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Friction and Fracture Characteristics of Engineered Crumb-Rubber Concrete at Microscopic Lengthscale

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Abstract

Using small-scale depth-sensing techniques, we shed light on the determinants of friction and hardness in engineered crumb rubberreinforced concrete with applications into railway sleeper ties. Microscopic scratch tests were carried out to assess the hardness, friction and fracture behavior of concrete specimens reinforced with crumb rubber inclusions. Optical microscopy and scanning electron microscopy are utilized to identify the micro-constituents. The partial replacement of aggregates with crumb rubber particle leads to an increase in the friction coefficient and the fracture toughness and a slight decrease in strength properties. Our research suggests that the crumb rubber particle specific area may play a role in dictating the levels of enhancement in friction coefficient. In addition, improper bonding at the cement/rubber interface is shown to result in poor strength characteristics. Furthermore, crumb rubber particles contribute to a higher durability as evidenced by sustained high values of the friction coefficient even in presence of surface lubrication with water or oil. Overall our study highlights the beneficial role of crumb rubber on the friction and fracture behavior while emphasizing the need for more research into the effect of specific surface area and interface bonding. *Keywords:* crumb-rubber concrete, Scratch tests, Hardness, Friction, Fracture Toughness

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1. Introduction

Crumb rubber concrete is an alternative way to reuse rubber waste and prevent pollution of the environment [1]. Up to 12 million tons of rubber waste are disposed annually in both the US and Europe [2, 3]. Recycling rubber into advanced construction materials provides a way to alleviate the pressure to landfills. A byproduct of the petroleum engineering industry, tire wastes are estimated at 75 million tons per year in the United States alone [4]. Tire wastes are problematic because (i) they are non-biodegradable, (ii) they require a significant amount of space, (iii) they pose a fire hazard [5], and (iv) they serve as a breeding ground for mosquitoes and larvae. A highly-explored strategy to recycle waste tire consists in embedding crumb rubber in cement mixtures for structural applications such as railway concrete sleepers [6, 7], asphalt pavements [8], or precast concrete [9].

Although previous studies have focused on the strength characteristics of rubber-reinforced concrete [5, 10], the friction characteristics have received little attention. For instance, Liu *et al.* recorded the mechanical and durability properties of the crumb rubber concrete from the macro level [2]. A negative correlation was observed between the compressive strength and the rubber content [11]. Taha *et al.* investigated the mechani-

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24	cal and fracture properties of rubber concrete using quasibrit-	(
25	tle fracture mechanics models. They concluded to the exis-39	(
26	tence of an optimal replacement ratio for tire rubber particles 80	
<mark>27</mark>	to enhance fracture toughness without compromising strength ₆₁	
28	[12], Ganesan <i>et al.</i> studied the flexural fatigue behavior of $_{62}$	1
29	self-compacting shredded rubber concrete and showed that a_{63}	1
30	(15 percentage or 20 volume percentage replacement of rubber) ₆₄	1
<mark>31</mark>	would significantly improve the distribution of the fatigue life. 85	(
32	[13]. Ganesan <i>et al.</i> studied the strength and durability char-	(
33	acteristics of self-compacting rubberized concrete with or with-	
34	out steel fibers. They found that the addition of steel fibers can $_{68}$	1
35	compensate the loss of strength due to by rubber addition [14]. $_{69}$	
<mark>36</mark>	Nevertheless, in the aforementioned studies, the rheological be- $_{70}$	1
37	(havior was not considered.) The impact of tire particle/cement ⁷¹	1
38	matrix bonding was not studied. Finally, the effect of surface 72	1
39	treatment on the mechanical performance was not investigated. 73	;
40	As friction and wear are important measures of the durability 74	
41	of railway tracks, new studies are needed. To this end, we rely 75	;
42	on micro-rheology tests such as scratch testing to gain a funda-	
42 43	on micro-rheology tests such as scratch testing to gain a funda- ⁷⁶ mental understanding at the micro- and meso-scale.	
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ture of cement hydration products [17, 18, 19]. Herein, we select constant-load and progressive-load scratch testing for its accuracy, reliability and rigor.

Scratch tests consist in pushing a sharp diamond probe across the surface of a weaker material. Scratch tests are frequently used to characterize the friction behavior of metals, polymers, thin films, coatings, and ceramics [20, 21, 22, 23, 24]. Very recently, scratch tests have been applied to characterize the tribology of cementitious materials and geomaterials, which exhibit a large degree of heterogeneity [25]. To our knowledge, scratch tests have not yet been applied to crumb rubber-reinforced concrete. A major challenge is the large range of scale between the whole concrete at the meso and macroscopic scale and the micro-constituents at the microscale. Herein, we apply fracture analysis, strength and hardness relationships, and friction analysis to scratch testing in order to understand the tribological behavior of crumb-rubber concrete at different length-scales and under different loading conditions and surface treatment options.

