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Prospect Relativity: How Choice Options Influence Decision Under Risk

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Abstract

In many theories of decision under risk (e.g., expected utility theory, rank dependent utility theory, and prospect theory) the utility or value of a prospect is independent of other prospects or options in the choice set. The experiments presented here show a large effect of the available options set, suggesting instead that prospects are valued relative to one another. The judged certainty equivalent is strongly influenced by the options available. Similarly, the selection of a preferred option from a set of prospects is strongly influenced by the prospects available. Alternative theories of decision under risk (e.g., the stochastic difference model, multialternative decision field theory, and range frequency theory), where prospects themselves or prospect attributes are valued relative to one another, can provide an account of these context effects.

Prospect Relativity: How Choice Options Influence Decision Under Risk

Human behavior, as distinct from mere unintentional movement, results from decision. And decisions almost always involve trading-off risk and reward. In crossing the road, we balance the risk of accident against the reward of saving time; in choosing a shot in tennis, we balance the risk of an unforced error against the reward of a winner. Choosing a career, a life-partner, or whether to have children, involves trading off different balances between the risks and returns of the prospects available. Understanding how people decide between different levels of risk and return is, therefore, a central question for psychology.

Understanding how people trade off risk and return is also a central issue for economics. The foundations of economic theory are rooted in models of individual decision making. For example, to explain the behavior of markets we need a model of the decision making behavior of buyers and sellers in those markets. Most interesting economic decisions involve risk. Thus, an economic understanding of markets for insurance, of risky assets such as stocks and shares, of the lending and borrowing of money itself, and indeed of the economy at large, requires understanding how people trade risk and reward.

In both psychology and economics, the starting point for investigating how people make decisions involving risk has not been empirical data on human behavior. Instead, the starting point has been a normative theory of decision making, expected utility theory (first axiomatized by von Neumann & Morgenstern, 1947) which specifies how people ought to make decisions and plays a key role in theories of rational choice (for a review see Shafir & LeBoeuf, 2002). The assumption has then been that, to an approximation, people do make decisions as they ought to, that is, expected utility theory can be viewed as a descriptive, as well as a normative, theory of human behavior. At the core of expected utility theory is the assumption that people make choices that maximize their utility, and they value a risky option by the expected utility (in a probabilistic sense of expectation) that it will provide. In general, the prospect $(x_1, p_1; x_2, p_2; ... ; x_n, p_n)$, where outcome x_i occurs with probability p_i,

and $p_1 + p_2 + ... + p_n = 1$, has expected utility (hereafter EU),

$$U(x_1, p_1; x_2, p_2; ...; x_n, p_n) = p_1 u(x_1) \quad p_2 u(x_2) \quad ... \quad p_n u(x_n) \tag{1}$$

(The function U gives the utility of a risky prospect. The function u is reserved for the utility of certain outcomes only.)

In psychology and experimental economics, there has been considerable interest in probing the limits of this approximation, that is, finding divergence, or agreement, between EU theory and actual behavior (e.g., Kagel & Roth, 1995; Kahneman, Slovic & Tversky, 1982; Kahneman & Tversky, 2000). In economics more broadly, there has been interest in how robust economic theory is to anomalies between EU theory and observed behavior (for a range of views, see, e.g., Akerlof & Yellen, 1985; de Canio, 1979; Cyert & de Groot, 1974; Friedman, 1953; Nelson & Winter, 1982; Simon, 1959, 1992).

The present paper demonstrates a new and large anomaly for EU theory in decision making under risk. Specifically, we report results that seem to indicate that people do not possess a well-defined notion of the utility of a risky prospect and hence, a fortiori, they do not view such utilities in terms of EU. Instead, people's perceived utility for a risky prospect appears highly context sensitive. We call this phenomenon *prospect relativity*. Considerable further work is, of course, required to establish the generality and scope of our results across the vast array of decision making domains of psychology and economic interest. But we believe that these anomalies are sufficiently striking to motivate the attempt to explore them further.

Motivation from Psychophysics

In judging risky prospects, people must assess the magnitudes of risk and return that they comprise. The motivation for the experiments presented here was the idea that some of the factors that determine how people assess these magnitudes might be analogous to factors underlying assessment of psychophysical magnitudes, such as loudness or weight. Specifically, people appear poor at providing stable absolute judgments of such magnitudes

and are heavily influenced by the options available to them. For example, Garner (1954) asked participants to judge whether tones were more or less than half as loud as a 90 dB reference loudness. Participants' judgments were entirely determined by the range of tones played to them. Participants played tones in the range 55-65 dB had a half-loudness point, where their judgments were more than half as loud 50% of the time and less than half as loud 50% of the time, of about 60 dB. Another group, who received tones in the range 65-75 dB had a half-loudness point of about 70 dB. A final group, who heard tones in the range 75-85 dB, had a half-loudness point of about 80 dB. Laming (1997) provides an extensive discussion of other similar findings. Context effects, like those found by Garner (1954), are consistent with participants making perceptual judgments on the basis of relative magnitude information, rather than absolute magnitude information (Laming, 1984, 1997; Stewart, Brown, & Chater, 2002a, 2002b). If the attributes of risky prospects behave like those of perceptual stimuli, then similar context effects should be expected in risky decision making. This hypothesis motivated the experiments in this paper, which are loosely based on Garner's (1954) procedure.

<center>Existing Experimental Investigations</center>

A small number of experiments has already investigated the effect of the set of available options in decision under risk. Mellers, Ordóñez and Birnbaum (1992) measured participants' attractiveness ratings and buying prices (i.e., the price that a participant would pay to obtain a single chance to play the prospect and receive the outcome) of simple binary prospects of the form "p chance of x" presented within two different sets of prospects. In one context, the distribution of expected values of accompanying prospects was positively skewed, and in the other context, the distribution of expected values was negatively skewed. Attractiveness ratings were significantly influenced by this manipulation, with higher ratings for prospects in the positive skew condition than for the same prospects in the negative skew condition. However, context had a minimal effect on buying price. With more complicated

prospects of the form "p chance of x otherwise y", the effect of skew on buying price was slightly larger. The large effect that the set of options available had on attractiveness ratings and much smaller effect on buying price is consistent with a similar demonstration by Janiszewski and Lichtenstein (1999). They gave participants a set of prices for different brands of the same product to study. The prices varied in range. The range had an effect on judgments of the attractiveness of a new price, but not on the amount participants would expect to pay for a new product.

The set of options available as potential certainty equivalents (hereafter CEs) has been shown to affect the choice of CE for risky prospects. In making a CE judgment, a participant suggests, or selects from a set of options, the amount of money for certain that is worth the same to him or her as a single chance to play the prospect. We shall consider CE judgments extensively in our experiments. Birnbaum (1992) demonstrated that skewing the distribution of options offered as CEs for simple prospects, whilst holding the maximum and minimum constant, influenced the selection of a CE. When the options were positively skewed (i.e., most values were small) prospects were under-valued compared to when the options were negatively skewed (i.e., most values were large).

MacCrimmon, Stanbury and Wehrung (1980) present some evidence that the set in which a prospect is embedded can affect judgments about the prospect. They presented participants with two sets of five prospects to be ranked in order of attractiveness. The expected value of each prospect was constant across all prospects and both sets. There were two prospects in common between the two sets. If context provided by the other prospects in a set did not affect the attractiveness of a prospect, each participant should have consistently ranked one prospect as more attractive than the other, in both sets. MacCrimmon et al. found that 9 of a total of 40 participants had a different ordering of the two prospects in the two sets. They argue that this is not merely inconsistency because these participants made consistent rankings within a set, and instead reflects the influence of the other prospects in the choice

set. Following this logic, however, it would take only one participant to have a different ordering of the two prospects, but who otherwise behaved consistently, to conclude that there was an effect of choice set. A random fluctuation in risk aversion between sets might produce this result. With such a small number of data points, and no concrete null hypothesis allowing a significance test to be made, any conclusion based on this results must be very tentative.

In summary, there is an effect of previously-considered prospects on the attractiveness rating assigned to a current prospect, and also a small effect on buying price. Moreover, the context provided by a set of values from which a CE is to be chosen affects CE judgments. Finally, in choosing between prospects there is a suggestion that the wider choice may affect preferences between identical pairs of prospects. In the experiments below we find large and systematic effects of choice set (both potential CEs and accompanying prospects) on the valuation of individual prospects. These effects are not compatible with EU theory or some of its most influential variants, according to which the value of a prospect is independent of other available options. These results are, though, compatible with a variety of models that discard this "independence" assumption concerning the value of prospects.

Summary of Experiments

As indicated above, in this paper we adapt methodologies from psychophysics to investigate the possibility of that context effects influence decision under risk. The aim of Experiments 1A-1C was to determine whether options offered as potential CEs influence estimates of a prospect's CE. We consistently found substantial effects. In Experiment 2, we introduce a new procedure to investigate these effects in which, under certain assumptions, it is optimal for participants to provide truthful CEs. In Experiment 3, we examine whether these effects are similar to those observed in magnitude estimation tasks. In the remaining two experiments, Experiments 4 and 5, we investigate whether the effect of available options arises in choices between prospects as well as in CE judgments about prospects.

Experiment 1A

Following a similar logic to Garner's (1954) loudness judgment experiment described above, participants were given a set of options as possible CEs for each prospect. Participants were asked to decide on a CE for the prospect, and then select the option closest to their estimate.[1] For each prospect, options were either all lower in value than the mean free choice CE (given by another group of participants) or all higher, as illustrated in Figure 1. If a participant is not influenced by the set of options, then his or her choice of option should be that nearest to his or her free choice CE. Under this hypothesis, the expected proportion of times each option will be chosen can be calculated by integrating the free choice distribution between appropriate bounds. The key prediction is that the highest option in the low condition (L_4) and the lowest option in the high condition (H_1) should be chosen more than half of the time. This prediction holds for any symmetrical distribution of free choice CEs. Alternatively, if participants' responses are solely determined by the set of options presented to them, then the distribution of responses across options should be the same for both the low and the high value range of option CEs.

Method

Participants. Free choice CEs were given by 14 undergraduates from the University of Warwick. Another 16 undergraduates chose CEs from sets of options. All participated for course credit.

Design. A set of 20 prospects, each of the form "*p* chance of *x*", was created by crossing the amounts £200, £400, £600, £800, and £1000 with the probabilities .2, .4, .6, and .8. Participants were presented with the prospects, and asked to select the option closest to their CE from a set of four options. Note that this method, in which a range of potential CEs is presented, is not uncommon in other experimental work in this area (e.g., Tversky & Kahneman, 1992). For each prospect, two sets of options were created as follows. The mean and standard deviation of free choice CEs (see Appendix) were calculated for each prospect. In the low options condition, the options participants received were 1/6th, 2/6ths, 3/6ths, and

4/6ths of a standard deviation below the mean. In the high options condition, options were 1/6th, 2/6ths, 3/6ths, and 4/6ths of a standard deviation above the mean. Thus the range of each set was half a standard deviation. The spacing of options compared to the distribution of free choice CEs is shown on the abscissa in Figure 1. Options were rounded to have familiar, easy-to-deal-with values.

Procedure. Participants were asked to imagine choosing between £30 for certain or a 50% chance of £100 to illustrate that prospects could have a value. They were told they would be asked to value a series of prospects. It was explained that the purpose of the experiment was to investigate how much they thought the prospects were worth, and that there was no correct answer. Participants were asked to choose the option nearest the value they thought the prospect was worth to them.

Each prospect was presented on a separate page of a 20 page booklet. The ordering of the prospects was random and different for each participant. Probabilities were always presented as percentages. Options were always presented in numerical order, as in the following example of a low option set:

How much is the gamble

"60% chance of £400"

worth?

Is it: £60   £80   £100   £120

Results

Participants took approximately 5 minutes to complete the task. Under free choice conditions, the average CE increased with both probability of winning and the amount that could be won, demonstrating that participants were sensitive to manipulations of both. The chosen CE was an approximately linear function of the independent effects of prospect amount and prospect probability.

The proportion of times each option was chosen is plotted in Figure 2. There is no evidence that the lowest option in the high options condition (H_1) and the highest option in the low condition (L_4) were preferred. Instead, the distribution of options is approximately the same for the two conditions. L_4 was chosen significantly less than half the time $t(7)=4.21$, $p=.0040$. The same was true of H_1, $t(7)=5.26$, $p=.0012$. An alpha level of .05 was used for all statistical tests.

