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23 The study is performed via Kendall's tau and copulas. Temporal trends are studied
24 visually and by formal tests, considering variables individually and jointly. Bivariate
25 joint return period curves associated with consecutive time periods are compared to
26 understand the joint implications of such bivariate trends. Although no significant
27 bivariate trends were detected, hydrologically relevant trends were found in the
28 urbanised catchment.

29 *Keywords:* copulas, flood trends, Kendall's tau, urbanisation.

30 **INTRODUCTION**

31 Accurate design flood estimates with specified return periods are necessary for
32 designing and operating hydraulic structures, such as culverts and dams. Traditionally,
33 flood frequency analyses are based on an assumption of stationarity, i.e., assuming that
34 the flood generating processes remain unchanged over time (e.g., Stedinger *et al.* 1993;
35 Goel *et al.* 1998; Yue *et al.* 1999; Shiau *et al.* 2006). It has long been recognised by
36 hydrologists that stationarity is, at best, a simplified working assumption when changes
37 in urbanisation, land uses or climate are involved in the problem under analysis (e.g.,
38 Benkhaled *et al.* 2014), as such impacts can affect the behaviour of hydrological
39 variables, e.g., leading to changes in flood characteristics.

40 In cases where these effects are considered important, a non-stationarity approach
41 should be applied. Mathematical implementations of non-stationarity into flood
42 frequency models, such as using a non-stationary Generalised Extreme Value (GEV) or
43 Pearson Type 3 (PE3) distributions are relatively straight-forward. However, assessing
44 what is the correct model structure that best describes the impact of changing drivers on
45 the characteristics of the flood series as well as giving realistic predictions of future
46 impacts is far more difficult (Stedinger & Griffis 2011).

47 The effects of urbanisation on the characteristics of flood runoff have been the subject
48 of several scientific investigations, and it is generally recognised that urbanisation will
49 result in increased runoff volumes (decreased infiltration rates) and reduced catchment
50 lag-times (e.g., Rose & Peters 2001; Shuster *et al.* 2005; Kjeldsen 2009), thus
51 potentially being a significant cause of non-stationarity in flood series impacting both
52 peak flow values and runoff volumes (e.g., Sheng & Wilson 2009).

53 Much attention has been given to studying trends in peak flow values as a function of
54 time (Petrov & Merz 2009; Wilson *et al.* 2010; Mediero *et al.* 2014), with some
55 exceptions such as the approach presented by Bender *et al.* (2014) for analysing
56 bivariate non-stationary in an uncommonly long peak-volume flood data record (191
57 years). Indeed, as it is expected that increased urbanisation will lead to changes in other
58 flood characteristics other than the peak flow, in particular the flood volume, a study of
59 the potential changes in multiple variables is necessary to better understand the changes
60 that could affect flood risk under increasing urbanisation. The present study aims to
61 introduce and discuss a simple and general framework to investigate changes of
62 multivariate flood characteristics under increasing urbanisation. This is performed by
63 studying the univariate and bivariate properties of peak (Q) and volume (V) in two
64 paired case catchments located in the northwest of England. Changes in the univariate
65 peak flow values for these two catchments have already been assessed in Prosdocimi *et*
66 *al.* (2015), who found that the increase of urbanisation in Catchment 70005 was
67 connected to increasing trends, especially for summer flows. The present work wishes
68 to complement such a study by proving the conceptual framework needed to investigate
69 the bivariate behaviour of flow peaks and flood volume. The analysis of this case study
70 is especially relevant due to the available information about urbanisation levels and flow
71 records of high quality, something not easily found. Nevertheless, the available

72 hydrological record is relatively short and the results presented in this work should be
73 considered as preliminary and taken with caution. The two catchments are
74 hydrologically and climatologically similar, except for the increasing urbanisation
75 levels which affect one of them but not the other. The differences in the changes in the
76 flood characteristics in the two catchments can be imputed to the changes in the land
77 cover of the urbanised catchment. Changes in the association of the bivariate
78 distribution of (Q,V) are investigated by both the Kendall's tau (τ), a rank-based
79 dependence measure, and copulas for bivariate design flood analysis. Copulas (e.g., Joe
80 1997), which have found several applications in multivariate hydrological analysis (e.g.,
81 De Michele *et al.* 2005; Renard & Lang 2007; Klein *et al.* 2010; Ganguli & Reddy
82 2013; Requena *et al.* 2015), allow obtaining the multivariate joint distribution of
83 multiple random variables by characterising the relation of dependence among them,
84 incorporating the corresponding univariate marginal distributions that can belong to
85 different families.

