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CoMapping: Efficient 3D-Map Sharing Methodology for Decentralized cases

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Abstract—CoMapping is a framework to efficient manage, share, and merge 3D map data between mobile robots. The main objective of this framework is to implement a Collaborative Mapping for outdoor environments. The framework structure is based on two stages. During the first one, the Pre-Local Mapping stage, each robot constructs a real time pre-local map of its environment using Laser Rangefinder data and low cost GPS information only in certain situations. Afterwards, the second one is the Local Mapping stage where the robots share their pre-local maps and merge them in a decentralized way in order to improve their new maps, renamed now as local maps. An experimental study for the case of decentralized cooperative 3D mapping is presented, where tests were conducted using three intelligent cars equipped with LiDAR and GPS receiver devices in urban outdoor scenarios. We also discuss the performance of the cooperative system in terms of map alignments.

I. INTRODUCTION

Mapping the environment can be complex since in certain situations, e.g. in large regions, it may require a group of robots that build the maps in a reasonable amount of time with regards to the expected accuracy [1]. A set of robots extends the capability of a single robot by merging measurements from group members, providing each robot with information beyond their individual sensors range. This leads to a better usage of resources and execution of tasks which are not feasible by a single robot. Multi-robot mapping is considered as a centralized approach when it requires all the data to be analysed and merged at a single computation unit. Otherwise, in a decentralized approach, each robot builds their local maps independent of one another and merge their maps upon rendezvous.



Fig. 1. Scheme of our CoMapping System considering a decentralized case

Figure 1 depicts the scheme of work proposed in this article for a group of robots where it was assumed that ZOE robot have direct exchange of data (as pose, size and limits of maps) with FLUENCE and GOLFCAR. And by contrast, FLUENCE and GOLFCAR are in a scenario of non-direct communication,

with limited access conditions to a same environment, and without any meeting point for map sharing between these mobile units.

Following this scenario, this paper presents the development and validation of a new Cooperative Mapping framework (CoMapping) where:

- In the first stage named “Pre-Local Mapping”, each individual robot builds its map by processing range measurements from a 3D LiDAR moving in six degrees of freedom (6-DOF) and using low cost GPS data (GPS/GGA).
- For the second stage named “Local Mapping”, the robots send a certain part of their pre-local maps to the other robots based on our proposed Sharing algorithm. The registration process includes an intersecting technique of maps to accelerate processing.

This work is addressed to outdoor environments applications denied of a continuous GPS service by using a decentralized approach. Our proposal has been tested and validated in an outdoor environment, with data acquired on the surroundings of the ECN (École Centrale Nantes) campus.

II. RELATED WORKS

In a scenario of cooperative mapping, robots first operate independently to generate individual maps. Here the registration method plays a fundamental role. Many registration applications use LiDAR as a Rangefinder sensor for map building [2]. However, a high Lidar scan rate can be harmful for this task, since it may create distortion in the map construction. For those cases, ICP approaches [3] can be applied to match different scans. Implementations, for 2 or 3-axis and geometric structures matches of a generated local point set, were presented in [4] [5]. Those methods use batch processing to build maps offline. In the first stage of our implementation we reconstruct maps as 3D point clouds in real-time using 3-axis LiDAR by extraction and matching of geometric features in Cartesian space based in [6]. Then our system uses GPS position data to coarsely re-localize that cloud in a global frame.

Once all the maps have been projected on a global frame, they have to be merged together to form a global map. In this context, [7] proposed a method for 3D merging of occupancy grid maps based on octrees [8] for multi-robots.

The method was validated in a simulation environment. For the merging step, an accurate transformation between maps was assumed as known, nevertheless in real applications, that information is not accurate, since it is obtained by means of uncertain sensor observations. In our case, real experiments were performed for a multi-robot application without perfect knowledge of the transformations between the maps. In [9] a pre-merging technique is proposed, which consists in selecting the subset of points included in the common region between maps bounding. Then, a centralized merging process refines the transformation estimate between maps by ICP registration [3]. We use a variation of [9] but previously we include an efficient technique to exchange maps between robots in order to optimize bandwidth.

