

Effects of medium on nuclear properties in multifragmentationJ. N. De,¹ S. K. Samaddar,¹ X. Viñas,² M. Centelles,² I. N. Mishustin,^{3,4} and W. Greiner³¹*Saha Institute of Nuclear Physics, 1/AF Bidhannagar, Kolkata 700064, India*²*Departament d'Estructura i Constituents de la Matèria, Facultat de Física, and Institut de Ciències del Cosmos, Universitat de Barcelona, Diagonal 645, 08028 Barcelona, Spain*³*Frankfurt Institute for Advanced Studies, J. W. Goethe University, D-60438 Frankfurt Am Main, Germany*⁴*Kurchatov Institute, Moscow 123182, Russia*

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In multifragmentation of hot nuclear matter, properties of fragments embedded in a soup of nucleonic gas and other fragments should be modified as compared with isolated nuclei. Such modifications are studied within a simple model where only nucleons and one kind of heavy nuclei are considered. The interaction between different species is described with a momentum-dependent two-body potential whose parameters are fitted to reproduce properties of cold isolated nuclei. The internal energy of heavy fragments is parametrized according to a liquid-drop model with density- and temperature-dependent parameters. Calculations are carried out for several subnuclear densities and moderate temperatures, for isospin-symmetric and asymmetric systems. We find that the fragments get stretched due to interactions with the medium and their binding energies decrease with increasing temperature and density of nuclear matter.

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I. INTRODUCTION

In energetic nuclear collisions, the participating hot nuclear matter after an initial dynamic stage of compression expands to a subsaturation density and then disassembles into many fragments due to growing instability. Statistical models of different genres [1–6] have generally been successful in explaining the many features associated with the fragment multiplicities, the caloric curve, the density of the fragmenting systems, etc. They also offer a broad hint about the general nature of the phase diagram of nuclear matter [7,8] at temperature $T \sim 3$ –8 MeV at subsaturation densities $\rho \sim 1/20$ to $1/5$ of the normal nuclear density ρ_0 . Possible liquid-gas phase transition and associated condensation [9–11] to form nuclear clusters at these temperatures and densities help in a better exploration of many phenomena of astrophysical interest, such as supernova explosions or explosive nucleosynthesis [12–17].

Analysis of recent laboratory experiments [18,19] on nuclear multifragmentation seems to indicate that the properties of the nuclides are modified at the subnuclear densities ($\rho \sim \rho_0/3$), corresponding to freeze-out, in which they are created. The symmetry energy, for example, is reported to be progressively reduced [20] with excitation energy, which is attributed to the in-medium modifications of the properties of the hot fragments [21,22]. A looming uncertainty about whether the measured symmetry energy corresponds to the hot fragments or the fragmenting system [20,23], however, does not allow an equivocal decision about the medium modifications. The reduction in symmetry energy can have a fair explanation from the thermal and expansion effects of the disassembling system [24]. The surface properties of the hot fragments [25] as well as their bulk energy [26] are also speculated to be modified due to the embedding environment. A quantum statistical approach to the nuclear equation of state taking into account the formation of clusters [27,28] shows that the properties of these clusters are modified due to the medium

in which they are formed. The symmetry energy of low-density warm nuclear matter predicted by this model seems to be in good agreement with the experimental data [29]. In a recent experiment [30], it is claimed that the binding energies of very light clusters ($A \leq 4$) produced in multifragmentation progressively tend to zero in the temperature range of $T \sim 5$ –10 MeV even at a very low in-medium density $\sim 0.05\rho_0$.

The changes, if any, of the bulk properties of the fragments produced in nuclear disassembly are expected to originate from the effects of the residual interaction of the fragments with the surroundings. The aim of the present article is to study these effects starting from an effective nucleon-nucleon interaction. To keep the physics simple and transparent and yet retain all the basic essentials, we allow the dilute matter to condense into only one kind of nuclear species surrounded by a hot nucleonic gas and species of the same kind. Then we introduce the interactions between them and look for the minimum of the free energy of the system with variation of the size of the fragments, maintaining chemical equilibrium between the fragments and the nucleon gas. The energy and free energy of the nuclei are evaluated in the liquid-drop framework, which makes it easier to account for the associated changes in the surface and symmetry energy with the change in the volume of the fragment species.

The organization of the paper is as follows. In Sec. II, the outlines of the theory are given. Results and discussions are contained in Sec. III. The concluding remarks are presented in Sec. IV.

II. THEORETICAL FORMULATION

As is well known, hot low-density nuclear matter condenses into nuclear fragments of different sizes surrounded by nucleons. We postulate that the nucleons and the fragments interact through a common effective interaction. The bulk

properties of the fragments may be modified because of this interaction too. For a qualitative understanding of such a system, we take only one kind of fragment species of mass A and charge Z . The interaction is chosen to be the modified Seyler-Blanchard (SBM) interaction. Its properties are summarized in Sec. II A. In Sec. II B, the method for evaluating the nucleon-fragment and the fragment-fragment interactions is described. In Sec. II C, we study the observables sensitive to the medium modification of the properties of finite nuclei.

A. The effective interaction

The SBM interaction is a momentum- and density-dependent effective interaction of finite range. In the context of the nuclear mass formula, an interaction of this type has been used with great success by Myers and Swiatecki [31]. It also reproduces the rms radii, charge distributions, and giant monopole resonance energies for a host of even-even nuclei ranging from ^{16}O to very heavy systems [32]. Its form is given by

$$\begin{aligned} v(r, p, \rho) &= C_{l,u} [v_1(r, p) + v_2(r, \rho)], \\ v_1 &= - \left(1 - \frac{p^2}{b^2} \right) f(\mathbf{r}_1, \mathbf{r}_2), \\ v_2 &= d^2 [\rho(r_1) + \rho(r_2)]^\kappa f(\mathbf{r}_1, \mathbf{r}_2), \end{aligned} \quad (1)$$

with

$$f(\mathbf{r}_1, \mathbf{r}_2) = \frac{e^{-|\mathbf{r}_1 - \mathbf{r}_2|/a}}{|\mathbf{r}_1 - \mathbf{r}_2|/a}. \quad (2)$$

The subscripts l and u to the interaction strength C refer to like-pair (nn or pp) and unlike-pair (np) interactions, respectively. The relative separation of the interacting nucleons is $\mathbf{r} = \mathbf{r}_1 - \mathbf{r}_2$ and the relative momentum is $\mathbf{p} = \mathbf{p}_1 - \mathbf{p}_2$. The potential parameters C_l , C_u , a , b , d , and κ are listed in Table I. The procedure for determining these parameters are given in detail in Ref. [33]. These parameters are somewhat different from those given in Ref. [32]; in the latter, the symmetry coefficient a_{sym} for infinite nuclear matter at saturation density ρ_0 was chosen to be 34 MeV; in the present calculation, it is taken to be 31 MeV to be more consistent with the recent estimates [34,35]. The effective mass of the nucleon coming from the momentum dependence of this effective interaction is $0.62m$ for symmetric nuclear matter, where m is the nucleon mass. For the interaction, the isoscalar volume incompressibility K_∞ , symmetry incompressibility K_{sym} , and L , a measure of the symmetry pressure, are 240, -101 , and 59.8 MeV, respectively. It is interesting to note that the symmetry coefficients a_{sym} , L , and K_{sym} of this interaction are within the range of values suggested

TABLE I. The parameters of the effective interaction (in MeV fm units).

C_l	C_u	a	b	d	κ
348.5	829.7	0.6251	927.5	0.879	1/6

by the empirical constraints emerging from recent analysis of different observables [34–40]. With this interaction, for symmetric nuclear matter, the critical temperature is reached at $T_c = 14.9$ MeV, when the surface energy vanishes.

B. Nucleon-fragment and fragment-fragment interaction energy

A low-density nucleonic matter of density ρ_b and asymmetry $X = (\rho_n^b - \rho_p^b)/\rho_b$ breaks up to a system of free (unbound) neutrons and protons of density ρ_n and ρ_p and a collection of mass- A fragments (we call it AN matter), all at temperature T . The clustered matter is thermodynamically more favorable than the uniform matter at the same (low) density, asymmetry, and temperature [41]. The baryonic density is then given by

$$\rho_b = \rho_N + A\rho_A, \quad (3)$$

where $\rho_N = \rho_n + \rho_p$ is the free nucleonic density and ρ_A is the number density of the fragment species. The total thermodynamic potential Ω of the system is

$$\Omega = E - TS - \sum_\tau \mu_\tau N_\tau - \mu_A N_A, \quad (4)$$

where E , S , μ_τ , μ_A , N_τ , and N_A are the total energy, entropy, chemical potentials of the free nucleons and the fragments, free nucleon number, and the number of the fragments of mass A , respectively. The isospin index (n , p) is represented by τ . Chemical equilibration ensures

$$\mu_A = N\mu_n + Z\mu_p, \quad (5)$$

where N and Z are the neutron and proton numbers in the fragment. The total internal energy of the AN system is written as

$$E = E_{NN} + E_{AN} + E_{AA}. \quad (6)$$

In Eq. (6), E_{AN} is the contribution coming from the nucleon-fragment interaction (V_{AN}). E_{NN} measures the kinetic energy of the free nucleons plus the interaction energy amongst themselves. E_{AA} is the sum total of the the kinetic energy of the fragments, interaction energy among them, and their binding energies.

