



# Deterministic coupling of quantum emitters in WSe<sub>2</sub> monolayers to plasmonic nanocavities

OLIVER IFF,<sup>1</sup> NILS LUNDT,<sup>1</sup> SIMON BETZOLD,<sup>1</sup> LAXMI NARAYAN TRIPATHI,<sup>1,2</sup> MONIKA EMMERLING,<sup>1</sup> SEFAATTIN TONGAY,<sup>3</sup> YOUNG JIN LEE,<sup>4</sup> SOON-HONG KWON,<sup>4</sup> SVEN HÖFLING,<sup>1,5</sup> AND CHRISTIAN SCHNEIDER<sup>1,\*</sup>

<sup>1</sup>*Technische Physik and Wilhelm Conrad Röntgen Research Center for Complex Material Systems, Physikalisches Institut, Universität Würzburg, Am Hubland, D-97074 Würzburg, Germany*

<sup>2</sup>*Present Address: Department of Physics, Birla Institute of Technology, Mesra, Ranchi 835215, Jharkhand, India*

<sup>3</sup>*School for Engineering for Matter, Transport, and Energy, Arizona State University, Tempe, Arizona 85287, USA*

<sup>4</sup>*Department of Physics, Chung-Ang University, Seoul, South Korea*

<sup>5</sup>*SUPA, School of Physics and Astronomy, University of St. Andrews, St. Andrews, KY16 9SS, UK*

\**christian.schneider@physik.uni-wuerzburg.de*

**Abstract:** We discuss coupling of site-selectively induced quantum emitters in exfoliated monolayers of WSe<sub>2</sub> to plasmonic nanostructures. Gold nanorods of 20 nm–240 nm size, which are arranged in pitches of a few micrometers on a dielectric surface, act as seeds for the formation of quantum emitters in the atomically thin materials. We observe characteristic narrow-band emission signals from the monolayers, which correspond well with the positions of the metallic nanopillars with and without thin dielectric coating. Single photon emission from the emitters is confirmed by autocorrelation measurements, yielding  $g^2(\tau = 0)$  values as low as 0.17. Moreover, we observe a strong co-polarization of our single photon emitters with the frequency matched plasmonic resonances, as a consequence of light-matter coupling. Our work represents a significant step towards the scalable implementation of coupled quantum emitter-resonator systems for highly integrated quantum photonic and plasmonic applications.

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## 1. Introduction

Engineering solid state quantum emitters and their integration in micro- and nanophotonic structures is one of the prime tasks in modern quantum engineering. Coupled solid state quantum emitter-cavity systems range among the most promising candidates for the realization of highly efficient single photon sources [1–5], spin photon interfaces [6, 7], quantum sensing probes [8] as well as building blocks for quantum simulation [9] and surface code quantum computing [10]. While quantum emitters have been identified, studied and engineered in a variety of crystals including III-V [11] and II-VI quantum dots [12–14], color defects in diamonds [15], impurities in SiC and organic polymers [16, 17], atomically thin materials [18–22] were recently established as a novel platform of quantum photonic devices. Quantum dots in III-V semiconductors [23] and defect centers in diamonds [24] certainly belong to the most mature implementations, but the quality of site-controlled emitters still needs to be improved, putting a serious thread regarding their scalable fabrication in ordered arrays. Ordered InAs/GaAs quantum dot arrays have been realized by selective area growth methods and epitaxial growth on patterned substrates [26], but in most cases the costly fabrication methods severely compromised their emission properties. Direct integration of positioned solid state quantum emitters with photonic resonators has been accomplished [27–29], but only in few selected cases, and genuine scalability has remained elusive.

The formation of quantum emitters in mono- and bilayers of transition metal dichalcogenides has now been studied in various implementations: initially, localized luminescence centers in exfoliated flakes were discovered close to their edges, and have been associated with strain wrinkles [20–22]. In epitaxially grown flakes, random positioning of such spots was observed [18], indicating emission from defect bound excitons. Recently, the formation of quantum emitters on modulated metal substrates [30, 31], as well as nanopillars [32, 33] was reported and associated with localized and engineered crystal strain fields, which outlines the unique possibility to deterministically induce quantum emitters in a straight forward manner by structuring the sample surface prior to the transfer of the monolayer.

