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Lock-in of the vortex-induced vibrations of a long tensioned beam in shear flow

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ABSTRACT

The occurrence of lock-in, defined as the local synchronization between the vortex shedding frequency and the cross-flow structural vibration frequency, is investigated in the case of a tensioned beam of length to diameter ratio 200, free to move in both the in-line and cross-flow directions, and immersed in a linear shear current. Direct numerical simulation is employed at three Reynolds numbers, from 110 to 1100, so as to include the transition to turbulence in the wake. The Reynolds number influences the response amplitudes, but in all cases we observed similar fluid–structure interaction mechanisms, resulting in high-wavenumber vortex-induced vibrations consisting of a mixture of standing and traveling wave patterns.

Lock-in occurs in the high oncoming velocity region, over at least 30% of the cylinder length. In the case of multi-frequency response, at any given spanwise location lock-in is principally established at one of the excited vibration frequencies, usually the locally predominant one. The spanwise patterns of the force and added mass coefficients exhibit different behaviors within the lock-in versus the non-lock-in region. The spanwise zones where the flow provides energy to excite the structural vibrations are located mainly within the lock-in region, while the flow damps the structural vibrations in the non-lock-in region.

1. Introduction

Long tensioned beams subject to vortex-induced vibrations (VIV) within a shear flow are encountered in a number of important applications, while they serve as a paradigm of a distributed flow-structure interaction problem. In the context of ocean engineering, the reliable estimation of the fatigue damage of risers and mooring lines placed within sheared ocean currents requires detailed understanding and efficient prediction of these self-excited oscillations.

The problems of a rigid circular cylinder free to move or forced to oscillate in the cross-flow direction, in uniform current, have contributed to elucidate some fundamental VIV mechanisms (Bearman, 1984; Sarpkaya, 2004; Williamson and Govardhan, 2004). Large amplitude oscillations occur when the vortex shedding and the structural vibration frequencies coincide, a condition referred to as 'lock-in'. The lock-in condition can occur over a range of oncoming flow velocities and the vortex shedding frequency can be driven relatively far from the Strouhal frequency, which results from the von Kármán instability behind a stationary cylinder; this phenomenon of frequency entrainment is described as 'wake capture'.

The case of long flexible cylinders has attracted less attention, especially for beams in sheared currents. Peltzer and Rooney (1985) studied the wake of a cable forced to oscillate in the cross-flow direction within a linearly sheared flow.

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As in the case of an oscillating rigid cylinder (Stansby, 1976), the wake exhibits a large spanwise cell of constant vortex shedding frequency, equal to the structural vibration frequency; the cell length increases with the amplitude of vibration. Thus, the vibration disrupts the cellular pattern observed in the wake of stationary cylinders in shear flow (or tapered cylinders in uniform flow), which is composed of smaller, regularly spaced cells (Peltzer and Rooney, 1985). Field and laboratory experiments on long flexible cylinders free to oscillate in sheared currents highlighted the mixed standing-traveling wave nature of the vibrations, involving high structural wavenumbers and, often, multiple frequencies of response (e.g. Trim et al., 2005; Lie and Kaasen, 2006; Vandiver et al., 2009). These studies have focused on an analysis of the structural response, but did not provide information concerning the occurrence of the lock-in condition. Huera-Huarte and Bearman (2009) performed laboratory experiments on a flexible cylinder.

Few numerical studies have been carried out in this context. Meneghini et al. (2004) and Yamamoto et al. (2004) quantified the response envelopes of long flexible cylinders in shear flows by using an hydrodynamic model based on a series of two-dimensional strips. On the basis of direct numerical simulations, Newman and Karniadakis (1997) reported mixed standing-traveling wave response in the case of a flexible cylinder of aspect ratio 100, allowed to oscillate in the cross-flow direction, under the effect of a shear oncoming flow with a maximum Reynolds number of 100. Lucor et al. (2001, 2006) considered flexible cylinders of aspect ratio larger than 500, also allowed to oscillate only in the cross-flow direction, within a shear flow at Reynolds number 1000, using low-resolution direct numerical simulations. In linear shear flow, Lucor et al. (2001) reported a region of lock-in located in the high velocity zone but did not correlate this observation to the energy exchanges between the flow and the structure.

As a consequence, the phenomenon of lock-in needs further investigation, especially for a flexible cylinder free to move in both the in-line and cross-flow directions. In the present work, direct numerical simulation is employed to predict the VIV of a long tensioned beam of aspect ratio 200, immersed in a linear shear flow, in the range of Reynolds numbers 110–1100. The objective is to provide a detailed characterization of the lock-in phenomenon and to analyze its impact on the fluid forces and on the main features of the fluid–structure energy transfer.