86 **CASE STUDY AND DATA EXTRACTION**

87 The two catchments of this study are located in the northwest of England (Figure 1).
88 High-quality runoff time series of 15min resolution recorded by the Environment
89 Agency are available for the common period 1976–2008. The urbanised catchment is
90 drained by the River Lostock and flow data are recorded at Littlewood Bridge (gauging
91 station numbered 70005). In this catchment there has been a relatively high degree of
92 rural land-use being transformed into build-up areas (urbanisation) over the past 40
93 years; from 9% in 1976 to 16% in 2008 as shown in Figure 2. The temporal change in
94 catchment urban extent was computed at decadal time steps using the methodology
95 presented by Miller & Grebby (2014) from historical 1:10 000 topographic maps.

96 The rural catchment drained by the River Conder is a nearby hydrologically and
97 climatologically similar catchment, where flow data is recorded near Galgate (gauging
98 station numbered 72014). This is a predominantly rural catchment, which has
99 experienced little change in the study period. Hereafter the catchments are referred to
100 with their gauging station number: the urbanised catchment corresponds to Catchment
101 70005, and the rural one to Catchment 72014.

102 Table 1 displays key catchment descriptors from Institute of Hydrology (1999) for the
103 catchments under study: catchment area (AREA), baseflow index as predicted by the
104 Hydrology of Soil Type (BFIHOST), Standard-period (1961-1990) Average Annual
105 Rainfall (SAAR), flood attenuation from upstream lakes and reservoirs (FARL), and
106 proportion of the catchment covered by the 100-year floodplain (FPEXT). The two
107 catchments are deemed hydrologically similar according to the similarity measure
108 developed in Kjeldsen & Jones (2009). The finding of a suitable paired catchment
109 should be based on similarities in both hydrological and climatological terms. The
110 importance of identifying a catchment with a similar climatology is a key step for a
111 robust attribution of flood trends to increasing urbanisation (Shastri *et al.* 2015), and the
112 catchments used in this study were the best match given the paucity of long, high
113 quality flow records. In the present study, catchments have similar geographical
114 conditions, being nearby and entailing a similar gauging station elevation. Besides,
115 flood events are of the synoptic type for both catchments (Mediero *et al.* 2015). They
116 also entail a similar annual precipitation (SAAR in Table 1), as well as similar
117 oscillations for different quantiles of the catchment average daily rainfall series (Figure
118 3). Hence, a similar climate is considered.

119 The water year in the UK runs from October to September: events occurring between
120 October and March (included) are classified as winter events, while the period April to

121 September constitutes the summer months. The water year 1988–1989 was removed
122 from the study period, as no summer events were available for the gauging station
123 72014 in this year.

124 The period 1976–2008 was divided into two equally sized time windows (e.g., Shastri *et*
125 *al.* 2015), representative of periods of low and high urbanisation levels for Catchment
126 70005, respectively. Note that by using two equally sized time periods the uncertainty in
127 the estimates for the two time windows can be assumed to be of a similar scale. Only
128 two time windows were considered because of the relatively short common data,
129 although if longer data records were available, the procedure could be applied
130 considering a greater number of time windows. The first time window (named as W1)
131 runs from 1976 to 1992; while the second period (W2) runs from 1993 to 2008.
132 Therefore, the data series (Q_m, V_m) (ordered in time), with $m = 1:n_{tot}$ and n_{tot} the total
133 number of water years, is also divided into (Q_k^{W1}, V_k^{W1}) and (Q_k^{W2}, V_k^{W2}) , with
134 $k = 1:n_{tot}/2$. Here (Q_k^{W1}, V_k^{W1}) represent the first $n_{tot}/2$ pairs of (Q_m, V_m) and
135 (Q_k^{W2}, V_k^{W2}) the last $n_{tot}/2$ pairs. To simplify formulas, hereafter the pairs are presented
136 as (Q_i, V_i) with $i = 1:n$. Depending on the time period considered, (Q_i, V_i) makes
137 reference to (Q_m, V_m) , (Q_k^{W1}, V_k^{W1}) or (Q_k^{W2}, V_k^{W2}) , with n the corresponding data length
138 in each case.

