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# EFFECTIVE LABOR REGULATION AND MICROECONOMIC FLEXIBILITY\*

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## Abstract

Microeconomic flexibility is at the core of economic growth in modern market economies because it facilitates the process of creative-destruction. The main reason why this process is not infinitely fast, is the presence of adjustment costs, some of them technological, others institutional. Chief among the latter is labor market regulation. While few economists object to the hypothesis that labor market regulation hinders the process of creative-destruction, its empirical support is limited. In this paper we revisit this hypothesis, using a new sectoral panel for 60 countries and a methodology suitable for such a panel. We find that job security regulation clearly hampers the creative-destruction process, especially in countries where regulations are likely to be enforced. Moving from the 20th to the 80th percentile in job security, in countries with strong rule of law, cuts the annual speed of adjustment to shocks by a third while shaving off about one percent from annual productivity growth. The same movement has negligible effects in countries with weak rule of law.

**JEL Codes:** E24, J23, J63, J64, K00.

**Keywords:** Microeconomic rigidities, creative-destruction, job security regulation, adjustment costs, rule of law.

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# 1 Introduction

Microeconomic flexibility, by facilitating the ongoing process of creative-destruction, is at the core of economic growth in modern market economies. This basic idea has been with economists for centuries, was brought to the fore by Schumpeter fifty years ago, and has recently been quantified in a wide variety of contexts.<sup>1</sup> In US Manufacturing, for example, more than half of aggregate productivity growth can be directly linked to this process.<sup>2</sup>

The main obstacle faced by microeconomic flexibility is adjustment costs. Some of these costs are purely technological, others are institutional. Chief among the latter is labor market regulation, in particular job security provisions. The literature on the impact of labor market regulation on the many different economic, political and sociological variables associated to labor markets and their participants is extensive and contentious. However, the proposition that job security provisions reduce restructuring is a point of agreement.

Despite this consensus, the empirical evidence supporting the negative impact of labor market regulation on microeconomic flexibility has been scant at best. This is not too surprising, as the obstacles to empirical success are legions, including poor measurement of restructuring activity and labor market institutions variables, both within a country and more so across countries.<sup>3</sup> In this paper we make a new attempt. We develop a methodology that allows us to bring together the extensive new data set on labor market regulation constructed by Botero et al. (2004) with comparable cross-country cross-sectoral data on employment and output from the UNIDO (2002) data-set. We also emphasize the key distinction between *effective* and official labor market regulation.

The methodology builds on the simple partial-adjustment idea that larger adjustment costs are reflected in slower employment adjustment to shocks.<sup>4</sup> The accumulation of limited adjustment to these shocks builds a wedge between frictionless and actual employment, which is the main right hand side variable in this approach. We propose a new way of estimating this wedge, which allows us to pool data on labor market legislation with comparable employment and output data for a broad range of countries. As a result, we are able to enlarge the effective sample to 60 economies, more than double the country coverage of previous studies in this literature.<sup>5</sup> Our attempt to measure *effective* labor regulation interacts existing measures of job security provision with measures of rule of law and government efficiency.<sup>6</sup>

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<sup>1</sup>See, e.g., the review in Caballero and Hammour (2000).

<sup>2</sup>See, e.g., Foster, Haltiwanger and Krizan (1998).

<sup>3</sup>On a closely related literature, there is an extensive body of empirical work, pioneered by Lazear (1990), that has put together data on job security provisions across countries and over time, and measured the effect of these provisions on aggregate employment. A recent survey of this literature can be found in Heckman and Pages (2003). Results are mixed. On the one hand, Lazear (1990), Grubb and Wells (1993), Nickell (1997) and Heckman and Pages (2000) find a negative relationship between job security and employment levels. On the other hand Garibaldi and Mauro (1999), OECD (1999), Addison, Teixeira and Grosso (2000), and Freeman (2001) fail to find evidence of such a relationship.

<sup>4</sup>For surveys of the empirical literature on partial-adjustment see Nickell (1986) and Hammermesh (1993).

<sup>5</sup>To our knowledge, the broadest cross-country study to date – Nickell and Nuziata (2000) – included 20 high income OECD countries. Other recent studies, such as Burgess and Knetter (1998) and Burgess et al. (2000), pool industry-level data from 7 OECD economies.

<sup>6</sup>See Loboguerrero and Panizza (2003) for a similar interaction term in their study of the relation between labor market institu-

Our results are clear and robust: countries with less effective job security legislation adjust more quickly to imbalances between frictionless and actual employment. In countries with strong rule of law, moving from the 20th to the 80th percentile of job security lowers the speed of adjustment to shocks by 35 percent which amounts to a cut in annual productivity of 0.85% in an *AK*-type world. The same movement for countries with low rule of law only reduces the speed of adjustment by approximately 1 percent and productivity growth by 0.02 percent.

The paper proceeds as follows. Section 2 presents the methodology and describes the new data set. Section 3 discusses the main results and explores their robustness. Section 4 gauges the impact of effective labor protection on productivity growth. Section 5 concludes and is followed by various appendices.

## 2 Methodology and Data

Our methodology is based on an adjustment cost model where the dynamic employment gap is given by a simple expression involving employment and nominal output, both of which are available in the sectoral panel for 60 countries we use in the empirical part.

### 2.1 Methodology

The starting point is a partial adjustment framework where the change in the number of (filled) jobs in sector  $j$  in country  $c$  between time  $t - 1$  and  $t$  is a fraction of the gap between desired and actual employment. That is:

$$\Delta e_{jct} = \Psi_{jct}(e_{jct}^* - e_{jct,t-1}), \quad (1)$$

where  $e$  and  $e^*$  denote the logarithm of employment and desired employment, respectively.

Equation (1) can be rationalized via quadratic adjustment costs (Sargent, 1978), or an exogenous process where the  $\Psi_{jct}$  are either zero or one (Calvo, 1983), or a stochastic adjustment cost model that nests the preceding models as particular cases (Caballero, Cowan, Engel and Micco, 2004). For simplicity we consider the Calvo interpretation— see Caballero et al. (2004) for the more general case. We therefore assume that the  $\Psi_{jct}$  are i.i.d., both across sectors and over time, taking values 0 or 1, with a country-specific mean  $\lambda_c$ . Since these stochastic adjustment speeds can be viewed as resulting from adjustment costs that are either zero (with probability  $\lambda_c$ ) or infinite (with probability  $1 - \lambda_c$ ) we refer to these frictions as “adjustment costs”. The parameter  $\lambda_c$  captures microeconomic flexibility. As  $\lambda_c$  goes to one, all gaps are closed quickly and microeconomic flexibility is maximum. As  $\lambda_c$  decreases, microeconomic flexibility declines.

Equation (1) hints at two important components of our methodology: We need a measure of the employment gap and a strategy to estimate the country-specific speeds of adjustment (the  $\lambda_c$ ). We describe both ingredients in detail in what follows. In a nutshell, we construct estimates of  $e_{jct}^*$ , the only unobserved element of the gap, by solving the optimization problem of a sector’s representative firm, as a function of ob-

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tions and inflation.

servables such as labor productivity and a suitable proxy for the average market wage. We estimate  $\lambda_c$  based upon the large cross-sectional size of our sample and the well documented heterogeneity in the realizations of the gaps (see, e.g., Caballero, Engel and Haltiwanger (1997) for US evidence).

### 2.1.1 Employment gap measure

A sector's representative firm faces an isoelastic demand and has access to a production technology that is Cobb-Douglas in labor and hours per worker:

$$\begin{aligned} y &= a + \alpha e + \beta h, \\ p &= d - \frac{1}{\eta} y, \end{aligned}$$

where  $y$ ,  $p$ ,  $e$ ,  $h$ ,  $a$  and  $d$  denote output, price, employment, hours per worker, productivity and demand shocks, and  $\eta$  is the price-elasticity of demand. We let  $\gamma \equiv (\eta - 1)/\eta$ , and assume  $\eta > 1$ ,  $\alpha > \beta > 0$  and  $\alpha\gamma < 1$ . Firms are competitive in the labor market but pay wages that increase with hours worked according to a wage schedule  $w(h)$ , with  $w'$  and  $w''$  strictly positive. All lower case variables are in logs.

If the firm can adjust hours and employment in every period at no cost, then its profit maximizing inputs, denoted by  $\hat{h}$  and  $\hat{e}$ , are characterized by:

$$w'(\hat{h}) = \frac{\beta}{\alpha}, \tag{2}$$

$$\hat{e} = \frac{1}{1 - \alpha\gamma} [\log \beta\gamma + d + \gamma a - (1 - \beta\gamma)\hat{h} - \log\{W'(\hat{H})\}], \tag{3}$$

where  $\log W(H) \equiv \{w(\log H)\}$  and  $\log \hat{H} \equiv \hat{h}$  (see Appendix A for the derivation). It follows from (2) that our functional forms imply that the optimal choice of hours,  $\hat{h}$ , does not depend on productivity and demand shocks.

