



## Mesh generation for fusion applications

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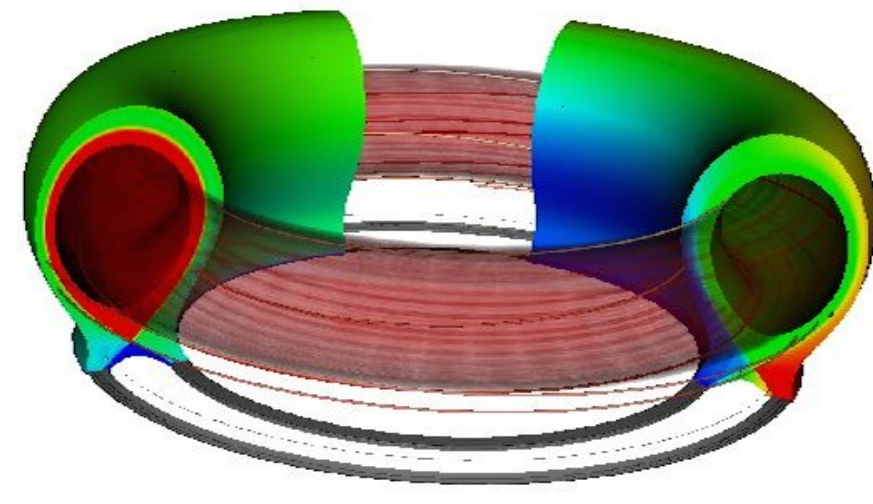
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## Context and motivations

- High anisotropy in magnetized fusion plasmas:  
⇒ requires the use of **flux aligned meshes**.
- Complex and realistic geometries:  
⇒ need other strategies (equidistribution, orthogonality).
- High order derivatives (in MHD for example):  
⇒ require **regular representation**.