While the ordered formation of quantum emitters thus far has been mainly observed on dielectric, nanostructured surfaces, spontaneous emission enhancement was reported on rough metallic surfaces and gold-coated nanopillars, giving rise to localized plasmonic modes [31]. Combining atomically thin materials which comprise either tightly localized excitons or strongly bound free excitons with nanoplasmonic cavities yields a promising pathway to study light-matter coupling on the nanoscale enabled by the enormous field enhancements provided by metallic nanostructures [34–38].

## 2. Sample structure and setup

In this work, we demonstrate the feasibility to induce ordered arrays of quantum emitters by defined arrays of metallic nanopillars, fabricated on a SiO<sub>2</sub> substrate. Such structures directly represent a coupled quantum dot-nanocavity system, and act as polarization-controlled single photon sources.

The sample consists of a semi-insulating silicon substrate, with a 200 nm thick SiO<sub>2</sub> layer on top. In order to fabricate the nanopillars, we first spin-coated a thin layer of PMMA and performed electron beam lithography to selectively expose rectangular areas in the resist with dimensions of 20 nm - 240 nm. After developing the resist, a 80 nm thick gold layer was evaporated on the sample, followed by a lift-off step. A scanning electron microscope (SEM) image of a prototype nanopillar array with a pitch of 2 μm is shown in Fig. 1(a). On selected samples we additionally deposited a 5 nm thin layer of Al<sub>2</sub>O<sub>3</sub> via atomic layer deposition. Next, we fabricated atomically thin layers of WSe<sub>2</sub> via mechanical exfoliation using adhesive tape, and transferred the layers on the pillar arrays via dry transfer [39] (Fig. 1(b)). We observe, that part of the pillars pierced the monolayer, while a substantial number of nanopillars (> 50 %) locally strained the layer, yielding the tent-like structure shown in Fig. 1(c).

Spatially resolved optical spectroscopy was performed in a micro-photoluminescence (μPL) setup with a high spatial resolution (≈ 0.5 μm using fiber based confocal setting). The sample is excited by a frequency-doubled Nd:YAG laser at 532 nm, mounted in a liquid helium cooled flow cryostat. A direct comparison of the PL of different pillars with and without Al<sub>2</sub>O<sub>3</sub> is presented in Fig. 1(d), which shows no significant quenching or change in intensity in the absence of the thin oxide layer.

## 3. Experimental results and discussion

Figure 2(a) depicts an exemplaric series of power dependent luminescence spectra recorded on the position of a nanopillar with dielectric coating. The spectrum is widely dominated by a zoo of sharp emission lines, a typical signature of strongly localized emission centers in the crystal. In Fig. 2(b) we plot the excitation power ( $P_{exc}$ ) dependent PL intensity  $I$  of such an emitter, while fitting it with the simple two-level approximation  $I = I_{sat} / (1 + P_n / P_{exc})$ . Here,  $I_{sat}$  is the saturation intensity and  $P_n$  is a free fit parameter to normalize the power. The observed saturation at moderate pump powers is a signature of an intrinsic blocking mechanism, provided by the finite lifetime of a localized two-level system.

