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A change-detection algorithm for short-circuit fault detection in closed-loop AC drives

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Abstract: This paper deals with an on-line method for turn-to-turn short-circuit fault detection in low-voltage permanent-magnet synchronous machine drives. Due to the closed-loop control, the fault effects are reflected in the voltage. Therefore, an appropriate diagnostic index is proposed, which is derived from the positive- and negative-sequences of the voltage references. These sequences are obtained in the time domain via adaptive filters, which require only a few calculations. To increase the sensitivity to the fault, the algorithm is only applied to a part of the voltage references, i.e. the output of the proportional-integral controllers. Further, the cumulative-sum algorithm is introduced to cope with changes of small magnitudes. This algorithm allows a change of a fault index to be detected and can be used as a decision system. The resulting fault detection scheme is computationally cheap and can be embedded in the control unit. Simulations and experimental results validate the proposed method in steady state and the performances under non-stationary operating conditions are also investigated.

Nomenclature

β_{SC}	Minimum fault amplitude due to the shorted turns to be detected
Δt_{det}	Fault detection delay
$\Delta V_{dq,SC}$	Additional *dq*-axis voltages due to the shorted turns
θ_e	Electrical position
μ_{SC}	Ratio of shorted turns compared with the number of turns in series within one phase
υ_{dq}	Bandwidths of the *dq*-axis closed-loop transfer functions
σ^2	Variance of the fault index
$\psi_{M,1}$	Magnitude of the fundamental component of the flux linkage due to the permanent magnets
ω_m	Mechanical pulsation
ω_e	Electrical pulsation

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abc	Subscripts related to natural quantities
$\alpha\beta$	Subscripts related to stator frame quantities
dq	Subscripts related to rotor frame quantities
$+$	Superscript related to the positive-sequence component
$-$	Superscript related to the negative-sequence component
$*$	Superscript related to the controller references
$[C]$	Clarke transformation matrix
$[R]$	Rotation matrix
$C_{dq}(s)$	dq-axis transfer function of the PI controllers
$D(s)$	Transfer function of the direct adaptive filter
$E_{xy(z)}$	Electromotive force expressed in *xy(z)* frame
g	CUSUM function
h_{det}	Threshold of the decision system
$I_{xy(z)}$	Phase currents expressed in *xy(z)* frame
k	Damping factor of the direct and quadrature adaptive filters
$K_{P,dq}$	Proportional gain of the *dq*-axis PI controllers
$K_{I,dq}$	Integral gain of the *dq*-axis PI controllers
$[L_{abc}]$	Inductance matrix
L_{dq}	*dq*-axis inductances
M_0	Mean value of the fault index in healthy condition
M_{SC}	Mean value of the fault index in faulty condition (short circuit)

p_0	Probability density function of the healthy distribution
p_{SC}	Probability density function of the faulty distribution
q	Phase-shift operator ($q = e^{-j\pi/2}$)
$Q(s)$	Transfer function of the quadrature adaptive filter
R_f	Fault resistance
R_{NP}	Fault index (ratio of the negative- to positive-sequence voltages)
R_s	Stator resistance
s	Laplace variable
T_s	Sampling period
$V_{xy\,(z)}$	Stator voltages expressed in *xy(z)* frame
$V_{xy\,(z),SC}$	Stator voltages expressed in *xy(z)* frame upon the occurrence of an inter-turn fault
CUSUM	Cumulative sum
LLR	Log-likelihood ratio

1. Introduction

Fault detection and diagnosis are paramount for optimizing the availability of electrical drives. In many works, inter-turn short-circuit faults have been highlighted as the most likely origin of winding failures [1-3]. This fault begins with a decrease of the turn-to-turn insulation capability, which is degraded primarily by temperature, environment and electrical stress due to the power converter [4].

Different techniques for insulation testing and monitoring have been reported in the literature [3], [5-7]. On-line techniques such as chemical analysis or discharge detection are generally not well suited for low voltage machines [5]. For example, partial discharges work either off-line or on-line, but are restricted to medium- and high-voltage machines since low-voltage machines are generally not subject to partial discharges [4]. Therefore, tests of the machine parameters are generally conducted off-line, i.e. during the inspection process.

For low-voltage machines, an on-line method is thus required for fault detection in case inspections are undesired or not frequently conducted. Non-invasive methods are usually preferred because of their lower cost. The most common methods reported in the literature are: current-based techniques [8-16], electromotive force- or voltage-based techniques [17-21], power-based techniques [22] and parameter estimation [23, 24].

In [8, 9], the authors give an overview of the specific harmonic components that appear in the current spectrum of induction machines in case of inter-turn short-circuit and mechanical faults respectively. Similar works have been presented more recently for PMSMs, e.g. in [10] and [17] for PMSMs operated with mechanical unbalance and with magnet faults respectively. In [11], frequency analysis is applied to the low-order harmonics due to the converter for the detection of rotor faults in induction machines.

Although the fast Fourier transform (FTT) is basically used for obtaining the harmonic spectrum [12], other methods have been proposed to mitigate its drawbacks such as a high computational cost for good resolution and lack of performances under non-stationary conditions. In [13], a maximum covariance method for frequency tracking combined with the zoom FFT is proposed to solve the problem of precision versus computational cost. Other methods for frequency estimation under non-stationary conditions have been investigated, i.e. using quadratic time – frequency representations [14], empirical mode decomposition and Wigner – Ville distributions [15], the short-time Fourier transform [22] and a frequency sliding pre-processing combined with the mean power of wavelet signals [16].

Considering drives, the impact of the closed-loop control has to be taken into account. Assuming a high-bandwidth current controller, the characteristic frequencies of faults are reflected in the voltage, as evidenced in [18] for induction machines, in [19] for PMSMs and in [20] for doubly-fed induction generators. Consequently, the negative-sequence voltage can be used as fault index. To avoid the measurement of the phase voltages, the voltage references can be used. These references are generally available within the control unit when a field-oriented control (FOC) is implemented with proportional-integral (PI) controllers, whereas they are generally not available for control methods such as direct torque control (DTC). FOC presents thus a significant advantage over DTC in regard to fault detection.

There are several methods that allow the negative-sequence component to be isolated. Actually, the same problems mentioned for the FFT can arise, that is, large data buffers give a good precision at the expense of a high computational cost, memory requirements and poor dynamic response. In [12], the authors propose a method to evaluate the steady-state condition of a PMSM drive. As soon as steady-state is reached, an analysis focused on the second harmonic of the *dq*-axis currents is performed with the FFT. In [16], the negative-sequence component at $-\omega_e$ is shifted to another frequency band via a pre-processing technique. Next, the

signal is analyzed by means of the discrete wavelet transform. The authors of [25] present a structure which isolates the positive- and negative-sequence components by means of adaptive filters. The advantage of the latter structure is that only a few calculations are required.

Once the fault detection method is selected, the derivation of an appropriate fault index is paramount. Regarding spectrum-based methods, the magnitude or rather the change of magnitude of specific harmonics can be used as fault index. For example, in [19] the authors observed that an inter-turn fault decreases the amplitude of the voltage positive-sequence component. Hence, a fault index was derived on the basis of the comparison between the actual value of the voltage references and the healthy value which was stored in a look-up table. In [21], a voltage mismatch technique is presented. This technique consists in calculating the expected positive- and negative-sequence voltages based on a machine model that had been previously determined and stored in a memory. The expected voltages are compared with the measured voltages to assess the severity of the fault current. For parameter-estimation-based methods, the fault indices are generally derived from the difference between the nominal parameters and estimated or measured parameters. So in [23], eccentricity faults are detected by measuring the *d*-axis inductance of saturated PMSMs at standstill, whereas an on-line estimation of the parameters is used in [24] to detect inter-turn short-circuit.

In any case, an important and common feature to almost all fault detection strategies is that only changes compared with the healthy situation can be observed. A procedure to obtain the value of the fault indices in healthy operation should always be conducted at the drive commissioning. An embedded procedure based on artificial intelligence is attractive to do so [18]; an automated procedure is proposed in [21]; quite often this procedure is still man-made in industry.

