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Curie temperature of multiphase nanostructures

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The Curie temperature and the local spontaneous magnetization of ferromagnetic nanocomposites are investigated. The macroscopic character of the critical fluctuations responsible for the onset of ferromagnetic order means that there is only one Curie temperature, independent of the number of magnetic phases present. The Curie temperature increases with the grain size and is, in general, larger than predicted from the volume averages of the exchange constants. However, the Curie-temperature enhancement is accompanied by a relative reduction of the spontaneous magnetization. Due to the quadratic dependence of the permanent-magnet energy product on the spontaneous magnetization, this amounts to a deterioration of the magnets performance. The length scale on which an effective intergranular exchange coupling is realized (coupling length) depends on the Curie-temperature difference between the phases and on the spacial distribution of the local interatomic exchange. As a rule, it is of the order of a few interatomic distances; for much bigger grain sizes the structures mimic an interaction-free ensemble of different ferromagnetic materials. This must be compared to the magnetic-anisotropy coupling length, which is of the order of 10 nm. The difference is explained by the nonrelativistic character of the Curie-temperature problem. © 2000 American Institute of Physics. [S0021-8979(00)63608-3]

I. INTRODUCTION

The onset of long-range order in ferromagnets has been a long-standing and mind-stimulating problem. Since the first third of the 20th century, when research focussed on the basic relation between quantum mechanics and magnetic order, ^{1,2} interest has shifted towards critical phenomena^{3,4} and the behavior of particular magnetic features such as surfaces^{5,6} and artificial structures. ^{7–13} In the case of multilayers, mean-field Curie temperatures are obtained by diagonalizing tridiagonal exchange-interaction matrices, ^{7–10} whereas Wang and Mills¹¹ used a Landau–Ginzburg type analysis to elaborate that the spontaneous magnetization varies continuously across phase boundaries.

A problem of scientific and technological interest is the Curie-temperature and spontaneous-magnetization behavior of nanocomposites. There are attempts to use the concept of exchange-field penetration known from multilayers to construct effective coupling parameters, 14 but there is no comprehensive theoretical understanding of nanocrystalline alloys. A particular question, important in the context of hightemperature permanent magnetism, is whether the Curie temperature T_L of any magnetic material can be improved by nanoscale exchange coupling to a phase having a Curie temperature $T_H > T_L$. In the context of magnetic hysteresis, it has been shown that interatomic exchange can be exploited to improve the hard-magnetic performance of a magnet by adding soft-magnetic material. 15,16 In that case, the coupling between the hard and soft regions is very effective on length scales up to about 10 nm.

II. CALCULATION AND RESULTS

A. Curie temperature and spontaneous magnetization

Let us start with a mean-field analysis of ferromagnetic nanocomposites. By definition, the spontaneous magnetization vanishes at the Curie temperature, so that the mean-field equations can be linearized and the spontaneous magnetization $M_i = M_z(\mathbf{r}_i)$ of the *i*th atom obeys

$$TM_i = \frac{1}{k_B} \sum_j J_{ij} M_j. \tag{1}$$

In this equation, the $J_{ij} = J(\mathbf{r}_i - \mathbf{r}_J)$ are local exchange parameters whose detailed meaning depends on the underlying model. Diagonalization of Eq. (1) yields a common Curie temperature, which is equal to the highest eigenvalue of the matrix J_{ii}/k_B . For multilayers, it has been found that the Curie temperature increases with increasing layer periodicity. 7,9 In the case of three-dimensional nanostructures, of arbitrary geometry, the matrix J_{ii}/k_B is no longer tridiagonal and the diagonalization is slightly more complicated. Figure 1 shows cubic inclusions of a material with a high (bulk) Curie temperature T_H in a matrix of a material having a low (bulk) Curie temperature $T_L < T_H$. The bars show the Curie temperatures for $T_H = 1000 \,\mathrm{K}$, $T_L = 400 \,\mathrm{K}$, and an intermediate nearest-neighbor interface exchange of $J_{ii}/k_B = 700/6$. As in the case of multilayers, T_C increases with the size of the T_H and T_L regions, and the composite Curie temperature is close to T_H .