Having solved the problem of a firm that faces no frictions, we turn next to the case with adjustment costs. A key assumption is that the representative firm within each sector only faces adjustment costs when it changes employment levels, not when it changes the number of hours worked.<sup>7</sup> It follows that the sector's choice of hours in every period can be expressed in terms of its current level of employment, by solving the corresponding first order condition for hours, which leads to an expression analogous to (3) with  $h$  and  $e$  in the place of  $\hat{h}$  and  $\hat{e}$ . Subtracting this expression from (3) and writing the Taylor expansion for  $\log\{W'(e^h)\}$  around  $h = \hat{h}$  as

$$\log\{W'(H)\} \cong \log\{W'(\hat{H})\} + (\mu - 1)(h - \hat{h}),$$

<sup>7</sup>For evidence on this see Sargent (1978) and Shapiro (1986). Also note that overtime payments, captured by the wage schedule  $w(h)$ , should not be viewed as adjustment costs since they depend on the level of hours worked, not on the change in hours.

with  $\mu - 1 \equiv W''(\hat{H})\hat{H}/W'(\hat{H})$  assumed positive, we obtain:<sup>8</sup>

$$\hat{e} - e = \frac{\mu - \beta\gamma}{1 - \alpha\gamma}(h - \hat{h}). \quad (4)$$

This is the expression used by Caballero and Engel (1993). It cannot be applied in our case, since we do not have information on hours worked. For this reason we derive next an analogous expression relating the employment gap to the labor productivity gap; as we discuss later in this section, we have the data to apply this expression.

The value of the marginal product of labor (referred to, with some abuse, as “marginal labor productivity” in what follows) satisfies:

$$v = \log \alpha\gamma + d + \gamma a - (1 - \alpha\gamma)e + \beta\gamma h.$$

Subtracting this expression from its frictionless counterpart (obtained by substituting  $\hat{h}$  and  $\hat{e}$  for  $e$  and  $h$ ) and then using (4) to get rid of the hours gap yields:

$$\hat{e} - e = \frac{\phi}{1 - \alpha\gamma}(v - \hat{w}), \quad (5)$$

where  $\hat{w} \equiv w(\hat{h})$  and  $\phi \equiv (\mu - \beta\gamma)/\mu$ . The parameter  $\phi$  is increasing in the elasticity of the marginal wage schedule with respect to average hours worked,  $\mu - 1$ , which is intuitive since the employment response to a given deviation of wages from marginal product will be larger if the marginal cost of the alternative adjustment strategy —changing hours— is higher.

The employment gap,  $\hat{e} - e$ , in (5) is the difference between the *static* target  $\hat{e}$  and realized employment, not the dynamic employment gap  $e_{jct}^* - e_{jct}$  related to the term on the right hand side of (1). However, if we assume that the linear combination of demand and productivity shocks,  $d + \gamma a$ , follows a random walk —an assumption consistent with the data<sup>9</sup>— we have that  $e_{jct}^*$  is equal to  $\hat{e}_{jct}$  plus a constant proportional to the drift in the random walk. Allowing for a country-specific stochastic drift (see Appendix B for details), and for sector-specific differences in  $\alpha$  and  $\gamma$ , leads to:

$$e_{jct}^* - e_{jct-1} = \frac{\phi}{1 - \alpha_j\gamma_j}(v_{jct} - w_{jct}^o) + \Delta e_{jct} + \delta_{ct}. \quad (6)$$

Note that both marginal product and wages are in nominal terms. However, since these expressions are in logs, their difference eliminates the aggregate price level component.

We proxy  $\alpha_j\gamma_j$  by the sample median of the labor share for sector  $j$  across year and income groups.

<sup>8</sup>No approximation is involved when the elasticity  $W''(\hat{H})\hat{H}/W'(\hat{H})$  does not vary with  $H$ , that is, when  $W(H) = c_1 + c_2H^\mu$  with  $c_1, c_2 > 0$  and  $\mu > 1$ . This is the case considered in Caballero and Engel (1993) and Caballero et al. (2004). Also note that  $\mu > 1$  is needed to ensure that the second order conditions hold for the frictionless optimum (see Appendix A).

<sup>9</sup>Pooling all countries and sectors together, the first order autocorrelation of the measure of  $\Delta e_{jct}^*$  constructed below is  $-0.018$ . Computing this correlation by country the mean value is 0.011 with a standard deviation of 0.179.

We estimate the marginal productivity of labor,  $v_{jct}$ , using output per worker multiplied by an industry-level labor share, assumed constant within country income groups (defined below) and over time.

Two natural candidates to proxy for  $w_{jct}^o$  are the average (across sectors within a country, at a given point in time) of either observed wages or observed marginal productivities. The former is consistent with a competitive labor market, the latter may be expected to be more robust in settings with long-term contracts and multiple forms of compensation, where the salary may not represent the actual marginal cost of labor.<sup>10</sup> We performed estimations using both alternatives and found no discernible differences (see below). This suggests that statistical power comes mainly from the cross-section dimension, that is, from the well documented and large magnitude of sector-specific shocks. In what follows we report the more robust alternative and approximate  $w^o$  by the average marginal productivity, which leads to:

$$e_{jct}^* - e_{jct-1} = \frac{\phi}{1 - \alpha_j \gamma_j} (v_{jct} - v_{.ct}) + \Delta e_{jct} + \delta_{ct} \equiv \text{Gap}_{jct} + \delta_{ct}, \quad (7)$$

where  $v_{.ct}$  denotes the average, over  $j$ , of  $v_{jct}$  (we use this convention throughout the paper).

Differencing (7), we estimate  $\phi$  from

$$\Delta e_{jct} = -\frac{\phi}{1 - \alpha_j \gamma_j} (\Delta v_{jct} - \Delta v_{.ct}) - \Delta \delta_{ct} + \Delta e_{jct}^* \equiv -\phi z_{jct} + \kappa_{ct} + \varepsilon_{jct}, \quad (8)$$

where  $\kappa_{ct} \equiv -\Delta \delta_{ct}$  is a country-year dummy,  $\varepsilon_{jct} \equiv \Delta e_{jct}^*$  is the change in the desired level of employment and  $z_{jct} \equiv (\Delta v_{jct} - \Delta v_{.ct}) / (1 - \alpha_j \gamma_j)$ . We assume that changes in sectoral labor composition are negligible between two consecutive years. In order to avoid the simultaneity bias present in this equation ( $\Delta v$  and  $\Delta e^*$  are clearly correlated) we estimate (8) using  $(\Delta w_{jct-1} - \Delta w_{.ct-1})$  as an instrument for  $(\Delta v_{jct} - \Delta v_{.ct})$ .<sup>11</sup>

Table 1 reports the estimation results of (8) for the full sample of countries and across income and job security groups. The first two columns use the full sample, with and without two percent of extreme values for the independent variable, respectively. The remaining columns report the estimation results for each of our three income groups and job security groups (more on both of these measures in Section 2.2). Based on our results for the baseline case, we set the value of  $\phi$  at its full sample estimate of 0.4 for all countries in our sample.

The expression for the employment gap defined implicitly in (7) ignores systematic variations in labor productivity across sectors within a country. For example, unobserved labor quality may be much higher in some sectors. The presence of such heterogeneity could bias estimates of the speed of adjustment downwards, since measured productivity gaps would be positive most of the time for sectors with high labor quality while being mostly negative for sectors with lower quality workers.<sup>12</sup> To avoid this potential bias,

<sup>10</sup>While we have assumed a simple competitive market for the base salary (salary for normal hours) within each sector, our procedure could easily accommodate other, more rent-sharing like, wage setting mechanisms (with a suitable reinterpretation of some parameters, but not  $\lambda_c$ ).

<sup>11</sup>We lag the instrument to deal with the simultaneity problem and use the wage rather than productivity to reduce the (potential) impact of measurement error bias.

<sup>12</sup>The impact of this bias on estimates of  $\phi$  is likely to be less important, since equation (8) is in differences while the equations

Table 1: ESTIMATING  $\phi$ 

Specification:	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
	Change in Employment (ln)							
$z_{jct}$	-0.280 (0.044)	-0.394 (0.068)	-0.558 (0.135)	-0.355 (0.119)	-0.387 (0.116)	-0.363 (0.091)	-1.168 (.357)	-0.352 (0.103)
Observations	22,810	22,008	8,311	6,378	7,319	7,730	6,883	7,036
Income Group	All	All	1	2	3	All	All	All
Job Sec. Group	All	All	All	All	All	1	2	3
Extreme obs. of instrument	Yes	No	No	No	No	No	No	No

Standard errors reported in parentheses. All estimates are significant at the 1% level. All regressions use lagged  $\Delta w_{ict} - \Delta w_{ct}$  as instrumental variable. As described in the main text,  $z_{jct}$  represents the log-change of the nominal marginal productivity of labor in each sector, minus the country average, divided by one minus the estimated labor share. All regressions disregard the 2% observations with most extreme change in employment values and include a country-year fixed effect ( $\kappa_{ct}$  in (8)). Income groups are 1: High Income OECD, 2: High Income Non OECD and Upper Middle Income, and 3: Lower Middle Income and Low Income. Job Security Groups correspond to the highest, middle and lowest third of the measure in Botero et al. (2004).

we subtract from  $(v_{jct} - v_{ct})$  in (7) a moving average of relative sectoral productivity,  $\hat{\theta}_{jct}$ , where

$$\hat{\theta}_{jct} \equiv \frac{1}{2}[(v_{jct-1} - v_{ct-1}) + (v_{jct-2} - v_{ct-2})].$$

As a robustness check, for our main specifications we also computed  $\hat{\theta}_{jct}$  using a three and four periods moving average, without significant changes in our results (more on this when we check robustness in Section 3.2). The resulting expression for the estimated employment-gap is:

$$\text{Gap}_{jct} = \frac{\phi}{1 - \alpha_j \gamma_j} (v_{jct} - v_{ct} - \hat{\theta}_{jct}) + \Delta e_{jct}. \quad (9)$$

It is important to point out that our methodology yields an employment gap measure, defined implicitly in (9), that has some advantages over standard partial adjustment estimations. First, it summarizes in a single variable all shocks faced by a sector. This feature allows us to increase precision and to study the determinants of the speed of adjustment using interaction terms. Second, and related, it only requires data on nominal output and employment, two standard and well-measured variables in most industrial surveys. Most previous studies on adjustment costs required measures of real output or an exogenous measure of sector demand.<sup>13</sup>

to estimate the speed of adjustment considered below are in levels.