Other solutions may be used in order to merge maps for a group of robots with a centralized approach [10], [9], [11], which are generally found in the literature. However this kind of solutions can compromise the team performance because merging and map construction depend exclusively on a processing unit. Another approach less explored and analysed is the decentralized one [12], [1], [13]. The advantage in this case lies in the independence and robustness of the system because map construction is not affected even if one of the robots has failures in communication or processing, since map merging can be executed in different units after traversing the environment. This kind of approach can consider a meeting point for the vehicles in order to exchange their maps and other data. This approach is also investigated in our final experiments.

III. METHODOLOGY

A. Pre-Local Mapping Stage

Each mobile robot executes a Pre-Local Mapping system using data provided by a LidarSLAM process. We just use coarse GPS position to project the generated map on a global frame. In order to reduce implementation costs, a beneficial cheap GPS service was used, specifically GPS/GGA (*Global Positioning System Fix Data*) at an accuracy of about 2 to 7 meters. Another advantage of our Pre-Local Mapping Stage is its versatile configuration, since it does not depend on a specific LidarSLAM method.

A modified version of the LOAM technique¹ [6] was thus chosen as the LidarSLAM method for this work.

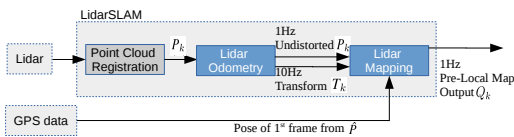


Fig. 2. Architecture of Pre-Local Mapping Stage

Figure 2 illustrates the block diagram of this stage, where \hat{p} is the raw point cloud data generated by a laser scanner in the beginning. The accumulated point cloud up to sweep k

is denoted P_k and processed by a *Lidar Odometry* algorithm, which runs at a frequency around 10Hz and computes the lidar motion (transform T_k) between two consecutive sweeps. The distortion in P_k is corrected using the estimated lidar motion. The resulting undistorted P_k is processed at a frequency of 1Hz by an algorithm known as *Lidar Mapping*, which performs the matching and registration of the undistorted cloud onto a map. Using the GPS information of the vehicle pose, it is possible to coarsely project the map of each robot into common coordinate frame for all the robots. This projected cloud is denoted as the Pre-Local Map.

1) *Lidar Odometry step*: The step begins with feature points extraction from the cloud P_k . The feature points are selected from sharp edges and planar surface patches. Let us define \bar{S} as the set of consecutive points i returned by the laser scanner in the same scan, where $i \in P_k$. An indicator proposed in [6] evaluates the smoothness of the local surface as following:

$$\bar{c} = \frac{1}{|\bar{S}| \cdot \|X_{(k,i)}^L\|} \left\| \sum_{j \in \bar{S}, j \neq i} (X_{(k,i)}^L - X_{(k,j)}^L) \right\|, \quad (1)$$

where $X_{(k,i)}^L$ and $X_{(k,j)}^L$ are the coordinate of two points from the set \bar{S} .

Moreover, a scan is split into four subregions to uniformly distribute the selected feature points within the environment. In each subregion is determined maximally two edge points and four planar points. The criteria to select the feature points as edge points is related to maximum \bar{c} values, and by contrast the planar points selection to minimum \bar{c} values. When a point is selected, it is thus mandatory that none of its surrounding points are already selected. Besides, selected points on a surface patch cannot be approximately parallel to the laser beam, or on boundary of an occluded region.

When the correspondences of the feature points are found, then the distances from a feature point to its correspondence are calculated. Those distances are named as d_E and d_H for edge points and planar points respectively. The minimization of the overall distances of the feature points leads to the Lidar odometry. That motion estimation is modeled with constant angular and linear velocities during a sweep.