The eigenmode belonging to T_C gives the spacial variation of the order parameter in the vicinity of T_C . [The other eigenvalues and eigenmodes of Eq. (1) have no physical meaning, because the spontaneous magnetization is finite below T_C and the mean-field equations are no longer linear.] Below T_C , the Brillouin-type nonlinearity of the mean-field

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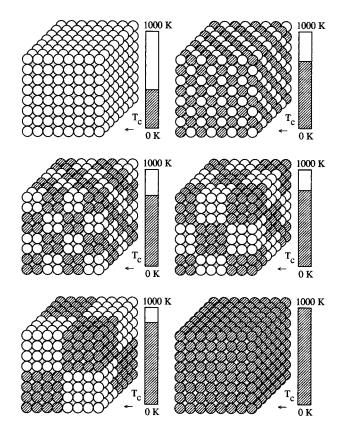


FIG. 1. Mean-field Curie temperatures of three-dimensional composites. The dark and bright areas correspond to high and low bulk Curie temperatures T_H = 1000 K and T_L = 400 K, respectively.

equations is important. For N nonequivalent sites, the local spontaneous magnetization $M_i(T)$ is obtained by solving the set of N nonlinear mean-field equations. Figure 2 shows a typical result for N=4 and classical $(J=\infty)$ Heisenberg spins. The considered structure exhibits four nonequivalent sites, one T_H site and three T_L sites, and each nonequivalent site has a different spontaneous magnetization below T_C . In

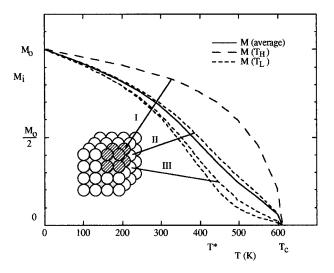


FIG. 2. Temperature dependence of the local spontaneous magnetization (classical Heisenberg model). There are four nonequivalent sites: one T_H site and three T_L sites. The T_L are classified by their position relative to the T_H site: nearest neighbors, neighbors connected by face diagonals, and neighbors connected by cube diagonals. The Curie temperature is 611.9 K.

the T_L phase, the spontaneous magnetization is largest for sites which are nearest neighbors to T_H sites. This is related to the above-mentioned continuity of the order parameter at phase boundaries and shows that the spontaneous magnetization is not element specific but depends on the distance from the T_H — T_L interfaces.

The lower single-phase Curie temperature T_L does not translate into any phase transition, although there are resonance-like magnetization features at some nonsingular temperature $T^* \approx T_L$ (Fig. 2). This is reminiscent of the many-sublattice behavior of garnets and rare-earth transition-metal intermetallics: 12,16,17 the rare-earth (or " T_L ") atoms are subject to the quasiparamagnetic exchange field of the iron-series (or " T_H ") atoms.

Above the thermodynamically not very well defined temperature T^* , the spontaneous magnetization for T_L sites far away from T_H sites is very low, but it remains nonzero between T^* and T_C . This smallness of the T_L magnetization is of practical importance. In particular, the quadratic dependence of the permanent-magnet energy product on the spontaneous magnetization 15,16 means that the exchange coupling between T_H and T_L nanocrystallites is not accompanied by an improvement of the material's permanent magnetic performance. In fact, the T_H phase dilutes the magnet's magnetization and reduces the energy product.