Further, most works on fault detection focus on the derivation of fault indices or methods, but do not provide a decision criterion. The decision-making process is paramount regarding the reliability of the fault detection system, which has to detect a fault and must minimize the number of false alarms. The cumulative-

sum (CUSUM) algorithm is a simple and effective change-detection algorithm which allows detecting a change in the statistical properties of fault indices and can be used as a decision system [26]. This algorithm is applied to fault detection of current-sensor faults and open-circuit phases in [27]-[30].

Finally, the objective of the decision system is to initiate an action upon fault detection, which can be a safe shutdown of the drive or a warning to an operator, who initiates or re-schedules a shutdown of the drive/plant and an inspection. A reconfiguration of the drive to mitigate the fault propagation is also an alternative, assuming the drive is fault-tolerant to short-circuit faults [31-38]. Regarding PMSMs, the requirements are: large inductances (>1pu), an appropriate design preventing demagnetization of the magnets and a topology allowing the machine to be operated with a part of the winding shorted, e.g. with dual three-phase windings.

In this paper, a specific implementation of the CUSUM algorithm is proposed for inter-turn fault detection. The method proposed in [25] for the calculation of the negative- and positive-sequence voltages is adapted for PMSM drives. An analysis shows that the sensitivity to the fault can be increased by applying the calculation to only a part of the voltage references, i.e. the output of the PI controllers. Further, changes of negative- and positive-sequence components upon the fault occurrence are combined in a single fault index. The proposed method has the advantages to be simple for use, sensitive and computationally cheap. For industrial application one major attraction of the method is the possibility to adjust simply the threshold of the fault detection in relation with the effect of the fault, in order to mitigate the risk of false alarms. The performances of the proposed scheme under stationary and non-stationary conditions are investigated through simulations and experimental results.

The paper is organized as follows. In section II, the drive model and control parameters are given. In section III, the fault detection scheme is described, which includes details on a specific calculation of the symmetrical components, the derivation of a relevant fault index, the theoretical background of the CUSUM algorithm and its practical implementation. Finally, the test-bed description and the experimental results of the proposed method are presented in section IV.

2. Drive model and control parameters

2.1 Model of healthy machine

The system under study is depicted in Fig. 1. The drive is composed of a three-leg inverter and a three-phase PMSM. The DC-link voltage, the mechanical position and the three phase currents are measured. A turn-to-turn fault is represented in the *a*-phase. The fault is characterized by the fault resistance R_f and the ratio of shorted turns compared to the number of series turns within one phase μ_{SC}. Both parameters are a priori unknown.

Regarding the healthy machine, the voltage equations expressed in the *abc* reference frame are given by:

$$[V_{abc}] = R_s[I_{abc}] + \frac{d}{dt}([L_{abc}][I_{abc}]) + [E_{abc}] \tag{1}$$

with $[V_{abc}]$ the *abc* voltages, R_s the stator resistance, $[L_{abc}]$ the inductance matrix, $[I_{abc}]$ the *abc* phase currents and $[E_{abc}]$ the emf induced by the permanent magnets in the stator windings.

The models of the machine expressed in the stator and in the rotor reference frames are obtained by applying successively the Clarke and rotation transformations defined by:

$$[X_{\alpha\beta}] = \frac{2}{3}[C][X_{abc}] \tag{2}$$

$$[X_{dq}] = [R][X_{\alpha\beta}] \tag{3}$$

with transformation matrices given by:

$$[C] = \begin{bmatrix} 1 & -1/2 & -1/2 \\ 0 & \sqrt{3}/2 & -\sqrt{3}/2 \end{bmatrix} \tag{4}$$

$$[R] = \begin{bmatrix} \cos\theta_e & \sin\theta_e \\ -\sin\theta_e & \cos\theta_e \end{bmatrix} \tag{5}$$

The quantity X can be a vector of currents, voltages or fluxes and θ_e is the electrical position of the rotor. The zero-sequence component is omitted as the machine is star-connected with isolated neutral point and ground fault is not considered. Applying the transformations (2) and (3) to the system (1) yields:

$$\begin{bmatrix} V_d \\ V_q \end{bmatrix} = R_s \begin{bmatrix} I_d \\ I_q \end{bmatrix} + \begin{bmatrix} L_d & 0 \\ 0 & L_q \end{bmatrix} \frac{d}{dt} \begin{bmatrix} I_d \\ I_q \end{bmatrix} + \begin{bmatrix} E_d \\ E_q \end{bmatrix} \tag{6}$$

with

$$\begin{bmatrix} E_d \\ E_q \end{bmatrix} = \omega_e \begin{bmatrix} -L_q I_q \\ L_d I_d + \psi_{M,1} \end{bmatrix} \tag{7}$$

with ω_e the electrical pulsation, $\psi_{M,1}$ the magnitude of the fundamental component of the flux linkage due to the permanent magnets and L_d and L_q the d- and q-axis inductances respectively.

2.2 Control parameters

The following control law with PI controllers and compensated emf is chosen (see Fig. 2):

$$\begin{bmatrix} V_d^* \\ V_q^* \end{bmatrix} = \begin{bmatrix} C_d(I_d^* - I_d) \\ C_q(I_q^* - I_q) \end{bmatrix} + \begin{bmatrix} E_d \\ E_q \end{bmatrix} \tag{8}$$

where C_d, C_q are the transfer functions of the PI controllers, given by:

$$C_d = K_{P,d} + \frac{K_{I,d}}{s} \tag{9}$$

$$C_q = K_{P,q} + \frac{K_{I,q}}{s} \tag{10}$$

with s the Laplace variable and $K_{P,d}$, $K_{P,q}$, $K_{I,d}$, $K_{I,q}$ the proportional and integral gains of the d- and q-axis controllers.

If the bandwidth of the d-axis closed-loop transfer function is equal to v_d, the pole-zero compensation technique allows the gains to be calculated as follows (similar calculation for the q-axis) [39]:

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$$K_{P,d} = \upsilon_d L_d \tag{11}$$

$$K_{I,d} = \upsilon_d R_s \tag{12}$$

2.3 Model of machine with inter-turn fault

The modeling of PMSMs with a turn-to-turn fault is discussed in [40-42]. In [40], a simple electrical model is proposed, which shows that a turn-to-turn fault causes an unbalance of the drive. Further, the author shows that the fault decreases the fundamental value of the magnet flux linkage, i.e. its positive-sequence component, and therefore the positive-sequence emf as well. In [41], an analytical model of the fault in the rotor reference frame is proposed, whereas in [42] a finite-element analysis shows that the current in the shorted turns depends on the position of the turns in the slot as well.

Upon the fault occurrence, the change can be expressed as:

$$\lfloor V_{dq,sc} \rfloor = \lfloor V_{dq} \rfloor + \lfloor \Delta V_{dq,sc} \rfloor \tag{13}$$

where $\lfloor V_{dq,sc} \rfloor$ are the *dq*-axis voltages upon the fault occurrence and $\lfloor \Delta V_{dq,sc} \rfloor$ are the changes due to the fault. Because of the stator unbalance, the fault components can be expressed as a development with even harmonics. Considering only the two first terms, $\lfloor \Delta V_{dq,sc} \rfloor$ can be expressed as:

$$\lfloor \Delta V_{dq,sc} \rfloor \approx \lfloor \Delta V_{dq,sc}(0) \rfloor + \lfloor \Delta V_{dq,sc}(2\omega_e) \rfloor \tag{14}$$

The first term of (14) is associated with a change of positive-sequence voltage, while the second term is associated with a change of negative-sequence voltage.

Although the quantification of the change is given as a function of the fault parameters in [41], the fault is characterized by two unknown parameters and therefore the magnitude of the change gives an estimate of the fault severity only.

