

1 **Impinging jet cleaning of tank walls: effect of jet length, wall curvature and related**
2 **phenomena**

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25 **Impinging jet cleaning of tank walls: effect of jet length, wall curvature and related**
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31

32 *Abstract*

33 The effect of jet length and wall curvature on the flow patterns generated by an impinging
34 water jet were quantified and the effect on cleaning investigated in a brief study. The length of
35 time taken to establish steady flow was characterised. Jet impingement on a flat vertical wall
36 was investigated for jets of diameter 2 – 4 mm for lengths, L , up to 1 m. The amount of liquid
37 lost to splatter was measured and found to be insensitive to L for short L (< 300 mm for these
38 nozzles) and strongly related to L for longer values. The shape of the radial flow zone on flat
39 walls agreed with existing models once the fraction of liquid lost to splatter was accounted for.
40 Tests on horizontal and vertical cylinders with curvatures in the range 6.9 to 20 m^{-1} showed
41 that the curvature of the impinged wall did not affect the shape of the radial flow zone until
42 higher flow rates ($> 1.5 \text{ dm}^3 \text{ min}^{-1}$). The cleaning of two viscoplastic model food soils was
43 studied briefly: a hydrophobic petroleum jelly and Carbopol[®], a water-soluble gel. The splatter
44 correction was not able to account for all the differences observed in cleaning at different jet
45 lengths. There was no appreciable effect of curvature on cleaning behaviour. Soaking of the
46 Carbopol[®] increased its cleaning rate.

47

48

49 *Keywords* Breakup, cleaning, curvature, hydrodynamics, hydraulic jump, jet.

50

51 Introduction

52 Liquid jets generated by rotating nozzles or spray balls are regularly employed as components
53 of cleaning-in-place (CIP) systems and are used to distribute cleaning solutions and rinsing
54 liquid around the walls of tanks, reactors and other process vessels. Quantitative models of the
55 hydrodynamics of the flow generated by a coherent liquid jet impinging on a flat vertical wall
56 have been developed in the last decade and combined with cleaning models to predict the
57 removal of soil layers from such walls (e.g. Glover *et al.*, 2016; Bhagat *et al.*, 2017). After
58 impingement, the liquid, which in the food sector is usually water or a solution thereof, spreads
59 radially outwards in a thin, fast moving film until surface tension causes a transition to a slower
60 moving, thicker film region. With a vertical wall, an almost circular jump forms initially.
61 Above the point of impingement this gives rise to a film jump with a narrow band (or rope) of
62 liquid which flows circumferentially downwards beyond it. Below the point of impingement,
63 gravity causes this this initial jump to evolve into a draining film, bounded by the ropes which
64 join from above and form the boundaries of the falling film (Aouad *et al.*, 2016; Bhagat *et al.*,
65 2018).

66
67 Impinging jets therefore generate two regions of flow which can promote cleaning. In the area
68 within the jump, here termed the radial flow zone (RFZ), the thin film of liquid is fast moving
69 and exerts a high shear stress, which can promote cleaning. In the falling film the shear stresses
70 are smaller but the area is considerably larger, achieving contact of the soil with the cleaning
71 solution and promoting any weakening of the deposit associated with soaking. The wall shear
72 stress exerted in the rope region is intermediate between the other two regions.

73
74 Wilson *et al.* (2012) modelled the flow in the RFZ as a laminar film with a parabolic velocity
75 profile similar to that in Nusselt's analysis of film condensation (Nusselt, 1916). The location
76 of the film jump was obtained from a balance between the outward flow of momentum in the
77 liquid and the surface tension force opposing wetting, giving

$$R = 0.276 \left[\frac{\rho^2 Q^3}{\mu \gamma (1 - \cos \beta)} \right]^{1/4} \quad [1]$$

78 where R is the half-width of the RFZ at the level of the point of impingement, ρ the liquid
79 density, Q the volumetric flow rate through the nozzle, μ the liquid dynamic viscosity, γ the
80 vapour-liquid surface tension and β the solid-liquid contact angle. The model includes a

81 contribution from the wall material via β . A more rigorous treatment of the flow in the RFZ
82 and formation of the film jump was given by Bhagat and Wilson (2016). Equation [1] provides
83 a reasonable first order estimate of R .

84

85 Much of the work on impinging jet hydrodynamics (*e.g.* Watson, 1964; Bush and Aristoff,
86 2003; Wilson *et al.*, 2012; Aouad *et al.*, 2016) has employed coherent jets impinging normally
87 on flat walls. The jets employed in practice are subject to several phenomena which affect the
88 transfer of those results to industrial systems. Figure 1 presents some of the considerations that
89 need to be considered in scaling up the results to industrial scales. Spray balls and CIP nozzles
90 do not normally generate coherent jets and the jet is often subject to breakup, which is promoted
91 by the length that the jet has to travel from the nozzle before striking the wall. Nozzle motion
92 (usually rotation) and gravity mean that the jet will rarely impinge normally on a wall. The
93 effect of oblique impingement by coherent jets was considered by Bhagat *et al.* (2017). The
94 other factors have not received much attention to date.

95

96 The effect of jet length, L , was investigated by Feldung Damkjær *et al.* (2017), who reported a
97 scale up study employing industrial nozzles in a full size tank with nozzle diameters, d_N ,
98 ranging from 2.0 to 5.5 mm and nozzle volumetric flow rates, ($Q = 0.8 - 50 \text{ dm}^3 \text{ min}^{-1}$;
99 $0.05 - 30 \text{ m}^3 \text{ h}^{-1}$) representative of industrial installations. They considered jet lengths of
100 80 – 2490 mm impinging normally on a flat, transparent, vertical target plate and found that
101 the hydrodynamic and cleaning behaviour was reasonably well described by the existing
102 models (*e.g.* Wilson *et al.*, 2012) for the 2 mm nozzles at low L (< 200 mm). They attributed
103 the observed differences at higher L to the combined effects of jet breakup, wherein the liquid
104 forms a procession of droplets, and splatter, whereby a fraction of the liquid rebounds from the
105 wall and does not join the spreading film. They showed that the dimensions of the film jumps
106 (*i.e.* height *vs.* width) agreed with the predictions of the Bhagat and Wilson (2016) model. They
107 concluded that existing models for the RFZ could be used if the flow rate used in the
108 expressions was corrected for losses due to splatter.

109

110 They also studied the rate of cleaning of petroleum jelly layers and found that longer jets often
111 gave cleaning behaviour which differed from that observed with a coherent jet. A jet impinging
112 normally on a wall creates a circular region within the RFZ which grows with time: Feldung
113 Damkjær *et al.* fitted their measurements to the cleaning model of Glover *et al.* (2016) and

114 reported that the cleaning rate constant extracted from tests with longer jets was smaller than
115 that **expected from tests** with coherent jet tests. **The** difference could not be explained simply
116 in terms of adjusting the flow rate. These observations indicate that the dynamics associated
117 with jet breakup and drop impact need to be considered in scale-up studies.

118

119 **Phenomena related to splatter caused by jets impinging on flat walls has been studied for well-**
120 **defined coherent jets by Errico (1986), Lienhard *et al.* (1992) and Bhunia and Lienhard (1994).**
121 **Liquid can be lost from the main flow by rebound or shedding from film boundaries. The**
122 **mechanics of jet breakup and splatter are complex (see review by Eggers and Villermaux,**
123 **2008) even for well-defined jets generated in carefully designed nozzles. Nozzles used in**
124 **industrial practice are not usually designed to deliver coherent jets and an effective method of**
125 **characterising these flows is therefore required.**

126

127 Wang *et al.* (2013) quantified the effect of splatter from short ($L = 50$ mm) jets generated by 2,
128 3 and 4 mm diameter convergent nozzles impinging on vertical walls using an apparatus similar
129 to that used in this work. They reported their results in terms of the splatter fraction, S , defined
130 as

$$Q_{\text{eff}} = Q(1 - S) \quad [2]$$

131 where Q_{eff} is the volumetric flow rate in the falling film. They found that S was small until the
132 jet Reynolds number (defined $Re = U_o d_N / \nu$, where U_o is the jet velocity and ν the liquid
133 kinematic viscosity) exceeded 12 000. Above this value S increased linearly with Re reaching
134 $S = 0.37$ at $Re = 20\ 000$. The value of S also depended on the angle of impingement (see Wang
135 *et al.*, 2013). **Feldung Damkjær *et al.* reported Q_{eff}/Q data corresponding to S values, calculated**
136 **using $S = 1 - Q/Q_{\text{eff}}$, up to 0.7. They estimated Q_{eff} by using Equation [1] to determine the flow**
137 **rate which would have given the observed value of R .**

138

139 This paper reports an experimental investigation of a subset of the factors identified in Figure
140 1 on impinging jet behaviour. The effect of jet length and breakup on the shape of the RFZ and
141 splatter is considered for longer jet lengths (up to 1 m) than the study of Wang *et al.* The effect
142 of jet length on cleaning is investigated briefly via testing on a hydrophobic soil, petroleum
143 jelly, similar to those employed by Feldung Damkjær *et al.* and Glover *et al.*

144

145 A second aspect which has received little attention is the curvature of the wall. As a first step
146 towards understanding these effects, the effect of jet length and wall curvature on jet
147 hydrodynamics was investigated for vertical and horizontal cylinders. Whilst wall curvature is
148 not expected to be large for tanks (as curvature is related to radius^{-1} , and the liquid film
149 thickness is submillimetre), it could be important for smaller items (bottles, small fermenters).

150

151 The third aspect, which is considered briefly, is the effect of soil contact with the liquid before
152 being exposed to the jet, *i.e.* soaking. This will occur in practice when a soil is contacted by
153 liquid draining from above. Many food soils weaken on soaking. Layers of Carbopol[®] gel were
154 used for these tests. Carbopol[®] gels are suspensions of crosslinked polyacrylic acid polymer in
155 water and are often used as model viscoplastic fluids (Dinkgreve *et al.*, 2018). Their yield stress
156 depends on the volume fraction of polymer and pH, so extended contact with water is expected
157 to reduce the yield stress and promote liquid-like behaviour.

158

159 **Materials and Methods**

160 Tests were conducted with tap water at room temperature using the apparatus and brass
161 convergent nozzles with diameter, d_N , of 2, 3 and 4 mm employed by Wang *et al.* (2013). Water
162 was pumped from a tank through a rotameter and flow control valves before entering a 7.5 mm
163 i.d. steel pipe which served as a flow straightening section ahead of the nozzle. Pipe lengths of
164 150 mm and 350 mm were used. The volumetric flow rate through the nozzle, Q , was read
165 from the rotameter which had been calibrated separately.

166

167 Horizontal jets were used in the majority of tests. The nozzle was located at horizontal distance
168 L from the target. At lower flow rates, jet droop could be significant and in some cases the jet
169 did not reach the target: for others the inclination of the nozzle was adjusted to ensure that the
170 jet impinged horizontally. Photographs of the jet from the side indicated that the midpoint of
171 the jet followed the trajectory expected from gravity, namely $z = -gx^2/2U_o^2$, where g is the
172 acceleration due to gravity, x the horizontal distance travelled by the jet and z the vertical
173 displacement.

174

175 All targets used were transparent. Photographs and videos of the flow pattern at and near the
176 point of impingement were taken from the dry side of the transparent target with a Nikon D3300
177 or Sony Cyber-shot RX100V digital camera, aligned co-axial with the jet. Transparent graticule

178 tape was placed on the dry side of the target to provide a length calibration for image
179 processing.

180

181 *Flow patterns*

182 Figure 2(a) shows the dimensions of the flow pattern extracted from photographs: the half-
183 width of the RFZ at the level of the point of impingement, R , and the half-width of the wetted
184 region, R_c ; and the height of the jump and the top of the rope, Z and Z_c , respectively. The
185 photograph shows a case where the flow pattern was not symmetrical about the vertical
186 midplane, which is captured in the large error bars used in reporting R and R_c .

187

188 The evolution of these parameters over time, t , for a jet impinging on an initially dry target is
189 illustrated in Figure 2(b). It can be seen that R and Z were initially almost equal, with Z slightly
190 smaller due to gravity. After 0.1 s the rapid growth stops and R and Z differ (one increases, the
191 other decreases) as the rope is established over the next 0.2 s. R_c stabilised after a further 0.2 s,
192 0.5 s after the initial impact. A detailed account of the formation of the initial film jump is
193 given in Bhagat *et al.* (2018): the change in R and Z in the period $0.1 \text{ s} < t < 0.3 \text{ s}$ are associated
194 with establishment of the boundary conditions downstream, *i.e.* as the rope develops. At the
195 top of the RFZ, the rope flows over the top of the thin film. Regular fluctuations are evident
196 thereafter in Z , indicating that the flow at the top of the rope was unstable. The time taken to
197 establish the radial flow zone, t_E , was measured for a 2.67 mm nozzle at a number of flow rates
198 using a high speed camera (Photron FASTCAM SA3).