Discussion

CE judgments were strongly influenced by the CE options offered, and were not skewed towards the mean free choice CE. This data therefore appears to illustrate prospect relativity: People do not seem to form a stable absolute judgment of the value of a prospect, but choose a CE relative to the CEs available. The preference for central options in these data may be an example of extremeness aversion (also called the compromise effect; see Simonson & Tversky, 1992). Indeed, in choosing amongst identical options, there is a tendency to prefer central ones (Christenfeld, 1995).

Experiment 1B

A natural explanation of the effect of the set of options available in Experiment 1A is that, on a given trial, the options available affect a participant's judgment. However, an alternative, and for our purposes less interesting, explanation is that when participants are repeatedly presented with trials containing too-high or too-low options, they learn to readjust their judgments to fit their responses within the alternatives given. One way of ruling out this alternative explanation is to use a within-participants design. In this design each participant is presented with some trials on which all the options were lower than the free-choice CE and others on which all the options were higher. If the effect seen previously was caused by a participant learning to adjust his or her judgments up or down to fit into the response scale, the effect should now disappear. However, if the effect was caused by the options available on that trial only, then the pattern of results demonstrated in Experiment 1A should be

replicated.

Method

Participants. Free choice CEs were given by 35 volunteers. Twenty-eight different volunteers chose CEs from sets of options. All participants were undergraduates from the University of Warwick and none had participated in Experiments 1A. They were paid £5 for taking part in this and other related experiments.

Design and Procedure. The design was the same as in Experiment 1, except that for each participant, 10 trials were randomly selected to have options all higher than the pretest mean for that prospect, the other 10 having options all below the mean. Trials were randomly intermixed. Free choice CEs and corresponding options are given in the Appendix. The procedure was as in Experiment 1A.

Results

Participants took approximately five minutes to complete the task. One participant's data were excluded from the analysis because he had been given a misleading answer to a query about the task which would have led to an inappropriate response strategy. As before, under free choice, the CE increased approximately linearly with both the amount that could be won and the probability of winning.

Figure 3 shows the proportion of choices of each option. In both conditions, the proportion of responses increases with proximity to the mean free choice CE. If participants were not affected by the available options, the proportion of L_4 and H_1 would be expected to be at least .5. Planned *t*-tests showed that the proportion of L_4 and H_1 responses was significantly below 0.5, with values of $t(26)=2.65$, $p=.0135$, and $t(26)=3.81$, $p=.0008$, respectively.

A further issue is whether the context effects found in the main analysis apply to all participants or whether some people show a larger context effect than others. For each participant two scores were constructed, one for each condition. A participant was awarded

one point for each time he or she chose the lowest option, two for the next lowest, three for the second highest and four for the highest. Those showing no effect of the option set should have chosen the L_4 and H_1. However, those who based their judgment entirely on the option set would choose mid-range options. Thus a negative correlation between low choice CEs and high choice CEs would be evidence that people vary in the extent to which context effects influence their CE decisions. Far from being negatively correlated, the scatter plot has a significant positive correlation ($r^2=.45$, $p=.0001$).

Perhaps surprisingly, we found no evidence that the options offered on the previous trial influenced the option selected on the current trial. One might imagine that, say, offering low options on the previous trial might cause a participant, who is trying to be consistent, to select an option lower than they otherwise would on the current trial. However, the rank (as described above) of the option selected within the set did not depend on the previous option set offered (mean rank 2.63, SE 0.11, for prior low options, and mean rank 2.62, SE 0.13, for prior high options), $t(26)=0.23$, $p=.8407$.[2]

Discussion

This experiment replicated the findings of Experiment 1A. Participants' CE judgments were influenced, at least in part, by the options from which the CE must be chosen. Although the context effect in Experiment 1A might have been explained by participants learning to recalibrate their judgments where options were either all too low or all too high, such an explanation cannot apply in this within-participants experiment. Overall, the pattern of results shown here is intermediate between that expected under the hypothesis that the available options are irrelevant and that expected if the available options were the only determinant of responses. This contrasts with Experiment 1A, where there was no skew in selection of options towards those nearest the mean free choice CE. The skew can be accounted for in two ways. First, encountering both low and high options can somehow cause participants to be less affected by context. Second, the skew could be caused by participants trying to be

consistent with their responses to previously completed questions. Such a consistency effect cannot be due to the immediately preceding trial alone, as there was no effect of the immediately preceding trial. Instead, if this kind of explanation is correct, the skew must be due to some larger window of previous trials.

Whilst the spacing of the options relative to the free choice distribution of CEs was the same in Experiments 1A and 1B, the options were actually more closely spaced in Experiment 1B because participants' free choice CEs were less variable. Thus an alternate account of the difference in the pattern of preferences across the options could be made in terms of the different absolute spacing of the options. For this reason, we replicated Experiments 1A and 1B as conditions of a single experiment, using the spacings from Experiment 1B throughout. The results remained essentially unaltered, and so we do not present them here. An explanation of the different pattern of preferences in Experiments 1A and 1B in terms of using different options can thus be ruled out.

Experiment 1C

The effect of available options in Experiments 1A and 1B appears to create difficulties for EU and related theories as descriptive accounts of decision under risk. But these difficulties may be less pressing if the effects demonstrated thus far arise only because the options presented as CEs are simply too close together, and that participants are roughly indifferent between them. (Although note that this ought to lead to a 'u' shaped preference across the options, rather than an 'n' shape.[3]) If this is the case then these effects should disappear when the options are more broadly spaced, and hence people are no longer indifferent between them. In this experiment we investigated the effect of increasing the spacing of the options.

Method

The method was the same as Experiment 1B, except that there were three between-participant spacing conditions. In the narrow condition, options were spaced at 1/6th of a free

choice standard deviation as in Experiments 1A and B. In the wide condition the spacing between adjacent options was doubled to 1/3th of a free choice standard deviation. In the gap condition, the option spacing was as in the narrow condition, but the mean of the low and the high options was set to equal that of the wide condition. Eighteen participants took part in the gap condition, and 19 each in the narrow and wide conditions.

Results and Discussion

The proportion of times each option was selected is shown in Figure 4. The proportions for the narrow and wide conditions closely resemble one another. In the narrow condition, option L4 was selected significantly less than half the time, $t(18)=4.02$, $p=.0008$, as was the H1 option, $t(18)=3.42$, $p=.0031$, replicating the results of Experiment 1B. In the wide condition, option L4 was selected less than half the time, $t(18)=2.04$, $p=.0565$, although this difference is only marginally significant. The H_1 option was selected significantly less than half of the time, $t(18)=3.52$, $p=.0024$. In the gap condition, L_4 was not chosen significantly less than half of the time, $t(17)=0.17$, $p=.8665$, but H_1 was, $t(17)=2.99$, $p=.0082$. For every condition, L_4 and H_1 were chosen significantly less than the proportion of times predicted by the relevant integrals over the free choice distribution (which was always $>.5$). The key result is that doubling the spacing of the options did not eliminate the context effect.

Experiment 2

Experiment 2 was designed to demonstrate the same effect of restricting the range of CE options in a task where it was optimal for participants to report CEs truthfully. Although psychologists typically assume that participants are "honest" when providing hypothetical CEs, economists are typically concerned with providing a system of incentives that ensures it is optimal for participants to provide truthful CEs. Hence the results above may be criticized from an economic perspective.

There is evidence that psychologists are correct in their assumption that participants are typically honest in their judgments. For example, Lichtenstein and Slovic (1971)

demonstrated preference reversals in choices between two prospects, and CE estimates for those prospects, in situations where decisions were hypothetical and situations where there was an incentive system (see also Tversky, Slovic, & Kahneman, 1990). Preference reversals have also been demonstrated with ordinary gamblers playing for high stakes in Las Vegas (Lichtenstein & Slovic, 1973, see also Grether & Plott, 1979). For further discussion of these and other similar findings see Hertwig and Ortmann (2001) and Luce (2000, pp. 15-16). However, because of the potential importance of the findings from Experiments 1A-C for models of economics, we include this experiment where the incentive system has been designed to motivate participants to provide truthful CEs.

The design follows a solution to the 'cake cutting' problem, where a cake must be divided fairly between two children. One solution is to allow one child to cut the cake into two pieces, and the other child to select the piece. The first child should cut the cake exactly in half, otherwise his or her friend will take the larger piece of cake, leaving him or her with the smaller piece.

In this experiment, participants divide a sum of money into an amount for certain, and an amount that could be be won with a known, fixed probability. For example, they might split £1000 into a sure amount of £300 and the prospect "60% chance of £700". Participants know that the other person (who was not the experimenter) will select either the prospect or the sure amount, taking the better of the two, leaving the participant with the other. Thus it is optimal for participants to split the given amount so that they have no preference between the resulting fixed amount and the resulting prospect. Note that this procedure will work only if each participant assumes that the chooser has the same level of risk preference as himself or herself. To this end, participants were told to assume that the chooser did have the same risk preference as they did.

This procedure more simple than other methods used to elicit truthful CEs, for example the first price auction, or the Becker, DeGroot & Marschak (BDM, 1964) procedure.

In the BDM procedure, participants are given the chance to play a prospect and are asked to state the minimum price at which they would sell the prospect. A buying price is then randomly generated by the experimenter and, if it exceeds the selling price, then the prospect is bought from the participant. If not, then the participant plays the prospect. It is the case that it is optimal for participants to state a selling price that is the CE of the prospect, though it is unlikely that many participants realize this.

Method

Participants. Participants were undergraduates from the University of Warwick, who had not participated in Experiments 1A-C. Seventeen participants took part in the free choice condition of the experiment. Nineteen further participants took part in the restricted choice conditions. Participants were paid £5, plus performance-related winnings of up to £4.

Design. In each trial of the free choice condition, participants divided a given amount of money, x, into two smaller amounts, y and z, to make one fixed amount (y) and the prospect "p chance of z". Probability p was known to participants before splitting amount x. Participants were told that one trial in the experiment would be selected at random at the end of the experiment and a second person would take either the fixed amount or the prospect for himself leaving the participant with the other option. Under the assumption that the chooser had the same risk preference as they did, it was explained to participants that the chooser would choose the option with greater utility, leaving the participants with their least preferred option, if they did not split the amount to make options of equal utility. It was therefore optimal for participants to split the amount x into amounts y and z, such that y and a "p chance of z" are equivalent for them, i.e., y is the CE for the prospect "p chance of z".

The restricted choice conditions differed by offering participants a choice from a set of four pre-split options, rather than giving them a completely free choice. That is, values for y and z were presented, and participants selected one pair which could be played at the end of the experiment. It could be argued that participants might reasonably think that the pairs of y

and z values presented might provide them with information about the chooser's risk preferences. For this reason two people were used in running the experiment. One person was responsible for administering the tests, and the other for making the choice at the end of the experiment. The intention was to keep the roles of the experimenter and the person making the choice at the end of the experiment separate in participants' minds, to minimize the degree to which participants would think that the options provided information about the chooser's risk preference.

It was hypothesized, as in Experiment 1, that the set of pairs of values for y and z presented would influence participants' choices. To investigate this, we varied one between-participants factor. The set of values for y and z were either selected such that y was always greater than the mean free choice value of y and z was smaller than the mean free choice value of z, or vice versa. These correspond to the low and high option sets in Experiment 1. The precise option sets were constructed as follows. The mean and standard deviation of the free choice amount were calculated for each prospect (see Appendix). The two sets of equally spaced options (for the high value and low value conditions) were calculated as described for Experiment 1A. As in Experiment 1A, if participants were not influenced by the set of choices, then the distribution of responses across the options should be biased towards the free choice splitting.

There were 32 trials in the experiment, made by crossing four values of p (.2, .4, .6, and .8) with eight values of x (£250, £500, ..., £2000).