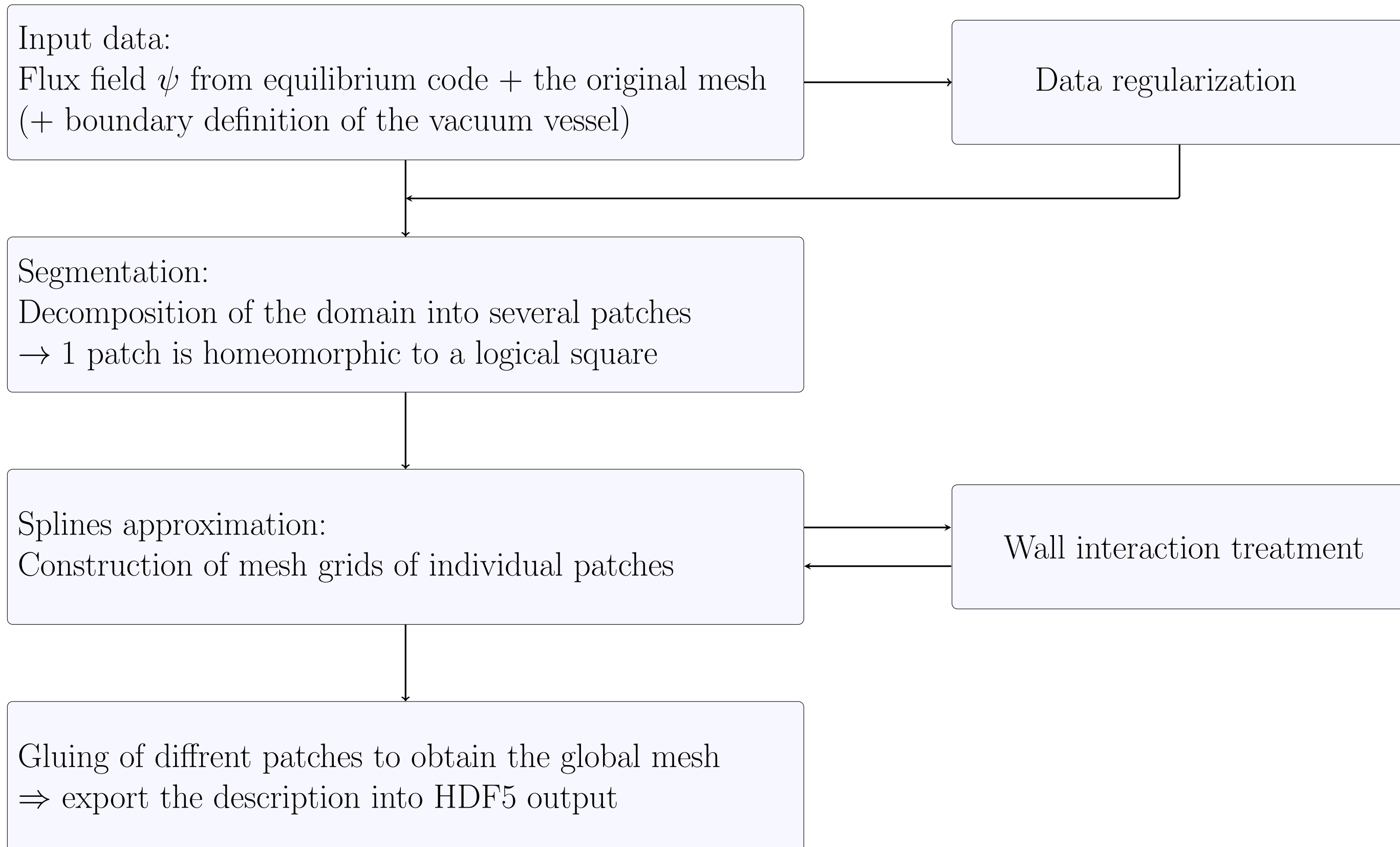


Sketch of a Tokamak reactor

### Unified code for the generation of flux aligned mesh in the poloidal plane.

- Different codes and type of meshes.
- Different numerical methods:
  - Semi-Lagrangian approaches.
  - Finite difference, Finite volume
  - Finite Element (Spline or Hermite-Bezier on quadrangles; Powell-Sabin, Clough-Tocher on triangles, etc..)