<sup>13</sup>Abraham and Houseman (1994), Hammermesh (1993), and Nickel and Nunziata (2000) evaluate the differential response of employment to observed real output. A second option is to construct exogenous demand shocks. Although this approach overcomes the real output concerns, it requires constructing an adequate sectorial demand shock for every country. A case in point are the papers by Burgess and Knetter (1998) and Burgess et al. (2000), which use the real exchange rate as their demand shock. The estimated effects of the real exchange rate on employment are usually marginally significant, and often of the opposite sign than expected.



### 2.1.2 Regressions

The central empirical question of the present study is how cross-country differences in job security regulation affect the speed of adjustment. Accordingly, from (1) and (9) it follows that the basic equation we estimate is:

$$\Delta e_{jct} = \lambda_{ct}(\text{Gap}_{jct} + \delta_{ct}), \quad (10)$$

where  $\Delta e_{jct}$  is the log change in employment and  $\lambda_{ct}$  denotes the speed of adjustment.

We assume that the latter takes the form:

$$\lambda_{ct} = \tilde{\lambda}_1 + \tilde{\lambda}_2 \text{JS}_{ct}^{\text{eff}}, \quad (11)$$

where  $\text{JS}_{ct}^{\text{eff}}$  is a measure of *effective* job security regulation. In practice we observe job security regulation (imperfectly), but not the rigor with which it is enforced. We proxy the latter with a “rule of law” variable, so that

$$\text{JS}_{ct}^{\text{eff}} = a\text{JS}_{ct} + b(\text{JS}_{ct} \times \text{RL}_{ct}), \quad (12)$$

where  $a$  and  $b$  are constants and  $\text{RL}_{ct}$  is a standard measure of rule of law (see below). When  $b = 0$  there is no difference between *de jure* and *de facto* regulation. Substituting this expression in (11) and the resulting expression for  $\lambda_{ct}$  in (10), yields our main estimating equation:

$$\Delta e_{jct} = \lambda_1 \text{Gap}_{jct} + \lambda_2 (\text{Gap}_{jct} \times \text{JS}_{ct}) + \lambda_3 (\text{Gap}_{jct} \times \text{JS}_{ct} \times \text{RL}_{ct}) + \tilde{\delta}_{ct} + \varepsilon_{jct}, \quad (13)$$

with  $\lambda_1 = \tilde{\lambda}_1$ ,  $\lambda_2 = a\tilde{\lambda}_2$ ,  $\lambda_3 = b\tilde{\lambda}_2$ , and  $\tilde{\delta}_{ct}$  denotes country  $\times$  time fixed effects (proportional to the  $\delta_{ct}$  defined above).

The main coefficients of interest are  $\lambda_2$  and  $\lambda_3$ , which measure how the speed of adjustment varies across countries depending on their labor market regulation (both *de jure* and *de facto*).

## 2.2 The Data

This section describes our sample and main variables. Additional variables are defined as we introduce them later in the text.

### 2.2.1 Job Security and Rule of Law

We use two measures of job security, or legal protection against dismissal: the job security index constructed by Botero et al. (2004) for 60 countries world-wide (henceforth  $\text{JS}_c$ ) and the job security index constructed by Heckman and Pages (2000) for 24 countries in OECD and Latin America (henceforth  $\text{HP}_{ct}$ ). The  $\text{JS}_c$  measure is available for a larger sample of countries and includes a broader range of job security variables. The  $\text{HP}_{ct}$  measure has the advantage of having time variation.

Our main job security index,  $\text{JS}_c$ , is the sum of four variables, measured in 1997, each of which takes

on values between 0 and 1: (i) grounds for dismissal protection  $PG_c$ , (ii) protection regarding dismissal procedures  $PP_c$ , (iii) notice and severance payments  $PS_c$ , and (iv) protection of employment in the constitution  $PC_c$ . The rules on grounds of dismissal range from allowing the employment relation to be terminated by either party at any time (employment at will) to allowing the termination of contracts only under a very narrow list of “fair” causes. Protective dismissal procedures require employers to obtain the authorization of third parties (such as unions and judges) before terminating the employment contract. The third variable, notice and severance payment, is the one closest to the  $HP_{ct}$  measure, and is the normalized sum of two components: mandatory severance payments after 20 years of employment (in months) and months of advance notice for dismissals after 20 years of employment ( $NS_{tc} = b_{ct+20} + SP_{ct+20}$ ,  $t = 1997$ ). The four components of  $JS_c$  described above increase with the level of job security.

The Heckman and Pages measure is narrower, including only those provisions that have a direct impact on the costs of dismissal. To quantify the effects of this legislation, they construct an index that computes the expected (at hiring) cost of a future dismissal. The index includes both the costs of advanced notice legislation and firing costs, and is measured in units of monthly wages.

Our estimations also adjust for the level of enforcement of labor legislation. We do this by including measures of rule of law  $RL_c$  and government efficiency  $GE_c$  from Kaufmann et al. (1999), and interact them with  $JS_c$  and  $HP_{ct}$ .<sup>14</sup> We expect labor market legislation to have a larger impact on adjustment costs in countries with a stronger rule of law (higher  $RL_c$ ) and more efficient governments (higher  $GE_c$ ).

The institutional variables as well as the countries in our sample and their corresponding income group are reported in Table 2. Table 3 reports the sample correlations between our main cross-country variables and summary statistics for each of these measures for three income groups (based on World Bank per capita income categories).<sup>15</sup> As expected, the correlation between the two measures of job security is positive and significant. Differences can be explained mainly by the broader scope of the  $JS_{ct}$  index. Also as expected, rule of law and government efficiency increase with income levels. Note, however, that neither measure of job security is positively correlated with income per capita, since both  $JS_{ct}$  and  $HP_c$  are highest for middle income countries.

### 2.2.2 Industrial Statistics

Our output, employment and wage data come from the 2002 3-digit UNIDO Industrial Statistics Database. The UNIDO database contains data for the period 1963-2000 for the 28 manufacturing sectors that correspond to the 3 digit ISIC code (revision 2). Because our measures of job security and rule of law are time invariant and measured in recent years, however, we restrict our sample to the period 1980-2000. Data on output and labor compensation are in current US dollars (inflation is removed through time effects in our regressions). Throughout the paper our main dependent variable is  $\Delta e_{jct}$ , the log change in total employment

<sup>14</sup>For rule of law and government efficiency we use the earliest value available in the Kaufmann et al. (1999) database: 1996, since this is closest to the Botero et al. (2004) measure, which is for 1997.

<sup>15</sup>Income groups are: 1=High Income OECD, 2=High Income Non OECD and Upper Middle Income, 3=Lower Middle Income and Low Income.

