

Electronic spin transitions and the seismic properties of ferrous iron-bearing MgSiO_3 post-perovskite

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[1] The elastic constants of post-perovskite of chemical composition $\text{Mg}_{0.9375}\text{Fe}_{0.0625}\text{SiO}_3$ and $\text{Mg}_{0.8750}\text{Fe}_{0.1250}\text{SiO}_3$ have been calculated at 0 K and 136 GPa using *ab initio* methods. For both compositions studied, iron remains in a high-spin state below 180 GPa at 0 K. The effect of spin state on elastic properties is small. Logarithmic derivations of isotropic wave velocities and density with respect to ferrous iron content are similar to those predicted from pure end-members. **Citation:** Stackhouse, S., J. P. Brodholt, D. P. Dobson, and G. D. Price (2006), Electronic spin transitions and the seismic properties of ferrous iron-bearing MgSiO_3 post-perovskite, *Geophys. Res. Lett.*, 33, L12S03, doi:10.1029/2005GL025589.

1. Introduction

[2] The bulk of the lower mantle is believed to be composed of iron-bearing magnesium silicate perovskite [Liu, 1975; Knittle and Jeanloz, 1997], coexisting with small amounts of magnesiowüstite and calcium silicate perovskite [Lee *et al.*, 2004], which transforms to a post-perovskite phase 200–400 km from the bottom [Murakami *et al.*, 2005; Ono and Oganov, 2005]. Deeper still, 5–20 km thick ultra-low velocity zones at the base of the mantle [Garnero and Helmberger, 1995] are postulated to comprise iron enriched post-perovskite [Mao *et al.*, 2005], iron-rich partial melt [Rost *et al.*, 2005], or relics of banded iron formation [Dobson and Brodholt, 2005]. In view of the ubiquitous nature of iron in the lower mantle, it is important to know how it may affect the properties of mantle phases, in order to accurately interpret seismic observations and construct good geophysical models.

[3] To estimate the effect of iron on the properties of minerals in the lower mantle is quite complex. Not only does one need to know the amount of iron present in the various phases, but also its crystallographic site, oxidation-state and spin-state. The latter has become of increasing interest since it was shown that iron in both magnesiowüstite and perovskite undergoes a high to low-spin transition under lower mantle pressures [Badro *et al.*, 2003, 2004]. The implications of these transitions may be significant. Because the spin state of iron affects its ionic radius, it could influence partitioning, which could, in turn, lead to seismic discontinuities [Badro *et al.*, 2003]. The spin state of iron in magnesiowüstite also has a large effect on its elastic properties [Lin *et al.*, 2005], which again could affect lower mantle velocity structure. In addition, it is postulated that

because lower mantle minerals incorporating iron in a low-spin state have a higher radiative thermal conductivity than those incorporating iron in a high-spin state, a high to low-spin transition will increase radiative thermal conductivity, hinder convection and favor mantle layering [Badro *et al.*, 2004].

[4] Investigations of the elastic properties of pure end-member FeSiO_3 post-perovskite found iron to be in a high-spin anti-ferromagnetic state at mantle pressures [Caracas and Cohen, 2005; Stackhouse *et al.*, 2006], but the spin state for lower and more appropriate concentrations is not known. In addition, because pure end-member FeSiO_3 post-perovskite was found to be dynamically unstable with iron in a low-spin state, its elastic properties could not be determined. Therefore at present we have no estimate of the extent to which the elastic properties of iron-bearing post-perovskite phase changes as iron goes from a high to low-spin state.

[5] Here we report the results of *ab initio* calculations on post-perovskite with composition $\text{Mg}_{0.9375}\text{Fe}_{0.0625}\text{SiO}_3$, similar to that expected in the lowermost mantle [Murakami *et al.*, 2005], and $\text{Mg}_{0.8750}\text{Fe}_{0.1250}\text{SiO}_3$. Estimated spin transition pressures for iron are presented for both post-perovskite compositions, along with the elastic properties with iron in both spin states. The possible geophysical implications of these are discussed, in particular, with regard to seismic discontinuities and mantle dynamics.