The physical model and the numerical method are presented in Section 2. The vibrations of the tensioned beam are quantified in Section 3. The phenomenon of lock-in is studied in Section 4 and its influence on the fluid forces in Section 5.

2. Model and numerical method

The flow past a flexible cylinder of circular cross-section is predicted using direct numerical simulation of the threedimensional incompressible Navier–Stokes equations. The cylinder is submitted to an oncoming flow which is parallel to the global x axis and linearly sheared along the global z axis, as illustrated in Fig. 1(a). In the following, all physical variables are non-dimensionalized using the cylinder diameter D and the maximum inflow velocity U, which occurs at z=0. The ratio between maximum and minimum inflow velocity is equal to 3.67. The Reynolds number (Re) is based on D and the inflow velocity. Three Re ranges are considered: Re \in [30,110], Re \in [90,330] and Re \in [300,1100]. The three corresponding simulations are denoted by the maximum Reynolds number Re_m.

The cylinder aspect ratio is L/D=200, where L is the cylinder length in its equilibrium position in quiescent flow. It is pinned at both ends, while it is free to move in both the in-line (x) and cross-flow (y) directions. The cylinder mass ratio is

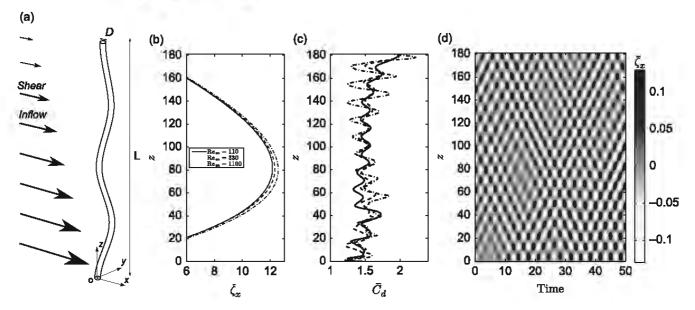


Fig. 1. (a) Sketch of the physical configuration, (b) time-averaged in-line displacement, (c) time-averaged drag coefficient and (d) selected time series of the in-line displacement fluctuation at $Re_m = 1100$, along the cylinder span.

defined as $m = \rho_c / \rho_f D^2$, where ρ_c is the cylinder mass per unit length, and ρ_f the fluid density. The mass ratio is set equal to 6 in reference to Jauvtis and Williamson (2004)'s work and lower values are currently under investigation. The constant tension, bending stiffness and damping of the structure are designated by *T*, *EI* and *K*, respectively. The in-line and cross-flow displacements of the cylinder are denoted by ζ_x and ζ_y . The drag and lift coefficients are denoted by C_x and C_y . The structural dynamics are governed by a tensioned beam model, expressed as follows in non-dimensional formulation (Evangelinos and Karniadakis, 1999):

$$\frac{\partial^2 \zeta}{\delta t^2} - \omega_c^2 \frac{\partial^2 \zeta}{\delta z^2} + \omega_b^2 \frac{\partial^4 \zeta}{\delta z^4} + \frac{K}{m} \frac{\partial \zeta}{\delta t} = \frac{1}{2} \frac{C}{m},\tag{1}$$

where $\zeta = [\zeta_x, \zeta_y]^T$ and $C = [C_x, C_y]^T$. *t* denotes the non-dimensional time variable. ω_c and ω_b are the cable and beam phase velocities, defined as $\omega_c^2 = T/m$ and $\omega_b^2 = EI/m$, respectively. The structural damping is set equal to zero (*K*=0) to allow maximum amplitude oscillations. A tensioned beam is considered in this study, with $\omega_c = 4.55$ and $\omega_b = 9.09$. As shown in Section 3, these structural parameters lead to vibrations involving high structural wavenumbers, which are representative of configurations encountered in the context of ocean engineering.