Table 2: SAMPLE COVERAGE AND MAIN VARIABLES

WDI code	Inc Group	Job Security		Institutions			
		Botero et al	HP	Strong RL	Rule of Law	Gov. Eff.	High Gov. Eff
AUS	1	-0.19	-0.71	1	1.03	0.95	1
AUT	1	-0.15	-0.65	1	1.13	0.92	1
BEL	1	-0.11	-0.70	1	0.81	0.81	1
CAN	1	-0.16	-1.64	1	1.02	0.92	1
DEU	1	0.17	-1.56	1	1.04	0.92	1
DNK	1	-0.21		1	1.17	1.02	1
ESP	1	0.17	1.29	1	0.41	0.64	1
FIN	1	0.24	-0.82	1	1.22	0.89	1
FRA	1	-0.02	-1.09	1	0.81	0.78	1
GBR	1	-0.13	-1.00	1	1.09	1.05	1
GRC	1	-0.04	-1.05	1	-0.01	-0.06	1
IRL	1	-0.21	-1.40	1	0.92	0.82	1
ITA	1	-0.09	0.79	1	0.09	0.05	1
JPN	1	-0.14	-1.84	1	0.76	0.46	1
NLD	1	0.04	-1.53	1	1.09	1.25	1
NOR	1	-0.03	-1.55	1	1.23	1.13	1
NZL	1	-0.29	-2.21	1	1.22	1.25	1
PRT	1	0.37	2.05	1	0.53	0.24	1
SWE	1	0.06	-0.50	1	1.17	0.97	1
USA	1	-0.25	-2.43	1	0.95	1.01	1
ARG	2	0.11	0.56	0	-0.48	-0.37	0
BRA	2	0.36	0.61	0	-1.00	-0.82	0
CHL	2	-0.02	0.21	1	0.44	0.32	1
HKG	2	-0.32		1	0.86	0.81	1
ISR	2	-0.17		1	0.36	0.42	1
KOR	2	-0.07	1.14	1	0.02	-0.15	0
MEX	2	0.38	0.73	0	-0.86	-0.85	0
MYS	2	-0.24		1	0.05	0.18	1
PAN	2	0.34	1.37	0	-0.50	-1.19	0
SGP	2	-0.22		1	1.26	1.41	1
TUR	2	-0.13	1.54	0	-0.73	-0.69	0
TWN	2	0.01		1	0.21	0.49	1
URY	2	-0.30	-0.20	0	-0.26	-0.17	0
VEN	2	0.31	4.29	0	-1.38	-1.32	0
ZAF	2	-0.17		0	-0.42	-0.40	0
BFA	3	-0.10		0	-1.46	-1.38	0
BOL	3	0.24	2.32	0	-1.37	-1.12	0
COL	3	0.29	1.17	0	-1.19	-0.61	0
ECU	3	0.34	0.97	0	-1.13	-1.29	0
EGY	3	0.13		0	-0.53	-0.99	0
GHA	3	-0.17		0	-0.86	-0.78	0
IDN	3	0.10		0	-1.09	-0.55	0
IND	3	-0.14		0	-0.77	-0.79	0
JAM	3	-0.20	-0.44	0	-0.95	-1.06	0
JOR	3	0.22		0	-0.56	-0.54	0
KEN	3	-0.16		0	-1.48	-1.13	0
LKA	3	0.09		0	-0.48	-0.93	0
MAR	3	-0.22		0	-0.57	-0.73	0
MDG	3	0.23		0	-1.55	-1.39	0
MOZ	3	0.38		0	-1.92	-1.23	0
MWI	3	0.11		0	-0.94	-1.32	0
NGA	3	-0.07		0	-1.89	-1.68	0
PAK	3	-0.15		0	-1.16	-1.02	0
PER	3	0.37	2.25	0	-1.08	-0.87	0
PHL	3	0.24		0	-0.86	-0.54	0
SEN	3	-0.04		0	-0.92	-1.04	0
THA	3	0.10		0	-0.29	-0.32	0
TUN	3	0.05		0	-0.69	-0.24	0
ZMB	3	-0.33		0	-1.08	-1.44	0
ZWE	3	-0.13		0	-0.97	-0.86	0

Table 3: BASELINE SAMPLE STATISTICS\*

<i>Employment Growth (Yearly Avge.): 1980-2000</i>					
Inc. Group	Obs.	Mean	SD	Min	Max
1	8,607	-0.01	0.06	-0.24	0.26
2	6,063	0.00	0.11	-0.43	0.42
3	7,063	0.02	0.16	-0.78	0.96
Total	21,733	0.00	0.11	-0.78	0.96

<i>Job Security from Botero et al. (2004): JS</i>					
Inc. Group	Countries	Mean	SD	Min	Max
1	20	-0.05	0.18	-0.29	0.37
2	15	-0.01	0.25	-0.32	0.38
3	25	0.05	0.21	-0.33	0.38
Total	60	0.00	0.21	-0.33	0.38

<i>Job Security from Heckman and Pages (2001): HP</i>					
Inc. Group	Countries	Mean	SD	Min	Max
1	19	-0.87	1.15	-2.43	2.05
2	9	1.14	1.30	-0.20	4.29
3	5	1.26	1.13	-0.44	2.32
Total	33	0.00	1.54	-2.43	4.29

<i>Rule of Law from Kaufmann et al. (1999): RL</i>					
Inc. Group	Countries	Mean	SD	Min	Max
1	20	0.88	0.37	-0.01	1.23
2	15	-0.16	0.72	-1.38	1.26
3	25	-1.03	0.42	-1.92	-0.29
Total	60	-0.18	0.96	-1.92	1.26

<i>Government Effectiveness from Kaufmann et al. (1999): GE</i>					
Inc. Group	Countries	Mean	SD	Min	Max
1	20	0.80	0.37	-0.06	1.25
2	15	-0.16	0.76	-1.32	1.41
3	25	-0.95	0.36	-1.68	-0.24
Total	60	-0.17	0.90	-1.68	1.41

<i>Correlation Country Means</i>					
	JS	HP	RL	GE	
JS	1.00				
HP	0.66	1.00			
RL	-0.36	-0.77	1.00		
GE	-0.35	-0.77	0.97	1.00	

\*Income groups are: 1=High Income OECD, 2=High Income Non OECD and Upper Middle Income, 3=Lower Middle Income and Low Income.

in sector  $j$  of country  $c$  in period  $t$ .

A large number of countries are included in the original dataset — however our sample is constrained by the cross-country availability of the independent variables measuring job security. In addition, we drop two percent of extreme employment changes in each of the three income groups. For our main specification the resulting sample includes 60 economies. Table 3 shows descriptive statistics for the dependent variable by income group.

### 3 Results

This section presents our main result, showing that effective job security has a significant negative effect on the speed of adjustment of employment to shocks in the employment-gap. It also presents several robustness exercises.

#### 3.1 Main results

Recall that our main estimating equation is:

$$\Delta e_{jct} = \lambda_1 \text{Gap}_{jct} + \lambda_2 (\text{Gap}_{jct} \times \text{JS}_c) + \lambda_3 (\text{Gap}_{jct} \times \text{JS}_c \times \text{RL}_c) + \tilde{\delta}_{ct} + \varepsilon_{jct}. \quad (14)$$

Note that we have dropped time subscripts from  $\text{JS}_c$  and  $\text{RL}_c$  as we only use time invariant measures of rule of law and job security in our baseline estimation. Note also that in all specifications that include the  $(\text{Gap}_{jct} \times \text{JS}_c \times \text{RL}_c)$  interaction we also include the respective  $\text{Gap}_{jct} \times \text{RL}_c$  as a control variable.

We start by ignoring the effect of job security on the speed of adjustment, and set  $\lambda_2$  and  $\lambda_3$  equal to zero. This gives us an estimate of the average speed of adjustment and is reported in column 1 of Table 4. On average (across countries and periods) we find that 60% of the employment-gap is closed in each period. Furthermore, our measure of the employment-gap and country  $\times$  year fixed effects explain 60% of the variance in log-employment growth.

The next three columns present our main results, which are repeated in columns 5 to 7 allowing for different  $\lambda_1$  by sectors and country income level.<sup>16</sup> Column 2 (and 5) presents our estimate of  $\lambda_2$ . This coefficient has the right sign and is significant at conventional confidence levels. Employment adjusts more slowly to shocks in the employment-gap in countries with higher levels of official job security.

Next, we allow for a distinction between effective and official job security. Results are reported in columns 3 and 4 (and, correspondingly, 6 and 7) for different rules-enforcement criteria. In columns 3 and 6 the distinction between effective and official job security is captured by the product of  $\text{JS}_c$  and  $\text{DSRL}_c$ , where  $\text{DSRL}_c$  is a dummy variable for countries with strong rule of law ( $\text{RL}_c \geq \text{RL}_{\text{Greece}}$  — where Greece is the OECD country with the lowest RL score). The three panels in Figure 1 show the value of the job

<sup>16</sup>We allow for an interaction between  $\text{Gap}_{jct}$  and 3 digit ISIC sector dummies (we also include sector fixed effects). We also control for the possibility that our results are driven by omitted variables, correlated with our measures of job security. For this, we include an additional interaction between  $\text{Gap}_{jct}$  and three income-group dummies.

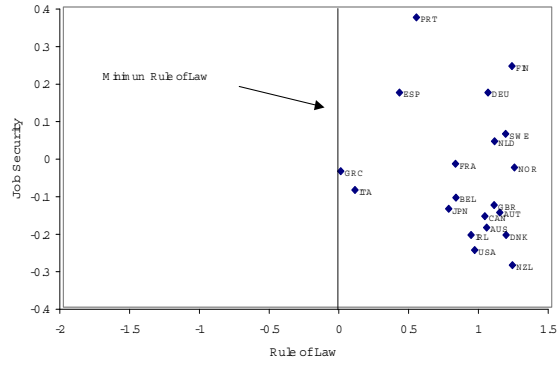
Table 4: ESTIMATION RESULTS

	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
	Change in Log-Employment							
Gap ( $\lambda_1$ )	0.600 (0.009)***	0.603 (0.008)***	0.607 (0.012)***	0.611 (0.012)***				
Gap×JS ( $\lambda_2$ ):		-0.080 (0.037)**	-0.015 (0.051)	-0.025 (0.051)	-0.126 (0.041)***	-0.027 (0.052)	-0.038 (0.051)	
Gap×JS×DSRL ( $\lambda_3$ )			-0.514 (0.068)***			-0.314 (0.070)***		
Gap×JS×DHGE ( $\lambda_3$ )				-0.515 (0.068)***			-0.326 (0.071)***	
Gap×HP ( $\lambda_2$ )								-0.022 (0.007)***
<i>Controls</i>								
Gap×DSRL			-0.076 (0.015)***			0.086 (0.023)***		
Gap×DHGE				-0.091 (0.015)***			0.045 (0.023)*	
Observations	21,733	21,733	21,733	21,733	21,733	21,733	21,733	12,012
R-squared	0.60	0.60	0.60	0.60	0.61	0.61	0.61	0.62
Gap-Income Interaction	No	No	No	No	Yes	Yes	Yes	Yes
Gap-Sector Interaction	No	No	No	No	Yes	Yes	Yes	Yes