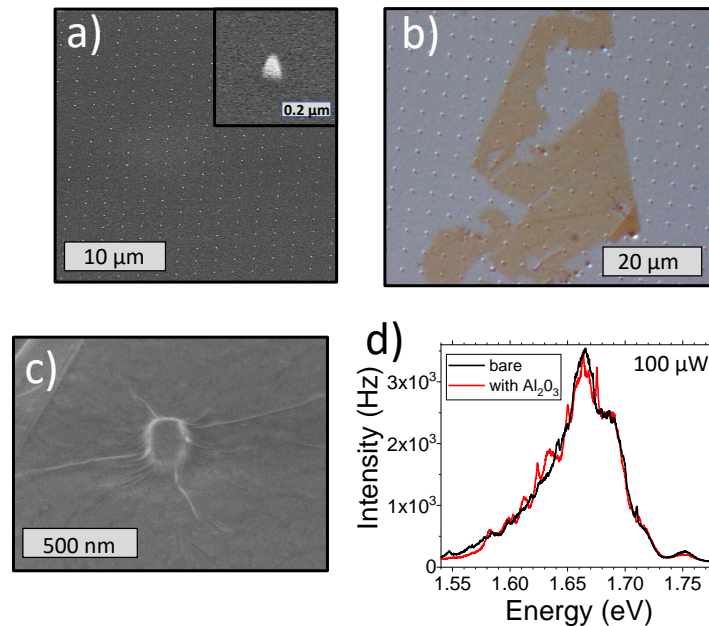


Fig. 1. a) Scanning electron microscope (SEM) image of the sample surface comprising metallic nanopillars as quantum emitter seeds and plasmonic nano-cavities. Inset: close-up view of a nanopillar. b) Optical image of the pillar array after successful dry-transfer of an atomically thin WSe<sub>2</sub> monolayer. c) Close-up SEM image of a single pillar covered by a strained monolayer, showing the formation of wrinkles. d) Comparison of the photoluminescence of pillars covered by WSe<sub>2</sub> with and without Al<sub>2</sub>O<sub>3</sub> coating at 100 μW. No significant influence or quenching is observed.

The ordered formation of emitters on the nanopillar arrays is confirmed in a highly spatially resolved scanning ( $\mu$ PL) study, applying the confocal configuration: Here, we carefully scan the sample's surface by utilizing a pair of motorized linear stages with a step width of 500 nm underneath the excitation and collection spot. The spectrally integrated map (700 nm-800 nm) is shown in Fig. 2(c). It clearly evidences a regular pattern of bright emission sites, perfectly coinciding with the positions of the metallic pillars with a pitch of 4 μm (dashed black pattern). Spectral information is best illustrated in a selected linescan between the blue arrows in Fig. 2(c). Here, we clearly observe a two-fold effect by the nanopillars (Fig. 2(d)): A strong luminescence enhancement of up to 100% occurring at the positions of the nano-pillars compared to off-pillar, signifies a resonant optical coupling to a plasmonic resonance [40], as well as the regular formation of the sharp peaks below the free exciton energy ( $<1.74$  eV), which we associate with tight exciton localization due to strain.

In order to provide evidence for the capability to emit single photons from the deterministically localized excitons, we performed second order correlation measurements by exciting the sample with a 532 nm CW laser (Fig. 3(a)). We selected a dominant emission feature from one square pillar (140 nm  $\times$  140 nm). The luminescence was spectrally filtered (selected bandwidth:  $\approx 1$  meV, 300 grooves/mm grating) and passed to a fiber coupled Hanbury Brown and Twiss (HBT) setup. We observed a well-pronounced anti-bunching signal at zero delay time ( $\tau = 0$ ), allowing us to extract a  $g^{(2)}(\tau = 0)$  value of  $0.17 \pm 0.15$ , which clearly puts our system in the regime of single photon emission.

Polarization resolved spectroscopy on different nanopillars revealed a strongly linear polar-

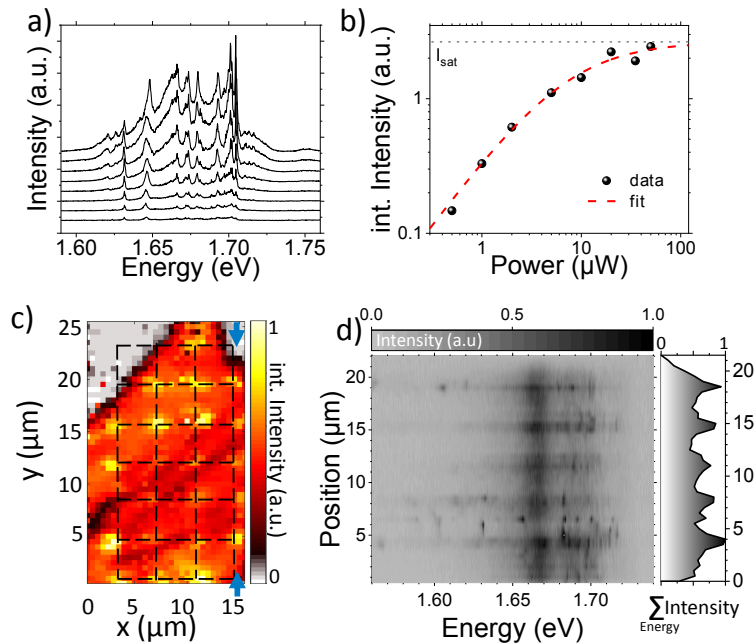


Fig. 2. a) Power-dependent spectra on a nanopillar revealing many discrete emitters. b) Power-dependent study of a quantum emitter emission line before saturation starts above  $10 \mu\text{W}$ . c) Spatial map of a  $\text{WSe}_2$  flake covering the nano-pillar array, showing the integrated intensity from  $700 - 800 \text{ nm}$ . The enhanced PL coincides with the  $4 \mu\text{m}$  pillar distance (black pattern). d) Spectral information extracted between the blue arrows in c), revealing a periodic increase in luminescence and the formation of additional localized emission centers at the pillar positions.