The parallelized code Nektar, based on the spectral/hp element method (Karniadakis and Sherwin, 1999), is used to solve the coupled fluid-structure system. Details regarding validation studies of the numerical method and parameters have been reported in Newman and Karniadakis (1997) and Evangelinos and Karniadakis (1999). The computational domain extends 50D downstream and 20D in front, above, and below the cylinder. A two-dimensional grid of 2175 elements with polynomial order p=6 or 7, depending on the Reynolds number, is used in the (x,y) planes. In the z direction, 512 planes (256 complex Fourier modes) are used for the $Re_m = 110$ case, and 1024 planes (512 complex Fourier modes) in the $\text{Re}_m = 330$ and 1100 cases. The spatial resolution is similar to Evangelinos and Karniadakis (1999)'s study for a cylinder of aspect ratio $L/D = 4\pi$ constrained to oscillate in the cross-flow direction, at Re=1000. The spanwise periodicity of the imposed shear velocity profile, due to Fourier expansion, is enforced in a buffer region. The buffer region inflow velocity profile is represented by a third-order polynomial that ensures continuity of the velocity profile and its slope. The size of the buffer region is chosen equal to 8% of the cylinder length ($\Delta z = 16$), in agreement with the recommendations of Lucor et al. (2006). Two additional simulations performed at $Re_m = 110$ with $\Delta z = 11$ and 21 have emphasized the negligible influence of the buffer region size on the rest of the domain, as long as it remains small compared to the cylinder length. The relative difference on the maximum RMS values of the structure displacements along the span is smaller than 3% between $\Delta z = 11$ and 21 cases. The relative difference on the vibration frequencies is smaller than 0.5%. The buffer region is not shown in the following. The results reported in this study are based on time series of more than 300 convective time units, collected after the initial transient dies out, for each Rem.

3. Structural responses

The structure exhibits an asymmetric time-averaged in-line deformation due to the oncoming shear flow, with a maximum displacement located near z=80 (Fig. 1(b)). The Reynolds number considered in the simulation has only a small influence on this deformation. The time-averaged drag coefficient normalized by the local inflow velocity, \overline{C}_d , is plotted in Fig. 1(c). The spanwise evolution of \overline{C}_d is substantially influenced by the structural motion, in particular by the cross-flow vibration pattern. A slight increase of the \overline{C}_d local maxima can be noticed with increasing Re_m in the region of maximum in-line displacement. Fluid forces are investigated in Section 5.

In both the in-line and cross-flow directions, the structural response is a combination of standing and traveling wave patterns, as illustrated in Fig. 1(d) by the spatio-temporal evolution of the in-line displacement fluctuation, over a selected time interval, for Re_m =1100. Maximum and RMS values of the vibration amplitudes reflect the mixed nature of the responses (Fig. 2). In these plots and in the following, only the deviations of the in-line motion from its mean value, $\tilde{\zeta}_x$, are considered. The standing character of the responses leads to the formation of cells along the span corresponding to alternating 'nodes' (minima of the response envelope) and 'anti-nodes' (maxima of the response envelope). Despite the shear flow, the displacements associated with anti-nodes remain relatively constant along the cylinder span. The standing character of the response is more pronounced near the ends. The RMS values of the displacements associated with nodes are different from zero, which emphasizes the modulation of the standing wave patterns by superimposed traveling wave components. The Re_m influence on response amplitudes is more pronounced in the in-line direction. The amplitudes of vibration reached at Re_m =1100 are similar to experimental measurements carried out with flexible cylinders at higher Reynolds numbers (Trim et al., 2005; Lie and Kaasen, 2006; Huera-Huarte and Bearman, 2009). The variability of the spanwise distance between the successive maxima (anti-nodes) of the cross-flow displacement RMS values illustrates the deviation of the actual standing wave components from sine Fourier modes, defined by $\sin(\pi nzD/L)$, for the *n*th mode.

Spanwise distributions of the temporal power spectra of the in-line $(\tilde{\zeta}_x)$ and cross-flow (ζ_y) vibrations are plotted in Fig. 3. The power spectral densities (PSD) are normalized at each spanwise location by the corresponding displacement variance.

Responses at a single frequency as well as responses at several frequencies can be observed along the span. These two types of response are referred to as 'mono-frequency' and 'multi-frequency', respectively. In the case of multi-frequency response, as, for instance, in the in-line direction at $Re_m=330$, it can be noticed that the peaks are clearly defined and

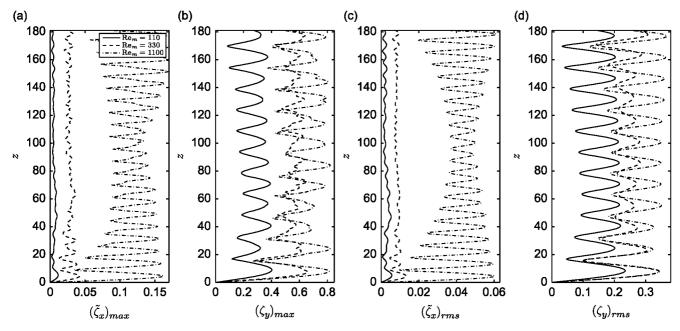


Fig. 2. (a,b) Maximum and (c,d) RMS values of the (a,c) in-line displacement fluctuation and (b,d) cross-flow displacement, along the cylinder span.

distinct from each other, despite a narrow-band vibration, in the range of [0.26,0.35]. The ratio between the in-line and cross-flow excited frequencies is generally close to 2, including the multi-frequency cases.