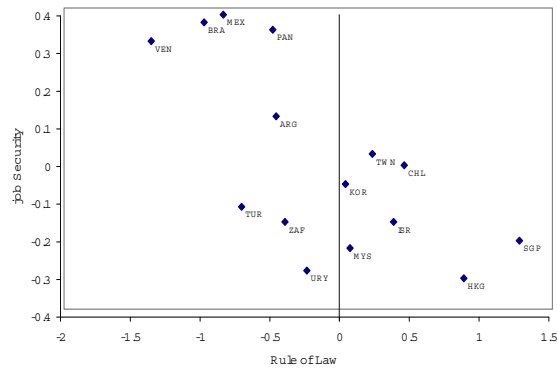
\* significant at 10%; \*\* significant at 5%; \*\*\* significant at 1%. Robust standard errors in parentheses. JS and HP stand for the Botero et al. (2004) and Heckman and Pages (2000) job security measures, respectively. DSRL and DHGE stand for strong Rule of Law and high Government Efficiency dummies (in both cases the threshold is given by Greece, see the main text), respectively, using the Kaufmann et al. (1999) indices. Each regression has country-year fixed effects. Gaps are estimated using a constant  $\phi = 0.40$ . Sample excludes the upper and lower 1% of  $\Delta e$  and of the estimated values of Gap.

Figure 1: Job Security and Rule of Law in Countries with High, Medium and Low Income

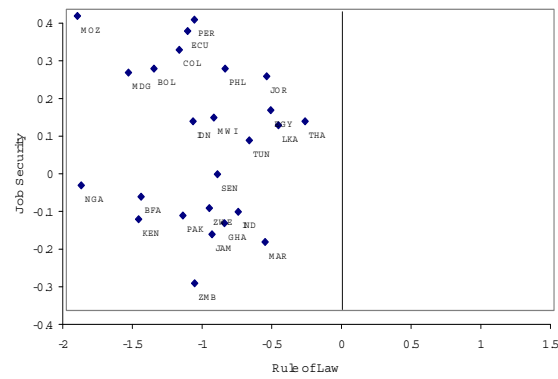
High Income Countries



Middle Income Countries



Low Income Countries



security index for countries in the high, medium and low income groups, respectively. Now  $\lambda_2$  becomes insignificant, while  $\lambda_3$  has the right sign and is highly significant. That is, the same change in  $JS_c$  will have a significantly larger (downward) effect on the speed of adjustment in countries with stricter enforcement of laws, as measured by our rule-of-law dummy. The effect of the estimated coefficients reported in column 3 is large. In countries with strong rule of law, moving from the 20th percentile of job security ( $-0.19$ ) to the 80th percentile ( $0.23$ ) reduces  $\hat{\lambda}$  by  $0.22$ . The same change in job security legislation has a considerable smaller effect,  $0.006$ , on the speed of adjustment in the group of economies with weak rule of law. That is, employment adjusts more slowly to shocks in the employment-gap in countries with higher levels of effective job security.

Columns 4 and 7 address whether the negative coefficient on  $\lambda_3$  is robust to other measures of legal enforcement. To do so we use an alternative variable from the Kaufmann et al. (1999) dataset – government effectiveness (GE) – and construct a dummy variable for high effectiveness countries ( $GE_c \geq GE_{Greece}$ ). Clearly, the results are very close to those reported in columns 3 and 7. Job security legislation has a significant negative effect on the estimated speed of adjustment when governments are effective – a proxy for enforcement of existing labor regulation.

Finally, the last column in Table 4 uses an alternative measure of job security. We repeat our specification from column 7 (including sector and income dummies) using the Heckman-Pages (2000) measure of job security. The  $HP_{ct}$  data are only available for countries in the OECD and Latin America so our sample size is reduced by half, and most low income countries are dropped. The flip side is that this measure is time varying which potentially allows us to capture the effects of changes in the job security regulation. As reported in column 8, we find a negative and significant effect of  $HP_{ct}$  on the speed of adjustment.

## 3.2 Further robustness

We continue our robustness exploration by assessing the impact of three broad econometric issues: alternative gap-measures, exclusion of potential (country) outliers, and misspecification due to endogeneity of the gap measure.

### 3.2.1 Alternative gap-measures

Table 4 suggests that conditional on our measure of the employment-gap, our main findings are robust: job security, when enforced, has a significant negative impact on the speed of adjustment to the employment-gap. Table 5 tests the robustness of this result to alternative measures of the employment-gap. Columns 1 and 2 relax the assumption of a  $\phi$  common across all countries. They repeat our baseline specifications—columns 2 and 3 in Table 4—using the values of  $\phi$  estimated per income-group reported in Table 1. In turn, columns 3 and 4 report the results of using values of  $\phi$  estimated across countries grouped by level of job security. Countries are grouped into the upper, middle and lower thirds of job security. Next, columns 5 through 8 repeat our baseline specifications using a three and four period moving average to estimate  $\hat{\theta}_{jct}$ . The final two columns (9 and 10) use an alternative specification for  $w_{jct}^o$  based on average wages instead



of average productivity (see equation 9) to build  $\text{Gap}_{jct}$ . In all of the specifications reported in Table 5, our results remain qualitatively the same as in Table 4.

### 3.2.2 Exclusion of potential (country) outliers

Table 6 reports estimates of  $\lambda_2$  and  $\lambda_3$  using the specification from column 3 in Table 4 but dropping one country from our sample at a time. In all cases the estimated coefficient on  $\lambda_3$  is negative and significant at conventional confidence intervals.

However, it is also apparent in this table that excluding either Hong Kong or Kenya makes a substantial difference in the point estimates. For this reason, we re-estimate our model from scratch (that is, from  $\phi$  up) now excluding these two countries. In this case the value of  $\phi$  rises from 0.40 to 0.42. Qualitatively, however, the main results remain unchanged. Table 7 reports these results.

### 3.2.3 Potential endogeneity of the gap measure

One concern with our procedure is that the construction of the gap measure includes the change in employment. While this does not represent a problem under the null hypothesis of the model, any measurement error in employment and  $\phi z_{jt}$  could introduce important biases. We address this issue with two procedures.

The first procedure maintains our baseline specification, but instruments for the contemporaneous gap measure. Given that  $\text{Gap}_{jct} = \phi z_{jt} + \Delta e_{jct}$  can be rewritten as  $\phi z_{j,t-1} + \Delta e_{jct}^*$ , a natural instrument is the lag of the ex-post gap,  $\phi z_{jct,t-1}$ . Unfortunately, the latter is not a valid instrument if it is computed with measurement error and this error is serially correlated. In our specification this could be the case because we use a moving average to construct the estimate of relative sectoral productivity,  $\hat{\theta}_{jct}$ . To avoid this problem, we construct an alternative measure of the ex-post gap letting wage data play the role of productivity data when calculating the  $v$  and  $\theta$  terms on the right hand side of (9).

The second procedure re-writes the model in a standard dynamic panel formulation that removes the contemporaneous employment change from the right hand side:<sup>17</sup>

$$\Delta \text{Gap}_{jct} = (1 - \lambda_c) \Delta \text{Gap}_{jct-1} + \varepsilon_{jct}. \quad (15)$$

Table 8 reports the values of the average  $\lambda$  estimated with these two alternative procedures (note the significant decline in the precision of the estimates). For comparison purposes, the first row reproduces the first column in Table 4. The second row shows the result for the IV procedure based on using lagged changes in wages as instruments. Finally, Row 3 reports the estimate from the dynamic panel. It is apparent from the table that the estimates of average  $\lambda$  are in the right ballpark, and hence we conclude that the bias due to a potentially endogenous gap is not significant.

<sup>17</sup>To estimate this equation we follow Anderson and Hsiao (1982) and use twice and three-times lagged values of  $\Delta \text{Gap}_{jct}$  as instruments for the RHS variable. Similar results are obtained if we follow Arellano and Bond (1991).

Table 5: ROBUSTNESS OF MAIN RESULTS TO ALTERNATIVE SPECIFICATIONS

	$\phi$ varies across income groups (1)	$\phi$ varies across job security groups (3)	$\phi = MA(3)$ (4)	$\theta = MA(3)$ (5)	$\theta = MA(4)$ (6)	$\theta = MA(4)$ (7)	$\theta = MA(4)$ (8)	$\theta = MA(4)$ (9)	$\theta = MA(4)$ (10)
Change in Log-Employment									
Gap	0.568 (0.009)***	0.574 (0.008)***		0.564 (0.008)***		0.529 (0.008)***		0.590 (0.009)***	
Gap×JS	-0.094 (0.038)***	-0.027 (0.037)	0.046 (0.051)	-0.069 (0.037)*	-0.008 (0.050)	-0.009 (0.036)	0.063 (0.050)	-0.108 (0.038)***	-0.135 (0.050)***
Gap×DSRL	-0.051 (0.015)***		-0.071 (0.015)***		-0.085 (0.015)***		-0.082 (0.015)***		-0.106 (0.016)***
Gap×JS×DSRL	-0.501 (0.069)***		-0.532 (0.069)***		-0.515 (0.068)***		-0.538 (0.068)***		-0.258 (0.071)***
Observations	21,733	21,733		20,902		20,219		20,439	
R-squared	0.58	0.58	0.58	0.59	0.59	0.58	0.58	0.60	0.60
Gap-Sector Int.	No	No	Yes	No	Yes	No	Yes	No	Yes

\* significant at 10%; \*\* significant at 5%; \*\*\* significant at 1%. Robust standard errors in parentheses. JS stands for the Botero et al. (2004) job security measure. DSRL stands for high (above Greece, see main text) Rule of Law using the Kaufmann et al. (1999) measure. Columns (1), (2), (3) and (4) use values of  $\phi$  estimated in Table 1. Samples exclude the upper and lower 1% of  $\Delta e$  and of the estimated values of Gap.