2. Materials and Methods

Four different types of crumb-rubber reinforced concrete were synthesized at the Birmingham Centre for Railway Research and Education at the University of Birmingham. The mix design is summarized in Table. 1. Mix 1 is the control material, which consists of cement, water, fine aggregate, and coarse aggregate. Table 2 provides the gradation of the aggregates used in this study. In order to compensate for the potential loss in mechanical resistance due to the addition of crumbrubber particles, fume silica was introduced in Mix 2–4 at a reason of 10% in weght with respect to the mass of fine aggregates. Mix 2 was reinforced with silica fume whereas both Mix 3 and Mix 4 were reinforced with rubber with a mass fraction of respectively 5% and 10% with respect to the mass of fine

Material	Cement (kg)	Water (kg)	Fine Aggregate (kg)	Coarse Aggregate (kg)	Silica fume (kg)	Rubber (kg)
Mix 1	530	233	630	986	0	0
Mix 2	477	233	630	986	53	0
Mix 3	477	233	599	986	53	32
Mix 4	477	233	567	986	53	63

Table 1: Design of crumb-rubber reinforced concrete systems considered in this study.

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Serial no.	Sieves	% re-	Cumulative	e % fine
	(mm)	tained	retained	
1	20	0	0	100
2	16	0	0	100
3	10	21	21	79
4	6.7	67.5	88.5	11.5
5	4.75	9	97.5	2.5
6	Base	2.5	100	0

 Table 2: Aggregate Gradation Table

Properties	Specification	Unit	106
SiO ₂	>90	%	107
Retention on 45 μ m	<1.5	%	108
sieve			109
H_2O (when packed)	<1.0	%	110
Bulk Density (U)	200 - 350	kg/m^3	111
Bulk Density (D)	500 - 700	kg/m^3	112
			113

Table 3: Chemical and Physical Properties of Silica Fume

aggregates. Silica fume, grade 940 was utilized for Mix 2–4 with the chemical and physical properties of silica fume given in Table-3. Two different sizes of crumb rubber were used: 425 μ m with a specific gravity of 1.14 ±0.02 for Mix 3, and 75 μ m with a specific gravity of 1.14±0.03 for Mix 4. For each design, 5.5-in.×2-in.×1-in. specimen blocks were manufactured. The specimens were subsequently aged for 28 days prior to microscopic examination and testing.

99 2.1. Material Preparation

In order to ensure accurate measurements, a rigorous specimen preparation procedure was devised so as to yield a low surface roughness relative to the maximum penetration depth [26]. The specimens were machined using a top-table bandsaw and later embedded under vacuum in an epoxy resin. A linear-precision diamond saw was later utilized to yield 5-mm thick cylindrical specimens with rigorously flat top and bottom faces. The resulting specimens were mounted onto metal disks using cyano-acrylate adhesive. The mounted specimens were then ground and polished using a semi-automatic grinder/polisher. Grinding occurred using silicon carbide abrasive discs of different gradations, consecutively 240, 400, 600, 800, and 1200. Afterward, polishing took place using colloidal suspensions of polycrystalline diamond with particle size consecutively 3 μ m, and 1 μ m. In between each steps of the grinding and polishing phases, the specimens were rinsed in N-Decane using an ultrasonic bath. The quality of the polished

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surface was assessed via optical microscopy and surface pro-150
filometry. After grinding and polishing, the specimens were151
stored in a vacuum desiccator at room temperature to prevent152
water-induced degradation[27].

121 2.2. Micro-structural Characterization

Scanning electron microscope (SEM) was used to image 122 the polished crumb-rubber cement specimens. A JEOL JSM-123 6060LV Low Vacuum Scanning Electron Microscope (SEM) 124 was utilized at the Frederick Seitz Materials research Labora-125 tory with an accelerating voltage of 15-20 kV and a working 126 distance of 10 mm. Fig.1 displays representative SEM images 127 for Mix 3. A matrix-inclusion micro-structure is observed. The 128 matrix phase is hardened cement whereas the inclusions consist of aggregates and rubber particles. The aggregate particles (light grey) are 200–2000 μ m in size. In particular, imperfect oonding is observed between the rubber particles and the sur-166 rounding hardened cement matrix. 167

