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# Top polarization in stop production at the LHC

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ABSTRACT: We survey the expected polarization of the top produced in the decay of a scalar top quark,  $\tilde{t} \to t \tilde{\chi}_i^0$ , i = 1 - 2. The phenomenology is quite interesting, since the expected polarization depends both on the mixing in the stop and neutralino sectors and on the mass differences between the stop and the neutralino. We find that a mixed stop behaves almost like a right-handed stop due to the larger hypercharge that enters the stop/top/gaugino coupling and that these polarisation effects disappear, when  $m_{\tilde{t}_1} \approx m_t + m_{\tilde{\chi}^0}$ . After a discussion on the expected top polarization from the decay of a scalar top quark, we focus on the interplay of polarization and kinematics at the LHC. We discuss different probes of the top polarization in terms of lab-frame observables. We find that these observables faithfully reflect the polarization of the parent top-quark, but also have a non-trivial dependence on the kinematics of the stop production and decay process. In addition, we illustrate the effect of top polarization on the energy and transverse momentum of the decay lepton in the *laboratory* frame. Our results show that both spectra are softened substantially in case of a negatively polarized top, particularly for a large mass difference between the stop and the neutralino. Thus, the search strategies, and the conclusions that can be drawn from them, depends not just on the mass difference  $m_{\tilde{t}} - m_{\tilde{\chi}_{1}^{0}}$  due to the usual kinematic effects but also on the effects of top polarization on the decay kinematics the extent of which depends in turn on the said mass difference.

**KEYWORDS:** Supersymmetry Phenomenology

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## 1 Introduction

The observation of a new boson at the LHC with properties broadly consistent with those of a Higgs boson expected in the Standard Model (SM), by both the ATLAS and CMS collaborations [1, 2], indicates that the process of establishing the last missing piece of the SM has now begun. In spite of the great success of the SM, which would be crowned by this discovery, there are a number of observational issues that point at the need for physics beyond the SM (BSM). In particular, dark matter (DM) and baryon asymmetry in the Universe (BAU). In addition, there are theoretical reasons for BSM physics, such as the instability of the EW scale under radiative corrections or a lack of fundamental understanding of the observed wide range of the fermion masses. Supersymmetry (SUSY) [3, 4] has been one of the favourite candidates for BSM physics, as it can provide a very elegant solution to many of these open questions, particularly significant being the prediction of at least one, low mass Higgs boson, possibly the resonance that has been observed. Searches for light-flavoured squarks and gluinos at the Large Hadron Collider (LHC) have so far come up empty [5–8]. A key feature of almost all SUSY models is that masses of all the supersymmetric particles depend crucially on the scale and the nature of the supersymmetry breaking mechanism, but the upper limit on the lightest Higgs boson mass depends only mildly on it. The only general theoretical pointers we have to the expected mass scales for SUSY breaking, and hence of the sparticle masses, come from naturalness arguments [9-11]. In SUSY, the low mass, is naturally stable under large radiative corrections, provided the supersymmetry breaking scale is not too large. In particular, the gluinos and most squarks can be quite heavy, as long as the top squark, or stop, is relatively light so that SUSY has a solution to offer to

the hierarchy problem as suggested originally [12, 13]. The upper limit on the allowed stop masses for a given Higgs mass depends on the amount of fine tuning that is tolerated [14-16].

The recent Higgs results [1, 2] suggest, in the context of SUSY, a Higgs boson mass quite close to the upper bound on the mass of the lightest Higgs state. This points towards at least one relatively heavy stop [17, 18], which naturally leads us to consider models with one light stop and at least one light neutralino, which is then the Lightest Supersymmetric Particle (LSP). This is the minimal 'light' SUSY particle content that one needs in order to account for the observational hints of BSM physics such as DM and BAU. It is therefore particularly interesting to investigate possibilities of such a light stop search at the LHC.

Two points are to be noted. Due to the large mass of the top quark, the limits on squark masses obtained from the generic missing  $E_T + jets(leptons)$  search [5–8] are not directly applicable, even if one were to look at the limits on the masses of light flavoured squarks produced 'directly'. Secondly, while it is true that the cross-section for the direct stop pair production is much smaller than the total squark-gluino cross-section, direct stop pair production processes are an interesting channel for stop searches, in view of the current constraints on the gluino mass. For example at  $\sqrt{s} = 8$  TeV the direct stop cross section at NLL level is ~ 85 fb for  $m_{\tilde{t}} = 500$  GeV, [19–22] a value for the stop mass that is currently allowed by the data.

The third generation sfermion sector has always been a subject of great interest in sparticle phenomenology [23]. In view of the above discussion, it is also clear why it has received even extra attention in both phenomenological [16, 24–32] and experimental investigations. Results on stop searches in direct stop pair production have been presented both by the ATLAS [33–36], and the CMS [37–40] collaborations. However, the interpretation of these searches has some model-dependence and usually limits are quoted in simplified models. In any case, present data allows for top squarks well below the TeV scale.

One new aspect of the stop search phenomenology is the possible presence of a top quark with possibly non-zero polarization in the resulting final state. Since the top quark decays before it hadronizes, the polarization can have implications for the kinematic distributions of the decay products and hence on the search strategies of the stop. If a stop is discovered, the top polarization can play a role in determining the properties of the stop and light neutralino. In this paper, we investigate the longitudinal polarization of the top quark that results from stop decay;

$$\tilde{t}_1 \to t \, \tilde{\chi}_i^0,$$
(1.1)

where  $\tilde{\chi}_i^0, i = 1, 4$  stand for the four neutralinos. It has been shown [41] that the fermions produced in sfermion decays can have non-zero polarization, which can depend on the mixing in the sfermion sector as well as the neutralino-chargino sector. It also depends on the velocity of the produced top quark and hence on the mass differences.

Suggestions for using the polarization of heavy fermions as a probe of new physics models abound in literature, (see ref. [42] and references therein for a recent summary). For example, in the *R*-parity violating MSSM, polarized top quarks can arise in the hadronic production of  $t\bar{t}$  pair via a *t*-channel exchange of a stau/stop [43, 44] or in associated production of a slepton with a *t* quark [45]. Different BSM explanations of the top forwardbackward asymmetry observed at the Tevatron, among them those involving t channel exchange of a color singlet and a color octet scalar, can be discriminated using top polarization [46–49]. Similarly, use of the top polarization to probe the mixing in the squark sector for the third generation squarks at  $e^+e^-$  colliders has been a subject of a lot of detailed investigations [50, 51]. At the  $e^+e^-$  colliders the  $\tilde{t}_i \tilde{t}_j^*$  production cross-sections also depend on the mixing in the stop sector. The joint measurements of the cross-sections and top polarization can then be used to reconstruct the parameters of the third generation squark sector. Of course at a collider like the LHC, in an *R*-parity conserving SUSY scenario, the production cross-sections do not depend on the mixing in the stop sector and hence it is only the polarization which can provide a handle on it.

Some aspects of top polarization in stop decay and observables for its measurements for the heavily boosted tops were discussed in [52]. Monte Carlo investigations of the top polarization expected in the decay of a light stop quark (~ 300-500 GeV) following direct stop pair production for 14 TeV LHC, along with its possible measurements in the effective top rest frame with a view to extract an effective top mixing angle, have been carried out in [53]. More recently, an observable for top polarization in terms of the energy fraction of decay leptons, in events containing  $t\bar{t}$  pair and missing  $E_T$  was studied for a light stop ~ 300-400 GeV, at the 8 TeV LHC [30]. Ref. [31] has explored the possibility of getting information on the top polarization and hence on the stop mixing angle at the 14 TeV LHC, including detector level effects, using the hadronic decay of the boosted top and jet substructure methods for measurement of the top polarization [54]. Experimental explorations of the top polarization at the LHC in  $t\bar{t}$  events, using the angular distributions of the decay products of the top in the reconstructed top rest frame have now begun [55].

Top polarization is indeed a very useful observable as a probe of new physics at the LHC as it is sensitive to the helicity structure of the production process and the bulk of top production at the LHC happens via the SM processes which lead to unpolarized top quarks. Due to the large mass of the top quark, its polarization is also amenable to experimental determination quite well through a study of its leptonic decay products. There is a strong correlation between the polarization of the top quark and the angular distributions of its decay leptons. This correlation is not affected by higher-order corrections [56–58] or new physics contributions [59–65] to the decay. Angular distributions of the decay leptons provide therefore a robust probe of the top polarization and hence of the new physics.