B. Range of exchange coupling

To analyze the coupling between T_H and T_L regions we transform Eq. (1) into a partial differential equation. Expanding $M_j = M_z[\mathbf{r}_i + (\mathbf{r}_j - \mathbf{r}_i)]$ in terms of $\mathbf{r}_j - \mathbf{r}_i$ and taking into account that $|\mathbf{r}_j - \mathbf{r}_i| = a$ for simple-cubic lattices with nearest-neighbor interactions we obtain after short calculation

$$\frac{a^2}{7}\nabla[T_o(\mathbf{r})\nabla M_z] + [T_o(\mathbf{r}) - T]M_z = 0.$$
 (2)

Here $T_o(\mathbf{r}) = zJ_o(\mathbf{r})/k_B$ is a local Curie-temperature parameter so that $T_o(\mathbf{r}) = T_L$ and $T_o(\mathbf{r}) = T_H$ in the T_L and T_H phases, respectively. For homogeneous magnets, $M_z(\mathbf{r}) = M_s$ and $T_C = T_o = T_L = T_H$, but in general Eq. (2) has to be interpreted as a generalized Landau–Ginzburg equation. It differs from the corresponding expression in Ref. 11 by containing the term $\nabla [T_o(\mathbf{r})\nabla M_z]$ rather than the $\nabla^2 M_z$ Landau–Ginzburg term. As analyzed in the context of two-phase micromagnetism, ¹⁵ the main effect of the inhomogeneous differential operator is to make the gradient of the eigenfunction discontinuous at phase boundaries. This modifies T_C but leaves the behavior of the spontaneous magnetization in a given phase unchanged.

Let us now consider the spontaneous magnetization in the T_L phase. The interesting temperature region is between T^* and T_C , because above T_C there is no ferromagnetism and below T_L the spontaneous magnetization is close to saturation throughout the magnet. We ask to what extent the T_H phase is able to create an appreciable spontaneous magnetization in the T_L phase. In the considered regime, Eq. (2) yields correlations which decay exponentially with the decay length (correlation length)

$$\xi_L = \frac{a}{\sqrt{z}} \sqrt{\frac{T_L}{T - T_L}}.$$
 (3)

The correlation length diverges at T_L , but it decreases with increasing temperature and is of the order of $(a/\sqrt{z})\sqrt{T_L/(T_H-T_L)}$ in the vicinity of the Curie temperature. In other words, the coupling or "penetration" length is large when $T_H{\approx}T_L$ but does not exceed a few interatomic distances for $T_L{<}T_H{\approx}T_C$, that is for materials of interest in two-phase permanent magnetism. The exponential decay of the spontaneous magnetization $M_z(\mathbf{r})$ in T_L regions quantifies our finding that $M_z(r)$ is very small in the centers of extended T_L regions.

This scenario is not restricted to the mean-field approximation. Due to renormalization-group effects it is necessary to replace Eq. (3) in the vicinity of T_L by 18

$$\xi_L \approx a \left(\frac{T_L}{T - T_L}\right)^{\nu},$$
 (4)

where ν is equal to 0.63 and 0.71 for the three-dimensional Ising and Heisenberg models, respectively. However, in the present context Eq. (4) yields only minor corrections to Eq. (3). For example, ¹⁸ grain radii R of order 5 nm give rise to an "effective Curie-temperature enhancement" of about 1%.

III. DISCUSSION

The spacial variation of the spontaneous magnetization and the existence of a unique Curie temperature T_C mean that there are neither element-specific magnetization curves in inhomogeneous structures nor order parameters vanishing at different temperatures. However, depending on the phases and coupling mechanism involved, the site-dependent average spontaneous magnetization of the T_L phase may be virtually undetectable. In that case, an exteremely high temperature resolution is necessary to distinguish a composite structure from a superposition of single-phase structures.