Let us define E_{k+1} and H_{k+1} as the sets of edge points and planar points extracted from P_{k+1} , for a sweep $k+1$. The lidar motion relies on establishing a geometric relationship between an edge point in E_{k+1} and the corresponding edge line:

$$f_E(X_{(k+1,i)}^L, T_{k+1}^L) = d_E, i \in E_{k+1}, \quad (2)$$

where T_{k+1}^L is the lidar pose transform between the starting time of sweep $k+1$ and the current time t_i . Analogously, the relationship between a planar point in H_{k+1} and the corresponding planar patch is:

$$f_H(X_{(k+1,i)}^L, T_{k+1}^L) = d_H, i \in H_{k+1}, \quad (3)$$

¹LOAM: https://github.com/laboshin/loam_velodyne

Equations (2) and (3) can be reduced to a general case for each feature point in E_{k+1} and H_{k+1} , leading to a nonlinear function:

$$\mathbf{f}(T_{k+1}^L) = \mathbf{d}, \quad (4)$$

in which each row of \mathbf{f} is related to a feature point, and \mathbf{d} possesses the corresponding distances. Levenberg-Marquardt method [14] is used to solve the Equation (4). Jacobian matrix (\mathbf{J}) of \mathbf{f} with respect to T_{k+1}^L is computed. Then, the minimization of \mathbf{d} through nonlinear iterations allows solving the sensor motion estimation:

$$T_{k+1}^L \leftarrow T_{k+1}^L - (\mathbf{J}^T \mathbf{J} + \lambda \text{diag}(\mathbf{J}^T \mathbf{J}))^{-1} \mathbf{J}^T \mathbf{d}, \quad (5)$$

where λ is the Levenberg-Marquardt gain.

Finally, the *Lidar Odometry* algorithm produces a pose transform T_{k+1}^L that contains the lidar tracking during the sweep between $[t_{k+1}, t_{k+2}]$ and simultaneously an undistorted point cloud \bar{P}_{k+1} . Both outputs will be used by the Lidar Mapping step, detailed in the next section.

2) *Lidar Mapping step*: This algorithm is used only once per sweep and runs at a lower frequency (1 Hz) than the Lidar Odometry step (10 Hz). The technique matches, registers and projects the cloud \bar{P}_{k+1} provided by the Lidar Odometry as a map into the coordinate system of a vehicle, noted as $\{V\}$. To understand the technique behaviour, let us defined Q_k as the point cloud accumulated until sweep k , and T_k^V as the sensor pose on the map at the end of sweep k , t_{k+1} . The algorithm extends T_k^V for one sweep from t_{k+1} to t_{k+2} , to get T_{k+1}^V , and projects \bar{P}_{k+1} on the robot coordinate system, denoted as \bar{Q}_{k+1} . Then, by optimizing the lidar pose T_{k+1}^V , the matching of \bar{Q}_{k+1} with Q_k is obtained.

In this step the feature points extraction and their correspondences are calculated in the same way as in Lidar Odometry, the difference just lies in that all points in \bar{Q}_{k+1} share the time stamp, t_{k+2} .

In that context, nonlinear optimization is solved also by the Levenberg-Marquardt method [14], registering \bar{Q}_{k+1} on a new accumulated cloud map. To get a uniform points distribution, down-sampling is performed to the cloud using a voxel grid filter [15] with a voxel size of 5 cm cubes.

Finally, since we have to work with multiple robots, we use a common coordinate system for their maps, $\{W\}$, coming from rough GPS position estimation of the 1st accumulated cloud frame Q_k .

B. Local Mapping Stage

In this section the Local Mapping is detailed, considering that the process is executed on the robot "i" with a shared map by robot "n" (see Figure 3).

1) *Map Sharing Step*: When the generation of Pre-Local Maps is done, the robots would have to exchange their maps to start the map alignment process. In several cases the sharing and processing of large maps can affect negatively the performance of the system with respect to runtime and

