Optimal Decentralized Spectral Resource Allocation for OFDMA Downlink of Femto Networks via Adaptive Gradient Vector Step Size Approach

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ABSTRACT

For the orthogonal frequency division multiple access (OFDMA) downlink of a femto network, the resource allocation scheme would aim to maximize the area spectral efficiency (ASE) subject to constraints on the radio resources per transmission interval accessible by each femtocell. An optimal resource allocation scheme for completely decentralized femtocell deployments leads to a nonlinear optimization problem because the cost function of the optimization problem is nonlinear. In this paper, an adaptive gradient vector step size approach is proposed for finding the optimal solution of the optimization problem. Computer numerical simulation results show that our proposed method is more efficient than existing exhaustive search methods.

Index Terms—Optimal decentralized spectral resource allocation, OFDMA downlink, macro/femto networks, ASE, nonlinear optimization, adaptive gradient vector step size approach.

I. INTRODUCTION

Mobile user equipments (UEs) have become increasingly important in our daily lives and mobile operators have been spending a lot of money and efforts to meet the growing customer demands. However, most current cellular networks suffer from poor indoor network coverage and cellsite usage saturation. As a consequence, mobile operators face poor customer retain-ability and increasing churn. One cost-effective solution for mobile operators to improve coverage and offload macrocell traffic as well as to reduce churn is the emerging femtocell paradigm. Typically, a large number of femtocell access points (FAPs) [1] are overlaid on macrocells. Each FAP provides high data-rate connections to UEs within a short range using the same radio access technology as the macrocell underlay.

A pertinent challenge for mobile operators is the management of interference between neighbouring femtocells. As FAPs are likely to be deployed by end users, the total number and locations of active FAPs are *a priori* unknown to mobile operators. Therefore, interference caused by femtocells cannot be managed using conventional network planning methods, and interference avoidance strategies are preferred over mutual interference in the hierarchical macro/femto network is closely related to the femtocell access policy, which defines the way how a femtocell allows or restricts its usage to users [2]. This paper will focus on the closed access femtocell, which serves a group of authorized UEs only, since the closed access policy would be preferred by subscribers of the femtocell [3].

As OFDMA has been considered in the downlink for next generation wireless networks [4]-[5], OFDMA based femtocells are widely expected to deliver massive improvements in coverage and capacity [1]. To mitigate intercell interference, frequency reuse [6]-[8] and intercell coordination [9], [10] schemes have been studied in OFDMA macro networks. A centralized downlink frequency planning across femtocells and macrocells was proposed in [11], but the large number of femtocells significantly complicates the centralized optimization process.

The spectrum allocation policy in [12] avoids cross-tier interference by assigning orthogonal spectrum resources to the macrocell and femtocell tiers and diminishes femto-to-femto interference by allowing each femtocell to access only a random subset of the spectrum resources that are assigned to the femtocell tier. As a result, the average number of

interfering femtocells in each frequency sub-channel is reduced. The portion of spectrum resources accessible by each femtocell is determined based on optimizing the throughput per cell and ASE [12]. To optimize such a decentralized resource allocation leads to an optimization problem for which the cost function is nonlinear. Although the nonlinear optimization problem was solved by exhaustive search methods [12]-[13], the computational costs of which are very high. In this paper we propose an adaptive gradient vector step size approach for finding the optimal solution of the nonlinear optimization problem so that the computational costs could be reduced.

The rest of the paper is organized as follows. The problem formulation of the decentralized spectral resource allocation for the OFDMA downlink of femto networks is presented in Section II. In Section III, the adaptive gradient vector step size approach is proposed for finding the optimal solution of the optimization problem. Computer numerical simulation results are presented in Section IV. Finally, conclusions are drawn in Section V.

II. PROBLEM FORMULATION

We consider the OFDMA downlink of a macro/femto cellular network. Closed access femtocells are randomly overlaid on the macrocell and the locations of FAPs form a stationary Poisson point process (SPPP) on \Re^2 [14]. It is assumed that macrocells and femtocells in the network are allocated with orthogonal spectrum resources, and there is no macro-to-femto or femto-to-macro interference. This paper focuses on the decentralized resource allocation between femtocells only. Denote the radius of a hexagonal macrocell and the spatial intensity of FAPs as r_M and λ_F , respectively, where λ_F is defined as the average number of femtocells per unit area. Denote the radius of each femtocell and the number of indoor UEs to be served by each femtocell as r_F and U_F , respectively, where it is assumed that they are the same for all femtocells. Denote the average number of FAPs per macrocell as N_F . Since cellular networks are typically interference limited, thermal noise at the receiver is neglected in this paper.