Procedure. All conditions of the experiment began with written instructions. It was explained to participants that they were playing a gambling game, and that they should try to win as much money as possible. They were told that a single trial would be randomly selected at the end of the experiment and used to determine their bonus. They were told the purpose of the experiment was to investigate how much people thought various prospects were worth. It was emphasized that it was optimal for the participant to split the money so
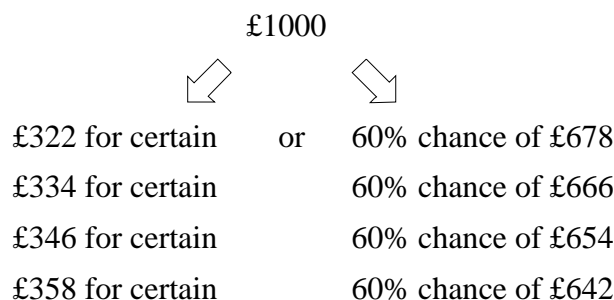
they thought the amount for certain was equal in worth to a chance on the prospect. Participants were told that if they allocated funds so that either the amount for certain was worth more than the prospect, or vice versa, then the chooser would take the 'better option', leaving them with less than if they had allocated the money so the prospect was worth the certain amount. They were told that although they could not be certain what the chooser would do, they should assume that the chooser would behave like them.

Participants were given five practice trials. One of the trials was chosen at random, and it was explained that if the chooser chose the fixed amount, then the prospect would be played, and they would get the winnings. They were also told that if instead the chooser took the prospect they would get the fixed amount. Note that this discussion was hypothetical, and participants were not actually told what the chooser's preference would be.

After the practice participants completed a booklet of options. The pairs of options were presented in a random order to each participant. An example page from a free choice condition booklet is shown below.

£1000

£____   or   60% chance of

for certain   £____
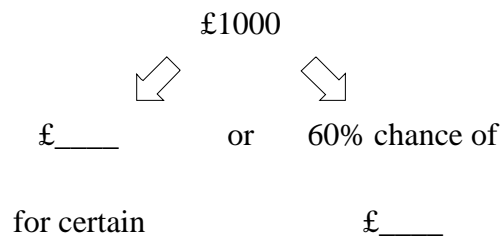
In the restricted choice conditions, pre-split options were presented as in the example below.

£1000

£322 for certain   or   60% chance of £678
£334 for certain   60% chance of £666
£346 for certain   60% chance of £654
£358 for certain   60% chance of £642

When the experiment was completed, one trial was chosen at random, and played to

determine each participant's bonus (using an experiment exchange rate of 0.0024).

Results

Participants took between half an hour and one hour to complete the booklet. It seems that the introduction of a bonus caused participants to deliberate on their answers for much longer than in Experiment 1A-C. One participant from the free choice condition was eliminated from subsequent analysis for showing a completely different pattern of results to other participants, suggesting he had misunderstood the task. The participant had decreased the value of the fixed amount, y, as the chance of the prospect amount, p, increased (i.e., he had responded as if prospects with a higher chance of winning were worth less to him). Fourteen out of 512 trials (16 participants x 32 trials), where the initial amount had been incorrectly split, were deleted and treated as missing data.

For the free choice splits, as the total amount x increased, then participants' allocation of the fixed amount y increased. As the probability p of winning the prospect increased, participants' estimates of the value of the prospect, y, also increased. Thus participants' responses seemed lawful and sensible, indicating that the task made sense to them.

The choices made in the restricted choice conditions are shown in Figure 5. Participants did prefer end options over central options in both conditions, as would be expected if participants were not influenced by the option set. However, if there were no effect of context, L_4 and H_1 should have been chosen over half of the time. L_4 was chosen significantly less than half of the time, $t(9)=3.47$, $p=.0070$, as was H_1, $t(8)=4.20$, $p=.0023$. Thus the proportion of times each option was selected differed significantly from the proportions expected under the assumption that participants were not influenced by the options available.

Discussion

The results of the restricted choice conditions in Experiment 2 replicate the prospect relativity finding shown in Experiment 1 under a more rigorous procedure. When participants

were presented with a range of pre-split total amounts, so that the CE options were either always lower or always higher than the free choice value, the context provided by the pre-split options influenced their choice of CE.

Experiment 3

The demonstration of apparent prospect relativity in risky decision making suggests that the representation of the utility dimension may be similar to that of perceptual psychological dimensions, where context effects have also been demonstrated.

Empirical investigations in absolute identification (Garner, 1953; Holland & Lockhead, 1968; Hu, 1997; Lacouture, 1997; Lockhead, 1984; Long, 1937; Luce, Nosofsky, Green, & Smith, 1982; Purks, Callahan, Braida, & Durlach, 1980; Staddon, King, & Lockhead, 1980; Stewart, 2001; Stewart et al., 2002b; Ward & Lockhead, 1970, 1971), magnitude estimation, matching tasks, and relative intensity judgment (e.g., Jesteadt, Luce, & Green, 1977; Lockhead & King, 1983; Stevens, 1975, p. 275) have shown that perceptual judgments of stimuli varying along a single psychological continuum are strongly influenced by the preceding material. If the representation of utility is similar to the representation of these simple perceptual dimensions, then preceding material might be expected to influence current judgments, as it does in the perceptual case.

Simonson and Tversky (1992) provide several cases where preceding material does indeed influence current judgments in decision making. For example, when choosing between pairs of computers that vary in price and amount of memory, the trade-off between the two attributes in the previous choice affects the current choice. Indeed, preference reversals can be obtained by varying the preceding products. In the present experiment we consider the effect of preceding material on judgments concerning a single dimension (utility), rather than the trade-off between two dimensions. Participants simply provided CEs for simple prospects of the form "p chance of x". We then examine the effect of preceding prospects on the CE assigned to the current prospect.

Method

Participants. Fourteen undergraduates from the University of Warwick participated for payment of £3. All participants had previously taken part in the free choice condition of Experiment 2.

Design. Participants were asked to state the value of a series of prospects. Participants had previously taken part in a task where estimating the value of prospects truthfully optimized their reward, compared to overestimating or underestimating the value of a prospect. Participants were instructed to continue providing CEs in the same way.

Ten sets of 10 simple prospects of the form "*p* chance of *x*" were constructed. Figure 6 shows the values of *p* and *x* for each prospect. Each set of prospects lying on the same curve (these are hyperbolas) shares a common expected value. (The slight deviation of the crosses from the line is caused by rounding the values of *p* and *x*.) Prospects were chosen in this fashion simply because it produces an equal number of prospects with each expected value. The order in which prospects were presented was random, and different, for each participant.

We hypothesized that the preceding prospect should affect the value assigned to the current prospect as follows. If the previous prospect had a low expected value, then we expected that the current prospect would be overvalued. Conversely, if the previous prospect had a high expected value, then we expected that the current prospect would be undervalued. This prediction is motivated by the contrast effects observed in the analogous perceptual task, magnitude estimation.

Procedure. Participants were told that they would be asked to value prospects, and that they should do this in the same way as in the previous experiment (the free choice condition of Experiment 2). Participants completed a booklet with a separate prospect on each page, together with a space for their valuation.

Results

Figure 7 plots the mean value of prospects, as a function of the expected value of the

previous prospect, for each possible expected value of the current prospect. CEs given to a prospect increased as the expected value of the prospect increased. The response was, on average, 97% of the expected value (s.d. 36%) showing slight risk aversion, on average. The expected value of the previous prospect has no effect on the value assigned to the current prospect (i.e., the lines in Figure 7 are flat).

To examine possible sequence effects more closely, a linear regression was completed for each participant, to see what proportion of the variability in the current response could be explained by the previous prospect's expected value, after the effects of the attributes of the current prospect had been partialled out. The previous prospect's expected value was a significant predictor of the current response for just 1 of the 14 participants, no more than would be expected by chance. For this participant, $r^2=.04$, and for all other participants $r^2<.04$. Similar analyses for the previous (a) response, (b) x and (c) p also showed no sequential dependencies.

Discussion

In perceptual tasks where a series of stimuli are presented, and a judgment is made after each stimulus, the response to the current stimulus is shown to depend on the stimuli (or responses; the two are normally highly correlated) on previous trials. In other words, the response on the current trial is systematically biased by (some aspect of) the previous trial. Some authors (e.g., Birnbaum, 1992) have suggested that judgments about risky prospects might be similarly affected. Here, CE judgments for simple prospects do not show sequential dependencies like those shown in the analogous perceptual judgment tasks. There is little carry-over of information from one trial to the next. This finding is consistent with Mellers et al.'s (1992) result, where the buying prices of a set of critical prospects were at most only slightly influenced by the expected value of (previously encountered) filler prospects.

Experiment 4

Experiments 1 to 3 investigated the effect of context in CE judgment tasks. Careful

discussion by Luce (2000) highlights the difference between judged CEs, where participants provide a single judgment of the value of a prospect, and choice CEs, derived from a series of choices between risky prospects and fixed amounts. For example, for the kinds of prospects used here, with large amounts and moderate probabilities, judged CEs are larger than choice CEs (e.g., Bostic, Herrnstein & Luce, 1990). The preference reversal phenomenon (e.g., Lichtenstein & Slovic, 1971) is evidence that there is often a discrepancy between choice-based and CE-based methods of assessing utility (see also Tversky, Sattath, and Slovic, 1988). Indeed, Luce (2000) goes as far as to advocate developing separate theories for judged and choice CEs.

Experiment 4 investigates context effects in a choice-based procedure rather than a judged CE-based procedure. Participants make a single choice from a set of simple prospects of the form "p chance of x" where the probability of winning was traded off against the amount that could be won. The context is provided by manipulating the range of values of p (and therefore of x) offered.

Method

Participants. Ninety-one undergraduates from the University of Warwick took part. None had previously participated in any other experiment described in this paper. Payment was determined by playing the prospect selected by each participant, and winnings were between £0 and £2.

Design. Participants were each offered a set of simple prospects of the form "p chance of x". Within the set, the probability of winning and the win amount were traded off against one another, and thus the choice was between a large probability of winning a small amount through to a smaller probability of winning a larger amount. Ten prospects were used: "50% chance of £50", "55% chance of £45", ..., "95% chance of £5".

If utility is assumed to be a simple power function of x, as is standardly assumed in economics, with exponent γ (i.e., $u(x)=x^\gamma$), the expected utility of each prospect can be

calculated.[4] Figure 8 plots utility as a function of the probability of winning *p* for different

curvatures of the utility function (values of γ). For a risk-neutral person (γ=1.0), for whom

utility is proportional to monetary value, the probability of winning for the prospect with the

maximum utility is *p*=.5. For a risk-averse person (γ<1.0), the prospect with maximum utility

has a larger probability of winning a smaller amount; the maximum falls at higher *p* for lower

γ. The key observation is that the prospect with maximum utility in the set is determined by

the level of risk aversion, γ. Thus a participant's choice of prospect can be mapped directly

onto a degree of risk aversion.

There were three conditions in the experiment. In the free choice condition, all 10

prospects were presented. In two other conditions, the choice of prospects was limited to

either the first or second half of the prospects available in the free choice condition. In the

more risky condition, the prospects ranged from a "50% chance of £50" to a "70% chance of

£30". In the less risky condition, the prospects ranged from a "75% chance of £25" to a "95%

chance of £5".

Procedure. Each participant was presented with a sheet listing a set of prospects. The

prospects were presented in an ordered table, with a row for each prospect and columns

headed "chance of winning" and "amount to win". Probabilities were presented as

percentages. Participants were asked to choose one prospect from the set to play. Before

making their choice they were given an explanation of how the prospect would be played.

The selected prospect was played and participants were paid according to its outcome,

multiplied by an experiment exchange rate (0.002).

Results

The results are displayed in Table 1. The table contains a row for each prospect. The

numbers in the third to fifth columns refer to the number of participants who selected that

prospect. Blank cells indicate that the prospect was not available for selection in that

condition. Two hypotheses were tested. The first is that participants are sensitive to the absolute values of prospect attributes, and are unaffected by the choice options. According to this hypothesis, in the restricted choice conditions, participants should choose the prospect in the set that is nearest to the prospect they would choose under free choice conditions. It is possible to predict the distribution of participants across prospects in the restricted choice conditions from the free choice condition. The last two columns of Table 1 show the distribution of participants that would be expected if the participants in the free choice condition had instead been offered the prospects in one of the restricted conditions. These distributions were generated by summing the frequencies for the prospects in the free choice condition that were unavailable in the restricted choice condition, and adding the resulting count to that for the closest available prospect. The distribution of the more risky condition differs significantly to that predicted from the free choice condition, $\chi^2(4)=71.82$, $p<.0001$. The distribution of choices in the less risky condition also differs significantly from that predicted from the free choice condition, $\chi^2(4)=24.55$, $p<.0001$. In conclusion, we can reject the hypothesis that participants in the restricted choice conditions chose the prospect in the set nearest to the prospect they would have chosen under free choice conditions and were otherwise uninfluenced by the set of options.