3. Fault detection scheme

3.1 Fortescue transformation for PMSM drives

The Fortescue transformation allows three-phase quantities to be split up into positive-, negative- and zero-sequence components. The conventional transformation is based on complex numbers (for quasi-steady-state operation at a given frequency), but an implementation in the time domain and stator reference frame is proposed in [25]. The authors show that:

$$\begin{bmatrix} X_\alpha^+ \\ X_\beta^+ \end{bmatrix} = \frac{1}{2}\begin{bmatrix} 1 & -q \\ q & 1 \end{bmatrix}\begin{bmatrix} X_\alpha \\ X_\beta \end{bmatrix} \tag{15}$$

$$\begin{bmatrix} X_\alpha^- \\ X_\beta^- \end{bmatrix} = \frac{1}{2}\begin{bmatrix} 1 & q \\ -q & 1 \end{bmatrix}\begin{bmatrix} X_\alpha \\ X_\beta \end{bmatrix} \tag{16}$$

The superscripts '+' and '-' denote the positive- and negative-sequence components respectively and $q = e^{-j\pi/2}$ is a phase-shift operator in the frequency domain which can be implemented in the time domain with adaptive filters. This structure allows a simplification of the implementation for variable-frequency

quantities as the use of a variable-length window is avoided. An instantaneous value of the symmetrical components is obtained without data storage and with a few calculations.

The scheme for the calculation of the symmetrical components is depicted in Fig. 3. The structure requires the pulsation of the input quantities X_α and X_β. Regarding PMSM drives, the electrical pulsation ω_e is directly available and no estimation is thus required. Each block "Filters" is composed of two filters with the following transfer functions:

$$D(s) = \frac{X'(s)}{X(s)} = \frac{k\omega_e s}{s^2 + k\omega_e s + \omega_e^2} \tag{17}$$

$$Q(s) = \frac{qX'(s)}{X(s)} = \frac{k\omega_e^2}{s^2 + k\omega_e s + \omega_e^2} \tag{18}$$

where k is a damping factor. The D-filter is a band-pass filter, of which the filter gain is equal to 1 at the electrical pulsation (i.e. at $s = j\omega_e$) and allows filtering higher-order harmonic components. At the electrical pulsation, the Q-filter has a unitary gain as well ($Q(j\omega_e) = -j$), but it is a low-pass filter with output in quadrature with the input. This filter is thus used for the implementation of $q = e^{-j\pi/2} = -j$.

3.2 Fault index

Considering grid-connected machines, the most common indices for turn-to-turn fault detection are the negative-sequence current or impedance. However, due to the closed-loop controller, the *dq* currents are likely to be close to their references, and as such unchanged upon the fault occurrence. In this case, the voltage at the machine terminals will be unbalanced. Therefore the fault index can be better derived from the negative- and positive-sequence component of the voltage references. At this step, a relevant fault index derived from (14) can be:

$$FI_1 = \frac{\left|\Delta v_{dq,sc}^*(2\omega_e)\right|}{\left|v_{dq,sc}^*(0)\right|} \tag{19}$$

The fault index (19) is the ratio of negative- to positive-sequence voltages. The advantages of (19) are:

- the index is theoretically equal to zero in healthy operation;
- as $V_{dq,sc}^*(0)$ decreases upon an intern-turn fault occurrence, the index takes benefit of an increase of

  the numerator and a decrease of the denominator upon the fault occurrence, what increases the sensitivity to the fault.

However, as the magnitude of the positive sequence is much bigger than the one of the negative sequence, the change of the fault index can be low. Looking further at the compensations terms (7) and assuming the number of shorted turns is small, it can be noticed that:

- the *dq* currents will be close to their references;

- the mechanical speed will be unaffected upon the fault occurrence.

Consequently, the compensation terms are constant and insensitive to the fault. To increase the sensitivity to the fault, the calculation of the negative- and positive-voltages is then applied to the output of the PI controllers, as depicted in Fig. 2. Hence, considering that upon the fault occurrence $\left[V_{dq}^*\right] = \left[V_{dq,sc}\right]$ and substituting (14), (13) and (6) into (8), the steady-state value of the fault index is given by (see also Appendix I):

$$FI_2 = \frac{\left|\Delta v_{dq,sc}^*(2\omega_e)\right|}{\left|R_s I_{dq} + \Delta v_{dq,sc}^*(0)\right|} \tag{20}$$

For implementation purpose, the proposed fault index R_{NP} is obtained as follows:

1. Apply the inverse rotation matrix $[R]^{-1} = [R]^T$ to the *dq* voltage outputs of the PI controllers $V_{PI,dq}^*$ (Fig. 2).

2. Calculate the negative- and positive-sequences of $V_{PI,\alpha\beta}^*$ according to the scheme of Fig. 3.

3. Calculate the ratio between the magnitudes of the negative- and positive-sequence components:

$$R_{NP} = \sqrt{\frac{\left(v_{PI,\alpha}^{*,-}\right)^2 + \left(v_{PI,\beta}^{*,-}\right)^2}{\left(v_{PI,\alpha}^{*,+}\right)^2 + \left(v_{PI,\beta}^{*,+}\right)^2}} \tag{21}$$

Fig. 4 shows simulation results obtained with the proposed scheme and a simple signal analysis. Initially, the three-phase signals are perfectly balanced, as shown in Fig. 4(a) and (b). Consequently, the signal has only a positive-sequence (Fig. 4(c) and (d)). At time t=0.05s, an unbalance of 0.05pu appears on the *a*-phase. Next, the magnitude of the positive sequence slightly drops to 0.983, while the magnitude of the negative sequence rises to 0.0167 (Fig. 4(e)). The ratio of both amplitudes is equal to the fault index $R_{NP} = 0.017$ (Fig. 4(f)).

The response of the fault index is related to the dynamics of the adaptive filters, which depends on the damping factor k and the pulsation ω_e. Simulations show that $k = \sqrt{2}$ is a good tradeoff between the rejection

of higher-order harmonics and the dynamics of the filters. Several simulation results are presented in Fig. 5 and Fig. 6, which show the value of the fault index under non-stationary conditions.

Fig. 5 shows the response of the fault index when starting the motor. Three speed ramps with different slopes have been simulated. The accelerations are 500, 1000 and 2000rpm per second on a time horizon of two seconds. The amplitude of the three *abc* signals is kept constant in these simulations. It can be observed in Fig. 5 that the value of the fault index is initially equal to one and decreases quickly to zero. The initial value is due to the filter dynamics as both sequences have a null magnitude at the beginning. Next, the convergence speed increases with the pulsation. These simulations show that the convergence speed is poor at low speed and the fault detection should be inhibited below a minimum speed.

Fig. 6 shows the response of the fault index in case of load changes at constant speed. The amplitude of the three-phase signals is initially equal to one and the final value is equal to two. The three plots show the response in case of step, first-order (FO)-like response with time constant equal to 0.01s and ramp with slope equal to 10. It can be seen that the index takes large values for the step and for the FO-like responses but the transient vanishes quickly. Obviously, this cannot be ignored as threshold-based fault detection will fail with this method. An additional low-pass filtering is a possible solution, but in the proposed solution the decision system will handle it. The latter is described in the following section. Its role consists of tracking changes of the fault index but also to verify that the changes are permanent, i.e. due to a fault.

3.3 Decision system

The decision system has to decide whether there is a fault or not. The CUSUM algorithm has been used for this purpose. A theoretical background of this algorithm can be found in [26]. In brief, this algorithm processes the fault index R_{NP} by detecting a change of its statistical properties, i.e. its mean value in this case.

It is assumed that the successive discrete values of the fault index R_{NP} are distributed according to a Gaussian probability law with mean M_0 and variance σ^2 before the fault occurrence and a mean $M_{SC} > M_0$ and same variance σ^2 following the fault occurrence. Fig. 7 shows the probability density functions associated with these distributions. The probability density functions associated to the healthy state is given by:

$$p_0(R_{NP}) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{1}{2}\left(\frac{R_{NP}-M_0}{\sigma}\right)^2} \tag{22}$$

Fig. 7 illustrates the confidence level to associate with each value of the fault index. As the distributions are symmetrical, the healthy state is more likely at time k in case $R_{NP}(k) < \frac{M_0+M_{SC}}{2}$ and conversely in case $R_{NP}(k) > \frac{M_0+M_{SC}}{2}$.

The CUSUM algorithm is based on the log-likelihood ratio (LLR) calculated at each sample k. The LLR is given by:

$$LLR(k) = \ln \frac{p_{SC}(R_{NP}(k))}{p_0(R_{NP}(k))} \tag{23}$$

where p_{SC} and p_0 are the probability density function of the faulty and healthy distributions respectively.

