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## WORKING PAPER SERIES

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Department of Economics

Competitive Advantage
in the Global Economy

# Mediation and Peace* 

Johannes Hörner ${ }^{\dagger} \quad$ Massimo Morelli ${ }^{\ddagger} \quad$ Francesco Squintani ${ }^{\S}$

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#### Abstract

This paper applies mechanism design to conflict resolution. We determine when and how unmediated communication and mediation reduce the ex ante probability of conflict in a game with asymmetric information. Mediation improves upon unmediated communication when the intensity of conflict is high, or when asymmetric information is significant. The mediator improves upon unmediated communication by not precisely reporting information to conflicting parties, and precisely, by not revealing to a player with probability one that the opponent is weak. Arbitrators who can enforce settlements are no more effective than mediators who only make non-binding recommendations.


## 1 Introduction

Over the years, the formal theory of international relations has much developed the positive analysis of conflict by making use of advanced game theoretical techniques. ${ }^{1}$ Instead, the powerful tools of mechanism design have not yet been extensively used to explore which

[^0]institutions may be more effective for conflict resolution and prevention. ${ }^{2}$ The revelation principle, a fundamental result in mechanism design due to Myerson (1979), identifies mediation as an efficient institution to deal with conflicts that arise because of asymmetric information, one of the main rationalist explanations for wars. ${ }^{3}$ Indeed, mediation has played an increasingly important role in the organization of peace talks to resolve recent international crises. According to the International Crisis Behavior (ICB) project, the most comprehensive empirical effort to date, $30 \%$ of international crises for the entire period 1918-2001 were mediated, and the fraction rises to $46 \%$ for the period 1990-2001 (see Wilkenfeld et al., 2005). In a simple model of conflict, this paper first asks when, and how, mediation improves the ex ante probability of peace with respect to unmediated peace talks. ${ }^{4}$ Second, we ask whether arbitration improves on mediation, to explore the relevance of the power of enforcing settlements in international conflict resolution. ${ }^{5}$

Before describing our specific set up and findings, we briefly motivate our general modelling choices.

In line with the mechanism design literature, we consider unbiased mediators who have no private information. ${ }^{6}$ Further, the mediator's objective is the minimization of the ex-ante

[^1]probability of war. Hence, our mediator must be able to commit to quit in some circumstances, instead seeking a peaceful agreement in all contingencies (see Watkins, 1998). Such commitments, in fact, facilitate information disclosure by the contestants, and ultimately improve the ex-ante chances of peaceful conflict resolution. ${ }^{7}$ Finally, we study mediators who have no independent budget for transfers or subsidies, and cannot impose peace to the contestants. To be sure, third-party states that mediate conflict, such as the United States, are neither unbiased nor powerless; However, single states account for less than a third of the mediators in mediated conflicts (Wilkenfeld, 2005), so that we view our assumption not only as a useful theoretical benchmark, but also as a reasonable approximation for numerous instances of mediated crises.

Unlike most of the mechanism design literature, we assume that the mediator's proposals must be self-enforcing. ${ }^{8}$ Indeed, countries are sovereign, and enforcement of contracts or agreements is often impossible in international relations (see e.g. Waltz, 1959). ${ }^{9}$ This assumption is formalized by introducing ex post individual rationality constraints requiring that both contestants find proposed peaceful settlements more advantageous than starting conflict. In the terminology of Fisher (1995), our mediators perform "pure mediation," i.e., they gather information and propose settlements, rather than "power mediation," which also involves mediator's power to reward, punish or enforce. In order to describe the difference between arbitration and mediation, in the final section, we relax ex post individual rationality and introduce standard ex interim individual rationality constraints.

To achieve their objectives, mediators can facilitate communication, formulate propos-

[^2]als, and manipulate the information transmitted (see Touval and Zartman, 1985, for a discussion of these three roles; and Wall and Lynn, 1993, for an exhaustive discussion of all observed mediation techniques). Because we consider unmediated cheap talk as a benchmark, our mediators can only improve the chances of peace by managing the flow of information between the parties. In practice, this corresponds to the mediator's role in "collecting and judiciously communicating select confidential material" (Raiffa, 1982, 108109). Obviously, this activity requires private and separate caucuses. Indeed, the practice of shuttle diplomacy has become popular since Henry Kissinger's efforts in the Middle East in the early 1970s and the Camp David negotiations mediated by Jimmy Carter, in which a third party conveys information back and forth between parties, providing suggestions for moving the conflict toward resolution (see, for example, Kydd, 2006). In the real world, mediators also often prevent conflict by facilitating communication or coordinating discussions among parties unwilling to communicate without a mediator. Such instances of mediation correspond to what we formally call unmediated communication. Our paper confirms the value of mediators as communication facilitators, by showing that communication often reduces the chance of conflict.

Having clarified our methodological choices and our general motivation, we now describe the basic features of our model and then offer a preview of our findings.

We consider a simple model of conflict, in which two players contest fixed amount of resources. ${ }^{10}$ A player cannot observe the opponent's strength, political resolve, or willingness to fight. Specifically, each player is strong (hawk) with some probability and weak (dove) otherwise. If the two players are of the same type, war is a fair lottery; else, the stronger wins with higher probability. For simplicity, we assume that all wars are equally costly. ${ }^{11}$

[^3]We consider a simple game where the two players simultaneously choose whether to agree to a given resource split, and war takes place unless both players agree. For any value of the split, we calculate the equilibrium that maximizes the ex ante chances of peace. Then, we choose values of the split that maximize the peace chances. ${ }^{12}$

In order to introduce unmediated communication, we augment our basic model by letting the peaceful split parameter depend on cheap-talk messages priorly shared by the players, and on the realization of a public randomization device. Indeed, it is known that public randomization devices may be reproduced by simultaneous cheap talk (see, Aumann and Hart, 2003). When war cannot be avoided in our benchmark model, the optimal separating communication equilibrium is shown to improve on no-communication. Intuitively, it allows players to reveal their type, and establish type-dependent splits to avoid conflict. However, war cannot be fully avoided. ${ }^{13}$

We then consider mediated communication. First, the mediator collects the players' messages privately. Then, she optimally chooses message-dependent split proposals, possibly randomizing. ${ }^{14}$ Given these definitions, we can now report our main results.

- When does a mediator help? The mediator's optimal solution cannot be worse than any equilibrium without the mediator. In fact, the mediator could always, trivially, make the messages she receives public, thereby mimicking the optimal unmediated communication equilibrium. Further, the mediator strictly improves the peace chance in two distinct sets of circumstances. First, when the intensity (or cost) of conflict is

[^4]high. Second, when the intensity of conflict is low, but the uncertainty regarding the disputants' strength is high. ${ }^{15}$

- How does the mediator help? When conflict intensity is high, the mediator can improve upon unmediated communication by offering unequal splits even when she observes both players reporting to be doves. This is equivalent to an obfuscation strategy by which the mediator does not reveal with probability one to a self-declared dove that she is facing a dove. When the intensity is low but uncertainty is high, the mediator's strategy involves proposing equal split settlements even when she receives different messages. Equivalently, the mediator does not always reveal to a self-declared hawk that she is facing a dove.

Although it is widely believed that a successful mediator should issue credible reports to the conflicting parties, we find that such a reporting strategy would be sub-optimal. Specifically (and realistically), the mediator should not always reveal that a player is weak, when this is the case.

- Does arbitration improve on mediation? Surprisingly, we find that an arbitrator who can enforce settlements is no more effective in preventing conflict than a mediator who can only propose self-enforcing agreements. ${ }^{16}$ Our results are in line with the view that a mediator should not necessarily need enforcement power: "A mediated settlement that arises as a consequence of the use of leverage may not last very long because the agreement is based on compliance with the mediator and not on internalization of the agreement-changed attitudes and perceptions" (Kelman, 1958).

[^5]We conclude the introduction by discussing a few papers that, like us, study mechanism design in international conflicts. The basic game of conflict and arbitration model studied in this paper are binary versions of the model by Bester and Wärneryd (2006), who, unlike us, do not solve the more involved mediation and unmediated communication problem. Fey and Ramsay (2009) establish simple sufficient conditions for mediation and communication to achieve peace with probability one; unlike us, do not characterize optimal mechanisms when they do not yield peace with probability one. ${ }^{17}$ Fey and Ramsay (2010) show that mediation and unmediated communication yield the same outcomes in the special case when all private information concerns only one's cost of fighting. Ours is the first paper that solves the optimal mediation and unmediated communication problem in a game of conflict where each player's private information includes features that bear direct implications on the outcome of war, such as military strength, political resolve, or preference for fighting.

The paper is organized as follows. Section 2 introduces our basic model of conflict. Section 3 studies unmediated communication. Section 4 solves optimal mediation. Section 5 compares mediation and arbitration. The final section offers some concluding comments. In particular, it discusses interim mechanism selection, mediator's commitment and contestants' renegotiation. All proofs are in appendices.

## 2 The Game of Conflict

Two players contest a cake of size normalized to one. ${ }^{18}$ War shrinks the value of the cake to $\theta<1$. The expected payoffs in case of war depends on both players' private types. Each player can be of type $H$ or $L$ with probability $q$ and $(1-q)$, respectively. ${ }^{19}$ This

[^6]private characteristic can be thought of as related to resolve, military strength, leaders' stubbornness, etc. We will often refer to type $H$ as a "hawk" and to a $L$ type as a "dove" (with no reference to the hawk-dove game). When the two players are of the same type, the expected share of the cake in case of war is $1 / 2$ for both. When a type $H$ player fights against an $L$ type, her expected share of the cake is $p>1 / 2$, and hence her expected payoff is $p \theta$. If $p \theta<1 / 2$, the problem is trivial as conflict can always be averted with the anonymous split $(1 / 2,1 / 2)$; we shall therefore assume henceforth that $p \theta>1 / 2$.

We consider a simple "agreement" game where the two players simultaneously choose whether to agree to a given cake division $(x, 1-x)$, where $x \in[0,1]$ is a parameter of the game. Unless both players agree to the split, war takes place. ${ }^{20}$ We assume that when the two players accept a peaceful split, this prevents war. ${ }^{21}$ For any value of the split, we calculate the equilibria that maximize the ex ante chances of peace. Then, we choose values of the split that maximize the peace chance, which will be denoted by $V$, the value. Our benchmark model is therefore directly comparable with the mediation and unmediated communication programs that we will later describe in details. In fact, it can be reformulated as a simple program where the split $x \in[0,1]$ is chosen so as to maximize peace chances, subject to ex-post individual rationality constraints only, without allowing players the possibility to communicate.

The model has three parameters: $\theta, p$, and $q$. Yet, it turns out that a more parsimonious

[^7]description of all results depend on only two statistics: ${ }^{22}$
$$
\lambda \equiv \frac{q}{1-q} \text { and } \gamma \equiv \frac{p \theta-1 / 2}{1 / 2-\theta / 2}
$$

The parameter $\lambda$ is the hawk/dove odds ratio, and $\gamma \geq 0$ represents the ratio of benefits over cost of war for a hawk: the numerator is the gain for waging war against a dove instead of accepting the equal split, and the denominator is the loss for waging war against a hawk rather than accepting equal split. Given that $\gamma$ is increasing in $\theta$, we will also interpret situations with low $\gamma$ as situations of high intensity or cost of conflict.

Armed with this simplification, we can now calculate the splits $(x, 1-x)$ and equilibria in the consequent war-declaration game that maximize the ex ante probability of peace. First, note that for $q \theta / 2+(1-q) p \theta \geq 1 / 2$, or $\lambda \geq \gamma$, both doves and hawks choose peace in the peace-maximizing equilibrium of the game with $x=1 / 2$. When $\lambda<\gamma$, the probability of peace is maximized by setting $x$ so that all doves play peace, together with the hawk type of one of the two players. This is achieved by setting $x \geq p \theta$, so as to convince the hawk type of player 1 to play peace, against a player 2 who plays peace if and only if dove, and $1-x \geq(1-q) \theta / 2+q(1-p) \theta$, so as to convince the dove type of player 2 to play peace, against a player 1 who always plays peace. These two inequalities are both satisfied for some $x$ if and only if $(1-q) \theta / 2+q(1-p) \theta+p \theta \leq 1$, i.e., $\lambda \geq \frac{1}{2}(\gamma-1)$, which is always satisfied when $\gamma \leq 1$. When this condition fails, the probability of peace is maximized by setting $x=1 / 2$ so that doves play peace, and hawks declare war.

In sum, the optimal probability of peace absent communication or mediation is:

$$
V= \begin{cases}(1-q)^{2}=\frac{1}{(\lambda+1)^{2}} & \text { if } \lambda<\frac{1}{2}(\gamma-1) \\ 1-q=\frac{1}{\lambda+1} & \text { if } \frac{1}{2}(\gamma-1) \leq \lambda<\gamma \\ 1 & \text { if } \lambda \geq \gamma\end{cases}
$$

[^8]
## 3 Communication Without Mediation

Communication Game In order to study the value of unmediated communication, we augment our basic model as follows. After privately learning her type, each player $i$ sends a message $m_{i} \in\{l, h\}$. The two messages are sent simultaneously. After observing each other's message, the players play a specification of the agreement game, where the split $x$ may depend on the messages $m=\left(m_{1}, m_{2}\right)$ and on the realization of a public randomization device. Specifically, we assume that with probability $1-p(m)$ a split $x(m)$ is selected that induces war as the unique equilibrium of the agreement game, e.g., $x(m)=0$. With probability $p(m)$, the split $x(m)$ is selected so as to induce peace in equilibrium. We calculate the optimal values of the peaceful splits $x(\cdot)$ and the probabilities $p(\cdot)$ subject to the constraints that players are willing to use the equilibrium communication and agreement strategies.

Before proceeding with the analysis, we briefly comment on the characteristics of our communication protocol. Relative to the benchmark without communication, we have introduced one round of binary cheap talk, and a public randomization device. Following Aumann and Hart (2003), such a public randomization device can be replicated by an additional round of communication (using so-called jointly controlled lotteries). Hence our game can be reformulated as a two-round communication game without any extraneous randomization device. For the sake of tractability, we do not consider the possibility of further rounds of cheap talk. ${ }^{23}$ The restriction to binary messages is natural given the binary type space. When focusing on pure-strategy equilibria, this restriction is without loss of generality. But it is possible that more messages might help in mixed-strategy equilibria (numerical optimization shows that allowing for three messages does not help). On the other hand, the restriction to a single peaceful split $x(m)$, for every $m$, rather than the consideration of a lottery over peaceful splits, is without loss of generality. ${ }^{24}$

[^9]Pure-strategy Equilibria. We momentarily ignore mixed strategies by the players at the message stage. Those will be considered in the next subsection. Evidently, there is always a pooling equilibrium in which both types choose the same reporting strategy, whose outcomes coincide with the equilibrium of the agreement game without communication. We now consider separating equilibrium, i.e., equilibrium in which each player truthfully reveals her type.

Let us consider here only equilibria with peaceful splits $x(m)$ and probabilities $p(m)$ that are symmetric across players. Such symmetry restriction entails that $x(h, h)=x(l, l)=$ $1 / 2$, and that we only need to find another split value, i.e., $b \equiv x(h, l)=1-x(l, h)$, given that the message space contains only two elements. We shall later see that this restriction is without loss of generality, because the separating equilibrium which minimizes the ex ante probability of peace is calculated by solving a linear program. ${ }^{25}$ To shorten notation further, we let $p_{L} \equiv p(l, l), p_{H} \equiv p(h, h)$ and $p_{M} \equiv p(h, l)=p(l, h)$.

Armed with these definitions, the optimal separating equilibrium is characterized by the following program. Maximize the peace probability

$$
\min _{b, p_{L}, p_{M}, p_{H}}(1-q)^{2}\left(1-p_{L}\right)+2 q(1-q)\left(1-p_{M}\right)+q^{2}\left(1-p_{H}\right)
$$

subject to the following ex post individual rationality (IR) constraints and ex interim incentive compatibility constraints $\left(I C_{L}^{*}, I C_{H}^{*}\right){ }^{26}$ First, reporting truthfully must be optimal.

[^10]For the dove. This constraint $\left(I C_{L}^{*}\right)$ states that

$$
\begin{aligned}
& (1-q)\left(\left(1-p_{L}\right) \theta / 2+p_{L} / 2\right)+q\left(\left(1-p_{M}\right)(1-p) \theta+p_{M}(1-b)\right) \geq \\
& (1-q)\left(\left(1-p_{M}\right) \theta / 2+p_{M} \max \{b, \theta / 2\}\right)+q\left(\left(1-p_{H}\right)(1-p) \theta+p_{H} \max \{1 / 2,(1-p) \theta\}\right) .
\end{aligned}
$$

The left-hand side is the dove's equilibrium payoff. With probability $1-q$, the opponent is also a dove, in which case the equal split $1 / 2$ occurs with probability $p_{L}$ and the payoff from war, $\theta / 2$, is collected with probability $\left(1-p_{L}\right)$. With probability $q$, the opponent is hawk. With probability $p_{M}$, this leads to the split $1-b$, and with probability $1-p_{M}$ to the payoff from war $(1-p) \theta$. The right-hand side is the expected payoff from exaggerating strength. When the opponent is dove, the split $b$ is recommended with probability $p_{M}$. In principle, the player may deviate from the recommendation, and collect the war payoff $\theta / 2$, hence the payoff is $\max \{b, \theta / 2\}$. Further, war takes place with probability $1-p_{M}$. When the opponent is hawk, the split $1 / 2$ is recommended with probability $p_{H}$, and war occurs with probability $1-p_{H}$. Similarly, for the hawk, the constraint $\left(I C_{H}^{*}\right)$

$$
\begin{aligned}
& (1-q)\left(\left(1-p_{M}\right) p \theta+p_{M} b\right)+q\left(\left(1-p_{H}\right) \theta / 2+p_{H} / 2\right) \geq \\
& (1-q)\left(\left(1-p_{L}\right) p \theta+p_{L} \max \{1 / 2, p \theta\}\right)+q\left(\left(1-p_{M}\right) \theta / 2+p_{M} \max \{1-b, \theta / 2\}\right)
\end{aligned}
$$

must hold, where the left-hand side is the equilibrium payoff and the right-hand side is the expected payoff from "hiding strength." ${ }^{27}$

Second, players must find it optimal to accept all peaceful splits. Given that, in a
constraints. As anticipated earlier, such maxima make the deviation payoff convex in the recommended peaceful split.
${ }^{27}$ Even though the constraints $\left(I C_{L}^{*}\right)$ and $\left(I C_{H}^{*}\right)$ are not linear because of the maxima and of the products $p_{M} b$, they can be turned into linear constraints as follows. First, one replaces each constraint with four constraints in which the left-hand sides equal the left-hand side of the original constraint with one of the four pairs of the arguments of the two maxima, in lieu of the maxima. Second, one changes the variable $b$ with $p_{B}=p_{M} b$ and the constraint $1 / 2 \leq b \leq 1$ with $p_{B} \leq p_{M} \leq 2 p_{B}$.
separating equilibrium, messages reveal types, this requires that

$$
b \geq p \theta, \quad 1-b \geq(1-p) \theta
$$

That is, a hawk facing a self-proclaimed dove must get a share $b$ that makes war unprofitable against a dove. Similarly, the dove's share against a hawk cannot be so low that it is better for her to go to war. The constraint that a player would accept an equal split when the opponent's type is the same as her own, $1 / 2>\theta / 2$, is always satisfied.