ization of the luminescence from the emitters. In Fig. 3(b) two exemplary  $90 \text{ nm} \times 30 \text{ nm}$  pillars are shown which are aligned perpendicular to each other and covered by the same monolayer. Comparing the polarization of several emitters from these two pillars shows a strong correspondence of the polarization and pillar orientation (Figs. 3(c) and (d)). This alignment of the polarization along the long axis of the gold rectangle can be associated with the coupling of the emitter to the plasmonic excitations in the metal which are much more pronounced in the extended axes as has been demonstrated with similar plasmonic structures before [41]. Slight modification of the rotation angle also depends on the way the monolayer bends around the pillar, which further acts on the polarization of the emission [42].

#### 4. Simulation

In order to understand the optical enhancement of the quantum emitters in a  $\text{WSe}_2$  via a metal nanopillar, we investigated the plasmon modes excited by finite-difference time-domain (FDTD) method. Two geometries have been considered: a rod-like nanopillar and a square pillar as experimentally studied above. In the square pillar with a size of  $140 \text{ nm} \times 140 \text{ nm}$ , the electric field distribution on top surface of the pillar is calculated, as shown in Fig. 4(a), where a quantum emitter of  $\text{WSe}_2$  can be placed. At two vertical side edges orthogonal to the  $E_x$  polarization, strong field enhancement ( $E/E_0$ ) with a maximum value of 20 compared with an incident light is observed. In addition, the vector plot shows, that the field enhancement is strongly attributed from the  $E_x$  field at the edges. Because the emitter in 2D materials oscillates in plane, strong emission enhancement for the defect emitters at the edges can be induced by the resonant coupling

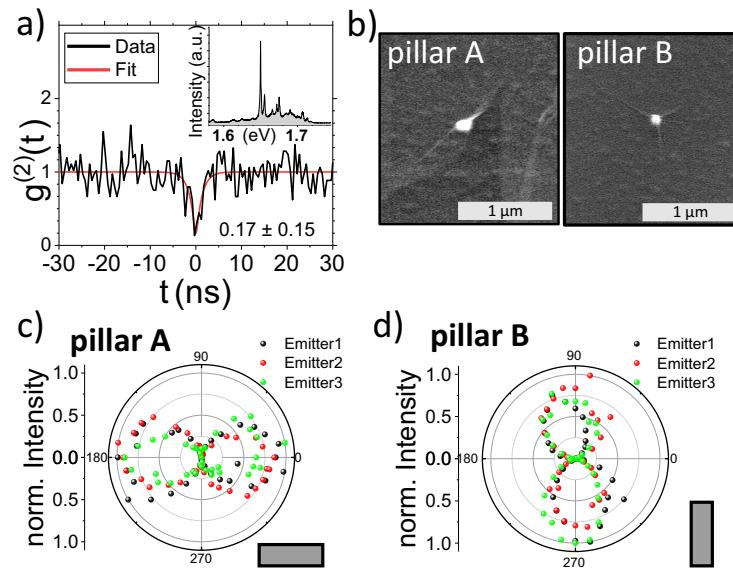


Fig. 3. a) Second-order autocorrelation function of a quantum emitter on a pillar. The value of  $g^{(2)}(\tau = 0) = 0.17 \pm 0.15$  confirms single photon emission. Inset: spectrum of single photon emitter. b) SEM images of two individual rectangles covered by WSe<sub>2</sub>. Pillar A is horizontally and pillar B vertically aligned. c) and d) Polarization characteristic of three individual quantum emitters each on two different 90 nm × 30 nm nanopillars shown in b).

of the plasmon mode. The mode of Fig. 4(a) is obtained by assuming  $E_x$  linearly polarized incident light, and a 90-degree rotated mode (not shown in the Fig.) can also be observed for  $E_y$  polarized incident light. The scattering cross-section spectra, which are plotted in Fig. 4(b), visualize the spectral dependence of the plasmonic mode in a square pillar for different sizes of the side edges from 40 nm to 140 nm, where the resonant peak for a size of 140 nm × 140 nm is centered around 733 nm with a large FWHM of 234 nm. Therefore, the radiative emission of the quantum emitter with a spectrum of Fig. 2(a) can be enhanced by resonant coupling with a plasmonic mode. As expected, the plasmon resonance shifts blue with decreasing the size.