134 2.3. Scratch Testing

Constant load scratch tests were applied to characterize the 135 hardness and friction properties. All tests were conducted using 136 a Micro Scratch Testing equipment (MST), that was compliant 137 172 with the standards ASTM G171, ASTM D7187, and ASTM 138 173 D7072 [28, 29]. The equipment featured a load resolution of 139 0.01 mN and a depth resolution of 0.05 nm. The scratch testing 175 unit was integrated with a high-resolution video microscope to 141 176 allow the precise positioning of the test. As shown in Fig. 2, in 142 our experiments, a sphero-conical diamond stylus was pushed 143 across the surface of the material while applying a constant or 144 linearly increasing vertical force. In all tests, a Rockwell C¹⁷⁸ 145 probe was used, characterized by a tip radius $R = 200 \,\mu\text{m}$ and 179 a half-apex angle $\theta = 60^{\circ}$. The scratch probe was accurately 147 measured using scanning confocal microscopy. Prior to testing, the specimen surface profile was measured via a surface 149

scan using a contact load of 3 mN. During the test, continuous stiffness measurement was utilized to record the forces and the penetration depth in real time along the scratch path. At the end of each test, a panorama image of the residual top surface was captured. In this study, the temperature was held constant at 72 ± 2 °F, the testing took place under an acoustic enclosure, and the scratch probe was thoroughly cleaned prior to each tests to prevent debris accumulation.

Table 4 displays the scratch parameters used in this study. A total of 304 scratch tests were performed following eight different protocols. We carried out both meso-scale tests, with a constant load of 15 N, and microscale tests, with a constant load of 1 N. In addition, for progressive-load testing, the vertical force was linearly increased from 0.1 N to 2 N. The meso-scale tests were carried out to assess the effective behavior of each mix (Protocol P1) as well as the influence of surface treatment (protocols P2 and P3). Fracture scratch tests (protocol P4) were performed to evaluate the fracture toughness of each mix design. For protocols P1–P4, the location was selected randomly within a given material specimen, Mix 1–4. In contrast, for protocols P5–P9, in-situ optical microscopy was utilized to select an aggregate, silica, rubber particle or a cement matrix space. Microscale scratch tests (protocols P5 and P6) were performed to measure the contribution of each micro-constituent- aggregate, micro-silica, cement paste, and rubber-to the overall behavior. Finally, we investigated the effect of loading rate and scratching speed on the measured scratch hardness and friction coefficient (protocols P7-9).

3. Theory

3.1. Friction and Hardness

Table 4 defines the mathematical notations employed in thisstudy.The friction and hardness were analyzed following

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Figure 1: a) Scanning Electron Microscope images of crumb-rubber concrete cement Mix 4 to identify the micro-constituents. The particle identified are aggregate and silica fume inclusions, in light grey, and rubber, in black.

Protocol	Р	V	X	Surface Lubricant	System
P1	15	6.0	3	None	Mix 1–4
P2	15	6.0	3	Deionized Water	Mix 1–4
P3	15	6.0	3	Oil	Mix 1–4
P4	0.1–2.0	6.0	3	None	Mix 1-4
P5	1	0.2	0.1	None	Rubb.
P6	1	2.4	0.2	None	Agg., Cem., Sil.
P7	0.1	2.4	0.2	None	Agg.
P8	1	0.4	0.2	None	Agg.
P9	0.1	0.4	0.2	None	Agg.

Table 4: Scratch protocols for our study. A total of 304 scratch tests was carried out. P is the prescribed vertical load in N. V is the scratch speed in mm/min, X is the scratch length in mm. Agg. = aggregate. Cem. = cement paste. Sil. = silica.



Figure 2: a) Digital photograph of a scratch test. Credits: Ange-Therese Akono, Pooyan Kabir, UIUC, 2016. b) Constant-load scratch test. c) Progressive-load scratch test. d) Scratch probe geometry. *d* is the penetration depth, F_T is the horizontal force, and *P* is the vertical force. *R* is the probe tip radius, meanwhile θ is the half-apex angle and *w* is the scratch width.

Mathematical symbol	Physical meaning
Α	horizontally-projected load-
	bearing contact area
β	Weibull shape parameter
d	Penetration depth
$\Delta \phi$	Increase in porosity due to
	improper bonding
d_t	scratch probe transition
	depth
F_T	Scratch horizontal load
Н	Hardness
l _r	rubber inter-particle dis-
	tance
K_c	Fracture toughness
μ	Apparent friction coefficient
η	Weibull scale parameter
Р	Scratch vertical load
р	perimeter
R	Probe tip radius
r	size of rubber particles
t	thickness of rubber particles
heta	Half-apex angle of probe
V	Scratch speed
W	Scratch width
X	Scratch path
ϕ_r	volume content rubber

Table 5: Description of the mathematical symbols used in thisstudy.

