents on average between 2.6 to 6 times less mass reduction than mortars OPC_0.38 and
526 OPC+FA_0.45 throughout the attack. According to these results, the lower ionic movement
527 between internal and external solutions in restrained conditions is more significant in matrices
528 with high water/cement ratios and the presence of air bubbles. This trend can be explained by the
529 expectedly higher ionic flux between internal and external solutions present in those matrices
530 due to a coarser pore network.

531

532 3.2.3 ULTRASONIC VELOCITY VARIATION

533

534 Figure 12 depicts the effects of expansion restraint on the ultrasonic velocity for the different
535 compositions stored in 30 and 3 g/l. In order to isolate the effects related to sulfate exposure from
536 the phenomena of hydration experienced by all samples in both configurations (free and
537 restrained), the results presented in this section correspond to the differences between exposed
538 and control specimens. The relative velocity change corresponds to the ratio between the velocity
539 variation and initial velocity. The envelopes covered by the measurements of relative ultrasonic
540 velocity change in all compositions for free and restrained specimens are represented with green
541 and grey domains, respectively. To facilitate the analysis, the effects of confinement are isolated
542 in Figure 12 by including the relative velocity variation curves corresponding to the difference
543 between restrained and free specimens for each composition (solid lines with markers). The
544 standard deviation of these curves range from 1.01 to 1.45 %, being the +1/-1 mean standard
545 deviation of +1.31/-1.31 %.

546

547 For high aggressive conditions (Figure 12a), shaded regions depict negative relative velocity
548 changes for free and restrained specimens. The decrease on the ultrasonic velocity indicates that
549 ESA has caused physical damage (micro-cracks) in both configurations since the beginning of
550 the test. Domains depicted in low aggressive conditions (Figure 12a) show either null or slightly
551 positive velocity variations throughout the attack. These results suggest that ESA did not
552 generate significant physical damage to the matrices in this exposure condition.

553

554 Most curves that illustrate the effects of confinement depict positive variations of ultrasonic
555 velocity. In this case, positive values indicate that confinement causes denser matrices and lower
556 levels of physical damage relative to the specimens in free-expanding conditions. The series
557 OPC_0.38 and OPC_0.45 describe the most significant reduction of damage caused by
558 confinement in high aggressive conditions (Figure 12a). For these compositions, restrained
559 conditions prevented almost completely the formation of physical damage. The effects of
560 confinement for the other compositions are less clear, with differences ranging from -2 to +2 %.
561 For low aggressive conditions, the 3 series evaluated present slight positive values, suggesting
562 that confinement also causes denser matrices. However, taking into account the relatively high
563 standard deviation of these measurements, the trends depicted in Figure 12b are not sufficiently
564 significant to sustain this statement.

565

566 *<Insert Figure 12>*

567

568 The higher integrity and density of confined matrices can be explained by the confining stresses
569 generated by the steel rings. The compressive stresses acting in the opposite direction of the

570 expansive forces caused by the ESA should reduce or delay the appearance of micro-cracks in
571 the matrix. As a consequence, sulfate ingress in confined specimens might be slower than in free
572 specimens (as suggested in section 3.2.2). A limited sulfate availability in the pore solution
573 should cause a decrease on the amount of expansive phases precipitated and thus, reduce the
574 damage generated. This hypothesis is verified in section 3.3.1. by the quantification of the
575 expansive phases in free and restrained specimens.

576

577 3.3 MICROSTRUCTURAL EFFECTS OF EXPANSION RESTRAINT

578

579 3.3.1 X-RAY DIFFRACTION

580

581 This section presents a comprehensive analysis of the evolution of phase composition for free
582 and restrained specimens by quantitative XRD. To simplify the interpretation of the results, only
583 the main crystalline phases interacting with the sulfate ions are presented. Phase contents are
584 expressed as a percentage of the cement content defined by the initial dosage of each
585 composition.