Solving this program yields the following characterization. We here omit the precise equilibrium formula, presented in the Appendix, as it is quite burdensome.

Proposition 1 There is a unique best separating equilibrium in the communication game without mediation. This equilibrium displays the following characteristics, for $\lambda<\gamma$ :

- The ex ante probability of peace is strictly greater than in the absence of communication.
- Dove dyads do not fight: $p_{L}=1$.
- Hawk dyads fight with positive probability, $p_{H}<1$, and the dove's incentive compatibility constraint $I C_{L}^{*}$ binds.
- If $\gamma \geq 1$ and/or $\lambda \geq(1+\gamma)^{-1}$, then the hawk's incentive compatibility constraint $I C_{H}^{*}$ does not bind, and $b=p \theta$; further:
- if $\lambda<\gamma / 2$, then hawk dyads fight with probability one, $p_{H}=0$, and asymmetric dyads fight with positive probability, $p_{M} \in(0,1)$;
- if $\lambda \geq \gamma / 2$ (which covers also the case $\lambda \geq(1+\gamma)^{-1}$ ), then hawk dyads fight with positive probability, $p_{H} \in(0,1)$, and asymmetric dyads do not fight, $p_{M}=0$.
- If $\gamma<1$ and $\lambda<(1+\gamma)^{-1}$, then $I C_{H}^{*}$ binds and $b>p \theta$; and further $p_{H}=0$ and $p_{M} \in(0,1)$ for $\lambda<\gamma /(1+\gamma)$, whereas $p_{H} \in(0,1)$ and $p_{M}=1$ otherwise.

We now elaborate on the characterization described above.
First, the separating equilibrium always improves upon the agreement game without communication. While intuitive, this result is far from obvious: While at least one equilibrium of the communication game must be at least as good as the optimal agreement game equilibrium, it is not an obvious implication that the separating equilibrium would strictly improve upon all equilibria without communication.

Second, war is never optimal when both players report low strength: $p_{L}=1$; intuitively, there is no need to punish self-reported doves by means of war, as they receive lower splits on average than if reporting to be hawks.

Third, the truth-telling constraint for the low type, $I C_{L}^{*}$, is always binding, because on average hawks receive higher peaceful splits than doves. Given that the incentive to exaggerate strength must be discouraged, there needs to be positive probability of war following a high report. The most potent channel through which the low type's incentive to exaggerate strength can be kept in check is by assigning a positive probability of war whenever there are two self-proclaimed high types. When $\lambda$ is low (few high types) it is indeed optimal to set $p_{H}=0$ and $p_{M}>0$, whereas for higher values of $\lambda, p_{H}<1$ and $p_{M}=1$. When $\lambda$ is sufficiently high, the likelihood of a hawk is sufficiently high that prescribing war against a dove is not needed to deter a dove to exaggerate strength. But when $\lambda$ is low, deterring misreporting by a dove requires having self-reported hawks fight both against hawks and doves, with positive probability.

Fourth, when the truth-telling constraint for the high type, $I C_{H}^{*}$, is not binding, then $b=p \theta$; and when both truth-telling constraints are binding, then the ex post IR constraint $b \geq p \theta$ does not bind. Hence, $b$ is either pinned down by the ex post IR constraint $b \geq p \theta$, or by the joint ex interim truth-telling constraints. Intuitively, both $\left(I C_{H}^{*}\right)$ and the constraint $b \geq p \theta$ need $b$ sufficiently large to be satisfied. On the other hand, keeping in check the (binding) constraint ( $I C_{L}^{*}$ ) requires keeping $b$ as low as possible. Hence $b$ will be such that either $I C_{H}^{*}$ binds, or $b=p \theta$.

The other properties of the characterization of Proposition 1 are best described by distinguishing the cases $\gamma \geq 1$ and $\gamma<1$.

Suppose first that $\gamma \geq 1$, so that the benefits from war are sufficiently high. Then the ex post IR constraint always binds, and hence $b=p \theta$; and the ex interim high-type truth-telling $I C_{H}^{*}$ constraint never binds. This is because the hawk hiding strength always prefers to wage war (both against hawks and doves). When $b=p \theta$, the condition $\gamma \geq 1$ is equivalent to $1-b \leq \theta / 2$. As a result, the hawk obtains the payoff $p \theta$ against doves, regardless of her message, whereas against hawks she obtains $\theta / 2$ if hiding strength, and either $\theta / 2$ (after a war recommendation) or $1 / 2$ (after settlement) when truthfully reporting. In sum, hawks receive a higher payoff if revealing their type, and the $I C_{H}^{*}$ constraint never binds.

Second, suppose that $\gamma<1$. For $\lambda \leq 1 /(1+\gamma)$, the high-type truth-telling constraint $I C_{H}^{*}$ binds, and $b>p \theta$. To see why, suppose by contradiction that $b=p \theta$. For $\gamma<1$, this would imply that $1-b>\theta / 2$. Consider a hawk pretending to be a dove. If she meets a dove, she can secure the payoff $p \theta$ by waging war. This is also the payoff for revealing being hawk and meeting a dove: She obtains $p \theta$ through war or through the split $b=p \theta$. If she meets a hawk, she gets $1-b$ with probability $p_{M}$ and $\theta / 2$ with probability $1-p_{M}$. By claiming to be a hawk, she gets $1 / 2$ with probability $p_{H}$ and $\theta / 2$ with probability $1-p_{H}$. But we know that $p_{M}$ is larger than $p_{H}$, and because $1-b>\theta / 2$, this gives an incentive to pretend to be a dove (hiding strength) to secure peace more often than by revealing that she is a hawk, which contradicts $I C_{H}^{*}$. To make sure that both truth-telling constraints are satisfied, we must have $b>p \theta$, so as to reduce the payoff from hiding strength. This reduces both the payoff from settling against a hawk when hiding strength and the payoff from settling against a dove when revealing to be hawk.

To see why $b=p \theta$ when $\lambda \in[1 /(1+\gamma), \gamma]$, even if $\gamma<1$, note that $p_{H}$ increases in $\lambda$, as in the case of $\gamma \geq 1$. Because the incentive to hide strength decreases as $p_{H}$ increases relative to $p_{M}$, we can reduce $b$ as $\lambda$ increases. When $\lambda$ reaches the threshold $1 /(1+\gamma)$,
the offer $b$ required for the high type truth-telling constraint to bind is exactly $p \theta$. Further increasing $\lambda$ cannot induce a further decrease in $b$, because the ex post IR constraint $b \geq p \theta$ becomes binding. So in the region where $\lambda \in[1 /(1+\gamma), \gamma]$, the $I C_{H}^{*}$ constraint does not bind and $b=p \theta$.

We conclude this subsection by discussing the probability of peace in the best separating equilibrium, pictured in Figure 1. For $\gamma \geq 1$, it is U -shaped in $\lambda$ for $\lambda \leq \gamma / 2$, and decreasing in $\lambda$ when $\lambda$ is between $\gamma / 2$ and $\gamma$. To understand the forces leading to the U-shaped effect of $\lambda$ in the lower region, note first that an increase in $\lambda$ shifts probability mass from the $L L$ dyad to the $L H$ dyad and from the $L H$ dyad to the $H H$ dyad (the overall effect on the likelihood of the $L H$ dyad is that it increases in $\lambda$ if and only if $\lambda<1$ ). Because $1=p_{L} \geq p_{M}>p_{H}$, these shifts make the probability of peace initially decrease in $\lambda$. However, $p_{M}$ strictly increases in $\lambda$ for $\lambda \leq \gamma / 2$, and eventually this makes the probability of peace increase in $\lambda$. Interestingly, despite the fact that $p_{H}$ strictly increases in $\lambda$, for $\lambda>\gamma / 2$, it still does not grow fast enough to compensate for the shift in probability mass towards the dyads with the higher probability of war. As a result, the probability of peace decreases in $\lambda$ when $\lambda$ is between $\gamma / 2$ and $\gamma$.


Figure 1: Probability of peace in the separating equilibrium

Mixed-strategy Equilibria. This subsection considers mixed strategy equilibria. Mixing can help, though its role in the unmediated communication game is relatively lim-
ited (compare Figure 1 and right panel of Figure 2). The following result states that, while there is no mixed-strategy equilibrium in which the hawk randomizes between sending the high and low report, there exists a mixed-strategy equilibrium in which the dove randomizes. ${ }^{28}$ Furthermore, in some parameter region, depicted in the right panel of Figure 2, such a mixed strategy equilibrium yields a higher ex ante peace probability than the separating equilibrium. The specific definition of the region in which mixing improves upon the separating equilibrium is rather cumbersome, as is the explicit description of the mixed-strategy equilibrium, and so it is relegated to the Appendix. But it is interesting to note that mixing may improve only in a small subset of the parameter region in which both ex interim IC* constraints bind: mixing by the dove may relax the incentive of the hawk to hide strength. We summarize our findings as follows.

Proposition 2 Allowing for mixed strategies in the unmediated communication game, the best equilibrium is such that the hawk always sends message $h$ and the dove sends $l$ with probability strictly less than one.

The probability $\sigma<1$ with which the dove sends $l$ is reported in appendix, and shown in the right panel of Figure 2.


Figure 2: Welfare in the best (pure or mixed) equilibrium, and region where mixing occurs

[^11]
## 4 Mediation

In the previous section, we have characterized the optimal equilibrium in the case in which players send public messages. In this section, we consider mediated communication.

We modify the game form to account for such a mediator. In the first stage, messages are no longer public. They are separately reported to a mediator, who then proposes the split, possibly at random. More precisely, the version of the revelation principle proved in Myerson (1982) guarantees that the following game form entails no loss of generality:

- After being informed of her type, each player $i$ privately sends a report $m_{i} \in\{l, h\}$ to the mediator.
- Given reports $m=\left(m_{1}, m_{2}\right)$, the mediator recommends a split $(b, 1-b)$ according to some cumulative distribution function $F(b \mid m)$, where the only recommendation leading to war in the support of $F(\cdot \mid m)$ is $b=0 .{ }^{29}$ Unlike the reports, the mediator's recommendation is public.
- The contestants play the agreement game with the recommended split $b$.

Again by the revelation principle, we may restrict attention to distributions $F$ such that truthful type revelation and obedience to the mediator's recommendation are part of the equilibrium. As before, this imposes both ex interim incentive compatibility constraints and ex post individual rationality constraints, which we now describe. To simplify notation, we restrict attention to mechanisms that are symmetric across players, where $F\left(\cdot \mid m_{1}, m_{2}\right)=$ $1-F\left(\cdot \mid m_{2}, m_{1}\right)$ for all $\left(m_{1}, m_{2}\right)$, and to discrete distributions $F$. We shall later see that these restrictions entail no loss of generality.

Let $\operatorname{Pr}\left[m_{-i}, b, m_{i}\right]$ denote the equilibrium joint probability that the players send messages $\left(m_{i}, m_{-i}\right)$ and that the mediator offers $(b, 1-b)$, and set $\operatorname{Pr}\left[b, m_{i}\right] \equiv \operatorname{Pr}\left[h, b, m_{i}\right]+$

[^12]$\operatorname{Pr}\left[l, b, m_{i}\right]$. When player $i$ is a hawk, she reports $m_{i}=h$ in equilibrium, and ex post individual rationality requires that
\[

$$
\begin{equation*}
b \operatorname{Pr}[b, h] \geq \operatorname{Pr}[l, b, h] p \theta+\operatorname{Pr}[h, b, h] \theta / 2, \text { for all } b \in(0,1), \tag{1}
\end{equation*}
$$

\]

which ensures that, if recommended the peaceful split $b$, i.e., for all $b \in(0,1)$ such that $\operatorname{Pr}[b, h]>0$, the hawk prefers accepting the split to starting a war. Similarly, when $i$ is a dove, ex post individual rationality dictates that

$$
\begin{equation*}
b \operatorname{Pr}[b, l] \geq \operatorname{Pr}[h, b, l](1-p) \theta+\operatorname{Pr}[l, b, l] \theta / 2, \text { for all } b \in(0,1) \tag{2}
\end{equation*}
$$

Ex interim incentive compatibility requires that, when player $i$ is a hawk, she truthfully reports $m_{i}=h$. The associated constraint $\left(I C_{H}^{*}\right)$ dictates that

$$
\begin{align*}
& q F(0 \mid h h) \theta / 2+(1-q) F(0 \mid h l) p \theta+\int_{0}^{1} b d F(b \mid h) \geq q F(0 \mid l h) \theta / 2+ \\
& (1-q) F(0 \mid l l) p \theta+\int_{0}^{1} \max \{b, \operatorname{Pr}[l \mid b, l] p \theta+\operatorname{Pr}[h \mid b, l] \theta / 2\} d F(b \mid l) \tag{3}
\end{align*}
$$

where $\operatorname{Pr}\left[m_{-i} \mid b, m_{i}\right]=\operatorname{Pr}\left[m_{-i}, b, m_{i}\right] / \operatorname{Pr}\left[b, m_{i}\right]$ whenever $\operatorname{Pr}\left[b, m_{i}\right]>0$, and $F\left(\cdot \mid m_{i}\right) \equiv$ $q F\left(\cdot \mid m_{i}, h\right)+(1-q) F\left(\cdot \mid m_{i}, l\right)$, for $m_{i}$ and $m_{-i}$ taking values $l$ and $h$. Note that, as in the optimal separating equilibrium program, player $i$ might behave opportunistically after deviating, as reflected by the maxima on the right-hand side.

Similarly, to ensure truth-telling by player $i$ when a dove, the following constraint ( $I C_{L}^{*}$ ) must be satisfied:

$$
\begin{align*}
& q F(0 \mid l h)(1-p) \theta+(1-q) F(0 \mid l l) \theta / 2+\int_{0}^{1}(1-b) d F(b \mid l) \geq q F(0 \mid h h)(1-p) \theta+ \\
& (1-q) F(0 \mid l h) \theta / 2+\int_{0}^{1} \max \{1-b, \operatorname{Pr}[l \mid b, h] \theta / 2+\operatorname{Pr}[h \mid b, h](1-p) \theta\} d F(b \mid h) \tag{4}
\end{align*}
$$

In the best equilibrium, the mediator seeks to minimize the probability of war, i.e.,

$$
(1-q)^{2} F(0 \mid h h)+2 q(1-q) F(0 \mid l h)+q^{2} F(0 \mid l l) .
$$

Because recommendations need to be self-enforcing, there is a priori no reason to restrict the mediator in the number of splits to which he assigns positive probability. In fact, recommendations convey information about the most likely opponents' revealed types, and it might be in the mediator's best interest to scramble such information by means of multiple recommendations. Nevertheless, Proposition 3 below shows that relatively simple mechanisms reach the maximal probability of peace among all possible mechanisms, including asymmetric ones. These simple mechanisms can be described as follows. Given reports $(h, h)$, the mediator recommends the peaceful split $(1 / 2,1 / 2)$ with probability $q_{H}$, and war with probability $1-q_{H}$. Given reports $(h, l)$, the mediator recommends the peaceful split $(1 / 2,1 / 2)$ with probability $q_{M}$, the split $(b, 1-b)$ with probability $p_{M}$, and war with probability $1-p_{M}-q_{M}$, for some $b \geq 1 / 2$. Given reports $(l, l)$, the mediator recommends the peaceful split $(1 / 2,1 / 2)$ with probability $q_{L}$, the splits $(b, 1-b)$ and $(1-b, b)$ with probability $p_{L}$ each, and war with probability $1-2 p_{L}-q_{L}$.

Again, we relegate the explicit formulas of the solution to the Appendix, and restrict ourselves here to the description of its main features.

Proposition 3 A solution to the mediator's problem is such that, for all $\lambda<\gamma$ :

- Doves do not fight: $q_{L}+2 p_{L}=1$.
- The low-type incentive compatibility constraint $I C_{L}^{*}$ binds, whereas the high-type incentive compatibility constraint $I C_{H}^{*}$ does not, and $b=p \theta$.
- For $\gamma \geq 1$ and $\lambda>\gamma / 2$, hawk dyads fight with positive probability, $q_{H} \in(0,1)$, mixed dyads do not fight ( $p_{M}+2 q_{M}=1$ ), and mediation strictly improves upon cheap talk.
- For $\gamma \geq 1$ and $\lambda \leq \gamma / 2$, the solution exactly reproduces the separating equilibrium of the cheap talk game (specifically, $q_{L}=1, q_{M}=0, p_{M} \in(0,1)$ and $q_{H}=0$ ), and mediation yields the same welfare as cheap talk.
- For $\gamma<1$, the probability $p_{L}$ of unequal splits among dove dyads is bounded above zero, and mediation strictly improves upon cheap talk.

We now comment on the solution and we make some comparisons with the optimal separating equilibrium characterized in Proposition 1.