ASTM G171-03 [29]. In turn, the scratch hardness provides in- $_{188}$ formation regarding the material strength characteristics [30]. $_{189}$ The scratch hardness was computed as the ratio of the applied $_{190}$ constant vertical force *P* to the vertically projected contact area; $_{191}$

$$H = \frac{P}{\frac{\pi}{8}w^2} \tag{1}$$

In this study, the vertically projected area, $\pi/8w^2$ is calculated from the scratch width. In turn, the scratch width *w* is calculated from the measured penetration depth as:

$$w = \begin{cases} 2\sqrt{R^2 - (R - d)^2} & d \le d_t \\ 2(d - R(1 - \sin\theta))\tan\theta + 2R\cos\theta & d \ge d_t \end{cases}$$
(2)¹⁹⁷

Herein *d* is the penetration depth that is recorded in real time using high-accuracy sensors, *R* is the probe tip radius, and θ is the probe half-apex angle. In particular, $d_t = R(1 - \sin \theta)$ is the scratch probe transition depth from the spherical into the conical domain. Analogously, the friction coefficient μ is defined as the ratio of the horizontal force F_T to the vertical force *P*:

$$\mu = \frac{F_T}{P} \tag{3}^{200}$$

180 *3.2. Fracture Analysis*

Nonlinear fracture mechanics was employed to relate the hor-²⁰⁹ izontal force F_T to the fracture toughness K_c [31, 32, 33]:²¹⁰

$$K_c = \frac{F_T}{\sqrt{2pA}} \tag{4}^{212}$$

Where,
$$2pA$$
 is the probe shape function that depends on the²¹⁴
geometry of the scratch probe as well as the penetration depth²¹⁵
 d [32, 31]. In our tests, the function $2pA(d)$ was calibrated²¹⁶
using a reference materials as described in [32]. d is the pene-²¹⁷
tration depth, which is measured using high-accuracy sensors.²¹⁸
The theoretical model is derived in details in [31, 32, 33] using²¹⁹
the *J*-integral, the energetic size effect law, and computational²²⁰

fracture mechanics. In particular, the method was validated on polymers, ceramics, and metals [31] and has been applied to characterize the fracture behavior of a wide range of materials including but not limited to cement-polymer composites [34], rocks and cement paste [35], and organic-rich shale [36]. Herein, we apply the scratch fracture method to understand the influence of crumb rubber reinforcement on the fracture behavior.

4. Results

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4.1. Individual Test Results

3 illustrates the analysis procedure from individual Fig. constant-load and progressive-load scratch tests. For instance, consider a single scratch test carried out under a constant vertical load of 15 N. Given the continuous stiffness measurement system, the forces—horizontal F_T , and vertical P—as well as the depth d are recorded every 3 μ m. Fig. 3 a) displays the continuous evolution of the force and depth profiles along the scratch path X. The depth profile d yields the width profile using Eq. (2). In turn, the width can be utilized to compute the hardness along the scratch path using Eq. (1). The force measurements can also be used to compute the friction coefficient μ as shown. Due to the heterogeneity of the specimen— consisting of hardened cement paste, aggregates, silica fume, and crumb rubber-, large variations occur along the scratch path for both the hardness and the friction. In particular, the maximum penetration depth oscillates between 52 μ m and 95 μ m; the hardness varies between 0.20 and 0.47 GPa, and the the friction coefficient varies between 0.06 and 0.56. Thus, each individual constant-load test yields 1,000 independent measurements of the friction coefficient μ and of the scratch hardness H.

Similarly, Fig. 3 b) displays the force and depth measurements recorded during a progressive-load test with a maximum vertical force of 2 N. In turn, the penetration depth increases up



Figure 3: a) Friction and hardness analysis from a single constant-load tests with a constant vertical force equal to 15²⁴⁷ N. b) Fracture toughness analysis from a progressive-load individual test with a maximum vertical force of 2 N. Tests on ²⁴⁹ crumb-rubber Mix 3.

²²¹ to 4.6 μ m. By application of Eq. (4), the fracture toughness ²²² can be estimated along the scratch path: K_c oscillates around ²²³ a mean value of 0.55 MPa \sqrt{m} with a standard deviation of ²²⁴ 0.2 MPa \sqrt{m} . Thus,each individual progressive-load test yields ²²⁵ 1,000 independent measurements of the fracture toughness K_c .

4.2. Effect of Scratch Speed and Normal Load

From a method development perspective, it is important to understand the influence of the prescribed normal load and scratch speed on the measured friction coefficient. Similarly, from an application standpoint, different train loads and speed will result in different rates and levels of mechanical loads applied locally. Thus we carried out a set of constant-load scratch tests on the aggregate phase at two different speeds, 400 mm/min and 2400 mm/min, and two different load levels: 0.1 N, and 1 N, following protocols P 6–9 in Table 5. For simplicity, we focused on a single micro-phase: aggregate. Fig. 4 the frequency distribution of the scratch friction coefficient μ and of the scratch hardness *H* for both load levels and scratch speeds.