The excited frequencies exhibit spectral peaks along the entire span. In both the in-line and cross-flow directions, these peaks form spanwise cellular patterns that can be related to the excitation of specific structural wavenumbers. A spatio-temporal spectral analysis based on a two-dimensional fast Fourier transform of the structural responses (not presented here) shows that wavenumbers in the ranges [0.055,0.063] and [0.033,0.038] are excited in the in-line and cross-flow directions, respectively. For illustration purposes, these excited wavenumbers can be loosely associated with the corresponding sine Fourier modes; $n \in \{22,23,24,25\}$ in the in-line direction and $n \in \{13,14,15\}$ in the cross-flow direction. The natural frequency associated with the wavenumber k can be evaluated as follows:

$$f^{\text{nat}}(k) = \sqrt{\frac{m}{m + \frac{\pi}{4}C_m}} k \sqrt{\omega_c^2 + 4\pi^2 \omega_b^2 k^2},\tag{2}$$

where C_m is the added mass coefficient induced by the fluid. The natural frequencies corresponding to the above mentioned modes, with $C_m=1$, are indicated in Fig. 3 by vertical dashed lines. The actual responses exhibit substantial deviations from f^{nat} , especially in the in-line direction.

4. Lock-in phenomenon

In the case of flexibly mounted rigid cylinders in uniform flow, the phenomenon of lock-in consists of self-excited, vortex-induced vibrations accompanied by the synchronization of the frequency of vortex formation with the frequency of cylinder vibration. The lock-in phenomenon has been extensively investigated in this context (Bearman, 1984; Sarpkaya, 2004; Williamson and Govardhan, 2004).

In the context of long flexible cylinders in shear flow, the lock-in condition can be defined locally; at each spanwise location, the lock-in condition is established when the local vortex shedding frequency coincides with the local cross-flow vibration frequency. In the absence of such synchronization, the condition is referred to as non-lock-in. The spanwise region which includes all the locally locked-in locations is referred to as the lock-in region and the rest of the span as the non-lock-in region.

The vortex shedding frequency is quantified from the cross-flow component of the flow velocity, v, along a spanwise line located downstream of the cylinder at (x,y)=(20,0). The PSD of the v velocity component is plotted along the span for the three Re_m in Fig. 4. The predominant cross-flow vibration frequencies determined in Fig. 3 are indicated by vertical dashed lines.

In all cases, a region of lock-in can be identified in the high oncoming flow velocity zone, near z=0. The rest of the span corresponds to a non-lock-in region, where the vortex shedding and the structural vibrations are not synchronized. The lock-in region covers 59D, 75D and 77D at Re_m=110, 330 and 1100, respectively. The case of Re_m=330 exhibits lock-in at all three distinct frequencies identified in the multi-frequency structural response. Despite some secondary contributions, it can be observed that, at each spanwise location, the vortex shedding is mainly synchronized with a single frequency, which can be different for each location. In addition, a comparison of the cross-flow vibration and flow velocity spectra