From (22) and (23), it follows (see Appendix II):

$$LLR(k) = \frac{M_{SC}-M_0}{\sigma^2}\left(R_{NP}(k) - \frac{M_{SC}+M_0}{2}\right) \tag{24}$$

The LLR at time k is therefore positive if $R_{NP}(k) > \frac{M_{SC}+M_0}{2}$ and negative if $R_{NP}(k) < \frac{M_{SC}+M_0}{2}$. Hence, if the mean of R_{NP} is equal to M_{SC} (faulty condition), the successive values $R_{NP}(k)$, $R_{NP}(k+1)$,... are generally positive, whereas these values are generally negative in case the mean of R_{NP} is equal to M_0 (healthy condition). Therefore, an appropriate decision function g is given by:

$$g(k) = \max(0, g(k-1) + LLR(k)) \tag{25}$$

This decision function is close to zero as long as there is no fault and starts increasing upon the fault occurrence. A decision that the faulty situation holds can be made in case g crosses a user-chosen threshold h_{det} which affects the fault detection delay Δt_{det}. A possible re-initialization of the CUSUM function allows observing the persistence of the fault.

3.4 Practical implementation of the fault detection scheme

The following observations have to be taken into account for the practical implementation of the fault detection scheme:

- the mean value of the fault index in healthy condition (M_0) is close to zero, but is not exactly zero. The residual value depends on the operating conditions and must be taken into account for the detection of small-magnitude changes;
- the mean value of the fault index in case of turn-to-turn fault (M_{SC}) depends on the fault parameters μ_{SC} and R_f, which are both unknown;
- the calculation of the symmetrical components is impossible at standstill and is imprecise at low speed;
- the fault index is sensitive to abrupt changes of the operating point.

To overcome these problems, the following implementation is proposed:

- a recording of the values of the fault index in healthy operation is performed (ideally at the drive commissioning and in real operating conditions), as already proposed in [1], [8], [18] and [21];
- a minimum fault magnitude β_{SC} is selected;
- the fault detection is inhibited at zero and low speed;
- the threshold h_{det} is chosen by also taking into account the drive operating conditions.

Regarding the CUSUM algorithm, the values of M_0 are stored in a 2-dimensional lookup table with speed and torque (or equivalently the torque reference) as inputs (see Fig. 8). The value of M_{SC} is such that:

$$M_{SC} = M_0 + 2\beta_{SC} \tag{26}$$

Further, the term $\frac{M_{SC} - M_0}{\sigma^2}$ in (24) is a constant gain which can be accounted for in the detection threshold h_{det}. That is, the variance σ^2 can be unknown and the LLR can be reformulated as follows:

$$LLR(k) = R_{NP}(k) - M_0 - \beta_{SC} \tag{27}$$

Hence, the number of samples M required for reaching the detection threshold h_{det} from the sample index *i* of the fault occurrence is such that:

$$h_{det} \cong \sum_{i=1}^{M} LLR(i) \tag{28}$$

Given a sampling period T_s and assuming $LLR(k)$ is constant for a given fault, the detection delay is given by:

$$\Delta t_{det} \cong \frac{T_s}{LLR(k)} h_{det} \tag{29}$$

The detection delay is thus proportional to the detection threshold and the sampling period and inversely proportional to the magnitude of the fault index.

3.5 Computational cost

An advantage of the proposed method is the low computational cost. Besides the control tasks, here is a summary of the operations required for fault detection.

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Starting from the output of the PI controllers, the operations are:

- inverse rotation: 4 multiplications and 2 sums;

- adaptive filters (17) and (18) (x2): 2 multiplications, 5 multiplications by a constant, 4 sums and 2 delays;

- positive- and negative-sequences (15) and (16): 8 sums and 4 multiplications by a constant;

- index calculation: 4 multiplications, 2 sums, 1 square root and 1 division;

- CUSUM algorithm: 4 sums, 2 delays, 3 comparisons, 2 multiplications by a constant and 1 memory access;

- additional logic for enabled execution of blocks.

4. Experimental results

4.1 Test-bed description

The test bed used for the experimentation is shown in Fig. 9. The setup is composed of two PMSMs, a torquemeter, a three-leg inverter and a dSPACE 1006 board. The load machine is connected to a three-phase resistance network and the load torque is thus proportional to the speed. The position sensor is a resolver mounted on the shaft of the motor. Three current sensors LEM LA55-P are available in an external box. The DC-link voltage sensor is integrated within the converter.

Table 1 *Ratings of the PMSM under study*

Rated power	2.59 kW
Rated speed ($\omega_{m,R}$)	2000 rpm
Rated torque ($T_{em,R}$)	13.5 Nm
Rated current ($I_R = 5.7\text{A}$)	5.7 A
Rated voltage (U_R)	325 V

Table 2 *Winding parameters of PMSM*

Winding parameter	Value
Number of parallel wires	4
Wire diameter	2x0.56 + 2x0.60 mm²
Number of slots	36
Number of series turns per coil	30
Number of coils per phase (series configuration)	6
Resistance of one phase at T=20°C	1.39Ω
dq-axis inductances	11.4mH
Number of pole pairs N_{pp}	3

The machine under study is a three-phase PMSM which has been rewound (see Fig. 10) to access the 6 main power terminals and to integrate additional turns for testing the fault detection scheme. The ratings of the machine are given in Table 1.

The winding parameters are given in Table 2, whereas the winding pattern is shown in Fig. 11 (single-layer integral-slot concentrated winding). The input (output) terminals of phase *x* is denoted by Ix (Ox), $x \in \{a, b, c\}$.

Additional turns have been added for generating inter-turn short-circuit faults. Two turns are located in slots 1 and 6, two in slots 13 and 18 and two in slots 25 and 30. Their copper section is approximately equal to the sum of the sections of the parallel wires, i.e. $\cong 1 \text{mm}^2$. These additional turns are all inserted in slots belonging to the *a*-phase. Therefore, by adding one or two turns in series with each phase, only the zero-sequence component of the emf is affected, what does not affect the asymmetry of the machine (no effect on the positive and negative voltage of the original winding). These turns can be individually shorted at the terminals of the machine via external cables or resistances. These cables increase the resistance of the turns, what can be considered as the fault resistance R_f. An external potentiometer was always used during early tests, but a verification has shown that a short-circuit fault at the terminals may be performed without excessive heating for a duration of approximately 30s.

4.2 Parameters of the fault-detection scheme

The parameters of the controllers and of the fault-detection scheme that have been used for the tests are given in Table 3.

Table 3 *Parameters of fault detection scheme*

Parameter	Value
d-axis current bandwidth υ_d	1000 rad/s
q-axis current bandwidth υ_q	1000 rad/s
Sampling period T_s	0.2 ms
Filter damping factor k	$\sqrt{2}$
Fault index in healthy condition M_0	See Fig. 12
Minimum fault amplitude β_{SC}	0.005
Fault resistance R_f (1 shorted turn)	0.06Ω
Fault resistance R_f (2 shorted turns)	0.14Ω
Detection threshold h_{det}	100
Minimum speed for fault detection $\omega_{m,min}$	200 rpm

The sampling time is equal to 0.2ms. The control loops and fault detection work within the same control platform at the same frequency (5kHz). As the discretization of the adaptive filters (17) and (18) influences the value of the fault index, a minimum ratio of 50 between the sampling frequency and the electrical frequency has to be kept.

The value M_0 of the fault index R_{NP} in healthy condition is depicted in Fig. 12, which shows the mapping of the fault index as a function of the electromagnetic torque for several mechanical speeds. This

mapping has been obtained by operating the machine at various speeds and loads in steady state. There are actually about 40 different operating points that have been considered. For each point, the value of M_0 are

equal to the average value of a data window of 4s. Combined with an interpolation between the various points, this proved to be enough for a good precision. Generally, the values M_0 decrease with larger electromagnetic

torques and increase for larger speeds. Tests have been conducted over a period of time longer than six months. The index has been stable within this period and a good reproducibility has been observed.

The minimum fault amplitude β_{SC} is chosen equal to 0.005. This value can be decreased but an

additional procedure to freeze the fault detection in transient operation should then be added to avoid false alarms (see following sections).