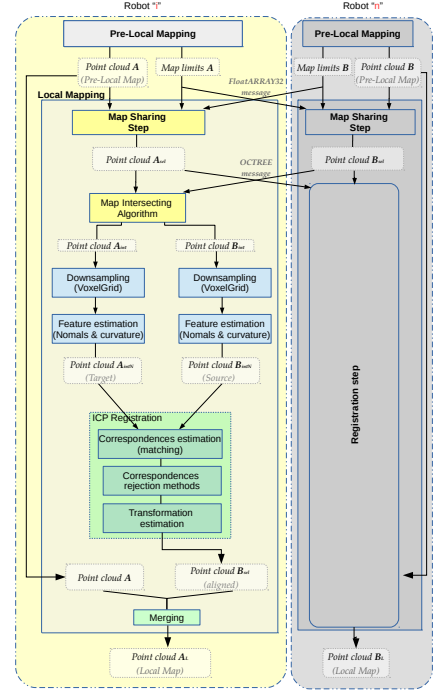


Fig. 3. Architecture of Local Mapping Stage for one robot "i", receiving map data from another robot "n".

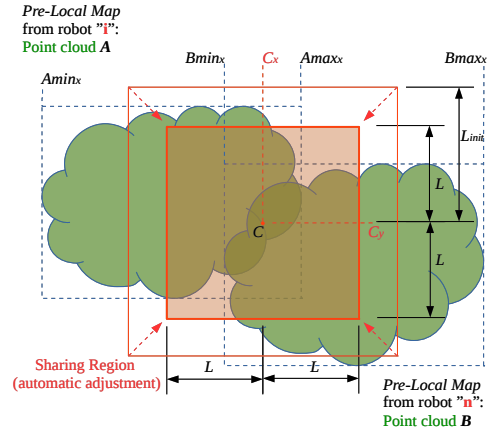


Fig. 4. Graphical representation of the Map Sharing technique (Top view of plane XY). $Amin_x$, $Amax_x$, $Bmin_x$ and $Bmax_x$ represent the point cloud limits along the x-axis.

memory usage. A sharing technique is presented in order to overcome this problem, in which each vehicle only sends a certain subset of points of its map to the other robots. When the maps are ready for transferring, they are compressed in octree format using OctoMap library [8] in order to optimize the robot-communication.

The proposed sharing technique is based on the method developed in [16]. Figure 4 depicts the behaviour, wherein point clouds A and B represent the Pre-Local Maps from two robots "i" and "n" respectively. In each robot the algorithm first receives only information about the 3D limits of the maps (i.e. bounding cubic lattice of the point clouds) and then

decides what part of its map will be shared to the other robot. These limits were determined previously using the function $GetBounds()$ that returns two vectors: in the first one, $Amin$, their components represent the lowest displacement from the origin along each axis in the point cloud; and the other vector, $Amax$, is related to the point of the highest displacement.

Data: Point Cloud A ; Limits: Vectors $Amin$, $Amax$, $Bmin$ and $Bmax$; Parameters: Scalars L_{init} , L_{step} , Np_{max}

Result: Point Cloud A_{sel}

```

begin
   $A_{sel} \leftarrow \emptyset$ ;
   $C_x = 0$ ;  $C_y = 0$ ;  $C_z = 0$ ;
   $(V2_x, V3_x) =$ 
   $GetValues(Amin_x, Amax_x, Bmin_x, Bmax_x)$ ;
   $(V2_y, V3_y) =$ 
   $GetValues(Amin_y, Amax_y, Bmin_y, Bmax_y)$ ;
   $(V2_z, V3_z) =$ 
   $GetValues(Amin_z, Amax_z, Bmin_z, Bmax_z)$ ;
   $C_x = (V2_x + V3_x)/2$ ;
   $C_y = (V2_y + V3_y)/2$ ;
   $C_z = (V2_z + V3_z)/2$ ;
   $Np = PointSize(A)$ ;
  for ( $L=L_{init}$  ;  $Np > Np_{max}$  ;  $L = L - L_{step}$ ) do
     $Smin_x = C_x - L$  ;  $Smax_x = C_x + L$ ;
     $Smin_y = C_y - L$  ;  $Smax_y = C_y + L$ ;
     $Smin_z = C_z - L$  ;  $Smax_z = C_z + L$ ;
    foreach  $a \in A$  do ;
      if  $Smin_x < a_x < Smax_x$  and  $Smin_y < a_y <$ 
       $Smax_y$  and  $Smin_z < a_z < Smax_z$  then
        |  $A_{sel} = A_{sel} + a$ ;
      end
    end
     $Np = PointSize(A_{sel})$ ;
  end
end

```

Algorithm 1: Selection of Point Cloud to share with another robot.