Assuming for simplicity that the fragments are sharp-surface liquid drops with a uniform nucleon density ρ_l , these terms can be explicitly written as

$$\begin{aligned} E_{NN} &= \sum_\tau \left\{ \int d\mathbf{r}_1 d\mathbf{p}_1 \frac{p_1^2}{2m_\tau} \tilde{n}_\tau(\mathbf{p}_1) + \frac{1}{2} \int d\mathbf{r}_1 d\mathbf{p}_1 d\mathbf{r}_2 d\mathbf{p}_2 \right. \\ &\quad \times [v_1(|\mathbf{r}_1 - \mathbf{r}_2|, |\mathbf{p}_1 - \mathbf{p}_2|) + v_2(|\mathbf{r}_1 - \mathbf{r}_2|, 2\rho_N)] \\ &\quad \left. \times [C_l \tilde{n}_\tau(\mathbf{p}_2) + C_u \tilde{n}_{-\tau}(\mathbf{p}_2)] \tilde{n}_\tau(\mathbf{p}_1) \right\}, \end{aligned} \quad (7)$$

$$\begin{aligned} E_{AN} &= \frac{1}{2} \sum_\tau \left\{ \int d\mathbf{r}_1 d\mathbf{p}_1 d\mathbf{r}_2 d\mathbf{p}_2 \right. \\ &\quad \times \tilde{n}_\tau(\mathbf{r}_1, \mathbf{p}_1) \tilde{n}_A(\mathbf{r}_2, \mathbf{p}_2) \sum_{\tau'} (C_l \delta_{\tau\tau'} + C_u (1 - \delta_{\tau\tau'})) \\ &\quad \times \int_{V_A} d\mathbf{r} \int d\mathbf{p}_{l\tau}^A \tilde{n}_{l\tau}^A(\mathbf{r}, \mathbf{p}_{l\tau}^A) [v_1(|\mathbf{r} + \mathbf{R}|, |\mathbf{p}_1 \\ &\quad \left. - (\mathbf{p}_{l\tau}^A + \mathbf{p}_2)|) + v_2(|\mathbf{r} + \mathbf{R}|, \rho_N + \rho_l)] \right\}, \end{aligned} \quad (8)$$

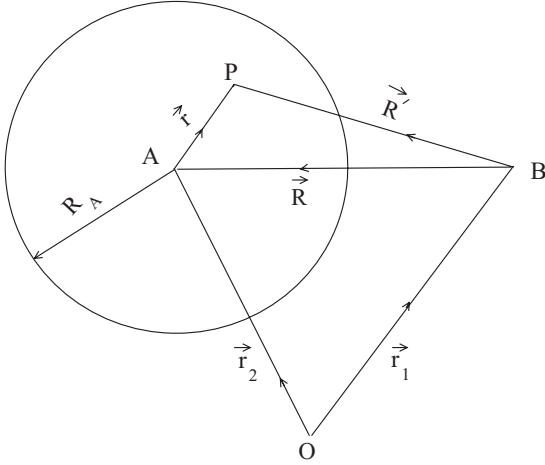


FIG. 1. Space coordinates shown for nucleon (located at B) and fragment (with center at A) configuration. The origin of the coordinate system is at O and P is any arbitrary point within the fragment.

and

$$E_{AA} = E_{AA}^0 - N_A B_A(\rho_l, T), \quad (9)$$

where

$$\begin{aligned} E_{AA}^0 = & \int d\mathbf{r} d\mathbf{p} \frac{p^2}{2m_A} \tilde{n}_A(\mathbf{r}, \mathbf{p}) + \frac{1}{2} \int d\mathbf{r}_1 d\mathbf{p}_1 d\mathbf{r}_2 d\mathbf{p}_2 \\ & \times \tilde{n}_A(\mathbf{r}_1, \mathbf{p}_1) \tilde{n}_A(\mathbf{r}_2, \mathbf{p}_2) \int_{V_A} d\mathbf{r} d\mathbf{r}' \\ & \times \sum_{\tau, \tau'} [C_l \delta_{\tau\tau'} + C_u (1 - \delta_{\tau\tau'})] \int d\mathbf{p}_{l\tau}^A d\mathbf{p}_{l\tau'}^A \\ & \times \tilde{n}_{l\tau}^A(\mathbf{r}, \mathbf{p}_{l\tau}^A) \tilde{n}_{l\tau'}^A(\mathbf{r}', \mathbf{p}_{l\tau'}^A) [v_1(|\mathbf{R} + \mathbf{r} - \mathbf{r}'|, |(\mathbf{p}_1 + \mathbf{p}_{l\tau}^A) \\ & - (\mathbf{p}_2 + \mathbf{p}_{l\tau'}^A)|) + v_2(|\mathbf{R} + \mathbf{r} - \mathbf{r}'|, 2\rho_l)]. \quad (10) \end{aligned}$$

In Eq. (8), $\mathbf{R} = \mathbf{r}_2 - \mathbf{r}_1$ is the distance between the nucleon and the center of the nucleus (see Fig. 1). In Eq. (10), \mathbf{R} is the distance between the two fragment centers (see Fig. 2). The various space coordinates occurring in Eqs. (8) and (10) are shown in Figs. 1 and 2, respectively. In evaluating the coordinate-space integrals in Eqs. (7), (8), and (10), we have assumed, as in the calculation of the equation of state of dilute

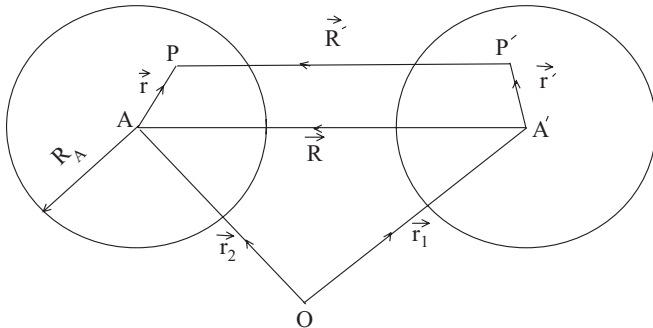


FIG. 2. Space coordinates shown for fragment-fragment configuration with O as the origin of the coordinate system. P and P' are arbitrary points within the fragments with A and A' as their centers.

nuclear matter [42,43], that the free nucleons do not penetrate the sharp surface nuclei and also that the fragments do not interpenetrate so that the identity of the free nucleons and the fragments is never altered. This “no-overlap” approximation is tantamount to use of the “excluded-volume” correction employed earlier [2] where the “free” volume available to fragments is reduced compared to the total volume V by at least the internal volume of the nucleons and the fragments.

In the above equations, m_τ and m_A are the masses of the nucleons and the fragments, and $B_A(\rho_l, T)$ is the binding energy of the produced fragments at temperature T with internal nucleon density ρ_l . Here $\tilde{n}_\tau = \frac{2}{h^3} n_\tau$ and $\tilde{n}_A = \frac{g_A}{h^3} n_A$; n_τ and n_A are the occupation probabilities for the free nucleons and the fragments, and g_A is the degeneracy of the fragments taken to be 1 or 2 depending on whether they are bosons or fermions. Since the system is infinite, the occupation functions \tilde{n}_τ are independent of space coordinates. Similar is the case for \tilde{n}_A . In the equations above, space dependence has, however, been retained to correlate with Figs. 1 and 2. Since the fragments are also taken to be uniform drops, $\tilde{n}_{l\tau}^A (= \frac{2}{h^3} n_{l\tau}^A)$, the distribution function of the constituent nucleons inside the fragments is also independent of the space coordinates. The explicit functional dependence of the distribution functions on the space coordinates is henceforth omitted from the equations where the distribution functions may enter. The momenta of these nucleons inside the fragment is designated by $\mathbf{p}_{l\tau}^A$. The notation \int_{V_A} refers to the configuration integral over the volume V_A of the fragment. All other integrals are over the entire configuration or momentum space unless otherwise specified. The distribution functions yield the densities as

$$\frac{2}{h^3} \int n_\tau(\mathbf{p}) d\mathbf{p} = N_\tau / V = \rho_\tau, \quad (11)$$

$$\frac{2}{h^3} \int n_A(\mathbf{p}) d\mathbf{p} = N_A / V = \rho_A, \quad (12)$$

$$\frac{2}{h^3} \int n_{l\tau}^A(\mathbf{p}) d\mathbf{p} = A_\tau / V_A = \rho_{l\tau}, \quad (13)$$

where V is the volume of the AN matter, A_τ is the neutron number N or proton number Z in the fragment, $\rho_N = \sum_\tau \rho_\tau$, $\rho_l = \sum_\tau \rho_{l\tau}$, and $V_A = \frac{4\pi}{3} R_A^3$. In Eq. (13), $\rho_{l\tau}$ refers to the neutron or proton number density in the fragment; R_A is its sharp-surface radius.