199

200 *Jet length and splatter*

201 To investigate the effect of jet length, a $360 \times 600 \times 5 \text{ mm}$ (width \times height \times depth) flat
202 vertical Perspex[®] (polymethylmethacrylate, PMMA) wall was used as the target. The jet
203 lengths and flow rates tested for each nozzle, and the associated jet velocities, Reynolds and
204 Weber ($We = \rho U_o^2 d_N / \gamma$) numbers are summarised in Table 1.

205

206 The volumetric flow rate in the falling film, Q_{eff} , was measured by collecting the water in a
207 wide reservoir located at the base of the target. The reservoir was fitted with a slotted roof so
208 that droplets originating from the jet due to breakup or droplets from rebound off the target
209 were unlikely to be collected.

210

211 *Wall curvature*

212 The effect of wall curvature on the flow pattern was investigated by impinging the jet on the
213 inner wall of a Perspex[®] cylinder. Four cylinders were tested with inner diameter, D , ranging
214 from 10 to 29 cm and wall curvature, $\kappa = 2/D$, from 20 to 6.9 m⁻¹ (see Table 2). The flat wall
215 served as a control with $\kappa = 0$. The feed pipe passed through a 40 × 40 mm slot in the cylinder
216 wall and the $d_N = 2$ mm nozzle was used to generate a coherent jet impinging normally on the
217 inner wall (with $L = 30$ mm). The target cylinder was mounted with its axis vertical or
218 horizontal. A photograph of a horizontal cylinder experiment is given in Figure 7(a). The
219 experimental conditions are summarised in Table 3.

220

221 The dimensions labelled in Figure 2(a) were calculated from photographs taken by the main
222 camera located externally, again aligned co-axial with the jet. The dimensions extracted from
223 the images were corrected for refraction effects which did not arise with flat walls. Appendix
224 A describes the approach taken: the estimates were compared with measurements made by a
225 second camera which was moved around the apparatus in order to obtain refraction-free
226 images.

227

228 *Cleaning*

229 Short sets of cleaning experiments were performed on walls coated with thin layers of
230 petroleum jelly (APC Pure, UK), a hydrophobic yield stress fluid, or Clearglide[™], a
231 commercial viscoplastic suspension of Carbopol[®] (crosslinked polyacrylic acid polymer) in
232 water. The static yield stress of the petroleum jelly, measured using a Kinexus Lab+ Rheometer
233 (Malvern Instruments, UK), was approximately 220 Pa (R.R. Fernandes, internal
234 communication). The yield stress of the Carbopol[®], measured using a vane tool, decreased
235 from approximately 20 Pa to 5 Pa when diluted 1:1 with water (D. Gibson, internal
236 communication). Layers of the required thickness were prepared on an initially dry target using
237 the spreading tool described by Glover *et al.* (2016). Petroleum jelly layers were rested for 30
238 minutes before cleaning while Carbopol[®] layers were cleaned immediately after preparation.
239 The targets were mounted vertically and subjected to jet impingement while being videod. A
240 dark food grade dye was added to the Carbopol[®] gel to make it easier to determine when
241 material had been removed from the wall. With both materials the cleaned area took the form
242 of a circle centred on the point of impingement which grew over time. The radius of the circle,
243 a , was extracted from images using a MATLAB script.

244 **Results and Discussion**

245 *Formation of steady flow patterns*

246 These tests were conducted with steady flows, which are directly related to continuous jets
247 generated by static and moving nozzles. Other workers (*e.g.* Fuchs *et al.*, 2017) have
248 investigated the use of intermittent jets as a means of increasing efficiencies based on total
249 water consumption. In these, a steady flow is applied for a period t_B , followed by a period
250 where no jet impacts and the liquid drains away (if the wall is inclined). The time taken to
251 establish the radial flow zone, labelled t_E (between 0.1 and 0.2 s in Figure 2(b)) is an important
252 parameter in such applications as it constitutes a characteristic timescale for the periodicity of
253 bursts: a shorter t_B would result in the liquid establishing a smaller RFZ (the region of
254 mechanically assisted cleaning), while longer periods would only influence the width of the
255 wetted region below the point of impingement. **A short series of tests were conducted to**
256 **establish this timescale.** This discussion focuses on RFZ formation, as the dynamics of the
257 wetted region were not explored in the experiments.

258

259 The measured values of t_E can be compared with an estimate based on the Wilson *et al.*
260 (2012) model, detailed in Appendix B,

$$t_E = 0.0477 \frac{\rho Q}{\gamma(1 - \cos \beta)} \quad [3]$$

261

262 Figure 3 shows that Equation [3] gives a reasonable estimate of the magnitude of t_E but does
263 not capture the dependency on jet diameter, **or jet velocity for a given flow rate.** Also shown in
264 the Figure are the predictions for t_E obtained with the more detailed model for the flow in the
265 thin film by Bhagat and Wilson (2016). This gives a more accurate description of the effect of
266 flow rate for the limited number of experimental results presented.

267

268 *Effect of jet length*

269 The shortest ($L \leq 70$ mm) jets were coherent. Surface fluctuations were evident on all longer
270 jets, and breakup was observed at lower Reynolds numbers with $L \geq 350$ mm. The splatter
271 fraction data in Figure 4 show a transition in splatter behaviour with increasing L , but this is
272 not associated with a transition to jet breakup. For the flow rates and nozzle sizes studied, **the**
273 **Reynolds and Weber numbers indicate that** jet breakup is associated with the first wind-assisted

274 regime (see Lin and Reitz, 1998). However, the applicability of correlations obtained for well-
275 defined jets (long cylindrical nozzles, *etc.*) to **the nozzles employed here (short, convergent**
276 **entry angle of $55^\circ \pm 10^\circ$)** is expected to be limited.

277

278 For shorter jets, $L < 300$ mm, the data exhibit an almost linear increase in S for $Re > 13\,000$,
279 which is consistent with the behaviour reported by Wang *et al.* (2013). The trend is almost
280 independent of d_N , indicating that the Reynolds number captures the effect of jet diameter in
281 this regime.

282

283 For longer jets, $L > 300$ mm, there is a noticeable transition to S being independent of Re and
284 strongly dependent on L , with a weak dependence on d_N (see Figure 4(b)). S approaches 0.4 for
285 the longest jets, indicating that a significant fraction of the liquid delivered by the nozzle does
286 not appear in the draining film. It was not possible using this apparatus to **differentiate between**
287 **water lost as a result of jet breakup and that lost from rebound**. The interplay of d_N and L
288 extends until $L > 0.5$ m: plotting the data in Figure 4(b) against L/d_N did not yield further insight
289 (see Supplementary Figure S1). For $L = 1$ m, S is almost insensitive to Re , d_N and Q , so there
290 is no advantage to using a particular nozzle to deliver a given flow rate of water in the jet (but
291 this will affect the pressure drop in the line).

292

293 Splatter was not determined solely by jet breakup: for the longer jets, the value of S did not
294 change appreciably when the jet was breaking up into droplets (indicated by open symbols in
295 the Figure). Splatter is attributed to the momentum of the drops formed as the jet breaks up and
296 whether this is large enough for rebound to occur. It is also related to the stability of the film
297 and rope, and whether surface tension is strong enough to prevent these shedding droplets.

298

299 **Similar trends were reported for industrial scale nozzles by Feldung Damkjær *et al.* (2017).**
300 **Their Q_{eff}/Q data are reported as S against Re in Supplementary Figure S2. In their case, jets**
301 **with $L \leq 300$ mm exhibited the trend of increasing S with Re which is not evident for longer**
302 **jets. The values of S are noticeably larger than the current work. It should be noted that Q_{eff} in**
303 **these tests was estimated from Equation [1].**

304

305 The radial flow zone dimensions, R and Z , increased with flow rate. Figure 5 shows that these
306 collapsed to common trends when R is plotted against Q_{eff} , indicating that the splatter fraction
307 correction is partly able to account for the differences in fluid flow behaviour. There is still

308 some variation, however, and this is evident when the data are compared with the Wilson *et al.*
309 (2012) model (Equation [1]) with $\beta = \pi/2$.

310

311 The shape of the radial flow zone (see inset in Figure 5) follows the same trend for all cases,
312 with $Z \approx 4R/5$, indicating the influence of gravity on the steady state RFZ shape. The common
313 trend suggests that there is no change in flow regime over the range of flow rates studied. Figure
314 5 supports the findings of Feldung Damkjær *et al.*, who estimated the splatter fraction in their
315 experiments.

316

317 The width of the draining film is related to R_c , this being the half-width of the wetted region at
318 the level of the point of impingement. The data fitted the relationship $R_c = 4R/3$ reported by
319 Wang *et al.* (2013) well (Supplementary Figure S3).

320

321 *Effect of wall curvature*

322 The flow patterns generated by the impinging water jet on cylindrical target walls were similar
323 to those observed with flat walls, namely radial flow near the impingement point, a film jump
324 above this point, and a confining rope of falling liquid.

325

326 Figure 6 summarises the effect of wall curvature on the dimensions of the radial flow zone, Z
327 and R , at different flow rates ($4\,200 < Re < 21\,000$). For vertical cylinders, the height of the
328 film jump, Z , does not change appreciably with curvature at lower flow rates. This might be
329 expected since the flow in the Z direction is not subject to curvature. As the flow rate increases,
330 the variation that occurs is attributed to splatter as there was noticeable spray observed within
331 the cylinders. The half-width of the radial flow zone, R , is similarly insensitive to curvature
332 (within experimental error) at lower flow rates. At higher flow rates, there is a steady decrease
333 in R with increasing curvature. In vertical cylinders, the flow in the azimuthal direction is
334 subject to curvature effects, so the results suggest that the amount of splatter increases (so Q_{eff} ,
335 decreases and thus R decreases) as κ increases.

336

337 Horizontal cylinders were expected to show the opposite behaviour, but little variation was
338 observed at lower flow rates while a decrease with κ was observed at higher flow rates for both
339 Z and R . The decrease at higher flow rates is attributed to splatter. The spray observed within
340 the cylinders was noticeably stronger with horizontal cylinders than vertical cylinders,

341 demonstrating the complexity of these wall curvature effects. Quantitative measurements of
342 splatter could not be made in the cylinder tests due to the limitations of the experimental set
343 up.

344

345 These results demonstrate that a positive curvature of the wall, as arises with jets striking the
346 internal wall of a cylinder, has a slight effect on the behaviour of the radial film pattern. The
347 width of the rope, B , did not change appreciably as a result of wall curvature (see
348 Supplementary Figure S4).

349

350 The curvatures studied here are larger than those likely to be encountered in tanks for food
351 manufacturing applications, so the influence of curvature in practice is therefore expected to
352 be small. Splatter measurements were not made in the cylinder tests. Furthermore, the results
353 presented here have been collected for concave walls: the impact of a convex wall on splatter
354 has not been studied and represents an avenue for further work as these are often encountered
355 in CIP applications as piping, fitting connections and other protuberances.

356

357 Larger jet diameters and higher flow rates were also investigated. At higher flow rates the radial
358 flow zone extended further around the cylinder inner wall. Two flow patterns not seen on flat
359 walls were observed in experiments with horizontal cylinders: shedding (Figure 7(a)) and
360 wraparound (Figure 7(b)).

361

362 Figure 7(a) shows an example in a horizontal cylinder where gravity causes water to be shed
363 from the rope above the nozzle. Shedding is not expected to affect the liquid velocity in the
364 RFZ, but it will reduce the flow rate in the rope.

365

366 At sufficiently high flow rates, the flow pattern wrapped around the inside of the cylinder.
367 Figure 7(b) shows an example in a horizontal cylinder, photographed from above. The curved
368 rope approaches the crown of the cylinder as the flow rate increases (Figure 7(b)(i)). At a
369 critical flow rate, the crown is reached and some of the rope drains beyond the crown: the rope
370 forms a Y-shape (Figure 7(b)(ii)). At higher flow rates, wraparound extends with almost linear
371 rope boundaries. The narrowing of the flow pattern after it wraps around shows that surface
372 tension dominates over downward momentum.