Pseudo-code of the map sharing step is described in Algorithm 1. Inside the code, the function $GetValues()$ sorts in ascending order the array of components along each axis of the vectors $Amin$, $Amax$, $Bmin$, $Bmax$ and returns the 2nd and 3rd values from this sorted array, denoted $V2$ and $V3$ respectively. Then for each axis, the average of the two values obtained by the function $GetValues()$ is used in order to determine the Cartesian coordinate (C_x, C_y, C_z) of the geometric center of the sharing region S . This map sharing region is a cube whose edge length $2L$ is determined iteratively. The Points from A contained in this cube region are extracted to generate a new point cloud A_{sel} . In each iteration the cube region is reduced until the number of points from A_{sel} is smaller than the manual parameter Np_{max} , which represents the number of points maximum that the user wants to exchange between robots. Once the loop ends, A_{sel} is sent to the other robot. Analogously on the other mobile robot “n”, the points from B included in this region are also extracted to obtain and share B_{sel} with the another robot “i”. Finally, the clouds A_{sel} and B_{sel} are encoded and sent in octree format to reduce

the usage of bandwidth resources of the multi-robot network. Then maps are decoded and reconverted in 3D point cloud format to be used in the Registration step.

2) *Registration Step:* The intersecting volumes of the two maps A_{sel} and B_{sel} are computed and denoted as A_{int} and B_{int} , obtained from the exchanged map bounds [9]. In order to improve the computation speed, point clouds A_{int} to B_{int} first go through a down-sampling process to reduce the number of points in the cloud alignment. Feature descriptors as surface normals and curvature are used to improve the matching, which is the most expensive stage of the registration algorithm [17]. These generated normal-point clouds A_{intN} and B_{intN} are then used by Iterative Closest Point (ICP) algorithm [18]. This method refines an initial alignment between clouds, which basically consists in estimating the best transformation to align a source cloud B_{intN} to a target cloud A_{intN} by iterative minimization of an error metric function. At each iteration, the algorithm determines the corresponding pairs (b', a') , which are the points from A_{intN} and B_{intN} respectively, with the least Euclidean distance.

Then, least squares registration is computed and the mean squared distance E is minimized with regards to estimated translation t and rotation R :

$$E(R, t) = \frac{1}{Np_{b'}} \sum_{i=1}^{Np_{b'}} \| a'_i - (R b'_i + t) \|^2, \quad (6)$$

where $Np_{b'}$ is the number of points b' .

The resulting rotation matrix and translation vector can be express in a homogeneous coordinate representation (4×4 transformation matrix T_j) and are applied to B_{intN} . The algorithm then re-computes matches between points from A_{intN} and B_{intN} , until the variation of mean square error between iterations is less than a defined threshold. The final ICP refinement for n iterations can be obtained by multiplying the individual transformations: $T_{ICP} = \prod_{j=1}^n T_j$. Finally the transformation T_{ICP} is applied to the point cloud B_{sel} to align and merge with the original point cloud A , generating the Local Map A_L then. Each robot thus performed its own merging according to data from other agents within communication range. We now present the corresponding experimental results.

IV. RESULTS



Fig. 5. Vehicles used in the tests: ZOE, FLUENCE and GOLFCAR.

In this section we show results validating the presented concepts and the functionality of our system. As we consider ground vehicles, the ENU (East-North-Up) coordinate system is used as external reference of the world frame $\{W\}$, where y -axis corresponds to North and x -axis corresponds to East,

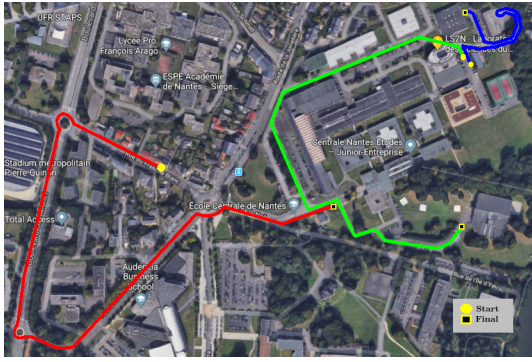


Fig. 6. Paths followed by ZOE (green one), FLUENCE (red one) and GOLFCAR robot (blue one) during experiments. Image source: Google Earth.

but coinciding its origin with the GPS coordinate [Longitude: -1.547963; Latitude: 47.250229].