The aim of this paper is to present in detail the dependence of the expected top polarization from stop decay on the mixings in the stop and chargino/neutralino sectors, as well as on the mass differences between the stop and neutralinos. We will present results in terms of the relevant supersymmetric parameters that are still allowed in view of the LHC results. This has a two-fold purpose. Firstly, it gives us a pointer to the possible kinematic effects that this top polarization can have on its decay products and hence to the implications of this feature for the search strategies for the stop which use final states containing a top quark. The second is to explore how measurement of the longitudinal polarization of the resulting top quark can be used to help determine the properties of the stop and the light neutralinos, after the discovery. To that end, we study observables of the top polarization, at the 8 TeV LHC in terms of the kinematic variables of the decay lepton in the laboratory frame that have been suggested earlier [42, 66–68].

In this paper, we will first discuss in section 2 how the polarization of the top is affected by the properties of the stop and the neutralinos. We then study possible top polarizations by scanning the relevant SUSY parameters in section 3. In section 4 we examine polarization-dependent kinematic variables in the laboratory frame for specific benchmark points and discuss possible observables for the polarization constructed out of the angular variables. We conclude in section 5.

#### 2 Top polarization from stop decay

We begin by briefly recalling the correlation between the top quark spin and the flight direction of the charged lepton in the decay. When determining the polarization of the top, we consider top quark decays that produce a charged lepton  $l^+$ , which we take to be an electron or a muon

$$t \to W^+ b \to l^+ \nu_l b \,. \tag{2.1}$$

For simplicity here and in what follows, we ignore off-diagonal elements in the CKM matrix and we only consider top quarks, which can be distinguished from anti-top quarks using the charge of the lepton. As mentioned in the introduction, the top polarization is sensitive to the production process. To see this explicitly [66], let us employ the Narrow Width Approximation (NWA) for the top quark. This allows us to split the spin-averaged matrix element squared  $\overline{|\mathcal{M}|^2}$  into a part  $\rho(\lambda, \lambda')$  that corresponds to the production of the top quark, and a part  $\Gamma(\lambda, \lambda')$  that corresponds to its decay

$$\overline{|\mathcal{M}|^2} = \frac{\pi \delta(p_t^2 - m_t^2)}{\Gamma_t m_t} \sum_{\lambda, \lambda'} \rho(\lambda, \lambda') \Gamma(\lambda, \lambda') \,. \tag{2.2}$$

Here  $p_t^{\mu}$ ,  $m_t$  and  $\Gamma_t$  are the top quark momentum, mass and total decay width respectively, while  $\rho(\lambda, \lambda')$  and  $\Gamma(\lambda, \lambda')$  are matrices given by

$$\rho(\lambda, \lambda') = \mathcal{M}_{\rho}(\lambda) \mathcal{M}_{\rho}^{*}(\lambda') \text{ and } \Gamma(\lambda, \lambda') = \mathcal{M}_{\Gamma}(\lambda) \mathcal{M}_{\Gamma}^{*}(\lambda'),$$

with  $\mathcal{M}_{\rho}(\lambda)$  the matrix element of the production of a top quark with helicity  $\lambda$  and  $\mathcal{M}_{\Gamma}(\lambda)$ the corresponding decay amplitude. To obtain the averaged matrix element squared  $|\mathcal{M}|^2$ , we have to sum over the helicities  $\lambda$  and  $\lambda'$ . However, we can also project on these helicities to obtain the polarized cross section. To this end, we define top polarization vectors  $S^a$  that form, together with the top momentum, an orthogonal set and are normalized to  $S^a \cdot S^b = -\delta^{ab}$ . We can then perform the helicity projection using the identities [69, 70]:

$$u(p_t, \lambda')\bar{u}(p_t, \lambda) = \frac{1}{2} \left( \delta_{\lambda\lambda'} + \gamma_5 \#^a \tau^a_{\lambda\lambda'} \right) (\not p_t + m_t), \qquad (2.3)$$

with  $\tau^a$  the Pauli matrices. Since the transverse polarization is generally small, we will only consider the longitudinal polarization vector  $S^3$ . Its spatial part is chosen to be parallel to the top three-momentum, leading to

$$S^{3} = \frac{1}{m_{t}} \left( |\mathbf{p}_{t}|, E_{t} \hat{\mathbf{p}}_{t} \right).$$
(2.5)

Note that  $S^3$  is not a Lorentz vector, reflecting the fact that the top quark helicity is not a Lorentz-invariant quantity. The top polarization is then defined as

$$P_t = \frac{\sigma(+,+) - \sigma(-,-)}{\sigma(+,+) + \sigma(-,-)},$$
(2.6)

where  $\sigma(+,+)(\sigma(-,-))$  is the cross section for a positive (negative) helicity top quark. A negative (positive) polarization therefore corresponds to a left-handed (right-handed) top quark. In [50] it was shown for a top quark originating from the decay (1.1), the following expression for the polarization holds

$$P_t(\tilde{t}_1 \to t\,\tilde{\chi}_i^0) = \frac{\left( (G_i^R)^2 - (G_i^L)^2 \right) f_1}{(G_i^R)^2 + (G_i^L)^2 - 2G_i^R G_i^L f_2},$$
(2.7)

where  $f_1$  and  $f_2$  are kinematical factors which in the stop rest frame reduce to

$$f_1 = \frac{\lambda^{\frac{1}{2}}(m_{\tilde{t}}^2, m_t^2, m_{\tilde{\chi}}^2)}{m_{\tilde{t}}^2 - m_t^2 - m_{\tilde{\chi}}^2}, \qquad f_2 = \frac{2m_t m_{\tilde{\chi}}}{m_{\tilde{t}}^2 - m_t^2 - m_{\tilde{\chi}}^2}, \qquad (2.8)$$

with  $\lambda(x, y, z) = x^2 + y^2 + z^2 - 2xy - 2xz - 2yz$  the Källén function. The quantities  $G_i^L$  and  $G_i^R$  are the stop couplings to the neutralino  $\tilde{\chi}_i^0$  and a left- or right-handed top respectively. If we ignore again mixing in the flavour sector and choose the mixing matrices to be real, they are given by [23]

$$G_{i}^{L} = -\sqrt{2}g_{2}\left(\frac{1}{2}Z_{i2} + \frac{1}{6}\tan\theta_{W}Z_{i1}\right)\cos\theta_{\tilde{t}} - \frac{g_{2}m_{t}}{\sqrt{2}M_{W}\sin\beta}Z_{i4}\sin\theta_{\tilde{t}}, \qquad (2.9)$$
$$G_{i}^{R} = \frac{2\sqrt{2}}{3}g_{2}\tan\theta_{W}Z_{i1}\sin\theta_{\tilde{t}} - \frac{g_{2}m_{t}}{\sqrt{2}M_{W}\sin\beta}Z_{i4}\cos\theta_{\tilde{t}},$$

where  $g_2$  is the SU(2)<sub>L</sub> gauge coupling,  $\theta_W$  is the weak mixing angle and  $M_W$  is the W mass. The polarization then depends on the SUSY parameters through the neutralino mixing matrix Z, the stop mixing angle  $\theta_{\tilde{t}}$  and the ratio of the two Higgs vacuum expectation values, tan  $\beta$ . Moreover it is clear from eq. (2.7) that the top polarization is affected by the masses involved and perhaps less obviously by the stop boost. Let us now discuss these effects in turn.