The second hypothesis tested was that, although there may be some effect of the choices available, there would still be some effect of the absolute magnitude of prospect attributes. If so, we would expect a tendency for participants in the most risky condition to choose the least risky prospect available, and vice versa. However, if participants' choices are determined solely by the set of available prospects, then the distribution of responses across options (from the most risky to the least risky) should not differ across the more risky and less risky conditions. There was no significant difference, $\chi^2(4)=2.89$ $p=.5767$. In other words, there is no evidence that the absolute riskiness of a prospect had any influence on the

choices made in each of the restricted choice conditions.

Discussion

Participants were asked to select a single prospect to play from a set. Within the set, the probability of winning a prospect was reduced as the amount that could be won was increased. Thus each participant faced a choice between prospects offering small amounts with high probability through to larger amounts with a lower probability. In the restricted conditions, participants were only offered a subset of the prospects available. If participants' preferences were not affected by the set of options provided, they should simply choose the prospect closest to the prospect they would select under free choice conditions. However, the distribution of choices differed significantly from those expected under this prediction. Instead, the set of options available seemed to determine participants' preferences and there was no significant evidence that participants were sensitive to the absolute level of risk implicit in a prospect. In conclusion, the level of risk aversion shown by a participant was shown here to be a function of the set of prospects offered.

We know of only one other experiment where the effects of the context provided by the choice set is shown to affect the prospect chosen. In an unpublished study by Payne, Bettman, and Simonson (reported in Simonson & Tversky, 1992), participants were asked to make a choice between a pair of three-outcome prospects. Adding a third prospect that was dominated by one of the original prospects, but not the other, significantly increased the proportion of times the (original) dominating prospect was selected over the (original) non-dominating prospect. This effect is also seen when making non-risky decisions where, for example, one must choose between a cheap, low quality product and a more expensive, higher quality product (Simonson & Tversky, 1992). The notion of trade-off contrast, where participants ,who are assumed to have little knowledge about the trade-off between two properties (e.g., quality and cost), deduce what the average trade-off is from the current or earlier choice sets, can account for this type of data.

However, it is not immediately obvious how the notion of trade-off contrast might account for the results of Experiment 5. Across both contexts the trade-off between probability and amount was constant (as the chance of winning the prospect was increased by 5%, the amount to win fell by £5). Instead, it seems that participants have no absolute grip of the level of risk implicit in each prospect in the choice set, and instead choose a prospect with reference to its riskiness relative to the other prospects in the set. This demonstration of prospect relativity in choice is consistent with that described in earlier experiments, where CE judgments were used.

Experiment 5

Our final experiment was designed to investigate the extent to which a choice between two prospects is affected by preceding context. Thus this experiment mirrors Experiment 3, but with actual choices rather than CE judgments. On each trial, participants chose between a sure amount of money and a prospect offering a larger amount with a known probability. Let us informally call a trial risky (or safe) to the degree that we expect participants to prefer the risky prospect (or the sure amount of money). Half of the trials, the common trials, were given to all participants and were designed so that the sure amount was such that a typical, moderately risk-averse participant would be indifferent between the sure amount and the risky prospect. The other half of the trials were filler trials and their properties were manipulated between participants. For half of the participants, the filler trials were constructed so that only a very risk-averse individual would be indifferent to the sure amount and the risky prospect. For these "risky trials", most participants would favor the risky prospect. For the other half of the participants the filler trials were constructed so that only relatively risk-neutral participants would favor the risky prospect. For these "safe trials", most participants should favor the sure amount. The intention was to assess whether the "riskiness" of the filler trials would affect choices on the common trials. If participants represent current prospects relative to previous prospects, then the common trials should

seem relatively safe if the filler trials are "risky", and participants should favor the safe, sure amount. Conversely, if the filler trials are "safe" then the common trials should seem relatively risky, and participants should favor the risky prospect.

Method

Participants. Thirty-five undergraduates from the University of Warwick took part in the experiment, and were paid £5 for participating in this and three other related experiments.

Design. Thirty-six trials were generated, each of which comprised a simple prospect of the form "*p* chance of *x*" and an amount offered for certain. The amounts £100, £200, £300, £400, £500, and £600 were crossed with the win probabilities of .1, .2, .4, .6, .8, and .9 to give 36 prospects. Half of the trials were selected at random and consistently used to set the context. For half of the participants, the fixed amount offered on these trials was low and, for the other half of the participants, the fixed amount was high. The other half of the trials was common to both groups, and the fixed amounts were at an intermediate level.

A sure amount was generated by using Equation 2.

$$y = x \, p^{\frac{1}{\gamma}} \tag{2}$$

where *y* is the sure amount and the prospect is a "*p* chance of *x*". γ describes the curvature of a hypothetical power law utility function, $u(x)=x^\gamma$. γ=1 for a risk-neutral person. Smaller values of γ denote greater risk aversion. For each condition, six values of γ were used. The values 0.50, 0.55, and 0.60 were used to generate sure amounts for the common trials. "Risky" fillers were generated using the values 0.35, 0.40, and 0.45, which makes the prospects on the experimental trials seem comparatively unattractive. "Safe" fillers were generated using the values of 0.65, 0.70, and 0.75. (For the population used in this experiment, we observed values of γ in this range in an unpublished study from our laboratory. The values of γ were deduced from choices between simple prospects and sure amounts.) The assignment of values of γ to trials was such that value of γ occurred only once

for each probability, and only once for each prospect amount. Otherwise, the assignment was random and the same for all participants.

Procedure. Participants were given brief oral instructions. They were told that they would have to imagine making choices between playing a prospect to receive an amount of money and taking a smaller amount for sure. Each pair of options was presented on a separate page of a 36-page booklet, and appeared as follows:

Which option do you prefer?

10% chance of £300

£12

Participants were told to mark the option they would prefer and move on to the next page. They were also made aware that there was no objective 'right' answer, and that it was a matter of personal preference.

Results

The dependent measure was the mean proportion of trials on which the prospect was preferred to the sure amount. With "safe" fillers, participants selected the risky prospect significantly more often in the experimental trials (mean .53, SE .04) than in the filler trials (mean .40, SE .05) as intended, $t(16)=7.10$, $p<.0001$. With "risky" fillers, participants selected the risky prospect less often in the experimental trials (mean .47, SE .05) than in the filler trials (mean .67, SE .04), again, as intended, $t(17)=7.39$, $p<.0001$. The comparison of interest is performance on the common trials across the "safe" and "risky" conditions. For the common trials the risky prospect was selected slightly more often in the condition in which it was designed to look more attractive, but the difference was not significant $t(33)=0.8$, $p=.4305$.

Discussion

Imagine being presented with a choice between a sure amount and a simple risky prospect. If, in previous trials, the sure amount was low compared to the prospect then the

sure amount on this trial might seem quite appealing. Conversely, if in previous trials, the sure amount was high compared to the prospect, then the prospect on this trial might seem quite appealing. However, this experiment found no evidence that the properties of preceding trials affected people's judgments between a prospect and a certain amount. The results of this experiment point further to the notion that context effects are much more potent within a trial than between trials, and that this is the case for CE judgments (Experiment 3) and choice paradigms (Experiment 5).

We are quite surprised by the small or lacking effect of previously considered prospects on the current choice, and so have conducted a meta-analysis of sequential effects in other choice experiments from our laboratory. The experiments involved making choices between two prospects, each of the form "p chance of x otherwise y", where $x>y$ 0. In each pair, one prospect was always more risky than the other (i.e., the probability of winning was smaller) but had a higher expected value. Thus the choice was always between a comparatively more likely but smaller amount verses a larger but less likely amount. Trials were split into two groups according to whether the total expected value of the prospects on the previous trial was more or less than the median amount. The proportion of risky picks on the current trial did differ significantly between the two groups, $t(95)=1.99$, $p=.0422$, although the actual difference in proportions was very small (.39 when the previous expected value was high, vs. .41 when the previous expected value was low). It seems that this small effect was largely caused by the prospect with the smaller expected value on the previous trial, as a median split of current trials on this attribute lead to a slightly larger significant difference (.39 vs. .42), $t(95)=1.99$, $p=.0079$. Splitting by other attributes of the previous trial (e.g., the difference in expected value, the maximum outcome, the higher expected value, the maximum probability of a zero outcome, and the probability of the maximum outcome) does not produce significant differences. In conclusion, it seems that the effects of previous choices between risky prospects on current choices are small in comparison to the within trial

effects.

General Discussion

Together, the results presented in this paper suggest that prospects are judged relative to accompanying prospects, a phenomenon that we call prospect relativity. In Experiments 1A-C, the set of options offered as potential CEs for simple prospects was shown to have a large effect on the CE selected. In Experiment 2, this effect was replicated despite monetary incentives designed to encourage participants to deliver accurate and truthful CEs. In Experiment 4, the set from which a simple prospect was selected was shown to have a large effect on the prospect that was chosen. In two further experiments, Experiments 3 and 5, we investigated whether attributes of previously considered prospects affected judgments about a current prospect. Previously considered prospects had little effect. It seems that the context provided by items that are considered simultaneously (e.g., the potential CEs in Experiment 1A-C or the set of available prospects in Experiment 4) does affect decisions about risky choice, but that the context provided by previously considered risky choices, even if they are very recent, has little effect. We call this effect the simultaneous consideration effect.

In the following section we briefly review existing theories of decision under risk, and investigate what account they might offer, if any, of the prospect relativity phenomena presented. Existing theories can, roughly, be divided into two classes: (a) those where the utility or value of a prospect depends only on the attributes of the prospect, and (b) those where prospect attributes are compared against those of other competing prospects.

Independent Prospect Evaluation Theories

Expected Utility Theory. The EU of the simple prospect "*p* chance of *x*" is given by $p.u(x)$ (see Equation 1). A prospect is acceptable if, when the prospect is integrated with current wealth, the expected utility is higher than the utility of the current wealth alone. Thus prospects with higher expected utility are preferred. EU theory provides no mechanisms for the options offered as CEs to influence the choice of CE, and thus cannot offer an account of

the results presented in Experiments 1 and 2. Under EU theory, the utility of a prospect is independent of the other prospects in the choice set. Thus EU theory cannot predict an effect of the context provided by the choice options demonstrated in Experiment 4.

Rank Dependent Utility Theory. In rank dependent utility (RDU) theory (Quiggin, 1982, 1993; see Diecidue & Wakker, 2001 for an intuitive introduction), the independence axiom of EU theory has been relaxed. Instead of transforming probabilities into decision weights, cumulative probabilities are transformed. Thus a decision weight depends not only on the probability of the corresponding outcome, but also on the probabilities of other possible outcomes in the same prospect, modulated by the rank of their associated outcomes. For extreme outcomes such a function causes low probabilities to be over-weighted, and high probabilities to be under-weighted.[5] However, for events with intermediate outcomes, the probabilities are minimally distorted (Quiggin, 1993, p. 56). However, as in EU theory, the utility of a prospect is independent of other prospects or options on offer, and thus RDU theory cannot account for these prospect relativity effects.

Configural Weight Models. Birnbaum, Patton, and Lott (1999) describe two configural weight models, where the utility of a prospect is modified by the rank or difference between the possible outcomes. However, the utility of a given prospect is independent of the other prospects in the choice set, and so these theories cannot account for these prospect relativity effects.

Prospect and Cumulative Prospect Theories. To address some of the empirical results that challenged EU as a descriptive theory, Kahneman and Tversky (1979) proposed prospect theory. Prospect theory states that there are two phases in the choice process. In the editing phase, prospects are first coded as gains and losses in relation to some neutral reference point, and then further simplified. The editing phase may be ignored in modeling performance in the experiments featured in this paper, as the simple prospects used remain unaltered by the edits. In the evaluation phase, the prospect with the highest value is preferred. When all of the

outcomes are gains, as was the case in these experiments, the value of a simple prospect "p chance of x" is given by $\pi(p)v(x)$, where v is the subjective value function and π is the decision weight function.[6] Thus, at least for the simple prospects used in the present experiments, the value of a prospect is independent of other prospects or options presented, as is the case for EU theory. Thus prospect theory cannot offer an account of these data. Tversky and Kahneman (1992) proposed a modification to prospect theory, where cumulative probabilities, rather than simple probabilities, are transformed, as in RDU theory. However, this modification does not change the fact that prospect values are independent of other prospects or options in the choice set.