The total entropy of the AN system is

$$S = \sum_\tau S_\tau + S_A^{tr} + S_A^{int}, \quad (14)$$

where, in the Landau quasiparticle approximation, the contribution $\sum_\tau S_\tau$ of the free nucleons is taken as

$$\begin{aligned} \sum_\tau S_\tau = & -\frac{2}{h^3} \sum_\tau \int d\mathbf{r} d\mathbf{p} [n_\tau(\mathbf{p}) \ln n_\tau(\mathbf{p}) \\ & + [1 - n_\tau(\mathbf{p})] \ln [1 - n_\tau(\mathbf{p})]]. \quad (15) \end{aligned}$$

S_A^{tr} is the entropy from the center-of-mass motion of the fragments, and S_A^{int} is their internal entropy. S_A^{tr} is evaluated as

$$\begin{aligned} S_A^{tr} = & -\frac{g_A}{h^3} \int d\mathbf{r} d\mathbf{p} [n_A(\mathbf{p}) \ln n_A(\mathbf{p}) \\ & \pm (1 \mp n_A(\mathbf{p})) \ln (1 \mp n_A(\mathbf{p}))]. \quad (16) \end{aligned}$$

In the above equation, the upper and lower signs correspond to a fermionic and bosonic fragment, respectively. The contribution TS_A^{int} from internal entropy to the thermodynamic potential can be absorbed along with the binding energy term of Eq. (9) in the free energy of the fragments $F_A(\rho_l, T) = [-B_A(\rho_l, T) - TS_A^{\text{int}}]$ when the thermodynamic potential takes the form

$$\Omega = E_{NN} + E_{AN} + E_{AA}^0 - T \left(\sum_{\tau} S_{\tau} + S_A^{\text{tr}} \right) - \sum_{\tau} \mu_{\tau} N_{\tau} - \mu_A N_A + N_A F_A(\rho_l, T). \quad (17)$$

Minimization of Ω with respect to n_{τ} and n_A , remembering that $\delta n_{\tau}(\mathbf{p})$ and $\delta n_A(\mathbf{p})$ are separately arbitrary over the whole phase space, after some algebraic manipulations, yields the distribution functions with the following structures:

$$n_{\tau}(\mathbf{p}) = \left[\exp \left(\frac{p^2}{2m_{\tau}^* T} - \eta_{\tau} \right) + 1 \right]^{-1}, \quad (18)$$

$$n_A(\mathbf{p}) = \left[\exp \left(\frac{p^2}{2m_A^* T} - \eta_A \right) \pm 1 \right]^{-1}. \quad (19)$$

In Eqs. (18) and (19), $\eta_{\tau} = (\mu_{\tau} - V_{\tau}^0 - V_{\tau}^2)/T$ and $\eta_A = (\mu_A - F_A - V_A^0)/T$ are the fugacities pertaining to the free nucleons and fragments, respectively, and m_{τ}^* and m_A^* are the effective masses of the nucleons and the fragments in the medium, the masses getting renormalized owing to the momentum dependence of the force. The nucleonic rearrangement potential V_{τ}^2 originates from the density dependence of the interaction. The effective nucleon and fragment masses are given by

$$m_{\tau}^* = \left[\frac{1}{m_{\tau}} + 2V_{\tau}^1 \right]^{-1} \quad (20)$$

and

$$m_A^* = \left[\frac{1}{m_A} + 2V_A^1 \right]^{-1}, \quad (21)$$

where $p^2 V_{\tau}^1$ and $p^2 V_A^1$ are the momentum-dependent contributions to the single-particle potentials V_{τ} and V_A :

$$V_{\tau}(p) = V_{\tau}^0 + p^2 V_{\tau}^1, \quad (22)$$

$$V_A(p) = V_A^0 + p^2 V_A^1. \quad (23)$$

Expressions for the momentum-independent components V_{τ}^0 and V_A^0 , along with those for V_{τ}^1 , V_{τ}^2 , and V_A^1 are given in the Appendix.

C. Energy and free energy of the system

We take recourse to a liquid-drop model for the evaluation of the total energy $E_A(\rho, T)$ of the fragments of mass A , charge Z , and neutron number N at a constant density ρ and temper-

ature T . The energy $E_A(\rho, T) [= -B_A(\rho, T)]$ is given by

$$E_A(\rho, T) = a_v(\rho, T)A + a_s(\rho, T)4\pi R_A^2 A^{2/3} + a_{\text{sym}}(\rho, T) \frac{(N-Z)^2}{A} + \frac{3}{5} Z^2 e^2 \left(\frac{1}{R_A} - \frac{1}{R_{WS}} \right). \quad (24)$$

The term a_v is the volume energy term for symmetric nuclear matter. Alongwith a_v , the surface energy coefficient a_s and the symmetry energy coefficient a_{sym} are all density and temperature dependent. The last term in Eq. (24) is the the Coulomb term. One may note that the Coulomb energy is different from that for an isolated nucleus. As the fragment is embedded in clusterized matter, its Coulomb energy gets 'dressed'. It is calculated in the Wigner-Seitz approximation [2]. Here R_{WS} is the radius of the spherical Wigner-Seitz cell, given as $R_{WS} = (\frac{4}{3}\pi\rho_A)^{-1/3}$. The Coulomb energy has no explicit temperature dependence. The radius R_A of the liquid drop is given by $R_A = A^{1/3}/[\frac{4}{3}\pi\rho(T)]^{1/3}$. In a similar vein to Eq. (24), the free energy of the nucleus is taken as

$$F_A(\rho, T) = f_v(\rho, T)A + f_s(\rho, T)4\pi R_A^2 A^{2/3} + f_{\text{sym}}(\rho, T) \frac{(N-Z)^2}{A} + \frac{3}{5} Z^2 e^2 \left(\frac{1}{R_A} - \frac{1}{R_{WS}} \right). \quad (25)$$

The volume terms a_v and f_v are calculated for symmetric nuclear matter at density ρ and at temperature T employing the SBM interaction. The density and temperature dependence of the surface free energy coefficient is assumed to be factorized [44] and is taken as

$$f_s(\rho, T) = a_s(\rho_0, T=0)\mathcal{U}(\rho)\mathcal{Y}(T), \quad (26)$$

where $a_s(\rho_0, T=0)$ is the surface energy coefficient at nuclear matter saturation density ρ_0 at $T=0$. The expressions for $\mathcal{U}(\rho)$ and $\mathcal{Y}(T)$ are taken from Refs. [45] and [2], respectively. They are given as

$$\mathcal{U}(\rho) = 1 - \frac{k_{\rho}}{2} \left(\frac{\rho - \rho_0}{\rho_0} \right)^2, \quad (27)$$

and

$$\mathcal{Y}(T) = \left(\frac{T_c^2 - T^2}{T_c^2 + T^2} \right)^{5/4}. \quad (28)$$

T_c is the critical temperature for nuclear matter, calculated to be 14.9 MeV with the SBM interaction. The value of $a_s(\rho_0, T=0)$ and k_{ρ} are taken to be 1.15 MeV fm⁻² and 5.0, respectively. The surface entropy per unit area $\mathcal{S}_{\text{surf}}$ is obtained from f_s as

$$\mathcal{S}_{\text{surf}} = - \frac{\partial f_s}{\partial T} \Big|_{\rho}, \quad (29)$$

which yields

$$\begin{aligned} a_s(\rho, T) &= f_s(\rho, T) + T S_{\text{surf}} \\ &= a_s(\rho_0, 0) \left[\mathcal{Y}(T) + 5 \left(\frac{T_c^2 - T^2}{T_c^2 + T^2} \right)^{1/4} \right. \\ &\quad \left. \times \frac{T_c^2 T^2}{(T_c^2 + T^2)^2} \right] \mathcal{U}(\rho). \end{aligned} \quad (30)$$