#### 2.1 Stop and neutralino mixing

The top polarization eq. (2.6) depends on the couplings  $G_i^{L,R}$ , eq. (2.9), which contain the stop mixing  $\theta_{\tilde{t}}$  and neutralino mixing. The mixing  $\theta_{\tilde{t}}$  results from the diagonalization of the stop mass matrix in the L - R basis, leading to the mass eigenstates  $\tilde{t}_1$  and  $\tilde{t}_2$ 

$$M_{\tilde{t}}^2 = \begin{pmatrix} m_{\tilde{t}_L}^2 + \Delta_L + m_t^2 & -m_t(A_t + \mu \cot \beta) \\ -m_t(A_t + \mu \cot \beta) & m_{\tilde{t}_R}^2 + \Delta_R + m_t^2 \end{pmatrix}, \quad \begin{pmatrix} \tilde{t}_1 \\ \tilde{t}_2 \end{pmatrix} = \begin{pmatrix} \cos \theta_{\tilde{t}} & \sin \theta_{\tilde{t}} \\ -\sin \theta_{\tilde{t}} & \cos \theta_{\tilde{t}} \end{pmatrix} \begin{pmatrix} \tilde{t}_L \\ \tilde{t}_R \end{pmatrix}, \quad (2.10)$$

with  $m_{\tilde{t}_{L,R}}$  the soft masses of the left- and right-handed stop,  $A_t$  the top trilinear coupling,  $\mu$  the Higgs mass parameter, and  $\Delta_L = (\frac{1}{2} - \frac{2}{3}\sin\theta_W^2)M_Z^2\cos 2\beta$ ,  $\Delta_R = (\frac{2}{3}\sin\theta_W^2)M_Z^2\cos 2\beta$ with  $M_Z$  the  $Z^0$  mass. The neutralino mixing matrix, Z is determined by the diagonalization of the neutralino mass matrix  $M_n$ :

$$M_{n} = \begin{pmatrix} M_{1} & 0 & -M_{Z}c_{\beta}s_{W} & M_{Z}s_{\beta}s_{W} \\ 0 & M_{2} & M_{Z}c_{\beta}s_{W} & -M_{Z}s_{\beta}c_{W} \\ -M_{Z}c_{\beta}s_{W} & M_{Z}c_{\beta}c_{W} & 0 & -\mu \\ M_{Z}s_{\beta}s_{W} & -M_{Z}s_{\beta}c_{W} & -\mu & 0 \end{pmatrix}, \quad \begin{pmatrix} \tilde{\chi}_{1}^{0} \\ \tilde{\chi}_{2}^{0} \\ \tilde{\chi}_{3}^{0} \\ \tilde{\chi}_{4}^{0} \end{pmatrix} = Z \begin{pmatrix} \tilde{B}^{0} \\ \tilde{W}^{0} \\ \tilde{h}_{1}^{0} \\ \tilde{h}_{2}^{0} \end{pmatrix}, \quad (2.11)$$

with  $M_1$  and  $M_2$  the bino and Wino gaugino masses,  $s_W = \sin \theta_W$ ,  $c_W = \cos \theta_W$ ,  $s_\beta = \sin \beta$ and  $c_\beta = \cos \beta$ . Our subsequent investigations of the to ppolarization will be guided by a few salient aspects in this mixing, which we now discuss.

Firstly, one notes that the strength of the bino(B) coupling to stop-top is proportional to the top hypercharge. As a result, a bino-like neutralino couples more strongly to the right-handed (RH) components than to the left-handed (LH) ones, yielding a more positive top polarization than one might naively expect from a given stop mixing.

Secondly, recall that the Wino  $\tilde{W}$  only couples to the left-handed stop components, producing left-handed top quarks only. According to eq. (2.7), a pure Wino thus always leads to  $P_t = -f_1$  in the stop rest frame. As a result, polarization cannot be used to distinguish between different stop mixing for Wino-type neutralinos. In the rest of the paper we will thus limit ourselves to neutralinos with a small Wino component.

Thirdly, for the intermediate to large values of  $\tan \beta$  that are allowed for the Higgs mass constraint,  $\sin \beta \approx 1$ , therefore the couplings in eq. (2.9) hence the top polarization only mildly depend on  $\tan \beta$ .

Finally, the stop-top-neutralino coupling does not involve the first higgsino component  $\tilde{h}_1^0$ . Ignoring the Wino component, the key variables in the neutralino mixing matrix are thus the bino component  $Z_{i1}$  and the second higgsino component  $Z_{i4}$ . The relative sign between the bino and the higgsino components can impact the polarization because of the term proportional to  $G_i^R G_i^L$  in eq. (2.7). This can be seen in figure 1, where the top polarization in the stop rest frame is plotted as a function of the bino content for both left- and right-handed stops. The figure on the right zooms into the region with high bino-content. The results are shown for both relative signs of  $Z_{i1}$  and  $Z_{i4}$  and also for stops that are not entirely left- or right-handed.

The figure shows that in general the polarization behavior is as expected: dominantly right-handed stops produce a negative top polarization when they decay to a higgsino, and a positive polarization when they decay to a bino. Left-handed stops have the opposite behaviour. Notice that is in correspondence to the first aspect mentioned above, for right-handed stops in particular, even a slight change in the stop mixing angle has a large effect on the polarization. We observe that the polarization for left-handed stops is not very sensitive to the exact neutralino content when it is higgsino-like and that the polarization varies very rapidly from 1 to -1 for an almost pure bino. Moreover, the maximum polarization  $P_t = \pm 1$  cannot occur for a decay into a pure bino or higgsino due to the mass effects in eq. (2.7). This effect becomes more pronounced for smaller stop-neutralino mass differences.



Figure 1. Dependence of the top polarization on the neutralino content in the stop rest frame. The red thin lines correspond to right-handed stops, while the black thick lines correspond to left-handed stops. Results are shown for pure as well as slightly mixed stops, and for different signs of  $\epsilon$ . We have taken  $Z_{i4} = \epsilon \sqrt{(1 - Z_{i1}^2)}$ ,  $\epsilon = \pm 1$  to approximate the higgsino-content for a given bino-content and have taken  $m_t = 173.1 \text{ GeV}$ ,  $m_{\tilde{t}} = 500 \text{ GeV}$ ,  $m_{\tilde{\chi}} = 200 \text{ GeV}$  and  $\tan \beta = 10$ . The plot on the right shows the behaviour for high bino-content.



Figure 2. Dependence of the top polarization on the stop mixing in the stop rest frame. The red thin lines correspond to higgsino-like neutralinos, while the black thick lines correspond to bino-like neutralinos. Results are shown for pure as well as slightly mixed neutralinos, and for different signs of  $\mu$ . We fix the parameters as in figure 1.

For a complementary perspective we show in figure 2 the dependence of the top polarization on the stop mixing for a top quark that originates from a stop that is at rest. For both the pure bino state and the dominantly higgsino state, the polarization indeed behaves as one would expect from eq. (2.7). As in figure 1, we see that the polarization is very sensitive to small fluctuations in the bino component for  $Z_{i1} \approx 1$ . In this case, both terms in the  $G_i^R$  coupling in eq. (2.9) become relevant, the first is suppressed by the stop mixing and the second by the higgsino mixing, hence the large fluctuation in the polarization for small values of  $\sin \theta_{\tilde{t}}$ .

#### 2.2 Masses

We have already seen that the stop and neutralino masses influence the polarization. This effect is shown in figure 3.



Figure 3. Dependence of the top polarization in the stop rest frame on the stop-neutralino mass difference for a neutralino that is purely bino and different stop mixing. We have taken  $m_t = 173.1 \text{ GeV}, m_{\tilde{\chi}} = 100 \text{ GeV}$  and  $\tan \beta = 10$ .

We see that a small mass difference between the stop and the neutralino leads to a smaller polarization due to the  $f_1$  and  $f_2$  functions in eq. (2.8). For mass differences of 200–300 GeV, this dependence is negligible. Note that the top originating from a completely mixed stop resembles a right-handed stop because of the effect of the hypercharge mentioned in the previous section.

Figure 3 only shows the results for the pure bino case, where the function  $f_2$  does not contribute significantly to the stop polarization (2.7). We have seen in figures 1 and 2 that masses can have more intricate effects for mixed states due to the contribution of the  $f_2$  function.

#### 2.3 Stop boost

So far we have studied the top polarization in the stop rest frame. However, as we can see from eq. (2.5), the polarization vector  $S^3$  is not a Lorentz vector. Thus the polarization is frame-dependent. We can quantify this effect using the stop boost

$$B_{\tilde{t}} = \frac{|\mathbf{p}_{\tilde{t}}|}{E_{\tilde{t}}} \,. \tag{2.12}$$

The result is plotted in figure 4, showing that the polarization is reduced with increasing stop boost. Note that the polarization is obtained after integration over the top direction, hence depends only on the boost. The helicity of the top quark is invariant under rotations about an arbitrary axis and under a boost along the direction of the top quark. The overall boost of the top quark in the laboratory frame depends on the boost of the stop, that of the top in the stop rest frame and the angle of emission of the top with respect to the stop. The relationship between the polarisation of the top calculated in the stop rest frame and that in the laboratory frame can, in principle, depend on all these in a complicated manner. If, for example, as a result of the different boosts, the top is at rest in the laboratory, the polarization information will be completely lost. However, for interesting values of stop and neutralino masses the boost that the top obtains from stop decay is somewhat lower than the boost of the stop itself and further the scalar nature of stop means that the angular



Figure 4. The dependence of the top polarization on the stop boost for a neutralino that is purely bino  $(Z_{11} = 1)$  and different stop mixing is shown. We have taken  $m_t = 173.1 \text{ GeV}, m_{\tilde{t}} = 500 \text{ GeV}, m_{\tilde{\chi}} = 100 \text{ GeV}$  and  $\tan \beta = 10$ .