373

374 Wraparound in a horizontal cylinder is expected to occur when $Z_c \geq \pi D/4$ when the jet impinges
375 normally at the midplane (see Figure 7(a)). Assuming $Z_c \approx R$, Equation [1] then predicts that
376 wraparound will occur at flow rates above a critical value, $Q_{\text{wraparound}}$, given by

$$Q_{\text{wraparound}} = \left[\frac{\mu\gamma(1 - \cos \beta)}{\rho^2} \left(\frac{Z_c}{0.276} \right)^4 \right]^{1/3} \quad [4]$$

377 For the case shown in Figure 7(b), with $\beta = \pi/2$, wraparound is then expected where
378 $Q \geq 4.7 \text{ dm}^3 \text{ min}^{-1}$, which is consistent with the observed transition in rope behaviour.

379

380 The area wetted by the cleaning liquid will be greater than that predicted by existing models
381 when wraparound occurs. The increase in wetted area would be advantageous for applications
382 where cleaning arises primarily from the chemical action of the cleaning liquid.

383

384 *Impact of jet length and curvature on cleaning*

385 Figure 8 shows the growth in the size of the cleaned region against time for layers of petroleum
386 jelly on flat, vertical Perspex[®] walls cleaned with jets of three different lengths. The values of
387 Q were chosen so that the jets had similar Q_{eff} values: Q_{eff} was estimated from measurements
388 on clean walls. The presence of a soil layer affects the flow in the thin film beyond the cleaning
389 front significantly: with the petroleum jelly a berm of dislodged soil collected at the cleaning
390 front which deflected the thin film away from the surface and created a spray.

391

392 The cleaning profiles in Figure 8 are of similar form, with all data sets exhibiting rapid initial
393 cleaning followed by an approach to an asymptote, denoted a_{max} . The asymptotic behaviour is
394 associated with the soil having a yield stress. In each case a_{max} did not approach location of the
395 film jump ($R = 36.9 \pm 2 \text{ mm}$ from experimental measurements on clean walls, see Figure 5).
396 Bhagat and Wilson (2016) presented a detailed model of the flow in the RFZ, and gave results
397 for two key transitions: r_b , where the growing viscous boundary layer reaches the surface, and
398 r_t , the transition from laminar to turbulent flow in the film. For $d_N = 2 \text{ mm}$ and $Q_{\text{eff}} = 1.6 \text{ dm}^3$
399 min^{-1} , their model gave $r_b = 12.3 \text{ mm}$ and $r_t = 15.2 \text{ mm}$, so a_{max} is estimated to lie in the region
400 where the flow in the film is turbulent.

401

402 The data were fitted to the cleaning model reported by Glover *et al.* (2016) in their study of a
403 different petroleum jelly, *viz.*

$$\frac{da}{dt} = \frac{K^5}{5a^4} \left[1 - \left(\frac{a}{a_{max}} \right)^4 \right] \quad a < a_{max} \quad [5]$$

404 where a is the radius of the cleaned region, K is the cleaning rate constant and t is time. For the
 405 case where $a = 0$ when $t = 0$, the growth of the cleaned region is given by

$$t = \frac{5}{4} \left(\frac{a_{max}}{K} \right)^5 \left[\ln \left(\frac{1 + \frac{a}{a_{max}}}{1 - \frac{a}{a_{max}}} \right) - 4 \left(\frac{a}{a_{max}} \right) + 2 \tan^{-1} \left(\frac{a}{a_{max}} \right) \right] \quad [6]$$

406

407 In the early stages of cleaning, $a \ll a_{max}$ and integrating Equation [5] gives

$$(a^5 - a_0^5)^{0.2} = K(t - t_0)^{0.2} \quad [7]$$

408 where a_0 is the radius of the cleaned region when the cleaning front is first seen at time t_0 .

409

410 The value of K was estimated by fitting the initial data to Equation [7] by eye. a_{max} was taken
 411 to be the maximum experimental value of $a + 1$ mm. All data sets had similar values of K and
 412 a_{max} , summarised in Table 4. The predictions from Equation [6] with these values are shown
 413 in Figure 8. The plots show that the cleaning profiles are not well described by the Glover *et*
 414 *al.* model. Feldung Damkjær *et al.* also reported that cleaning profiles obtained with petroleum
 415 jelly with longer jets deviated from the model behaviour. These results indicate that whilst Q_{eff}
 416 captures the effect of breakup and splatter on hydrodynamics, it does not give a complete
 417 description of the impact of the film dynamics on cleaning. Using Q_{eff} (based on S) tended to
 418 underestimate the rate: in this case it provides a useful engineering result and indicates that this
 419 topic requires further investigation.

420

421 Figure 9 shows the cleaning profiles obtained for Carbopol[®] layers applied to the inner wall of
 422 three of the vertical Perspex[®] cylinders alongside that obtained for a jet impinging on a
 423 similarly coated flat vertical wall. All four tests employed a coherent jet, so that the degree of
 424 splashing and jet breakup was similar. Under these conditions, wall curvature had little impact
 425 on cleaning dynamics, which is consistent with the observations on flow patterns.

426

427 Particular care had to be taken with the Carbopol[®] layers as the cleaning rate increased
 428 noticeably if they were left in contact with water, which is attributed to water diffusing into the
 429 layer and changing its rheology. The effect of soaking is demonstrated in Figure 10, which

430 shows that the approach to an asymptote, a_{\max} , was not observed at long times with the soaked
431 layers. The fit of all three data sets to the expression $a = K t^{0.2}$ (see Wilson *et al.*, 2014), which
432 Equation [5] collapses to when $a_{\max} \rightarrow \infty$, improves with soaking time. The K values (reflecting
433 ease of cleaning) increased from 24.1 mm s^{0.2} (no soaking) to 29.1 (after 10 s) and 30.9 mm
434 s^{0.2} (after 60 s), which is expected from the increased water content of the layer. Relating the
435 value of K to the rheology of the layer is the subject of ongoing work.

436

437 The observed change in K (and a_{\max}) on soaking is important for industrial application. Soil in
438 the lower regions of a tank is often contacted with cleaning liquid for extended times as a result
439 of the falling film created by jets striking the wall above. The width of the cleaned region
440 created by the passage of a jet will therefore increase with soaking time and this would suggest
441 that for soaking-sensitive materials the jet would not have to make so many passes over the
442 lower regions of a tank in order to clean it.

443

444 **Conclusions**

445 An experimental investigation of some of the factors influencing impinging water jet cleaning
446 of vessel walls was conducted. The time taken to establish a steady flow pattern is short and
447 can be estimated with some confidence from simple flow theory. The effect of jet length and
448 wall curvature on the flow pattern and cleaning performance of impinging liquid jets has been
449 investigated. Splatter arising from jet **breakup** and related phenomena **was** significant with non-
450 coherent jets. The splatter data show a noticeable transition in behaviour as jet length increases.

451

452 Correcting the jet flow rate for losses due to splatter in existing models gave reasonable
453 predictions for the shape of the radial flow zone. **Correcting the flow rate in the film was not**
454 **able to account for the differences observed in cleaning behaviour, but the splatter correction**
455 **does provide an engineering estimate of the cleaning rate.** The curvature of the **wall** had little
456 effect on hydrodynamics and cleaning. The Carbopol[®] layers' cleaning behaviour changed on
457 extended contact with water, which highlighted the need to understand how the soil interacts
458 with the cleaning fluid.

459

460

461 **Acknowledgements**

462 Funding for MWLC from Newnham College, Cambridge, and a Commonwealth Scholarship
463 for RKB are gratefully acknowledged, as is travel funding for DIW **to attend the FCFP2018**
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465 and Douglas Gibson. TVA, NT, SAW and RLW were all MEng research project students.

466

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511 horizontal surfaces by coherent impinging liquid jets, *Chem. Eng. Sci.*, **109**, 183-196.
- 512

513 **Nomenclature**

514 Roman

515	a	radius of cleaned area	m
516	a_o	radius of cleaned area when cleaning front is first seen	m
517	a_{\max}	radius of cleaned area, asymptotic value	m
518	B	rope width	m
519	C	chord length	m
520	d_N	nozzle diameter	m
521	D	cylinder inner diameter	m
522	g	gravitational acceleration	m s^{-2}
523	K	cleaning rate constant	$\text{m s}^{-0.2}$
524	L	horizontal distance from nozzle to target	m
525	\dot{m}	mass flow rate leaving nozzle	kg s^{-1}
526	Q	volumetric flow rate through the nozzle	$\text{m}^3 \text{s}^{-1}$
527	Q_{eff}	volumetric flow rate in the falling film	$\text{m}^3 \text{s}^{-1}$
528	$Q_{\text{wraparound}}$	volumetric flow rate above which wraparound is expected to occur	$\text{m}^3 \text{s}^{-1}$
529	r	distance in radial direction	m
530	r_b	radius where the boundary layer reaches the surface in the RFZ	m
531	r_o	jet radius	m
532	r_t	transition radius from laminar to turbulent flow in the RFZ	m
533	R	half-width of the RFZ at the level of the point of impingement	m
534	R_c	half-width of the wetted region at the level of the point of impingement	m
535	Re	Reynolds number	-
536	S	splatter fraction	-
537	t	time	s
538	t_o	time at which cleaning front of radius a_o is first seen	s
539	t_B	duration of jet burst	s
540	t_E	time taken to establish RFZ	s
541	U	mean velocity of liquid film	m s^{-1}
542	U_o	jet velocity	m s^{-1}
543	We	Weber number	-
544	x	distance in horizontal direction	m
545	y	estimate of length of interest	m

546	Y	length of interest	m
547	z	distance in vertical direction	m
548	Z	height of the film jump	m
549	Z_c	height of the top of the rope	m
550			
551	Greek		
552	β	solid-liquid contact angle	rad.
553	γ	vapour-liquid surface tension	N m ⁻¹
554	θ	angular position on liquid film	rad.
555	κ	wall curvature	m ⁻¹
556	μ	liquid dynamic viscosity	Pa s
557	ν	liquid kinematic viscosity	m ² s ⁻¹
558	ρ	liquid density	kg m ⁻³
559	ϕ	jet impingement angle	rad.
560	ψ	angle of the liquid film from the point of impingement	rad.
561	Ψ	angle of the second camera from the point of impingement	rad.
562			
563	Acronyms		
564	CIP	cleaning-in-place	
565	PMMA	polymethylmethacrylate	
566	RFZ	radial flow zone	
567			

568 **Appendix A – Correction for refraction**

569 The curvature of the cylinders affects the extraction of dimensions from photographs: R and R_c
 570 in vertical cylinders, and Z and Z_c in horizontal cylinders.

571

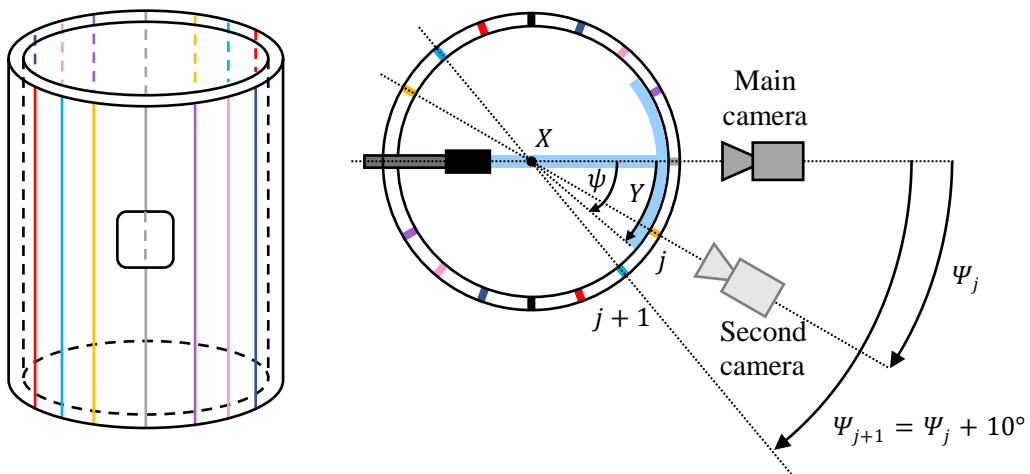
572 A second camera was moved around the apparatus to obtain refraction-free images so that the
 573 dimension of interest could be read directly off the graticule tape. To ensure that the camera
 574 was aligned normal to the surface of the cylinder, pairs of calibration lines showing the
 575 diameter of the cylinder were drawn at 10° intervals on the outer surface of the cylinder, shown
 576 in Figure A1.

577

578

579 (a) Side view

(b) Plan view



588

589

591 Figure A1 Schematic of a vertical cylinder showing calibration lines: (a) side view, and
 592 (b) plan view. ψ and Ψ are the angles of liquid film and second camera from the
 593 point of impingement, respectively. X is the axis of the cylinder. Position of
 594 calibration lines not drawn to scale: in this case the second camera is positioned
 595 at j .