The fault resistance R_f is somewhat high since its value is several times larger than the turn resistance

(approximately equal to $R_t = \frac{1.39}{180} = 0.008\ \Omega$). As a result, the short-circuit current is relatively low

(approximately equal to $6I_R$), but the value of the fault index is lower as well in case of fault.

The value of the detection threshold h_{det} will be discussed in the following sections.

Fault detection is inhibited below 200rpm, mainly due to a high cogging torque and low inertia of the test bed. The calculated positive and negative- voltages were not accurate below this threshold and fault detection was not effective (fault could not be distinguished from noise). As voltages which induce the short-circuit currents are associated with the electromotive forces, they are proportional to the speed. It is then normal that the effect is less detectable at low speed since the short-circuit currents amplitudes are lower than at high speed. It is also less important to detect a fault when its impact on the ageing of the machine is lower. Of course, if it is wanted to detect short-circuit from zero speed, a complementary technic is necessary. For the prototype, RMS currents in one and two turns short-circuited have been measured in the range 0 to 400 rpm at different loads. The results confirm a linear dependence with the speed with a maximum value of 0.43 pu for the short-circuit current at 400 rpm.

4.3 Turn-to-turn detection in steady-state operation

Experimental results of the whole scheme are presented in Fig. 14, Fig. 14 and Fig. 15. The test is performed in steady state with $\omega_m = 600 \text{rpm}$ and $T_{em} = 0.67 \text{pu}$.

Fig. 14 compares the sampled phase currents in healthy and faulty conditions. Because of the closed-loop control, no difference is observed. This is confirmed in Fig. 14, which presents experimental results of a short-circuit fault occurring at time t=2.85s until t=17s (2 turns out of 182). Fig. 14(a) and (b) show the *dq* currents and measured electromagnetic torque respectively, both being unaffected by the fault. The fault index is shown in Fig. 14(c), while the CUSUM function is shown in Fig. 14(d). For the operating conditions under study, the corresponding value of the fault index in healthy operation M_0 is equal to 0.019, as it can be seen in Fig. 12

and Fig. 14(d). Upon the fault occurrence, the fault index rises to approximately 0.03 and the CUSUM function starts increasing. The decision function crosses the detection threshold at time $t = 6.21s$. The CUSUM function

is then re-initialized. For this test, the fault disappears at time $t = 17s$ and the CUSUM function returns to zero.

Regarding the detection delay, the value predicted by (29) gives $\Delta t_{det} = 3.33s$, which coincides with

the observed value of $3.36s$.

Additional details are given in Fig. 15(a), (b) and (c), which show the voltage references expressed in the rotor reference frame, the PI controller output positive-sequence magnitude and the PI controller-output negative-sequence magnitude respectively. A zoom on the fault occurrence at t=2.85s is presented. The value of V_q^* drops of about 1V upon the fault occurrence and the voltage ripple increases. This is better explained in

Fig. 15(b) and (c), where the voltage drop is seen as a decrease of the positive-sequence magnitude and the voltage ripple as an increase of the negative-sequence magnitude. The difference as regards to the sensitivity when using the PI controller output instead of the voltage reference is also evidenced: the decrease of the positive-sequence magnitude is approximately equal to 1/85 for the voltage references, while the decrease is approximately equal to 1/20 for the PI controller output.

In case only one turn is shorted with a fault resistance R_f equal to 0.06Ω, the change of the fault index is about 0.002 for the same operating conditions, as shown in Fig. 16. Although it is possible to detect a change of such a low magnitude, i.e. by setting β_{SC} to 0.001, the detection becomes very sensitive to transient

operation (see following section).

It has to be noted that the index was observed to be insensitive at no load for faults with one and two shorted turns.

4.4 Behavior of the fault-detection method in transient operation (without fault)

Fig. 17 shows the response of the fault-detection method in case of transient operation (speed and load ramps) without fault. The machine is first at standstill and M_0 is approximately equal to 0.07. The speed starts

increasing at time $t = 0.8s$, as shown in Fig. 17(a). The load torque is proportional to the mechanical speed as it

can be seen in Fig. 17(b). The fault detection is enabled when the speed crosses 200rpm and R_{NP} and M_0

become quickly close. When the speed starts decreasing at time $t = 2.35s$, the transient operation causes a

transient of the fault index which becomes temporally larger than its steady-state value (Fig. 17(c)), similarly to the simulation results of Fig. 6. The CUSUM function starts increasing, but the fault index is restored before the decision function crosses the threshold (Fig. 17(d)).

Obviously, under non-stationary conditions, the value of the decision threshold h_{det} is not only

dependent of the detection delay, but has to be chosen in a way that false alarms due to dynamic conditions are avoided. This can be investigated at early stages by testing a mission profile in simulation.

At the drive commissioning, a further verification has to be performed to ensure that this threshold is never crossed during the healthy operation.

In case of torque-controlled drives with very high dynamics, the value of the fault index can become high during transient operation and this would lead to unreasonably high thresholds. In that case, a pragmatic solution consists in activating the fault detection only when sufficient steady state is observed, for example, in case the compensation terms (7) are close to the voltage references (8).

4.5 Behavior of the fault detection method in transient operation (with fault)

Fig. 18 shows the response of the fault detection method in case of transient operation and two shorted turns. It can be observed that the fault index is greater than in healthy operation all along the test. It can also be noticed that the short periods in which the fault detection is inhibited (near zero speed) do not cause a significant change of the detection delay.

5. Conclusions

A complete method for fault detection of inter-turn faults in PMSM drives has been presented and experimentally validated. The main advantages of the method are: the simple implementation, a low computational cost which allows the fault detection to be embedded on the control platform at no cost and a good sensitivity thanks to an access to the PI controller outputs.

Although the implementation of the proposed fault index in the time domain makes it sensitive to non-stationary conditions, the association with the CUSUM algorithm allows mitigating this drawback to some extent. Hence, the method can be applied to various industrial applications such as fans or pumps, but also to applications such as wind turbines and electric vehicles.

Various objectives can be achieved by considering the decision of the monitoring system. For example, this gives a condition for inspection, maintenance or replacement of the electric machine, or also a criterion to initiate a reconfiguration of the drive, assuming the drive is fault-tolerant.

For future works, the authors suggest to combine this fault-detection method with other techniques for monitoring mechanical, inverter and sensor faults. Investigations of complementary techniques based on signal injection seem also promising for extending fault detection at zero and in the low-speed region.

6. Appendix I

The system equations are given by:

$$[V_{dq,sc}] = [V_{dq}] + [\Delta V_{dq,sc}] \tag{A.1}$$

That is:

$$\begin{bmatrix} V_{d,sc} \\ V_{q,sc} \end{bmatrix} = R_s \begin{bmatrix} I_d \\ I_q \end{bmatrix} + \begin{bmatrix} L_d & 0 \\ 0 & L_q \end{bmatrix} \frac{d}{dt} \begin{bmatrix} I_d \\ I_q \end{bmatrix} + \begin{bmatrix} E_d \\ E_q \end{bmatrix} + \begin{bmatrix} \Delta V_{d,sc}(0) + \Delta V_{d,sc}(2\omega_e) \\ \Delta V_{q,sc}(0) + \Delta V_{q,sc}(2\omega_e) \end{bmatrix} \tag{A.2}$$

The control law is such that:

$$\begin{bmatrix} V_d^* \\ V_q^* \end{bmatrix} = \begin{bmatrix} C_d(I_d^* - I_d) \\ C_q(I_q^* - I_q) \end{bmatrix} + \begin{bmatrix} E_d \\ E_q \end{bmatrix} \tag{A.3}$$

Applying the voltage references (A.3) to the system (A.2) yield:

$$\begin{bmatrix} V_d^* \\ V_q^* \end{bmatrix} = \begin{bmatrix} V_{d,sc} \\ V_{q,sc} \end{bmatrix}$$

$$\begin{bmatrix} C_d(I_d^* - I_d) \\ C_q(I_q^* - I_q) \end{bmatrix} + \begin{bmatrix} E_d \\ E_q \end{bmatrix} = R_s \begin{bmatrix} I_d \\ I_q \end{bmatrix} + \begin{bmatrix} L_d & 0 \\ 0 & L_q \end{bmatrix} \frac{d}{dt} \begin{bmatrix} I_d \\ I_q \end{bmatrix} + \begin{bmatrix} E_d \\ E_q \end{bmatrix} + \begin{bmatrix} \Delta V_{d,sc}(0) + \Delta V_{d,sc}(2\omega_e) \\ \Delta V_{q,sc}(0) + \Delta V_{q,sc}(2\omega_e) \end{bmatrix} \tag{A.4}$$