2. Computational Details

[6] It is well known that standard density functional methods fail to predict the correct band structure of strongly correlated systems (typically those containing metal ions with partially filled *d* or *f* shells). For example, both Fe_2SiO_4 [Cococcioni *et al.*, 2003] and FeO [Alfredsson *et al.*, 2004] are predicted to be metals when they are insulators. This has led to the use of advanced techniques, such as hybrid functionals [Alfredsson *et al.*, 2004], which compute their correct band structure. It is often assumed, however, that although standard density functional methods are unable to determine accurate band structure, they may still be employed to calculate other important properties such as magnetic state, lattice parameters, bulk and shear moduli. Several studies using density functional methods to determine the spin state of iron in pertinent minerals [Cococcioni *et al.*, 2003; Li *et al.*, 2005a] have found good agreement with experiment. Others have used them to calculate the elastic properties of iron-bearing silicate perovskite [Li *et al.*, 2005b]. Further calculations using mixed functionals are necessary to confirm the validity of our results.

[7] Experimental studies of iron partitioning amongst lower mantle mineral phases [Murakami *et al.*, 2005;

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Table 4. Calculated Density and 0 K Elastic Moduli of Iron-Bearing MgSiO_3 Post-Perovskite (in GPa)

P/GPa	Spin State		$\rho/\text{g cm}^{-3}$	C_{11}	C_{22}	C_{33}	C_{12}	C_{13}	C_{23}	C_{44}	C_{55}	C_{66}	K	G
	Fe_{Mg}	$\text{Fe}_{\text{Mg}'}$												
136	-	-	5.528	1332	995	1318	461	362	525	291	279	442	702	345
						$\text{MgSiO}_3^{\text{a}}$								
136	0/2	-	5.631	1331	992	1314	477	360	526	297	270	451	705	344
136	4/2	-	5.624	1326	992	1320	474	362	525	293	275	437	704	343
						$\text{Mg}_{0.9375}\text{Fe}_{0.0625}\text{SiO}_3$								
						$\text{Mg}_{0.8750}\text{Fe}_{0.1250}\text{SiO}_3$ – SSM2 Model								
136	0/2	-0/2	5.729	1318	987	1302	488	369	528	290	237	426	706	327
136	4/2	-4/2	5.716	1311	989	1317	482	372	525	288	271	431	706	337
136	4/2	-4/2	5.716	1311	989	1317	482	372	525	288	271	431	706	337
						$\text{Mg}_{0.8750}\text{Fe}_{0.1250}\text{SiO}_3$ – SSM4 Model								
136	0/2	-0/2	5.732	1319	983	1304	489	369	528	285	247	433	706	329
136	4/2	-4/2	5.718	1310	987	1318	483	372	524	289	272	429	706	337
136	4/2	-4/2	5.716	1311	989	1316	483	372	525	288	271	431	706	337
						$\text{FeSiO}_3^{\text{b}}$								
136	4/2	-4/2	6.947	1174	993	1236	543	486	550	192	221	320	727	261

^aTaken from *Stackhouse et al.* [2005].^bTaken from *Stackhouse et al.* [2006].

layers, as the layers are compressed the tilting of the silica octahedra pushes them into one another, thereby lowering their spin transition pressure.

[11] Our results indicate that, in post-perovskite, ferrous iron remains in a high-spin state up to 180 GPa at 0 K. Taking into account temperature is expected to increase transition pressures [*Badro et al.*, 2004]. According to the arguments of *Badro et al.* [2004], this could mean that radiative thermal conductivity will be low in the lower mantle. This should be taken into account when considering the dynamics of the lower mantle. The spin state of ferric iron in post-perovskite, under lower mantle conditions, is unknown. Further work must be done to investigate this.