Dependent Prospect Evaluation Theories

In the following theories, the utility or value of a prospect is not independent of the other prospects in the choice set. Thus these theories are potential candidates in accounting for the findings in this paper.

Regret Theory. According to regret theory (Loomes and Sugden, 1982) people may have feelings of regret (or rejoicing) on experiencing the outcome of a prospect. Moreover, they then try to anticipate and take into account these feelings when making choices. Anticipated feelings of regret modify the utility of a prospect that results from a particular choice with respect to the prospects that result from other possible choices. Specifically, for binary choices, regret is assumed to be a function of the difference in utilities of the actual outcome and the outcome that would have been obtained if the other choice was made. Thus, one choice is preferred over another if and only if its expected (choiceless) utility and the corresponding regret is greater than for the other choice. As a result, preferences are not necessarily transitive, and therefore extension to the multiple choice situation, as in our Experiment 4, is not straightforward. Loomes and Sugden (1982) suggest that the regret in choosing an option from a set of options might be the average of the regret from all possible pairwise comparisons. Quiggin (1994) suggests that this regret might instead be the regret of

choosing the option in a pairwise comparison with the best option, as this means that dominated options (which presumably would never have been chosen) are ignored. Effectively, regret theory weights states where there is a large difference in (choiceless) utility between choices more heavily.

For the simple gamble "p chance of x", the CE is such that the difference in utilities between the outcomes, plus the difference in regret, summed over all world states, is zero. As in the independent theories, the options on offer simply do not enter into the equation, and thus regret theory cannot offer an account of the results from Experiments 1 and 2.

In Experiment 4, the set of prospects from which a prospect was to be chosen influenced the choice. As, in regret theory, the utility of a prospect is not independent of the other prospects in the choice set, at first sight it seems that regret theory might be able to offer an account of this context effect. Unfortunately, with 10 independent binary prospects (as in the free choice conditions) there are $2^{10}=1024$ possible world states, each with a different pattern of possible outcomes depending on which prospect is chosen. Thus it is not obvious what the predictions of regret theory would be. We therefore simulated the results of Experiment 4, assuming utility to be a power function of money, and regret a power function of the difference in the actual outcome and the best outcome that could have occurred (cf. Quiggin, 1994). The key question is, for an individual with fixed utility and regret functions, can regret theory ever predict that, in each set, a non-extreme prospect will be preferred? For every point in the parameter space, if regret theory predicts a mid-set prospect is preferred in one restricted set, then in the other set the corresponding extreme prospect is preferred. Roughly, the pattern of preference for a restricted choice set can always be predicted from the pattern of reference across a free choice of all 10 prospects. In summary, at least for this implementation of regret theory, the context effects in Experiment 4 cannot be predicted.

Stochastic Difference Model. In the stochastic difference model (González-Vallejo, 2002) prospects are judged relative to one another. For simplicity, González-Vallejo assumed

that subjective prospect attributes are the actual prospect attributes, and the function

comparing attributes gives the difference between them as a proportion of the larger attribute.

(No other instantiations of the theory have been investigated.) This proportional difference

strategy is a special case of the stochastic difference model, and we apply it to our data. The

differences are summed over all attributes to give the overall preference for one prospect over

another. This model can account for violations of stochastic dominance, independence, and

stochastic transitivity, and thus seems a plausible candidate model to account for the context

effects presented in this paper.

The stochastic difference model is primarily a model of choice. It is not obvious how

it might be extended to produce CEs. Here, we assume that the CE is a prospect of the form

"y for certain" where the model predicts no preference for the CE over the prospect "p chance

of x" under consideration. There will be no preference for the prospect over the CE when the

proportion difference in the probabilities is equal to the proportion difference in amounts.

Thus the model predicts risk neutrality, where the CE is the expected value of the prospect.

Allowing the options presented to enter into the evaluation of the monetary attributes as

implicit standards (following González-Vallejo, 2002, p. 139) makes no difference, as all of

the options are smaller than the amount that could be won.

Preliminary suggestions are given (González-Vallejo, 2002, p. 152) as to how the

model might be extended to choice amongst multiple prospects using the notion of trade-off

contrast (Simonson & Tversky, 1992) in a two-step procedure. First, the strengths of

preference for one prospect over another are calculated for all pairwise comparisons within

the set of prospects. The overall preference for a given prospect is then the sum of all of the

pairwise strengths where that prospect was favored. The extended model can be applied to

our Experiment 4 as follows.

The stochastic difference model predicts that, for any pair of prospects from

Experiment 4 (from a 50% chance of £50 to a 5% chance of £95), the more risky prospect is

favored. This is because the proportional difference in probabilities is smaller than the proportional difference in money for all pairwise combinations of prospects. Averaging across all pairwise combinations in the free choice condition, the model predicts a skew in preferences towards the more risky prospects, with a "60% chance of £40" most preferred. In the restricted choice conditions, the skew remains, with the most risky prospect being preferred most in each case. These predictions are independent of the decision threshold (which modulates the weight placed on each attribute). However, given the closeness of the overall preference values, we think that it is unlikely that this prediction is independent of the form of the functions mapping actual attribute values into subjective values or the choice of generalization to the multiple prospect case. Thus we conjecture that the stochastic difference model may be flexible enough to accommodate our data.

Multialternative Decision Field Theory. Roe, Busemeyer, and Townsend (2001) extended decision field theory (Busemeyer & Townsend, 1993) to scenarios with multiple alternatives to offer an account of three key results. Consider a binary choice between two options, A and B, that vary on two dimensions, where one option might be higher on one dimension and the other option higher on the other dimension. In the similarity effect (e.g., Tversky, 1972), the addition of a new competitive option that is highly similar to option A, but not option B, can reverse a preference for A in the binary case to a preference for B in the ternary case. The attraction effect (e.g., Huber, Payne, & Puto, 1982) describes the increase in preference for a dominating option, A, when an asymmetrically dominated option is added to the binary set. In the compromise effect (e.g., Simonson, 1989), an option that represents a compromise between two alternatives (A and B) may be preferred over the alternatives in the ternary choice, even though it was not preferred in either pairwise binary choice.

Multialternative decision field theory is able to offer an account of the similarity, attraction, and compromise effects using two key mechanisms. First, attribute values are compared across options, and these (weighted) differences are summed across dimensions to

produce what Roe, Busemeyer, and Townsend (2001) term momentary "valences" for each option. The relative weight for each dimension is assumed to vary over time. Preferences are constructed for each option by integrating valences over time. This process contrasts with the accumulation of absolute attribute values. Instead, valences represent the "comparative affective evaluations" (Roe, Busemeyer, & Townsend, 2001, p. 387). Thus, the choice between options is made in relative rather than absolute terms, as in the stochastic difference model. The second key mechanism is the competition of valences via lateral inhibitory connections such that preferences for more similar options compete more.

There are two natural representations of the simple prospects used in Experiment 4.[7] First, the probability of winning and the amount to win can be considered as separate attributes for each prospect. In this case, the valences for the less risky set (when attending to either the win amount or the win probability) are the same as those for the more risky set. This is because it is the location of the prospects in the space relative to one another that determines their associated valences, rather than their absolute location. Thus multialternative decision field theory predicts that the pattern of preferences should be the same across the less risky and more risky conditions. In other words, the theory predicts pure context effects. Multialternative decision field theory also predicts a tendency to prefer the central prospects in a set in the same way that it predicts the compromise effect.

The second natural representation of the prospects in Experiment 4 uses a single attribute representing the subjective expected utility of each prospect. This representation might be considered more plausible, as it seems rather odd, perhaps, to represent the probability of an outcome happening in the same way as actual outcome attributes (e.g., price, quality). Following the original decision field theory, weights no longer represent the strength of attention to an attribute at a given moment. Instead, weights represent the strength of attention to a world state (as the subjective probabilities in subjective EU theory do). Thus for a given prospect, the valence is the difference in subjective EU for that prospect and the

average subjective EU for all remaining prospects. Thus within a given context, the pattern of valences is the same as the pattern of actual subjective EUs. Thus in the same way that EU cannot predict any context effects, neither can multialternative decision field theory using this second representation.

The Componential-Context Model. Tversky and Simonson (1993) present a model of context dependent preference, which is a generalization of the contingent weighting model (Tversky, Sattath, & Slovic, 1988). The model was devised to provide an account of trade-off contrast and extremeness aversion (Simonson & Tversky, 1992). Each attribute on an object has a subjective value depending on its magnitude. The value of an option is a weighted sum of its attribute values. The value of an option depends on the background context established over previous choices and the current choice set. The effect of the background context is to modify the weighting of each attribute according to the trade-off between attributes implicit in the background context. The value of an option is then modified by the relative value of the option averaged over pairwise comparisons with the other options in the choice set.

Tversky and Simonson (1993) did not apply their model to choices between risky prospects. We consider the representation where probability is simply represented as any other option attribute, as we did for multialternative decision field theory. The effects of choice set in Experiment 4 can then be accounted for as another example of extremeness aversion. Specifically, the componential-context model explains the pattern by assuming that losses on the value of one attribute loom larger than gains in the value of another attribute as the two attributes are traded-off, and thus a central compromise option, where the overall loss is minimized, is preferred. An alternative representation, with a single dimension for the outcome, and probabilities determining the weighting of that outcome, reduces to something like regret theory, and therefore we do not consider it further.

Range Frequency Theory. Range frequency theory (Parducci, 1965, 1974) predicts how items that vary along a single dimension will be valued or rated. The subjective value

given to an attribute is a function of its position within the overall range of attributes, and its rank. Thus attributes are judged purely in relation to one another. Increasing all of the attributes by a constant value, for example, would not change their position within the range or their rank, and thus, according to range frequency theory, their subjective value should remain unaltered.

There is some precedent for using range frequency theory to account for context effects in decision under risk. Birnbaum (1992) found his data to be consistent with the theory. Recall that he investigated the effect of skewing the values of options offered as CEs for simple prospects. The subjective value of a given option will be larger in the positive skew condition since the option will have a higher rank because of the presence of many smaller options. This is consistent with the finding that, when options were positively skewed, prospects were assigned smaller CEs compared to the case where options were negatively skewed.

In all of the experiments presented here, the stimuli can be considered to vary along a single risk dimension. For example, in Experiment 1, selecting an option at one end of the range represents a risk-averse choice, whilst selecting an option at the other end represents a less risk-averse choice. In Experiment 4, the prospects in the set vary from risky (50% chance of £50) through to safe (95% chance of £5). If it is assumed that people are poor at making judgments about the absolute risk attached to each choice, then people may instead make relative judgments (cf. the evaluability hypothesis, Hsee, Loewenstein, Blount, & Bazerman, 1999) of the type described by range frequency theory. Whilst such relative comparisons will allow people to evaluate which options are more risky than others, and even by how much, it does not provide information on how risky the overall set is; all of the options in the set may all be relatively low risk, relatively high risk, or span the entire range of risk. The only strategy a (say) risk-averse person would have left would be to select a relatively safe option. Alternatively, a more risk-prone person could select a relatively more risky option. An

individual following such a strategy will display pure context effects.

Summary of Theoretical Accounts

Theories where prospects are valued independently of one another, such as EU theory, prospect theory, configural weight theory, and RDU theory, must, by definition, fail to predict context effects of the sort reported here. When prospects are judged in relation to one another, as in the stochastic difference model, multialternative decision field theory, and range frequency theory, the effect of choice set can, under some circumstances, be predicted. These relational theories all have in common the idea that preferences are constructed for a given choice set (see Slovic, 1995). Regret theory and the componential-context model can be considered a hybrid theories, where utilities derived independently for each prospect are modified depending on their relationship to other prospects in the choice set.

There are two ways in which to view the challenge to theories of decision under risk that cannot explain the prospect relativity effects shown in this paper. First, assume that the theory is correctly representing the underlying decision process and that the context effects demonstrated here merely represent a biasing of judgments. We discuss this possibility below. However, if people are subject to such biases in making everyday decisions, and we see no reason why they shouldn't be, then the descriptive theories should be revised to provide an account of these effects (see Tversky & Simonson, 1993, for a similar point). Given the large size of the effects, there is a second possibility that should be given some consideration; that the models are inadequate, and should be rejected. It is too early to say which of these possibilities is correct. Hybrid models where an underlying EU-type decision process is biased by the context may prove adequate. Alternatively, purely relative models, where judgments about prospects are made relative to the choice set and other anchors, may be extended to account for the classic phenomena that traditional models describe.