596

597 The experimental set up is limited in that the second camera can only be positioned accurately
 598 at 10° intervals, labelled Ψ , from the point of impingement. It does, however, remove the
 599 uncertainty in judging the exact position of the water film by eye. To obtain an estimate of the
 600 measurement from the second camera, a harmonic weighting was used

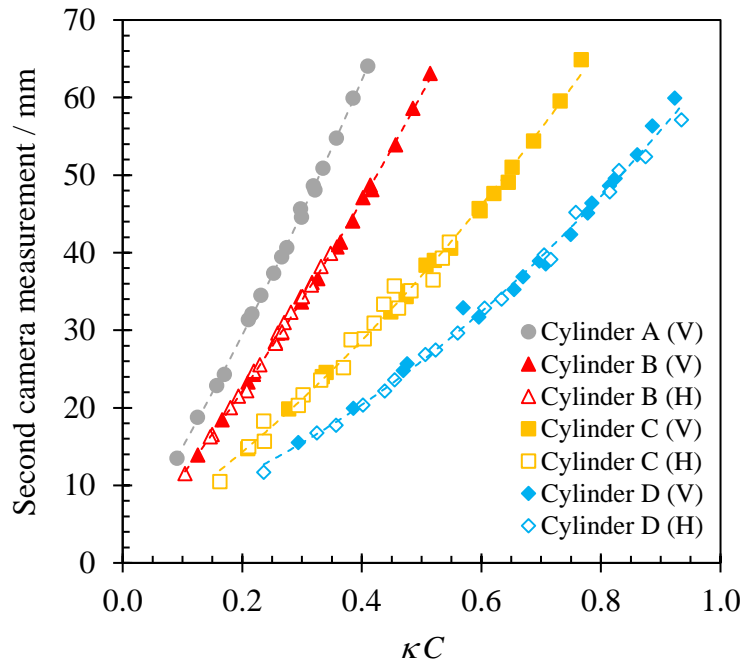
$$Y = \frac{\left[y_j * \frac{1}{|\psi_j - \Psi_j|} \right] + \left[y_{j+1} * \frac{1}{|\psi_{j+1} - \Psi_{j+1}|} \right]}{\left[\frac{1}{|\psi_j - \Psi_j|} + \frac{1}{|\psi_{j+1} - \Psi_{j+1}|} \right]} \quad [\text{A1}]$$

601 where the estimate of the length of interest, Y , and its angle ψ , are y_j and ψ_j at position j ,
 602 respectively; these are y_{j+1} and ψ_{j+1} at the next position ($j + 1$).

603

604 The estimates from the second camera were plotted against the chord length measured using
 605 the main camera, C , scaled by the wall curvature, κ (Figure A2). A second order polynomial
 606 was found to give the best fit to the experimental data (see Table A1). Measurements of R and
 607 R_c on vertical cylinders and Z and Z_c on horizontal cylinders were obtained using only the main
 608 camera and this calibration.

609



610

611 Figure A2 Fit of empirical correlations (Table A1) to experimental data. Error bars omitted
 612 for clarity. (V): R and R_c on vertical cylinders, and (H): Z and Z_c on horizontal
 613 cylinders.

614

615 Table A1 Empirical correlations used to correct for refraction, where $m = R, R_c, Z$ or Z_c .

Cylinder	Curvature, κ / m^{-1}	Correlation	Regression coefficient
A	6.9	$m = 66.1 (\kappa C)^2 + 124.9 (\kappa C) + 1.74$	0.9992
B	9.1	$m = 49.2 (\kappa C)^2 + 93.1 (\kappa C) + 1.55$	0.9989
C	14	$m = 38.2 (\kappa C)^2 + 49.0 (\kappa C) + 2.97$	0.9944
D	20	$m = 36.2 (\kappa C)^2 + 23.8 (\kappa C) + 5.07$	0.9947

616

617

618 **Appendix B – Estimate of time taken to establish the initial jump**

619 Wilson *et al.* (2012) presented an approximate model for the flow in thin radial film in the RFZ
 620 in the steady state, which yielded the estimate of R via Equation [1]. The mean velocity in the
 621 film, U , at radial position r was given by

$$\frac{1}{U} \approx \frac{1}{U_o} + \frac{10\pi^2 \rho \mu}{3\dot{m}^2} (r^3 - r_o^3) \quad [\text{B1}]$$

622 where r_o is the radius of the jet and $\dot{m} = \rho Q$ is the mass flow rate leaving the nozzle. Using
 623 this result to describe the mean velocity in the growing film and setting

$$U = \frac{dr}{dt} \quad [\text{B2}]$$

624 allows the time for the liquid to reach the location of the jump to be estimated from

$$\int_0^{t_E} dt = \int_{r_o}^R \frac{dr}{U} \quad [\text{B3}]$$

625 Substituting [B1] into [B3], assuming $1/U_o \approx 0$ and $r^3 \gg r_o^3$, integrating, setting $R^4 \gg r_o^4$ and
 626 using the expression for R from Equation [1] gives

$$t_E = \frac{0.276^4}{4} \frac{10\pi^2}{3} \frac{\dot{m}}{\gamma(1 - \cos\beta)} \quad [\text{B4}]$$

627 For high flow rate jets, the wall has a weak influence on R , suggesting $\cos\beta \approx 0$ (Bhagat and
 628 Wilson, 2016), yielding

$$t_E = 0.0477 \frac{\dot{m}}{\gamma} \quad [\text{B5}]$$

629 The surface tension of water at 20°C is 0.074 N m⁻¹, giving $t_E = 0.65\dot{m}$. For the case in Figure 2,
 630 $\dot{m} = 2$ kg min⁻¹ and $t_E = 20$ ms.

631

632 Bhagat and Wilson (2016) presented a more detailed model for the velocity in the thin film.

633 Employing this in the above derivation yields

$$t_E = \frac{8}{U_o} \left[0.125r + \frac{2.12r^{5/2}}{5(2r_o)^{3/2}\sqrt{Re}} \right]_{r_o}^{0.48r_o Re^{1/3}} + \frac{8}{U_o} \left[0.1975r + \frac{3.792r^4}{4(2r_o)^3 Re} \right]_{0.48r_o Re^{1/3}}^{0.5928r_o Re^{1/3}} + \frac{1}{U_o} \left[(2.37 - 0.0108\sqrt{Re})r + \frac{0.668r^{13/4}}{13(2r_o)^{9/4} Re^{1/4}} \right]_{0.5928r_o Re^{1/3}}^R \quad [\text{B6}]$$

634

635 **Tables**

636 Table 1 Summary of experimental conditions used to investigate the effect of jet length.

637

	d_N		
	2 mm	3 mm	4 mm
$Q / \text{dm}^3 \text{min}^{-1}$	0.8 – 3.5	0.8 – 5.5	1.0 – 7.0
$U_o / \text{m s}^{-1}$	4.2 – 18.6	1.9 – 13.0	1.3 – 9.3
L / m	0.06 – 1	0.06 – 1	0.06 – 1
Re	8 500 – 37 000	5 700 – 39 000	5 300 – 37 000
We	480 – 9 300	140 – 6 800	95 – 4 700

638

639

640

641 Table 2 Dimensions of the Perspex[®] cylinders used.

642

Cylinder	Inner diameter, D / mm	Wall thickness / mm	Curvature, κ / m^{-1}
A	290	5	6.9
B	220	5	9.1
C	138	6	14
D	100	5	20

643

644

645

646 Table 3 Summary of experimental conditions used to investigate the effect of wall curvature.

647

	d_N		
	2 mm	2 mm	4 mm
$Q / \text{dm}^3 \text{min}^{-1}$	0.4 – 2.0	0.4 – 2.0	4.0 – 7.0
$U_o / \text{m s}^{-1}$	2.1 – 11	2.1 – 11	5.3 – 9.3
L / m	0.07	0.03	0.03
Re	4 200 – 21 000	4 200 – 21 000	21 000 – 37 000
We	120 – 3 000	120 – 3 000	1 500 – 4 700
Target	Flat wall	Cylinders A – D	Cylinder D

648

649

650

651 Table 4 Summary of the Glover *et al.* (2016) model parameters obtained from the
652 experimental data shown in Figure 8.

653

L / mm	$K / \text{mm s}^{-0.2}$	$a_{\text{max}} / \text{mm}$
60	9.8 ± 1.1	19.3
245	8.6 ± 1.2	18.5
350	8.3 ± 1.9	18.6

654

655 **List of Figures**

656 **Figure 1** Schematic of phenomena affecting the flow pattern and cleaning performance of a
657 long liquid jet in a tank cleaning application. Q is the flow rate at the nozzle and L
658 is the distance travelled by the jet. Droop and breakup can cause the angle of
659 impingement ϕ to differ from that for a direct path.

660

661 **Figure 2** Flow pattern created by normal jet impinging on a flat vertical Perspex[®] wall,
662 $d_N = 2$ mm, $Q = 2$ dm³ min⁻¹, and $L = 70$ mm. (a) Steady pattern, showing key
663 dimensions – subscript c refers to external edge of the rope. (b) Evolution of flow
664 pattern following initial impingement by a steady jet. Horizontal loci indicate
665 steady state values.

666

667 **Figure 3** Comparison of predictions of the RFZ formation time, t_E , with experimental
668 measurements obtained for a coherent water jet at 20°C impinging on a flat vertical
669 glass wall, $d_N = 2.67$ mm. The growth of the thin film was analysed in the three
670 different directions indicated on the inset sketch: the average value \pm standard error
671 is plotted.

672

673 **Figure 4** Effect of (a) jet Reynolds number, and (b) L , on measured splatter fraction.
674 Symbols defined in legend: symbol shape indicates jet length while open symbols
675 indicate that jet breakup was observed. For clarity, data in (b) are offset on the y-
676 axis in order of nozzle diameter and error bars are omitted. Data sets for $d_N = 2$ mm
677 are shown in blue in the colour version of this Figure.

678

679 **Figure 5** Comparison of measured half-width of the radial flow zone at the level of the point
680 of impingement, R , with the Wilson *et al.* (2012) model (Equation [1]). Data plotted
681 against flow rate in film, Q_{eff} . Inset shows correlation between height Z and R ,
682 $Z \approx 4R/5$. Dashed line shows line of equality, $Z = R$. Data sets for $d_N = 2$ mm are
683 shown in blue in the colour version of this Figure.

684

685 **Figure 6** Effect of flow rate on (a) Z , and (b) R , for a coherent horizontal water jet
686 ($d_N = 2$ mm) impinging normally on (i) vertical cylinders, and (ii) horizontal

687 cylinders. Error bars omitted for clarity: these are approximately ± 2 mm for Z , \pm
688 2 mm for R and ± 0.1 dm³ min⁻¹ for Q .

689

690 Figure 7 (a) Shedding from the rope ($Q = 4.5$ dm³ min⁻¹), and (b) plan view of a horizontal
691 jet impinging normally on a horizontal cylinder. Flow rate increases from (i) to (iv).
692 $d_N = 4$ mm, $L = 30$ mm and $\kappa = 20$ m⁻¹. Vertical black line in (b) indicates the
693 crown (top) of the cylinder.

694

695 Figure 8 Evolution of the cleaned region radius over time for 0.2 mm thick petroleum jelly
696 layers on flat walls. Conditions: $d_N = 2$ mm, $Q_{\text{eff}} = 1.6$ dm³ min⁻¹ for $L = 60, 245$
697 and 350 mm. Note log₁₀ time scale. Loci show fit to Equation [6]. Error bars
698 omitted for clarity: these are approximately ± 2 mm for a .

699

700 Figure 9 Effect of curvature on size of cleaned region for 1.3 mm thick Carbopol[®] layers on
701 vertical cylinders. Coherent jet, $d_N = 2.0$ mm, $Q_{\text{eff}} = 1.0$ dm³ min⁻¹, no soaking. Note
702 log₁₀ time scale. Error bars omitted for clarity: these are approximately ± 2 mm
703 for a .

704

705 Figure 10 Effect of soaking time on the removal of 0.2 mm thick Carbopol[®] layers on flat
706 walls. A thin film of water covered the wall for 0 s (no soaking), 10 s or 60 s. In
707 these tests the target wall was horizontal rather than vertical, and the jet was vertical
708 rather than horizontal, as this allowed the soil to be cleaned directly after soaking.
709 Conditions: $d_N = 2$ mm, $Q = 2$ dm³ min⁻¹ and $L = 245$ mm. Loci show fit to the
710 expression $a = K t^{0.2}$. Error bars omitted for clarity: these are approximately ± 2
711 mm for a .