The basic resource unit that is addressable for OFDMA transmissions is a resource block (RB), which is a two dimensional block defined in the time and frequency domains. In the third generation partnership project (3GPP) long term evolution (LTE) release 8 [15], an RB has a time duration of 1 ms and spans either 12 subcarriers with a subcarrier bandwidth of 15 kHz or 24 subcarriers with a subcarrier bandwidth of 7.5 kHz. Intracell interference is avoided by maintaining the orthogonality among co-cell UEs in OFDMA networks [16], i.e, maintaining one scheduled UE per RB in each cell. Not to clutter subsequent analysis, it is

assumed that an FAP assigns equal transmission power all over RBs for a given transmission interval.

Let the total number of distinct RBs available to all femtocells for each transmission time interval be $F (\in Z^+)$. Each FAP is allowed to use only $K (\in Z^+, K \le F)$ RBs for downlink transmissions in each transmission time interval. For ease of implementation, the value of *K* is assumed to be the same for all femtocells. Define the fraction of radio resources per transmission interval accessible by each femtocell as ρ_F and we have

$$\rho_F = \frac{K}{F},\tag{1}$$

where $0 \le \rho_F \le 1$. When $\rho_F = 1$, each femtocell can access all the available RBs.

If each femtocell chooses the *K* distinct RBs independently and with equal probability, then the probability of a femtocell selecting a given RB for transmission is ρ_F . This implies that the average number of interfering femtocells in each RB is effectively reduced and the femto-to-femto interference is diminished.

For a given RB, denote the received signal to interference ratio (SIR) of a femto UE as SIR_F, the distance from an interfering FAP to the femto UE of interest as $|X_{Fi}|$, the path loss exponent on the link from the home FAP to the femto UE as α_F , the path loss exponent on the link from an interfering FAP to the femto UE as α_{FF} , the channel power gain between the home FAP and the femto UE as $H_0 \sim \text{EXP}(1)$ (unit mean exponential distribution), the channel power gain between an interfering FAP and the femto UE as $H_{0i} \sim \text{EXP}(1)$, the indoor lognormal shadowing on the link from the home FAP to the femto UE as Θ_0 , and the lognormal shadowing on the link from an interfering FAP to the femto UE as Θ_{0i} . It is assumed that all H_0 , H_{0i} , Θ_0 and Θ_{0i} are mutually independent. Let the mean and the standard deviation of Θ_0 be μ and σ , respectively, and those of Θ_{0i} be μ_i and σ_i , respectively, i.e., $\Theta_0 \sim \text{LN}(\zeta \mu, \zeta^2 \sigma^2)$ and $\Theta_{0i} \sim \text{LN}(\zeta \mu_i, \zeta^2 \sigma_i^2)$, where all Θ_{0i} are i.i.d and $\zeta = 0.1 \ln 10$ is a scaling constant [12]. Denote the single-wall penetration loss as ϕ . Consider the case of double-wall penetration losses for links from an interfering FAP to the femto UE. The worst case scenario that all femto UEs are located on the edge of their home femtocells is assumed. Denote the index set corresponding to all FAP, that have access to the given RB as Φ , then we have

$$SIR_{F} = \frac{\Theta_{0}H_{0}r_{F}^{-\alpha_{F}}}{\sum_{i \in \Phi} \Theta_{0i} \phi^{2}H_{0i} |X_{Fi}|^{-\alpha_{FF}}}.$$
(2)