The symmetry coefficient a_{sym} is dependent on the nuclear mass. It is taken as [35]

$$a_{\text{sym}}(\rho = \rho_0, T = 0) = \frac{\alpha}{1 + \frac{\alpha}{\beta} A^{-1/3}}, \quad (31)$$

where α is the symmetry coefficient of cold symmetric nuclear matter taken as 31.0 MeV, and $\frac{\alpha}{\beta} = 2.4$. For infinite matter, it is generally seen that a_{sym} decreases with temperature whereas f_{sym} shows the opposite temperature dependence [46]. A nearly similar trend has been observed for finite nuclei [47]; here f_{sym} increases with temperature (though in some cases an occasional decrease is seen at low T). The density dependence of the symmetry energy of nuclear matter calculated with the SBM interaction is seen to be given by $\sim(\rho/\rho_0)^\gamma$ with $\gamma \sim 0.69$ [24], in consonance with the reported experimental behavior [20]. With this in mind, we write the symmetry free energy coefficient in a factorized form as

$$f_{\text{sym}}(\rho, T) = a_{\text{sym}}(\rho, T = 0)g(T), \quad (32)$$

where

$$a_{\text{sym}}(\rho, T = 0) = a_{\text{sym}}(\rho_0, T = 0)(\rho/\rho_0)^\gamma. \quad (33)$$

For $g(T)$, we assume a polynomial in T of the form

$$g(T) = (1 + v_1 T + v_2 T^2 + v_4 T^4). \quad (34)$$

Then,

$$S_{\text{sym}} = - \left. \frac{\partial f_{\text{sym}}}{\partial T} \right|_\rho, \quad (35)$$

and therefore

$$a_{\text{sym}}(\rho, T) = f_{\text{sym}}(\rho, T) - T \left. \frac{\partial f_{\text{sym}}(\rho, T)}{\partial T} \right|_\rho \quad (36)$$

$$= a_{\text{sym}}(\rho, T = 0)[1 - v_2 T^2 - 3v_4 T^4]. \quad (37)$$

In a schematic model [47], the observed T dependence of a_{sym} and f_{sym} has been seen to be moderately explained with values of v_1 , v_2 , and v_4 as -0.00848 , 0.00201 , and 0.0000147 , respectively, the dimensions of these quantities being in relevant inverse powers of MeV.

The internal entropy S_A^{int} of the fragments has contributions from the volume, surface, and the asymmetry. The latter two contributions have already been taken into account through Eqs. (29) and (35), respectively. Since the fragments are taken to have uniform density ρ , the volume entropy is calculated using the expression given in Eq. (15) for symmetric nuclear matter at temperature T and at a density ρ .

Combining the terms given by Eqs. (7)–(10), the total energy of the (n, p, A) system can then be written as

$$\begin{aligned} E &= V \left[\left\{ \sum_\tau \rho_\tau T J_{3/2}(\eta_\tau) / J_{1/2}(\eta_\tau) (1 - m_\tau^* V_\tau^*) + \frac{1}{2} \rho_\tau V_\tau^0 \right\} \right. \\ &\quad \left. + \rho_A T C_A (1 - m_A^* V_A^1) + \frac{1}{2} \rho_A V_A^0 - \rho_A B_A(\rho_l, T) \right]. \end{aligned} \quad (38)$$

We remind here that ρ_τ corresponds to the free nucleonic density after condensation. The total entropy of the free nucleonic matter is, from Eq. (15),

$$\sum_\tau S_\tau = V \sum_\tau \rho_\tau \left[\frac{5}{3} J_{3/2}(\eta_\tau) / J_{1/2}(\eta_\tau) - \eta_\tau \right]. \quad (39)$$

Similarly, the translational entropy from the fragments is

$$S_A^{\text{tr}} = N_A \left[\frac{5}{3} C_A - \eta_A \right], \quad (40)$$

where C_A is given by

$$C_A = J_{3/2}(\eta_A) / J_{1/2}(\eta_A), \quad (41)$$

or

$$C_A = B_{3/2}(\eta_A) / B_{1/2}(\eta_A), \quad (42)$$

depending on whether the fragments are fermionic or bosonic. In the above equations, the quantities J_k and B_k are the Fermi and Bose integrals; their definitions are given in Eq. (A4) in the Appendix. As the fragment densities are usually very low, $C_A \sim 3/2$. Since the internal entropy S_A^{int} of the fragments is now known as explained earlier, the free energy \mathcal{F} of the total AN matter can be calculated.

III. RESULTS AND DISCUSSIONS

In this paper, our primary aim is to investigate the changes in the properties of nuclei embedded in a hot medium of nucleons and other fragments produced in nuclear multifragmentation. To simplify the problem yet retain the main physics essence, we assume that after nuclear disassembly the system contains a collection of only one kind of fragments of mass A and charge Z in thermodynamic equilibrium, with a hot soup of neutrons and protons. To begin with, we take a baryon matter of given density ρ_b , at a temperature T with an isospin asymmetry X . The binding energies and the free energies of the nuclear fragments that enter into the calculation have been modeled in the context of the liquid-drop mass formula. For the effective interaction, the momentum and density dependent SBM force as described in Eqs. (1) and (2) has been chosen. Assumptions are made that the free nucleons do not penetrate the sharp-surface nuclei and that the fragments do not overlap.

The three unknowns in the calculation are the free nucleon densities ρ_n , ρ_p and the fragment densities ρ_A in the matter. The three constraints are the conservation of the total baryon number, the total isospin, and the condition of chemical equilibrium between the nucleon gas and the fragments. For a given set of ρ_b , T , and X , the calculations start with a chosen value of the density ρ_l of the constituent nucleons in the nuclear

fragments at temperature T and an input guess density of ρ_A . The energies and the free energies of the fragments are then known from Eqs. (24) and (25). Exploiting the constraints, the final densities ρ_A , ρ_n , and ρ_p are determined iteratively. The total free energy \mathcal{F} of the given AN matter [see Eqs. (6) and (14)] is then calculated as outlined earlier. Changing ρ_l gives different values of \mathcal{F} , whose minimum determines ρ_l at a given baryonic density ρ_b with asymmetry X at temperature T , which then, in the liquid-drop framework, determines all the properties under investigation of the produced fragments.

The calculations have been done in the temperature range 2.5–8 MeV for symmetric and asymmetric nuclear matter. Initially a symmetric matter ($X = 0.0$) of low baryon density $\rho_b = 0.005 \text{ fm}^{-3}$ is chosen, and the calculations are then repeated at a higher baryon density $\rho_b = 0.02 \text{ fm}^{-3}$. This helps to see how a denser medium accentuates changes in the nuclear properties. Three representative fragments are selected, namely, ^{40}Ca , ^{56}Fe , and a heavier one, ^{150}Sm . In Fig. 3, the percentage of nucleons in the fragments produced ($A\rho_A/\rho_b \times 100$) is shown as a function of temperature for the three fragment species. The left panels correspond to $\rho_b = 0.005 \text{ fm}^{-3}$ and the right panels refer to the higher baryon density $\rho_b = 0.02 \text{ fm}^{-3}$. The blue full line is obtained from calculations with inclusion of all three interaction contributions, namely, (NN), (AN), and (AA) [see

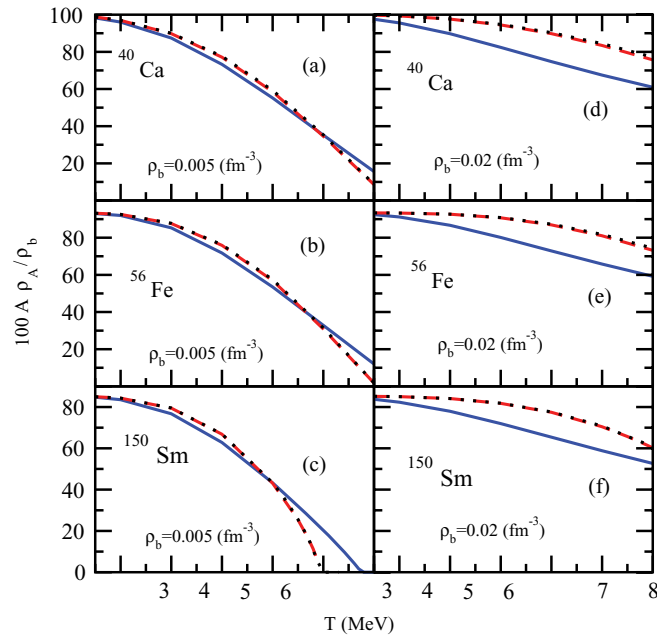


FIG. 3. (Color online) The percentage of nucleons contained in the fragments at a given baryon density ρ_b at $X = 0.0$ shown as a function of temperature after fragmentation. The left panels correspond to $\rho_b = 0.005 \text{ fm}^{-3}$, the right panels to $\rho_b = 0.02 \text{ fm}^{-3}$. The fragment specimens chosen are ^{40}Ca , ^{56}Fe , and ^{150}Sm , respectively. The blue full line corresponds to the case (1,1,1), i.e., the calculation where all three interactions NN , AN , and AA are included. The red dashed line refers to the case (1,0,1) where the AN contribution is neglected, whereas the black dotted line corresponds to the (1,0,0) calculation without both the AN and AA contributions. For details, see text.