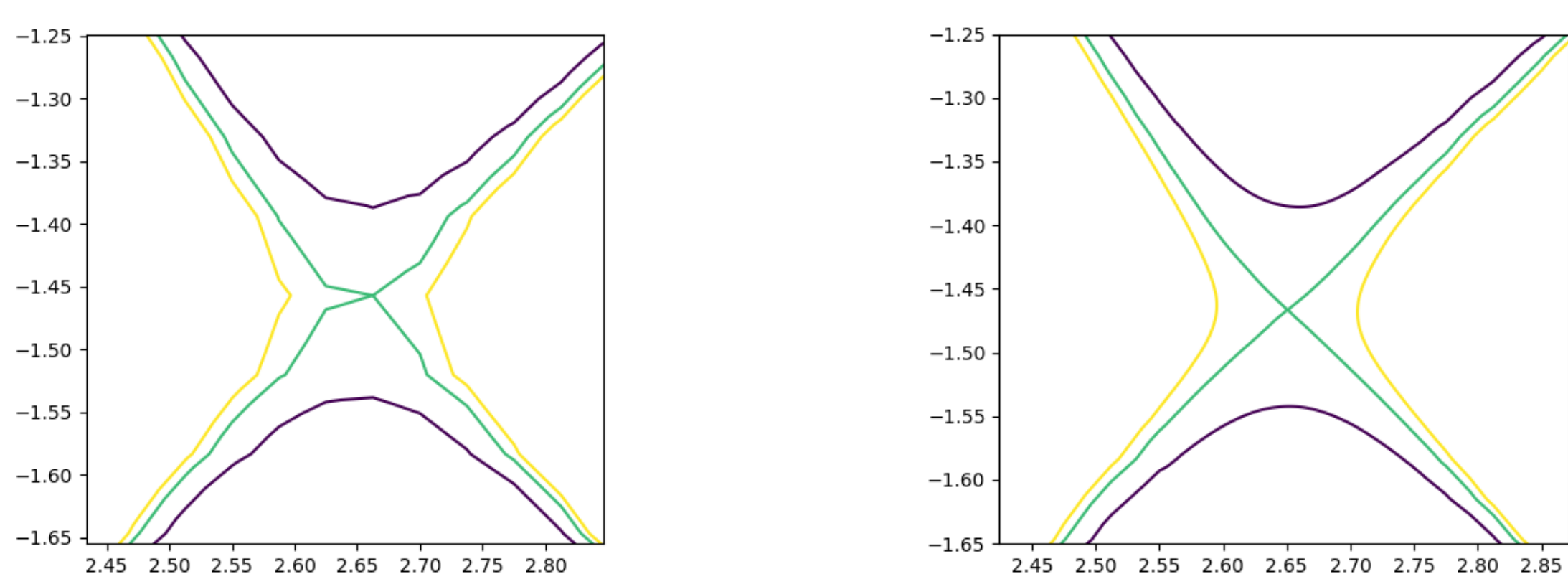
## Workflow diagram



## Pre-processing of the data

### Isolines regularization

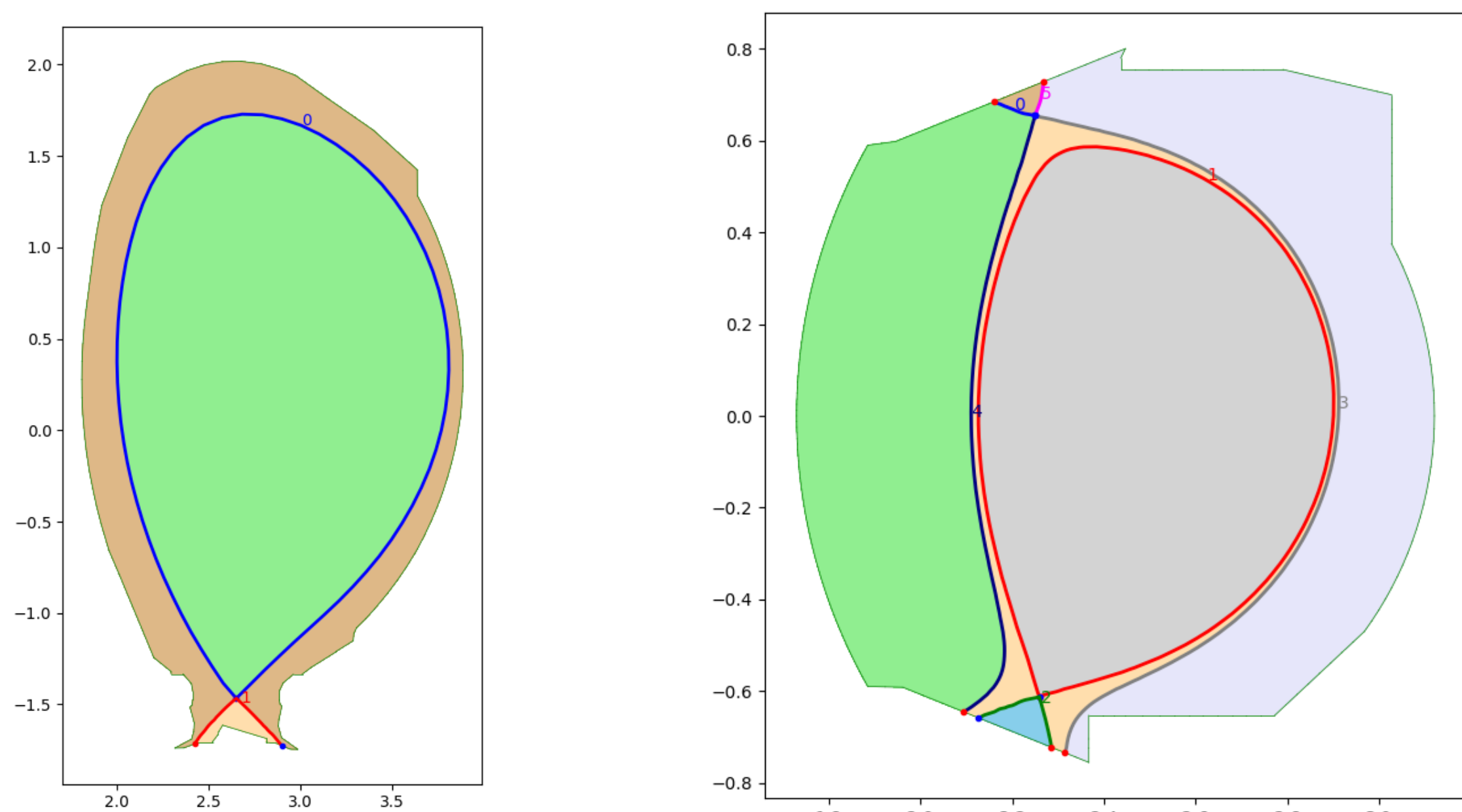
If the equilibrium solver results are not smooth enough : low-order discretization, coarse resolution, ...  
⇒ Replace the flux function by its Clough Tocher interpolant on the refined mesh (locally).