The product of a lognormal shadowing and an exponential fading coefficient can be modeled as a lognormal distribution using Turkmani's approximation [17]. That is, $\Theta_0 H_0$ is approximated by a lognormal random variable denoted as $\Psi_0 \sim \text{LN}(\mu', \sigma'^2)$ where $\mu' = \zeta(\mu - 2.5)$ and $\sigma' = \zeta \sqrt{\sigma^2 + 5.57^2}$. Similarly, each $\Theta_i H_i$ is approximated by a lognormal random variable denoted as $\Psi_{0i} \sim \text{LN}(\mu'_i, \sigma'^2)$ where $\mu'_i = \zeta(\mu_i - 2.5)$ and $\sigma'_i = \zeta \sqrt{\sigma_i^2 + 5.57^2}$. Then, (2) can be simplified to

$$SIR_{F} = \frac{\psi_{0} r_{F}^{-\alpha_{F}}}{\sum_{i \in \Phi} \psi_{0i} \phi^{2} |X_{Fi}|^{-\alpha_{FF}}}.$$
(3)

Define the boundary of the SIR as Γ . Based on (3), the cumulative distribution function (CDF) of the SIR of a femto UE can be calculated as

$$\Pr(\operatorname{SIR}_{F} \leq \Gamma) = \Pr\left(\frac{\psi_{0}r_{F}^{-\alpha_{F}}}{\sum_{i \in \Phi} \psi_{0i} \phi^{2} |X_{Fi}|^{-\alpha_{FF}}} \leq \Gamma\right)$$

$$= E_{\psi_{0}}\left(\Pr\left(\sum_{i \in \Phi} \psi_{0i} \phi^{2} |X_{Fi}|^{-\alpha_{FF}} \geq \frac{\psi_{0}r_{F}^{-\alpha_{F}}}{\Gamma} |_{\psi_{0}}\right)\right)$$

$$\geq 1 - E_{\psi_{0}}\left(\exp\left(-\pi\lambda_{F}\rho_{F}E\left(\psi_{I}^{\delta_{f}}\left(\frac{\Gamma}{\psi_{0}r_{F}^{-\alpha_{F}}}\right)^{\delta_{f}}\right)\right)\right)$$

$$= 1 - E_{\psi_{0}}\left(\exp\left(-\rho_{F}k_{f}\Gamma^{\delta_{f}}\psi_{0}^{-\delta_{f}}\right)\right), \quad (4)$$

where $\delta_f \equiv \frac{2}{\alpha_{\rm FF}}$, ψ_I is the equivalent value of $\psi_i \quad \forall i \in \Phi$, $k_f \equiv \pi \lambda_F E(\psi_I^{\delta_f}) r_{\rm F}^{\alpha_F \delta_f}$, $E_{\psi_0}(\cdot)$ and $E(\psi_I^{\delta_f})$ are the expected values with respect to ψ_0 and ψ_I , respectively.

Define the total number of discrete rates that an adaptive modulation realizes as $L \in Z^{\dagger}$, the Shannon gap of quadrature amplitude modulations (QAMs) as Ψ , the boundaries of the SIR ranges as Γ_l for $l \in \{1,...L\}$, and the transmission rates as b_l for $l \in \{1,...L\}$. When the UE received SIR lies in $[\Gamma_l, \Gamma_{l+1})$ for $l \in \{1,...L\}$, the FAP decides the transmission rate according to

$$b_l = \log_2\left(1 + \frac{\Gamma_l}{\Psi}\right), \quad (b/s/Hz).$$
 (5)

With $b_l = l$ for l = 1, 2, ..., L, the expected throughput of a femtocell is given by

$$T_{f} = \sum_{l=1}^{L-1} l \operatorname{Pr}\left(\Gamma_{l} \leq \operatorname{SIR}_{F} < \Gamma_{l+1}\right) + L \operatorname{Pr}\left(\operatorname{SIR}_{F} \geq \Gamma_{l}\right)$$

$$= \sum_{l=1}^{L-1} l E_{\psi_{0}} \left[\exp\left(-\rho_{F} k_{f} \Gamma_{l}^{\delta_{f}} \psi_{0}^{-\delta_{f}}\right) - \exp\left(-\rho_{F} k_{f} \Gamma_{l+1}^{\delta_{f}} \psi_{0}^{-\delta_{f}}\right) \right] + L E_{\psi_{0}} \left[\exp\left(-\rho_{F} k_{f} \Gamma_{L}^{\delta_{f}} \psi_{0}^{-\delta_{f}}\right) \right]$$

$$= E_{\psi_{0}} \left[\sum_{l=1}^{L} l \exp\left(-\rho_{F} k_{f} \Gamma_{l}^{\delta_{f}} \psi_{0}^{-\delta_{f}}\right) - \sum_{l=1}^{L-1} l \exp\left(-\rho_{F} k_{f} \Gamma_{l+1}^{\delta_{f}} \psi_{0}^{-\delta_{f}}\right) \right]$$

$$= E_{\psi_{0}} \left[\sum_{l=1}^{L} \exp\left(-\rho_{F} k_{f} \Gamma_{l}^{\delta_{f}} \psi_{0}^{-\delta_{f}}\right) \right]. \tag{6}$$