586

587 Figure 13 shows ettringite, gypsum and portlandite contents for all compositions submerged in
588 the high aggressive solution (30 g/l) at 365 days. Values corresponding to free and restrained
589 conditions are represented as circles and triangles, respectively. Ettringite and gypsum contents
590 vary between 11-19 % and 3-11 %, respectively. Higher ettringite over gypsum contents were
591 expected due to the lower solubility of ettringite [28]. The composition with the least amount of
592 expansive phases correspond to OPC_0.38, followed by the mortar with sulfate-resisting cement.

593 Increasing amounts of expansive phases are measured for the compositions OPC_0.55 and
594 OPC+AE_0.45. These trends might be explained by an increase of sulfate availability in the pore
595 solution caused by the increase of water/cement ratio and the presence of air bubbles. Portlandite
596 contents evolve similarly to ettringite contents. In this case, the increase of water/cement ratio
597 and the presence of air bubbles seems to promote hydration of the silicate phases. The only
598 composition that does not follow this trend is OPC+FA_0.45, which presents the lowest
599 portlandite content amongst all mortars evaluated. This result can be explained by the pozzolanic
600 activity of the fly ash, which consumes reactive silica and calcium hydroxide, producing calcium
601 silicate hydrate [29].

602

603 The differences on phase content between restrained and free specimens are presented in
604 clustered columns for each composition. Positive values indicate that restrained conditions
605 promote phase precipitation while negative values suggest that the confining stresses from the
606 steel ring hinder its formation. For most compositions, expansion restraint causes a slight
607 decrease on ettringite content. The reduction seems to increase with the amount of ettringite
608 measured in free conditions. Series OPC+AE_0.45 presents the highest influence, with a relative
609 decrease of 22 % between free and restrained specimens. These results might be explained by the
610 reduced mobility of ions between external and internal solutions in restrained conditions. As
611 described in section 3.2.2, the decrease of ionic mobility and sulfate availability is more
612 significant in compositions with high water/cement ratio and air-entrainer, which is consistent
613 with the XRD results presented here. The effects of confinement on gypsum formation is unclear
614 as confinement causes significant variations on gypsum content without any recognizable
615 pattern.

616

617

<Insert Figure 13>

618

619 Phase composition analysis at different ages are performed to investigate the effects of
620 confinement throughout the attack. Figure 14 shows the evolution of ettringite, gypsum and
621 portlandite content for free and restrained OPC_0.45, OPC+AE_0.45, SRPC_0.45 and OPC_FA
622 samples stored in 30 g/l at 90, 180 and 365 days. These mixtures are selected to cover different
623 magnitudes of free expansions (Figure 6a). Rietveld quantification reveals only slight variations
624 on the total phase content within each composition from 90 days of exposure. Even though the
625 amount of ettringite remains approximately constant, ultrasonic velocity measurements indicate
626 that physical damage increases with time. This could suggest that the amount of ettringite is not
627 an accurate indicator of the damage generated. Instead, the increasing levels of damage measured
628 might be explained by variations in the location of the precipitation promoted by the continuous
629 refinement of the pore network [30].

630

631 The phase contents depicted with clustered columns in Figure 14 (difference between restrained
632 and free specimens) indicate that confined conditions cause a progressive reduction on the
633 amount of expansive phases over time for series OPC+AE_0.45, SRPC_0.45 and
634 OPC+FA_0.45. The composition OPC_0.45 do not follow the same trend due to an unexpected
635 increase on the gypsum content at 180 and 365 days in restrained condition.

636

637

<Insert Figure 14>

638

639 Figure 15a shows ettringite, gypsum and portlandite contents for all compositions stored in low
640 aggressive conditions (3 g/l) at 365 days. The phase content of all phases increases with the
641 water/cement ratio of the composition. However, in this case the amount of expansive phases is
642 considerably reduced due to the lower external sulfate concentration. By lowering the sulfate
643 concentration from 30 g/l to 3 g/l, the average ettringite contents are reduced by 8.1 and 19.2 %
644 in free and restrained specimens, respectively. In the case of gypsum, this reduction increases to
645 36.6 and 48.4 % for free and restrained specimens. The clustered columns indicate that
646 confinement causes a significant reduction of the ettringite content for the series OPC_0.55.
647 However, the other compositions do not show any clear trend, with slight positive and negative
648 variations of the ettringite and gypsum contents. Figure 15b illustrates the evolution of phase
649 composition at 90, 180 and 365 days for series OPC_0.45 stored in 3 g/l. Similarly to the results
650 obtained for this composition in 30 g/l, absolute values of phase content remain approximately
651 constant since 90 days of exposure and the results do not show any clear trend regarding the
652 influence of expansion restraint.