712

713 **List of Supplementary Figures**

714 **Figure S1** Data in Figure 4(b) plotted against L/d_N . Error bars omitted for clarity. Data sets
715 for $d_N = 2$ mm are shown in blue in the colour version of this Figure.

716

717 **Figure S2** Splatter fraction estimated from the Q_{eff}/Q data reported by Feldung Damkjær *et*
718 *al.* (2017) for industrial nozzles and long jet travel distances. Error bars are not
719 shown as no attempt was made to quantify the errors. Data sets for $d_N = 3.8$ mm
720 are shown in blue in the colour version of this Figure.

721

722 **Figure S3** Comparison of measured half-width of the radial flow zone at the level of the point
723 of impingement, R , with measured half-width of the wetted region at the level of
724 the point of impingement, R_c . Dashed line shows line of $R_c = 4R/3$. Data sets for
725 $d_N = 2$ mm are shown in blue in the colour version of this Figure.

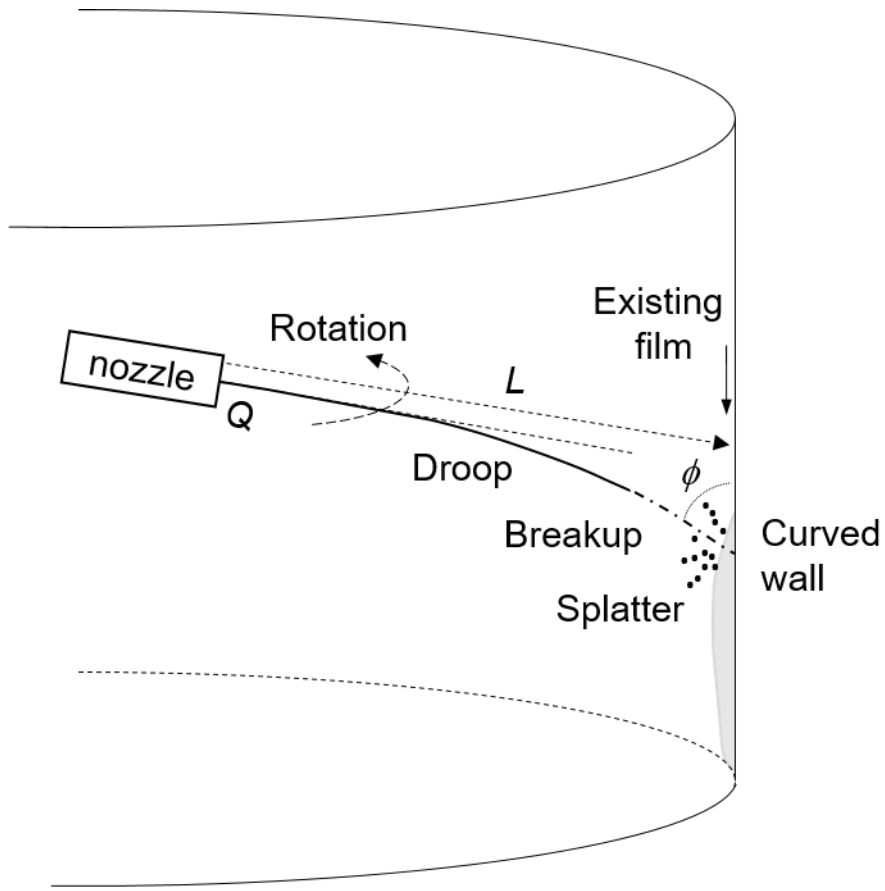
726

727 **Figure S4** Effect of wall curvature on the width of the rope, $B(0)$, at the top of the RFZ and at
728 the level of the impingement point, $B(\pi/2)$. Also plotted are the loci for the model
729 for B presented by Wang *et al.* (2013). Conditions: coherent jets, $d_N = 2.0$ mm.
730 Error bars omitted for clarity: these are approximately ± 2 mm for B and
731 ± 0.1 dm³ min⁻¹ for Q .

732

733 **Figures**

734



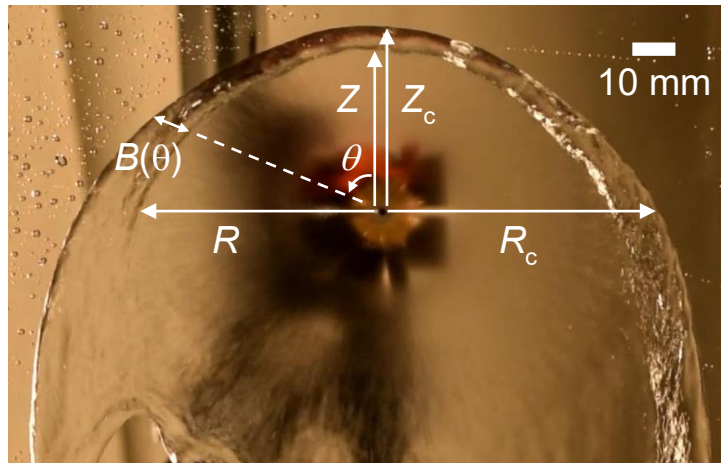
735

736

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738 long liquid jet in a tank cleaning application. Q is the flow rate at the nozzle and L
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740 impingement ϕ to differ from that for a direct path.

741

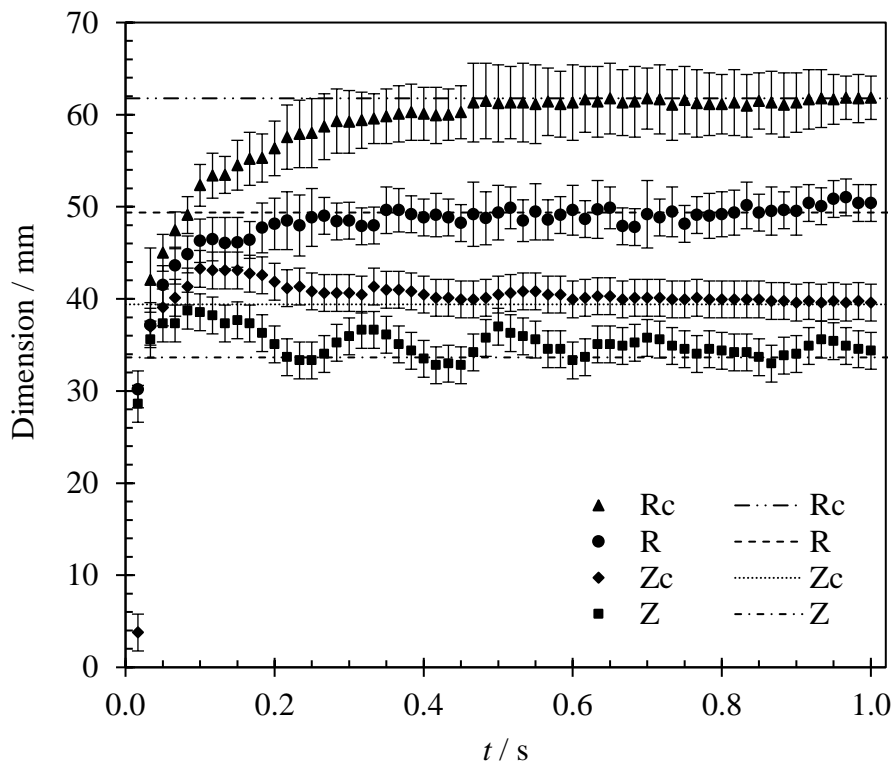
742 (a)



743

744

745 (b)

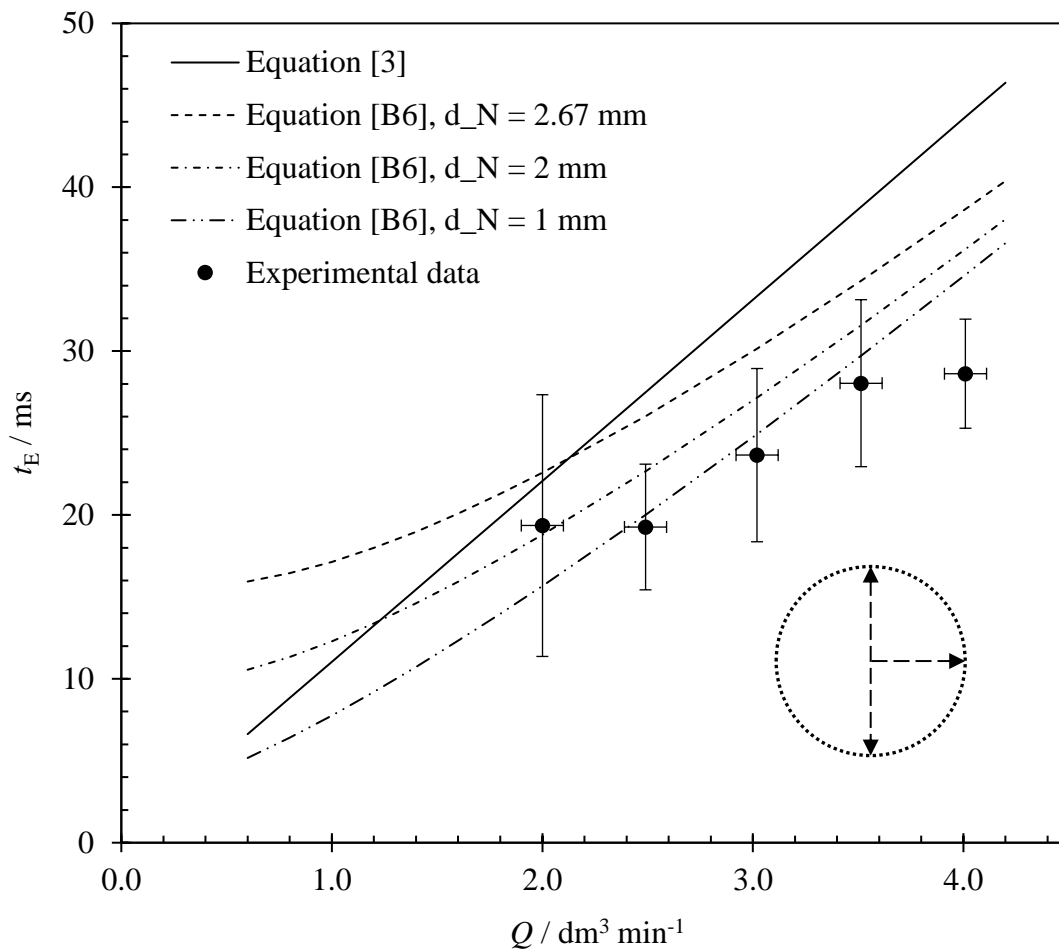


746

747

748 **Figure 2** Flow pattern created by normal jet impinging on a flat vertical Perspex[®] wall,
 749 $d_N = 2$ mm, $Q = 2$ dm³ min⁻¹, and $L = 70$ mm. (a) Steady pattern, showing key
 750 dimensions – subscript c refers to external edge of the rope. (b) Evolution of flow
 751 pattern following initial impingement by a steady jet. Horizontal loci indicate
 752 steady state values.

753



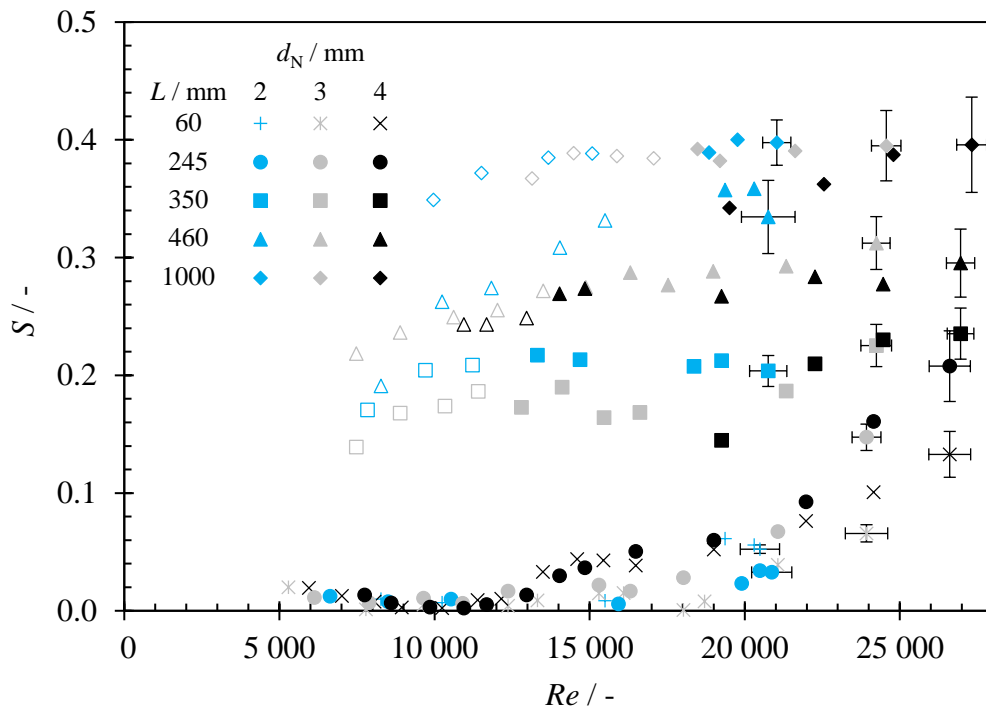
755

756

757 **Figure 3** Comparison of predictions of the RFZ formation time, t_E , with experimental
 758 measurements obtained for a **coherent** water jet at 20°C impinging on a **flat** vertical
 759 glass **wall**, $d_N = 2.67 \text{ mm}$. The growth of the thin film was analysed in the three
 760 different directions indicated on the inset sketch: the average value \pm standard error
 761 is plotted.