Figure 5. The distribution of the stop boost at the LHC with an 8 TeV CM energy for different stop masses is shown on the left-hand side and 14 TeV CM energy on the right-hand side. Both distributions have been generated with Madgraph [71, 72].

distribution of the top in the stop rest frame is uniform. These two facts ensure that the reduction in the top polarization is not so drastic. Figure 5 shows the distribution of the stop boost at the LHC with a CM energy of 8 and 14 TeV. We see that within the relevant range of stop masses, the boost is fairly constant. Thus, the effect of the boost will reduce the polarization for all stop masses, but the explicit mass dependence due to the boost is small.

#### **3** Sensitivity to SUSY parameters

The top polarization in the stop rest frame is sensitive to the stop and neutralino masses and mixing. In the previous section, we have varied one of the relevant parameters at a time. In this section, we examine the dependence of the polarization on the MSSM parameters. We choose parameters such that the value of the light stop mass is around 500 GeV. This mass leads to a large production cross section and has sufficient phase space for the stop to decay in a top and a neutralino for a wide range of values for the neutralino mass. Furthermore, this mass satisfies the limits from direct stop production at the LHC 7 TeV.

|     | $M_{\tilde{Q}_3}$ (TeV) | $M_{\tilde{u}_3}$ (TeV) | $A_t \ ({\rm TeV})$ | $\tan\beta$ | $M_{\tilde{t}_1}$ (GeV) | $\sin\theta_{\tilde{t}}$ | $\cos\theta_{\tilde{t}}$ | $M_h \; ({\rm GeV})$ |
|-----|-------------------------|-------------------------|---------------------|-------------|-------------------------|--------------------------|--------------------------|----------------------|
| LH  | 0.49                    | 2.00                    | 3.00                | 10          | 521.                    | -0.126                   | 0.992                    | 126.4                |
| XLH | 0.55                    | 1.40                    | 2.40                | 20          | 510.                    | -0.223                   | 0.975                    | 124.8                |
| XRH | 1.05                    | 0.60                    | 1.88                | 20          | 498.                    | 0.946                    | -0.323                   | 124.0                |
| RH  | 2.00                    | 0.45                    | 2.40                | 10          | 508.                    | 0.996                    | -0.095                   | 125.5                |

**Table 1.** Choices of parameters in the stop sector for two mostly LH and two mostly RH stops. In each case we also consider a partly mixed light stop (XLH and XRH). The last columns specify the light stop mass, the stop mixing and the Higgs mass for  $|\mu| = 300 \text{ GeV}$ ,  $M_1 = 250 \text{ GeV}$ .

For example the ATLAS Collaboration has excluded a stop up to nearly 500 GeV when the neutralino is massless, but provide no limit if the LSP is heavier than 150 GeV [34].

We first choose fixed values for the soft parameters in the stop sector and vary  $M_1$ and  $\mu$  to show the dependence on the neutralino composition. The four sets of parameters are given in table 1. We set  $M_2 = 4M_1$  to decouple the wino-state and fix  $M_3 = 1.5$  TeV,  $M_A = 1$  TeV. For the soft parameters in the sfermion sector, we choose a common mass for all sleptons  $M_{\tilde{l}} = 800$  GeV and for the first and second generation of squarks,  $M_{\tilde{q}_i} = 2$  TeV. All trilinear couplings except  $A_t$  are set to zero. The supersymmetric spectrum and the Higgs masses are computed with SuSPect [73], which includes radiative corrections.

At this point, we do not impose any constraints on the model. However, we choose the parameters of the stop sector such that the Higgs mass is within the measured range ( $m_H = 125.7 \pm 0.4 \text{ GeV}$ , the average of CMS and ATLAS results [1, 2]) for a large fraction of the parameter space explored after allowing for an additional 2–3 GeV theoretical uncertainty. The expectations for different observables from the flavour or dark matter sector are not taken into account at this point. They will be briefly discussed at the end of this section.

The contour plots for the top polarization as well as for the branching ratio  $BR(\tilde{t}_1 \rightarrow t\tilde{\chi}_1^0)$  in the  $\mu - M_1$  planes are displayed in figure 6–9 for the four different choices of stop parameters. Here we only consider the region where the decay  $\tilde{t}_1 \rightarrow t\tilde{\chi}_1^0$  is kinematically accessible. Note that the maximal variation of the Higgs mass in the  $|\mu| < 1$  TeV,  $M_1 < 750$  GeV plane is about 3 GeV, within the theoretical uncertainties, while corrections to  $m_{\tilde{t}_1}$  of the order of 30 GeV can be found for large values of  $M_2$  due to the quark/gaugino loop correction.

The dominantly left-handed stop. As we have discussed in the previous section, in the case of a left-handed stop we expect  $P_t \approx -1$  when the LSP is bino-like  $(|\mu| \gg M_1)$  and  $P_t \approx 1$  when the LSP is higgsino-like  $(|\mu| \ll M_1)$ . The polarization contours in figure 6 (left) for  $\mu < 0$  illustrate this general behaviour as well as the rapid transition between  $P_t = 1 \rightarrow -1$  in the region where one goes from a bino to a higgsino LSP  $(M_1 \approx \mu)$ . Note, however, that as the LSP becomes almost pure bino, the top polarization starts to deviate from -1. For example at  $M_1 = 100 \text{ GeV}, \mu = -600 \text{ GeV}$  the top polarization is only  $P_t \approx -0.73$ . This occurs because we are not dealing with a pure LH stop, indeed here  $\sin \theta_{\tilde{t}} = -0.127$ . Finally, the kinematic effects which lead to  $P_t \rightarrow 0$  show up at the boundary of the grey region.



Figure 6. Contours of the top polarization in the top rest frame for  $\mu < 0$  and a dominantly LH stop (left panel) with the LH parameters in table 1. Branching ratios for  $\tilde{t}_1 \rightarrow t \tilde{\chi}_1^0$  (right panel). In the bottom right corner, the decay is not kinematically accessible.

To be able to exploit the top polarization as an observable, the branching ratio for  $\tilde{t}_1 \to t \tilde{\chi}_1^0$  must be large enough. The contours for this branching ratio are displayed in the right panel of figure 6. Large branching ratios are found over most of the parameter space with two exceptions. The first occurs near the kinematic limit where the three-body decay  $\tilde{t}_1 \to bW\tilde{\chi}_1^0$  dominates and the second occurs for low values of  $M_1$ . The latter behaviour is a peculiarity due to the fact that we have set  $M_2 = 4M_1$ . Thus for low values of  $M_1$  and of  $M_2$  the lightest chargino, which is dominantly wino, drops below the mass of the stop and the decay  $\tilde{t}_1 \to b\tilde{\chi}_1^+$  becomes dominant. If in addition  $\mu$  is small, the decay into the second chargino becomes possible as well.

In the region where the LSP is mostly higgsino  $|\mu| < M_1$ , the mass of the two lightest neutralino and of the lightest chargino are of the same order. Thus the stop can decay into  $t\tilde{\chi}_1^0, t\tilde{\chi}_2^0$  as well as into  $b\tilde{\chi}_1^+$ . The chargino channel is only at the few percent level while the decay into the LSP increases with the higgsino component reaching a maximum of 70%. An important fact to keep in mind is that the two lightest neutralinos will have higgsino-components of similar magnitude. Thus the polarization of the top in the two processes  $\tilde{t}_1 \rightarrow t\tilde{\chi}_{1,2}^0$  is similar for the higgsino LSP. Thus one can exploit both decay modes to measure the top polarization, as will be demonstrated below. In the region where the LSP is a bino,  $M_1 < |\mu|$ , the branching ratio into the LSP is nearly 100%, except for low values of  $\mu$ , where the channels  $b\tilde{\chi}_1^+$  (for  $|\mu| < 500 \,\text{GeV}$ ) and  $t\tilde{\chi}_2^0$  (for  $|\mu| < 380 \,\text{GeV}$ ) also become accessible.