It is important to emphasize that Eq. (1) is model independent, that is for appropriately rescaled exchange constants it applies equally well to, e.g., Ising and Heisenberg models. By contrast, due to the nontrivial involvement of the Brillouin functions, the temperature dependence of the local spontaneous magnetization is lattice- and model-dependent. However, this does not affect the characteristic involvement of the different nonequivalent sites shown in Fig. 2. 18

Aside from the secondary dependence on $T-T_L$, the coupling length scales as the interatomic distance, that is ultimately as the Bohr radius $a_0 = 0.529 \,\text{Å}$. This must be compared with the "micromagnetic" coupling length (exchange length) $a_0/\alpha = 7.52 \, \text{nm}$, where $\alpha = 1/137$ is Sommerfeld's fine structure constant. To explain this difference we note that the inhomogenity $T_o(\mathbf{r}) - T$ in Eq. (2) is analog to

the inhomogenity term $2K_1(\mathbf{r}) - \mu_0 H_N M_s$ in Ref. 15. However, anisotropies (K_1) and nucleation fields (coercivities) H_N are small relativistic corrections to the leading Coulomb and exchange energies. (In temperature units, they are of the order of 1 K, that is much smaller than T_C . ¹⁶) Since both the micromagnetic coupling in Ref. 15 and the present "Curie-temperature" interaction are realized by interatomic exchange, Curie-temperature disorder is much more effective in reducing the magnetic order than anisotropy disorder.

IV. CONCLUSIONS

In nanocomposites, there is only one Curie temperature T_C , independent of the bulk Curie temperatures of phases involved. The Curie temperature is higher than the volume average of the Curie temperatures of the individual phases. Below T_C , the spontaneous magnetization is site dependent but nonzero throughout the magnet, because regions with strong exchange coupling polarize all other sites. However, in the middle of extended regions with low single-phase Curie temperatures the spontaneous magnetization may be very low, and for large crystallite sizes the overall behavior of the magnet is reminiscent of an interaction-free ensemble of two (or more) ferromagnets with two (or more) Curie temperatures. Due to the nonrelativistic character of the interatomic exchange, the Curie-temperature coupling range is atomic rather than nanoscale, so that the comparatively high Curie temperatures of nanocomposites do not translate into an enhanced permanent-magnet energy product.

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<sup>1</sup>W. Heisenberg, Z. Phys. 49, 619 (1928).
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²E. Ising, Z. Phys. **31**, 253 (1925).

³L. Onsager, Phys. Rev. **65**, 117 (1944).

⁴K. G. Wilson, Rev. Mod. Phys. **55**, 583 (1983).

⁵K. Binder and P. C. Hohenberg, Phys. Rev. B **9**, 2194 (1974).

⁶R. Skomski, C. Waldfried, and P. A. Dowben, J. Phys.: Condens. Matter 10, 5833 (1998).

⁷H.-R. Ma and Ch.-H. Tsai, Solid State Commun. **55**, 499 (1985).

⁸H. K. Sy, Phys. Lett. A **120**, 203 (1987).

⁹W. Maciejewski and A. Duda, Solid State Commun. **64**, 557 (1987).

¹⁰W. Maciejewski, IEEE Trans. Magn. **26**, 213 (1990).

¹¹R. W. Wang and D. L. Mills, Phys. Rev. B **46**, 11681 (1992).

¹²R. Skomski, J. Appl. Phys. 83, 6724 (1998).

¹³ U. Bovensiepen, F. Wilhelm, P. Srivastava, P. Poulopoulos, M. Farle, A. Ney, and K. Baberschke, Phys. Rev. Lett. 81, 2368 (1998).

¹⁴I. Navarro, M. Ortuño, and A. Hermando, Phys. Rev. B 53, 11656 (1996).

¹⁵R. Skomski and J. M. D. Coey, Phys. Rev. B 48, 15812 (1993).

¹⁶R. Skomski and J. M. D. Coey, *Permanent Magnetism* (Institute of Physics, Bristol, 1999).

¹⁷ A. Herpin, *Théorie du Magnétisme* (Institut National des Sciences et Techniques Nucléaires, Saclay, 1968).

¹⁸R. Skomski (unpublished).

¹⁹R. Skomski, H.-P. Oepen, and J. Kirschner, Phys. Rev. B **58**, 3223 (1998).