The proposed framework is validated considering three vehicles for experiments, a *ZOE Renault*, a *FLUENCE Renault* and a *GOLFCAR* (see Figure 5) customized and equipped with a *Velodyne VLP-16 3D LiDAR*, with 360° horizontal and a 30° vertical field of view. All data come from the campus outdoor environment in an area of approximately 1000m x 700m. The vehicles traversed that environment following different paths and collected sensor observations about the world, running pre-local mapping process in real-time.

For the validation, the vehicles build clouds from different paths (see Figure 6). Results of the Pre-Local Mapping of this experiment are shown in Figure 7.

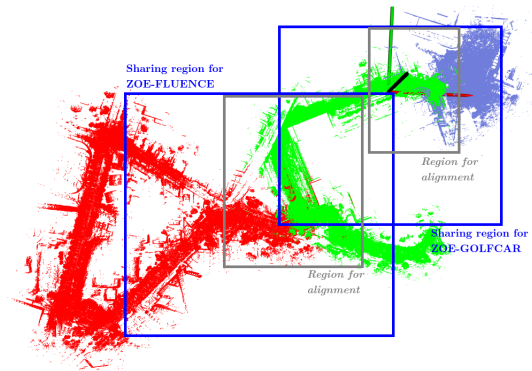


Fig. 7. Top view of unaligned Pre-Local Maps generated by ZOE (green one), FLUENCE (red one) and GOLFCAR robot (blue one) projected on common coordinate system

Figure 7 also depicts the “sharing region” determined during the map exchange process in each robot. It was assumed that all the vehicles have the constraint of exchanging a maximum number of points $N_{p_{max}}$ of 410000 to simulate restrictions in resources of bandwidth network or memory usage in robots. The tests were divided in two. In the first one, test A, ZOE and FLUENCE car define a meeting point to transfer their maps. Around this position, ZOE car exchanges and updates its local map and then a new point of rendezvous for map sharing is determined by ZOE and GOLFCAR in the following test B.

As we assume a decentralized scenario, each robot performs a relative registration process considering its Pre-Local map as target cloud for alignment reference. Each vehicle also executes the intersecting algorithm and then an ICP refinement to obtain an improved transform between each map. Figures 8 and 9 depict in yellow color the intersection between the shared point clouds during the alignment process. Once the refined transformation is obtained, it is then applied to the shared map.

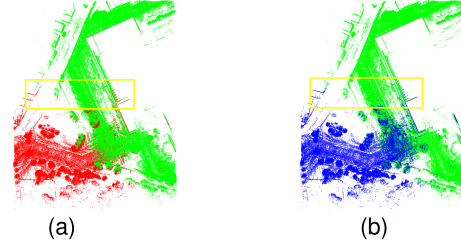


Fig. 8. Test A: Alignment of the intersecting regions with ICP refinement performed in ZOE robot, when it received the FLUENCE map (a) Green and red maps represent the target and source clouds pre ICP, top view (b) Green and blue maps represent the target and aligned source clouds post ICP, top view. Alignment can be better appreciated in yellow box

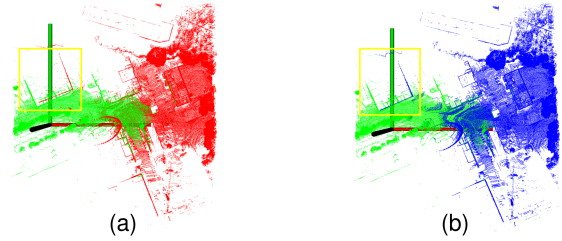


Fig. 9. Test B: Alignment of the intersecting regions with ICP refinement performed in ZOE robot, when it received the GOLFCAR map (a) Green and red maps represent the target and source clouds pre ICP, top view (b) Green and blue maps represent the target and aligned source clouds post ICP, top view. Alignment can be better appreciated in yellow box