For  $\mu > 0$ , the polarization and the branching ratio contours have roughly the same behaviour, so we do not illustrate this case. Rather, we consider a case where the light stop is still dominantly left-handed but where the mixing angle is larger,  $\sin \theta_{\tilde{t}} = -0.223$ , see the XLH parameters in table 1. The polarization and branching ratio contours are rather similar to the LH case we have just discussed, see figure 7. The main difference is that in the bino region at large  $\mu$  and small  $M_1$  the polarization is generally not maximal. As we have explained above, the mixing implies that the main contribution to the  $G_i^R$  coupling comes from the first term in eq. (2.9), leading to  $|P_t| < 1$ . This means that in the bino case, the top polarization is quite sensitive to the mixing in the stop sector.



Figure 7. Same as figure 6 for  $\mu > 0$  and a mixed but dominantly LH stop corresponding to the XLH parameters in table 1. In the upper right corner the decay is not kinematically accessible.

The dominantly right-handed stop. Next we consider the case of a dominantly righthanded stop. The polarization contours for  $\mu < 0$  in figure 8 for a mixed RH stop and figure 9 for a pure RH stop follow the expected behaviour:  $P_t \approx 1$  when the LSP is binolike  $(|\mu| \gg M_1)$  and  $P_t \approx -1$  when the LSP is higgsino-like  $(|\mu| \ll M_1)$ . As before, the kinematic effects (at the boundary of the white region) bring  $P_t \rightarrow 0$ . Note also that the sign flip in the polarization as one goes from the bino/higgsino region is very sharp. The only impact of the larger stop mixing, as illustrated in figure 8, lies in the higgsino region ( $\mu < M_1$ ): when the mixing in the stop sector is larger, the top polarization is not maximal. This is because in this case the main contribution to the  $G_i^R$  coupling comes from the second term in eq. (2.9), thus leading to a larger value for  $G_i^R$  and  $|P_t| < 1$ .

In both the pure and mixed RH stop cases, the behaviour of the branching ratio contours are rather similar. The branching ratio  $\tilde{t}_1 \to t \tilde{\chi}_1^0$  is above 90% in the bino region, except near the kinematic limit where the stop decays only into 3-body, and at low values of  $M_1$  for the mixed RH stop. As mentioned above, this is caused by the channel  $\tilde{t}_1 \to b \tilde{\chi}_1^+$ becoming kinematically accessible, which is only possible through the LH component of the light stop. In the higgsino LSP region, the BR never becomes very large (up to roughly 25% for  $t\tilde{\chi}_1$  and to 20% for  $\tilde{\chi}_2, \tilde{\chi}_3$ ). Here the main decay channel is into  $b\tilde{\chi}_1^+$  which has a partial width that is proportional to the top Yukawa coupling for a RH stop and is therefore much larger than in the case of a LH stop where the width is determined by the bottom Yukawa coupling. Thus for a RH stop and a higgsino LSP, it will be more difficult to measure the top polarization because of the suppressed rate.

**Decays into heavier neutralinos.** For a higgsino LSP, the branching ratio of the stop into the lightest neutralino can be rather small. However, in this case the top polarization is almost the same when one considers the decay  $\tilde{t}_1 \rightarrow t \tilde{\chi}_1^0$  or  $t \tilde{\chi}_2^0$  as illustrated in figure 10. For the dominantly LH stop (left panel), the difference between the polarizations in the two channels never exceeds 10% when  $M_1 > \mu$  which marks the onset of the higgsino LSP region. For the RH stop (right panel) the difference between the polarizations can reach 30% when  $M_1 \approx \mu = 280$  GeV although both polarizations quickly become almost equal as  $M_1$  is increased and thus the higgsino fraction of the neutralinos. The difference between



Figure 8. Contours of the top polarization in the top rest frame for  $\mu < 0$  and a mixed dominantly RH stop (left). Branching ratios for  $\tilde{t}_1 \to t \tilde{\chi}_1^0$  (right).



**Figure 9.** Same as figure 8 for  $\mu > 0$  and dominantly RH stop.

the top polarization in the two higgsino channels is purely a kinematic effect due to the smaller mass splitting between the stop and the second neutralino. This effect is more pronounced for the RH stop case simply because the mass of  $\tilde{t}_1$  is lower. Note that since the two lightest neutralinos are almost degenerate the decay of the second neutralino into the LSP is accompanied by soft leptons and has basically the same missing  $E_T$  signature as the LSP. One can therefore use both decay channels to determine the top polarization without being handicapped by small rates.

In the above, we have considered only the behaviour of the top polarization without worrying about other constraints on the model. We briefly comment on the impact of these constraints. For the bino case the relic density is typically much too large, it is however possible to bring it to a reasonable value by decreasing the mass of the sleptons to just above the LSP mass thus adding an important contribution from coannihilation processes. This would have no impact on the polarization observables discussed here. In the higgsino region, as expected the relic density is typically too small. This only means that the neutralino cannot form all of the dark matter. Constraints on observables from the flavour sector are easily satisfied. For instance the branching ratio for  $B_s \to \mu^+\mu^-$  remains near the SM value since we are considering only moderate values of tan  $\beta$  and a heavy pseudoscalar.



Figure 10. Comparison of the top polarization for the decay  $\tilde{t}_1 \rightarrow t \tilde{\chi}_1^0$  (full line) and  $\tilde{t}_1 \rightarrow t \tilde{\chi}_2^0$  (dashed line) as a function of the gaugino mass  $M_1$  for  $|\mu| = 150 \text{ GeV}$  (blue) and  $|\mu| = 300 \text{ GeV}$  (red). SUSY parameters are fixed as in table 1 for a dominantly LH stop (left panel) and a dominantly RH stop (right panel).

For the same reason, the value for  $b \to s\gamma$  falls within the allowed range in the dominantly RH stop case where we have fixed a high mass for the sbottom. However, this observable can receive too large contributions from sbottom/gluino corrections in the LH stop scenario since the LH sbottom is also not too heavy. These contributions can be cancelled, bringing the value for  $b \to s\gamma$  back within the measured range by adjusting the pseudoscalar mass.

#### 4 Top polarization: effect on decay kinematics and observables

We have seen in the previous sections how the top polarization is influenced by (1) the mixing of the stop and neutralinos and (2) the masses of the particles in the decay chain. In this section, we first study the effect of this polarization of the decaying top on the kinematics of the lepton produced in its semi-leptonic decay (eq. (2.1)) and assess the possible effects top polarization can have for the search strategies for the stop. Further we study qualitatively if top polarization at the LHC, measured via this semi-leptonic decay can be a useful probe for the neutralino and stop mixing parameters when there is prior knowledge on SUSY masses. We start by reviewing the decay of the top. We will also see that the angular observables of the semi-leptonic decay can provide a pure measure of polarization.

The polar angle distribution of the top decay product f is described, in the top rest frame, by

$$\frac{1}{\Gamma_l} \frac{\mathrm{d}\Gamma_l}{\mathrm{d}\cos\theta_{f,\mathrm{rest}}} = \frac{1}{2} \left( 1 + \kappa_f P_t \cos\theta_{f,\mathrm{rest}} \right),\tag{4.1}$$

with  $\Gamma_l$  the partial decay width,  $\theta_{f,\text{rest}}$  the rest frame angle between decay product f and the top spin vector,  $\kappa_f$  the analyzing power of the decay product and  $P_t$  the polarization of the top. Effects of polarization are studied most easily for a decay to a positively charged lepton or a down-type quark in which case  $\kappa_f = 1$ . The value of  $\kappa_f$  is only mildly influenced by higher order corrections and non standard tbW couplings. The former induce corrections to  $\kappa_f$  at the permil level for a decay to a down-type quark [58], whereas the latter do not influence  $\kappa_f$  at leading order [67]. Therefore the leptonic decay provides a good probe for the polarization of the top quark, even in the presence of such anomalous couplings. We will further only consider top quarks, since the anti-top can be distinguished by the charge of the decay lepton. In fact while measuring the polarization, one can double the sample by using decays of both the tops and the anti-tops.

One obvious way to measure the polarization of the top is to construct the rest frame of the decaying top. We will here look here however, at the laboratory frame observables with a two fold objective. This will give us an idea of the effect that the top polarization can have on the kinematics of the decay lepton in the laboratory frame and hence on search strategy. Further, it may not be necessarily easy to construct the rest frame of the top at LHC and also because observables constructed out of the laboratory variables can provide an alternate measure of the top polarization.

The use of laboratory frame means that the polar distribution  $\theta_l$  of the top decay products is now described by eq. (4.1) and the subsequent boost from the rest frame to the lab frame. The azimuthal distribution, which is uniform in the rest frame, is influenced by the kinematics of the stop production process through the boost. To determine the azimuthal angle  $\phi_l$ , we must define a frame. The z axis is taken to be the beam direction, and the direction of top momentum together with the beam axis defines the xz plane. The y-axis can then be constructed according to the right-hand rule.