In order to understand the strong polarization dependence of the emission from a rod-like nanopillar as shown in Figs. 3(c) and (d), the mode profile and the scattering cross-section of such a nanopillar with the experimentally studied cross-section of 90 nm × 30 nm are investigated. For the  $E_x$  polarized incident light, the electric field distribution of the plasmonic mode in Fig. 4(c) resembles that of our square pillar, Fig. 4(a) except for that the mode is elongated along the x-direction following the rod-like shape. In the scattering cross-section spectrum, the rod-like pillar exhibits strong plasmon resonance peak at a wavelength of 686 nm for an  $E_x$  polarized light, however, there are no significant resonances for an  $E_y$  polarized light (Fig. 4(d)). Therefore, 90 nm × 30 nm nanopillar can enhance the x-directionally polarized emission of a quantum emitter and selectively suppress the y-directionally polarized emission, resulting in strong linear polarization aligned along the long axis, as shown in Figs. 3(c) and (d).

## 5. Summary

In conclusion, we demonstrated the formation of ordered arrays of quantum emitters in an atomically thin layer of WSe<sub>2</sub>, transferred on a metal nanorod array. The metallic nanostructures yield the formation of quantum emitters, and furthermore can act as plasmonic resonators granting active polarization control via deterministic light-matter coupling. Our work is a first

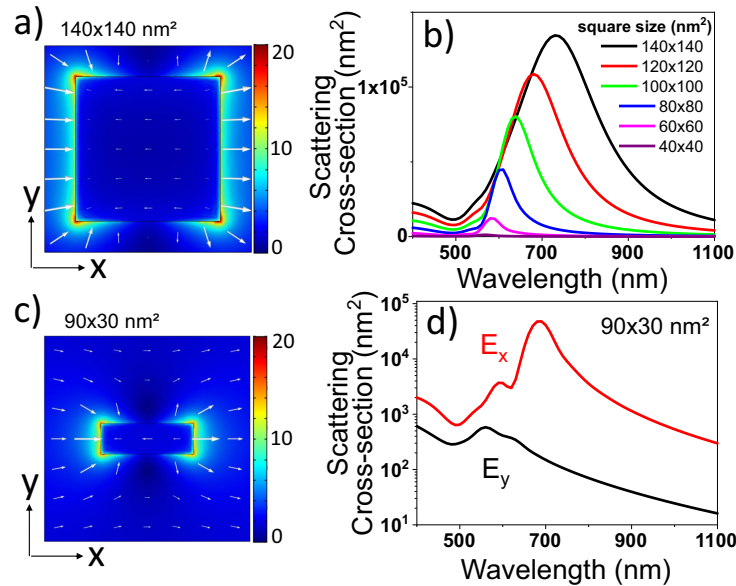


Fig. 4. FDTD simulation: Vector maps of the field distribution and electric field enhancement  $E/E_0$  at top surface of a pillar with a) a square cross-section of (140 nm  $\times$  140 nm) and c) a rod-like cross-section of (90 nm  $\times$  30 nm) excited by an electromagnetic field  $E_0$  of 1 V/m at 740 nm. b) Calculated scattering cross-section spectrum of square nanopillars with different size from 140 nm to 40 nm. d) Two scattering cross-section spectrums of a rod-like nanopillar with a size of 90 nm  $\times$  30 nm for an incident light with orthogonal polarizations,  $E_x$  (red) and  $E_y$  (black). X-direction represents the direction of the long edge of the rod-like nanopillar.

step towards highly scalable cavity quantum electrodynamics with engineered quantum emitters in two dimensional materials.

During the preparation of this report, we became aware of two similar studies claiming light-matter coupling with ordered quantum emitters on plasmonic nanostructures [43, 44].

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