Quantitative alignment results of the ICP transformation relative to each robot are shown in Tables I and II. All the ICP transformations are expressed in Euler representation $(x, y, z, roll, pitch, yaw)$ in meters and radians. The first row of Table I corresponds to the merging process in ZOE, when this robot received the map shared by FLUENCE and it aligned that map to its own pre-local map. The decentralized system demonstrated alignments in opposite directions for both robots, since each robot performs the merging process considering its Pre-Local map as target cloud for alignment reference. Table II also reveals this symmetrical behavior, where the algorithm on ZOE converged to the value of displacement of -0.1782 m and -3.2605 m along the x-axis and y-axis respectively. On the other hand on the GOLFCAR robot, the algorithm converged to a value of displacement of 0.2213 m and 3.3857 m along the x-axis and y-axis respectively, reconfirming relative alignments in opposite directions.

Figure 10 shows one of the merging results corresponding to the ZOE robot, in which the cloud represents the final

TABLE I

TEST A: RELATIVE ICP TRANSFORMATIONS IN EULER FORMAT BETWEEN ZOE AND FLUENCE ROBOT

Robot	x	y	z	roll	pitch	yaw
ZOE	-1.6517	3.0966	-9.9729	0.0132	0.0730	0.0022
FLU.	4.5748	-4.4556	6.6061	-0.0054	-0.0624	-0.0084

TABLE II

TEST B: RELATIVE ICP TRANSFORMATIONS IN EULER FORMAT BETWEEN ZOE AND GOLFCAR ROBOT

Robot	x	y	z	roll	pitch	yaw
ZOE	-0.1782	-3.2605	1.7771	-0.0516	0.0115	0.0356
GOL.	0.2213	3.3857	-2.6070	0.0411	-0.0256	-0.0380

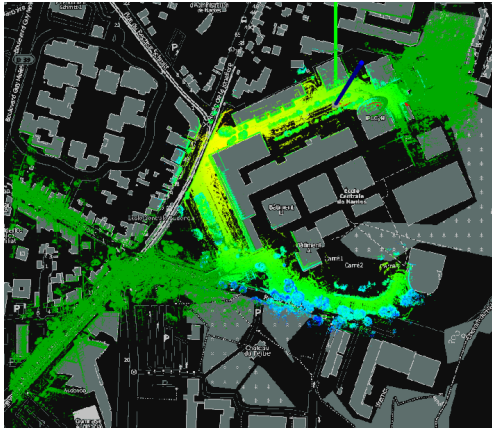


Fig. 10. Top view of final 3D Local Map of ZOE robot (color). Uniform green point clouds come from the aligned maps of FLUENCE (left) and GOLFCAR (right)

3D local map projected on a 2D map in order to make qualitative comparisons. Experiments showed the impact of working with intersecting regions, since it can accelerate the alignment process by decreasing the number of points to compute. In the same way, tests demonstrated that our proposed map sharing technique developed a transcendental position in the performance of the entire mapping collaborative system by reducing the map size to transmit. Finally, the sharing algorithm proves to be a suitable candidate to exchange efficiently maps between robots considering the use of clouds of large dimensions.

V. CONCLUSION AND FUTURE WORK

A framework was presented for decentralized 3D mapping system for multiple robots. The work has showed that maps from different robots can be successfully merged, from a coarse initial registration and a suitable exchange of data volume. The system uses initially range measurements from a 3D LiDAR, generating a pre-local maps for each robot. The complete system solves the mapping problem in an efficient and versatile way that can run in computers dedicated to three vehicles for experiments, leading to merge maps independently on each vehicle for partially GPS-denied environments. Future work will focus on the analysis of the consistency of the final maps estimated on each robots

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