Then the ASE offered by the femtocell network is given by $ASE_{E}(\rho_{E}) = \rho_{E}\lambda_{E}T_{E}$

$$= \rho_F \lambda_F \operatorname{E}_{\psi_0} \left[\sum_{l=1}^{L} \exp\left(-\rho_F k_f \Gamma_l^{\delta_f} \psi_0^{-\delta_f}\right) \right]$$

$$= \rho_F \lambda_F \int_0^{+\infty} \left[\sum_{l=1}^{L} \exp\left(-\rho_F k_f \Gamma_l^{\delta_f} \psi_0^{-\delta_f}\right) \right] p(\psi_0) d\psi_0$$
, (7)

where $p(\psi_0) = \frac{1}{\psi_0 \sigma' \sqrt{2\pi}} \exp\left(-\frac{(\ln(\psi_0) - \mu')^2}{2\sigma'^2}\right)$ is the PDF of ψ_0 . Hence, the decentralized

spectrum resource allocation that maximizes the ASE_F can be formulated as the following optimization problem:

Problem (P')

$$\max_{\rho_F} \qquad ASE_F(\rho_F), \tag{8a}$$

subject to
$$0 < \rho_F \le 1$$
. (8b)

This maximization problem is equivalent to the following minimization problem:

Problem (P)

$$\min_{\rho_F} \quad -\operatorname{ASE}_F(\rho_F), \tag{9a}$$

subject to $0 < \rho_F \le 1$. (9b)

III. ADAPTIVE GRADIENT VECTOR STEP SIZE APPROACH

According to (7), problem (\mathbf{P}) is a nonlinear optimization problem. Exhaustive search methods are used for finding the optimal solution of problem (\mathbf{P}) [12], [13]. However, the computational costs of exhaustive search methods are very high [12], [13]. In order to solve

the optimization problem efficiently, we propose the following method for finding the optimal solution of problem (\mathbf{P}).

Algorithm

Step 1:

Initialize k=1, $\rho_1 \in [0,1]$, $\varepsilon > 0$, D > 1 and $\alpha_1 > \varepsilon$.

Step 2:

Case I:

If
$$\alpha_k \ge \varepsilon$$
 and $-ASE_F\left(\rho_k + \alpha_k \frac{\partial ASE_F(\rho)}{\partial \rho}\Big|_{\rho=\rho_k}\right) \le -ASE_F(\rho_k)$, where
 $\frac{\partial}{\partial \rho_F} ASE_F(\rho_F) = \int_0^{+\infty} \frac{\lambda_F}{\psi_0 \sigma' \sqrt{2\pi}} \exp\left(-\frac{(\ln(\psi_0) - \mu')^2}{2\sigma'^2}\right) \sum_{l=1}^L \left\{\frac{\partial}{\partial \rho_F} \left[\rho_F \exp\left(-\rho_F k_f \Gamma_l^{\delta_f} \psi_0^{-\delta_f}\right)\right]\right\} d\psi_0$
 $= \int_0^{+\infty} \frac{\lambda_F}{\psi_0 \sigma' \sqrt{2\pi}} \exp\left(-\frac{(\ln(\psi_0) - \mu')^2}{2\sigma'^2}\right) \sum_{l=1}^L \left[\left(1 - k_f \Gamma_l^{\delta_f} \psi_0^{-\delta_f} \rho_F\right) \exp\left(-\rho_F k_f \Gamma_l^{\delta_f} \psi_0^{-\delta_f}\right)\right] d\psi_0$

then define $\rho_{k+1} \equiv \rho_k + \alpha_k \frac{\partial ASE_F(\rho)}{\partial \rho}\Big|_{\rho = \rho_k}$ and $\alpha_{k+1} \equiv \alpha_k$. Increment the value of k to k+1 and

iterate Step 2.