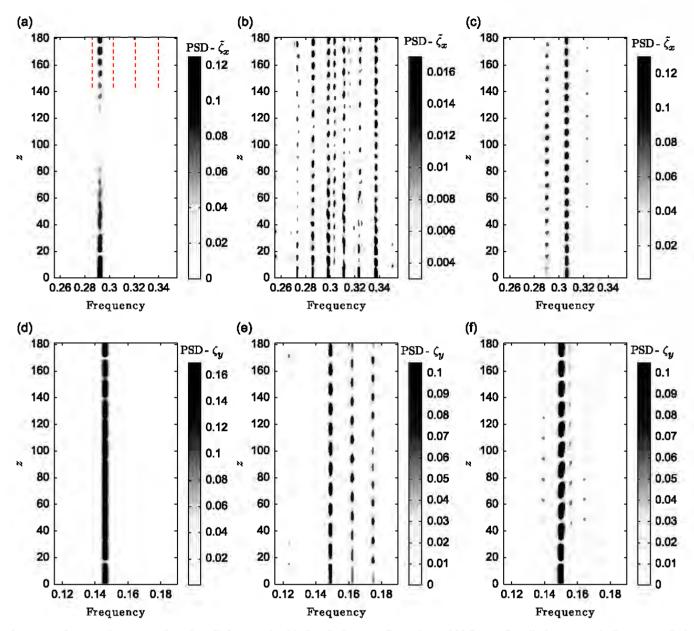


Fig. 3. PSD of structural responses along the cylinder span: (a–c) in-line displacement fluctuation and (d–f) cross-flow displacement at (a,d) $Re_m = 110$, (b,e) $Re_m = 330$, (c,f) $Re_m = 1100$. Selected natural frequencies of the structure are indicated by vertical dashed lines.

(Figs. 3(e) and 4(b)) shows that the locally predominant vibration frequency is preferred by the coupled fluid-structure system when establishing the lock-in condition. At $\text{Re}_m = 1100$, the spanwise evolution of the predominant frequency of v is more irregular than in other cases, due to the absence of stable wake patterns in several spanwise regions. These zones form 'holes' in the lock-in spanwise pattern.

The spectral amplitude of the cross-flow response at the local lock-in frequency is plotted in Fig. 5 as a function of the local vibration frequency, normalized by the local Stroubal frequency. The local vibration frequency is defined as $f_i = fU/U_i$, where f is the local frequency non-dimensionalized by U, the maximum oncoming flow velocity (z=0), and U_i is the local oncoming flow velocity. The local Stroubal frequency (f_{st}) is estimated as a function of the local Reynolds number on the basis of the vortex shedding frequency past a stationary cylinder in uniform flow (Williamson, 1996; Norberg, 2003). In the case of multi-frequency response (Fig. 5(b)), different symbols are used to specify which vibration frequency is the local lock-in frequency among the three dominant frequencies identified in Fig. 3(e). On these plots are superimposed the lower and upper limits of the wake synchronization zones reported by Koopmann (1967) and Cheng and Moretti (1991) for forced cross-flow oscillations of a rigid cylinder in uniform flow at Re \in {100,200,300} and Re=1500, respectively.

Under the lock-in condition, the vortex shedding frequency exhibits large deviations from the Strouhal frequency. In the present case of a freely vibrating flexible cylinder in shear flow, the combinations of amplitudes and frequencies observed under the lock-in condition remain within the wake capture region established from forced vibrations, for the

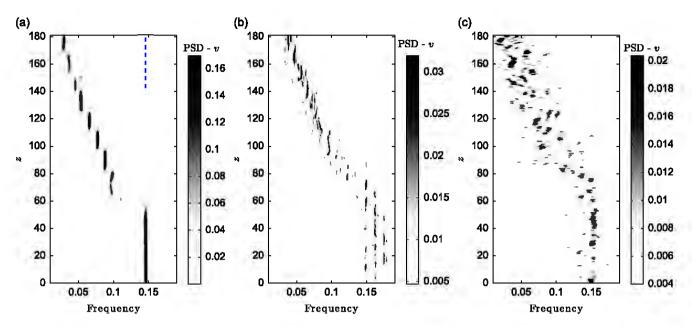


Fig. 4. PSD of the temporal evolution of the cross-flow component of flow velocity along a spanwise line at (xy)=(20,0) at (a) Re_m=110, (b) Re_m=330, (c) Re_m=1100. Vertical dashed lines indicate frequencies identified in Fig. 3.

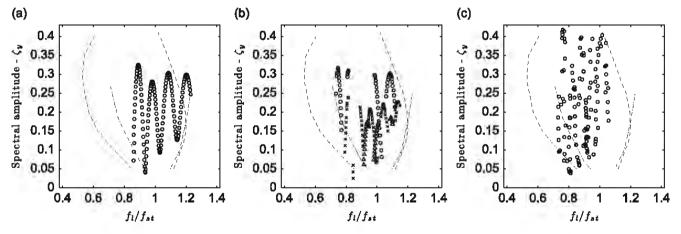


Fig. 5. Spectral amplitude of the cross-flow displacement under the lock-in condition as a function of the local vibration frequency normalized by the Strouhal frequency, at (a) Re_m =110, (b) Re_m =330, (c) Re_m =1100. In (b), different symbols are used to identify the global lock-in frequency at the corresponding location point, among the three possible ones: (\bigcirc) f=0.149, (\times) f=0.162, (\triangle) f=0.174. The lower and upper limits of wake capture region reported by Koopmann (1967) and Cheng and Moretti (1991), obtained for forced oscillations, are indicated by dotted and dashed lines, respectively.

corresponding Reynolds number. At $\text{Re}_m = 1100$ and to a lesser extent $\text{Re}_m = 330$, the frequencies of lock-in slant towards lower frequencies ($f_l < f_{st}$,), as previously noted by Cheng and Moretti (1991) for forced oscillations. At $\text{Re}_m = 330$, the multi-frequency nature of the response does not lead to a partitioning of the synchronization domain in three distinct zones. Instead, the three global frequencies of vibration overlap over most of the domain.