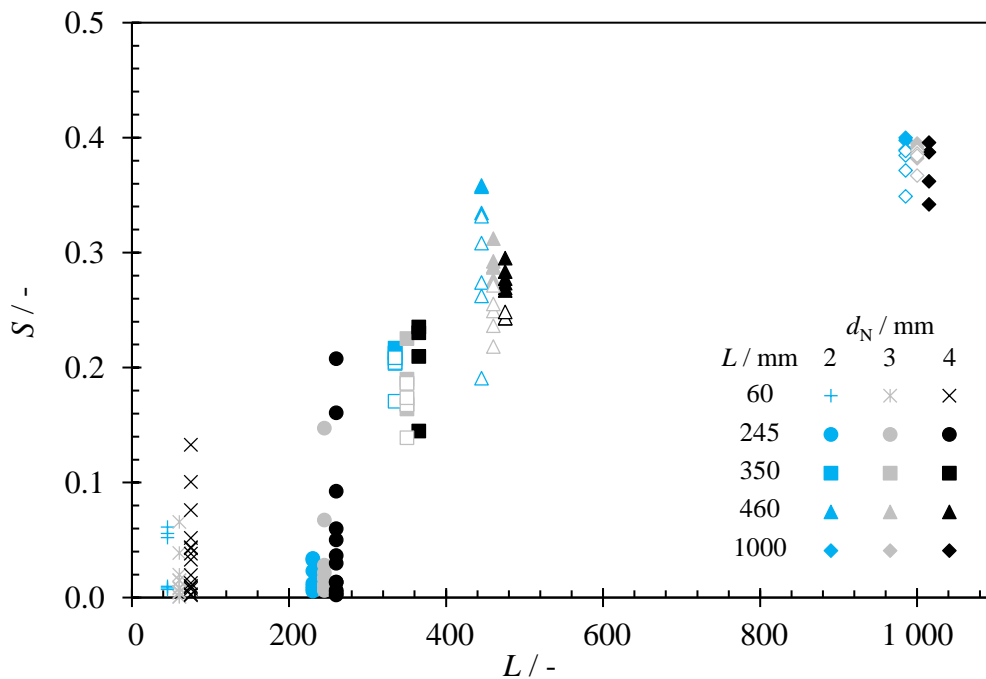
762

763 (a)



764

765 (b)



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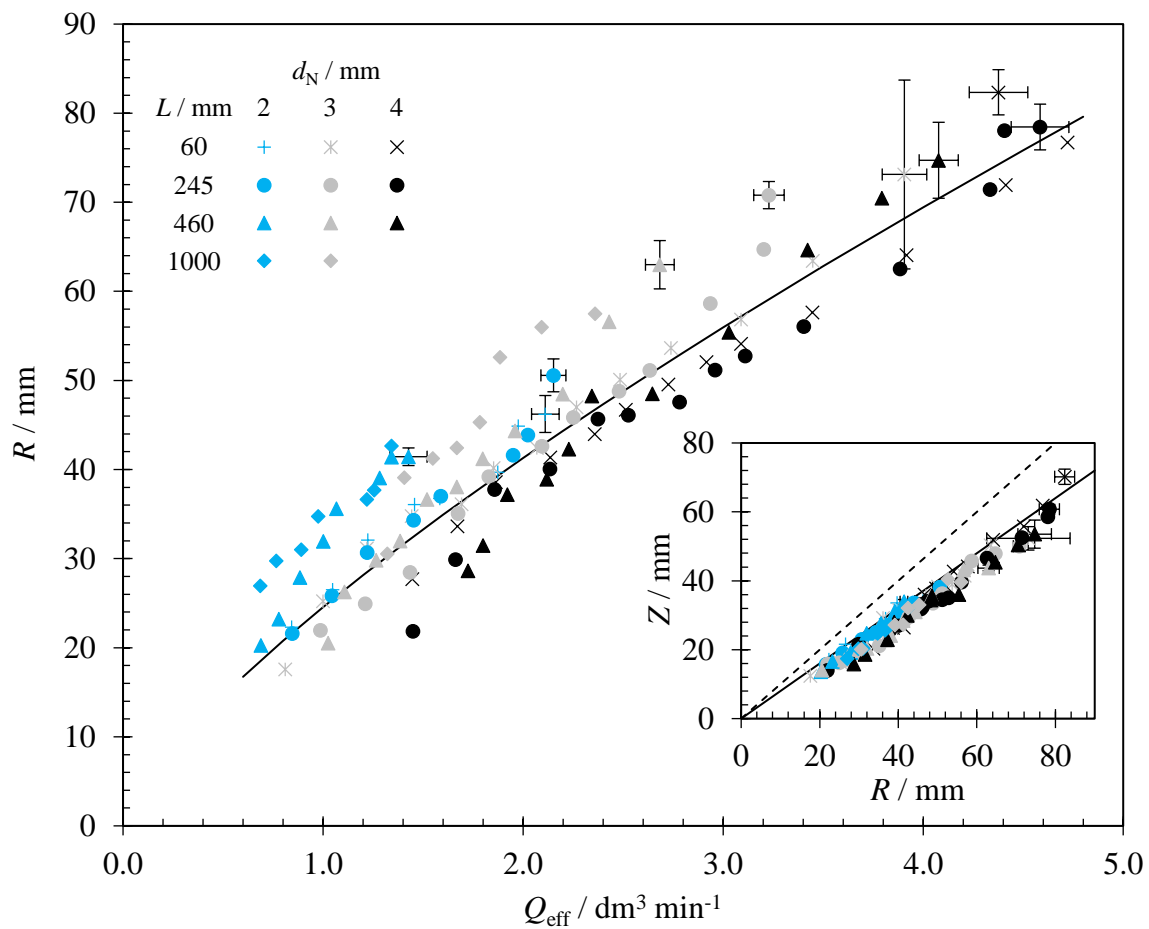
768 Figure 4 Effect of (a) jet Reynolds number, and (b) L , on measured splatter fraction.

769 Symbols defined in legend: symbol shape indicates jet length while open symbols

770 indicate that jet breakup was observed. For clarity, data in (b) are offset on the y -

771 axis in order of nozzle diameter and error bars are omitted. Data sets for $d_N = 2$ mm

772 are shown in blue in the colour version of this Figure.



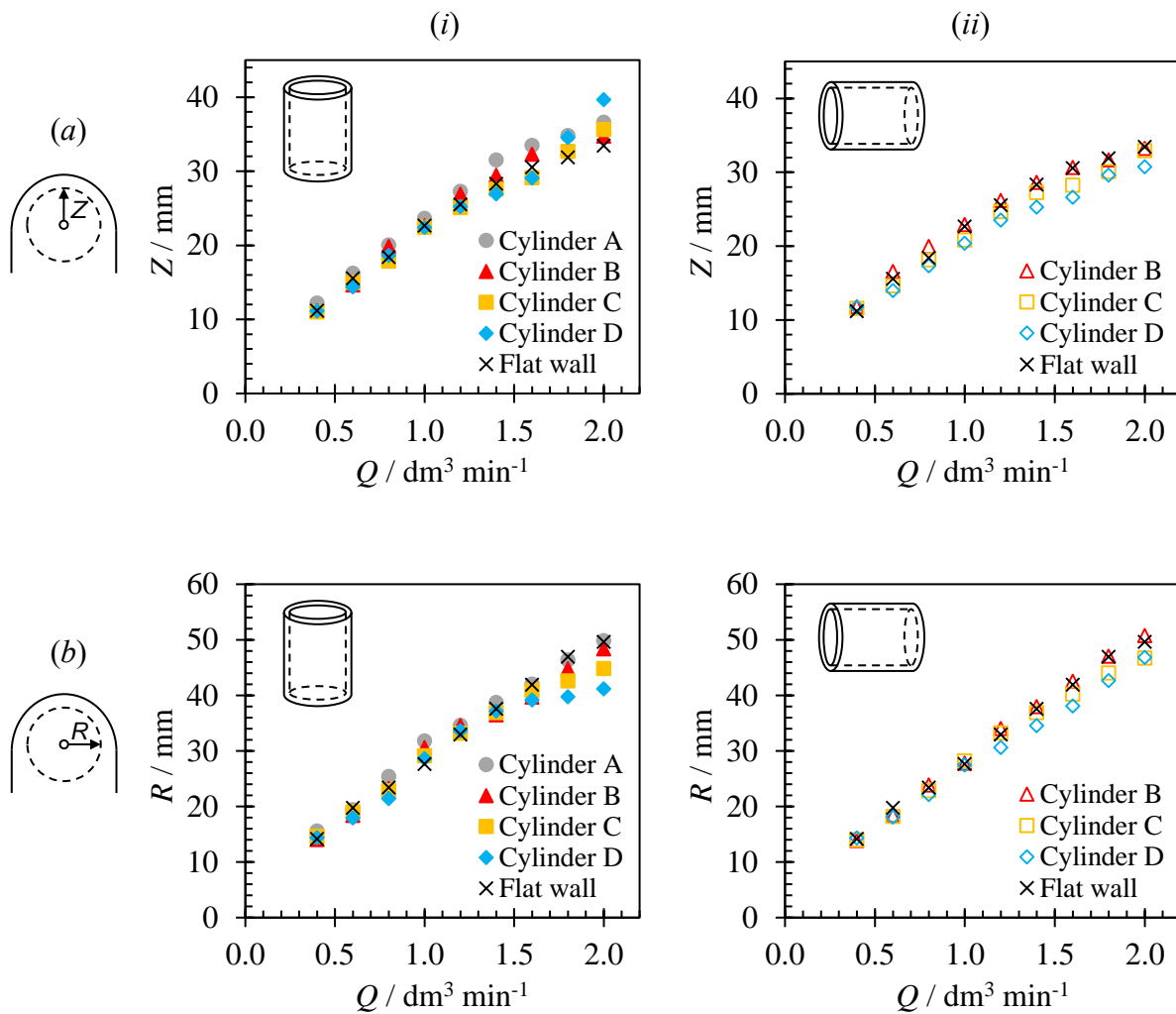
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776 **Figure 5** Comparison of measured half-width of the radial flow zone at the level of the point
 777 of impingement, R , with the Wilson *et al.* (2012) model (Equation [1]). Data plotted
 778 against flow rate in film, Q_{eff} . Inset shows correlation between height Z and R ,
 779 $Z \approx 4R/5$. Dashed line shows line of equality, $Z = R$. Data sets for $d_N = 2 \text{ mm}$ are
 780 shown in blue in the colour version of this Figure.