Suppose that $\gamma>1$. If $\lambda>\gamma / 2$, then $q_{M}>0$ : the mediator sometimes recommends the equal split $(1 / 2,1 / 2)$ when one player reports to be a hawk, and the other claims to be a dove. In this way, the ex post IR constraint of the high type who is recommended the equal split becomes binding. We remark that this ex post constraint was slack in the unmediated equilibrium. By making a slack constraint binding, the mediator increases the probability of peace. Indeed, the mediator lowers the gain from pretending to be a hawk, by making exaggerating strength less profitable against doves. When $\lambda \leq \gamma / 2$ instead, $q_{H}=q_{M}=0$ and the mediator does not improve upon unmediated communication. In this case, in fact, in both the mediated and the best (unmediated) separating equilibrium, war needs to occur with probability one in dyads of hawks, to avoid that doves misreport their type. But then the above-mentioned slack constraint is not relevant for either program, and the mediator cannot improve upon unmediated communication.

In contrast with the case of $\gamma \geq 1$, the mediator always yields a strict welfare improvement when $\gamma<1$. When $\lambda>1 /(1+\gamma)$, so that $b=p \theta$ in the perfectly separating equilibrium, it is also the case that $\lambda>\gamma / 2$ (note that $1 /(1+\gamma)>\gamma / 2)$, and hence the mediator helps for the same reasons as when $\gamma \geq 1$. When $\lambda<1 /(1+\gamma)$, the mediator makes sure that the $I C_{H}^{*}$ constraint is satisfied with $b=p \theta$. In fact, the mediator offers $(b, 1-b)$ with positive probability when both players report to be doves. A hawk who is hiding strength, and who is offered $1-b$ believes that the opponent is most likely a hawk, and does not wage war. This reduces the incentive to hide strength in order to wage war
if revealed that the opponent is weak, that we observed in the unmediated equilibrium. Hence, the expected payoff of hiding strength is lower, and the $I C_{H}^{*}$ constraint is satisfied with $b=p \theta$. Note that the ex post individual rationality constraint $b \geq p \theta$ was slack in the unmediated equilibrium. By making this rationality constraint binding, the mediator can improve the objective function, i.e. increase the probability of peace.

We can now precisely answer the first set of questions presented in the introduction:

- When does mediation improve on unmediated communication?
- When the intensity and/or cost of conflict is high (low $\gamma$ ), mediation strictly improves the peace chance with respect to unmediated cheap-talk.
- When conflict is not expected to be very costly or intense (high $\gamma$ ), mediation strictly improves the peace chance if and only if the proportion of hawks is intermediate, i.e., for high expected power asymmetry.
- How does mediation improve on unmediated communication?
- When the proportion of hawks is intermediate (high expected power asymmetry), the mediator lowers the reward for a dove from mimicking a hawk, by not always giving the lion's share to a declared hawk facing a dove (or, equivalently by not always revealing to a self-reported hawk that she is facing a dove). This lowers the incentive to exaggerate strength and achieves a favorable peace settlement with a dove.
- Instead, when the probability of facing a hawk is low and conflict is expected to be costly, the mediator's strategy is to offer with some probability unequal split to two parties reporting low type (or, equivalently the mediator does not always reveal to a dove that she is facing a dove). This lowers the incentive to hide strength and seek peace with a hawk.

Figure 3 shows the probability of peace in the mediated game compared to the probability of peace induced by the best separating equilibrium. We note one sharp difference between mediated and unmediated communication: the ex ante probability of peace is decreasing in $\lambda$, for $\lambda \in[\gamma / 2, \gamma)$, without mediation, whereas in the same range the ex ante probability of peace is increasing in $\lambda$ with mediation. This difference could have an important impact on an important debate in international relations, namely the debate on "deterrence:" the higher is $\lambda$ (or $q$ ), the more "deterred" a country should be from initiating a war, due to a higher likelihood of facing a hawk. Hence, a possible interpretation of this difference is that an international system with a level of deterrence higher than another is "good" for peace if every bilateral crisis is dealt with using mediators, whereas it is "bad" if direct communication is the most common way in which countries try to avoid wars.


Figure 3: Probability of peace in the mediated vs. unmediated case, and region where mediation dominates

We conclude by briefly discussing the comparison between mediation and the best completely mixed-strategy equilibrium. It should not be surprising to the reader familiar with the literature on correlated equilibrium (see, e.g. Aumann, 1974) that mediation strictly improves the chance of peace. By randomizing over recommendations, the mediator can
reproduce any distribution induced by mixing. In unmediated communication, however, because players must mix independently of each other, they cannot generate the optimal correlated distribution chosen by the mediator. The mixing by the dove may improve welfare upon the pure-strategy equilibrium, but at the cost of inducing war with positive probability within dove dyads. This does not occur with a mediator, who induces war only when at least one of the players is a hawk.

## 5 The Role of Enforcement

Even though the cause of war is asymmetric information, the analysis of the optimal mediation problem involves a significant enforcement problem. Countries are sovereign, and enforcement of contracts or agreements is often impossible. Because war can be started unilaterally, we have incorporated ex post IR and ex interim IC* constraints in the formulation of the optimal mediation program. In our model, the residual ex ante chance of war that results in the optimal mediation solution, can be thought as being due to a combination of asymmetric information and enforcement problems.

So far, mediation has reduced to optimal information elicitation from, and transmission to, the conflicting parties. One might also wonder whether the mediator could further reduce the ex ante probability of war if she were an arbitrator, i.e. if she were endowed with the power of enforcing agreements. For this, it is enough to compare our findings with those of Bester and Wärneryd (2006). Rather than imposing ex post IR constraints and ex interim IC* constraints in our basic game of conflict, they study the same set up with ex interim IR and IC constraints. Conflicting parties must be willing to participate in the arbitration process, and to reveal their information to the arbitrator. But the arbitrator's recommendations are enforceable by external actors, such as the international community. Hence, they abstract away from enforcement, and their model is suitable to describe arbitration.

Formally, invoking the version of the revelation principle proved by Myerson (1979), the Bester-Wärneryd problem can be summarized as follows. The parties truthfully report their types $L, H$ to the arbitrator. The arbitrator recommends peaceful settlement with probability $p(m)$ after report $m$. Because recommendations are enforced by an external agency, they can restrict attention to a single peaceful recommendation $x(m)$, for each report pair $m .{ }^{30}$ Symmetry is without loss of generality because the arbitrator's program is linear, and entails that the settlement is $(1 / 2,1 / 2)$ if the players report the same type, that the split is $(b, 1-b)$ if the reports are $(h, l)$, and $(1-b, b)$ if they are $(l, h)$, for some $b \in[1 / 2,1]$. Let $p_{L}=p(l, l), p_{M}=p(l, h)=p(h, l)$ and $p_{H}=p(h, h)$. The arbitrator chooses $b, p_{L}, p_{M}$ and $p_{H}$ so as to solve the program

$$
\min _{b, p_{L}, p_{M}, p_{H}}(1-q)^{2}\left(1-p_{L}\right)+2 q(1-q)\left(1-p_{M}\right)+q^{2}\left(1-p_{H}\right)
$$

subject to ex interim individual rationality (for the hawk and dove, respectively)

$$
\begin{aligned}
& (1-q)\left(p_{M} b+\left(1-p_{M}\right) p \theta\right)+q\left(p_{H} / 2+\left(1-p_{H}\right) \theta / 2\right) \geq(1-q) p \theta+q \theta / 2 \\
& (1-q)\left(p_{L} / 2+\left(1-p_{L}\right) \theta / 2\right)+q\left(p_{M}(1-b)+\left(1-p_{M}\right)(1-p) \theta\right) \geq(1-q) \theta / 2+q(1-p) \theta
\end{aligned}
$$

and to the ex interim incentive compatibility constraints (for the hawk and dove, respectively)

$$
\begin{aligned}
& (1-q)\left(\left(1-p_{M}\right) p \theta+p_{M} b\right)+q\left(\left(1-p_{H}\right) \theta / 2+p_{H} / 2\right) \geq \\
& (1-q)\left(\left(1-p_{L}\right) p \theta+p_{L} / 2\right)+q\left(\left(1-p_{M}\right) \theta / 2+p_{M}(1-b)\right)
\end{aligned}
$$

[^13]\[

$$
\begin{aligned}
& (1-q)\left(\left(1-p_{L}\right) \theta / 2+p_{L} / 2\right)+q\left(\left(1-p_{M}\right)(1-p) \theta+p_{M}(1-b)\right) \geq \\
& (1-q)\left(\left(1-p_{M}\right) \theta / 2+p_{M} b\right)+q\left(\left(1-p_{H}\right)(1-p) \theta+p_{H} / 2\right)
\end{aligned}
$$
\]

In general, the solution of the program with an arbitrator (with enforcement power) provides an upper bound to the solution of the program with a mediator (without enforcement power), as described in Section 4. Surprisingly, the solution of the latter program yields the same welfare as the solution of the former program. ${ }^{31}$ Specifically, for $\lambda \leq \gamma / 2$, the mechanisms with and without enforcement coincide. When $\lambda>\gamma / 2$, the simplest optimal mechanism with enforcement is such that $b<p \theta$, which is not self-enforcing. But the optimal mechanism without enforcement obfuscates the players' reports, and this obfuscation succeeds in fully circumventing the enforcement problem.

Proposition 4 An arbitrator who can enforce recommendation is exactly as effective in promoting peace as a mediator who can only propose self-enforcing agreements.

The intuition is as follows. First, note that the dove's IC constraint and hawk's ex interim IR constraint are the only ones binding in the solution of the mediator's program with enforcement power. Conversely, the only binding constraints in the mediator's program with self-enforcing recommendations are the dove's IC* constraint and the two ex post hawk's IR constraints. Recall that, in our solution, the hawk is always indifferent between war and peace if recommended a settlement. Further, the dove's IC* constraint in the mediator's problem with self-enforcing recommendations is identical to the dove's IC constraint in the arbitrator's program, because a dove never wages war after exaggerating strength in the solution of mediator's problem with self-enforcing recommendation.

Further, the hawk's ex interim IR constraint integrates the two binding hawk's ex post IR constraints in the arbitrator's problem. While requiring a constraint to hold in

[^14]expectation is generally a weaker requirement than having the two constraints, it turns out that the induced welfare is the same. This is easiest to see when $\lambda \leq \gamma / 2$, as in this case the only settlement ever granted to a hawk is $b$, when the opponent is dove. For any mechanism with this property, the ex interim IR and the ex post IR constraints trivially coincide. Let us now consider the case $\lambda>\gamma / 2$. In this case, the optimal truthful arbitration mechanism prescribes a settlement $b<p \theta$ that is not ex post IR for a hawk meeting a dove, as well as prescribing a settlement with slack, equal to $1 / 2$, to same type dyads. The mediator cannot reproduce this mechanism. But it circumvents the problem with the obfuscation strategy whereby the hawk is made exactly indifferent between war and peace when recommended either the split $1 / 2$ or the split $b=p \theta$. Hence, it optimally rebalances the ex post IR constraints so as to achieve the same welfare as the arbitrator.

We can now answer the last question that we posed in the introduction.

- How do mediation and arbitration differ in terms of conflict resolution?
- In our game, there is no difference in terms of optimal ex ante probability of peace between the two institutions.
- Either the two optimal mechanism coincide, for $\lambda$ low relative to $\gamma$, or the mediator's optimal obfuscation strategy circumvents her lack of enforcement power.

As striking as the results in this section might sound, we do not want to rule out the possibility that they rely on our discrete type space assumption. It would be interesting to examine when it extends to richer environments ${ }^{32}$

## 6 Concluding Remarks

By applying mechanism design techniques to the study of international conflict resolution, this paper derives a number of lessons on mediation, arbitration and unmediated

[^15]communication. First, we have determined when mediation improves upon unmediated communication. This is the case when the intensity of conflict and/or cost of war is high (low $\theta$ ); when power asymmetry has little impact on the probability of winning; and even when neither $\theta$ nor $p$ is low, mediation can still be strictly better than direct communication when the ex ante chance of power asymmetry is high (intermediate q). Second, we have characterized how mediation improves upon unmediated communication. In intuitive terms, this is achieved by not reporting to a player with probability one that her opponent is weak. In particular, when the ex ante chance of power asymmetry is high, the mediator lowers the reward from mimicking a hawk by not always giving the lion's share to a hawk facing a dove. When the expected intensity or cost of conflict are high, regardless of the expected degree of uncertainty, the mediator reduces the temptation to hide strength by a strong player. The mediator's strategy is to lower the reward from mimicking a dove by giving sometimes an unequal split to two parties reporting being a low type. Third, we have shown that the value of deterrence may depend on the conflict resolution institution. For intermediate probability that the players are strong, the probability of peace increases in the level of militarization when crises are mediated, whereas it decreases when peace talk are unmediated. Finally, we have shown that an arbitrator who can enforce outcomes is exactly as effective as a mediator who can only propose self-enforcing agreements.

We conclude the paper by discussing a few matters that arise from our analysis.
First, we address the question of whether disputants would consent to the involvement of a mediator in the peace talks. Specifically, suppose that we augment our mediation game to include a stage in which, immediately after being informed of their types, the contestants simultaneously and independently choose whether to accept the mediator or resort to unmediated cheap talk. Further assume that mediation will take place if and only if both players agree. It can be shown that this game admits both equilibria in which mediation always takes place and ones in which it never occurs (details available upon
request). Hence, the optimal equilibrium of this game is, again, the one with mediation. ${ }^{33}$
Second, we note that, while we have required recommendations to be self-enforcing, they need not be renegotiation-proof, as they might be Pareto-dominated for the players. For instance, when there is common belief that both players are hawks, they would be better off settling for an equal split rather than going to war, although doing so is part of the solution. Yet renegotiation-proofness does not seem to be a first and foremost concern of real world mediators. It is not overly realistic to think that, after the mediator quits, contestants who struggled to find an agreement in the presence of the mediator, will autonomously sit down at the negotiation table again, in search for a Pareto improving agreement. Indeed, while the literature on the causes of conflict underlines that contestants may not be able to individually commit to peaceful conflict resolutions, it may well be the case that they can jointly or even individually commit to belligerent resolutions, when such commitments are ex ante valuable. Audience costs, for instance, are recognized to provide an important channel that makes war threats credible (see, for instance, Tomz, 2007).

Finally, we revisit the issue of commitment by the mediator. Our analysis suggests that the mediator's success relies on her commitment to quit in some circumstances, rather than seeking a peaceful agreement in all contingencies. As stressed by Watkins (1998), this may be achieved by means of so-called action-forcing events. Further, before starting the mediation process, mediators often make clear to the disputants under which circumstances they will quit. Such contingent plan of actions often include deadlines. According to Avi Gil, one of the key architects of the Oslo peace process, "A deadline is a great but risky tool. Great because without a deadline it's difficult to end negotiations. [The parties] tend to play more and more, because they have time. Risky because if you do not meet the deadline, either the process breaks down, or deadlines lose their meaning" (Watkins, 1998). Among the many cases in which this technique was used, see for instance Curran and Sebenius

[^16](2003)'s account of how a deadline was employed by former Senator George Mitchell in the Northern Ireland negotiations. Committing to such deadlines might be somewhat easier for professional mediators whose reputation is at stake, but they have been also used both by unofficial and official individuals, including Pope John Paul II and former U.S. President Jimmy Carter. ${ }^{34}$ Meanwhile, institutions like the United Nations increasingly sets time limits to their involvement upfront (see, for instance, the U.N. General Assembly report, 2000).

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## Appendix A - Unmediated Communication

Proof of Proposition 1 All the statements in the proposition, but the comparison with no-communication, follow from the following characterization lemma:

Lemma 1 The best separating equilibrium is characterized as follows.

1. Suppose that $\gamma \leq 1$.
(a) When $\lambda<\gamma /(1+\gamma)$, both ex interim $I C^{*}$ constraints bind,

$$
b>p \theta, p_{H}=0, p_{M}=\frac{1}{(1+\gamma)(1-\lambda)}, \quad \text { and } V=\frac{1+\gamma+\lambda(1-\gamma)}{(1+\gamma)(1-\lambda)(1+\lambda)^{2}}
$$

(b) When $\lambda \in[\gamma /(1+\gamma), \min \{1 /(1+\gamma), \gamma\}]$, both $I C^{*}$ constraints bind,

$$
b>p \theta, p_{M}=1, \quad p_{H}=1-\frac{\gamma}{(1+\gamma) \lambda}, \quad \text { and } V=1-\frac{\gamma \lambda}{(1+\gamma)(1+\lambda)^{2}} .
$$

(c) When $\lambda \in[1 /(1+\gamma), \gamma)$, only the $I C_{L}^{*}$ constraint binds,

$$
b=p \theta, p_{M}=1, p_{H}=\frac{2 \lambda-\gamma}{\lambda(2+\gamma)}, \quad \text { and } V=\frac{2(1+\lambda)+\gamma}{2+\gamma+\lambda(2+\gamma)} .
$$

2. Suppose that $\gamma>1$.
(a) When $\lambda<\gamma / 2$, only the $I C_{L}^{*}$ constraint binds,

$$
b=p \theta, p_{H}=0, p_{M}=\frac{1}{1+\gamma-2 \lambda}, \text { and } V=\frac{1+\gamma}{(1+\gamma-2 \lambda)(1+\lambda)^{2}} .
$$

(b) When $\lambda \in[\gamma / 2, \gamma)$, only the $I C_{L}^{*}$ constraint binds,

$$
b=p \theta, p_{M}=1, p_{H}=\frac{2 \lambda-\gamma}{\lambda(\gamma+2)}, \text { and } V=1-\frac{\gamma \lambda}{(2+\gamma)(1+\lambda)} .
$$

The proof of lemma 1 proceeds in two parts.
Part $1(\gamma \geq 1)$.
We set up the following relaxed problem:

$$
\min _{b, p_{L}, p_{M}, p_{H}}(1-q)^{2}\left(1-p_{L}\right)+2 q(1-q)\left(1-p_{M}\right)+q^{2}\left(1-p_{H}\right)
$$

subject to the high-type ex post IR constraints:

$$
b \geq p \theta
$$

to the probability constraints:

$$
p_{L} \leq 1, p_{M} \leq 1,0 \leq p_{H}
$$

and ex ante low-type IC* constraint:

$$
\begin{aligned}
& (1-q)\left(\left(1-p_{L}\right) \frac{\theta}{2}+p_{L} \frac{1}{2}\right)+q\left(\left(1-p_{M}\right)(1-p) \theta+p_{M}(1-b)\right) \geq \\
& (1-q)\left(\left(1-p_{M}\right) \frac{\theta}{2}+p_{M} b\right)+q\left(\left(1-p_{H}\right)(1-p) \theta+p_{H} \frac{1}{2}\right)
\end{aligned}
$$

Step 1. We want to show that $p_{L}=1$. We first note that setting $p_{L}=1$ maximizes the LHS of the relaxed low-type IC* constraint and does not affect the RHS. It is immediate to see that the high-type ex post constraint is not affected either.