Conversational Pragmatics

An important question for future research concerns whether the impact of the set of

alternatives on people's choices involves reasoning about the experimenter's intentions. That is, is it critical that participants view the options they are given as provided by a co-operative and reasonable experimenter, and hence infer that their response should naturally fall within that range? If it is, then we might explain the performance that we observe as follows: people have a weak grip on a notion of the utility of a risky option, but they may take the options available as a clue from the experimenter about what answers may be appropriate. They might, for example, assume that the experimenter will have chosen the options so that each will be the choice of some experimental participant. Then, if a participant judges that they are, for example, slightly happier with risk than the average participant, they may decide to choose a value slightly higher than the average option available. Accordingly, context would be expected to play a substantial role in determining participants' choices. This would build connections between the current work and pragmatic theory in linguistic communication (e.g., Grice, 1975; Levinson, 1983).[8]

These sorts of pragmatic effects can be very subtle. For example, in Kahneman and Tversky's (1973) demonstration that individuating information is overweighted compared to base rate information when judging a person's occupation, it matters whether participants think the individuating information was compiled carefully by a psychologist, or selected randomly from a pool of sentences describing the target person (Schwarz, Strack, Hilton, & Naderer, 1991). The numerical options attached to descriptive labels on a rating scale can alter the meaning of the labels (Schwarz, Grayson & Knäuper, 1998; Schwarz, Knäuper, Hippler, Noelle-Neumann, & Clark, 1991; Schwarz, Strack, Müller & Chassein, 1988). More dramatically, some research has shown that even when a question is unambiguous, the options given to a participant strongly affect their selection. Schwarz, Hippler, Deutsch and Strack (1985) asked participants to report the number of hours they spent watching television each day. Half of the participants were given a scale that varied from 'up to 1/2 an hour' to 'more than 2 1/2 hours', and half were given the scale 'up to 2 1/2 hours' to 'more than 4 1/2

hours'. Twice as many respondents claimed to have watched less than 2 1/2 hours of television per night with the latter scale (16% vs. 38%). Schwarz (1994) reports that the effect of response alternatives completely disappears when the informational value of the scale is removed (by saying it is a pretest to explore the adequacy of the response alternatives or by informing the student participants that the scale was taken from a survey of the elderly). Given the similarity of these studies to our experiments, our results may well be attributed to conversational pragmatics.

Anchoring Effects

Alternatively, though, it may be that the set of available options merely 'primes' participants' choices in a way that is insensitive to intentional factors. Tversky & Kahneman (1974) have demonstrated large effects of standard or anchor values in judgment. Estimates are typically assimilated towards the anchor provided, even if participants know that the anchors were randomly selected. Use of randomly selected anchors makes it unlikely that participants take their inclusion to be informative. Further, such effects are evident even for quite implausible anchor values (e.g., Chapman & Johnson, 1994). The more uncertain a participant is about a judgment the more his or her estimates are assimilated towards the anchor value (Jacowitz & Kahneman, 1995). This effect of uncertainty is consistent with a demonstration from Mussweiler and Strack (2000a), who showed that, when the context suggested the category to which an item belonged, anchoring effects were smaller compared to the case where the context did not.

Recent research provides evidence that the anchoring effect is largely caused by the retrieval of relevant semantic information, rather than numerical priming (Mussweiler & Strack, 2001a, but see also Wong & Kwong, 2000). When the use of semantic information is prohibited by a change in the target between an initial comparative judgment containing the anchor and a subsequent absolute judgment, only small numerical anchoring effects remain (Mussweiler & Strack, 2001a). When dealing with plausible anchors, participants are

hypothesized to create an anchor-consistent mental model of the target (Mussweiler and Strack, 1999, 2000a; Strack & Mussweiler, 1997). Mussweiler and Strack instantiate this idea in their selective accessibility model by assuming that participants compare a target with an anchor by testing the possibility that the target value is equal to the anchor. This is consistent with the finding that judgments were faster for an implausible anchor, but that subsequent absolute judgments were faster for those participants who had received a plausible anchor. When the anchor is implausible, the judgment can be made without the construction of a mental model of the target. However, when the anchor is plausible a mental model is constructed, causing the judgment to be slower. However, the construction of this model primes the subsequent absolute judgment. For implausible anchors Mussweiler and Strack (2001b) hypothesize that the nearest plausible anchor is considered.

In Experiments 1A-C and Experiment 2, options offered as potential CEs had a large effect on the option chosen. If the options are acting as anchors, then according to Mussweiler and Strack's selective accessibility model of anchoring, participants test the hypothesis that each option is the CE, and this testing process assimilates the judgment of the CE towards the options. It is less obvious how the selective accessibility model might account for the choice results in Experiment 4.

One way to test between anchoring and conversational-pragmatic explanations would be to repeat the experiments here, under conditions where participants believe that the ranges of choices are generated randomly (e.g., by spinning a roulette wheel or similar device). Thus, the participants cannot reasonably attribute these choices to a 'co-operative' experimenter. If the effects described here are intentionally mediated, we would expect the context effects to be eliminated; if they result from non-intentional factors, then they should remain unchanged.

Methodological Implications

The results presented here have implications for the empirical work on descriptive

theories of decision making under risk and uncertainty. There are various procedures that are typically employed as part of this research, but here we divide them into the two broad categories based on the type of questions they employ. Firstly, there are those procedures that require participants to select between two prospects: choice experiments. Secondly, there are those that elicit a quantity, either probabilistic or monetary, which will cause a participant to be indifferent between two prospects: certainty equivalence experiments. A brief, directional poll of 38 such studies finds that 19 fall into the choice category, 16 are based on certainty equivalence and 3 combine the two.

This paper presents no direct evidence regarding choice experiments involving only two prospects (and we are aware of only a handful of other choice based papers that involve simultaneously presenting more than two prospects). However, we note that Weber and Kirsner (1997) succeeded in manipulating participants into exhibiting greater preference for risky options in an experiment offering choices between two prospects, simply by visually emphasising or de-emphasising the highest outcome relative to the lowest outcome of each prospect. If participants' decisions can be influenced by such a comparatively simple contextual manipulation, then it seems reasonable to speculate that distortions equivalent to those described here might also exist. We therefore conclude that this should be the subject of further research, particularly when considering the relevance to at least half the existing experimental literature.

For those papers concerned with certainty equivalence, about one third presented participants with an array of options to choose between, rather than relying on participants to generate their own amounts. For example, Tversky and Fox (1995) elicited CEs using a series of choices. On one side of a computer screen they presented the risky prospect and on the other they presented a sequence of sure payments. Firstly, six sure payments were offered, one at a time, in descending order. These were roughly spaced between the highest outcome available in the risky prospect and $0. Then, seven further options were presented, spanning

the narrower range between the lowest payment the participant had accepted and the highest payment rejected by the participant. Whilst the presentation of prospects in a sequence may have mitigated the influence of the selected scale, the fact that participants could backtrack if they felt they had made a mistake and the general transparency of the procedure could also have induced participants to consider the options simultaneously. Indeed Loomes (1988) has found differences between CEs elicited through such a sequence of choices and those that are generated by participants independently.

If participants' CEs are impacted by the set of choices presented, then it could be countered that when the set is generated using some reasonable and lawful process, in some sense, context had been held constant across the experiment. However, this defense does not seem satisfactory. Whilst we are still lacking a theory to explain the effects of choice set and therefore predict in detail the influence that it has on such experiments, there is no reason for us to assume that these effects will be stable. For example, Tversky and Kahneman (1992) employed a similar sequencing approach to that described for Tversky and Fox (1995). Whilst Tversky and Kahneman (1992) also used seven sure options, spanning the extreme outcomes of the relevant risky prospect, the options were spaced logarithmically. Furthermore, CEs were elicited for a wide variety of outcome ranges, including both gains and losses and differing scales of money. Since all these CEs were then used in combination to fit curves and test cumulative prospect theory, it seems unlikely that the effects of the different contexts during the elicitation process would have acted in the affine manner necessary to preserve the findings. For other examples of potentially distorted CEs see Cohen, Jaffray, and Said (1987), Hershey and Schoemaker (1985), and Lichtenstein, Slovic, and Zink (1969).

The findings we have described have potentially important implications for practical survey research methods that are used to elicit people's utilities. One implication, which we have already discussed, is that providing sets of response options can substantially, if

unintentionally, bias people's responses. But these results may also have a second, and more fundamental implication concerning the existence of an underlying scale of utility for risky prospects.

The present studies were inspired by Garner's (1954) study showing that people's judgments of what sound is half as loud as another sound can be dramatically manipulating by choosing different responses alternatives. Laming (1997) argues that this result is the strongest single piece of evidence against the notion that there is an underlying internal psychophysical scale for loudness, an assumption that has been taken for granted in much psychophysical research (e.g., Stevens, 1975). If Laming's reasoning is correct it would seem that the present data provide equal difficulties for the idea that there is an underlying internal utility scale for risky prospects. If this is the case, then the project of asking people to make judgments about risky prospects may be ill-founded; and hence, decision analysis methods which typically involve such judgments (see Baron, 2000, for a review) may also be difficult to interpret. Thus, for example, the so-called "standard gamble" method of eliciting preferences, in which people value the outcome of interest by choosing a probability mixture of two other standard comparison gambles seems to be undermined, if people cannot meaningfully assign utilities to risky prospects, such as probability mixtures. Similarly, contingent valuations studies (Cummings, Brookshire, & Schulzze, 1986; Mitchell & Carson, 1989), which are widespread in environmental economics, frequently require people to assign a value to some risky outcome (the possibility of a nuclear accident or an oil-spill), which they may be unable to do.

If this line of reasoning is accepted, then a natural recommendation is to elicit preferences for "simple" outcomes rather than risky prospects. Related problems may, of course, arise, to the degree that people evaluate simple outcomes by considering prospects over their consequences. But it is also possible that the prospect relativity effects that we have found here do not apply only in the context of risk. It is possible that similar effects might be

found, even where people make direct judgments about simple outcomes (e.g., judging that one injury is twice as bad as another; or that a level of disability is a certain fraction along a continuum between normal health and death). If response options can radically affect people's judgments in contexts of these kinds, then concerns must at least be raised over the existence of an underlying "subjective utility" that can be elicited. If the concept of a subjective utility that can be elicited is not to be abandoned, then, at minimum, important theoretical developments will be required to show how utility-based models can be flexible enough to capture these effects.

There is already some evidence that challenges the notion of an underlying "subjective probability" scale. Slovic and Monahan (1995) investigated risk perceptions in mental health law, and found that probability judgments were quite malleable. Participants read vignettes describing various attributes of a person supposedly interviewed by a psychiatrist because of mental illness. Participants estimated "the probability that this person will harm someone else during the three years following the examination" and whether this person should be described as dangerous. Two sets of probability options were used. (This experiment, then, is analogous to our Experiments 1A-C, and so we describe it in some detail.) In the large probability condition options ran from 0% to 100% in increments of 10%. In the small probability condition there were 13 options, starting with <1/1000, with increasing increments up to >40%. Both lay and psychiatric professionals exhibited strong effects of the options available. In the small probability condition the six categories which were less than or equal to 10% attracted 67.7% of the vignettes. This compares to 10.8% in the large probability condition. Likewise, the mean probability of doing harm was judged as 44% in the large probability condition and 12% in the small probability condition. Furthermore, whilst the effect was smaller, there was also a carry-over consequence from the probability condition to the participants' judgments of dangerousness. In the small probabilities condition, 30.5% of the vignettes were described as dangerous, versus 37.0% for

large probabilities condition. That similar results were also found for participants' judgments on whether a patient should be hospitalized, even if it involved coercion, dramatically highlights the social importance of context effects in decision making.

Concluding Remarks

The data presented here suggest that prospects are not valued independently of the other options available in the choice set, whether the options are potential CEs or other prospects. This finding presents another challenge to EU theory as a descriptive theory of decision under risk and to other theories where prospects are independently valued. We considered accounts of this finding in terms of conversational pragmatics, anchoring, and theories of choice where prospects are valued relative to other prospects in the choice set.

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Appendix

Table A1

Free Choice Certainty Equivalents and Options for Experiment 1A, 1B, and the narrow condition of 1C.