On the one hand, the scratch load alters the shape of the frequency distribution and the median value of the friction coefficient. In particular, a very small increase-only 16% -of the friction coefficient is recorded when the normal load is multiplied by 10. The dependency of the friction coefficient on the applied normal force is similar to AFM-based friction tests carried out by Bhushan et al. on polished silicon, silica, and diamond [37] with nanoscale normal loads. This increase of the friction coefficient with the normal load at the nanoscale is commonly attributed to ploughing. On the other hand, the shape and the and the median value of the frequency distribution is not altered when the scratch speed is increased by 500 %. In the scientific literature, the influence of sliding speed on friction has been linked to the viscoelastic behavior for polymers [38, 39, 40] and rocks [41, 42]. In this case a rate-independent behavior is observed for the friction coefficient showing that for

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Figure 4: Effect of the normal load and scratch speed on frequency distribution of the friction for aggregate phase. (Color online)

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the timescales and length-scales of our experiments, and for the²⁷³ aggregate phase, the visco-elastic energy dissipation is negli-²⁷⁴ gible compared to friction-induced energy dissipation. Thus,²⁷⁵ in what follows, we can consider the friction coefficient to be²⁷⁶ invariant with respect to the loading rate and scratch speed. ²⁷⁷

260 4.3. Influence of Individual Micro-constituents

Protocols P4 and P5 were followed to measure the friction₂₈₀ 261 and hardness properties of individual micro-constituents: ag-262 gregate, silica, hardened cement paste, and rubber. The micro-281 263 constituent were selected randomly and tested within speci-282 264 mens from all four mixes Mix 1-4 using optical microscopy.283 265 Fig. 5 displays the frequency distribution for both the friction₂₈₄ 266 coefficient and the coefficient hardness. For aggregate, silica,285 267 and hardened cement paste, the frequency distribution of the286 268 friction coefficient exhibits a single peak whereas the frequency287 269 distribution of the hardness exhibits several peaks. This differ-288 270 ence points to the different nature of hardness-characteristic of289 271 strength [30, 43]— and friction. Strength dissipation is due to290 272

bulk plastic dissipation taking place inside the probed volume element whereas friction dissipation is due to the interaction of asperities at the surface. As a result, the hardness is primarily influenced by the composition and the morphology whereas friction is primarily driven by the topology of the surfaces in contact. Thus, the different peaks in the hardness frequency distribution is caused by different types of aggregates, silica inclusions, and different cement hydration products.

We can rank the micro-constituents according to the average friction coefficient: in descending order, rubber, cement paste, silica, and aggregate. Friction is promoted in hardened cement paste due to the presence of nanopores, micropores, along with grains boundaries for the cement hydration products. As for silica, its particulate nature–with a particle size ranging from — promotes asperities at the inclusion boundaries. Finally, rubber presents an intrinsically textured surface. This textured surface, coupled with the bimodal particle distribution—with average 75 μ m and 425 μ m explain the broad range of the resulting fric-



Figure 5: Friction and Hardness of Individual micro-constituents. (Color online)



Figure 6: Frequency distribution of the friction coefficient μ for₃₂₁ all four mixes, Mix 1–4. (Color online)

tion coefficient. In turn, the micro-constituents can be ranked
 according to their hardness, in ascending order: rubber, cement
 paste, silica, and aggregate. The reverse order between fric tion and hardness suggests a compromise between friction and
 strength, as characterized by the hardness.

296 5. Discussion

297 5.1. Synergistic Effects on Friction

Fig. 6 shows the impact of fume silica and crumb-rubber³³² 298 addition on the friction coefficient. The frequency distribu-333 299 tion of the friction coefficient is represented for constant-load³³⁴ 300 scratch tests carried out on materials Mix 1-4 following proto-335 301 col P1. On the one hand, looking at each curve, separately, we³³⁶ 302 observe a synergistic effect. For instance, Mix 1 exhibits val-337 303 ues of the friction coefficient greater than 0.5 whereas its basic338 304 constituents-hardened cement paste, silica, and aggregate-339 305 are characterized by values of the friction coefficient strictly₃₄₀ 306 less than 0.3, cf. Fig. 6 b), c), d). In other words, due to the₃₄₁ 307 high heterogeneity and the large local variations in morphol-342 308 ogy, the effective friction coefficient is significantly higher than₃₄₃ 309 that of each microphase considered individually. On the other₃₄₄ 310

hand, we note that the frequency distribution is altered by the presence of silica fume and crumbed-rubber. Finally, each frequency distribution curve presents multiple peaks, which are evidence of a discrete range of friction mechanisms.