Eqs. (7)–(10)]. We refer to these calculations as (1,1,1). The dashed red line corresponds to calculations without the (AN) contribution and the dotted black line is the one obtained when both (AN) and (AA) contributions are excluded. The latter two calculations are referred to as (1,0,1) and (1,0,0), respectively. At low temperatures, most of the nucleons are contained in the fragments and the free nucleons are rare. This is expected: vapor tends to condense to drops at low temperature. As temperature increases, the fragment formation probability decreases. Fragment formation also depends on the total baryon density ρ_b ; at the higher ρ_b , fragment formation probability is higher. As the system heats up, this probability goes down.

Examination of the figure reveals a few further features. The nucleus-nucleus interaction (AA) does not have a very significant role [as seen from the almost overlapping of the red dashed (1,0,1) and black dotted (1,0,0) lines], and the nucleon-nucleus interaction (AN) is important, the importance growing with increasing baryon density ρ_b . Normally, it is seen that the (1,0,1) or (1,0,0) calculations favor the production of fragments compared to a full (1,1,1) calculation. These results allow us to conclude that heavy nuclei embedded in the medium are affected mostly by the nucleons (and perhaps light clusters) surrounding them. This means that the description of the multicomponent nuclear system can be simplified by subdividing it into noninteracting cells containing one heavy nucleus and a proportional amount of the medium. This Wigner-Seitz approximation is widely used for studying inhomogeneous phases of nuclear matter [48–50].

In Fig. 4, the progressive changes in the internal nucleonic density in the three nuclei produced from disassembly of symmetric nuclear matter of density $\rho_b = 0.005 \text{ fm}^{-3}$ are displayed as a function of temperature in the three panels. The blue (full line), red (dashed), and the black (dotted) lines

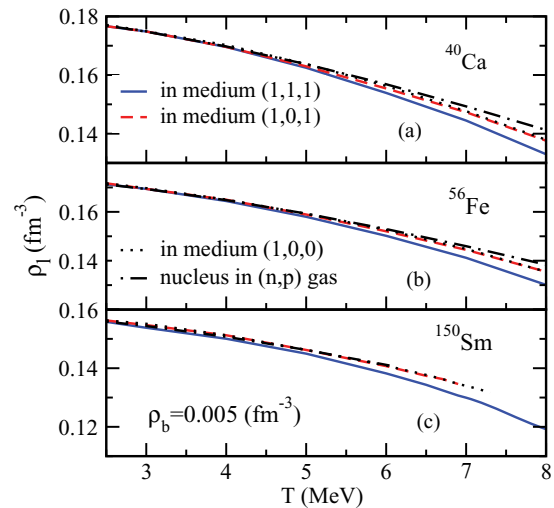


FIG. 4. (Color online) The nucleon number density in the fragments shown as a function of temperature, for baryon density $\rho_b = 0.005 \text{ fm}^{-3}$ at $X = 0.0$. The blue full line, red dashed line, and the black dotted line convey the same meaning as in Fig. 3. The dash-dotted (black) lines refer to the nuclear density when the nuclei (^{40}Ca , ^{56}Fe , or ^{150}Sm) are in phase equilibrium with their own vapor.

have the same meaning as stated earlier. The dash-dotted black line refers to calculations for isolated hot nuclei (^{40}Ca , ^{56}Fe , or ^{150}Sm) in phase equilibrium with their own vapor (n - p gas). In that case, the phase-equilibrium conditions [51] determine the density and asymmetry of the embedding nucleonic gas along with the internal density of the dipped nucleus. The dot-dashed black line is drawn so as to serve as a reference against which the other ones can be compared. In this case thermodynamic equilibrium ensures that the temperatures of the nucleus and the surrounding (n , p) gas are the same, that the pressure exerted by the nucleus balances that of the gas, and that the chemical potentials of the neutrons and protons of the nucleus are the same as those of the free neutrons and protons in the gas, respectively. Discussion of this part of the physics is left out here; it is given in detail in Refs. [51,52]. The densities of the embedding n - p gas in clusterized matter and in the case of an isolated hot nucleus are somewhat different. In both cases the density of the surrounding n - p gas is low at low temperatures and increases with increase in temperature. The asymmetry of this gas is also different in both cases. As an illustrative example, these properties of the embedding nucleonic gas are displayed in Fig. 5. The asymmetry of the disassembling system is $X = 0.2$ and the fragment concerned is ^{150}Sm . The asymmetry of the gas has a very insignificant role to play on the properties of the fragments, as will be shown later.

From Fig. 4, it transpires as expected that the fragment nuclei in equilibrium in an embedding medium expand with temperature in all four calculations displayed in this figure. In the reference calculation (black dash-dotted line), nuclei such as ^{40}Ca or ^{56}Fe bloat up in volume by $\sim 17\%$ – 19% from their ground-state equilibrium values when the temperature is raised

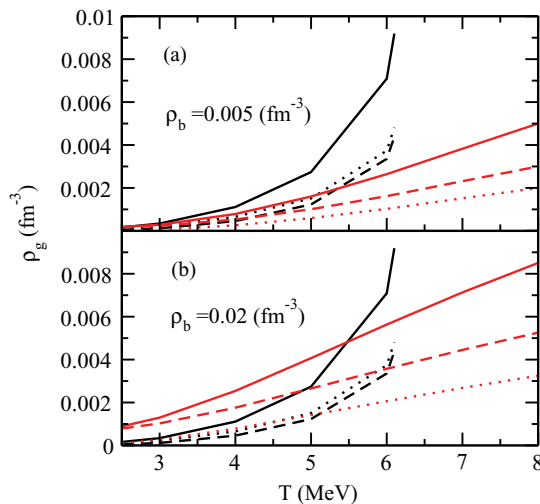


FIG. 5. (Color online) The embedding nucleon gas density plotted as a function of temperature in AN matter where A is ^{150}Sm . The panels (a) and (b) correspond to $\rho_b = 0.005 \text{ fm}^{-3}$ and 0.02 fm^{-3} , respectively. The red dotted, dashed, and full lines refer to proton and neutron densities and their sum in the calculation for disassembled matter at asymmetry $X = 0.2$. The black dotted, dashed, and full lines correspond to proton and neutron densities and their sum in the phase-equilibrium calculation for ^{150}Sm .

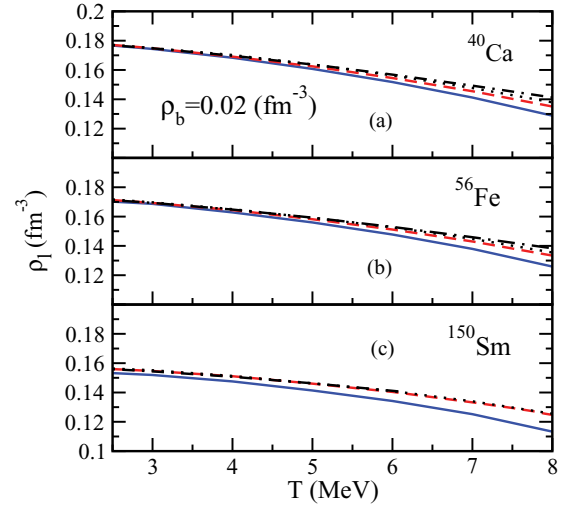


FIG. 6. (Color online) Same as in Fig. 4 when $\rho_b = 0.02 \text{ fm}^{-3}$.

to ~ 7 – 8 MeV. In the full (1,1,1) fragmentation calculation for nuclear matter at $\rho_b = 0.005 \text{ fm}^{-3}$ they do so by $\sim 25\%$. As is seen from the figure, incorporation of the nucleon-fragment (AN) interaction plays a significant role in the expansion of the fragments; also it is seen, as stated earlier, that the fragment-fragment interaction (AA) has little effect. In panel (c) of Fig. 4, it is noticed that the black dash-dotted line does not extend beyond 6.1 MeV. This is the limiting temperature as obtained for ^{150}Sm in the phase equilibrium calculation. Solutions for calculations without incorporation of both AN and AA (1,0,0) interactions and for calculations without AN interactions (1,0,1) could not be obtained for this nucleus beyond 7.2 and 6.9 MeV, respectively. This absence of solutions possibly points to the nuclear instability beyond these temperatures in these calculations. When the baryon density ρ_b is increased, the nuclear soup of fragments and nucleons becomes denser. In this denser environment, a further expansion of the fragments by another $\sim 4\%$ could be noticed. This is displayed in Fig. 6 where $\rho_b = 0.02 \text{ fm}^{-3}$. The (1,0,1) and (1,0,0) calculations for ^{150}Sm could now be extended to 8.0 MeV.