Prospect		Free choice		Option							
p	x	Mean	SD	L_1	L_2	L_3	L_4	H_1	H_2	H_3	H_4
.2	200	35.0	36.8	15	20	25	30	40	45	50	55
.4	200	48.2	35.1	25	30	35	40	55	60	65	70
.6	200	90.7	94.4	50	60	70	80	100	110	120	130
.8	200	100.0	64.0	60	70	80	90	110	120	130	140
.2	400	70.4	71.5	50	55	60	65	75	80	85	90
.4	400	92.9	65.5	20	40	60	80	100	120	140	160
.6	400	142.9	91.3	60	80	100	120	160	180	200	220
.8	400	148.6	104.2	70	90	110	130	170	190	210	230
.2	600	102.5	102.5	20	40	60	80	120	140	160	180
.4	600	138.6	105.1	60	80	100	120	160	180	200	220
.6	600	225.0	176.8	125	150	175	200	250	275	300	325
.8	600	269.3	176.4	175	200	225	250	300	325	350	375
.2	800	95.0	104.5	20	40	60	80	110	130	150	170
.4	800	161.4	109.7	80	100	120	140	180	200	220	240
.6	800	212.9	171.0	125	150	175	200	250	275	300	325
.8	800	324.3	192.7	225	250	275	300	350	375	400	425
.2	1000	140.0	136.7	100	110	120	130	150	160	170	180
.4	1000	207.9	136.2	120	140	160	180	220	240	260	280
.6	1000	298.6	190.6	200	225	250	275	325	350	375	400
.8	1000	382.9	267.5	200	250	300	350	450	500	550	600

Note: In selecting the options, participants whose free choice values followed an inconsistent pattern (e.g., increasing their certainty equivalent as the amount to win was reduced) were excluded.

Table A2

Free Choice Certainty Equivalents and Options for Experiment 1B.

| Prospect | | Free choice | | | | | | | | | |
p	x	Mean	SD	L₁	L₂	L₃	L₄	H₁	H₂	H₃	H₄
.2	200	40.7	19.0	16	22	28	34	46	52	58	64
.4	200	70.2	23.0	30	40	50	60	80	90	100	110
.6	200	92.1	30.2	50	60	70	80	100	110	120	130
.8	200	122.1	41.6	60	75	90	105	135	150	165	180
.2	400	71.0	32.9	30	40	50	60	80	90	100	110
.4	400	121.7	49.8	60	75	90	105	135	150	165	180
.6	400	197.1	64.9	120	140	160	180	220	240	260	280
.8	400	279.5	69.1	200	220	240	260	300	320	340	360
.2	600	80.5	47.5	40	50	60	70	90	100	110	120
.4	600	199.8	93.1	120	140	160	180	220	240	260	280
.6	600	292.9	92.0	210	230	250	270	310	330	350	370
.8	600	390.7	105.5	290	315	340	365	415	440	465	490
.2	800	133.8	73.4	55	75	95	115	155	175	195	215
.4	800	261.7	99.5	160	185	210	235	285	310	335	360
.6	800	324.3	146.0	185	220	255	290	360	395	430	465
.8	800	511.0	174.1	350	390	430	470	550	590	630	670
.2	1000	149.5	85.6	70	90	110	130	170	190	210	230
.4	1000	311.9	92.5	210	235	260	285	335	360	385	410
.6	1000	444.1	165.8	305	340	375	410	480	515	550	585
.8	1000	666.7	160.6	490	535	580	625	715	760	805	850

Table A3

Free Choice Splits and Options and for Experiment 2

		Free choice y					y Option			
z	p	Mean	SD	L_1	L_2	L_3	L_4	H_1	H_2	H_3	H_4
250	20	59.7	15.5	52	54	56	58	62	64	66	68
250	40	82.3	20.2	66	70	74	78	86	90	94	98
250	60	96.1	17.6	84	87	90	93	99	102	105	108
250	80	102.9	13.5	91	94	97	100	106	109	112	115
500	20	109.4	36.0	86	92	98	104	116	122	128	134
500	40	170.0	43.2	142	149	156	163	177	184	191	198
500	60	192.8	18.4	170	175	180	185	195	200	205	210
500	80	204.7	30.2	185	190	195	200	210	215	220	225
750	20	174.2	54.2	140	150	160	170	190	200	210	220
750	40	240.7	66.4	200	210	220	230	250	260	270	280
750	60	285.8	46.4	245	255	265	275	295	305	315	325
750	80	304.1	49.0	276	283	290	297	311	318	325	332
1000	20	232.2	101.3	170	185	200	215	245	260	275	290
1000	40	323.8	49.4	274	286	298	310	334	346	358	370
1000	60	370.7	87.1	322	334	346	358	382	394	406	418
1000	80	416.9	28.4	375	385	395	405	425	435	445	455
1250	20	299.4	121.5	220	240	260	280	320	340	360	380
1250	40	404.7	99.4	345	360	375	390	420	435	450	465
1250	60	479.7	99.2	420	435	450	465	495	510	525	540
1250	80	514.7	102.9	466	478	490	502	526	538	550	562
1500	20	363.8	173.7	265	290	315	340	390	415	440	465
1500	40	499.1	121.5	440	455	470	485	515	530	545	560
1500	60	590.0	112.5	510	530	550	570	610	630	650	670
1500	80	645.7	79.8	585	600	615	630	660	675	690	705
1750	20	436.7	208.3	310	340	370	400	470	500	530	560
1750	40	585.6	121.7	505	525	545	565	605	625	645	665
1750	60	678.3	131.3	600	620	640	660	700	720	740	760
1750	80	770.7	80.6	710	725	740	755	785	800	815	830
2000	20	445.3	166.8	305	340	375	410	480	515	550	585
2000	40	659.4	123.1	580	600	620	640	680	700	720	740
2000	60	771.6	128.5	670	695	720	745	795	820	845	870
2000	80	870.6	111.6	790	810	830	850	890	910	930	950

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Footnotes

[1]This experiment differs from Birnbaum's (1992) experiment. Birnbaum manipulated the distribution of potential CE options whilst holding the maximum and minimum constant. Here, the spacing of potential CE options has been held constant, while the maximum and minimum have been manipulated.

[2]We thank Jonathon Baron for suggesting this analysis.

[3]Consider the options £401, £402, £403, £404 as CEs for the prospect 50% chance of £1000. Much of the time the true CE will lie outside this narrow range, and thus the extreme options should be selected much of the time.

[4]The choice of a power function is a reasonably standard assumption. Fishburn and Kochenberger (1979) fitted power and exponential functions and found that although there was little difference between these two functions, they both fitted the data better than a linear function. See Bell and Fishburn (1999) for a consideration of alternative functions, and Luce (2000, pp. 80-84).

[5]In empirical studies (e.g., Prelec, 1998; Wu & Gonzalez, 1996, 1999), the decision weight function is typically found to be inverse s-shaped.

[6]The evaluation of prospects containing both gains and losses follows a different rule.

[7]Roe, Busemeyer, and Townsend (2001) do not consider MDFT for probabilistic outcomes.

[8]We thank Klaus Fiedler for pointing out the importance of this issue.

Table 1

Results of Experiment 5. The first two columns are the prospect attributes, the next three are

the number of participants who selected each prospect, and the remaining two columns are

the predictions for the more risky and less risky conditions based on the free choice data.

		Condition			Predictions	
p	x	Free choice	More risky	Less risky	Free choice (more risky)	Free choice (less risky)
0.5	50	8	10		8	
0.55	45	0	3		0	
0.60	40	0	9		0	
0.65	35	3	4		3	
0.70	30	3	5		19	
0.75	25	6		8		20
0.80	20	3		2		3
0.85	15	1		8		1
0.90	10	5		9		5
0.95	5	1		3		1
		30	31	30	30	30

Figure Captions

Figure 1. The dotted and dashed curve represents a hypothetical free choice distribution of certainty equivalents. The leftmost set of labels (L_1 - L_4) represents the options available in the low options condition. The rightmost set (H_1 - H_4) represents the options available in the high options condition. The spacings of the options represent those used in Experiment 1A, 1B, and the narrow options condition of Experiment 1C.

Figure 2. The proportion of times each option was chosen in Experiment 1A. (Error bars are standard error of the mean.)

Figure 3. The proportion of times each option was chosen in Experiment 1B. (Error bars are standard error of the mean.)

Figure 4. The proportion of times each option was chosen in Experiment 1C. The spacing of the options on the abscissa is to scale across the three spacing conditions. (Error bars are standard error of the mean.)

Figure 5. The proportion of times each option was chosen in Experiment 2. (Error bars are standard error of the mean.)

Figure 6. Prospects used in Experiment 3. Curves represent contours of equal expected value.

Figure 7. Certainty equivalents for the prospect on the current trial as function of the expected value of the previous prospect.