To examine the effect of the top polarization on the kinematic distributions of the semi-leptonic top quark decay product we have generated sets of events with Madgraph [71, 72]. This set of benchmarks has been selected based on the degree of top polarization in the stop rest frame as well as a roughly constant mass difference between stop and neutralino. The physical parameters corresponding to these benchmarks are listed in table 2. We have generated the process

$$p \ p \to \tilde{t} \ \tilde{\bar{t}} \to t \ \tilde{\chi}_1^0 \ \tilde{\bar{t}} \to l^+ \nu_l \ b \ \tilde{\chi}_1^0 \ \tilde{\bar{t}}$$

$$\tag{4.2}$$

We took 8 TeV as LHC center of mass energy and use the following parameter values: the top mass and width are  $m_t = 173.1 \text{ GeV}$  and  $\Gamma_t = 1.50 \text{ GeV}$ , and the W mass and width are  $m_W = 79.82 \text{ GeV}$  and  $\Gamma_W = 2.0 \text{ GeV}$ . The factorization and renormalization scales are set to  $\mu_R = \mu_F = m_{\tilde{t}}$ . It was shown in [42] that NLO corrections do not change the qualitative features of the lab-frame observables constructed out of the angular variables, so we show leading-order (LO) results, which were calculated with the CTEQ6L1 [74] pdf set. Here we implicitly assume that the anti-stop decays hadronically and have generated events where only the stop is decayed. Note however that the sign of the lepton charge can distinguish between the top and the antitop. Hence, exploiting the information from events where the stop decays hadronically and the anti-stop leads to final state with (anti)lepton would only provide increased sensitivity.<sup>1</sup>

<sup>&</sup>lt;sup>1</sup>There could be some ambiguity in pairing the lepton with the parent top, thus reducing the signal efficiency. This issue as well as the problem of the reconstruction of both top quarks would be best addressed with a full simulation which is beyond the scope of this investigation.

| $P_t$ | $m_{\tilde{t}} \; (\text{GeV})$ | $m_{\tilde{\chi}^0_1} \; (\text{GeV})$ | $\sin(\theta_{\tilde{t}})$ | $Z_{i1}$ | $Z_{i4}$  | $\tan(\beta)$ |
|-------|---------------------------------|--|----------------------------|----------|-----------|---------------|
| 1     | 500.0                           | 318.6                                  | 0.998                      | 0.958    | -0.176    | 7.8           |
| 0.5   | 500.0                           | 321.1                                  | 0.998                      | 0.988    | -0.0866   | 7.8           |
| 0     | 500.0                           | 320.5                                  | -0.124                     | 0.975    | -0.128    | 10.0          |
| -0.5  | 501.1                           | 319.2                                  | 0.995                      | 0.440    | -0.618    | 20.0          |
| -0.8  | 502.0                           | 319.3                                  | -0.0988                    | 0.0232   | -0.190    | 35.0          |
| 1     | 500.7                           | 130.2                                  | 0.9928                     | 0.9976   | -0.01883  | 10.           |
| 0.5   | 499.6                           | 129.7                                  | 0.9987                     | 0.9164   | -0.2112   | 29.6          |
| 0     | 500.1                           | 129.3                                  | -0.05954                   | 0.9729   | -0.1017   | 35.0          |
| -0.5  | 500.1                           | 130.3                                  | -0.05948                   | 0.9865   | -0.06113  | 35.0          |
| -1    | 499.4                           | 130.0                                  | -0.05911                   | 0.9990   | -0.007184 | 35.0          |

**Table 2**. Set of benchmarks sorted by polarization. The upper five correspond to small mass differences and the lower five to large mass differences. The mass of the second neutralino is shown for the cases where its branching is non-zero.

## 4.1 Effect of top polarization on $E_l$ and $P_T^l$

In this subsection we show the effect of the top polarization on the energy  $E_l$  and the transverse momentum  $P_T^l$  of the lepton produced in the decay of the top in the laboratory frame for our benchmark points. These two distributions in the laboratory depend on the angular distribution of the lepton given in eq. (4.1) in the top rest frame, as well as the energy and the  $P_T$  of the decaying top which decides the direction and the magnitude of the boost to the laboratory frame. Since the angular distributions have a dependence on the polarization of the decaying top, the  $E_l$  and  $P_T^l$  distributions have a dependence on the top polarization. Most of the decay leptons in the rest frame come in the forward direction for a positively polarized t quark , i.e. the direction of the would-be momentum of the t quark in the laboratory. Thus after a boost from the rest frame to the lab frame the energies of these leptons are increased. Similarly, for negative polarized t quarks most of the decay leptons come out in the backward direction w.r.t. the lab momentum of the t quark. This results in an opposite boost direction and hence a decrease in the energy of the leptons. The effect on the  $P_T$  distribution of the lepton in the laboratory is further also affected by the  $P_T$  of the t quark as well.

Figure 11 shows the  $E_l$  distribution in the laboratory for three different polarizations of the parent top quark: 1, 0 and -1, being depicted in blue, red and black respectively. Since, for the three cases in each figure, the mass difference between the stop and the top is nearly the same, the entire difference in the distributions can only be due to polarization of the decay top. Consistent with the qualitative argument given above, the peak of the  $E_l$ distribution shifts to lower energies for the left polarized top with respect to an unpolarized top and to higher energies for the right polarized one. The shift is higher for the case of large mass differences (with peaks occurring at respectively 26, 42 and 66 GeV) compared



Figure 11. The distribution in the energy of the lepton coming from the decay of the top quark, for three different polarizations of the decaying t quark: 1,0 and -1 being given by the blue, red and the black lines respectively. The left graph represents benchmarks with a small mass difference and the right graph benchmarks with a large mass difference between stop and neutralino.



Figure 12. The distribution in  $P_T$  of the lepton coming from the decay of the top quark. The left graph represents benchmarks with a small mass difference and the right graph benchmarks with a large mass differences between stop and neutralino.

to the small mass difference (with peaks occuring at 34.5, 37.5 and 40.5 GeV). Since, one puts cuts on the lepton kinematic variables to reduce the background from the SM tops (which would have polarization zero) one sees that such cuts will be less effective for a left polarized top and it will be even more so for the case of large mass differences. The distributions for the transverse momentum of the lepton, shown in figure 12 shows similar features. For small mass differences the transverse momentum distribution of a polarization of -1, 0 and +1 respectively peaks at 24, 26 and 31 GeV. For large mass differences the distribution of a polarization of -1, 0 and +1 respectively peaks at 23, 23 and 40 GeV. In fact we also notice that the shifts in the  $P_T^l$  distributions are substantial compared to the possible effects which would come from changes in the  $P_T^{\tilde{t}}$  distribution coming from NLO effects [20, 75, 76] So, this effect needs to be taken into account even in an analysis that neglects the NLO effects on the stop production.

Thus we clearly see that the current limits quoted on the stop quark mass from direct production, using the  $t\tilde{\chi}_1^0$  channel, will depend on the amount of top polarization and in

addition the effect of the mass difference  $m_t - m_{\tilde{\chi}_1^0}$ . This needs to be kept in mind while assessing the limits being quoted currently. The observation above also means that the searches for the stop with SUSY parameters, which give rise to negatively polarized tops are in fact doubly challenged as the single top background will also produce top quarks which are negatively polarized. Whereas for the case of positively polarized top quarks being produced by SUSY, one can use the above distribution to discriminate effectively against the background coming from single top quark production.

This also means that, in principle, information on the energy of the lepton may be used as a 'measure' of the parent top polarization. In fact, for heavily boosted top quarks, studying distributions in fractional energy of the decay lepton and b quark has been shown to carry information about the top polarization [52]. In fact a recent study demonstrates their use for the case of hadronically decaying tops, at the 14 TeV LHC [31]. It should be noted, however, as mentioned earlier, that the energy distributions of the decay products can be affected by the anomalous tbW coupling and hence are less robust a measure of the top polarization of the parent top quark, than the angular observables [42, 66]. We discuss these in the next subsection.

#### 4.2 Observables

In this subsection now we focus on the observables which will give us a measure of the polarization of the top quark, using angular observables of the decay lepton which has the highest analyzing power, which is furthermore unaffected by the anomalous tbW coupling to the leading order [59–65]. We explore utility of various asymmetries constructed out of the  $\phi_l$  and  $\theta_l$  distributions, as in [42, 65, 77, 78].