As the internal densities of the nuclei change progressively with temperature from those obtained from the reference calculation as mentioned earlier, it is expected that there should be a corresponding change in the binding energies and free energies of the nuclei embedded in medium. We display those quantities for ^{40}Ca in Fig. 7. The left panels (a) and (b) show the results for the lower baryon density $\rho_b = 0.005 \text{ fm}^{-3}$, and the right panels (c) and (d) do so for $\rho_b = 0.02 \text{ fm}^{-3}$, both at $X = 0.0$. The upper panels display the binding energy, the lower panels the free energy. The (1,0,0) calculations, being nearly indistinguishable from the (1,0,1) calculations, are not shown here. The results for the binding energies from the (1,1,1) and (1,0,1) calculations at the lower baryon density are nearly indistinguishable from each other; at the higher baryon density ($\rho_b = 0.02 \text{ fm}^{-3}$) only little changes are observed at the high temperatures. Compared to the reference calculation (dash-dotted black line representing phase equilibrium in a n - p gas), there is a gain in the binding energy. This comes mostly from the decrease of the Coulomb energy because of the

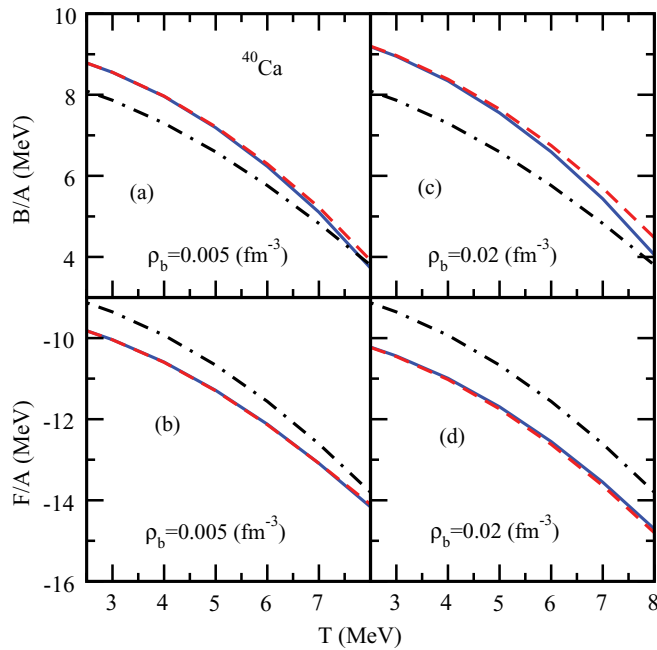


FIG. 7. (Color online) The binding energy and free energy of ^{40}Ca , produced in fragmentation of symmetric nuclear matter. The left panels refer to $\rho_b = 0.005 \text{ fm}^{-3}$, the right panels correspond to $\rho_b = 0.02 \text{ fm}^{-3}$. The full (blue), dashed (red), and the dash-dotted (black) lines have the same meaning as in Fig. 4.

presence of other fragments [see Eq. (24)]. At higher baryon density, the fragment density is comparatively higher, which explains the larger gap in binding energy with reference to the phase equilibrium calculation. For a given baryon density the reduction in the density of the fragments with temperature reduces the gap. Similar arguments follow for the lower free energy of the embedded fragments as compared to that from the reference calculation. Not much of a difference is seen for the heavier nucleus ^{150}Sm as displayed in Fig. 8.

In order to see the importance of asymmetry on the fragment observables, the calculations have been repeated for asymmetric nuclear matter with $X = 0.2$. In Fig. 9, comparisons of the percentage of nucleons contained in the fragments are made for symmetric and asymmetric nuclear matter at the two baryon densities we have considered for the three fragment species. We display only the full calculations (1,1,1). The blue full lines correspond to $X = 0.0$, and the blue dotted lines refer to $X = 0.2$. ^{40}Ca and ^{56}Fe , being symmetric and nearly symmetric nuclei, respectively, have comparatively larger populations in symmetric nuclear matter. For the more asymmetric ^{150}Sm nucleus, population is larger in the asymmetric matter. The difference between the two calculations at the two asymmetries is more pronounced at lower temperatures, gradually narrowing down as the temperature is raised. The internal nucleon densities of the fragments and their binding energies, however, show no significant change when the isospin asymmetry of the matter changes. This is displayed in Figs. 10 and 11, respectively, for the three nuclear fragments at the two baryon densities; the blue full and dotted lines nearly overlap each other over the whole temperature range in which we work.

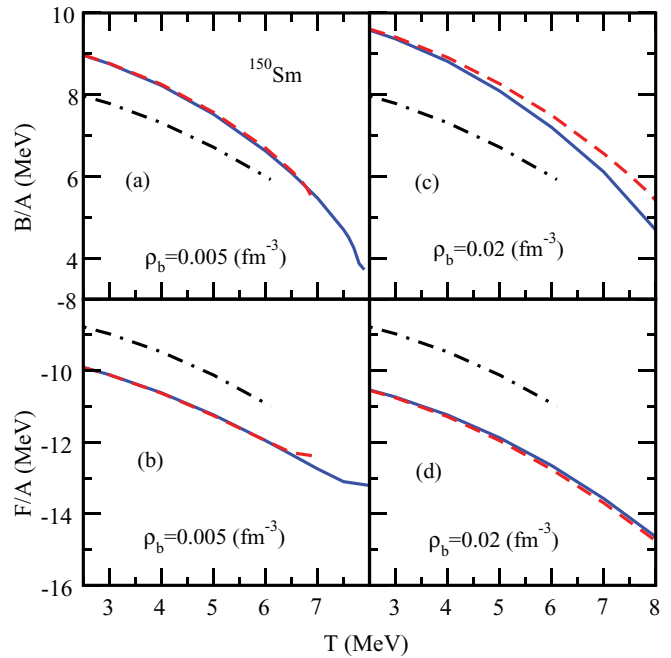


FIG. 8. (Color online) Same as in Fig. 7 for ^{150}Sm .

IV. CONCLUDING REMARKS

Analysis of nuclear multifragmentation data showed that, for the results calculated in thermodynamic models to conform to the experimentally observed ones, the established nuclear parameters taken as inputs in these calculations needed subtle changes [21,22,25,26]. Such a fact points out that the properties of the fragments produced in nuclear disassembly

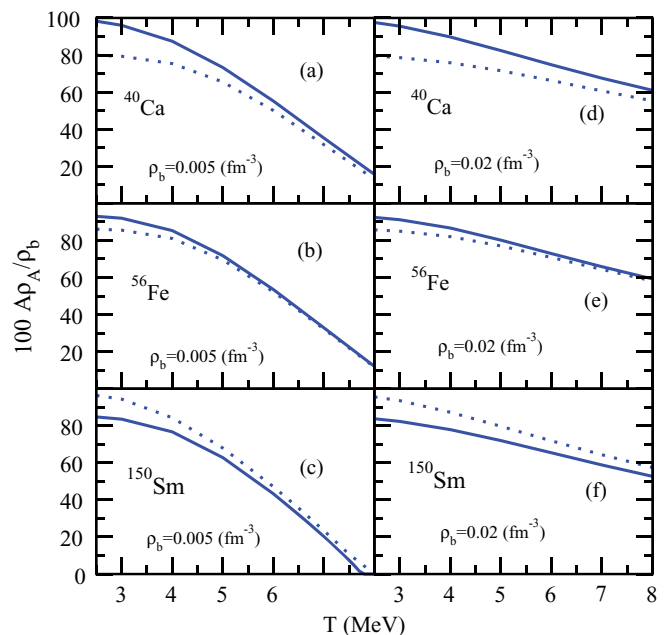


FIG. 9. (Color online) Comparison of fragment population in symmetric and asymmetric nuclear matter for the case (1,1,1) calculated for two baryon densities. The full and dotted lines correspond to $X = 0.0$ and $X = 0.2$, respectively.

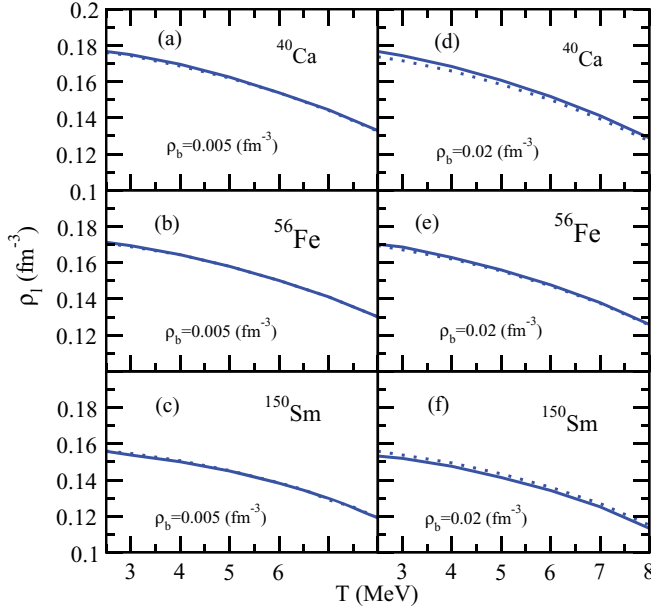


FIG. 10. (Color online) Comparison of the internal nucleon densities of the fragments produced in symmetric and asymmetric ($X = 0.2$) nuclear matter calculated for two baryon densities. The full and dotted lines have the same meaning as in Fig. 9.