Case II:

If
$$\alpha_k \ge \varepsilon$$
 and $-ASE_F\left(\rho_k + \alpha_k \frac{\partial ASE_F(\rho)}{\partial \rho}\Big|_{\rho=\rho_k}\right) > -ASE_F(\rho_k)$, then define $\rho_{k+1} \equiv \rho_k$ and

 $\alpha_{k+1} \equiv \frac{\alpha_k}{D}$. Increment the value of k to k+1 and iterate Step 2.

If $\alpha_k < \varepsilon$, then go to Step 3.

Step 3:

Take the value of ρ_k as the optimal solution of Problem (**P**).

The working principal of the algorithm is as follows. Step 1 is the initialization routine. Step 2 is the main optimization routine. $-\frac{\partial ASE_F(\rho)}{\partial \rho}\Big|_{\rho=\rho_k}$ is the slope of the curve $-ASE_F(\rho)$ evaluated at ρ_k and α_k relates to the incremental step size between the current evaluation point and the test evaluation point, where the test evaluation point is set at $\rho_k + \alpha_k \frac{\partial ASE_F(\rho)}{\partial \rho}\Big|_{\rho=\rho_k}$ and α_k is initially set at a large value. If $-ASE_F(\rho, + \alpha, \frac{\partial ASE_F(\rho)}{\partial \rho}\Big|_{\rho=\rho_k}) \leq -ASE_F(\rho)$, then the next evaluation point is set at the test

$$-ASE_F\left(\left.\rho_k+\alpha_k\frac{\partial ASE_F(\rho)}{\partial\rho}\right|_{\rho=\rho_k}\right) \leq -ASE_F(\rho_k)$$
, then the next evaluation point is set at the test

evaluation point $\rho_{k+1} = \rho_k + \alpha_k \frac{\partial ASE_F(\rho)}{\partial \rho}\Big|_{\rho=\rho_k}$, and α_k is remained unchanged. It is worth noting

that as
$$-ASE_F\left(\rho_k + \alpha_k \frac{\partial ASE_F(\rho)}{\partial \rho}\Big|_{\rho=\rho_k}\right) \leq -ASE_F(\rho_k)$$
, the next evaluation point

 $\rho_{k+1} = \rho_k + \alpha_k \frac{\partial ASE_F(\rho)}{\partial \rho} \Big|_{\rho = \rho_k}$ is moving closer to the optimal solution, because the cost value

evaluated at the next evaluation point is smaller than that at the current evaluation point. The incremental step size between two consecutive evaluation points depends on α_k . As α_k is initially set at a large value, the next evaluation point is moving towards the optimal solution significantly. Thereby, the proposed method could significantly improve the convergence rate and reducing the computational costs. It is worth noting that if $-\frac{\partial ASE_F(\rho)}{\partial \rho}\Big|_{\rho=\rho_k} < 0$, then

$$-ASE_{F}(\rho_{k}^{+}) < -ASE_{F}(\rho_{k}). \text{ If } \left. -\frac{\partial ASE_{F}(\rho)}{\partial \rho} \right|_{\rho=\rho_{k}} > 0, \text{ then } -ASE_{F}(\rho_{k}^{-}) < -ASE_{F}(\rho_{k}). \text{ In other words,}$$

$$-ASE_{F}\left(\rho_{k}+\alpha\frac{\partial ASE_{F}(\rho)}{\partial\rho}\Big|_{\rho=\rho_{k}}\right) \leq -ASE_{F}(\rho_{k}) \quad \text{if} \quad \alpha \to 0^{+} \quad \text{and} \quad -\frac{\partial ASE_{F}(\rho)}{\partial\rho}\Big|_{\rho=\rho_{k}} \neq 0 \quad \text{However, if}$$

 $-ASE_{F}\left(\rho_{k}+\alpha_{k}\frac{\partial ASE_{F}(\rho)}{\partial\rho}\Big|_{\rho=\rho_{k}}\right) > -ASE_{F}(\rho_{k}), \text{ then it implies that the test evaluation point has been}$

moved beyond the optimal solution. Hence, the next evaluation point is set at the current evaluation point, that is $\rho_{k+1} = \rho_k$, but α_k is reduced according to $\alpha_{k+1} = \frac{\alpha_k}{D}$, in which D > 1. By iterating the above procedures, the optimal solution can be reached efficiently. Finally, if α_k is reduced to a very small value such that $\alpha_k < \varepsilon$, then the algorithm terminates and we can assume that the optimal solution is reached.