Table 6: EXCLUDING ONE COUNTRY AT A TIME

Country	$\lambda_2$		$\lambda_3$		Country	$\lambda_2$		$\lambda_3$	
	Coeff.	St. Dev.	Coeff.	St. Dev.		Coeff.	St. Dev.	Coeff.	St. Dev.
ARG	-0.01	0.05	-0.51	0.07	KOR	-0.02	0.05	-0.52	0.07
AUS	-0.02	0.05	-0.52	0.07	LKA	-0.02	0.05	-0.51	0.07
AUT	-0.02	0.05	-0.52	0.07	MAR	-0.02	0.05	-0.51	0.07
BEL	-0.02	0.05	-0.52	0.07	MDG	-0.02	0.05	-0.51	0.07
BFA	-0.03	0.05	-0.50	0.07	MEX	0.00	0.05	-0.53	0.07
BOL	0.00	0.05	-0.52	0.07	MOZ	0.02	0.05	-0.55	0.07
BRA	-0.01	0.05	-0.52	0.07	MWI	-0.01	0.05	-0.52	0.07
CAN	-0.02	0.05	-0.52	0.07	NYS	-0.02	0.05	-0.46	0.07
CHL	-0.02	0.05	-0.53	0.07	NGA	0.00	0.05	-0.53	0.07
COL	-0.02	0.05	-0.51	0.07	NLD	-0.02	0.05	-0.51	0.07
DEU	-0.02	0.05	-0.52	0.07	NOR	-0.02	0.05	-0.51	0.07
DNK	-0.02	0.05	-0.52	0.07	NZL	-0.02	0.05	-0.53	0.07
ECU	-0.03	0.05	-0.50	0.07	PAK	0.02	0.05	-0.55	0.07
EGY	-0.02	0.05	-0.51	0.07	PAN	-0.01	0.05	-0.52	0.07
ESP	-0.02	0.05	-0.53	0.07	PER	0.06	0.05	-0.59	0.07
FIN	-0.02	0.05	-0.54	0.07	PHL	-0.03	0.05	-0.50	0.07
FRA	-0.02	0.05	-0.51	0.07	PRT	-0.02	0.05	-0.54	0.07
GBR	-0.02	0.05	-0.51	0.07	SEN	0.00	0.05	-0.53	0.07
GHA	-0.05	0.05	-0.48	0.07	SGP	-0.02	0.05	-0.52	0.07
GRC	-0.02	0.05	-0.51	0.07	SWE	-0.02	0.05	-0.53	0.07
HKG	-0.02	0.05	-0.37	0.07	THA	-0.01	0.05	-0.51	0.07
IDN	-0.02	0.05	-0.51	0.07	TUN	-0.02	0.05	-0.51	0.07
IND	0.01	0.05	-0.54	0.07	TUR	-0.03	0.05	-0.50	0.07
IRL	-0.02	0.05	-0.54	0.07	TWN	-0.02	0.05	-0.49	0.07
ISR	-0.02	0.05	-0.52	0.07	URY	-0.02	0.05	-0.50	0.07
ITA	-0.02	0.05	-0.51	0.07	USA	-0.02	0.05	-0.53	0.07
JAM	-0.02	0.05	-0.51	0.07	VEN	0.00	0.05	-0.53	0.07
JOR	-0.04	0.05	-0.49	0.07	ZAF	-0.02	0.05	-0.51	0.07
JPN	-0.02	0.05	-0.52	0.07	ZMB	-0.02	0.05	-0.51	0.07
KEN	-0.15	0.05	-0.38	0.07	ZWE	0.03	0.05	-0.55	0.07

This table reports the estimated coefficients for  $\lambda_2$  and  $\lambda_3$ , for the specification in Column 3 of Table 4, leaving out one country (the one indicated for each set of coefficients) at a time.

Table 7: ESTIMATION RESULTS EXCLUDING HONG KONG AND KENYA

	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
	Change in Log-Employment							
Gap ( $\lambda_1$ )	0.615 (0.009)***	0.620 (0.009)***	0.649 (0.012)***	0.652 (0.012)***				
Gap×JS ( $\lambda_2$ ):		-0.105 (0.039)***	-0.156 (0.051)***	-0.163 (0.051)***	-0.204 (0.042)***	-0.171 (0.052)***	-0.183 (0.052)***	
Gap×JS×DSRL ( $\lambda_3$ )			-0.231 (0.062)***			-0.062 (0.072)		
Gap×JS×DHGE ( $\lambda_3$ )				-0.227 (0.070)***			-0.071 (0.072)	
Gap×HP ( $\lambda_2$ )								-0.021 (0.007)***
<i>Controls</i>								
Gap×DSRL			-0.121 (0.015)***			0.065 (0.023)***		
Gap×DHGE				-0.136 (0.015)***			0.023 (0.024)	
Observations	20,881	20,881	20,881	20,881	20,881	20,881	20,881	12,003
R-squared	0.61	0.61	0.61	0.61	0.62	0.62	0.62	0.62
Gap-Income Interaction	No	No	No	No	Yes	Yes	Yes	Yes
Gap-Sector Interaction	No	No	No	No	Yes	Yes	Yes	Yes

\* significant at 10%; \*\* significant at 5%; \*\*\* significant at 1%. Robust standard errors in parentheses. JS and HP stand for the Botero et al. (2004) and Heckman and Pages (2000) job security measures, respectively. DSRL and DHGE stand for high (above Greece, see main text) Rule of Law and Government Efficiency dummies, respectively, using the Kaufmann et al. (1999) indices. Each regression has country-year fixed effects. Gaps are estimated using a constant  $\phi = 0.42$ . Sample excludes the upper and lower 1% of  $\Delta e$  and of the estimated values of Gap.

Table 8: IV ESTIMATION

Estimation Method	Average speed of adjustment	
	Point Estimate	Robust Standard Error
Baseline Model (Column 1 in Table 4)	0.600	0.009
Gap instrumented with wage data	0.570	0.065
Standard dynamic panel formulation	0.543	0.078

Finally, we note that the standard solution of passing the  $\Delta e$ -component of the gap defined in (9) to the left hand side of the estimating equation (10) does not work in our context. Passing  $\Delta e$  to the left suggests that the coefficient on the resulting gap will be equal to  $\lambda/(1-\lambda)$ . This holds only in the case of a partial adjustment model. By contrast, when Calvo-type adjustments are also present, the corresponding coefficient will, on average, be negative.<sup>18</sup> More important, even small departures from a partial adjustment model introduce significant biases when estimating  $\lambda$  using this approach.<sup>19</sup>

## 4 Gauging the Costs of Effective Labor Protection

By impairing worker movements from less to more productive units, effective labor protection reduces aggregate output and slows down economic growth. In this section we develop a simple framework to quantify this effect. Any such exercise requires strong assumptions and our approach is no exception. Nonetheless, our findings suggest that the costs of the microeconomic inflexibility caused by effective protection is large. In countries with strong rule of law, moving from the 20th to the 80th percentile of job security lowers annual productivity growth by close to one percentage point. The same movement for countries with weak rule of law has a negligible impact on TFP.<sup>20</sup>

Consider a continuum of establishments, indexed by  $i$ , that adjust labor in response to productivity shocks, while their share of the economy's capital remains fixed over time. Their production functions exhibit constant returns to (aggregate) capital,  $K_t$ , and decreasing returns to labor:

$$Y_{it} = B_{it}K_tL_{it}^\alpha, \quad (16)$$

where  $B_{it}$  denotes plant-level productivity and  $0 < \alpha < 1$ . The  $B_{it}$ 's follow geometric random walks, that can be decomposed into the product of a common and an idiosyncratic component:

$$\Delta \log B_{it} \equiv b_{it} = v_t + v_{it}^I,$$

where the  $v_t$  are i.i.d.  $\mathcal{N}(\mu_A, \sigma_A^2)$  and the  $v_{it}^I$ 's are i.i.d. (across productive units, over time and with respect to the aggregate shocks)  $\mathcal{N}(0, \sigma_I^2)$ . We set  $\mu_A = 0$ , since we are interested in the interaction between rigidities and idiosyncratic shocks, not in Jensen-inequality-type effects associated with aggregate shocks.

The price-elasticity of demand is  $\eta > 1$ . Aggregate labor is assumed constant and set equal to one. We define *aggregate productivity*,  $A_t$ , as:

$$A_t = \int B_{it}L_{it}^\alpha di, \quad (17)$$

---

<sup>18</sup>In the Calvo-case, for every observation either the (modified) gap or the change in employment is zero. The former happens when adjustment takes place, the latter when it does not. It follows that the covariance of  $\Delta e$  and the (modified) gap will be equal to minus the product of the mean of both variables. Since these means have the same sign, the estimated coefficient will be negative.