### Segmentation

- Based on Morse theory and Reeb graph.
- Automatic decomposition of isolines including arbitrary number of X-Points.
- Topological set of the isolines consists of finite connected components and contains only closed orbits.

Examples of domain segmentation for JET and WEST tokamaks:



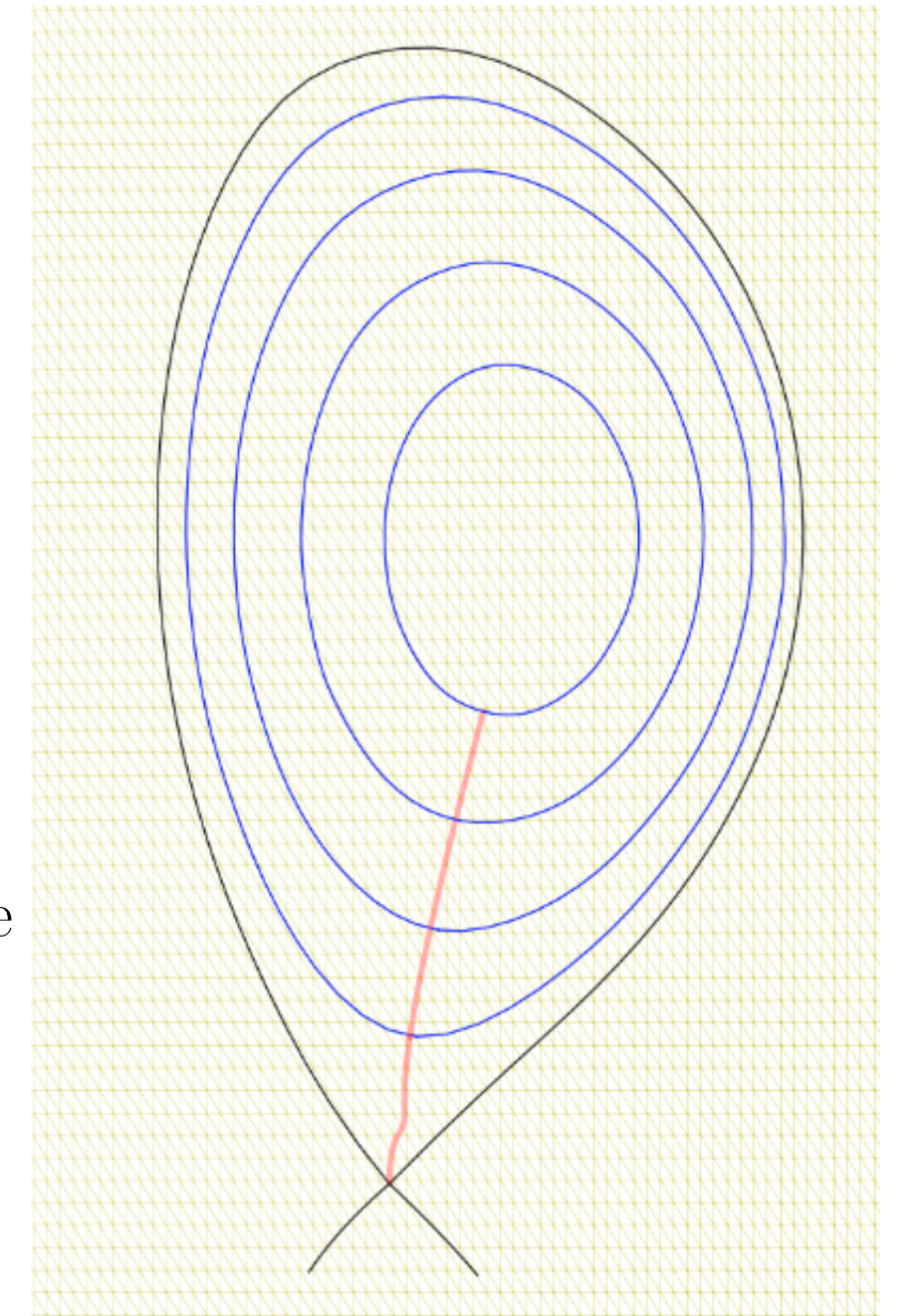
## Structured grid construction

### I. Isolines generation

1. Identify a mapping:  $(s, t) \in [0, 1] \times [0, 1] \rightarrow \mathbf{x}(s, t) \in \Omega$
2. Get the radial curve  $\mathcal{S}(s)$ , solution of the ODE:

$$\begin{cases} \frac{d\mathbf{x}}{ds} = \frac{\psi_M - \psi_0}{\|\nabla\psi\|^2} \nabla\psi \\ \mathbf{x}(0) = \mathbf{x}_0 \end{cases}$$

3. Compute the spline interpolation of the radial curve and generate a set of internal isolines.



### II. Meshing of individual patch $\Omega_k$

1. Choose a finite number of isolines  $f^{-1}(c_i)$ .
2. Approximate each level set by a spline:  $f^{-1}(c_i) \sim \mathcal{C}_i(t) = \sum_j \mathbf{C}_j^i N_j(t)$ .  
 $N_j$ : B-spline Basis.  
 $\mathbf{C}_j^i$ : Control Points.
3. Construct a 2D tensor product mapping  $[0, 1] \times [0, 1] \rightarrow \Omega_k$ :

$$\mathcal{S}(s, t) = \sum_i \sum_j \mathbf{P}_{i,j} N_i(s) N_j(t), \text{ s.t. } \mathcal{S}(s_i, t) = \mathcal{C}_i(t), \forall i.$$