Step 2. We want to show that the relaxed low-type IC* constraint binds. Suppose it does not. It is possible to increase $p_{H}$ thus decreasing the objective function without violating the constraint (note that there is no constraint that $p_{H}<1$ in the relaxed problem).

Step 3. We want to show that the high-type ex post constraint binds. Suppose it does not. Then $b>p \theta$, and it is possible to reduce $b$ without violating the ex post constraint. But this makes the low-type relaxed IC* constraint slack, because $-b$ appears in the LHS and $b$ in the RHS. Because step 2 concluded that the low-type relaxed IC* constraint cannot be slack in the solution, we have proved that the ex post constraint cannot be slack.

Step 4. We want to show that for $\lambda \leq \gamma / 2: p_{H}=0, p_{M}=\frac{1}{1+\gamma-2 \lambda}$ in the relaxed program. The low-type relaxed IC* constraint and ex post constraint define the function

$$
\begin{equation*}
p_{M}=\frac{\left(1-\lambda p_{H}(\gamma+2)\right)}{(\gamma-2 \lambda+1)} \tag{5}
\end{equation*}
$$

substituting this function into the objective function

$$
W=2(1-q)\left(1-p_{M}\right)+q\left(1-p_{H}\right)
$$

duly simplified in light of step 1, we obtain the following expression:

$$
W=p_{H} \frac{(2 \lambda+\gamma+3) \lambda}{(\gamma-2 \lambda+1)(\lambda+1)}+\frac{2 \gamma-3 \lambda+\lambda \gamma-2 \lambda^{2}}{(\gamma-2 \lambda+1)(\lambda+1)}
$$

where we note that, because $\gamma \geq 2 \lambda$, the coefficient of $p_{H}$ is positive and the whole expression is positive. Hence, minimization of $W$ requires minimization $p_{H}$. Setting $p_{H}=0$ and solving for $p_{M}$ in (5) yields

$$
p_{M}=\frac{1}{1+\gamma-2 \lambda} .
$$

Because $\lambda \leq \gamma / 2$, it follows that $p_{M} \leq 1$, as required. We note that the probability of war equals:

$$
C=\frac{\left(2 \gamma-3 \lambda+\lambda \gamma-2 \lambda^{2}\right) \lambda}{(\gamma-2 \lambda+1)(\lambda+1)^{2}} .
$$

Step 5. We want to show that for $\lambda \geq \gamma / 2, p_{M}=1, p_{H}=\frac{2 \lambda-\gamma}{\lambda(\gamma+2)}$ in the relaxed problem. In light of the previous step, the solution $p_{H}=0$ yields $p_{M}>1$ and is not admissible when $\lambda>\gamma / 2$. Because $p_{M}$ decrease in $p_{H}$ in (5), the solution requires setting $p_{M}=1$ and, from (5), $p_{H}=\frac{2 \lambda-\gamma}{\lambda(\gamma+2)}$. When $\lambda \geq \gamma / 2, p_{H} \geq 0$ and hence the solution is admissible. We note that the probability of war equals:

$$
C=\frac{\gamma \lambda}{(\gamma+2)(\lambda+1)} .
$$

Step 6. We want to show that the solution constructed satisfies all the program constraints. The low-type ex post constraint $1-b \geq(1-p) \theta$ is trivially satisfied, when $b=p \theta$. Because $b>\theta / 2$ and $1 / 2>(1-p) \theta$, the low-type ex ante IC* constraint coincides with the low-type ex ante relaxed IC* constraint. The condition $1-b=1-p \theta \leq \theta / 2$ yields $2-2 p \theta \leq \theta$, i.e. $1-\theta \leq 2 p \theta-1$, i.e. $\gamma=\frac{2 p \theta-1}{1-\theta} \geq 1$. Hence, for $\gamma \geq 1$, we conclude that $1-b \leq \theta / 2$. So, after simplification, the ex ante high-type IC* constraint becomes:

$$
\begin{aligned}
& (1-q) p \theta+q\left(\left(1-p_{H}\right) \frac{\theta}{2}+p_{H} \frac{1}{2}\right) \\
= & (1-q)\left(\left(1-p_{M}\right) p \theta+p_{M} b\right)+q\left(\left(1-p_{H}\right) \frac{\theta}{2}+p_{H} \frac{1}{2}\right) \geq \\
& (1-q)\left(\left(1-p_{L}\right) p \theta+p_{L} p \theta\right)+q\left(\left(1-p_{M}\right) \frac{\theta}{2}+p_{M} \frac{\theta}{2}\right) \\
= & (1-q) p \theta+q \theta / 2,
\end{aligned}
$$

which is satisfied (with slack when $\lambda \geq \gamma / 2$ ). The probability constraints are obviously satisfied.

Part $2(\gamma<1)$. We allow for two cases:

Case 1. I will temporarily consider the following relaxed problem:

$$
\min _{b, p_{L}, p_{M}, p_{H}}(1-q)^{2}\left(1-p_{L}\right)+2 q(1-q)\left(1-p_{M}\right)+q^{2}\left(1-p_{H}\right)
$$

subject to the low-type and high-type relaxed IC* constraints:

$$
\begin{aligned}
& (1-q)\left(\left(1-p_{L}\right) \frac{\theta}{2}+p_{L} \frac{1}{2}\right)+q\left(\left(1-p_{M}\right)(1-p) \theta+p_{M}(1-b)\right) \geq \\
& (1-q)\left(\left(1-p_{M}\right) \frac{\theta}{2}+p_{M} b\right)+q\left(\left(1-p_{H}\right)(1-p) \theta+p_{H} \frac{1}{2}\right) \\
& (1-q)\left(\left(1-p_{M}\right) p \theta+p_{M} b\right)+q\left(\left(1-p_{H}\right) \frac{\theta}{2}+p_{H} \frac{1}{2}\right) \geq \\
& (1-q) p \theta+q\left(\left(1-p_{M}\right) \frac{\theta}{2}+p_{M}(1-b)\right) .
\end{aligned}
$$

which embed the assumption (to be verified ex post) that $1-b \geq \theta / 2$, and to the probability constraints:

$$
p_{L} \leq 1, p_{M} \leq 1,0 \leq p_{H}
$$

Step 1. As in the previous case, we conclude that $p_{L}=1$.
Step 2. We want to show that the low-type relaxed IC* constraint binds. Indeed, if it does not, we can increase $p_{H}$ without violating neither relaxed IC* constraints (note that the LHS of the high-type relaxed $\mathrm{IC}^{*}$ constraint increases in $p_{H}$ ).

Step 3. We want to show that the high-type relaxed $\mathrm{IC}^{*}$ constraint binds. Suppose not. We can then reduce $b$ because the LHS of the high-type relaxed IC* constraint increases in $b$ and the RHS decreases in $b$. This makes the low-type relaxed IC* constraint slack, without changing $p_{M}$ and $p_{H}$. But in light of step 2 , this cannot minimize the objective function. Hence, the high-type relaxed IC* constraint must bind.

Step 4. We want to show that for $\lambda<\gamma /(1+\gamma), p_{H}=0$ and $p_{M}=\frac{1}{(1+\gamma)(1-\lambda)}$ solve the relaxed problem. The binding relaxed ex ante IC* constraints define the function:
$\left[p_{M}, b\right]\left(p_{H}\right)$, after substituting $\lambda$ for $q$ and $\gamma$ for $p$, we obtain:

$$
\begin{align*}
b & =\frac{2 \lambda+\gamma-\theta \lambda-\theta \gamma-2 \lambda p_{H}+\theta \lambda p_{H}-3 \lambda \gamma p_{H}+2 \theta \lambda \gamma p_{H}-\lambda^{2} p_{H}-\lambda \gamma^{2} p_{H}-\lambda^{2} \gamma p_{H}+\theta \lambda \gamma^{2} p_{H}+1}{2\left(1-\lambda p_{H}-\lambda \gamma p_{H}\right)(\lambda+1)} \\
p_{M} & =\frac{\left(1-\lambda p_{H}(1+\gamma)\right)}{(\gamma+1)(1-\lambda)} . \tag{6}
\end{align*}
$$

Substituting $p_{M}$ into the objective function

$$
W=2(1-q)\left(1-p_{M}\right)+q\left(1-p_{H}\right)
$$

duly simplified in light of step 1 , we obtain:

$$
W=p_{H} \frac{\lambda}{1-\lambda}+\frac{2 \gamma-\lambda-\lambda \gamma-\lambda^{2}-\lambda^{2} \gamma}{(\gamma+1)(\lambda+1)(1-\lambda)}
$$

because the coefficient of $p_{H}$ is positive, this quantity is minimized by setting $p_{H}=0$. Then, solving for $p_{M}$ and $b$ when $p_{H}=0$ we obtain:

$$
\begin{aligned}
b & =-\frac{1}{2 \lambda+2}(-2 \lambda-\gamma+\theta \lambda+\theta \gamma-1) \\
p_{M} & =\frac{1}{(\gamma+1)(1-\lambda)}
\end{aligned}
$$

we know that $1 \geq \gamma \geq \lambda$, so $p_{M} \geq 0$, but the condition $p_{M} \leq 1$ yields $\frac{1}{(\gamma+1)(1-\lambda)}-1 \leq 0$, i.e. $\lambda \leq \frac{\gamma}{\gamma+1}$, as stated. We note that the probability of war equals:

$$
C=\frac{\left(\lambda-2 \gamma+\lambda \gamma+\lambda^{2}+\lambda^{2} \gamma\right) \lambda}{(\gamma+1)(\lambda+1)(\lambda-1)}
$$

Step 5. We want to show that for $\lambda<\gamma /(1+\gamma), p_{H}=0$ and $p_{M}=\frac{1}{(1+\gamma)(1-\lambda)}$ solve the original problem. Again, the low-type ex ante $\mathrm{IC}^{*}$ constraint coincides with the relaxed low-type ex ante $\mathrm{IC}^{*}$ constraint. We need to show that the ex post constraint $b \geq p \theta$ is satisfied. In fact, simplification yields:

$$
b-p \theta=\frac{1}{2}(\lambda+1)^{-1}(1-\gamma)(1-\theta) \lambda>0
$$

Finally we show that the high-type $\mathrm{IC}^{*}$ constraint coincides with the (binding) relaxed high-type IC* constraint, i.e. that $1-b \geq \theta / 2$. Note in fact, that this implies that the ex post constraint $1-b \geq(1-p) \theta$ is satisfied, because $\theta / 2>(1-p) \theta$. Indeed, after simplification, we obtain:

$$
1-b-\theta / 2=\frac{1}{2}(\lambda+1)^{-1}(1-\gamma)(1-\theta) \lambda \geq 0
$$

Step 6. We want to show that for $\lambda \in[\gamma /(1+\gamma), \min \{1 /(1+\gamma), \gamma\}], p_{M}=1, p_{H}=$ $1-\frac{\gamma}{(1+\gamma) \lambda}$ solves the relaxed problem. When $\lambda>\gamma /(1+\gamma)$, setting $p_{H}=0$ violates the constraint $p_{M}=1$. Further, the expression (6) reveals that $p_{M}$ decreases in $p_{H}$. Hence minimization of $p_{H}$, which induces minimization of $W$, requires setting $p_{M}=1$. Solving for $b$ and $p_{H}$, we obtain:

$$
\begin{aligned}
b & =-\frac{\left(-\lambda-3 \gamma+2 \theta \gamma-\lambda \gamma-\gamma^{2}+\theta \gamma^{2}-1\right)}{2 \lambda+2 \gamma+2 \lambda \gamma+2} \\
p_{H} & =\frac{\lambda-\gamma+\lambda \gamma}{(\gamma+1) \lambda}=1-\frac{\gamma}{(1+\gamma) \lambda} .
\end{aligned}
$$

The condition that $p_{H} \geq 0$ requires that $\lambda \geq \frac{\gamma}{\gamma+1}$ as stated.
Step 7. We want to show that for $\lambda \in[\gamma /(1+\gamma), \min \{1 /(1+\gamma), \gamma\}], p_{M}=1, p_{H}=$ $1-\frac{\gamma}{(1+\gamma) \lambda}$ solves the original problem. Again, the low-type ex ante $\mathrm{IC}^{*}$ constraint coincides with the relaxed low-type ex ante $\mathrm{IC}^{*}$ constraint. We need to show that the ex post constraint $b \geq p \theta$ is satisfied. In fact, simplification yields:

$$
b-p \theta=\frac{1}{2}(\gamma+1)^{-1}(\lambda+1)^{-1}(\lambda+\lambda \gamma-1)(\theta-1) \gamma
$$

and this quantity is positive if and only if $\lambda \leq \frac{1}{\gamma+1}$. Finally we show that the high-type $e x$ ante IC* constraint coincides with the (binding) relaxed high-type ex ante IC* constraint, i.e. that $1-b \geq \theta / 2$. Note in fact, that this implies that the ex post constraint $1-b \geq$ $(1-p) \theta$ is satisfied, because $\theta / 2>(1-p) \theta$. Indeed, after simplification, we obtain:

$$
1-b-\theta / 2=\frac{1}{2}(\gamma+1)^{-1}(\lambda+1)^{-1}(1-\theta)\left(\lambda-\gamma+\lambda \gamma-\gamma^{2}+1\right)
$$

and $\lambda-\gamma+\lambda \gamma-\gamma^{2}+1 \geq 0$ if and only if $\lambda \geq \frac{1}{\gamma+1}\left(\gamma+\gamma^{2}-1\right)$ but because $\frac{1}{\gamma+1}\left(\gamma+\gamma^{2}-1\right)<$ $\frac{\gamma}{\gamma+1}$, this condition is less stringent than $\lambda \geq \frac{\gamma}{\gamma+1}$.

Case 2. We want to show that for $\lambda \in[1 /(1+\gamma), \gamma), p_{M}=1, p_{H}=\frac{2 \lambda-\gamma}{\lambda(2+\gamma)}$ solve the original problem. Consider now the same relaxed problem that we considered in the proof for the case of $\gamma \geq 1$. We know from the analysis for the case $\gamma \geq 1$, that this relaxed problem is solved by $p_{H}=0, p_{M}=\frac{1}{1+\gamma-2 \lambda}, b=p \theta$ for $\lambda<\gamma / 2$ and by $p_{M}=1, p_{H}=$ $\frac{2 \lambda-\gamma}{\lambda(\gamma+2)}, b=p \theta$ for $\lambda \in[\gamma / 2, \gamma)$. We now note that

$$
\frac{1}{\gamma+1}-\gamma / 2=\frac{1}{2}(\gamma+1)^{-1}(1-\gamma)(\gamma+2)
$$

and this quantity is positive when $\gamma \leq 1$. Hence the possibility that $\lambda<\gamma / 2$ is ruled out: On the domain $1 /(1+\gamma) \leq \lambda \leq \gamma \leq 1$, the solution to the relaxed problem is $p_{M}=1, p_{H}=\frac{2 \lambda-\gamma}{\lambda(\gamma+2)}$, with $b=p \theta$. We now need to show that this is also the solution of the original problem. Again, the low-type ex ante IC* constraint coincides with the relaxed low-type ex ante IC* constraint. Consider the ex ante high-type IC* constraint. The condition $1-b=1-p \theta \geq \theta / 2$ yields $\gamma=\frac{2 p \theta-1}{1-\theta} \leq 1$. Hence, for $\gamma \leq 1$, we conclude that $1-b \geq \theta / 2$, and hence that $1-b \geq(1-p) \theta$. So the ex ante high-type $\mathrm{IC}^{*}$ constraint becomes:

$$
(1-q)\left(\left(1-p_{M}\right) p \theta+p_{M} p \theta\right)+q\left(\left(1-p_{H}\right) \frac{\theta}{2}+p_{H} \frac{1}{2}\right)-(1-q) p \theta-q\left(\left(1-p_{M}\right) \frac{\theta}{2}+p_{M}(1-p \theta)\right) \geq 0
$$

and indeed, after simplification, the LHS equals:

$$
\frac{1}{2}(\gamma+2)^{-1}(\lambda+1)^{-1}(\lambda+\lambda \gamma-1)(1-\theta) \gamma,
$$

a positive quantity as long as $\lambda+\lambda \gamma-1$, i.e., $\lambda>\frac{1}{\gamma+1}$, which is exactly the condition under which we operate.

This concludes the proof of the characterization lemma.
One can then verify by inspection that the above full characterization determines all the characteristics highlighted in Proposition 1, but the comparison with no communication, which we now determine.

For $\gamma>1, \lambda<\gamma / 2$ and $\lambda<\frac{\gamma-1}{2}$, the separating equilibrium optimal value $\frac{1+\gamma}{(1+\gamma-2 \lambda)(1+\lambda)^{2}}$ is evidently larger than the optimal no-communication value $\frac{1}{(1+\lambda)^{2}}$.