<sup>19</sup>See Caballero, Cowan, Engel and Micco (2004) for a formal derivation.

<sup>20</sup>Of course, a weak rule of law has an adverse impact on productivity through various channels not considered in this paper.

so that aggregate output,  $Y_t \equiv \int Y_{it} di$ , satisfies

$$Y_t = A_t K_t.$$

Units adjust with probability  $\lambda_c$  in every period, independent of their history and of what other units do that period.<sup>21</sup> The parameter that captures microeconomic flexibility is  $\lambda_c$ . Higher values of  $\lambda_c$  are associated with a faster reallocation of workers in response to productivity shocks.

Standard calculations show that the growth rate of output,  $g_Y$ , satisfies:

$$g_Y = sA - \delta, \tag{18}$$

where  $s$  denotes the savings rate (assumed exogenous) and  $\delta$  the depreciation rate for capital.

Now compare two economies that differ only in their degree of microeconomic flexibility,  $\lambda_{c,1} < \lambda_{c,2}$ . Tedious but straightforward calculations relegated to Appendix C show that:

$$g_{Y,2} - g_{Y,1} \cong (g_{Y,1} + \delta) \left[ \frac{1}{\lambda_{c,1}} - \frac{1}{\lambda_{c,2}} \right] \xi, \tag{19}$$

with

$$\xi = \frac{\alpha\gamma(2 - \alpha\gamma)}{2(1 - \alpha\gamma)^2} \sigma^2,$$

where we recall that  $\gamma = (\eta - 1)/\eta$ , and  $\sigma^2 = \sigma_I^2 + \sigma_A^2$ .<sup>22</sup>

We choose parameters to apply (19) as follows: The mark-up is set at 20% (so that  $\gamma = 5/6$ ),  $g_{Y,1}$  to the average rate of growth per worker in our sample for the 1980-1990 period, 0.7%,  $\sigma = 27\%$ ,<sup>23</sup>  $\alpha = 2/3$ , and  $\delta = 6\%$ .

Table 9 reports the annual productivity costs of 20 percentile changes in job security regulation. These numbers are large. They imply that moving from the 20th to the 80th percentile in job security, in countries with strong rule of law, reduces annual productivity growth by 0.85%. The same change in job security legislation has a much smaller effect on TFP growth, 0.02%, in the group of economies with weak rule of law.

We are fully aware of the many caveats that such ceteris-paribus comparison can raise, as well as to the impact of the linear aggregate technology assumption on the growth versus levels claim, but the point of the table is simply to provide an alternative metric of the potential significance of observed levels of effective

<sup>21</sup>More precisely, whether unit  $i$  adjusts at time  $t$  is determined by a Bernoulli random variable  $\xi_{it}$  with probability of success  $\lambda_c$ , where the  $\xi_{it}$ 's are independent across units and over time. This corresponds to the case  $\zeta = 1$  in Section 2.1.

<sup>22</sup>There also is a (static) jump in the level of aggregate productivity when  $\lambda$  increases, given by:

$$\frac{A_2 - A_1}{A_1} \cong \left[ \frac{1}{\lambda_1} - \frac{1}{\lambda_2} \right] \xi.$$

See Appendix C for the proof.

<sup>23</sup>This is the average across the five countries considered in Caballero et al. (2004).

Table 9: PRODUCTIVITY GROWTH AND JOB SECURITY

Change in Job Security Index	Cost in Annual Growth Rate	
	Weak Rule of Law	Strong Rule of Law
20th to 40th percentile	0.002%	0.083%
40th to 60th percentile	0.007%	0.292%
60th to 80th percentile	0.008%	0.478%

Reported: change in annual productivity growth rates associated with moving across percentiles in the distribution of country job security measures computed in Botero et al. (2004). Lower values of job security index correspond to less job security. Values of speed of adjustment calculated using Column 3 in Table (4). The threshold for weak and strong rule of law is given by the OECD country with the lowest Rule of Law score (Greece). Changes in annual productivity growth calculated based on (19). Parameter values used:  $\gamma = 5/6$ ,  $g_{Y,1} = 0.007$ ,  $\sigma = 0.27$ ,  $\alpha = 2/3$ , and  $\delta = 0.06$ .

labor protection.

## 5 Concluding Remarks

Many papers have shown that, in theory, job security regulation depresses firm level hiring and firing decisions. Job security provisions increase the cost of reducing employment and therefore lead to fewer dismissals when firms are faced with negative shocks. Conversely, when faced with a positive shock, the optimal employment response takes into account the fact that workers may have to be fired in the future, and the employment response is smaller. The overall effect is a reduction of the speed of adjustment to shocks.

However, conclusive empirical evidence on the effects of job security regulation has been elusive. One important reason for this deficit has been the lack of information on employment regulation for a sufficiently large number of economies that can be integrated to cross sectional data on employment outcomes. In this paper we have developed a simple empirical methodology that has allowed us to fill some of the empirical gap by exploiting: (a) the recent publication of two cross-country surveys on employment regulations (Heckman and Pages (2000) and Botero et al. (2004)) and, (b) the homogeneous data on employment and production available in the UNIDO dataset. Another important reason for the lack of empirical success is differences in the degree of regulation enforcement across countries. We address this problem by interacting the measures of employment regulation with different proxies for law-enforcement.

Using a dynamic labor demand specification we estimate the effects of job security across a sample of 60 countries for the period from 1980 to 1998. We consistently find a relatively lower speed of adjustment of employment in countries with high legal protection against dismissal, especially when such protection is likely to be enforced.

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# APPENDIX

## A Representative firm's frictionless problem

**Proposition 1** *A firm with production function  $Y = AE^\alpha H^\beta$  faces (inverse) demand  $P = DY^{-1/\eta}$ , where  $Y$ ,  $E$ ,  $H$ ,  $P$ ,  $A$  and  $D$  denote output, employment, hours per worker, price, productivity shock and demand shock, respectively. We denote  $\gamma \equiv (\eta - 1)/\eta$  and assume  $\eta > 1$ ,  $\alpha > \beta > 0$  and  $\alpha\gamma < 1$ . The firm faces a wage schedule  $W(H)$ , and we define  $w(h) \equiv \log W(e^h)$ . We assume  $w' > 0$ ,  $w'' > 0$ ,  $w'(0) < \beta/\alpha < w'(+\infty)$  and  $W''(\hat{H}) > 0$ , with  $\hat{H}$  defined via (20) below. In general, lower case letters denote the logs of upper case variables.*

*Then the values of  $h$  and  $e$  that solve the firm's static optimization problem are denoted by  $\hat{h}$  and  $\hat{e}$  and characterized by:*

$$w'(\hat{h}) = \frac{\beta}{\alpha}, \quad (20)$$

$$\hat{e} = \frac{1}{1 - \alpha\gamma} [\log \beta\gamma + d + \gamma a - (1 - \beta\gamma)\hat{h} - \log\{W'(\hat{H})\}]. \quad (21)$$

**Proof** The firm's (static) profit function is

$$\Pi(E, H) \equiv DA^\gamma E^{\alpha\gamma} H^{\beta\gamma} - W(H)E.$$

The corresponding partial derivatives and first order conditions then are:

$$\frac{\partial \Pi}{\partial E} = \alpha\gamma DA^\gamma E^{\alpha\gamma-1} H^{\beta\gamma} - W(H) = 0, \quad (22)$$

$$\frac{\partial \Pi}{\partial H} = \beta\gamma DA^\gamma E^{\alpha\gamma} H^{\beta\gamma-1} - W'(H)E = 0. \quad (23)$$

Multiplying (22) by  $(\beta E)/(\alpha H)$ , subtracting (23), and noting that  $w'(h) = W'(H)H/W(H)$  leads to the first order condition  $w'(h) = \beta/\alpha$ . This equation has a unique solution due to the assumptions we made for  $w$ . Expression (21) follows from taking logs in (23).

Next we check that the second order conditions hold at  $\hat{h}$  and  $\hat{e}$ . From (22) and (23) we have

$$\frac{\partial^2 \Pi}{\partial E^2} = -\alpha\gamma(1 - \alpha\gamma)DA^\gamma E^{\alpha\gamma-2} H^{\beta\gamma}, \quad (24)$$

$$\frac{\partial^2 \Pi}{\partial H^2} = -\beta\gamma(1 - \beta\gamma)DA^\gamma E^{\alpha\gamma} H^{\beta\gamma-2} - W''(H), \quad (25)$$

$$\frac{\partial^2 \Pi}{\partial E \partial H} = \alpha\beta\gamma^2 DA^\gamma E^{\alpha\gamma-1} H^{\beta\gamma-1} - W'(H) = -\beta\gamma(1 - \alpha\gamma)DA^\gamma E^{\alpha\gamma-1} H^{\beta\gamma-1}, \quad (26)$$

where in the last step we used (23) evaluated at  $\hat{H}$ .