Azimuthal asymmetries. The azimuthal distributions of the charged lepton from top decay for selected benchmarks are plotted in figure 13. The left plot contains the benchmarks with a small mass difference between stop and neutralino, and the right plot those with a large mass difference. The distributions peak at 0 (and of course  $2\pi$ ), with the stronger peaking for a positively polarized top. The unpolarized top case ( $P_t = 0$  benchmarks) illustrates the influence of the kinematics, since an unpolarized top generates a uniform distribution of decay products in the rest frame. The boost gathers the decay products towards the boost axis. The boost axis in the xy-plane coincides with the x-axis, which is defined by the top momentum in this plane, so around this axis all distributions peak. The peak is not as pronounced for a negative polarization since in this case the decay products are mostly generated backwards in the rest frame (cf. eq. (4.1)). At  $\phi_l = \pi$  the order of peaking is inverted since we are plotting normalized distributions. As expected, the benchmarks with a large mass difference differentiate stronger between different polarizations than small mass differences. In general, the distributions in figure 13 seem to be well separated by their polarization value. Therefore we quantify this with an asymmetry parameter  $A_{\phi}$  defined by

$$A_{\phi} = \frac{\sigma(\cos\phi_l > 0) - \sigma(\cos\phi_l < 0)}{\sigma(\cos\phi_l > 0) + \sigma(\cos\phi_l < 0)}.$$
(4.3)

The polarization is influenced by the boost to the stop labframe (section 2.3). We will treat the transverse momentum  $(p_T)$  of the top as a crude qualifier of this boost and apply



Figure 13. The azimuthal distribution  $\phi_l$  of the decay lepton of the top quark. The left graph represents benchmarks with a small mass difference and the right graph benchmarks with a large mass differences between stop and neutralino.

| $P_t$ | $A_{\phi}$ no cut | $A_{\phi}$ loose cut | $A_{\phi}$ strict cut | $A_{\phi}$ no cut | $A_{\phi}$ loose cut | $A_{\phi}$ strict cut |
|-------|-------------------|----------------------|-----------------------|-------------------|----------------------|-----------------------|
| +1    | 0.57              | 0.51                 | 0.48                  | 0.87              | 0.90                 | 0.90                  |
| +0.5  | 0.53              | 0.45                 | 0.41                  | 0.81              | 0.84                 | 0.84                  |
| 0     | 0.48              | 0.42                 | 0.39                  | 0.69              | 0.67                 | 0.64                  |
| -0.5  | 0.44              | 0.37                 | 0.34                  | 0.61              | 0.60                 | 0.58                  |
| -1.0  | 0.39              | 0.33                 | 0.29                  | 0.55              | 0.50                 | 0.46                  |

Table 3. Relative azimuthal asymmetry parameter for the process as defined in eq. (4.2). The left side of the table denotes small mass differences and the right side large mass differences between stop and neutralino. An adaptive cut is applied on the transverse momentum as defined in eq. (4.4).

a cut on  $p_T$  [67]. Thereby attempting to reduce the polluting effect of the kinematics on the angular distribution. We have defined an adaptive cut as

$$\frac{p_T^{\max}}{x} < p_T < x \, p_T^{\max} \,. \tag{4.4}$$

We define both a strict (x = 1.5) and loose (x = 2) cut. The results for these choices are given in table 3.

From table 3 we notice that the asymmetry parameter  $A_{\phi}$  is large for positive polarizations, decreases for lower polarizations and reaches its lowest value at a negative polarization. As expected, the  $p_T$  cut improves the asymmetry parameter. In the case of a small mass difference, the effect is small. For large mass differences however, the two  $p_T$  cuts enhance the separation of different polarizations. This is natural, as a large stop-neutralino mass difference endows the top with more kinetic energy.

**Polar asymmetries.** We can apply a similar analysis to the distribution in the polar angle, defined as the angle between the direction of the top quark and its decay lepton in the lab frame. The distributions are shown in figure 14. We notice a peaking in the direction of the



Figure 14. The polar distribution  $\theta_l$  of the decay lepton of the top quark. Polarizations in the left figure are chosen such that there is a small mass difference between stop and neutralino. In the right figure the mass difference is large.

| $P_t$ | $A_{\theta}$ no cut | $A_{\theta}$ loose cut | $A_{\theta}$ strict cut | $A_{\theta}$ no cut | $A_{\theta}$ loose cut | $A_{\theta}$ strict cut |
|-------|---------------------|------------------------|-------------------------|---------------------|------------------------|-------------------------|
| +1    | 0.12                | 0.02                   | -0.02                   | 0.66                | 0.66                   | 0.64                    |
| +0.5  | 0.06                | -0.05                  | -0.08                   | 0.55                | 0.55                   | 0.52                    |
| 0     | -0.001              | -0.10                  | -0.13                   | 0.32                | 0.25                   | 0.20                    |
| -0.5  | -0.06               | -0.14                  | -0.17                   | 0.18                | 0.12                   | 0.07                    |
| -1.0  | -0.12               | -0.20                  | -0.22                   | 0.06                | -0.03                  | -0.10                   |

Table 4. Relative polar asymmetry parameter for the process as defined in eq. (4.2). The left side denotes benchmarks with a small mass difference and the right side large mass differences between stop and neutralino. An adaptive cut is applied on the transverse momentum as defined in eq. (4.4).

tion of the top boost which is again strongest for a positive polarization and weakest for a negative polarization. Again the large mass difference cases show a stronger correlation with the polarization  $P_t$  than the small mass difference cases. Because the distribution of  $\theta_l$  is non-symmetric we have more choice for an asymmetry parameter definition that quantifies the shape differences. We have chosen

$$A_{\theta} = \frac{\sigma(\theta_l < \pi/4) - \sigma(\theta_l > \pi/4)}{\sigma(\theta_l > \pi/4) + \sigma(\theta_l < \pi/4)}.$$
(4.5)

The values for this parameter for various values of the adaptive cut on  $p_T$  are listed in table 4.

We notice that  $A_{\theta}$  may become negative. It is of course possible to define the asymmetry parameter such that all values are positive. However, in an experimental analysis, the definition of  $A_{\theta}$  will be tuned to enhance the effects of polarization. As the outcome of this procedure will depend on the masses of the sparticles, we will use the definition given in [42] to show the qualitative effect. The value of  $|A_{\theta}|$  is lowest for positive polarization, increases as the polarization decreases and reaches its highest value at a polarization of  $P_t = -1$ . The adaptive cut again has little effect for the small mass differences but en-

hances mildly the separation of  $A_{\theta}$  for large mass differences and can therefore be a useful probe for polarization.

Impact of the stop neutralino mass difference. We have seen in section 2.2 that the polarization depends on the mass difference between the stop and the neutralino, more precisely on  $\Delta m = m_{\tilde{t}_1} - m_{\tilde{\chi}_1^0} - m_t$ , and that the asymmetry parameter  $A_{\phi}$  is highest for a high polarization for both mass differences. So far we have been studying the effects of polarization whilst keeping this difference constant. However, when we vary  $\Delta m$ , the asymmetry values corresponding to different polarizations are not well separated anymore. For example, we consider a new benchmark with a mass difference that falls in between the two cases in table 2. For this point  $P_t = 0$ ,  $m_{\tilde{t}} = 508.9 \,\text{GeV}$ ,  $m_{\tilde{\chi}_1^0} = 292.4 \,\text{GeV}$ ,  $\sin \theta_{\tilde{t}} = 0.1234$ , and yet the asymmetry  $A_{\phi} = 0.56$  is quite similar to the value for the benchmark  $P_t = 0.5$  in table 3 which has  $A_{\phi} = 0.53$ . The mass difference for these points varies from  $\Delta m = 53 \,\text{GeV}$  for the former and  $\Delta m = 6 \,\text{GeV}$  for the latter. Imposing the adaptive cut on the  $p_T$  of the top enhances the differences between the two benchmarks, but neither cuts are able to isolate the purely polarization induced behavior. For the  $P_t = 0$  benchmark we get  $A_{\phi} = 0.55(0.53)$  for the loose (strict) cut to be compared with  $A_{\phi} = 0.45(0.42)$  for the  $P_t = 0.5$  benchmark. We conclude that varying the mass difference slightly has a large effect on the angular distributions and therefore pollutes the information about polarization present in these angular distributions. Thus, detailed mass measurements will be needed in addition to the polarization-dependent observables. to extract information about the top polarization from these.