5. Fluid forces

The fluid forces exerted on the cylinder are representative of non-linear equilibrium states reached by the coupled fluid-structure system and can be used to identify the properties of the fluid-structure energy transfer. The maximum and RMS values of the drag and lift coefficients along the cylinder span are shown in Fig. 6. The fluid forces include both the pressure and viscous components and are normalized by the local oncoming flow velocity. They are denoted by C_d and C_l , to avoid confusion with C_x and C_y , which are normalized by the maximum velocity. The force coefficients reach very high magnitudes in the non-lock-in region, compared to the case of a stationary cylinder, reported for example in Persillon and Braza (1998) and Norberg (2003). Despite the influence of Re_m on the force coefficient amplitudes, the three Reynolds number cases present comparable spanwise trends.

Spanwise distribution of the temporal power spectra of the drag and lift coefficients are presented in Fig. 7. These plots show that the frequencies at which the fluid forces are exerted on the structure mainly coincide with the predominant vibration frequencies, indicated by vertical dashed lines. Some peaks also appear at secondary vibration frequencies, as for

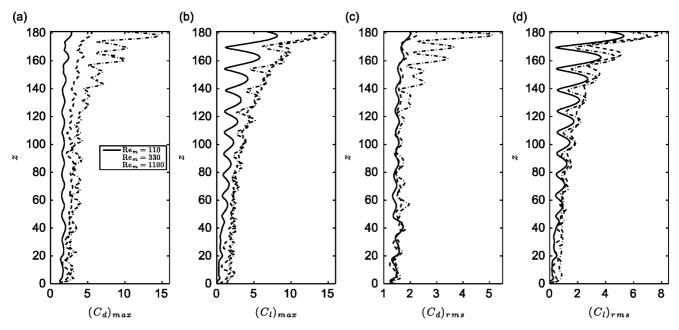


Fig. 6. (a,b) Maximum and (c,d) RMS values of the (a,c) drag and (b,d) lift coefficients along the cylinder span.

instance in the in-line direction at Re_m =330 (Fig. 7(b)). The spanwise modulation of the power spectra by the standing component of the vibrations is clearly visible. At Re_m =330 and 1100, the regular spanwise distribution of the frequency peaks is considerably altered in the lock-in region.

The time-averaged total (C_{tv}) , drag (C_{xv}) and lift (C_{yv}) force coefficients in phase with the cylinder velocity, and total (C_{ta}) , drag (C_{xa}) and lift (C_{ya}) force coefficients in phase with the cylinder acceleration, are defined as follows:

$$C_{tv} = \frac{\sqrt{2} \langle \tilde{C}_x \tilde{\zeta}_x + C_y \dot{\zeta}_y \rangle}{\sqrt{\langle \dot{\tilde{\zeta}}_x^2 + \dot{\zeta}_y^2 \rangle}}, \quad C_{xv} = \frac{\sqrt{2} \langle \tilde{C}_x \tilde{\tilde{\zeta}}_x \rangle}{\sqrt{\langle \dot{\tilde{\zeta}}_x^2 \rangle}}, \quad C_{yv} = \frac{\sqrt{2} \langle C_y \dot{\zeta}_y \rangle}{\sqrt{\langle \dot{\tilde{\zeta}}_y^2 \rangle}}, \quad (3a)$$

$$C_{ta} = \frac{\sqrt{2} \langle \tilde{C}_x \tilde{\tilde{\zeta}}_x + C_y \tilde{\zeta}_y \rangle}{\sqrt{\langle \tilde{\tilde{\zeta}}_x^2 + \tilde{\zeta}_y^2 \rangle}}, \quad C_{xa} = \frac{\sqrt{2} \langle \tilde{C}_x \tilde{\tilde{\zeta}}_x \rangle}{\sqrt{\langle \tilde{\tilde{\zeta}}_x^2 \rangle}}, \quad C_{ya} = \frac{\sqrt{2} \langle C_y \tilde{\zeta}_y \rangle}{\sqrt{\langle \tilde{\zeta}_y^2 \rangle}}, \quad (3b)$$