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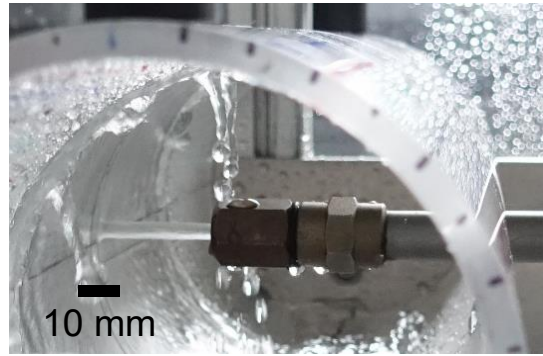
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790 **Figure 6** Effect of flow rate on (a) Z , and (b) R , for a **coherent** horizontal water jet
791 ($d_N = 2$ mm) impinging normally on (i) vertical cylinders, and (ii) horizontal
792 cylinders. Error bars omitted for clarity: **these are approximately ± 2 mm for Z , \pm**
793 **2 mm for R and ± 0.1 dm³ min⁻¹ for Q .**

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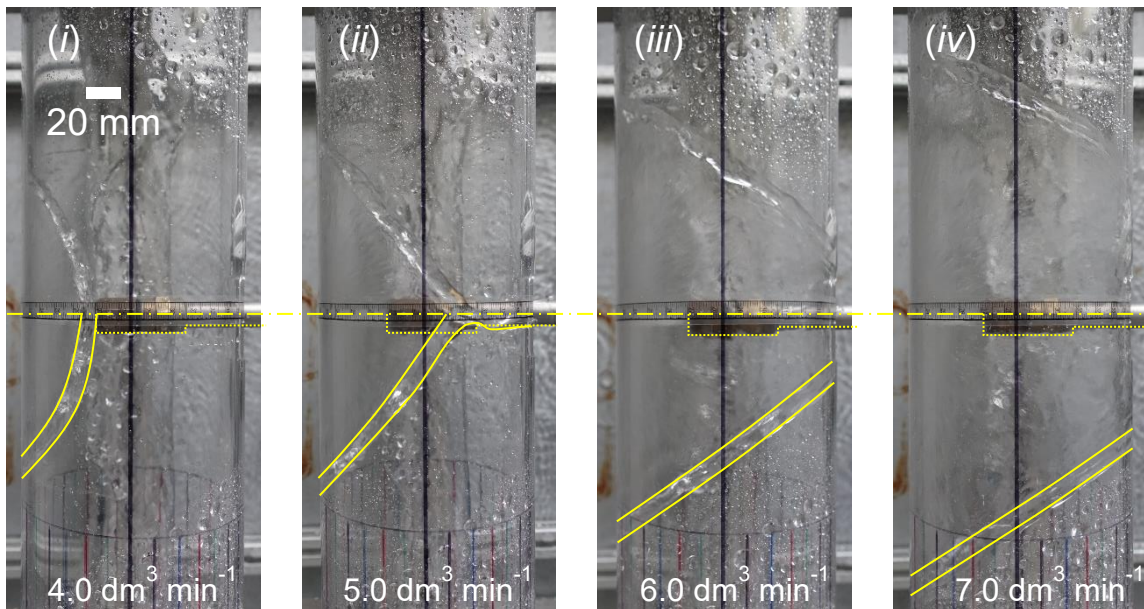
795 (a)



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798 (b)

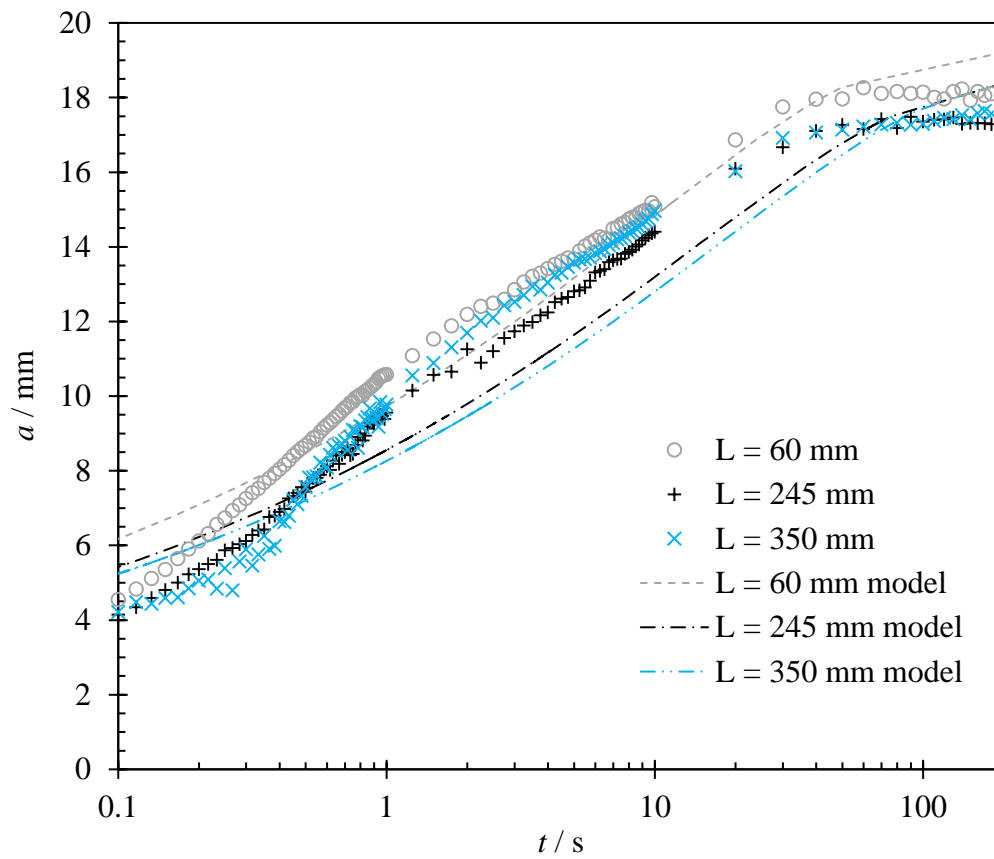


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801 **Figure 7** (a) Shedding from the rope ($Q = 4.5 \text{ dm}^3 \text{ min}^{-1}$), and (b) plan view of a horizontal
802 jet impinging normally on a horizontal cylinder. Flow rate increases from (i) to (iv).
803 $d_N = 4 \text{ mm}$, $L = 30 \text{ mm}$ and $\kappa = 20 \text{ m}^{-1}$. **Vertical black line** in (b) indicates the
804 crown (top) of the cylinder.

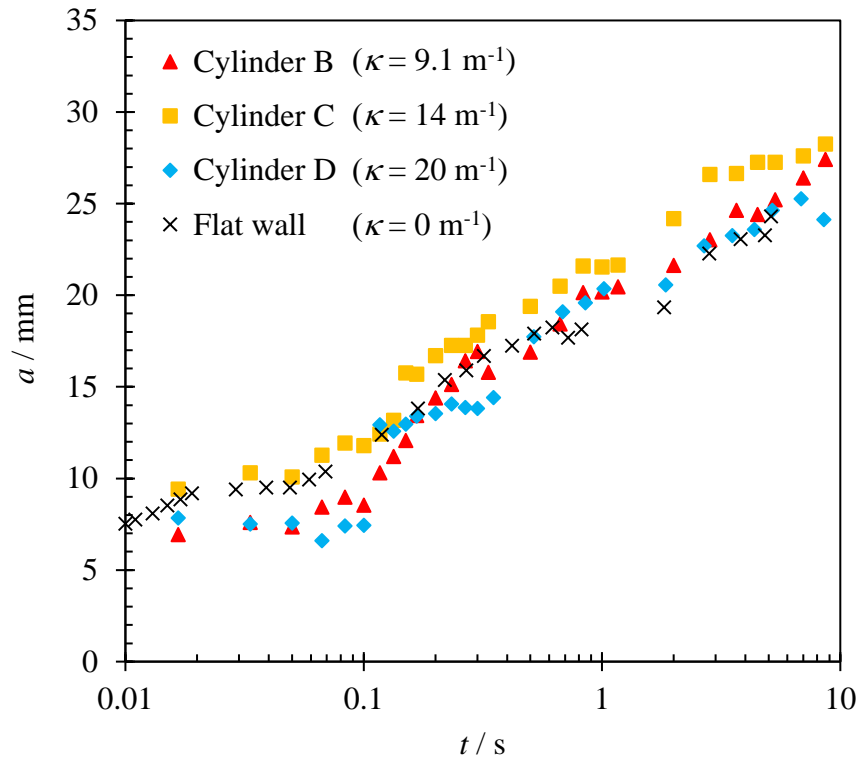
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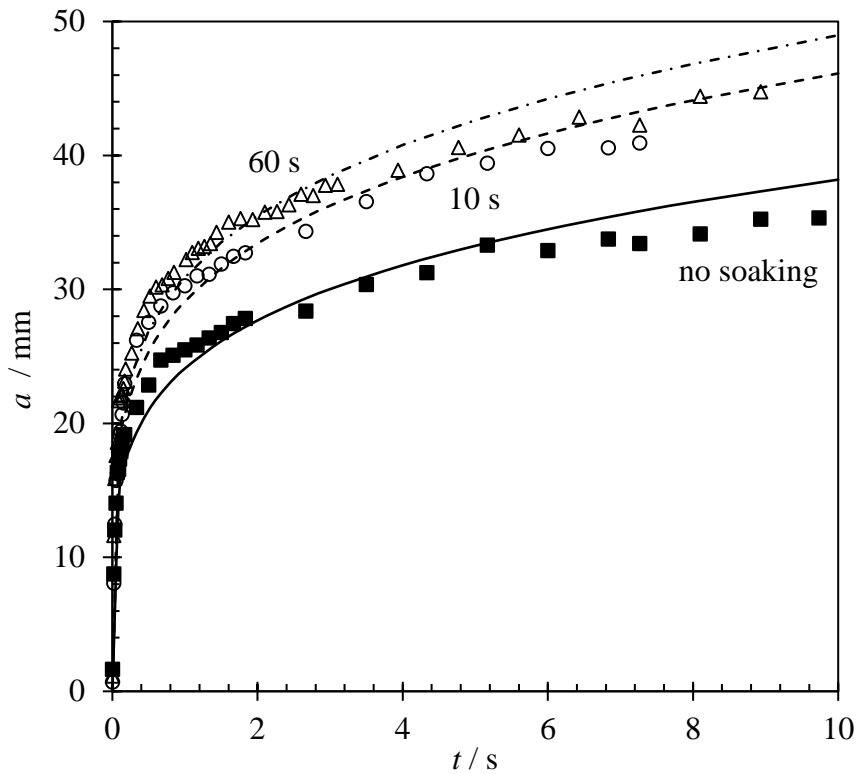
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809 **Figure 8** Evolution of the cleaned region radius over time for 0.2 mm thick petroleum jelly810 layers on flat walls. Conditions: $d_N = 2$ mm, $Q_{\text{eff}} = 1.6$ dm³ min⁻¹ for $L = 60, 245$ 811 and 350 mm. Note \log_{10} time scale. Loci show fit to Equation [6]. Error bars812 omitted for clarity: these are approximately ± 2 mm for a .



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Figure 9 Effect of curvature on size of cleaned region for 1.3 mm thick Carbopol[®] layers on vertical cylinders. Coherent jet, $d_N = 2.0 \text{ mm}$, $Q_{\text{eff}} = 1.0 \text{ dm}^3 \text{ min}^{-1}$, no soaking. Note \log_{10} time scale. Error bars omitted for clarity: these are approximately $\pm 2 \text{ mm}$ for a .



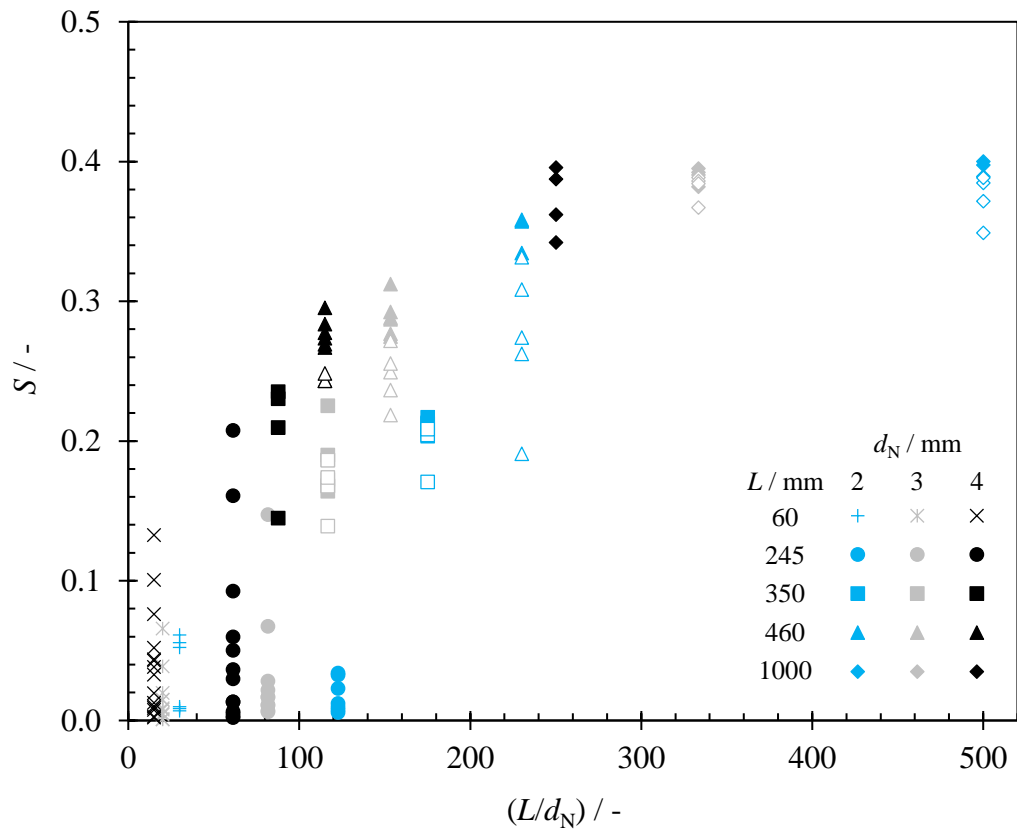
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Figure 10 Effect of soaking time on the removal of 0.2 mm thick Carbopol[®] layers on flat walls. A thin film of water covered the wall for 0 s (no soaking), 10 s or 60 s. In these tests the target wall was horizontal rather than vertical, and the jet was vertical rather than horizontal, as this allowed the soil to be cleaned directly after soaking. Conditions: $d_N = 2$ mm, $Q = 2$ dm³ min⁻¹ and $L = 245$ mm. Loci show fit to the expression $a = K t^{0.2}$. Error bars omitted for clarity: these are approximately ± 2 mm for a .