Suppose that $\gamma>1, \lambda<\gamma / 2$, and $\lambda>\frac{\gamma-1}{2}$. The separating equilibrium optimal value and the no-communication values are, respectively, $\frac{1+\gamma}{(1+\gamma-2 \lambda)(1+\lambda)^{2}}$ and $\frac{1}{\lambda+1}$. The difference is:

$$
\frac{1+\gamma}{(1+\gamma-2 \lambda)(1+\lambda)^{2}}-\frac{1}{\lambda+1}=\frac{(2 \lambda+1-\gamma) \lambda}{(\gamma-2 \lambda+1)(\lambda+1)^{2}},
$$

and this quantity is positive because $\lambda>\frac{\gamma-1}{2}$ and $\lambda<\gamma / 2$.
Suppose that $\gamma>1$ and $\lambda>\gamma / 2$, and $\lambda>\frac{\gamma-1}{2}$. The separating equilibrium optimal value is $1-\frac{\gamma \lambda}{(2+\gamma)(1+\lambda)}$. Taking the difference with the no-communication value,

$$
1-\frac{\gamma \lambda}{(2+\gamma)(1+\lambda)}-\frac{1}{\lambda+1}=2 \frac{\lambda}{(\gamma+2)(\lambda+1)}>0 .
$$

Suppose that $\gamma<1$ and $\lambda<\gamma /(1+\gamma)$. The separating equilibrium optimal value is $\frac{1+\gamma+\lambda(1-\gamma)}{(1+\gamma)(1-\lambda)(1+\lambda)^{2}}$. Hence,

$$
\frac{1+\gamma+\lambda(1-\gamma)}{(1+\gamma)(1-\lambda)(1+\lambda)^{2}}-\frac{1}{\lambda+1}=\frac{(\lambda-\gamma+\lambda \gamma+1) \lambda}{(\gamma+1)(\lambda+1)^{2}(1-\lambda)},
$$

because $\lambda<\gamma<1$, the above is positive if $\lambda-\gamma+\lambda \gamma+1>0$, i.e. $\lambda>\frac{\gamma-1}{\gamma+1}$ which always holds.

Suppose that $\gamma<1$ and $\lambda<\gamma /(1+\gamma)$. The separating equilibrium optimal value is $1-\frac{\gamma \lambda}{(1+\gamma)(1+\lambda)^{2}}$. Hence,

$$
1-\frac{\gamma \lambda}{(1+\gamma)(1+\lambda)^{2}}-\frac{1}{\lambda+1}=\frac{(\lambda+\lambda \gamma+1) \lambda}{(\gamma+1)(\lambda+1)^{2}}>0
$$

Suppose that $\gamma<1$ and $\lambda \in[1 /(1+\gamma), \gamma)$, so that the separating equilibrium optimal value is $\frac{2(1+\lambda)+\gamma}{2+\gamma+\lambda(2+\gamma)}$ and

$$
\frac{2(1+\lambda)+\gamma}{2+\gamma+\lambda(2+\gamma)}-\frac{1}{\lambda+1}=2(\gamma+2)^{-1}(\lambda+1)^{-1} \lambda>0 .
$$

This concludes the proof of Proposition 1.
Proof of Proposition 2. The Proposition follows from this Lemma.
Lemma 2 Allowing players to play mixed strategies in the unmediated communication game, the optimal equilibrium is such that the hawk always sends message $h$ and the dove sends message $l$ with probability $\sigma$, where $\sigma<1$ if and only if $\gamma<1$ and

$$
\begin{aligned}
\frac{\gamma}{1+\gamma}> & \lambda>\max \left\{\frac{-1-\gamma(5+6 \gamma)+\sqrt{(1+3 \gamma)(1+\gamma(11+8 \gamma(3+2 \gamma)))}}{2(1+\gamma)(1+3 \gamma)}\right. \\
& \left.\frac{-1-\gamma(8+3 \gamma)+\sqrt{1+\gamma(16+\gamma(54+\gamma(48+25 \gamma)))}}{2\left(\gamma^{2}-1\right)}\right\}
\end{aligned}
$$

For $\lambda<2 \gamma^{2} /(1+3 \gamma)$,

$$
\begin{gathered}
p_{M}=\frac{2 \gamma-\lambda+\gamma \lambda}{2(1+\gamma)(\gamma-\lambda)}, \quad p_{H}=0, \sigma=1+\frac{\lambda}{2}(1-1 / \gamma), b=(1+\gamma(1-\theta)) / 2 \\
\text { and } V=\frac{\lambda\left(\gamma^{2}(4+3 \lambda)-\lambda-2 \gamma \lambda(3+2 \lambda)\right)}{4 \gamma(\gamma-\lambda)(1+\lambda)^{2}} .
\end{gathered}
$$

For $\lambda>2 \gamma^{2} /(1+3 \gamma)$,

$$
p_{M}=1, p_{H}=0, b=p \theta, \sigma=\frac{(1+\gamma)(1+\lambda)}{(1+2 \gamma)}, \text { and } V=\frac{\gamma^{2}}{(1+2 \gamma)^{2}}
$$

We omit the proof of Lemma 2 as it is very involved, and the Lemma is only a secondary result in the paper. The proof is available upon request.

## Appendix B - Mediation

For reasons of clarity, the proof of Proposition 3 is postponed to after the proof of Proposition 4

Proof of Proposition 4. The proof follows from this Lemma.
Lemma 3 The solution of the mediator's program with enforcement power is such that: For $\lambda \leq \gamma / 2$,

$$
p_{M}=\frac{1}{\gamma-2 \lambda+1}, p_{H}=0, \text { and } V=\frac{(\gamma+1)}{(\gamma-2 \lambda+1)(\lambda+1)^{2}} \text {; }
$$

For $\lambda \geq \gamma / 2$,

$$
p_{M}=1, p_{H}=\frac{2 \lambda-\gamma}{(\gamma-\lambda+1) \lambda}, \text { and } V=\frac{\gamma+1}{(\gamma-\lambda+1)(\lambda+1)} .
$$

Proof. We first solve the following relaxed program:

$$
\min _{b, p_{L}, p_{M}, p_{H}}(1-q)^{2}\left(1-p_{L}\right)+2 q(1-q)\left(1-p_{M}\right)+q^{2}\left(1-p_{H}\right)
$$

subject to high-type ex interim individual rationality:

$$
(1-q)\left(p_{M} b+\left(1-p_{M}\right) p \theta\right)+q\left(p_{H} \frac{1}{2}+\left(1-p_{H}\right) \frac{\theta}{2}\right) \geq(1-q) p \theta+q \frac{\theta}{2},
$$

to low-type ex interim incentive compatibility:

$$
\begin{aligned}
& (1-q)\left(\left(1-p_{L}\right) \frac{\theta}{2}+p_{L} \frac{1}{2}\right)+q\left(\left(1-p_{M}\right)(1-p) \theta+p_{M}(1-b)\right) \geq \\
& (1-q)\left(\left(1-p_{M}\right) \frac{\theta}{2}+p_{M} b\right)+q\left(\left(1-p_{H}\right)(1-p) \theta+p_{H} \frac{1}{2}\right),
\end{aligned}
$$

and to

$$
p_{L} \leq 1, p_{M} \leq 1 \text { and } p_{H} \geq 0 .
$$

First, note that $p_{L}=1$ in the solution because $p_{L}$ appears in the constraints only in the right-hand side of the low-type ex interim incentive compatibility constraint, which is increasing in $p_{L}$. Second, note that the low-type ex interim incentive compatibility must be binding in the relaxed program's solution, or else one could increase $p_{H}$ thus reducing the value of the objective function, without violating the high-typeex interim individual rationality constraint. Third, note that the high-type ex interim individual rationality constraint must be binding in the relaxed program's solution, or else one could decrease $b$ and make the low-type ex interim incentive compatibility slack.

Solving for $b$ and $p_{H}$ as a function of $p_{M}$ in the system defined by the low-type ex interim incentive compatibility and high-type ex interim individual rationality constraints, and plugging back the resulting expressions in the objective function, we obtain

$$
C=-p_{M} \frac{\gamma+1}{(\lambda+1)(\gamma+1-\lambda)}+K
$$

where $K$ is an inconsequential constant. Hence, the probability of conflict is minimized by setting $p_{M}=1$ whenever possible. Substituting $p_{M}=1$, in the expression for $p_{H}$ earlier derived, we obtain $p_{H}=\frac{2 \lambda-\gamma}{(\gamma-\lambda+1) \lambda}$, which is strictly positive for $\lambda \geq \gamma / 2$ and always smaller than one.

Solving for $b$ and $p_{M}$ as a function of $p_{H}$ in the system defined by the low-type ex interim incentive compatibility and high-type ex interim individual rationality constraints, and plugging back the resulting expressions in the objective function, we obtain

$$
C=\frac{(\gamma+1) \lambda}{(\gamma-2 \lambda+1)(\lambda+1)} p_{H}+K,
$$

where $K$ is another inconsequential constant. The coefficient of $p_{H}$ is positive for $\lambda \leq \gamma / 2$, hence the probability of conflict is minimized by setting $p_{H}=0$, which entails $p_{M}=\frac{1}{\gamma-2 \lambda+1}$, a quantity positive and smaller than one when $\lambda \leq \gamma / 2$.

The proof of Lemma 3 and hence of Proposition 4 is concluded by showing that this solution does not violate the high-type ex interim incentive compatibility and low-type ex interim individual rationality constraints in the complete program.

Indeed, for $\lambda \geq \gamma / 2$, we verify that the slacks of these constraints are, respectively

$$
\begin{aligned}
& \frac{1}{2}(\gamma-\lambda+1)^{-1}(1-\theta)(\gamma-\lambda)(\gamma+1)>0 \\
& \quad \text { and } \frac{1}{2}(\gamma-\lambda+1)^{-1}(\gamma+1)(1-\theta)>0
\end{aligned}
$$

Similarly, for $\lambda \leq \gamma / 2$, the slacks are

$$
\begin{aligned}
& \frac{1}{2}(\gamma-2 \lambda+1)^{-1}(\lambda+1)^{-1}(1-\theta)(\gamma-\lambda)(\gamma+1)>0 \\
& \quad \text { and } \frac{1}{2}(\gamma+1-2 \lambda)^{-1}(\lambda+1)^{-1}(\gamma+1)(1-\theta)>0
\end{aligned}
$$

Proof of Proposition 3. The characterization follows from this Lemma.
Lemma $4 A$ solution to the mediator's problem is such that:

- For $\lambda \leq \gamma / 2$,

$$
q_{L}+2 p_{L}=1, q_{H}=q_{M}=0, b=p \theta, p_{M}=\frac{1}{1+\gamma-2 \lambda} .
$$

Further,

$$
p_{L} \leq \frac{2 \lambda}{(\gamma-2 \lambda+1)(\gamma-1)}, \text { if } \gamma \geq 1, p_{L} \geq \frac{(1-\gamma) \lambda}{2 \gamma^{2}} \frac{(\lambda-\gamma)(\gamma+2)}{(\lambda-\gamma-1)} \text { if } \gamma<1 \text {; }
$$

The ex ante peace probability is

$$
V=\frac{\gamma+1}{(1+\gamma-2 \lambda)(1+\lambda)^{2}}
$$

- For $\lambda \geq \gamma / 2$,

$$
q_{L}+2 p_{L}=1, p_{M}+q_{M}=1, b=p \theta, q_{H}=\frac{2 \lambda-\gamma}{\lambda(\gamma+1-\lambda)}, q_{M}=\frac{2 \lambda-\gamma}{\gamma(\gamma+1-\lambda)},
$$

and $q_{L} \geq \frac{\lambda(2 \lambda-\gamma)}{\gamma^{2}(\gamma-\lambda+1)}$. Further, for $\gamma \geq 1$,

$$
p_{L} \leq 2 \frac{(\gamma-\lambda)(\gamma+2) \lambda}{(\gamma-\lambda+1) \gamma(\gamma-1)} \text { if } \gamma \geq 1, p_{L} \geq \frac{(1-\gamma) \lambda}{2 \gamma^{2}} \frac{(\lambda-\gamma)(\gamma+2)}{(\lambda-\gamma-1)} \text { if } \gamma<1 \text {; }
$$

The ex ante peace probability is

$$
V=\frac{\gamma+1}{(\gamma-\lambda+1)(\lambda+1)}
$$

Proof. Consider the general mechanisms subject to the ex post IR and ex interim IC* constraints (1)-(4). It is straightforward to observe that the ex post IR constraints constraints are stronger than the following (high-type and low-type, respectively) ex interim IR constraints

$$
\begin{aligned}
& \int_{0}^{1} b d F(b \mid h) \geq \operatorname{Pr}[l, h] p \theta+\operatorname{Pr}[h, h] \theta / 2, \\
& \int_{0}^{1} b d F(b \mid l) \geq \operatorname{Pr}[h, l](1-p) \theta+\operatorname{Pr}[l, l] \theta / 2, \text { for all } b \in[0,1]
\end{aligned}
$$

and that the ex interim $\mathrm{IC}^{*}$ constraint are stronger than the ex interim IC constraint obtained by substituting the maxima with their first argument (the interim payoff induced by accepting peace recommendations later in the game).

By the revelation principle by Myerson (1979), the optimal ex ante probability of peace within the class of mechanisms which satisfy these ex interim IC and IR constraints cannot be larger than the ex ante probability of peace identified in Lemma 3 in Appendix D. Because the ex interim IC and IR constraints are weaker than the ex interim IC* and ex post IR constraints, it follows that any mechanism subject to the constraints (1)-(4) cannot yield a higher ex ante probability of peace than the one identified in Lemma 3.

Hence, to prove the result, it is enough to show that the formulas for the choice variables ( $b, p_{L}, q_{L}, p_{M}, q_{M}, q_{H}$ ) satisfy the constraints (1)-(4) and achieve the same ex ante probability of peace as in Lemma 3. Specialize to the mechanisms described by
(b, $\left.p_{L}, q_{L}, p_{M}, q_{M}, q_{H}\right)$, the ex post IR constraints take the following form, for the high type:

$$
b p_{M} \geq p_{M} p \theta, \quad\left(q q_{H}+(1-q) q_{M}\right) \cdot 1 / 2 \geq q q_{H} \theta / 2+(1-q) q_{M} p \theta
$$

and for the low type:

$$
\begin{aligned}
& p_{L} b \geq p_{L} \theta / 2, \quad\left(q p_{M}+(1-q) p_{L}\right)(1-b) \\
&\left(q q_{M}+(1-q) q_{L}\right) \cdot 1 / 2 \geq q p_{M}(1-p) \theta+(1-q) p_{L} \theta / 2 \\
&(1-p) \theta+(1-q) q_{L} \theta / 2
\end{aligned}
$$

whereas the high-type ex interim IC* constraint is

$$
\begin{aligned}
& q\left(q_{H} / 2+\left(1-q_{H}\right) \theta / 2\right)+(1-q)\left(p_{M} b+q_{M} / 2+\left(1-p_{M}-q_{M}\right) p \theta\right) \geq \\
& \max \left\{\left(q p_{M}+(1-q) p_{L}\right)(1-b), q p_{M} \theta / 2+(1-q) p_{L} p \theta\right\}+\max \left\{(1-q) p_{L} b,(1-q) p_{L} p \theta\right\} \\
& +\max \left\{\left(q q_{M}+(1-q) q_{L}\right) \cdot 1 / 2, q q_{M} \theta / 2+(1-q) q_{L} p \theta\right\} \\
& +q\left(1-p_{M}-q_{M}\right) \theta / 2+(1-q)\left(1-2 p_{L}-q_{L}\right) p \theta,
\end{aligned}
$$

and the low-type ex interim IC* constraint is

$$
\begin{aligned}
& q\left(p_{M}(1-b)+q_{M} / 2+\left(1-p_{M}-q_{M}\right)(1-p) \theta\right) \\
& +(1-q)\left(p_{L} b+p_{L}(1-b)+q_{L} / 2+\left(1-2 p_{L}-q_{L}\right) \frac{\theta}{2}\right) \geq \\
& \max \left\{(1-q) p_{M} b,(1-q) p_{M} \frac{\theta}{2}\right\}+\max \left\{\left(q q_{H}+(1-q) q_{M}\right) \cdot 1 / 2, q q_{H}(1-p) \theta+(1-q) q_{M} \frac{\theta}{2}\right\} \\
& +q\left(1-q_{H}\right)(1-p) \theta+q\left(1-p_{M}-q_{M}\right) \theta / 2
\end{aligned}
$$

It is straightforward to verify that the values provided in Lemma 4 are such that the $e x$ ante $\mathrm{IC}^{*}$ constraint in which the low type does not wage war after misreporting is binding. Also, plugging in our two sets of values for the choice variables gives the same welfare as in Proposition 3. We are left with showing that all other constraints are satisfied. We distinguish the two cases.