might have been modified because of the interaction of the fragments with the embedding environment in which they are created. The calculations presented in this paper throw light in a quantitative manner on how significant these modifications can be. For simplicity, the fragmented system was assumed to contain a collection of only one kind of

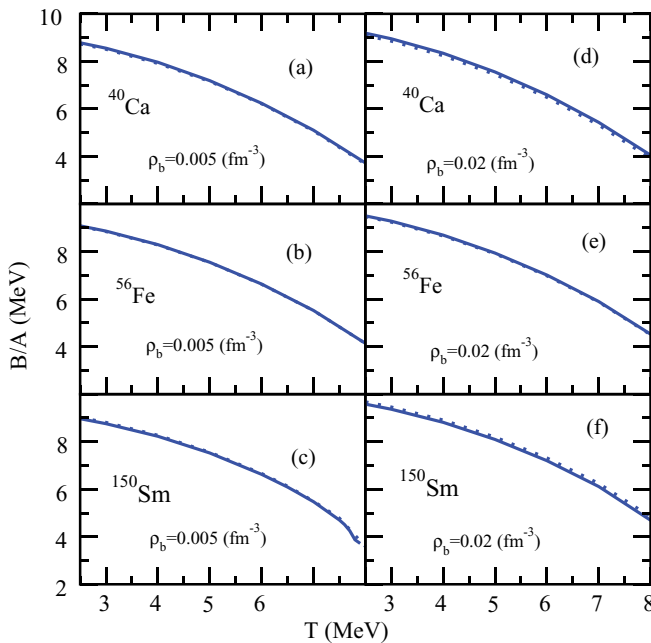


FIG. 11. (Color online) Comparison of the binding energies of the fragments produced in symmetric and asymmetric ($X = 0.2$) nuclear matter calculated for two baryon densities. The full and dotted lines have the same meaning as in Fig. 9.

nuclear species in addition to neutrons and protons. For comparison, a benchmark calculation of the hot fragments in phase equilibrium with its own vapor was also done. In both cases, it was seen that the fragments expand with temperature as expected, but compared to the results from the phase-equilibrium (benchmark) calculation, the embedding medium in multifragmentation produced larger changes in the fragment properties. The fragments get comparably more stretched; the volume energy, surface properties, or the symmetry properties of the fragments undergo the consequential changes.

Questions may arise on the justification of the choice of only one kind of species in the calculations. Close examination of the results shows that, in the medium, the interaction of the nucleons with the fragments plays the dominant role in bringing forth the modification in the fragment properties. The fragment-fragment interaction has a very nominal role. The selection of the multispecies in the medium thus may not alter the results much.

Experiments with intermediate energy heavy ion beams in the last few decades have indicated [53] that nuclei can sustain only temperatures that are much lower than the critical temperature (~ 16 MeV) for symmetric nuclear matter. The origin of such a limiting temperature is usually traced to an interplay between the Coulomb instability and the corrections due to the finite size of the nuclear drops. Phase-equilibrium calculations for hot isolated nuclei surrounded by their own vapor yield limiting temperatures $\sim 5-7$ MeV for heavier nuclei [51,52,54]. In the calculations presented in this paper, it is seen that, for nuclei dripped in a nuclear soup, the interaction with the surrounding medium might overcome the said instability to a certain extent and extend somewhat the limit of temperature that the nuclei may hold. This might be of significant relevance in the context of nuclear astrophysics and needs further exploration.

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APPENDIX

From Eqs. (11) and (18), the density of the free nucleons ρ_τ is found to be

$$\rho_\tau = \frac{4\pi}{h^3} (2m_\tau^* T)^{3/2} J_{1/2}(\eta_\tau). \quad (\text{A1})$$

Similarly, from Eqs. (12) and (19), the fragment density ρ_A comes out as

$$\rho_A = \frac{4\pi}{h^3} (2m_A^* T)^{3/2} J_{1/2}(\eta_A), \quad (\text{A2})$$

or

$$\rho_A = \frac{2\pi}{h^3} (2m_A^* T)^{3/2} B_{1/2}(\eta_A), \quad (\text{A3})$$

depending on whether the fragments are fermions or bosons. The $J_k(\eta)$ and $B_k(\eta)$ are the Fermi and Bose integrals,

$$J_k(\eta) = \int_0^\infty \frac{x^k dx}{e^{(x-\eta)} + 1}, \quad (\text{A4})$$

$$B_k(\eta) = \int_0^\infty \frac{x^k dx}{e^{(x-\eta)} - 1}.$$

The expression for V_τ^0 in Eq. (22) is given as

$$V_\tau^0 = -4\pi a^3 \{1 - d^2(2\rho_N)^\kappa\} (C_l \rho_\tau + C_u \rho_{-\tau}) + \frac{16\pi^2 a^3}{b^2 h^3} \left[C_l (2m_\tau^* T)^{5/2} J_{3/2}(\eta_\tau) + C_u (2m_{-\tau}^* T)^{5/2} \right. \\ \left. \times J_{3/2}(\eta_{-\tau}) \right] + \frac{1}{2} I \rho_A \left\{ \left(\frac{\langle p_A^2 \rangle}{b^2} - 1 \right) (C_l \rho_{l\tau} + C_u \rho_{l-\tau}) + \frac{4\pi}{h^3 b^2} [C_l (2m_{l\tau}^{A*} T)^{5/2} J_{3/2}(\eta_{l\tau}^A) + C_u (2m_{l-\tau}^{A*} T)^{5/2} \right. \right. \\ \left. \left. \times J_{3/2}(\eta_{l-\tau}^A)] + (C_l \rho_{l\tau} + C_u \rho_{l-\tau}) d^2 [\rho_N + \rho_l]^\kappa \right\}. \quad (\text{A5})$$

In this equation, the fugacity $\eta_{l\tau}^A$ is defined corresponding to the nucleons of density $\rho_{l\tau}$ inside the fragment (exactly in parallel with the definition of the fugacity η_τ of the free nucleons corresponding to the free nucleon density ρ_τ); $m_{l\tau}^{A*}$ is the effective mass of these nucleons.

Similarly, expressions for V_τ^1 , V_τ^2 , V_A^0 , and V_A^1 are

$$V_\tau^1 = \frac{4\pi a^3}{b^2} [C_l \rho_\tau + C_u \rho_{-\tau}] + \frac{1}{4} I (C_l + C_u) \frac{\rho_A \rho_l}{b^2}, \quad (\text{A6})$$

$$V_\tau^2 = 4\pi a^3 \kappa d^2 (2\rho_N)^{\kappa-1} \sum_{\tau'} [C_l \rho_{\tau'} + C_u \rho_{-\tau'}] \rho_{\tau'} + \frac{1}{2} I \rho_A \rho_N (C_l \rho_{l\tau} + C_u \rho_{l-\tau}) [\kappa d^2 (\rho_N + \rho_l)^{\kappa-1}], \quad (\text{A7})$$

$$V_A^0 = \frac{1}{2} I \sum_\tau \rho_\tau \left[(C_l \rho_{l\tau} + C_u \rho_{l-\tau}) \left\{ -1 + \frac{4\pi}{h^3} \frac{(2m_\tau^* T)^{5/2}}{b^2 \rho_\tau} \times J_{3/2}(\eta_\tau) + d^2 \{\rho_N + \rho_l\}^\kappa \right\} + \frac{4\pi}{b^2 h^3} \left\{ C_l (2m_{l\tau}^{A*} T)^{5/2} J_{3/2}(\eta_{l\tau}^A) \right. \right. \\ \left. \left. + C_u (2m_{l-\tau}^{A*} T)^{5/2} J_{3/2}(\eta_{l-\tau}^A) \right\} \right] + I_A \rho_A \sum_\tau \rho_{l\tau} \left\{ C_l \rho_{l\tau} \left(-1 + \frac{\langle p_A^2 \rangle}{b^2} + \frac{8\pi}{b^2 h^3} \frac{(2m_{l\tau}^{A*} T)^{5/2}}{\rho_{l\tau}} J_{3/2}(\eta_{l\tau}^A) \right) \right. \\ \left. + C_u \rho_{l-\tau} \left(-1 + \frac{\langle p_A^2 \rangle}{b^2} + \frac{4\pi}{b^2 h^3} \frac{(2m_{l\tau}^{A*} T)^{5/2}}{\rho_{l\tau}} J_{3/2}(\eta_{l\tau}^A) + \frac{4\pi}{b^2 h^3} \frac{(2m_{l-\tau}^{A*} T)^{5/2}}{\rho_{l-\tau}} J_{3/2}(\eta_{l-\tau}^A) \right) \right\} \\ \left. + I_A \rho_A d^2 \left[\sum_\tau \rho_{l\tau} (C_l \rho_{l\tau} + C_u \rho_{l-\tau}) \right] (2\rho_l)^\kappa, \quad (\text{A8})$$

$$V_A^1 = \sum_\tau (C_l \rho_{l\tau} + C_u \rho_{l-\tau}) \left(\frac{I_A \rho_A}{b^2} \rho_{l\tau} + \frac{I}{2b^2} \rho_\tau \right). \quad (\text{A9})$$