In order not to terminate the algorithm when the convergence rate of the algorithm is slow and to have a high accuracy of the solution, ε should be chosen at a small value and Dshould be chosen as a positive number larger than but close to 1. We choose, $\varepsilon = 10^{-6}$ and D = 1.0001 which are good enough for most applications. The initial search point of the optimization algorithm ρ_1 is set at the midpoint of the range of ρ_F , that is $\rho_1 = 0.5$. As α_1 should be set to a large value initially, we set it as 0.1, which is good enough for most applications.

IV. COMPUTER NUMERICAL SIMULATIONS

For a fair comparison of our proposed method with the exhaustive search method (with

100 searching points) [12], the same set of parameter values used in [12] are employed in our simulations. That is, L = 8, $\delta_f = 0.5714$, $\Gamma_l = (2^l - 1) \times 10^{0.3}$ for $l = 1, 2, \dots, 8$, $\mu = 0$ dB, $\sigma^2 = 4 \text{ dB}, \quad \mu_i = 0 \text{ dB} \quad \forall i \in \Phi \quad \text{and} \quad \sigma_i^2 = 12 \text{ dB} \quad \forall i \in \Phi , \quad r_F = 40 \text{ and} \quad r_M = 288 \text{ for}$ $N_f = 10,50,100$. Based on these sets of parameters, we ran the proposed adaptive gradient vector step size algorithm and obtain optimal values of ρ_F as shown in Figure 1, i.e. $\rho_F = 1$ for $N_f = 10$, $\rho_F = 0.55$ for $N_f = 50$ and $\rho_F = 0.3$ for $N_f = 100$, which are the same as those obtained by exhaustive searches in [12]. It is worth noting that there is only one single stationary point in the curves shown in the Figure. This is because of the nature of the probability density functions. However, in terms of the computational cost, it takes only 4.5687 seconds for running our proposed algorithm for these three cases, while it takes 7.8321 minutes for running the exhaustive search method [12] under the same computer setup in a computer with the AMD Athlon(tm) II X4 630 Processor 2.8GHz, 6.00GB RAM and 64-bit operating system (windows 7 Home Premium). Hence, it can be concluded that our proposed method is more efficient than the exhaustive search method. Figure 1 shows the different strategies that can be adopted in order to maximize the ASE. For a small number of femtocells in the network ($N_f = 10$), it is best for each femtocell to access the entire allocated spectrum ($\rho_F = 1$). On the other hand, the higher the number of femtocells in the network ($N_f = 100$), the lower the percentage of accessible allocated spectrum for each femtocell ($\rho_F = 0.3$) is required in order to maximize the ASE.

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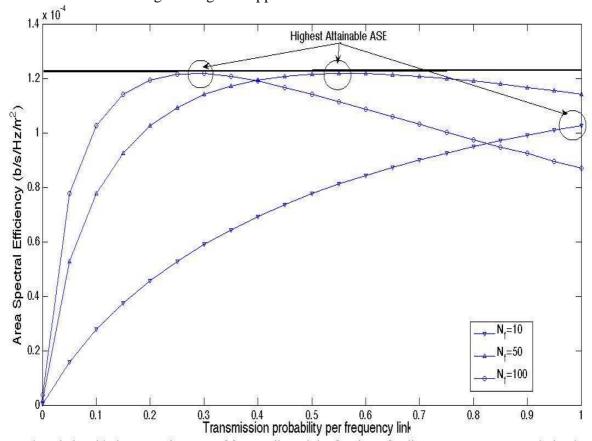


Figure 1. The relationship between the ASE of femtocells and the fraction of radio resources per transmission interval

V. CONCLUSIONS

In this paper, an adaptive gradient vector step size approach is proposed for finding the optimal solution of the decentralized resource allocation scheme for the OFDMA downlink of a femto network. The ASE is maximized subject to a constraint on the radio resource per transmission interval accessible by each femtocell. Based on the numerical computer simulation results, it can be concluded that the computational costs of our proposed method are much lower than that of the existing exhaustive search methods.

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