Step 1. Suppose that $\lambda<\gamma / 2$, so that $q_{M}=q_{H}=0$. After simplification, the low-type IC* constraint becomes

$$
\begin{aligned}
& q\left(p_{M}(1-p \theta)+\left(1-p_{M}\right)(1-p) \theta\right)+(1-q) \cdot 1 / 2 \geq \\
& (1-q) p_{M} p \theta+q(1-p) \theta+q\left(1-p_{M}\right) \theta / 2
\end{aligned}
$$

which is binding for $p_{M}=\frac{1}{1+\gamma-2 \lambda}$. Consider the high-type IC* constraint

$$
\begin{aligned}
& q \theta / 2+(1-q)\left(p_{M} b+\left(1-p_{M}\right) p \theta\right) \geq \max \left\{\left(q p_{M}+(1-q) p_{L}\right)(1-b), q p_{M} \theta / 2+(1-q) p_{L} p \theta\right\} \\
& +\max \left\{(1-q) p_{L} b,(1-q) p_{L} p \theta\right\}+\max \left\{(1-q) q_{L} \cdot 1 / 2,(1-q) q_{L} p \theta\right\}+q\left(1-p_{M}\right) \theta / 2,
\end{aligned}
$$

Note that

$$
\left(q p_{M}+(1-q) p_{L}\right)(1-b) \leq q p_{M} \theta / 2+(1-q) p_{L} p \theta
$$

as long as either $\gamma>1$ or $p_{L} \geq \frac{(1-\gamma) \lambda}{2 \gamma} p_{M}=\frac{(1-\gamma) \lambda}{2 \gamma^{2}} \frac{(\lambda-\gamma)(\gamma+2)}{(\lambda-\gamma-1)}$ for $\gamma<1$, that

$$
(1-q) p_{L} b=(1-q) p_{L} p \theta
$$

and that

$$
(1-q) q_{L} \cdot 1 / 2 \leq(1-q) q_{L} p \theta .
$$

Then we substitute in the high-type $\mathrm{IC}^{*}$ constraint (duly simplified):

$$
q \theta / 2+(1-q)\left(p_{M} b+\left(1-p_{M}\right) p \theta\right) \geq q \theta / 2+(1-q) p \theta
$$

which is clearly satisfied because $b=p \theta$.
Similarly, we find that the two high-type ex post constraints

$$
p_{M} b \geq p_{M} p \theta, \text { and }\left(q q_{H}+(1-q) q_{M}\right) \cdot 1 / 2 \geq q q_{H} \theta / 2+(1-q) q_{M} p \theta
$$

are satisfied - the second one because both sides equal zero.
We need to show that the low-type ex post constraints are satisfied. Indeed:

$$
p_{L} p \theta>p_{L} \theta / 2,(1-q) q_{L} \cdot 1 / 2>(1-q) q_{L} \theta / 2,
$$

whereas

$$
\left(q p_{M}+(1-q) p_{L}\right)(1-p \theta) \geq q p_{M}(1-p) \theta+(1-q) p_{L} \theta / 2
$$

as long as $p_{L}(\gamma-1)=p_{L} \frac{(\theta+2 p \theta-2)}{(1-\theta)} \leq 2 \frac{q}{(1-q)} p_{M}=2 \lambda p_{M}$. So that if $\gamma \geq 1, p_{L} \leq \frac{2 \lambda}{(\gamma-2 \lambda+1)(\gamma-1)}$ and if $\gamma<1, p_{L} \geq 0 \geq \frac{2 \lambda}{(\gamma-2 \lambda+1)(\gamma-1)}$.

Finally the probability constraints are satisfied. In fact, $0 \leq p_{M} \leq 1$ requires only that $1 \leq 1+\gamma-2 \lambda$, i.e., that $\lambda \leq \gamma / 2$.

Step 2. Suppose that $\lambda \geq \gamma / 2$. Consider the low-type constraint, first. After simplifying
maxima, as the low type always accepts the split if exaggerating strength, the low-type $\mathrm{IC}^{*}$ constraint is satisfied as an equality when plugging in the expressions $p_{M}+q_{M}=1, b=p \theta$, $q_{H}=\frac{2 \lambda-\gamma}{\lambda(\gamma+1-\lambda)}, q_{M}=\frac{2 \lambda-\gamma}{\gamma(\gamma+1-\lambda)}$.

Then we consider the high-type $\mathrm{IC}^{*}$ constraint. We proceed in two steps. We first determine the off-path behavior of the high type and show that

$$
\left(q p_{M}+(1-q) p_{L}\right) \cdot(1-b) \leq q p_{M} \theta / 2+(1-q) p_{L} p \theta
$$

as long as either $\gamma>1$ or $p_{L} \geq \frac{(1-\gamma) \lambda}{2 \gamma} p_{M}^{+}=\frac{(1-\gamma) \lambda}{2 \gamma^{2}} \frac{(\lambda-\gamma)(\gamma+2)}{(\lambda-\gamma-1)}$ for $\gamma<1$, that

$$
(1-q) p_{L} b=(1-q) p_{L} p \theta \quad \text { and that } \quad\left(q q_{M}+(1-q) q_{L}\right) 1 / 2 \leq q q_{M} \theta / 2+(1-q) q_{L} p \theta
$$

as long as $q_{L} \geq \frac{1-\theta}{2 p \theta-1} \frac{q}{1-q} q_{M}$, i.e. $q_{L} \geq \frac{\lambda}{\gamma} q_{M}=\frac{\lambda(2 \lambda-\gamma)}{\gamma^{2}(\gamma-\lambda+1)}$.
Then we verify that the consequentially simplified high-type $\mathrm{IC}^{*}$ constraint is satisfied with equality, when substituting in the expressions $p_{M}+q_{M}=1, b=p \theta, q_{H}=\frac{2 \lambda-\gamma}{\lambda(\gamma+1-\lambda)}$, $q_{M}=\frac{2 \lambda-\gamma}{\gamma(\gamma+1-\lambda)}$.

We then verify that the two high-type ex post constraints

$$
p_{M} b \geq p_{M} p \theta, \text { and }\left(q q_{H}+(1-q) q_{M}\right) \cdot 1 / 2 \geq q q_{H} \theta / 2+(1-q) q_{M} p \theta
$$

are satisfied with equality when substituting in the expressions for $b=p \theta, q_{H}=\frac{2 \lambda-\gamma}{\lambda(\gamma+1-\lambda)}$, $q_{M}=\frac{2 \lambda-\gamma}{\gamma(\gamma+1-\lambda)}$.

Finally, show that the low-type ex post constraints are satisfied. In fact

$$
\begin{aligned}
& p_{L} p \theta>p_{L} \theta / 2, \text { and }\left(q q_{M}+(1-q) q_{L}\right) \cdot 1 / 2>q q_{M}(1-p) \theta+(1-q) q_{L} \theta / 2, \\
& \left(q p_{M}+(1-q) p_{L}\right)(1-p \theta) \geq q p_{M}(1-p) \theta+(1-q) p_{L} \theta / 2
\end{aligned}
$$

as long as $p_{L}(\gamma-1)=p_{L} \frac{(\theta+2 p \theta-2)}{(1-\theta)} \leq 2 \frac{q}{(1-q)} p_{M}=2 \lambda p_{M}$. So that if $\gamma \geq 1, p_{L} \leq$ $2 \frac{(\gamma-\lambda)(\gamma+2) \lambda}{(\gamma-\lambda+1) \gamma(\gamma-1)}$ and if $\gamma<1, p_{L} \geq 0 \geq 2 \frac{(\gamma-\lambda)(\gamma+2) \lambda}{(\gamma-\lambda+1) \gamma(\gamma-1)}$.

Finally the probability constraints are satisfied. In fact, because $\gamma+1-\lambda>0,2 \lambda-$ $\gamma-\lambda(\gamma+1-\lambda)=(\lambda+1)(\lambda-\gamma)<0$, and $2 \lambda-\gamma-\gamma(\gamma+1-\lambda)=(\gamma+2)(\lambda-\gamma)$, the conditions $0 \leq q_{H} \leq 1$ and $0 \leq q_{M} \leq 1$ require only that $2 \lambda-\gamma \geq 0$.

Having proved that the claimed solution satisfies all constraints, the proof of Lemma 4, and hence Proposition 3 is now concluded.

## Mediation and Peace

Johannes Horner, Massimo Morelli, and Francesco Squintani

## MATERIAL NOT FOR PUBLICATION

Proof of Lemma 2. We proceed in three parts.
Part 1. (The low type mixes).
The choice variables are $b, \sigma, p_{L}, p_{M}$, and $p_{H}$. We have 19 constraints, i.e. one IC for the low type which is binding, four IC for the high type to get rid of the maximum in the constraint, two ex post constraints for high type, four ex post constraints for low type, and eight probability constraints. First we rearrange the IC constraint for low type and express $b$ in terms of the other variables. Substituting $b$ into objective function and constraints, we get rid of $b$ and IC constraint for low type. After simplifying the constraints, we are left with the following constraints, referred to as constraints $\mathrm{C} i, i=1, \ldots, 9$. (We omit the constraints that all probabilities must be in $[0,1]$.)

1. $I C H 1:(1+\gamma) p_{M}(1+\lambda-2 \sigma)-(1+\gamma) p H(1+\lambda-\sigma)+p_{L} \sigma$;
2. $I C H 2:-p H+p_{M}+\frac{\left(p H+p_{L}-2 p_{M}\right) \sigma}{1+\lambda}$;
3. ICH3: $(1+\lambda)(-\gamma+\lambda) p H+(-1+\gamma-2 \lambda) \sigma\left(p H-p_{M}\right)+\left(p H+p_{L}-2 p_{M}\right) \sigma^{2}$;
4. ICH4: $(1+\lambda)(-\gamma+\lambda) p_{H}+\left((-1+\gamma-2 \lambda) p_{H}+\gamma\left(p_{L}+\lambda p_{L}-p_{M}\right)+p_{M}+2 \lambda p_{M}\right) \sigma+$ $\left(p H+p_{L}-2 p_{M}\right) \sigma^{2} ;$
5. EXH1: $p_{M}+p_{L} \sigma+p H(-1-(2+\gamma) \lambda+\sigma)-p_{M}(\gamma-2 \lambda+2 \sigma)$;
6. EXH2 : $\lambda+\gamma(-1+\sigma)$;
7. $E X L 1: p H(1+\lambda-\sigma)(1+(2+\gamma) \lambda-\sigma)+\sigma\left(p_{M}(2+(3+\gamma) \lambda-2 \sigma)+p_{L}(-1-\lambda+\sigma)\right)$;
8. $E X L 3: p_{M}(2+(3+\gamma) \lambda-2 \sigma)+p_{L} \sigma+p H(-1-(2+\gamma) \lambda+\sigma)$;
9. $E X L 4: 1-\frac{(1+\gamma) \lambda}{-1-\lambda+\sigma}$.

- case 1: C5 binds

This section covers the case that only C 5 binds. We do not assume C 5 binds ex ante.

We set up the following relaxed problem:

$$
\min _{p_{L}, p_{M}, p_{H}, \sigma} 1-\left(\left(\frac{\sigma}{1+\lambda}\right)^{2} p_{L}+2 \frac{\sigma}{1+\lambda} \frac{1+\lambda-\sigma}{1+\lambda} p_{M}+\left(\frac{1+\lambda-\sigma}{1+\lambda}\right)^{2} p_{H}\right)
$$

subject to the following constraints:

1. $p_{L} \leq 1$,
2. $0 \leq p_{M} \leq 1$,
3. $p_{H} \geq 0$,
4. $0 \leq \sigma \leq 1$,
5. $C 5 \geq 0 \Leftrightarrow p_{L} \sigma \geq(1+(2+\gamma) \lambda-\sigma) p_{H}+(\gamma-2 \lambda+2 \sigma-1) p_{M}$.

- Case 1.1: Parameter Region is $1 / 2<\lambda \leq \frac{1}{2}(-1+\sqrt{5})$ and $\frac{1-\lambda}{\lambda}<\gamma<2 \lambda$, or $\lambda>\frac{1}{2}(-1+\sqrt{5})$ and $\lambda<\gamma<2 \lambda$.

1. We want to show that $p_{L}=1$. Suppose $p_{L}<1$. We can set $p_{L}=1$ and increase $p_{H}$ to make sure C 5 is satisfied. By doing so, no constraint will be violated and the objective function is strictly decreased.
2. We want to show that C5 binds. Suppose it does not. We can increase $p_{H}$ without violating other constraints and decrease the objective function.
3. Suppose $(\gamma-2 \lambda+2 \sigma-1)>0$. Then $\frac{M C p_{M}}{M C p_{H}}=\frac{2 \sigma+(\gamma-2 \lambda-1)}{1+\lambda-\sigma+(1+\gamma) \lambda}<\frac{2 \sigma}{1+\lambda-\sigma}=\frac{M U p_{M}}{M U p_{H}}$, since $(\gamma-2 \lambda-1)<0$ and $(1+\gamma) \lambda>0$. Therefore, we want $p_{M}$ to be as large as possible and $p_{H}$ to be as small as possible, i.e. $p_{M}=1$ or $p_{H}=0$. If $\sigma \leq \gamma-2 \lambda+2 \sigma-1, p_{H}=0$ and $p_{M}=\frac{\sigma}{\gamma-2 \lambda+2 \sigma-1}$. If $\sigma \geq \gamma-2 \lambda+2 \sigma-1, p_{M}=1$ and $p_{H}=\frac{1-\sigma+2 \lambda-\gamma}{1-\sigma+2 \lambda+\gamma \lambda}$.
4. Suppose $(\gamma-2 \lambda+2 \sigma-1) \leq 0$. We have $p_{L} \sigma+(-\gamma+2 \lambda-2 \sigma+1) p_{M} \geq$ $(1+(2+\gamma) \lambda-\gamma) p_{H}$. Then $p_{L}=1, p_{M}=1$ and $p_{H}=\frac{1-\sigma+2 \lambda-\gamma}{1-\sigma+2 \lambda+\gamma \lambda}$.
5. To sum up, we conclude that:
(a) If $0 \leq \sigma \leq 1+2 \lambda-\gamma$, then $p_{L}=1, p_{M}=1, p_{H}=\frac{1-\sigma+2 \lambda-\gamma}{1-\sigma+2 \lambda+\gamma \lambda}$, and $V=\frac{\gamma(1+\lambda-\sigma)^{2}}{(1+\lambda)(1+(2+\gamma) \lambda-\sigma)}$.
(b) If $1 \geq \sigma \geq 1+2 \lambda-\gamma$, then $p_{L}=1, p_{H}=0, p_{M}=\frac{\sigma}{\gamma-2 \lambda+2 \sigma-1}$, and $V=-\frac{(1+\lambda-\sigma)((-1+\gamma-2 \lambda)(1+\lambda)+(1+\gamma) \sigma)}{(1+\lambda)^{2}(1-\gamma+2 \lambda-2 \sigma)}$.
Under the parameter region we specify above, we know that $1+2 \lambda-\gamma \geq 1$. Since $\sigma \leq 1$, only case (a) is possible. And $V$ is minimized when $\sigma=1$.
6. The solution to the relaxed problem is $p_{L}=1, p_{M}=1, p_{H}=\frac{2 \lambda-\gamma}{2 \lambda+\gamma \lambda}, \sigma=1$, and $V=\frac{\gamma \lambda}{2+\gamma+2 \lambda+\gamma \lambda}$. Substituting these into the original problem, we can show that all the constraints are satisfied. Therefore, this is also the solution to the original problem.

- Case 1.2: Parameter Region is $0<\lambda \leq \frac{1}{2}$ and $\gamma>1$, or $\lambda>\frac{1}{2}$ and $\gamma>2 \lambda$.

1. We want to show that $p_{L}=1$. Suppose not. We can increase $p_{L}$ and $p_{H}$ and decrease the objective function without violating the other constraints.
2. It is easy to show that C5 binds. Suppose not. We can increase $p_{H}$ and decrease the objective function without violating the other constraints.
3. Suppose $(\gamma-2 \lambda+2 \sigma-1)>0$.

If $\frac{M C p_{M}}{M C p_{H}}=\frac{2 \sigma+(\gamma-2 \lambda-1)}{1+\lambda-\sigma+(1+\gamma) \lambda} \leq \frac{2 \sigma}{1+\lambda-\sigma}=\frac{M U p_{M}}{M U p_{H}}$, then we want $p_{M}$ to be as large as possible and $p_{H}$ to be as small as possible, i.e. $p_{M}=1$ or $p_{H}=0$. If $\sigma \leq \gamma-2 \lambda+2 \sigma-1, p_{H}=0$ and $p_{M}=\frac{\sigma}{\gamma-2 \lambda+2 \sigma-1}$. If $\sigma \geq \gamma-2 \lambda+2 \sigma-1$, $p_{M}=1$ and $p_{H}=\frac{1-\sigma+2 \lambda-\gamma}{1-\sigma+2 \lambda+\gamma \lambda}$.
If $\frac{M C p_{M}}{M C p_{H}}=\frac{2 \sigma+(\gamma-2 \lambda-1)}{1+\lambda-\sigma+(1+\gamma) \lambda}>\frac{2 \sigma}{1+\lambda-\sigma}=\frac{M U p_{M}}{M U p_{H}}$, we want $p_{M}$ to be as small as possible and $p_{H}$ to be as large as possible, i.e. $p_{M}=0$ and $p_{H}=\frac{\sigma}{1+(2+\gamma) \lambda-\sigma}$.
4. Suppose $(\gamma-2 \lambda+2 \sigma-1) \leq 0$. We have $p_{L} \sigma+(-\gamma+2 \lambda-2 \sigma+1) p_{M} \geq$ $(1+(2+\gamma) \lambda-\gamma) p_{H}$. Then $p_{L}=1, p_{M}=1$ and $p_{H}=\frac{1-\sigma+2 \lambda-\gamma}{1-\sigma+2 \lambda+\gamma \lambda}$.
5. To sum up, we conclude that:
(a) If $0 \leq \sigma \leq \frac{1+2 \lambda-\gamma}{2}$, we have $p_{L}=1, p_{M}=1, p_{H}=\frac{1-\sigma+2 \lambda-\gamma}{1-\sigma+2 \lambda+\gamma \lambda}$, and $V=\frac{\gamma(1+\lambda-\sigma)^{2}}{(1+\lambda)(1+(2+\gamma) \lambda-\sigma)}$.
(b) If $\frac{(-1+\gamma-2 \lambda)(1+\lambda)}{-1+\gamma+2 \gamma \lambda}>\sigma \geq \frac{1+2 \lambda-\gamma}{2}, p_{L}=1, p_{M}=0, p_{H}=\frac{\sigma}{1+(2+\gamma) \lambda-\sigma}$. And $V=\frac{(1+\lambda-\sigma)(1-\sigma+\lambda(3+2 \lambda+\gamma(1+\lambda+\sigma)))}{(1+\lambda)^{2}(1+(2+\gamma) \lambda-\sigma)}$.
(c) If $\max \left(\frac{1+2 \lambda-\gamma}{2}, \frac{(-1+\gamma-2 \lambda)(1+\lambda)}{-1+\gamma+2 \gamma \lambda}\right) \leq \sigma \leq 1+2 \lambda-\gamma$, then $p_{L}=1, p_{M}=1$, $p_{H}=\frac{1-\sigma+2 \lambda-\gamma}{1-\sigma+2 \lambda+\gamma \lambda}$, and $V=\frac{\gamma(1+\lambda-\sigma)^{2}}{(1+\lambda)(1+(2+\gamma) \lambda-\sigma)}$.
(d) If $\max \left(1+2 \lambda-\gamma, \frac{(-1+\gamma-2 \lambda)(1+\lambda)}{-1+\gamma+2 \gamma \lambda}\right) \leq \sigma \leq 1, p_{L}=1, p_{H}=0, p_{M}=$ $\frac{\sigma}{\gamma-2 \lambda+2 \sigma-1}$, and $V=-\frac{(1+\lambda-\sigma)((-1+\gamma-2 \lambda)(1+\lambda)+(1+\gamma) \sigma)}{(1+\lambda)^{2}(1-\gamma+2 \lambda-2 \sigma)}$.
6. Under the parameter region we specify above, all the cases specified above are possible. After comparing all the minimized values, we find that case (d) achieves the minimized $V$ when $\sigma=1$.
7. The solution to the relaxed problem is $p_{L}=1, p_{M}=\frac{1}{1+\gamma-2 \lambda}, p_{H}=0, \sigma=1$, and $V=\frac{\lambda(\gamma(2+\lambda)-\lambda(3+2 \lambda))}{(1+\gamma-2 \lambda)(1+\lambda)^{2}}$. Substituting these into the original problem, we can show that all the constraints are satisfied. Therefore, this is also the solution to the original problem.