Table 6 displays the average values of the friction coefficient for constant-load tests under dry conditions for all four mix designs. The friction coefficient μ increases by 1% when fume silica (Mix 2) is added to plain concrete. μ increases by 10% when 75-µm crumb-rubber particles are added at a volume fraction of 5% (Mix 3). Finally, μ increases by 7% when 425- μ m crumb-rubber particles are added at a volume fraction of 10% (Mix 4). Although Mix 3 and Mix 4 represent an improvement in terms of friction coefficient with respect to Mix 1 and Mix 2, the increase in the value of the friction coefficient is not proportional to the volume fraction of crumb rubber. The reason is that friction is a surface phenomenon, as a result, the relevant variable is the specific area *a* of rubber particles. Assuming a statistically uniform dispersion, we have $a \propto \phi_r r^2$ where ϕ_r is the rubber volume content and r is the size of rubber particles. In particular, when comparing Mix 3, and Mix 4, the rubber particles in Mix 3 are in average 5.6 times larger than those in Mix 4; whereas the volume content of Mix 4 is only twice that of Mix 3. Thus, Mix 3 exhibits a specific are which is 15.7 times greater than that of Mix 4, which explains why the increase in friction coefficient is greater for Mix 3 than for Mix 4. Thus, the enhancement in friction coefficient is a function of the specific crumb rubber particle area.

Nevertheless, rubber reinforcement adversely impacts the strength properties. As seen in Table 6, although the average value of the scratch hardness increases by 46% after addition of 10% wt microsilica, a subsequent decrease of 20% and 16% in scratch hardness is recorded after further addition of respectively 5% wt and 10% wt of crumb rubber particles. Similar results have been reported in the literature: a loss in compressive

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Property	Mix 1	Mix 2	Mix 3	Mix 4
H, MPa	473.7	690.3	549.08	580.2
μ	0.270	0.273	0.297	0.289
K_c ,	0.34	0.44	0.47	0.38
MPa \sqrt{m}				
η	0.40	0.51	0.54	0.42
β	2.15	4.04	2.42	3.18

Table 6: Influence of crumb rubber content and fume silica content on aggregate mechanical characteristics. *H* is the scratch hardness, μ is the friction coefficient, and K_c is the fracture toughness. Moreover η and β are the Weibull scale and shape distribution parameters.

strength was observed after partial replacement of aggregates 345 by crumb rubber in self-compacting concrete [14, 44]. Further-346 more, the strength loss was positively correlated to the volume 347 content of rubber [44]. However, in our case, due to imperfect 348 bonding between the rubber particles and the surrounding hard-349 ened cement matrix, additional air voids where incorporated in 350 the mix as seen in Fig. 1 b). This increase in porosity $\Delta \phi$ due 351 to improper bonding is proportional to the rubber particle size r352 and the rubber volume content ϕ_r : $\Delta \phi \propto 2\pi r t \phi_r$, where t is the 363 353 thickness of rubber particles. As a result, the relative increase364 354 in porosity due to improper bonding is 2.5 times greater for Mix365 355 3 than for Mix 4. Therefore, the additional porosity due to im-366 356 proper bonding explains the slightly lower scratch hardness of 367 357 Mix 3 compared to Mix 4. Nevertheless, the joint addition of 368 358 fume silica and crumb-rubber results in an overall increase in₃₆₉ 359 scratch hardness of more than 15 % compared to the reference370 360 mix, plain concrete (Mix 1). 371 361

362 5.2. Mesoscale Fracture Behavior

Fig. 7 displays the frequency distribution of the fracture₃₇₄ toughness for all specimens. The scratch-based fracture tests₃₇₅



Figure 7: Frequency distribution of the fracture toughness K_c for all four materials. (Color online)

were carried out following protocol P 4, and the results were analyzed using Eq. (4). In addition, for each specimen the frequency distribution was evaluated based on the population consisting of all measurements for all scratch tests performed. A two-parameter Weibull distribution was adopted to fit the frequency distribution function of the fracture toughness K_c according to:

$$f(x) = \frac{\beta}{\eta} \left(\frac{x}{\eta} \right)^{\beta - 1} \exp\left(- \left(\frac{x}{\eta} \right)^{\beta} \right)$$
(5)

where *f* is the probability distribution function of the variable $x \equiv K_c$, η is the scale parameter and β is the shape parameter. Table 6 lists the values of the scale and shape parameters, η and β , as well as the average value of the fracture toughness K_c . Both the scale parameter η and the shape parameter vary for different mix design: in other words, the mix design influences the frequency distribution of the fracture resistance. The addition of fume silica and crumb-rubber contributes to shifting the frequency distribution curve towards high values.