where $\langle \cdot \rangle$ denotes the time-averaging operator and \tilde{p} the fluctuating component of p. The spanwise evolution of these coefficients are plotted in Fig. 8, for the three Re_m studied. The force coefficients in phase with the cylinder velocity are used to identify the fluid-structure energy transfer in a similar way as used in Newman and Karniadakis (1997) and Dahl et al. (2010). These coefficients quantify the power developed by the fluid acting on the vibrating cylinder, including both the in-line and cross-flow directions (C_{tv}) or each direction separately (C_{xv} and C_{yv}). The drag and lift coefficients are normalized by the maximum oncoming flow velocity U(z=0) so that the force coefficients in phase with velocity are representative of the relative contribution of each spanwise location to the overall energy transfer. Positive values of these coefficients imply that the fluid supplies, on average, energy to the structure and hence excites the cylinder vibration, while negative values indicate that the fluid is damping the cylinder motion.

For the three Re_m studied, positive values of C_{tv} are principally located in the lock-in region, within the high velocity zone. In the non-lock-in region, C_{tv} remains generally negative. C_{yv} exhibits a very similar spanwise pattern. As in the cross-flow direction, the principal excitation zone in the in-line direction corresponds to the lock-in region. However, a secondary zone of positive energy transfer of smaller magnitude can be identified in the non-lock-in region. A comparison with the spanwise evolution of the vortex shedding frequency (Fig. 4) shows that this secondary excitation zone occurs in the region where the cross-flow vibration frequency is approximately equal to twice the frequency of vortex shedding. However, it should be mentioned that the secondary lock-in phenomenon, i.e. at half the vibration frequency, reported by Stansby (1976) for a rigid cylinder, does not appear in the present case; well-defined secondary lock-in cells are not observed. The secondary zone of positive C_{xv} appears to be caused by the proximity of the vortex shedding frequency with a submultiple of the vibration frequency. An analysis of the vortex shedding pattern (not presented here) shows that 2S-like modes, with two counter-rotating vortices shed per wake period (Williamson and Roshko, 1988), dominate in the non-lock-in region at the present Re_m . As a consequence, the vibration excited in the cross-flow direction by the shedding of a single vortex over a cylinder oscillation cycle, will be damped during the next cycle by the shedding of a counterrotating vortex. This mechanism can explain why C_{yv} remains negative when the cross-flow vibration frequency is twice

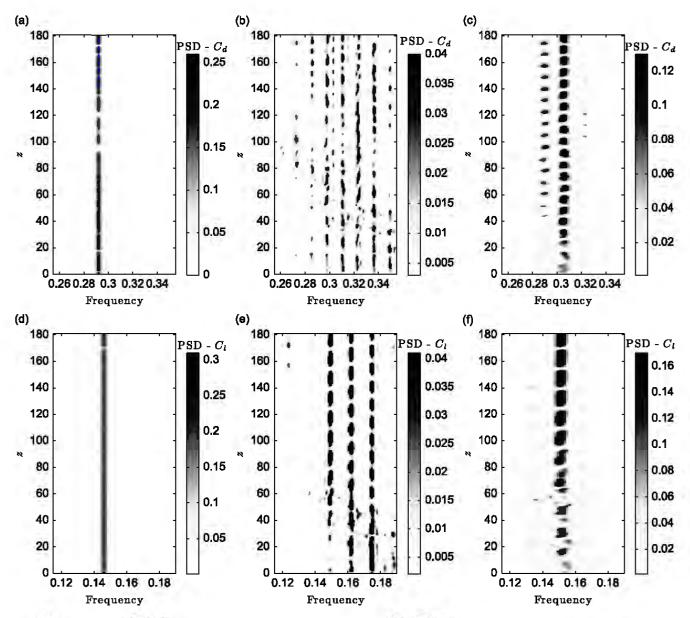


Fig. 7. PSD of fluid force coefficients along the cylinder span: (a-c) drag and (d-f) lift coefficients at (a,d) $Re_m = 110$, (b,e) $Re_m = 330$, (c,f) $Re_m = 1100$. The predominant vibration frequencies are indicated by vertical dashed lines.

the vortex shedding frequency. The similarity of C_{yv} and C_{tv} emphasizes the very small contribution of the in-line component to the overall distribution of energy transfer. The vibration excitation is not uniform across the lock-in region: negative peaks and thus damping zones can occur near the minima of vibration amplitude envelope.