- case 2: C1 binds

This section covers the case that C1 binds and C5 might bind. We do not assume C1 binds ex ante.

We set up the following relaxed problem:

$$
\min _{p_{L}, p_{M}, p_{H}, \sigma} 1-\left(\left(\frac{\sigma}{1+\lambda}\right)^{2} p_{L}+2 \frac{\sigma}{1+\lambda} \frac{1+\lambda-\sigma}{1+\lambda} p_{M}+\left(\frac{1+\lambda-\sigma}{1+\lambda}\right)^{2} p_{H}\right)
$$

subject to the following constraints:

1. $p_{L} \leq 1$,
2. $0 \leq p_{M} \leq 1$,
3. $p_{H} \geq 0$,
4. $0 \leq \sigma \leq 1$,
5. $C 1 \geq 0 \Leftrightarrow p_{L} \sigma \geq(1+\gamma)(1+\lambda-\sigma) p_{H}+(1+\gamma)(-1-\lambda+2 \sigma) p_{M}$.
6. $C 5 \geq 0 \Leftrightarrow p_{L} \sigma \geq(1+(2+\gamma) \lambda-\sigma) p_{H}+(\gamma-2 \lambda+2 \sigma-1) p_{M}$.

- Case 2.1:

Parameter Region is $0<\lambda \leq \frac{1}{2}$ and $\lambda<\gamma \leq \frac{\lambda}{1-\lambda}$, or $1 / 2<\lambda \leq \frac{1}{2}(-1+\sqrt{5})$ and $\lambda<\gamma<\frac{1-\lambda}{\lambda}$.

1. We want to show that $p_{L}=1$. Suppose not. We can increase $p_{L}$ and $p_{H}$ and decrease the objective function without violating other constraints.
2. It's easy to show that either C1 or C5 binds. Suppose both are not binding. We can increase $p_{H}$ without violating other constraints. Here, we first consider the case where C 1 binds.
3. Suppose $2 \sigma-\lambda-1 \geq 0$. Then $\frac{M C p_{M}}{M C p_{H}}=\frac{2 \sigma-\lambda-1}{1+\lambda-\sigma}<\frac{2 \sigma}{1+\lambda-\sigma}=\frac{M U p_{M}}{M U p_{H}}$. Therefore, $p_{M}=1$ or $p_{H}=0$. If $\sigma \geq(1+\gamma)(-1-\lambda+2 \sigma)$, we have $p_{M}=1$ and $p_{H}=\frac{\sigma+(1+\gamma)(1+\lambda-2 \sigma)}{(1+\gamma)(1+\lambda-\sigma)} \geq 0$. If $\sigma \leq(1+\gamma)(-1-\lambda+2 \sigma)$, we have $p_{H}=0$, $p_{M}=\frac{\sigma}{(1+\gamma)(-1-\lambda+2 \sigma)} \leq 1$.
4. Suppose $2 \sigma-\lambda-1<0$, we have $p_{L}=1, p_{M}=1$, and $p_{H}=\frac{\sigma+(1+\gamma)(1+\lambda-2 \sigma)}{(1+\gamma)(1+\lambda-\sigma)}$.
5. To sum up ,we can show that:
(a) If $0 \leq \sigma \leq \frac{(1+\gamma)(1+\lambda)}{1+2 \gamma}$, then $p_{L}=1, p_{M}=1$ and $p_{H}=\frac{\sigma+(1+\gamma)(1+\lambda-2 \sigma)}{(1+\gamma)(1+\lambda-\sigma)}$.
(b) If $1 \geq \sigma \geq \frac{(1+\gamma)(1+\lambda)}{1+2 \gamma}$, then $p_{L}=1, p_{H}=0$, and $p_{M}=\frac{\sigma}{(1+\gamma)(-1-\lambda+2 \sigma)}$.
6. Since in the parameter region specified above $\frac{(1+\gamma)(1+\lambda)}{1+2 \gamma} \geq 1$, we know that only case (a) is possible. Hence, $p_{L}=1, p_{M}=1, p_{H}=\frac{\sigma+(1+\gamma)(1+\lambda-2 \sigma)}{(1+\gamma)(1+\lambda-\sigma)}$, and $V=\frac{\gamma(1+\lambda-\sigma) \sigma}{(1+\gamma)(1+\lambda)^{2}}$. Notice that $V$ is a quadratic function of $\sigma$ which is maximized at $\sigma=\frac{1+\lambda}{2}$.
7. Substituting $p_{L}, p_{M}$, and $p_{L}$ into C5, we have the following constraint on $\sigma$ :

$$
\gamma\left(-1-2 \lambda+\frac{\lambda(1+\lambda)}{1+\lambda-\sigma}+\frac{\sigma}{1+\gamma}\right) \geq 0
$$

which is equivalent to

$$
\sigma_{1} \leq \sigma \leq \sigma_{2}
$$

where

$$
\begin{aligned}
\sigma_{1} & =\frac{1}{2}\left(2+\gamma+3 \lambda+2 \gamma \lambda-\sqrt{2 \gamma \lambda(3+4 \lambda)+\lambda(4+5 \lambda)+(\gamma+2 \gamma \lambda)^{2}}\right) \\
\sigma_{2} & =\frac{1}{2}\left(2+\gamma+3 \lambda+2 \gamma \lambda+\sqrt{2 \gamma \lambda(3+4 \lambda)+\lambda(4+5 \lambda)+(\gamma+2 \gamma \lambda)^{2}}\right) .
\end{aligned}
$$

Since $\frac{1+\lambda}{2}<\sigma_{1} \leq 1<\sigma_{2}$, we know that $V$ is minimized at $\sigma=1$.
8. Next we consider the case that C5 is binding. Using the same method, we get the minimized value which is larger than the $V$ specified above. Hence, the solution to the relaxed problem is $p_{L}=1, p_{M}=1, p_{H}=1-\frac{\gamma}{\lambda+\gamma \lambda}, \sigma=1$, and $V=\frac{\gamma \lambda}{(1+\gamma)(1+\lambda)^{2}}$. Substituting the solution to the original problem, we show that all the constraints are satisfied. Hence, this is also the solution to the original problem.

- Case 2.2: Parameter Region is $0<\lambda \leq \frac{1}{2}$ and $\frac{\lambda}{1-\lambda} \leq \gamma \leq 1$.

1. $p_{L}=1$. Suppose not. We can increase $p_{L}$ and $p_{H}$ without violating other constraints.
2. It is easy to show that either C1 or C5 binds. Suppose both are not binding. We can increase $p_{H}$ without violating other constraints. Here, we first consider the case where C1 binds.
3. Suppose $2 \sigma-\lambda-1 \geq 0, \frac{M C p_{M}}{M C p_{H}}=\frac{2 \sigma-\lambda-1}{1+\lambda-\sigma}<\frac{2 \sigma}{1+\lambda-\sigma}=\frac{M U p_{M}}{M U p_{H}}$. Therefore, $p_{M}=1$ or $p_{H}=0$. If $\sigma \geq(1+\gamma)(-1-\lambda+2 \sigma)$, we have $p_{M}=1$ and $p_{H}=\frac{\sigma+(1+\gamma)(1+\lambda-2 \sigma)}{(1+\gamma)(1+\lambda-\sigma)} \geq 0$. If $\sigma \leq(1+\gamma)(-1-\lambda+2 \sigma)$, we have $p_{H}=0$, $p_{M}=\frac{\sigma}{(1+\gamma)(-1-\lambda+2 \sigma)} \leq 1$
4. Suppose $2 \sigma-\lambda-1<0$, we have $p_{L}=1, p_{M}=1$, and $p_{H}=\frac{\sigma+(1+\gamma)(1+\lambda-2 \sigma)}{(1+\gamma)(1+\lambda-\sigma)}$.
5. To sum up ,we can show that:
(a) If $0 \leq \sigma \leq \frac{(1+\gamma)(1+\lambda)}{1+2 \gamma}$, then $p_{L}=1, p_{M}=1$ and $p_{H}=\frac{\sigma+(1+\gamma)(1+\lambda-2 \sigma)}{(1+\gamma)(1+\lambda-\sigma)}$.
(b) If $1 \geq \sigma \geq \frac{(1+\gamma)(1+\lambda)}{1+2 \gamma}$, then $p_{L}=1, p_{H}=0$, and $p_{M}=\frac{\sigma}{(1+\gamma)(-1-\lambda+2 \sigma)}$.
6. Since in the parameter region specified above $\frac{(1+\gamma)(1+\lambda)}{1+2 \gamma} \leq 1$, we know that both case (a) and (b) are possible.
(a) If $0 \leq \sigma \leq \frac{(1+\gamma)(1+\lambda)}{1+2 \gamma}, p_{L}=1, p_{M}=1, p_{H}=\frac{\sigma+(1+\gamma)(1+\lambda-2 \sigma)}{(1+\gamma)(1+\lambda-\sigma)}$, and $V=\frac{\gamma(1+\lambda-\sigma) \sigma}{(1+\gamma)(1+\lambda)^{2}}$.
Substituting $p_{L}, p_{M}$, and $p_{L}$ into C5, we have the following constraint:

$$
\gamma\left(-1-2 \lambda+\frac{\lambda(1+\lambda)}{1+\lambda-\sigma}+\frac{\sigma}{1+\gamma}\right) \geq 0
$$

which is equivalent to

$$
\sigma_{1} \leq \sigma \leq \sigma_{2},
$$

where

$$
\begin{aligned}
\sigma_{1} & =\frac{1}{2}\left(2+\gamma+3 \lambda+2 \gamma \lambda-\sqrt{2 \gamma \lambda(3+4 \lambda)+\lambda(4+5 \lambda)+(\gamma+2 \gamma \lambda)^{2}}\right) \\
\sigma_{2} & =\frac{1}{2}\left(2+\gamma+3 \lambda+2 \gamma \lambda+\sqrt{2 \gamma \lambda(3+4 \lambda)+\lambda(4+5 \lambda)+(\gamma+2 \gamma \lambda)^{2}}\right) .
\end{aligned}
$$

Taking into account all constraints on $\sigma$, we have the following problem:

$$
\min _{\sigma} V=\frac{\gamma(1+\lambda-\sigma) \sigma}{(1+\gamma)(1+\lambda)^{2}}
$$

such that

$$
\begin{gathered}
0 \leq \sigma \leq \frac{(1+\gamma)(1+\lambda)}{1+2 \gamma}=\sigma_{3}, \\
\sigma_{1} \leq \sigma \leq \sigma_{2} .
\end{gathered}
$$

We can show that if $\gamma<\frac{1}{4}\left(3 \lambda-\sqrt{8 \lambda+9 \lambda^{2}}\right)$, or $\gamma>\frac{1}{4}\left(3 \lambda+\sqrt{8 \lambda+9 \lambda^{2}}\right)$, then $\sigma_{3}<\sigma_{1}$ and the feasible region of $\sigma$ is empty. If $\frac{1}{4}\left(3 \lambda-\sqrt{8 \lambda+9 \lambda^{2}}\right) \leq$ $\gamma \leq \frac{1}{4}\left(3 \lambda+\sqrt{8 \lambda+9 \lambda^{2}}\right)$, then $\frac{1+\lambda}{2}<\sigma_{1} \leq \sigma \leq \sigma_{3} \leq 1$. Since $V$ is a quadratic function of $\sigma$, it is obvious that $V$ is minimized at $\sigma=\sigma_{3}=\frac{(1+\gamma)(1+\lambda)}{1+2 \gamma}$, and $V=\frac{\gamma^{2}}{(1+2 \gamma)^{2}}$.
Here we rearrange the parameter region. We show that if $0 \leq \gamma \leq 1$ and $\frac{2 \gamma^{2}}{1+3 \gamma} \leq \lambda \leq \frac{\gamma}{1+\gamma}$, then $p_{L}=1, p_{M}=1, p_{H}=0, \sigma=\frac{(1+\gamma)(1+\lambda)}{1+2 \gamma}$, and $V=\frac{\gamma^{2}}{(1+2 \gamma)^{2}}$.
(b) If $1 \geq \sigma \geq \frac{(1+\gamma)(1+\lambda)}{1+2 \gamma}$, we have $p_{L}=1, p_{H}=0, p_{M}=\frac{\sigma}{(1+\gamma)(-1-\lambda+2 \sigma)}$, and

$$
V=\frac{(1+\lambda-\sigma)((1+\lambda)(1+\lambda-\sigma)+\gamma(1+\lambda-2 \sigma)(1+\lambda+\sigma))}{(1+\gamma)(1+\lambda)^{2}(1+\lambda-2 \sigma)} .
$$

Substituting $p_{L}, p_{M}$, and $p_{L}$ into C5, we have the following constraint:

$$
\frac{(-\lambda+\gamma(2+\lambda-2 \sigma)) \sigma}{(1+\gamma)(1+\lambda-2 \sigma)} \leq 0
$$

which is equivalent to

$$
0 \leq \sigma \leq \frac{1+\lambda}{2} \text { or } \frac{1}{2}\left(2+\lambda-\frac{\lambda}{\gamma}\right) \leq \sigma .
$$

Taking into account all constraints on $\sigma$, we have the following reduced problem:

$$
\min _{\sigma} V=\frac{(1+\lambda-\sigma)((1+\lambda)(1+\lambda-\sigma)+\gamma(1+\lambda-2 \sigma)(1+\lambda+\sigma))}{(1+\gamma)(1+\lambda)^{2}(1+\lambda-2 \sigma)}
$$

such that

$$
\begin{gathered}
1 \geq \sigma \geq \frac{(1+\gamma)(1+\lambda)}{1+2 \gamma} \\
0 \leq \sigma \leq \frac{1+\lambda}{2} \text { or } \frac{1}{2}\left(2+\lambda-\frac{\lambda}{\gamma}\right) \leq \sigma .
\end{gathered}
$$

If $0 \leq \lambda \leq \frac{2 \gamma^{2}}{1+3 \gamma}$, then $1 \geq \sigma \geq \frac{1}{2}\left(2+\lambda-\frac{\lambda}{\gamma}\right)$. If $\frac{\gamma}{1+\gamma} \geq \lambda>\frac{2 \gamma^{2}}{1+3 \gamma}$, then $1 \geq \sigma \geq \frac{(1+\gamma)(1+\lambda)}{1+2 \gamma}$. Since the curve of $V$ is inverse U-shaped, we know that the minimal can be achieved at $\sigma=1, \sigma=\frac{1}{2}\left(2+\lambda-\frac{\lambda}{\gamma}\right)$, or $\sigma=$ $\frac{(1+\gamma)(1+\lambda)}{1+2 \gamma}$. When $\sigma=1, V_{1}=\frac{\lambda\left(\lambda+\lambda^{2}+\gamma\left(-1+\lambda+\lambda^{2}\right)\right)}{(1+\gamma)(-1+\lambda)(1+\lambda)^{2}}$. When $\sigma=\frac{1}{2}\left(2+\lambda-\frac{\lambda}{\gamma}\right)$, $V_{2}=\frac{\lambda\left(\lambda+2 \gamma \lambda(3+2 \lambda)-\gamma^{2}(4+3 \lambda)\right)}{4 \gamma(1+\lambda)^{2}(-\gamma+\lambda)}$. When $\sigma=\frac{(1+\gamma)(1+\lambda)}{1+2 \gamma}, V_{3}=\frac{\gamma^{2}}{(1+2 \gamma)^{2}}$.
To sum up, we have following three cases:
i. $V_{1}$ is chosen when $0<\gamma<\gamma^{*}$ and $0 \leq \lambda \leq \frac{-1-2 \gamma}{2(1+\gamma)}+\frac{1}{2} \sqrt{\frac{1+11 \gamma+24 \gamma^{2}+16 \gamma^{3}}{(1+\gamma)^{2}(1+3 \gamma)}}$ or $\gamma^{*}<\gamma<1$ and $0 \leq \lambda \leq \frac{-1-8 \gamma-3 \gamma^{2}}{2\left(-1+\gamma^{2}\right)}-\frac{1}{2} \sqrt{\frac{1+16 \gamma+54 \gamma^{2}+48 \gamma^{3}+25 \gamma^{4}}{\left(-1+\gamma^{2}\right)^{2}}}$.
ii. $V_{2}$ is chosen when $\gamma^{*}<\gamma<1$ and $\frac{-1-8 \gamma-3 \gamma^{2}}{2\left(-1+\gamma^{2}\right)}-\frac{1}{2} \sqrt{\frac{1+16 \gamma+54 \gamma^{2}+48 \gamma^{3}+25 \gamma^{4}}{\left(-1+\gamma^{2}\right)^{2}}}<$ $\lambda<\frac{2 \gamma^{2}}{1+3 \gamma}$.
iii. $V_{3}$ is chosen when $0<\gamma<\gamma^{*}$ and $\frac{-1-2 \gamma}{2(1+\gamma)}+\frac{1}{2} \sqrt{\frac{1+11 \gamma+242^{2}+16 \gamma^{3}}{(1+\gamma)^{2}(1+3 \gamma)}}<\lambda<$ $\frac{\gamma}{1+\gamma}$, or $\gamma^{*}<\gamma<1$ and $\frac{\gamma}{1+\gamma} \geq \lambda>\frac{2 \gamma^{2}}{1+3 \gamma}$.
Since the solution given in case (b) is superior to that in case (a), the above solution is the final solution.
7. Next we consider the case that C5 is binding. Using the same method, we
get the minimized value which is not smaller than the value for $V$ specified above. Substituting the solution to the original problem, we show that all the constraints are satisfied. Hence, this is also the solution to the original problem.