The average fracture toughness K_c increases by 29% by addition of microsilica, and by 38% and 12% after subsequent addition of respectively 5% and 10% crumb rubber. Our findings concur with that of other scientists who reported an en-

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hancement in fracture resistance after addition of crumb rub-410 ber particles [12]. The gain in fracture resistance is commonly411 attributed to the intrinsic ductility of rubber particles as well412 the presence of toughening mechanisms such as crack ligament413 bridging, which are promoted by the presence of rubber parti-414 cles.

5.3. Influence of Surface Lubricant or Resistance to Weather ing

In railway applications, a major concern is to appraise the 384 419 durability of materials in harsh environmental conditions: wet 385 420 due to water (rain, snow) or oil (leaking from an engine). Thus, we assessed the the influence of lubricant on the surface proper-387 ties via surface lubrication with oil and deionized water as per 388 protocols P 2–3. Fig. 8 displays the distribution of the friction 389 424 coefficient for all four mixes and for all three surface conditions: 390 425 dry, wet with oil, and wet with water. In addition, cluster analy-391 426 sis was implemented to decompose the overall probability dis-392 427 tribution of the friction coefficient as a weighted sum of individ-393 ual Gaussian distributions [45, 46]. Herein, each single Gaus-394 429 sian distribution represents a specific friction micromechanism. 395 Friction is a surface phenomena that results from the interlock-396 431 ing of surface asperities. A the microscopic and nanoscale, 397 friction depends on a wide range of parameters such as asper-398 433 ity density, asperity radius of curvature, contact shear strength, 399 contact junction plastic yield strength, etc. [47]. We opt for 400 435 a discrete representation of this continuum of friction-inducing 401 micromechanisms using cluster analysis and multivariate mix-402 ture analysis [45, 46]. Section 7 in the Appendix displays the 403 weights and average friction coefficient of each individual mi-404 cromechanisms, whereas the corresponding probability distri-405 bution curves are shown in Fig. 8. 406

Without crumb rubber, high-net-friction micromechanisms are curbed due to chemical reactivity. For instance, for the reference specimen, Mix 1 without crumb rubber, friction mi-442 cromechanisms with a net average friction coefficient of 0.45 and above are drastically suppressed after surface wetting with oil or deionized water. This drastic reduction in high-netfriction mechanisms is even more noticeable for surface treatment with deionized water. A plausible reason is the interaction of water molecules with hardened cement paste. Surface water may activate a further hydration of cement paste, seep into the cement paste micropores and nanopores, locally increase the pore pressure and generate additional microcracking. As a result of the interaction between cement paste and water, local topological features such as asperities may be masked, resulting in a smoothing of the surface. A similar phenomenon is observed for Mix 2 (conc+silica) when the surface is wet with water. In this case, the water will contribute to sub-critical cracking of silica via stress corrosion cracking [48].

In contrast, crumb rubber inclusions promote the rise of highnet-friction micromechanisms. For Mix 3 (conc+silica+5% wt rubber), friction micromechanisms with a net average friction coefficient greater than 0.5 are still active in presence of oil or water. As a result, for Mix 3, higher values of the friction coefficient were recorded in presence of water and oil. One reason is the chemical inertia of rubber with respect to water and oil which contributes to an enhancement of local asperities. Mix 4 (conc+silica+10% wt rubber) experiences a sharper decrease of the friction coefficient when the surface is treated with oil. This might be due to the smaller specific surface are R_a of the crumb rubber. nevertheless, overall the partial replacement of aggregates with crumb rubber contributes to a higher resistance to weathering and an improved stability of surface friction properties with respect to surface treatment with a lubricant.

6. Conclusions

To understand the tribological behavior of crumb-rubber concrete, scratch testing has been applied at different length-scales,

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Figure 8: Influence of lubricant on friction coefficient. (Color online)

and under different loading and speed rates, and for various475
surface treatments. Optical microscopy and scanning electron476
microscopy were utilized to identify the micro-constituents,477
whereas contact mechanics and fracture mechanics were uti-478
lized to yield the mechanical characteristics. Based on the testing results, the following conclusions can be derived:

- Crumb rubber inclusions contribute to an increase in the
 effective friction behavior.
- 451 2. An enhancement of the fracture toughness is observed⁴⁸²
 452 with the addition of crumb rubber particles.
- A high resistance to weathering a higher stability in the₄₈₅
 tribological response with respect to surface lubrication is⁴⁸⁶
 observed for crumb-rubber reinforced concrete.
- 4. The specific surface area of crumb rubber particles may₄₈₉
 plan a crucial roles in governing the level on improvement⁴⁹⁰
 of the friction coefficient. In addition, the functionaliza-⁴⁹¹
 tion of the cement/rubber interface using bonding agent⁴⁹²
 may stall the decrease in strength observed due to the par-⁴⁹⁴
 tial replacement of aggregates with crumb rubber particles.⁴⁹⁵
 Nevertheless, further research is needed.