In steady state, the derivative terms are equal to zero. Hence:

$$\begin{bmatrix} C_d(I_d^* - I_d) \\ C_q(I_q^* - I_q) \end{bmatrix} = R_s \begin{bmatrix} I_d \\ I_q \end{bmatrix} + \begin{bmatrix} \Delta V_{d,sc}(0) + \Delta V_{d,sc}(2\omega_e) \\ \Delta V_{q,sc}(0) + \Delta V_{q,sc}(2\omega_e) \end{bmatrix} \tag{A.5}$$

In the rotor reference frame, the constant terms are associated with the positive sequence, while the terms rotating at $2\omega_e$ are associated with the negative sequence. Finally, the fault index is calculated as follows:

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$$FI_2 = \frac{|\Delta V^*_{dq,SC}(2\omega_s)|}{|R_s I_{dq} + \Delta V^*_{dq,SC}(0)|} \tag{A.6}$$

7. Appendix II

The log-likelihood ratio is calculated as follows:

$$
\begin{aligned}
LLR(k) \quad &= \quad \ln\frac{p_{SC}(R_{NP}(k))}{p_0(R_{NP}(k))} \\[2mm]
&= \quad \ln\frac{\frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{1}{2}\left(\frac{R_{NP}-M_{SC}}{\sigma}\right)^2}}{\frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{1}{2}\left(\frac{R_{NP}-M_0}{\sigma}\right)^2}} \\[2mm]
&= \quad \ln\left(e^{-\frac{1}{2}\left(\frac{R_{NP}-M_{SC}}{\sigma}\right)^2 + \frac{1}{2}\left(\frac{R_{NP}-M_0}{\sigma}\right)^2}\right) \\[2mm]
&= \quad \frac{1}{2\sigma^2}\left(2R_{NP}M_{SC} - 2R_{NP}M_0 - M_{SC}^2 + M_0^2\right) \\[2mm]
&= \quad \frac{1}{2\sigma^2}\left(2R_{NP}[M_{SC}-M_0] - [M_{SC}+M_0][M_{SC}-M_0]\right) \\[2mm]
&= \quad \frac{M_{SC}-M_0}{\sigma^2}\left(R_{NP} - \frac{M_{SC}+M_0}{2}\right)
\end{aligned}
$$

8. Acknowledgments

9. References

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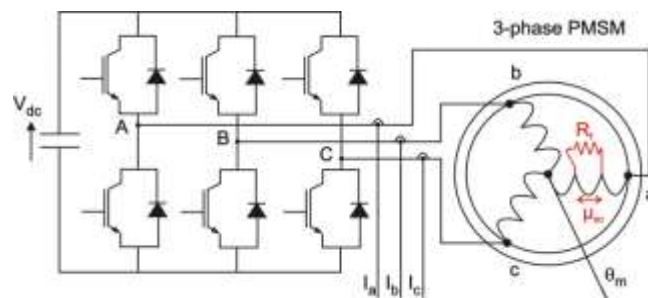
Fig. 1 *PMSM drive with an inter-turn fault*
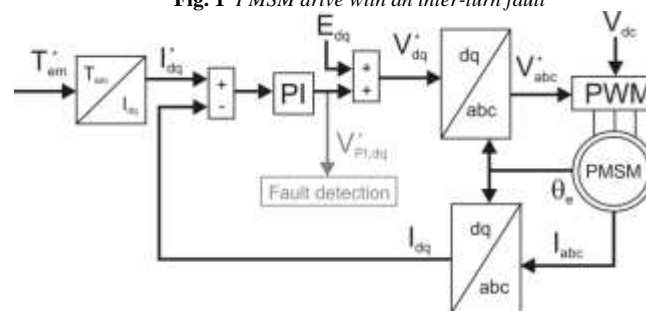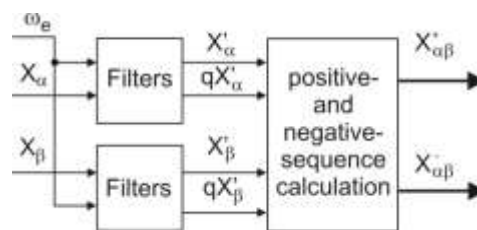

Fig. 2 *General control scheme*

Fig. 3 *Fortescue transformation in the time domain*

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(a) Test signal X_{abc}

(b) Zoom on the test signal X_{abc}

(c) Positive sequence of $X_{\alpha\beta}$

(d) Zoom on the positive sequence of $X_{\alpha\beta}$
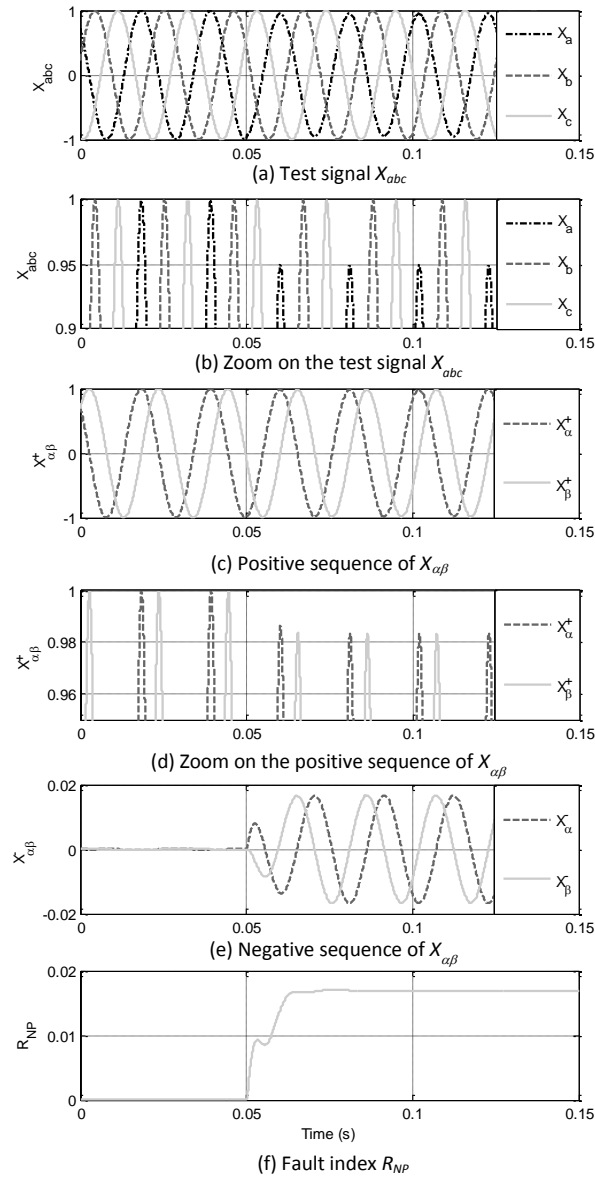
(e) Negative sequence of $X_{\alpha\beta}$

(f) Fault index R_{NP}

Fig. 4 *Simulation results for an unbalance of 0.05 occurring on phase a at time t=0.05s with ω_e=300 rad s^{-1}*
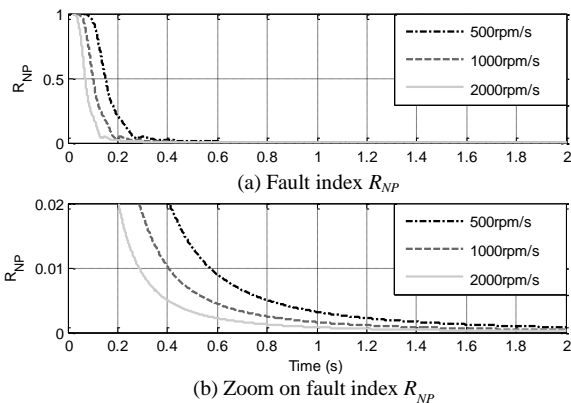
(a) Fault index R_{NP}