Part 2 (The high type mixes). Suppose that the high type mix between the high message (with probability $\rho$ ) and the low message. The low type only sends the low message. Let $\zeta:=\frac{q(1-\rho)}{1-q \rho}$ be the posterior of facing a high type after the low message. Let $\pi:=1-q \rho$ be the probability of low message. The optimal equilibrium is found by solving the following program.

$$
\min _{b, p_{L}, p_{M}, p_{H}, \sigma} \pi^{2}\left(1-p_{L}\right)+2 \pi(1-\pi)\left(1-p_{M}\right)+(1-\pi)^{2}\left(1-p_{H}\right)
$$

subject the ex ante $\mathrm{IC}^{*}$ constraint for the for the low type:

$$
\begin{aligned}
& \pi\left(\left(1-p_{L}\right)(\zeta(1-p) \theta+(1-\zeta) \theta / 2)+p_{L} \frac{1}{2}\right)+(1-\pi)\left(\left(1-p_{M}\right)(1-p) \theta+p_{M}(1-b)\right) \\
\geq & \pi\left(\left(1-p_{M}\right)\left(\zeta(1-p) \theta+(1-\zeta) \frac{\theta}{2}\right)+p_{M} \max \left\{b,\left(\zeta(1-p) \theta+(1-\zeta) \frac{\theta}{2}\right)\right\}\right) \\
& +(1-\pi)\left(\left(1-p_{H}\right)(1-p) \theta+p_{H} \max \left\{\frac{1}{2},(1-p) \theta\right\}\right)
\end{aligned}
$$

to the indifference condition for the high type

$$
\begin{aligned}
& \pi\left(\left(1-p_{M}\right)\left(\zeta \frac{\theta}{2}+(1-\zeta) p \theta\right)+p_{M} b\right)+(1-\pi)\left(\left(1-p_{H}\right) \frac{\theta}{2}+p_{H} \frac{1}{2}\right)= \\
& \pi\left(\left(1-p_{L}\right)\left(\zeta \frac{\theta}{2}+(1-\zeta) p \theta\right)+p_{L} \frac{1}{2}\right)+(1-\pi)\left(\left(1-p_{M}\right) \frac{\theta}{2}+p_{M}(1-b)\right)
\end{aligned}
$$

to the high-type ex post constraints:

$$
b \geq \zeta \theta / 2+(1-\zeta) p \theta, 1 / 2 \geq \theta / 2,1 / 2 \geq \zeta \frac{\theta}{2}+(1-\zeta) p \theta, 1-b \geq \frac{\theta}{2}
$$

to the low-type ex post constraints:

$$
1-b \geq(1-p) \theta, 1 / 2 \geq \zeta(1-p) \theta+(1-\zeta) \theta / 2
$$

and to the probability constraints:

$$
0 \leq p_{L} \leq 1,0 \leq p_{M} \leq 1,0 \leq p_{H} \leq 1,0 \leq \sigma \leq 1
$$

But is immediate to note that the constraint set is empty. Indeed, the third high-type ex post constraint is equivalent to:

$$
-\frac{1}{2}(1-\theta) \frac{\gamma-\lambda(1-\rho)}{1+\lambda(1-\rho)} \geq 0
$$

which cannot be the case for $\gamma>\lambda$.
Part 3 (Both types mix). Suppose that the low type mixes between the low message (with probability $\sigma$ ) and the high message. The high type mixes between the high message (with probability $\rho$ ) and the low message. Let $\chi:=\frac{q \rho}{1-\pi}$ be the posterior of facing a high type after the high message. Let $\pi:=(1-q) \sigma+q(1-\rho)$ be the probability of a low message. Let $\zeta:=\frac{q(1-\rho)}{\pi}$ be the posterior of facing a high type after the low message. The optimal equilibrium solves the following program:

$$
\min _{b, p_{L}, p_{M}, p_{H}, \sigma} \pi^{2}\left(1-p_{L}\right)+2 \pi(1-\pi)\left(1-p_{M}\right)+(1-\pi)^{2}\left(1-p_{H}\right)
$$

subject the ex ante $\mathrm{IC}^{*}$ constraint for the for the low type:

$$
\begin{aligned}
& \pi\left(\left(1-p_{L}\right)(\zeta(1-p) \theta+(1-\zeta) \theta / 2)+p_{L} \frac{1}{2}\right)+(1-\pi)\left(\left(1-p_{M}\right)\left(\chi(1-p) \theta+(1-\chi) \frac{\theta}{2}\right)+p_{M}(1-b)\right) \\
& =\pi\left(\left(1-p_{M}\right)(\zeta(1-p) \theta+(1-\zeta) \theta / 2)+p_{M} b\right)+(1-\pi)\left(\left(1-p_{H}\right)\left(\chi(1-p) \theta+(1-\chi) \frac{\theta}{2}\right)+p_{H} \frac{1}{2}\right)
\end{aligned}
$$

to the indifference condition for the high type

$$
\begin{aligned}
& \pi\left(\left(1-p_{M}\right)\left(\zeta \frac{\theta}{2}+(1-\zeta) p \theta\right)+p_{M} b\right)+(1-\pi)\left(\left(1-p_{H}\right)\left(\chi \frac{\theta}{2}+(1-\chi) p \theta\right)+p_{H} \frac{1}{2}\right)= \\
& \pi\left(\left(1-p_{L}\right)\left(\zeta \frac{\theta}{2}+(1-\zeta) p \theta\right)+p_{L} \frac{1}{2}\right)+(1-\pi)\left(\left(1-p_{M}\right)\left(\chi \frac{\theta}{2}+(1-\chi) p \theta\right)+p_{M}(1-b)\right)
\end{aligned}
$$

to the high-type ex post constraints:
$b \geq \zeta \theta / 2+(1-\zeta) p \theta, 1 / 2 \geq \chi \theta / 2+(1-\chi) p \theta, \frac{1}{2} \geq \zeta \frac{\theta}{2}+(1-\zeta) p \theta, 1-b \geq \chi \frac{\theta}{2}+(1-\chi) p \theta$
to the low-type ex post constraints:
$1-b \geq \chi(1-p) \theta+(1-\chi) \theta / 2,1 / 2 \geq \zeta(1-p) \theta+(1-\zeta) \theta / 2, b \geq \zeta(1-p) \theta+(1-\zeta) \frac{\theta}{2}$

$$
\frac{1}{2} \geq \chi(1-p) \theta+(1-\chi) \frac{\theta}{2}
$$

and to the probability constraints:

$$
0 \leq p_{L} \leq 1,0 \leq p_{M} \leq 1,0 \leq p_{H} \leq 1,0 \leq \sigma \leq 1,0 \leq \rho \leq 1
$$

But is immediate to note that the constraint set is empty. Indeed, second and fourth high-type ex post constraints are equivalent to:

$$
X:=\frac{1}{2}(1-\theta) \frac{(\rho+\sigma) \lambda-\gamma}{\rho \lambda+1-\sigma} \geq 0, Z:=\frac{1}{2}(1-\theta) \frac{\rho \lambda-\lambda+\sigma \gamma}{\rho \lambda-\lambda-\sigma} \geq 0
$$

Evidently, $X \geq 0$ requires $\lambda \geq \frac{\gamma}{\rho+\sigma}$, which, in light of $\gamma>\lambda$, requires $\rho+\sigma>1$. Consider $Z$, note that it increases in $\lambda$. When $\lambda$ takes its upper value $\gamma$,

$$
Z=\frac{1}{2}(1-\theta) \frac{(1-\sigma-\rho) \gamma}{\sigma+\gamma(1-\rho)}
$$

which is positive if and only if $\sigma+\rho \leq 1$. This concludes that whenever $\gamma>\lambda$, either $X<0$ or $Z<0$ or both.


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    ${ }^{\dagger}$ Yale University, Department of Economics.
    ${ }^{\ddagger}$ European University Institute, Department of Economics, and Columbia University, Department of Political Science.
    ${ }^{\text {§ }}$ Essex University, Department of Economics.
    ${ }^{1}$ See Jackson and Morelli (2011) for an updated survey of such a positive analysis.

[^1]:    ${ }^{2}$ A few papers study mechanism design in international relations (Bester and Wärneryd, 2006, and Fey and Ramsay 2009, 2010); we discuss them later in details. A discussion on the importance of institutional design for conflict or international cooperation is in Koremenos et al (2001).
    ${ }^{3}$ Blainey (1988) famously argued that wars begin when states disagree about their relative power and end when they agree again (see also Brito and Intriligator, 1985, and Fearon, 1995). Wars may arise because of asymmetric information about military strength, but also about the value of outside options or about the contestants' political resolve, i.e. about the capability of the leaders and the peoples to sustain war. For example, it is known that Saddam Hussein grossly under-estimated the US administration political resolve, when invading Kuwait in 1990.
    ${ }^{4}$ The role of communication in reducing the probability of conflict due to asymmetric information is established by Baliga and Sjostrom (2004).
    ${ }^{5}$ As well as international conflict, the intuition that private information may cause bargaining failures has been invoked as an explanation for costly trials in the case of litigation, and strikes in the case of wage bargaining (see Kennan and Wilson, 1993, for an early review). But unlike in international relations, where nations are sovereign, arbitration is always possible in these contexts; and hence the study of mediation has not been much developed. Further, most of the analysis has focused on the performance of currently available arbitration mechanisms in specific game theoretic models, rather than characterizing optimal arbitration, which is the scope of mechanism design analysis.
    ${ }^{6}$ As some scholars claim, "mediator impartiality is crucial for disputants' confidence in the mediator, which, in turn, is a necessary condition for his gaining acceptability, which, in turn, is essential for mediation success to come about" (see e.g. Young, 1967, and the scholars mentioned in Kleiboer, 1996). On the other

[^2]:    hand, when a mediator possesses independent information that needs to be credibly transmitted, some degree of bias may be optimal (see Kydd, 2003, Rauchaus, 2006).
    ${ }^{7}$ In the final discussion, we provide some anecdotal evidence supporting our assumption of full mediator's commitment, which is obviously also one of our normative prescriptions.
    ${ }^{8}$ Among the few papers studying self-enforcing mechanisms, see Matthews and Postlewaite (1989), Banks and Calvert (1992), Cramton and Palfrey (1995), Forges (1999), Compte and Jehiel (2008), and Goltsman et al. (2009).
    ${ }^{9}$ Viewed another way, countries cannot commit not to initiate war if such an attack is a profitable deviation from an agreement. In this sense, even if the bargaining problem comes from asymmetric information, we also have a natural form of commitment problem built in. See Powell (2006) for a recent comprehensive discussion of the relative importance of asymmetric information and commitment problems in creating bargaining breakdown.

[^3]:    ${ }^{10}$ This is a standard metaphor for many types of wars, for example related to territorial disputes or to the present and future sharing of the rents from the extraction of natural resources. Indeed, Bercovitch et al (1991) show that mediation is useful mostly when the disputes are about resources, territory, or in any case divisible issues.
    ${ }^{11}$ It might be interesting to allow for different costs for symmetric and asymmetric wars, but the additional notational and computational costs appear a heavy price to pay.

[^4]:    ${ }^{12}$ One of the mediator's role in our model will be to make peaceful split recommendations after hearing the players' private report. By selecting the split values that induce equilibria with the highest chance of peace in our benchmark, we isolate the information management role of the mediator from her split proposal role.
    ${ }^{13}$ In a small parameter region, in which the cost of war is high, the players can improve on the separating equilibrium, by playing a mixed strategy equilibrium in the cheap talk game. Of course, mixed strategy equilibria are strictly dominated by mediation, as mixed strategies induce randomizations independent across players, instead of the optimally correlated randomizations chosen by the mediator (see, e.g. Aumann, 1974).
    ${ }^{14}$ The model by Banks and Calvert (1992) can be related to our construction. They also compare the solution of self-enforcing mediation to what can be achieved without a mediator in an underlying two-by-two game. But their underlying game is very different from our game of conflict: They consider a coordination game with incomplete information.

[^5]:    ${ }^{15}$ Interestingly, the intensity of conflict and asymmetric information are considered among the most important variables that affect when mediation is most successful (see e.g. Bercovitch and Houston, 2000, and Bercovitch et al., 1991). Our findings resonate with well-documented stylized facts in the empirical literature on negotiation (Bercovich and Jackson 2001, Wall and Lynn, 1993), that show that parties are less likely to reach an agreement without a mediator when the intensity of conflict is high than when it is low. Rauchhaus (2006) provides quantitative analysis showing that mediation is especially effective when it targets asymmetric information.
    ${ }^{16}$ This result is in contrast with findings in other environments (e.g., Cramton and Palfrey, 1995, Compte and Jehiel, 2008, or Goltsman et al., 2009).

[^6]:    ${ }^{17}$ Another difference is that unlike them we impose sequential rationality after every history, including after deviations, as it affects incentives at the reporting stage (see for instance Green and Laffont, 1987 for the importance of applying sequential rationality after every history).
    ${ }^{18}$ Depending on the context, of course, the interpretation of the cake ranges from territory or exploitation of natural resources to any measure of social surplus in a country or partnership.
    ${ }^{19}$ To simplify the analysis, and keep the problem's dimensionality in check, we adopt a fully symmetric model. We believe that our results will hold approximately, for models that are close to symmetric.

[^7]:    ${ }^{20}$ Even though simultaneous decisions to go to war are sequentially rational in all circumstances, one could conceive other game forms with sequential decisions to accept or reject an agreement, and in such game forms one could intuitively expect a lower frequency of war. Since this intuition about alternative game forms can apply only for the game without communication and for unmediated communication, while with mediation the order of play is irrelevant, it follows that our choice of game form, if anything, stacks the deck against the mediator, hence making our conclusions to follow on the importance of mediation robust to changes in the underlying game.
    ${ }^{21}$ If the cake is a resource that can be depleted in a short period and does not have spillovers on relative strength, then there is no commitment problem. If the cake sharing is instead to be interpreted as a durable agreement for example on the exploitation of a future stream of resources or gains from trade, then the commitment problem is non trivial. In this case the agreement could be about periodic tributes to be made in perpetuity, and there are ways to implement the agreement with sufficient use of dynamic incentives. See for example Schwartz and Sonin (2008).

[^8]:    ${ }^{22}$ This feature will allow us to give graphical illustrations of most results.

[^9]:    ${ }^{23}$ This might help, however. Aumann and Hart (2003) provide examples of games in which longer, indeed unbounded, communication protocols improve upon finite round communication.
    ${ }^{24}$ Note that can replace without loss any lottery over peaceful recommendations with its certainty equiv-

[^10]:    alent. In fact, at the agreement stage, the requirement that the players accept such a deterministic average split is less stringent than the requirement that they accept all splits in the support of the lottery. Further, lotteries over peaceful splits affect each player's equilibrium payoff at the communication stage only through their expectations. Finally, the payoff of a player who deviates at the communication stage is convex in the recommended split, as we shall later see. Hence, the deviation payoff is lower when replacing a lottery with its certainty equivalent, thus making the equilibrium requirement less stringent.
    ${ }^{25}$ We will see that each player's constraints are linear in the maximization arguments. Thus, the constraint set is convex. Hence, suppose that an asymmetric mechanism maximizes the probability of peace. Because the set-up is symmetric across players, the anti-symmetric mechanism, obtained by interchanging the players' identities, is also optimal. But then, the constraint set being convex, it contains also the symmetric mechanism obtained by mixing the above optimal mechanisms. As the objective function is linear in the maximization argument, such symmetric mixed mechanism is also optimal.
    ${ }^{26}$ The "star" superscript refers to the fact that, when a player contemplates deviating at the message stage, she also anticipates and takes into account that she might prefer to declare war ex post, even when players are supposed to coordinate on peace. This explains the maxima on the right-hand side of the two

[^11]:    ${ }^{28}$ In this subsection, and this subsection only, attention is restricted to symmetric equilibria. That is, we did not establish whether asymmetric mixed-strategy equilibria may yield a higher welfare.

[^12]:    ${ }^{29}$ Clearly all recommendation leading to war induce the same payoffs, and hence can be subsumed by the recommendation $b=0$, which only induces war in the agreement game. This feature of the model should not be taken literally. In the real world, mediators do not literally make recommendation leading to war, but they may quit, and this usually results in conflict escalation by the contestants.

[^13]:    ${ }^{30}$ In fact, both participation and revelation decisions are taken before knowing the arbitrator's recommendation, and hence the players' payoffs depend only on the expected recommendation, and not on the realized one. Hence, as in footnote 24 , any lottery over peaceful recommendations can be replaced without loss with its certainty equivalent.

[^14]:    ${ }^{31}$ This result facilitates the proof of Proposition 3. It is enough to establish that the simple mechanism characterized there, and described in closed form in the Appendix, satisfies the more stringent constraints of the mediator's program. Because this mechanism achieves the same welfare as the solution to the arbitration problem, it must be optimal, a fortiori, in the mediator's program.

[^15]:    ${ }^{32}$ Indeed, it is known since at least Myerson and Satterthwaite (1983) that such possibility results might hinge on discreteness.

[^16]:    ${ }^{33}$ Interestingly, scholars seem to disagree on the likely motives for consenting to mediation. According to Princen (1992), such motives are individual interests, rather than "shared values". But Bercovitch (1992, 1997) argues that disputants might view mediation as an expression of their commitment to peaceful conflict resolution, and seek it out of a desire to improve their relationships with each other.

[^17]:    ${ }^{34}$ See Bebchik (2002) on how Clinton and Ross attempted to impress upon Arafat the urgency of accepting the proposal being offered for a final settlement, calling it a "damn good deal" that would not be within his grasp indefinitely.