Thus, these results will contribute to the development of 498 enhanced-performance materials for railroad applications.

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627 Appendix

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7. Mixture Analysis of Friction Frequency Distribution: Effect of Surface Lubricant

Tables 7–10 below display the characteristics of the individual friction mechanisms identified for each mix and for each surface treatment condition. Three surface treatment were considered; Dry, wet witl Oil and wet with Deionized Water. The individual friction mechanisms are characterized by their fraction, (%), average friction coefficient, $< \mu >$, and standard deviation of the friction coefficient, $< \sigma_{\mu} >$.

Mix 1		Mechanism	Mechanism	Mechanism	Mechanism	Mechanism	Mechanism
		1	2	3	4	5	6
	(%)	0.43	0.11	0.10	0.20	0.11	0.05
Dry	< µ >	0.16	0.24	0.30	0.38	0.47	0.64
	σ_{μ}	0.03	0.03	0.03	0.05	0.04	0.13
	(%)	0.59	0.05	0.07	0.18	0.05	0.07
Oil	$<\mu>$	0.18	0.25	0.30	0.38	0.47	0.65
	σ_{μ}	0.03	0.02	0.02	0.05	0.05	0.12
	(%)	0.58	0.05	0.07	0.15	0.09	0.05
DI Water	< µ >	0.10	0.18	0.24	0.32	0.42	0.65
	σ_{μ}	0.03	0.02	0.03	0.05	0.05	0.17

Table 7: Deconvolution analysis of the friction distribution for Mix 1.

Mix 2		Mechanism	Mechanism	Mechanism	Mechanism	Mechanism	Mechanism
		1	2	3	4	5	6
	(%)	0.41	0.13	0.13	0.23	0.05	0.05
Dry	$<\mu>$	0.15	0.24	0.31	0.41	0.49	0.69
	σ_{μ}	0.05	0.04	0.03	0.05	0.04	0.15
	(%)	0.30	0.05	0.12	0.43	0.05	0.05
Oil	$<\mu>$	0.11	0.19	0.25	0.35	0.49	0.65
	σ_{μ}	0.04	0.02	0.04	0.06	0.04	0.12
	(%)	0.54	0.09	0.15	0.08	0.09	0.05
DI Water	$<\mu>$	0.16	0.25	0.34	0.41	0.48	0.64
	σ_{μ}	0.03	0.04	0.04	0.03	0.04	0.12

Table 8: Deconvolution analysis of the friction distribution for Mix 2.

Mix 3		Mechanism	Mechanism	Mechanism	Mechanism	Mechanism	Mechanism
		1	2	3	4	5	65
	(%)	0.45	0.07	0.12	0.18	0.10	0.07
Dry	$<\mu>$	0.12	0.23	0.31	0.41	0.49	0.57
	σ_{μ}	0.05	0.03	0.04	0.04	0.03	0.04
	(%)	0.15	0.16	0.15	0.09	0.37	0.07
Oil	$<\mu>$	0.12	0.21	0.29	0.36	0.46	0.58
	σ_{μ}	0.04	0.03	0.04	0.03	0.06	0.03
	(%)	0.48	0.05	0.09	0.14	0.18	0.05
DI Water	< µ >	0.18	0.28	0.35	0.44	0.53	0.72
	σ_{μ}	0.04	0.03	0.04	0.05	0.05	0.14

Table 9: Deconvolution analysis of the friction distribution for Mix 3.

Mix 4		Mechanism	Mechanism	Mechanism	Mechanism	Mechanism	Mechanism
		1	2	3	4	5	6
Dry	(%)	0.38	0.09	0.16	0.26	0.05	0.05
	< µ >	0.14	0.22	0.31	0.44	0.55	0.75
	σ_{μ}	0.05	0.04	0.05	0.06	0.05	0.15
Oil	(%)	0.43	0.14	0.13	0.11	0.12	0.06
	$<\mu>$	0.12	0.22	0.31	0.39	0.49	0.63
	σ_{μ}	0.04	0.04	0.03	0.03	0.04	0.01
DI Water	(%)r	0.56	0.05	0.10	0.16	0.06	0.07
	$<\mu>$	0.16	0.24	0.31	0.40	0.51	0.64
	σ_{μ}	0.04	0.03	0.04	0.05	0.05	0.08

Table 10: Deconvolution analysis of the friction distribution for Mix 4.