653

654

<Insert Figure 15>

655

656 In general, XRD results indicate that expansion restraint causes a reduction on the amount of
657 ettringite in most of the compositions evaluated. This reduction is more significant in the mortars
658 with high water/cement ratio and air-entrainer (OPC_0.55 and OPC+AE_0.45). However, this
659 trend is unclear for the compositions with lower water/cement ratios (OPC_0.38 and OPC_0.45).
660 Notice that both OPC_0.38 and OPC_0.45 showed the highest influence of confinement
661 according to ultrasonic velocity measurements at 30 g/l (section 3.2.3). For these series, the

662 presence of confining stresses caused a significant increase of ultrasonic velocity and a reduction
663 of physical damage. This behavior was initially attributed to a limited sulfate availability and a
664 lower precipitation of expansive phases in confined conditions. However, the results obtained in
665 this section indicate that the lower damage measured cannot be attributed to a lower precipitation
666 of ettringite and gypsum. Therefore, results suggest that there might be an additional
667 phenomenon acting in restrained specimens that causes the lower levels of deterioration
668 observed.

669

670 3.3.2 SEM AND EDS MICROANALYSIS

671

672 Free and restrained samples of mortar compositions OPC+AE_0.45, OPC_0.55 and OPC_0.38
673 submerged in the high aggressive solution (30 g/l) were evaluated at 365 days. The regions
674 analyzed by EDS are indicated by a red circle in the corresponding image. The relative
675 intensities of each element calculated from the counting are placed on the upper right corner. The
676 peaks considered to measure the intensity of Ca, Si, S and Al correspond to the energies of 3.73,
677 1.78, 2.33 and 1.52 keV, respectively.

678

679 Figure 16 shows the microstructure of porous regions observed in OPC+AE_0.45 for free and
680 restrained configurations. In free expanding conditions, a significant fraction of the visible pores
681 is partially or completely filled with large needle-like ettringite crystals (Figure 16a). The length
682 of those crystals is approximately 10 μm . In restrained conditions, the majority of pores are not
683 filled with any large crystalline structure, giving the appearance of emptiness. However, most
684 pores present a thin layer of poorly crystalline phases covering the pore walls (Figure 16b). EDS

685 analysis in the pore walls reveals the presence of Ca, Si, S and Al, which suggests that small AFt
686 crystals are spread over the pore walls instead of growing into larger structures.

687

688 *<Insert Figure 16>*

689

690 A comparison between the microstructure of free and restrained OPC_0.55 samples also reveals
691 significant differences on the morphology of the crystals formed (Figure 17). In free conditions,
692 large portlandite plates and ettringite clusters are easily observed inside pores (Figures 17a and
693 16b). The arrangement of these phases suggest a simultaneous growth, probably due to the early
694 age when specimens were exposed to sulfates. However, such crystalline formations are not
695 observed in restrained conditions. In this configuration, pores are either empty or filled with a
696 highly amorphous phase covering the pore walls (Figures 17c and 17d). EDS analysis performed
697 in this phase identify mostly calcium. Large ettringite crystals were not found. Highly dispersed
698 needle-like crystals were found mixed with the CSH gel in some regions outside the pores. EDS
699 detected the presence of S and Al at these locations, which might suggest that ettringite is
700 precipitating within the CSH gel.

701

702 *<Insert Figure 17>*

703

704 Similar trends are observed in the composition with lower water/cement ratio (OPC_0.38).

705 Figures 18a and 18b show large amounts of ettringite and portlandite covering the pore walls of
706 the samples in free expanding conditions. As observed in OPC_0.55, both phases present well-
707 defined structures and seem to be growing simultaneously (Figure 18b). For this composition,

708 some pores with similar hydration products were also found in restrained conditions (Figure
709 18c). However, a magnification of the crystals covering the pore walls depicts smaller structures
710 with lower degrees of crystallinity than the ones observed in free conditions (Figure 18b).