Figure 8. The utility of simple prospects of the form "p chance of x". x and p are linearly related so increasing the probability of winning, p, reduces the amount won, x. The different curves represent different degrees of risk aversion, from risk neutral (γ=1.0) to very risk averse (γ=0.2). To force the curves to lie in the same range, utility has been normalized for each curve, so that maximum utility over the entire prospect set is 1 for each value of γ.
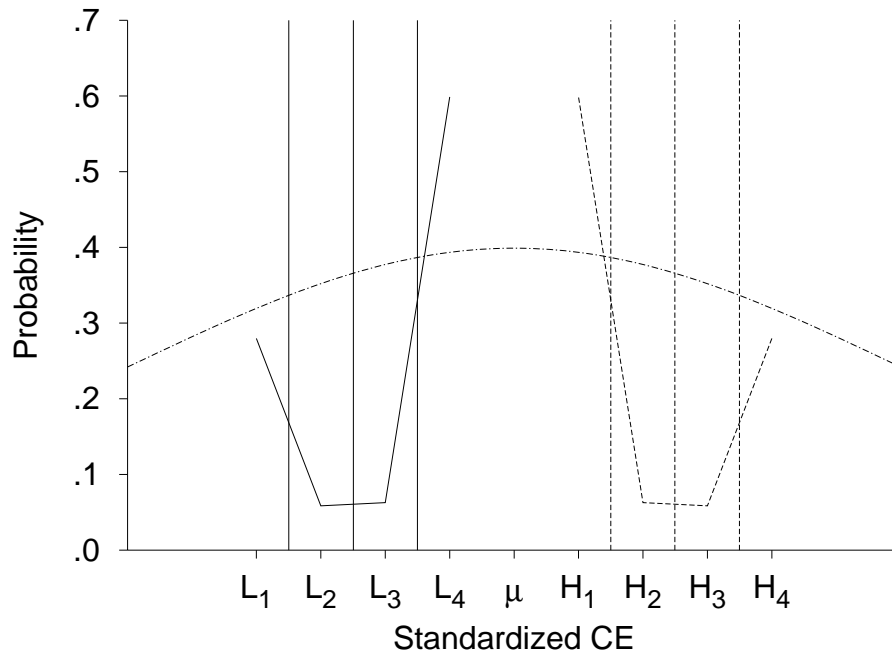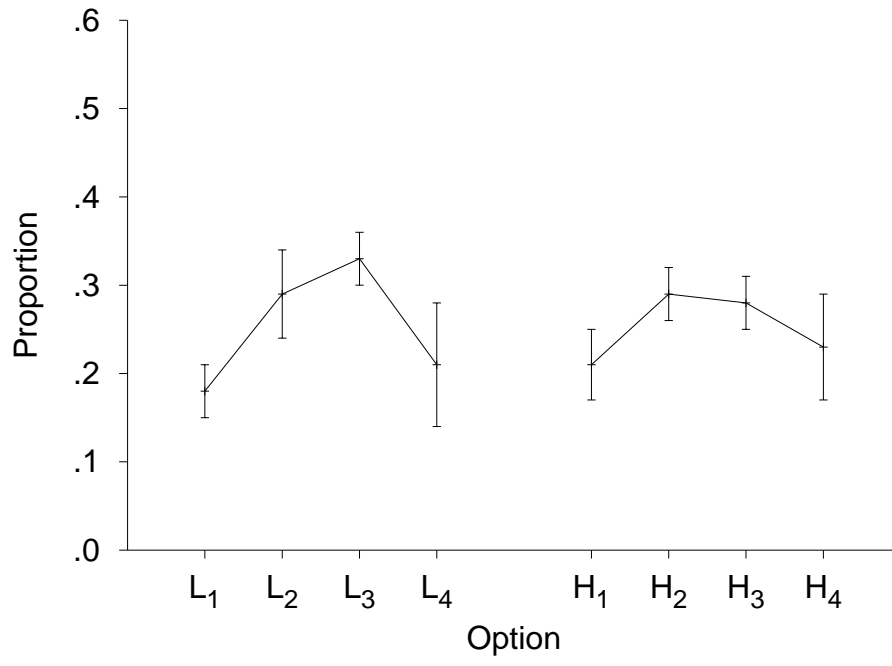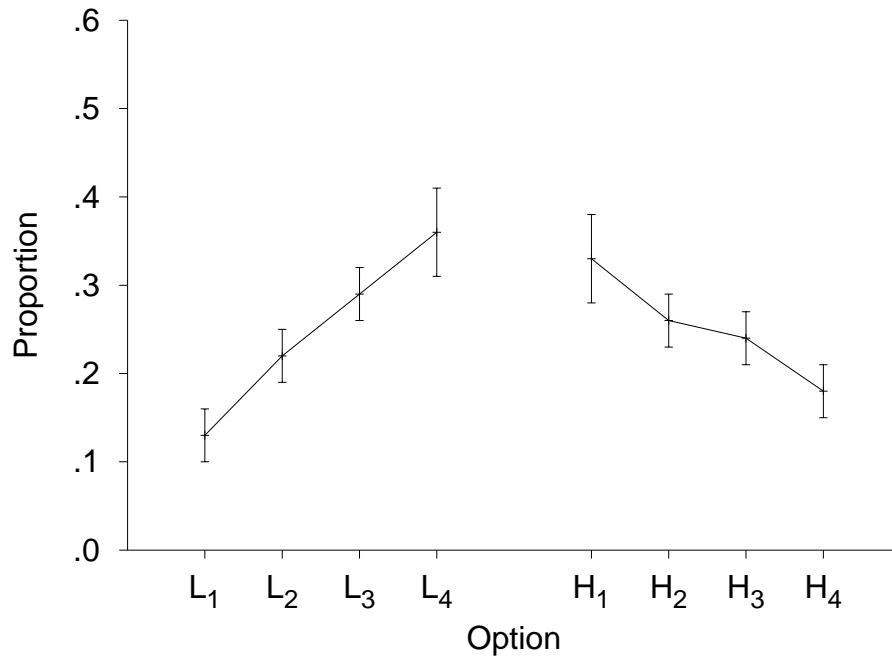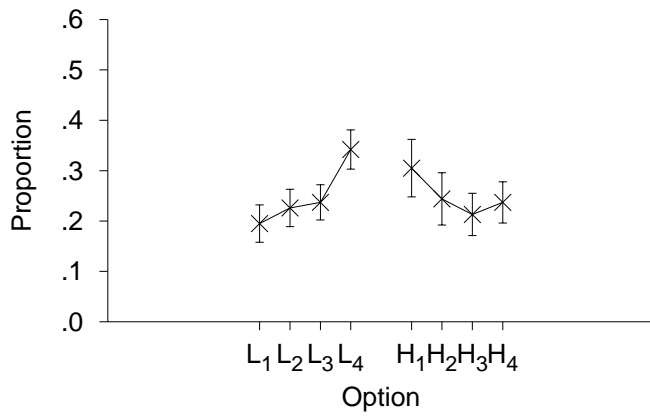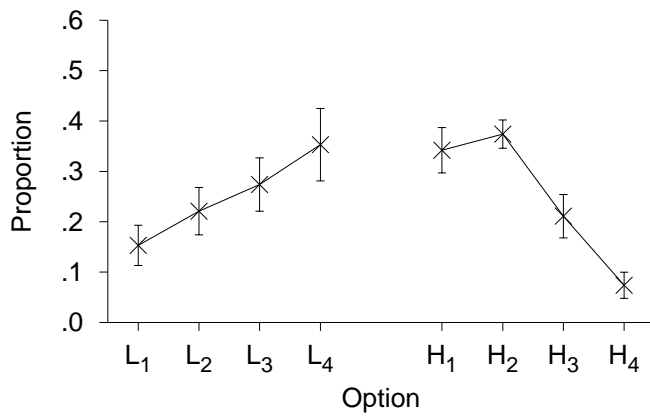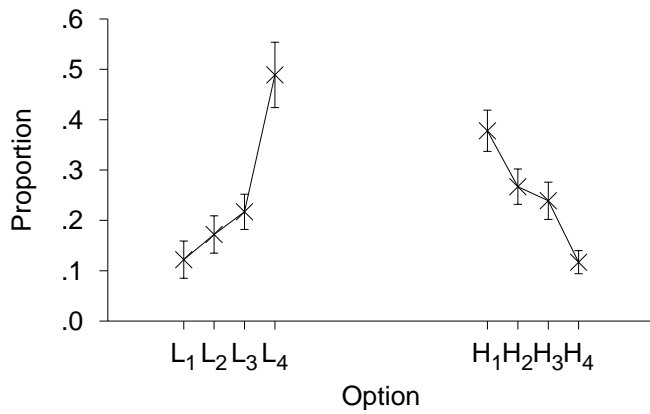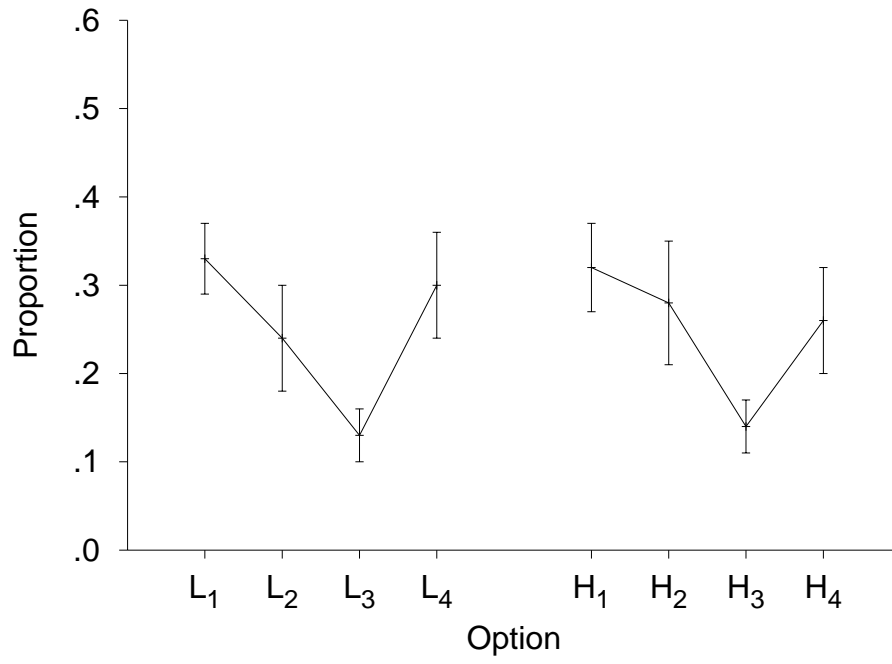
Figure 1
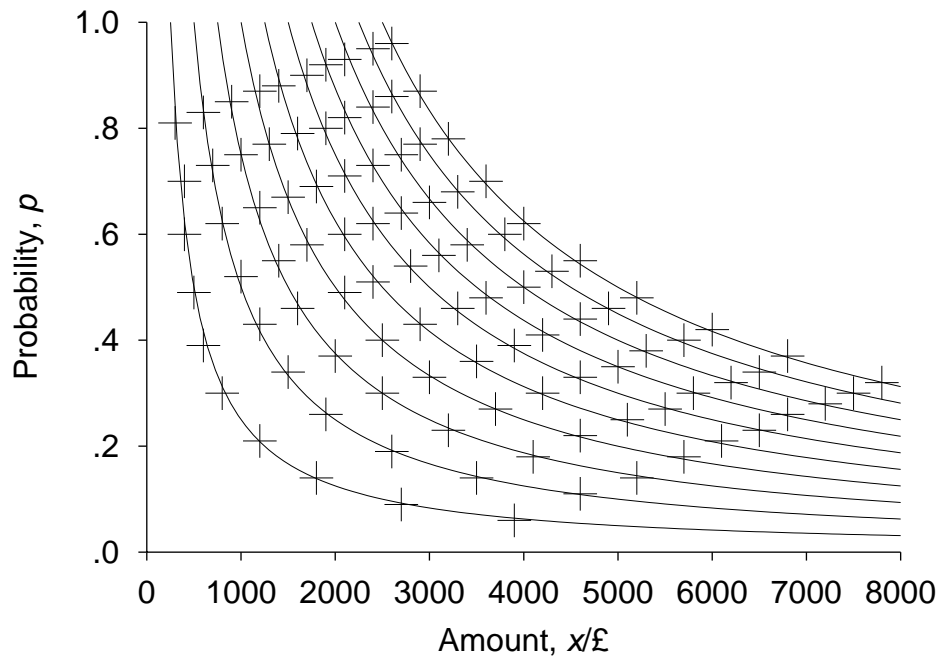
Figure 2

Figure 3

Figure 4

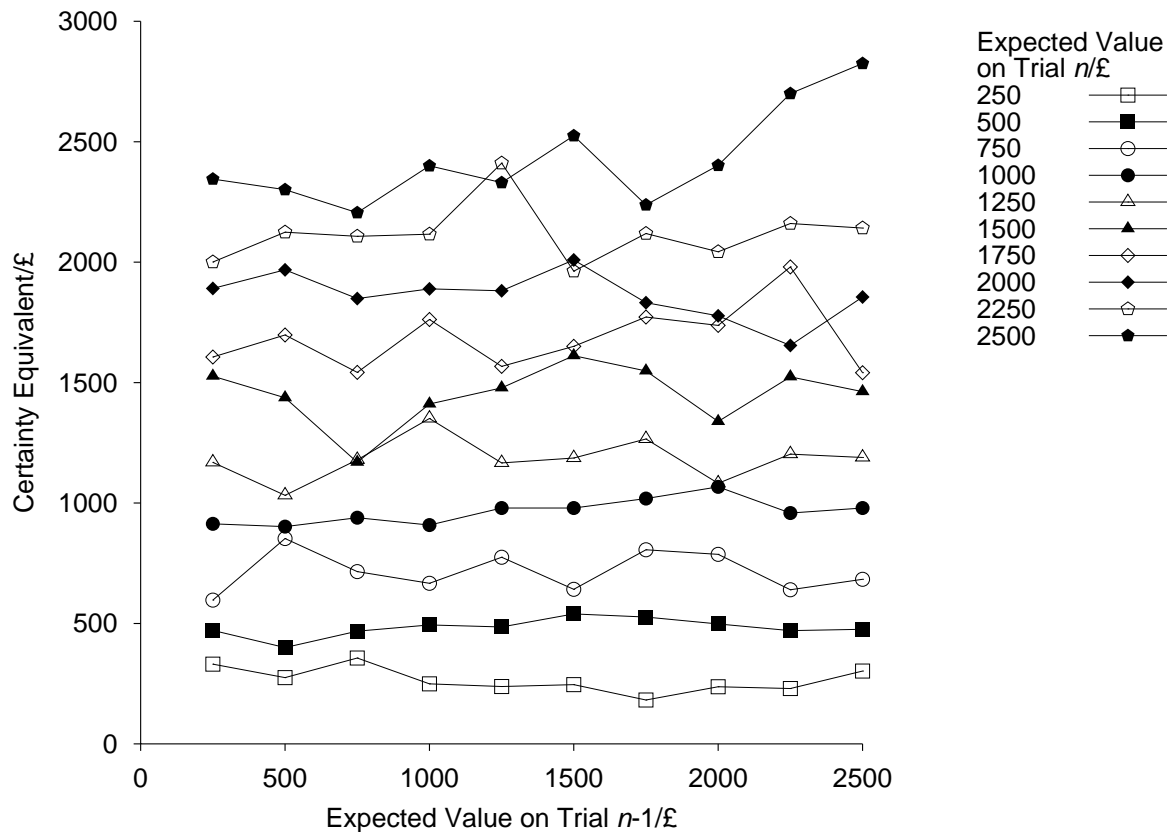A Narrow

B Wide

C Gap

Figure 5

Figure 6

Figure 7

Figure 8