**Decays to**  $\tilde{\chi}_2^0, \tilde{\chi}_3^0$ . Thus far we have studied the case where the stop decays to one, generic neutralino type. We next examine the case where we allow for a decay to multiple neutralino types. Two large mass difference benchmarks of table 2 have stop branching ratios to several neutralino types, those with A)  $P_t = 0.5$  and B)  $P_t = 0$ . In case A the heavier neutralino masses are  $m_{\tilde{\chi}_2^0} = 207 \,\text{GeV}, m_{\tilde{\chi}_3^0} = 213 \,\text{GeV}$  while in case B,  $m_{\tilde{\chi}_2^0} = 276 \,\text{GeV}, m_{\tilde{\chi}_3^0} = 282 \,\text{GeV}$ . The heavier neutralinos are higgsino-like so that the polarization is close to  $P_t = -1$  in case A which has a RH stop and to  $P_t = 1$  in case B with a LH stop. We have listed the separate contributions to  $P_t$  and the asymmetries  $A_{\phi}$  and  $A_{\theta}$  in table 5. The difference in the asymmetries between various neutralino channels is somewhat less than naively expected. This is because the mass difference  $\Delta m$  is smaller for heavier neutralinos, thus reducing the difference in the asymmetries as discussed above. This effect is particularly noticeable for the second case where despite the fact that  $P_t = 0(1)$  for the light (heavier) neutralinos, all three neutralinos give rise to almost the same asymmetries.

With the theoretical prediction on the rest frame polarization per decay mode on the basis of eqs. (2.8) and (2.9), the lab frame distributions can then be predicted after combination with the appropriate Lorentz transformations. The asymmetry parameter for all decays is a sum of the individual values weighted by branching ratios. The extent to which  $A_{\phi}$  depends on the angular distribution of a certain decay mode therefore depends strongly on the branching fractions. The results including adaptive cuts for the two benchmarks of table 5 are shown in table 6. Clearly the asymmetries are dominated by the heavier

|   | Case A       |       |      |            | Case B       |       |               |  |  |
|---|--------------|-------|------|------------|--------------|-------|---------------|--|--|
| $A_{\phi}$  | $A_{\theta}$ | $P_t$ | BR   | $A_{\phi}$ | $A_{\theta}$ | $P_t$ | $\mathbf{BR}$ |  |  |
| 0.81  | 0.55         | 0.5   | 6.5% | 0.69       | 0.31         | 0.0   | 2.7%          |  |  |
| 0.53  | 0.04         | -1.0  | 20%  | 0.71       | 0.34         | 0.99  | 29.3%         |  |  |
| 0.53  | 0.05         | -0.88 | 18%  | 0.69       | 0.31         | 0.96  | 29.8%         |  |  |
| and polar asymmetry parameter for the process as defined in eq. $(4.2)$ all |              |       |      |            |              |       |               |  |  |

**Table 5.** Azimuthal and polar asymmetry parameter for the process as defined in eq. (4.2) allowing for decays of the stop to a certain neutralino type. The polarization and branching fraction for the decay into each neutralino channel is also specified. Case A and Case B correspond respectively to the second and third rows of the large mass difference benchmarks in table 2.

|   | $P_t(t\tilde{\chi}_1^0)$ | $A_{\phi}$ no cut | $A_{\phi}$ loose cut | $A_{\phi}$ strict cut | $A_{\theta}$ no cut | $A_{\theta}$ loose cut | $A_{\theta}$ strict cut |
|---|--------------------------|-------------------|----------------------|-----------------------|---------------------|------------------------|-------------------------|
| A | +0.5                     | 0.58              | 0.53                 | 0.50                  | -0.13               | -0.03                  | 0.02                    |
| В | 0                        | 0.70              | 0.69                 | 0.68                  | -0.32               | -0.26                  | -0.22                   |

Table 6. Azimuthal and polar asymmetry parameter for the process as defined in eq. (4.2) allowing for decays of the stop to all neutralino types. An adaptive cut is applied on the transverse momentum as defined in eq. (4.4).

neutralino decay channels for case A while they receive similar contributions from all three neutralino channels for case B.

# 5 Conclusion

 $\frac{\text{decay to}}{\chi_1^0}$  $\frac{\chi_2^0}{\chi_3^0}$ 

The phenomenology of the third generation sfermions has always been an interesting subject to explore as this can yield non-trivial information about SUSY parameters. In view of the ever increasing upper limits on the masses of the strongly interacting sparticles that are being extracted from LHC data and the observation of a light, single Higgs-like particle naturalness considerations within the MSSM leads to the possibility of third generation sfermions that are much lighter than the first two generations. Thus direct pair production cross-sections of both stops and sbottoms can be large enough to be probed within the current run of the LHC. The top quarks produced in these decays are generally polarized and this polarization holds information about mixing in the squark sector, mixing in the chargino/neutralino sectors as well as on the top velocity, hence on the mass difference between the squark and the neutralino/chargino. The parameters that affect the top polarization will influence the effectiveness of the searches for stops. Thus, the limits extracted will not only depend on the stop and neutralino mass but also on the assumed polarization. Indeed, the polarization can affect the energies of decay leptons and hence the optimization of cuts to reduce the background from the QCD produced unpolarized top. Since the top polarization goes to zero in the limit of a small stop-neutralino mass difference, the polarization-induced kinematic effects will be particularly important for models where this mass difference is large. This is an important factor to keep in mind in analyses using simplified models with large mass differences. To obtain a conservative limit, one should use a model which produces a completely negatively polarized top quark.

We have explored the possible values of the top polarization in the decay of the lightest stop into a top and a neutralino and we have scanned the parameter space which is consistent with a light Higgs. We find that the bino content of the neutralino is a critical parameter and that due to the largeness of the hypercharge for the right-handed top which drives the bino-stop-top coupling, a mixed stop often behaves like a RH stop. A dominantly RH stop produces a negative top polarization when it decays into a higgsino and a positive polarization when the decay is into a bino, and vice-versa for a LH stop. This implies that positive top polarization leads to more energetic leptons, allowing for events to be separated more easily from the top pair background. The LH stop with a higgsino LSP and the RH stop with a bino LSP could be more tightly constrained at the LHC than the other two combinations. We have also shown that although small branching ratios into the lightest neutralino can occur especially for the decay into a higgsino, similar polarizations for the decay into the two higgsino states imply that we can exploit both decay modes to measure the top polarization. Finally, a small mass difference between the stop and the neutralino leads to a very small polarization.

We analyzed the kinematics of the decay products of the top arising from stop decay into a top and a neutralino in the laboratory frame. Since the majority of the top quarks in the SM background are unpolarized the stop search is particularly challenged in the  $t\tilde{\chi}_1^0$  mode for points in the parameter space which give rise to tops with negative polarization. The spectrum of the electron energy as well as transverse momentum of the lepton, softens (hardens) for negatively (positively) polarized top quarks respectively, compared to an unpolarized top quark. This modification of the position of the peak increases with increasing value of  $m_{\tilde{t}} - m_{\tilde{\chi}_1^0}$ . For the electron energy spectrum the shift is -30 GeV for  $m_{\tilde{t}} - m_{\tilde{\chi}_1^0} \sim 320 \text{ GeV}$  and -16 GeV for  $m_{\tilde{t}} - m_{\tilde{\chi}_1^0} \sim 130 \text{ GeV}$ . Thus we see that even with the same kinematics, the reach of a particular search using the lepton is less efficient for negatively polarized tops. This effect is more pronounced for large mass differences between the stop and the neutralino.

Finally, we have studied lab-frame observables and defined asymmetries in the polar and azimuthal angle. These asymmetries have both a polarization-dependent and independent part and provide a useful probe for top polarization provided the masses of the particles involved are known, since the polarization is very sensitive to mass differences. In conclusion, study of the top polarization can provide useful information on supersymmetric parameters at the LHC when the supersymmetric partner of the top is discovered.

Note added. As this paper was finalised new results from direct stop searches were presented by ATLAS including  $13fb^{-1}$  of data from the 8TeV run [79]. These extend the stop exclusion to 580 GeV for massless neutralinos. When they decay exclusively into  $t\tilde{\chi}_1^0$ stops of 500 GeV are excluded if the neutralino LSP is lighter than 200 GeV. These limits can be somewhat weakened because of smaller branching ratios as well as because of top polarization effects. Only one of the benchmark we have used in this paper falls within the ATLAS exclusion, the one with  $P_t = 1$  and large mass difference.

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