(b) Zoom on fault index R_{NP}

Fig. 5 *Simulation of the fault detection scheme under healthy and non-stationary conditions: speed ramp from standstill with different accelerations (balanced three-phase signals with constant peak values and three pole-pairs)*
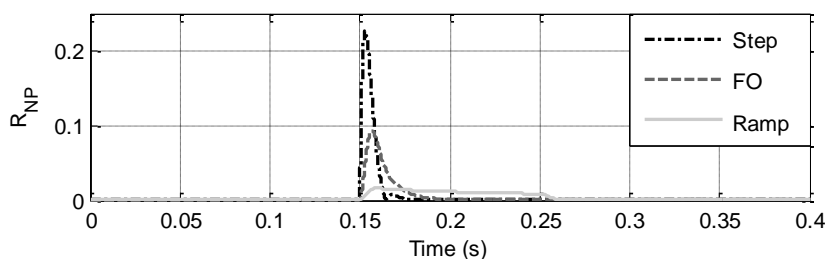
Fig. 6 *Simulation of the fault detection scheme under healthy and non-stationary conditions: load changes from 1pu to 2pu at constant pulsation ω_ε=300 rad s^{-1} and with different dynamics (step, first-order-like response with time constant equal to 0.01s and ramp with slope equal to 10)*
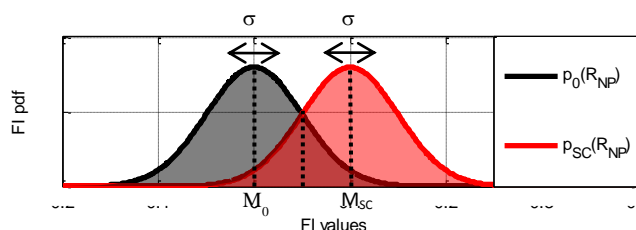
Fig. 7 *Probability density functions of the fault index under healthy and fault conditions.*
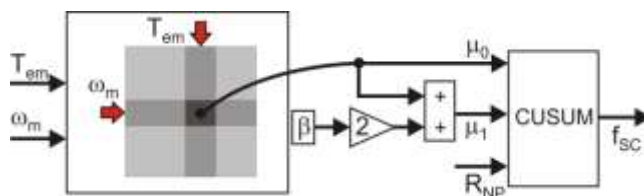
Fig. 8 *Implementation of the CUSUM algorithm for turn-to-turn short-circuit fault detection*
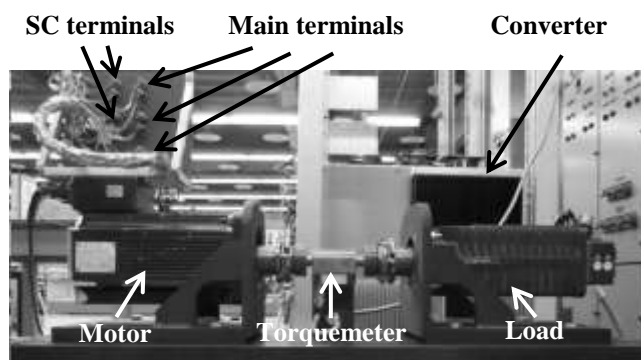
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Fig. 9 *Test bed used for the experimentation*

Fig. 10 *Stator of rewound PMSM with additional turns (only one can be seen in the figure)*
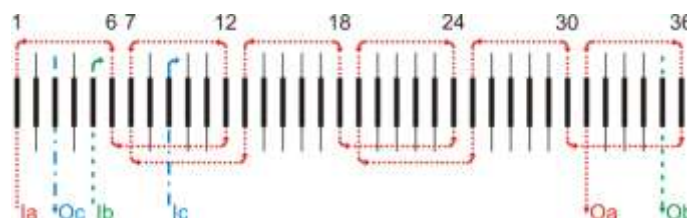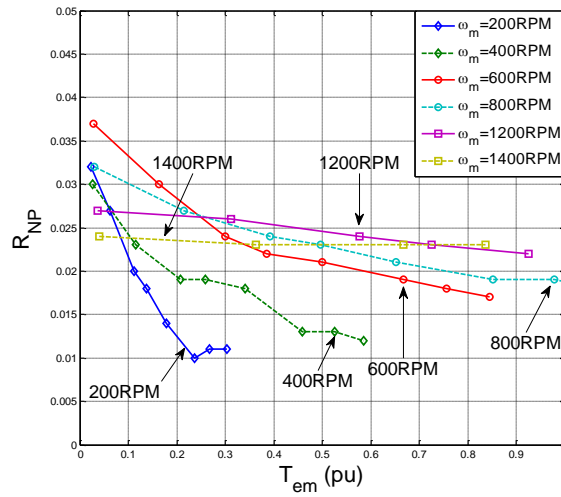

Fig. 11. *Winding pattern of PMSM*

Fig. 12 *Mapping of the residual value of the fault index M_0 in healthy operation as a function of the operating*
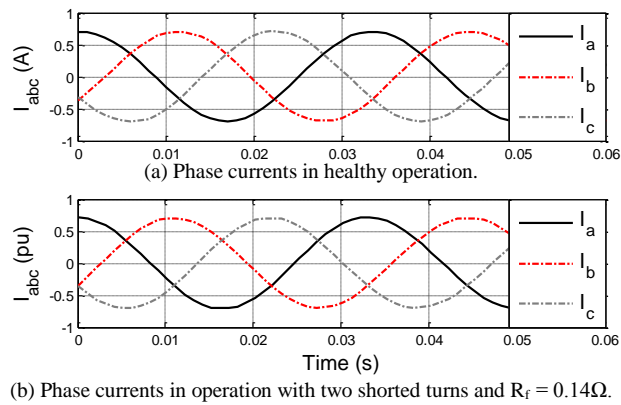
conditions

(a) Phase currents in healthy operation.

(b) Phase currents in operation with two shorted turns and $R_f = 0.14\Omega$.

Fig. 13 *Experimental results showing the sampled phase currents in healthy and faulty conditions.*

(a) Currents expressed in the rotor reference frame.

(b) Measured electromagnetic torque.

(c) Fault index and its reference for the operating conditions.
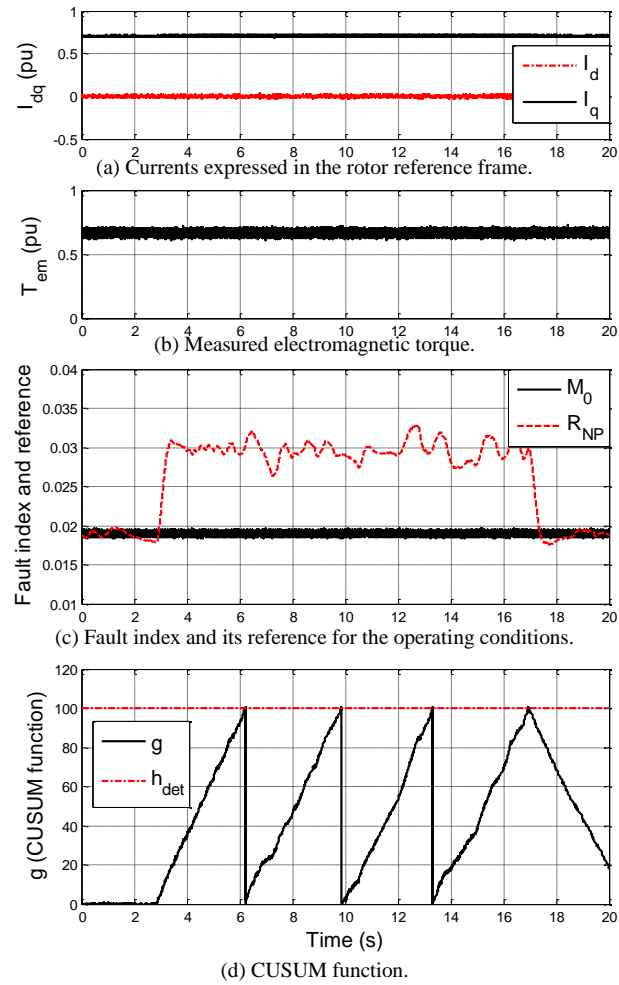
(d) CUSUM function.