The time-averaged force coefficients in phase with acceleration also present a substantial spanwise variability. As previously, the cross-flow force component exhibits a spanwise distribution close to the total force coefficient. These coefficients remain negative over most of the span, except in short zones within the lock-in region, leading to negative added mass coefficients, as shown in the following. Contrary to C_{ya} and C_{ta} , the in-line component C_{xa} exhibits significant sensitivity to Re_m.

The time-averaged added mass coefficient can be quantified as follows, in the in-line and cross-flow directions:

$$C_{xm} = -\frac{2}{\pi} \frac{\langle \tilde{C}_x \tilde{\zeta}_x \rangle}{\langle \tilde{\zeta}_x^2 \rangle}, \quad C_{ym} = -\frac{2}{\pi} \frac{\langle C_y \tilde{\zeta}_y \rangle}{\langle \tilde{\zeta}_y^2 \rangle}.$$
(4)

Within the non-lock-in region, the cross-flow component C_{ym} is relatively close to the value of 1, which is associated with an absence of dynamical effects; C_{ym} tends further towards 1 as Re_m increases. In contrast, within the lock-in region, smaller and even negative values are reached. Despite a more pronounced influence of Re_m , the in-line added mass coefficients present similar trends, except that they remain smaller than 1.

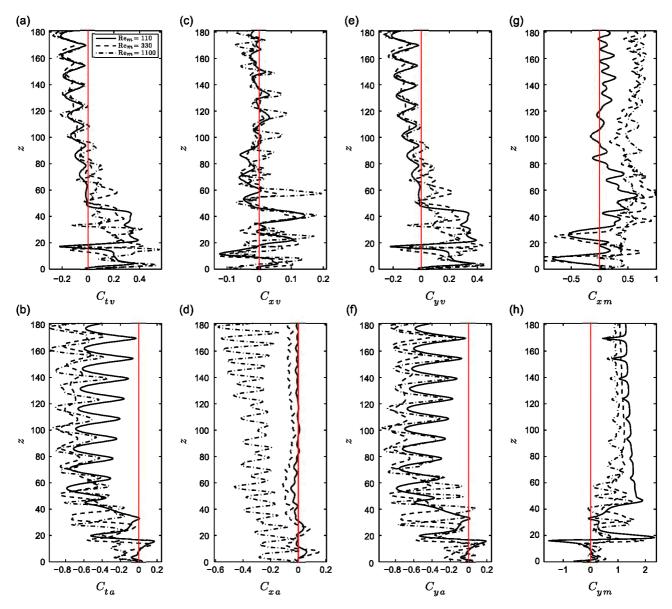


Fig. 8. Time-averaged (a-f) total, drag and lift force coefficients in phase with the structure velocity and acceleration, (g) in-line and (h) cross-flow added mass coefficients, along the cylinder span.

6. Conclusions

The in-line and cross-flow vortex-induced vibrations of a long tensioned beam immersed in a linearly sheared current have been predicted by means of direct numerical simulation, in the range of Reynolds numbers 110–1100. Despite the influence of Re_m on the displacement amplitudes, and the possibly different nature of frequency response (mono- versus multi-frequency vibrations), the main features of the structural responses and of the fluid-structure interaction mechanisms remain the same for all three Re_m cases studied. In all cases, the structural vibrations are mixtures of standing and traveling wave patterns, and a frequency ratio of approximately 2 can be established between the excited frequencies in the in-line and cross-flow directions.

Local synchronization of the vortex shedding with the cross-flow vibration, the lock-in condition, occurs in the high velocity region over at least 30% of the cylinder length. In the case of multi-frequency response, vortex shedding exhibits synchronization with all the vibration frequencies. However, at any given point along the cylinder length, lock-in is generally established at a single vibration frequency. Under lock-in, the vibration amplitudes are related with the local frequency in accordance with the capture region obtained from forced oscillation experiments on rigid cylinders for similar Reynolds number.

There are regular spanwise patterns of drag and lift coefficients, controlled by the standing wave patterns of the structural responses, within the non-lock-in region. In contrast, these patterns are strongly altered within the lock-in region. The flow excites the structure principally within the lock-in region, while it generally damps the structural vibrations in the non-lock-in region. In the in-line direction, a secondary zone of excitation of smaller magnitude has been

identified in a spanwise zone where the vortex shedding frequency is approximately half of the cross-flow vibration frequency.

The time-averaged added mass coefficients present contrasting behaviors along the cylinder span: while values relatively close to 1 are observed in the non-lock-in region, especially in the cross-flow direction, small and even negative values are reached within the lock-in region.

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