711

712 *<Insert Figure 18>*

713

714 3.3.3 DISCUSSION OF SEM RESULTS

715

716 Results of the SEM analysis suggest that size and degree of crystallinity of phases formed during
717 ESA might be affected by expansion restraint. In the same way a structure element deforms after
718 the application of an external stress, when a crystal is subjected to stresses it might change its
719 dimensional configuration by precipitation and dissolution mechanisms until equilibrium is
720 reached with the surrounding media. Some authors studied different aspects related to the effects
721 of pressure on crystal growth caused by salt crystallization between pore walls [31-34]. The
722 theoretical framework developed by M. Steiger [32,33] is used here to assess the influence of
723 externally generated confining stresses due to expansion restraint on crystal development.

724

725 When a crystal grows in directions in which growth is opposed by external forces, free and
726 loaded faces of the crystal present different values of chemical potential. According to [35], the
727 chemical potential of a crystal face under pressure p (μ_p) can be expressed as indicated in Eq. 5
728 when elastic behavior is assumed. The contribution of the molar strain energy of a deformed
729 crystal is neglected since the pressure difference between free and confined specimens is below
730 100 MPa [32,35].

731

$$\mu_p = \mu_0 + pV_m \quad (\text{Eq. 5})$$

732

733 In this equation, μ_0 is the chemical potential of the solid in the unstressed reference state and V_m
734 is the molar volume of the solid in the stressed state. This equation shows that the loaded faces of
735 a crystal have higher chemical potentials than unloaded faces. On the other hand, the chemical
736 potential of the salt in the solution (μ_l) increases with the ion activity of the solute (K) in the pore
737 solution (Eq. 6). The term μ_l^0 refers to the chemical potential in the standard state.

738

$$\mu_l = \mu_l^0 + RT\ln(K) \quad (\text{Eq. 6})$$

739

740 Both loaded and unloaded faces of a crystal seek equilibrium with the surrounding pore solution.
741 Therefore, as indicated in Eq. 7, the chemical potential of the solute must be equal to the
742 chemical potential of the respective crystal face.

743

$$\mu_0 + pV_m = \mu_l^0 + RT\ln(K) \quad (\text{Eq. 7})$$

744

745 Eq. 7 shows that when a pressure is introduced to the crystal, the solubility of that crystal
746 increases to balance the increase on chemical potential produced by the pressure. This
747 phenomenon is sometimes referred to as “Riecke’s principle”. It states that the crystal solubility
748 increases with the pressure applied. According to this principle and assuming that the pressure
749 caused by the steel rings is transferred to the crystals growing in confined conditions, crystals
750 formed in restrained samples should exhibit higher solubility than those in free expanding
751 conditions. If the pressure is anisotropic, the dissolved material may then be redeposited on those

752 parts of the crystal exposed to lower pressures. This phenomenon should cause crystals with
753 smaller sizes and lower degrees of crystallinity in restrained specimens.

754

755 However, as indicated in section 3.1, the confining stresses generated by the steel rings are below
756 5 MPa. Such low stresses may not be able to cause significant effects on the solubility of the
757 phases precipitated, as stresses in the order of 20 MPa are necessary to increase 20 % the
758 solubility of NaCl crystals at 25 °C [32]. According to M. Steiger [32], the increase of solubility
759 due to an increase of pressure (Δp) can be estimated by Eq. 8. In this equation, the term K_0
760 corresponds to the ion activity product of the saturated solution.