Fig. 14 *Experimental results of the fault-detection scheme in steady state with 2 shorted turns out of 182 and $R_f = 0.14\Omega$. Fault occurs at time t=2.85s and disappears at t=17s*

(a) Voltage references expressed in the rotor reference frame.

(b) Magnitude of the voltage positive-sequence (output of the PI

controller).

(c) Magnitude of the voltage negative-sequence (output of the PI
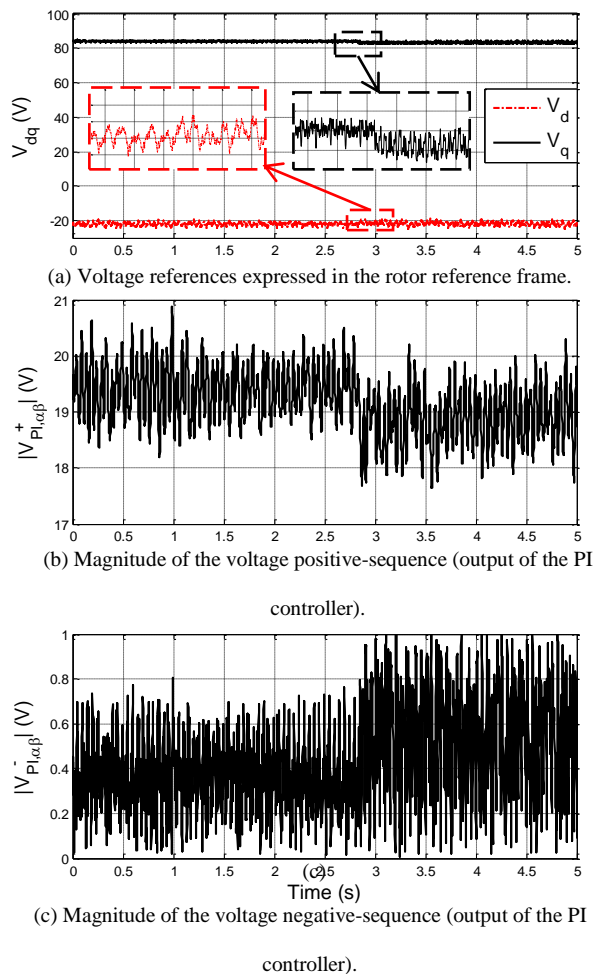
controller).

Fig. 15 *Experimental results showing the effects of a short-circuit fault (2 turns out of 182 and $R_f = 0.14\Omega$) on the voltage references. Fault occurs at time t=2.85s*
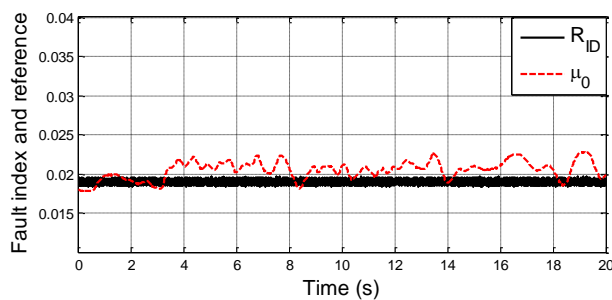

Fig. 16 *Experimental results of the fault-detection scheme in steady state with 1 shorted turn out of 181 and $R_f = 0.06\Omega$. Fault occurs at time t=3s*
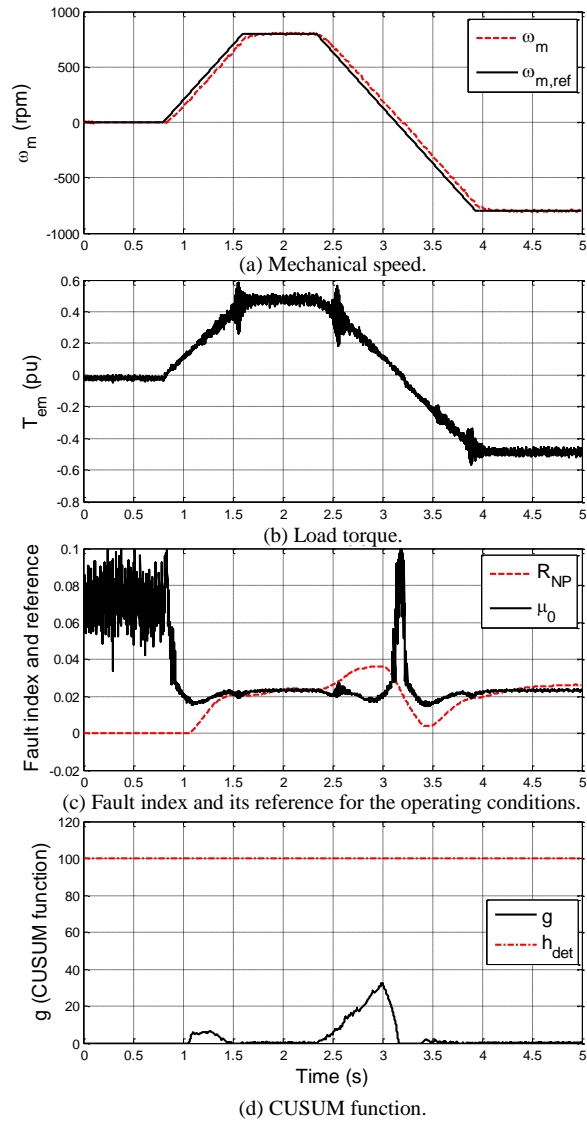
(a) Mechanical speed.

(b) Load torque.

(c) Fault index and its reference for the operating conditions.

(d) CUSUM function.

Fig. 17 *Experimental results of the fault detection scheme in case of transient operation (speed and load ramps) and healthy operation*

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(a) Mechanical speed.

(b) Load torque.

(c) Fault index and its reference for the operating conditions.
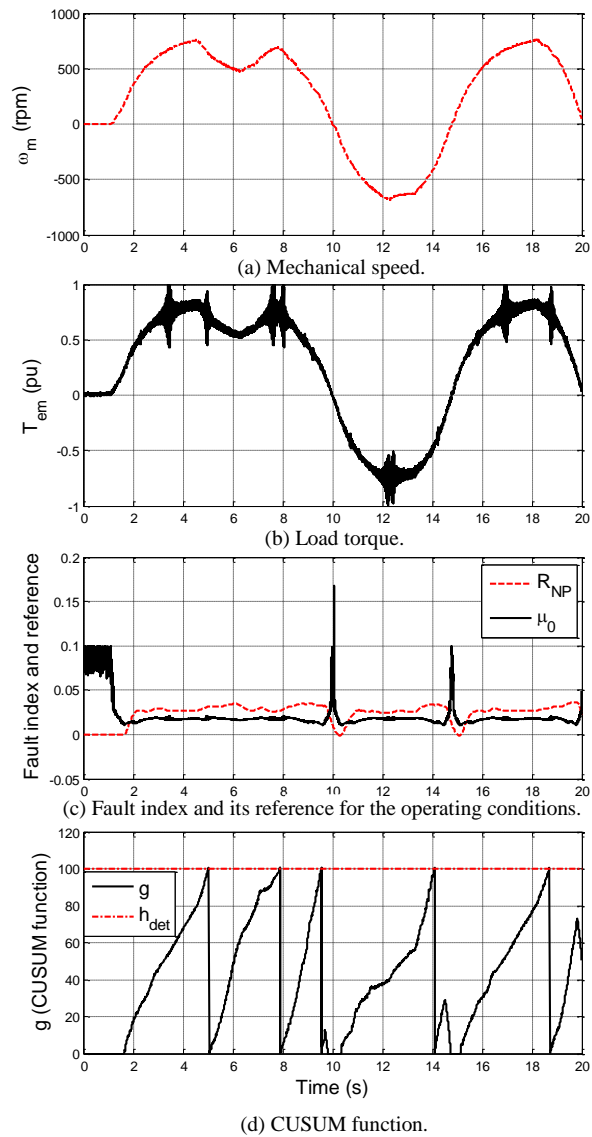
(d) CUSUM function.

Fig. 18 *Experimental results of the fault detection scheme in case of transient operation (random speed profile) with 2 shorted turns*