We therefore have  $\partial^2 \Pi / \partial E^2 < 0$ , while (24), (25) and (26) can be used to show that

$$\frac{\partial^2 \Pi}{\partial E^2} \frac{\partial^2 \Pi}{\partial H^2} - \left[ \frac{\partial^2 \Pi}{\partial E \partial H} \right]^2 = \beta\gamma^2(1 - \alpha\gamma)(\alpha - \beta)D^2 A^{2\gamma} E^{2\alpha\gamma-2} H^{2\beta\gamma-2} + \alpha\gamma(1 - \alpha\gamma)DA^\gamma E^{\alpha\gamma-1} H^{\beta\gamma} W''(H).$$

The first term on the r.h.s. is positive because we assumed  $\alpha > \beta$  and  $\alpha\gamma < 1$ . The second term is positive because we assumed  $W''(\widehat{H}) > 0$ . ■

## B Relation between static and dynamic targets

**Proposition 2** *The firm's static employment target,  $\widehat{e}_t$ , satisfies:*

$$\widehat{e}_t = \widehat{e}_{t-1} + g_t + \varepsilon_t,$$

with  $\varepsilon_t$  i.i.d. innovations with zero mean and variance  $\sigma_\varepsilon^2$ . The drift,  $g_t$ , is observed by the firm and satisfies:

$$g_t - g = \rho(g_{t-1} - g) + v_t,$$

with  $0 \leq \rho \leq 1$  and  $v_t$  i.i.d. innovations with zero mean and variance  $\sigma_v^2$ , independent from the  $\varepsilon_t$ s.

The firm's discount factor is  $\beta$  and its adjustment technology is Calvo, that is, in every period it either adjusts at no cost (with probability  $\lambda$ ) or it cannot adjust (with probability  $1 - \lambda$ ). The firm's loss from deviating from its static target is quadratic in the employment log-difference,

Then the firm's dynamic employment target, that is, its optimal employment choice should it adjust, is given by:

$$e_t^* = \widehat{e}_t + \delta_t \tag{27}$$

with

$$\delta_t \equiv \frac{\beta(1-\lambda)}{1-\beta(1-\lambda)}g + \frac{\beta(1-\lambda)\rho}{1-\beta(1-\lambda)\rho}(g_t - g). \tag{28}$$

**Proof** If the firm adjusts in  $t$ , it will choose its employment level,  $e_t^*$ , so as to minimize the expected cost of deviating from its static target during the period where the new price is in place:

$$E_t \sum_{k \geq 0} [\beta(1-\lambda)]^k (e_t^* - \widehat{e}_{t+k})^2.$$

It follows that:

$$e_t^* = [1 - \beta(1-\lambda)] \sum_{k \geq 0} [\beta(1-\lambda)]^k E_t \widehat{e}_{t+k}. \tag{29}$$

The assumptions for  $\widehat{e}_t$  imply that

$$\widehat{e}_{t+k} = \widehat{e}_t + \sum_{i=1}^k g_{t+i} + \sum_{i=1}^k \varepsilon_{t+i},$$

and therefore

$$E_t \widehat{e}_{t+k} = \widehat{e}_t + kg + \frac{\rho}{1-\rho}(1-\rho^k)(g_t - g).$$

Substituting this expression in (29) yields (27) and (28). ■

## C Gauging the Costs

In this appendix we derive (19). From (18) and (19) it follows that it suffices to show that under the assumptions in Section 4 we have:

$$\frac{A_2 - A_1}{A_1} \cong \left[ \frac{1}{\lambda_1} - \frac{1}{\lambda_2} \right] \xi, \quad (30)$$

where we have dropped the subindex  $c$  from the  $\lambda$  and

$$\xi = \frac{\alpha\gamma(2 - \alpha\gamma)}{2(1 - \alpha\gamma)^2} (\sigma_I^2 + \sigma_A^2). \quad (31)$$

The intuition is easier if we consider the following, equivalent, problem. The economy consists of a very large and fixed number of firms (no entry or exit). Production by firm  $i$  during period  $t$  is  $Y_{i,t} = A_{i,t} L_{i,t}^\alpha$ ,<sup>24</sup> while (inverse) demand for good  $i$  in period  $t$  is  $P_{i,t} = Y_{i,t}^{-1/\eta}$ , where  $A_{i,t}$  denotes productivity shocks, assumed to follow a geometric random walk, so that

$$\Delta \log A_{i,t} \equiv \Delta a_{i,t} = v_t^A + v_{i,t}^I,$$

with  $v_t^A$  i.i.d.  $\mathcal{N}(0, \sigma_A^2)$  and  $v_{i,t}^I$  i.i.d.  $\mathcal{N}(0, \sigma_I^2)$ . Hence  $\Delta a_{i,t}$  follows a  $\mathcal{N}(0, \sigma_T^2)$ , with  $\sigma_T^2 = \sigma_A^2 + \sigma_I^2$ . We assume the wage remains constant throughout.

In what follows lower case letters denote the logarithm of upper case variables. Similarly, \*-variables denote the frictionless counterpart of the non-starred variable.

Solving the firm's maximization problem in the absence of adjustment costs leads to:

$$\Delta l_{i,t}^* = \frac{\gamma}{1 - \alpha\gamma} \Delta a_{i,t}, \quad (32)$$

and hence

$$\Delta y_{i,t}^* = \frac{1}{1 - \alpha\gamma} \Delta a_{i,t}. \quad (33)$$

Denote by  $Y_t^*$  aggregate production in period  $t$  if there were no frictions. It then follows from (33) that:

$$Y_{i,t}^* = e^{\tau \Delta a_{i,t}} Y_{i,t-1}^*, \quad (34)$$

with  $\tau \equiv 1/(1 - \alpha\gamma)$ . Taking expectations (over  $i$  for a particular realization of  $v_t^A$ ) on both sides of (34) and noting that both terms being multiplied on the r.h.s. are, by assumption, independent (random walk), yields

$$Y_t^* = e^{\tau v_t^A + \frac{1}{2} \tau^2 \sigma_I^2} Y_{t-1}^*, \quad (35)$$

Averaging over all possible realizations of  $v_t^A$  (these fluctuations are not the ones we are interested in for the calculation at hand) leads to

$$Y_t^* = e^{\frac{1}{2} \tau^2 \sigma_I^2} Y_{t-1}^*,$$

and therefore for  $k = 1, 2, 3, \dots$ :

$$Y_t^* = e^{\frac{1}{2} k \tau^2 \sigma_I^2} Y_{t-k}^*. \quad (36)$$

---

<sup>24</sup>That is, we ignore hours in the production function.

Denote:

- $Y_{t,t-k}$ : aggregate  $Y$  that would attain in period  $t$  if firms had the frictionless optimal levels of labor corresponding to period  $t - k$ . This is the average  $Y$  for units that last adjusted  $k$  periods ago.
- $Y_{i,t,t-k}$ : the corresponding level of production of firm  $i$  in  $t$ .

From the expressions derived above it follows that:

$$\frac{Y_{i,t,t-1}}{Y_{i,t}^*} = \left( \frac{L_{i,t-1}^*}{L_{i,t}^*} \right)^\alpha = e^{-\alpha\gamma\tau\Delta a_{i,t}},$$

and therefore

$$Y_{i,t,t-1} = e^{\Delta a_{i,t}} Y_{i,t-1}^*.$$

Taking expectations (with respect to idiosyncratic and aggregate shocks) on both sides of the latter expression (here we use that  $\Delta a_{i,t}$  is independent of  $Y_{i,t-1}^*$ ) yields

$$Y_{t,t-1} = e^{\frac{1}{2}\sigma_T^2} Y_{t-1}^*,$$

which combined with (36) leads to:

$$Y_{t,t-1} = e^{\frac{1}{2}(1-\tau^2)\sigma_T^2} Y_t^*.$$

A derivation similar to the one above, leads to:

$$Y_{i,t,t-k} = e^{\Delta a_{i,t} + \Delta a_{i,t-1} + \dots + \Delta a_{i,t-k+1}} Y_{t-k}^*,$$

which combined with (36) gives:

$$Y_{t,t-k} = e^{-k\xi} Y_t^*, \tag{37}$$

with  $\xi$  defined in (31).

Assuming Calvo-type adjustment with probability  $\lambda$ , we decompose aggregate production into the sum of the contributions of cohorts:

$$Y_t = \lambda Y_t^* + \lambda(1-\lambda)Y_{t,t-1} + \lambda(1-\lambda)^2 Y_{t,t-2} + \dots$$

Substituting (37) in the expression above yields:

$$Y_t = \frac{\lambda}{1 - (1-\lambda)e^{-\xi}} Y_t^*. \tag{38}$$

It follows that the production gap, defined as:

$$\text{Prod. Gap} \equiv \frac{Y_t^* - Y_t}{Y_t^*},$$

is equal to:

$$\text{Prod. Gap} = \frac{(1-\lambda)(1-e^{-\xi})}{1 - (1-\lambda)e^{-\xi}}. \tag{39}$$

A first-order Taylor expansion then shows that, when  $|\xi| \ll 1$ :

$$\text{Prod. Gap} \cong \frac{(1-\lambda)}{\lambda} \xi. \quad (40)$$

Subtracting this gap evaluated at  $\lambda_1$  from its value evaluated at  $\lambda_2$ , and noting that this gap difference corresponds to  $(A_2 - A_1)/A_1$  in the main text, yields (30) and therefore concludes the proof. ■