761

$$\ln\left(\frac{K}{K_0}\right) = \frac{\Delta p V_m}{RT} \quad (\text{Eq. 8})$$

762

763 Figure 19 presents the equilibrium curve of the solubility increase produced by pressures
764 between 0 – 5 MPa in ettringite, gypsum and portlandite crystals at 25 °C. The molar volumes
765 considered for those phases are 707, 75 and 33 cm³/mol, respectively [28]. Ettringite depicts a
766 significant increase of solubility within the pressures evaluated. The solubility at 5 MPa of
767 pressure is 4.2 times the reference solubility in the absence of load, which indicates that ettringite
768 is very sensitive to the range of pressures applied. This phenomenon could promote a decrease of
769 large ettringite crystals in restrained conditions. For the other phases considered, the influence of
770 stresses up to 5 MPa on the solubility is minimum.

771

772 The high supersaturation needed to counteract the effects of pressure might alter the balance
773 between crystal growth and nucleation rate around the ettringite crystals growing in confined
774 conditions. According to [36], the rate of nucleation (I) can be expressed as indicated in Eq. 9.

775 This equation has been simplified by grouping all the parameters other than supersaturation into
776 the positive coefficients A and B. Large K/K_0 leads to rapid nucleation of ettringite. Therefore, a
777 local increase of solubility might promote ettringite nucleation over crystal growth in those
778 regions where ettringite is mainly growing in confined conditions, ultimately resulting in smaller
779 crystals distributed over a large surface.

780

781

<Insert Figure 19>

782

$$I = A \exp \left[\frac{-B}{(\ln(K/K_0))^2} \right] \quad (\text{Eq. 9})$$

783

784 The crystallization pressure theory states that the crystals must be confined in order to exert
785 pressure. Therefore, the expansive stress generated in a specimen depends on the volume fraction
786 of crystals growing in confined conditions [34]. The smaller crystal size distribution of ettringite
787 caused by its increased solubility in the restrained specimens might reduce the fraction of
788 crystals growing in confined conditions and thus, the amount of crystals exerting pressure. This
789 phenomenon, together with the lower presence of ettringite, could explain the low confining
790 stresses measured and the reduced damage observed in specimens under restrained conditions.
791 However, further experimental research is needed to link the theoretical framework developed
792 here and the trends described by the SEM images of section 3.3.2, as it was not possible to
793 compare images of ettringite crystals growing in confined conditions for free and restrained
794 specimens.

795

796 **4. CONCLUSIONS**

797

798 The results presented in this paper indicate that the confining stresses alter the normal
799 development of the ESA by reducing the potential damage generated. The following specific
800 conclusions may be derived from this study.

801

802 (1)- The level of stress generated by the attack in confined samples exposed to accelerated ESA
803 is significantly smaller than the stresses predicted considering the free expansions of equivalent
804 unconfined samples. Such difference confirms the important role of the confinement in the
805 outcome of the attack and raises questions about the representativeness of the accelerated
806 laboratory tests conducted under unconfined conditions. The numerical simulation of the
807 structural repercussion of the ESA obtained by applying free expansion in structural models
808 should also be questioned since it is likely to bring higher stresses than expected in reality in case
809 confinement exists.

810

811 (2)- Results of mass variation suggest that the ionic transport process between external and pore
812 solutions is reduced in confined conditions. This behavior might be explained by the lower
813 micro-cracking generated, which decreases the penetration paths and reduces the sulfate
814 concentration in the pore network.

815

816 (3)- The evolution of the ultrasonic velocity confirms that confined specimens present denser
817 matrices and lower presence of micro-cracks than equivalent unconfined specimens.

818

819 (4)- In general, XRD results indicate that the confinement causes a reduction on the amount of
820 expansive phases precipitated, especially in compositions with high water/cement ratios and air-

821 entrainer. The lower precipitation observed might be explained by the reduced availability of
822 sulfates in confined conditions.

823

824 (5)- The theoretical framework formulated to explain the effects of confinement on the
825 morphology and arrangement of the crystals formed suggests that confinement might increase
826 the solubility of ettringite and promote a spread nucleation of small crystals in those regions
827 where ettringite growth is restrained. These phenomena might reduce the amount of crystals
828 growing in confined conditions and thus generating pressure, which may contribute to explain
829 the lower stresses generated by the attack in the confined specimens. Further experimental
830 evidences are needed to validate this hypothesis.

831

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833

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837

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