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833 **Supplementary Figures**

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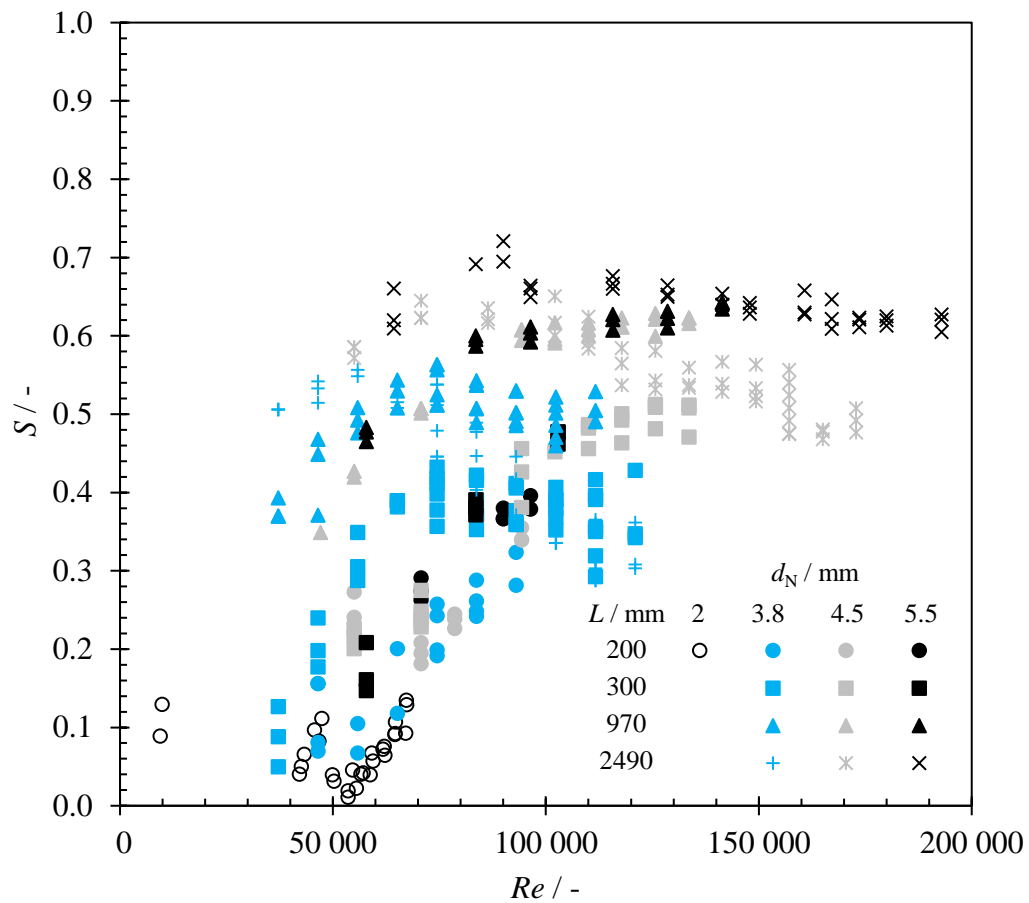
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837 Figure S1 Data in Figure 4(b) plotted against L/d_N . Error bars omitted for clarity. Data sets
838 for $d_N = 2$ mm are shown in blue in the colour version of this Figure.

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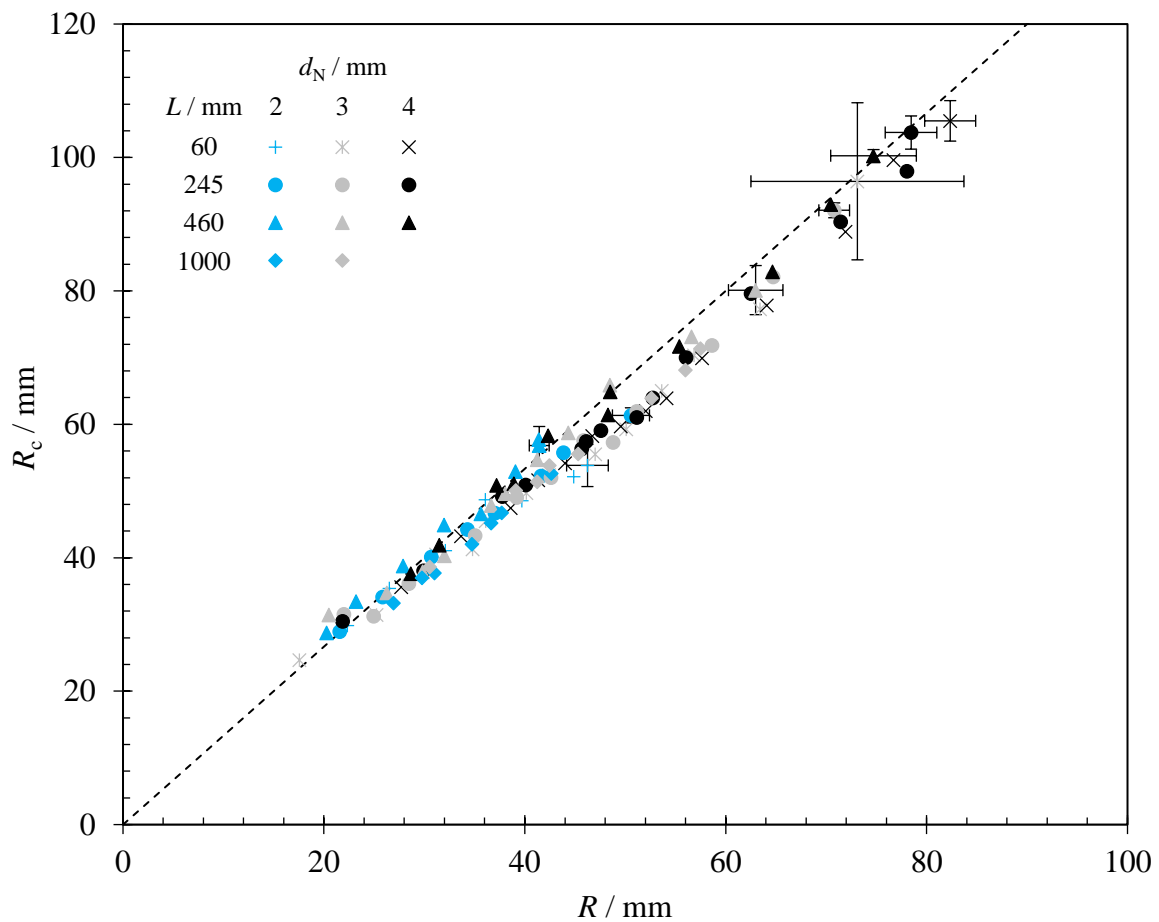
844 **Figure S2** Splatter fraction estimated from the Q_{eff}/Q data reported by Feldung Damkjær *et*
 845 *al.* (2017) for industrial nozzles and long jet travel distances. Error bars are not
 846 shown as no attempt was made to quantify the errors. Data sets for $d_N = 3.8$ mm
 847 are shown in blue in the colour version of this Figure.

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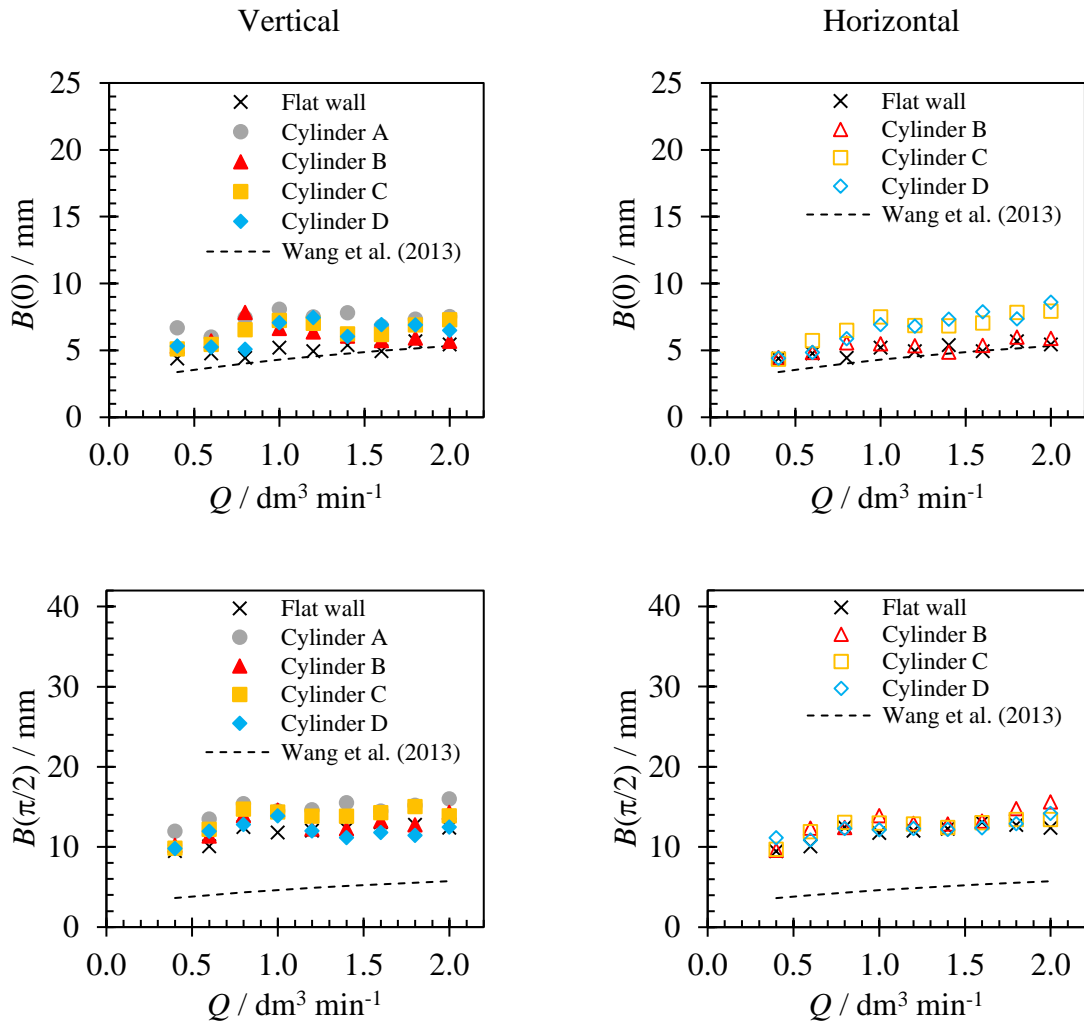
854 **Figure S3** Comparison of measured half-width of the radial flow zone at the level of the point
855 of impingement, R , with measured half-width of the wetted region at the level of
856 the point of impingement, R_c . Dashed line shows line of $R_c = 4R/3$. **Data sets for**
857 **$d_N = 2 \text{ mm}$ are shown in blue in the colour version of this Figure.**

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864 Figure S4 Effect of wall curvature on the width of the rope, $B(0)$, at the top of the RFZ and at
 865 the level of the impingement point, $B(\pi/2)$. Also plotted are the loci for the model
 866 for B presented by Wang *et al.* (2013). **Conditions: coherent jets, $d_N = 2.0$ mm.**
 867 **Error bars omitted for clarity: these are approximately ± 2 mm for B and**
 868 **± 0.1 $\text{dm}^3 \text{min}^{-1}$ for Q .**

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