### III. Gluing patches

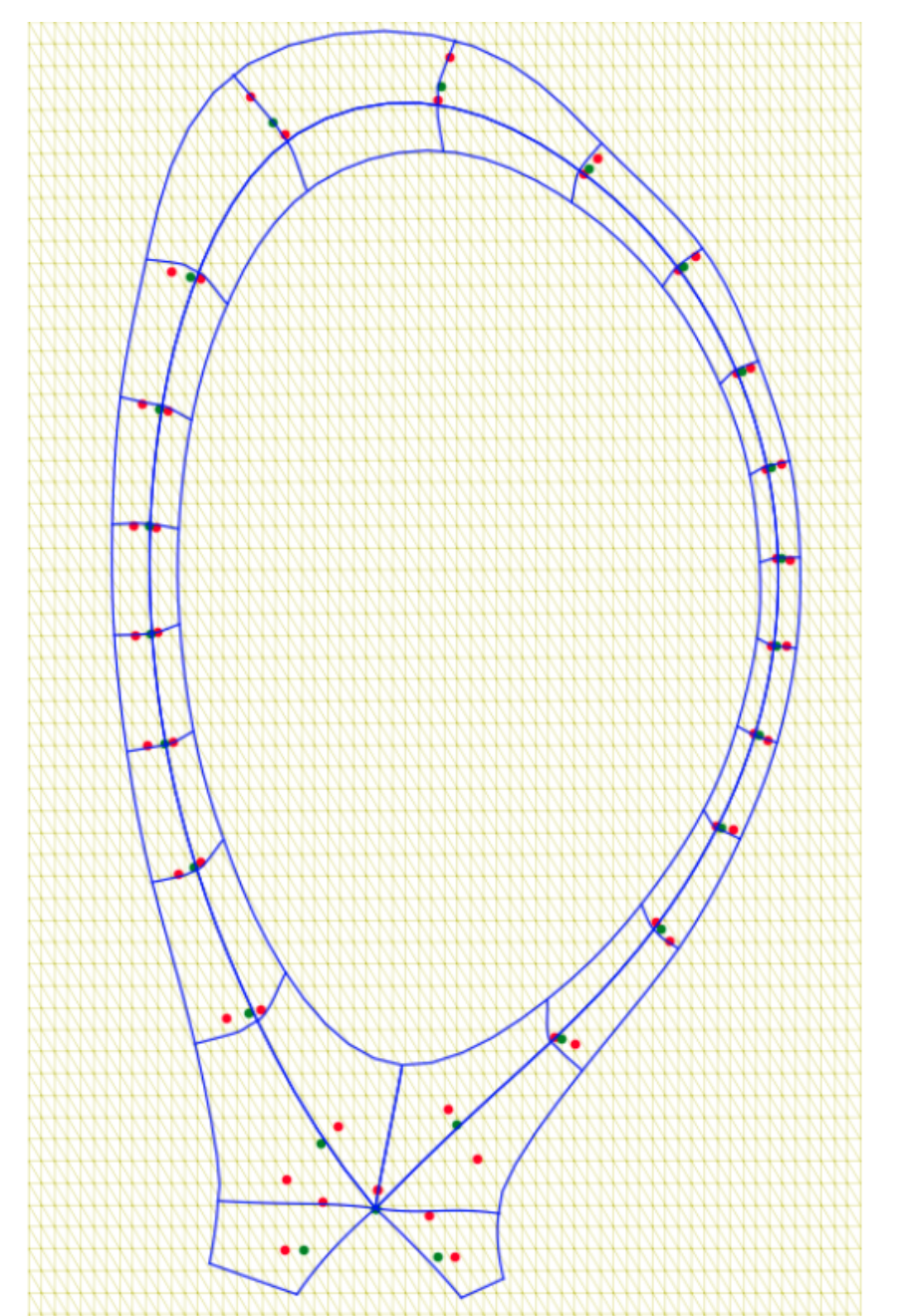
Given 2 subdomains  $\Omega_1$  and  $\Omega_2$  described by:

$$\mathcal{S}_1(s, t) = \sum_i \sum_j \mathbf{P}_{i,j} N_i(s) N_j(t)$$

$$\mathcal{S}_2(s, t) = \sum_i \sum_j \mathbf{Q}_{i,j} N_i(s) N_j(t)$$

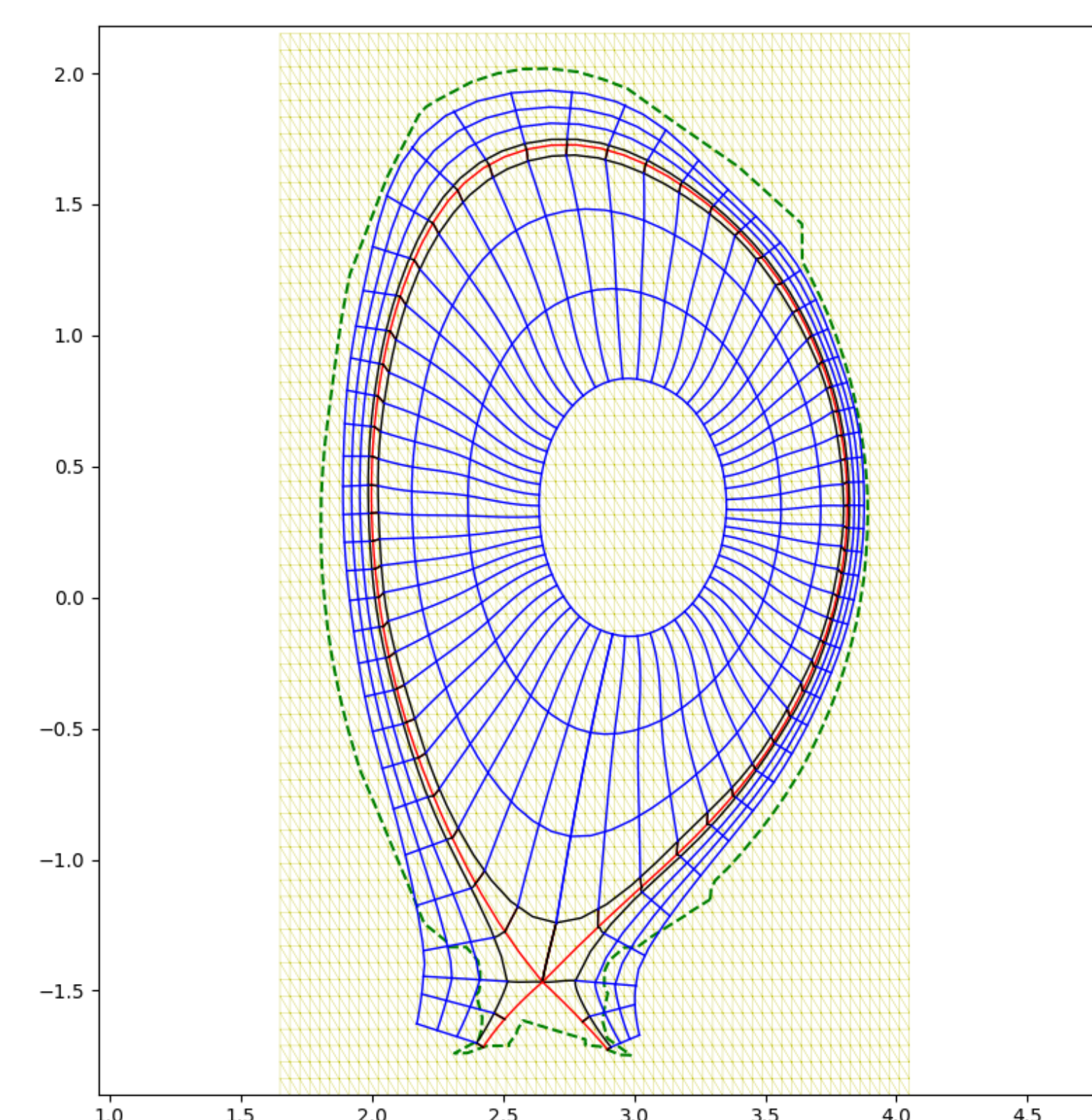
with a common boundary for instance:  $\mathcal{S}_1(0, t) = \mathcal{S}_2(0, t)$

1.  $\mathcal{C}^0$  continuity:  $\mathbf{P}_{0,j} = \mathbf{Q}_{0,j}, \forall j$ .
2.  $\mathcal{C}^1$  continuity: geometric condition on the control points,  $\mathbf{P}_{1,j}, \mathbf{P}_{0,j} = \mathbf{Q}_{0,j}, \mathbf{Q}_{1,j}$  have to be aligned.



## Multipatch example

Flux aligned mesh for JET (Core/Edge/SOL regions):



## Summary

Development of a mesh generation software for tokamak simulations:

- Can be used by different codes and handle different types of meshes.
- Written in Python with Fortran bindings:  
→ using open source libraries (except Segmentation module but free for academics).