In Eqs. (A5)–(A8), $\langle p_A^2 \rangle$ is the mean-squared value of the fragment momentum in AN matter. Its value is given by

$$\langle p_A^2 \rangle = (2m_A^* T) C_A, \quad (\text{A10})$$

where C_A is given by Eqs. (41) or (42). The integrals I and I_A appearing in Eq. (A5)–(A9) for nucleon-nucleus and nucleus-nucleus interactions are given by

$$I = \int_{V_A} d\mathbf{r} \int d\mathbf{R} \frac{e^{-|\mathbf{r}+\mathbf{R}|/a}}{|\mathbf{r}+\mathbf{R}|/a}, \quad (\text{A11})$$

$$I_A = \int_{V_A} d\mathbf{r} \int_{V_A} d\mathbf{r}' \int d\mathbf{R} \frac{e^{-|\mathbf{R}+\mathbf{r}-\mathbf{r}'|/a}}{|\mathbf{R}+\mathbf{r}-\mathbf{r}'|/a}. \quad (\text{A12})$$

Integrations on \mathbf{R} exclude the fragment volumes. The integrals are evaluated numerically.

- [1] J. P. Bondorf, R. Donangelo, I. N. Mishustin, C. J. Pethick, H. Schultz, and K. Sneppen, *Nucl. Phys. A* **443**, 321 (1985).
- [2] J. P. Bondorf, A. S. Botvina, A. S. Iljinov, I. N. Mishustin, and K. Sneppen, *Phys. Rep.* **257**, 133 (1995).
- [3] D. H. E. Gross, *Rep. Prog. Phys.* **53**, 605 (1990).
- [4] Subrata Pal, S. K. Samaddar, A. Das, and J. N. De, *Phys. Lett. B* **337**, 14 (1994).
- [5] J. N. De, S. K. Samaddar, X. Vinas, and M. Centelles, *Phys. Lett. B* **638**, 160 (2006).
- [6] J. Pan and S. D. Gupta, *Phys. Rev. C* **51**, 1384 (1995).
- [7] H. Müller and B. D. Serot, *Phys. Rev. C* **52**, 2072 (1995).
- [8] T. Sil, S. K. Samaddar, J. N. De, and S. Shlomo, *Phys. Rev. C* **69**, 014602 (2004).
- [9] B. S. Meyers, *Annu. Rev. Astron. Astrophys.* **32**, 153 (1994).
- [10] C. J. Horowitz and A. Schwenk, *Nucl. Phys. A* **776**, 55 (2006).
- [11] J. N. De and S. K. Samaddar, *Phys. Rev. C* **78**, 065204 (2008).
- [12] G. Shen, C. J. Horowitz, and S. Teige, *Phys. Rev. C* **82**, 045802 (2010).
- [13] C. Ishizuka, A. Ohnishi, and K. Sumiyoshi, *Nucl. Phys. A* **723**, 517 (2003).
- [14] A. S. Botvina and I. N. Mishustin, *Phys. Lett. B* **584**, 233 (2004).
- [15] A. S. Botvina and I. N. Mishustin, *Nucl. Phys. A* **843**, 98 (2010).
- [16] M. Hempel and J. Schaffner-Bielich, *Nucl. Phys. A* **837**, 210 (2010).
- [17] S. Furusawa, S. Yamada, K. Sumiyoshi, and H. Suzuki, *Astrophys. J.* **738**, 178 (2011).
- [18] A. Le Fevre *et al.*, *Phys. Rev. Lett.* **94**, 162701 (2005).
- [19] J. Iglieo *et al.*, *Phys. Rev. C* **74**, 024605 (2006).
- [20] D. V. Shetty, S. J. Yennello, and G. A. Souliotis, *Phys. Rev. C* **76**, 024606 (2007).
- [21] G. A. Souliotis, A. S. Botvina, D. V. Shetty, A. L. Keksis, M. Jandel, M. Veselsky, and S. J. Yennello, *Phys. Rev. C* **75**, 011601(R) (2007).
- [22] R. Ogul *et al.*, *Phys. Rev. C* **83**, 024608 (2011); **85**, 019903 (2012).
- [23] A. Ono, P. Danielewicz, W. A. Friedman, W. G. Lynch, and M. B. Tsang, *Phys. Rev. C* **68**, 051601 (2003).
- [24] S. K. Samaddar, J. N. De, X. Viñas, and M. Centelles, *Phys. Rev. C* **76**, 041602(R) (2007).
- [25] A. S. Botvina, N. Buyukcizmeci, M. Erdogan, J. Lukasik, I. N. Mishustin, R. Ogul, and W. Trautmann, *Phys. Rev. C* **74**, 044609 (2006).
- [26] N. Buyukcizmeci, A. S. Botvina, I. N. Mishustin, and R. Ogul, *Phys. Rev. C* **77**, 034608 (2008).
- [27] S. Typel, G. Röpke, T. Klähn, D. Blaschke, and H. H. Wolter, *Phys. Rev. C* **81**, 015803 (2010).
- [28] M. D. Voskresenskya and S. Typel, *Nucl. Phys. A* **887**, 42 (2012).
- [29] J. B. Natowitz *et al.*, *Phys. Rev. Lett.* **104**, 202501 (2010).
- [30] K. Hagel *et al.*, *Phys. Rev. Lett.* **108**, 062702 (2012).
- [31] W. D. Myers and W. J. Swiatecki, *Ann. Phys. (N.Y.)* **204**, 401 (1990).
- [32] J. N. De, N. Rudra, Subrata Pal, and S. K. Samaddar, *Phys. Rev. C* **53**, 780 (1996).
- [33] D. Bandyopadhyay, C. Samanta, S. K. Samaddar, and J. N. De, *Nucl. Phys. A* **511**, 1 (1990).
- [34] D. V. Shetty, S. J. Yennello, and G. A. Souliotis, *Phys. Rev. C* **75**, 034602 (2007).
- [35] P. Danielewicz, *Nucl. Phys. A* **727**, 233 (2003).
- [36] L. W. Chen, C. M. Ko, B. A. Li, and J. Xu, *Phys. Rev. C* **82**, 024321 (2010).
- [37] M. Warda, X. Viñas, X. Roca-Maza, and M. Centelles, *Phys. Rev. C* **80**, 024316 (2009).
- [38] X. Roca-Maza, M. Centelles, X. Viñas, and M. Warda, *Phys. Rev. Lett.* **106**, 252501 (2011).
- [39] L. W. Chen and J. Z. Gu, *J. Phys. G* **39**, 035104 (2012).
- [40] J. Dong, W. Zuo, J. Gu, and U. Lombardo, *Phys. Rev. C* **85**, 034308 (2012).
- [41] J. N. De and S. K. Samaddar, *Phys. Rev. C* **76**, 044607 (2007).
- [42] G. Shen, C. J. Horowitz, and S. Teige, *Phys. Rev. C* **83**, 035802 (2011).
- [43] S. K. Samaddar and J. N. De, *Phys. Rev. C* **83**, 055802 (2011).
- [44] D. G. Ravenhall, C. J. Pethick, and J. M. Lattimer, *Nucl. Phys. A* **407**, 571 (1983).
- [45] J. P. Blaizot, *Phys. Rep.* **64**, 171 (1980).
- [46] J. Xu, L.-W. Chen, B.-A. Li, and H.-R. Ma, *Phys. Rev. C* **75**, 014607 (2007).
- [47] J. N. De and S. K. Samaddar, *Phys. Rev. C* **85**, 024310 (2012).
- [48] P. Bonche and D. Vautherin, *Nucl. Phys. A* **372**, 496 (1981).
- [49] J. M. Lattimer, C. J. Pethick, D. G. Ravenhall, and D. Q. Lamb, *Nucl. Phys. A* **432**, 646 (1985).
- [50] Toshiki Maruyama, Toshitaka Tatsumi, Dmitri N. Voskresensky, Tomonori Tanigawa, and Satoshi Chiba, *Phys. Rev. C* **72**, 015802 (2005).
- [51] D. Bandyopadhyay, J. N. De, S. K. Samaddar, and D. Sperber, *Phys. Lett. B* **218**, 391 (1989).
- [52] S. Levit and P. Bonche, *Nucl. Phys. A* **437**, 426 (1985).
- [53] G. Auger *et al.*, *Phys. Lett. B* **169**, 161 (1986).
- [54] E. Suraud, *Nucl. Phys. A* **462**, 109 (1987).