[12] Elastic constants for selected post-perovskite models are reported in Table 4. Incorporation of iron into MgSiO_3 post-perovskite results in an expected density increase, a larger bulk modulus and lower shear modulus. This confirms previous work [*Stackhouse et al.*, 2006] where the affect of incorporating ferrous iron on the elastic and seismic properties of MgSiO_3 post-perovskite was estimated from linear mixing of end-member properties. Figure 1

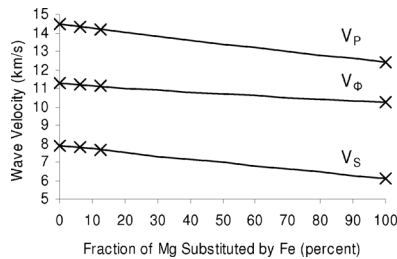


Figure 1. Decrease in compressional (V_p), shear (V_s) and bulk (V_ϕ) isotropic wave velocities for post-perovskite as a function of ferrous iron content at 136 GPa and 0 K. Solid lines represent values calculated from linear mixing of pure end-member properties, taken from *Stackhouse et al.* [2005, 2006], while markers show values calculated for models incorporating an explicit percentage of iron.

shows how compressional (V_p), shear (V_s) and bulk (V_ϕ) isotropic wave velocities of post-perovskite vary as a function of ferrous iron content. Solid lines represent values calculated from linear mixing of densities, bulk and shear moduli of the MgSiO_3 and FeSiO_3 end-members, taken from *Stackhouse et al.* [2005, 2006], while markers show values from the present study. One can see that, linear mixing provides excellent estimates of seismic velocities. This validates previous estimations of the seismic properties of an iron-rich post-perovskite phase [*Stackhouse et al.*, 2006], which were found to be compatible with those often seen for ultra-low velocity zones. Useful derivatives of elastic and seismic properties of post-perovskite with respect to ferrous iron content are given in Table 5. The slight affect of small amounts of iron on the seismic properties of post-perovskite strengthens previous arguments for the compatibility of the phase with observations for the lowermost mantle [*Wookey et al.*, 2005].

[13] The spin state of iron appears to have only a small effect on the elastic properties of post-perovskite, at least when present in the small fractions studied here. This is similar to observations for ferric iron in perovskite [*Li et al.*, 2005b]. It is surprising in light of recent experimental work reporting it to have a large effect on the bulk modulus of magnesiowüstite (composition $\text{Mg}_{0.83}\text{Fe}_{0.17}\text{O}$) [*Lin et al.*,

Table 5. Derivatives of Seismic Properties and Density of (Mg, Fe) SiO_3 Post-Perovskite With Respect to Iron Content at 136 GPa and 0 K^a

	Derivative
$\partial \ln \rho / \partial \text{Fe}$	0.2261
$\partial \ln K / \partial \text{Fe}$	0.0349
$\partial \ln G / \partial \text{Fe}$	-0.2870
$\partial \ln V_p / \partial \text{Fe}$	-0.1532
$\partial \ln V_s / \partial \text{Fe}$	-0.2566
$\partial \ln V_\phi / \partial \text{Fe}$	-0.0956

^aFe = fraction of Mg substituted by Fe.

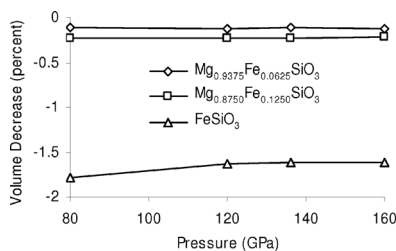


Figure 2. Difference in volume for post-perovskite containing ferrous iron in a high and low-spin state at 0 K, as a function of composition and pressure. FeSiO₃ values taken from Stackhouse et al. [2006].

2005]. It is important to note, however, that for a given iron to magnesium ratio, the volume fraction of iron in magnesiowüstite is two and a half times that of post-perovskite, due to their different formula units. In addition, the authors of the experimental investigation [Lin et al., 2005] report the contrast between the bulk moduli at 60 GPa. One can see in Figure 2 how the volume difference for post-perovskite containing ferrous iron in a high and a low-spin state increases with iron content, but decreases with pressure. One should, therefore, perhaps not expect such a large contrast in bulk modulus in post-perovskite at 136 GPa, as that reported for magnesiowüstite at 60 GPa [Lin et al., 2005].

[14] In conclusion, ferrous iron incorporated into magnesium silicate post-perovskite is expected to be in a high-spin state across the entire pressure range of the lower mantle, and this should be taken into account when considering the dynamics of the region. Incorporation of low amounts of ferrous iron into the post-perovskite phase has only a slight affect on its elastic properties, irrespective of spin state, which are compatible with seismic observations for the lowermost mantle.

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