139 A simple method for extracting the bivariate properties of flood events is considered to
140 study the effect of urbanisation on the typical shape of hydrographs, as it is
141 characterised by the strength of the correlation between peak flow and a measure of
142 flood volume. Traditional techniques for baseflow separation work with daily data
143 (Chapman 1999; Eckhardt 2008). However, this method should be applicable in an
144 empirical data-based study; and it should work with highly variable sub-hourly data,

145 rather than more smooth daily data. Then, because of the difficulty of isolating
146 individual flood hydrographs generated by distinct rainfall events, and due to the focus
147 of this study is to analyse the joint properties of volume and flood peak, the measure of
148 flood volume, V , adopted in this study is defined as the part of the event hydrograph
149 above a threshold set at 40% of the flood peak Q , i.e., V is considered as the volume
150 associated with the upper 60% of the flood event. By considering only flow above a
151 relatively high threshold, the event volumes were not unduly influenced by post-peak
152 small amounts of rainfall causing the flow to increase part way down the recession
153 curve. The 40% threshold used in this study was found to be sufficiently high to remove
154 the nuisance effects caused by secondary rainfall inputs while maintaining the
155 generality of the results. Also note that volumes extracted using different thresholds
156 were found to be correlated. In this regard, for instance, Karmakar & Simonovic (2007)
157 reported a highly significant correlation between peak and volume regardless of the
158 discharge threshold level. Note that a more detailed analysis of each individual event
159 would not result in more informative results, but rather lead to a less transparent
160 analysis. As an example, the identification of the (Q_i, V_i) pair associated with a given
161 water year i is shown in Figure 4.

162 For both catchments, the annual, summer and winter maxima of the instantaneous peak
163 flow value are identified and the corresponding volumes are extracted. Seasonal
164 maxima are also investigated to better understand whether the changes seen in the
165 annual series are driven by changes in a specific type of events. The autocorrelation for
166 the annual and seasonal series has been plotted and tested, indicating that the standard
167 iid assumption is verified (not shown). Types of floods were not analysed because
168 floods in UK mainly belong to the synoptic type (Mediero *et al.* 2015). In summary two
169 catchments are studied, 70005 (urban) and 72014 (rural), two event characteristics are

170 considered (Q and V), three maximum series of events are extracted (winter, summer
171 and annual maximum flow events), and three time periods are considered: 1976–1992
172 (W1), 1993–2008 (W2) and 1976–2008 (whole series).

173 **METHODOLOGY AND RESULTS**

174 The investigation of potential changes in the Q - V relationship proceeds as follows: at
175 first trends in the univariate series for Q and V separately and in the association between
176 the two variables are studied. Then, a non-parametric procedure is used to assess the
177 statistical significance of the observed trends. Finally, changes in the bivariate return
178 period curves computed via copulas are investigated. Results for the two catchments
179 under study are shown directly after the description of the methodological steps.

180 **Analysis of univariate flood trends in Q and V series**

181 The first step of the methodology consists in the analysis of univariate temporal trends
182 in the flood series, using visual inspection and the widely used Mann-Kendall test (e.g.,
183 Villarini *et al.* 2009; Coch & Mediero 2015), a non-parametric test based on Kendall's
184 τ . The Mann-Kendall test (Kendall 1975) is used to assess the null hypothesis of no
185 association between two variables, and the presence of significant temporal trends can
186 be assessed by taking time as one of the variables. The statistical significance is
187 assessed with a two-sided test at a 95% confidence level.

188 Figure 5 shows the evolution in time of the Q and V annual and seasonal series for
189 Catchment 70005 and Catchment 72014 (see Table 1 for descriptive statistics). A
190 smaller variation in time of Q and V can be seen in Catchment 70005 in comparison to
191 the characteristics of the flood events recorded in Catchment 72014. To ease the visual
192 identification of trends least squares fits are superimposed to each plot. Overall, the
193 regression slopes for Q appear to be steeper than those for V . Indeed, p -value of the

194 Mann-Kendall test indicate that only the trends of the annual and summer peak flow
195 series in Catchment 70005 are statistically significant at a 5% significance level (Table
196 2).

197 **Analysis of bivariate flood trends via Kendall's τ**

198 Bivariate trends are assessed through an exploratory analysis of the relationship
199 between Q and V using both graphical tools and a non-parametric measure on changes
200 in the dependence between the variables, as estimated by the Kendall's τ . Finally,
201 hydrograph shape and its connection with Kendall's τ is also analysed. Note that the
202 whole methodology followed in this section is first presented and later results are
203 displayed.

204 First a scatter plot of the $(R_i/(n+1), S_i/(n+1))$ pairs, where R_i is the rank of Q_i and
205 S_i is the rank of V_i (with $i = 1, \dots, n$) is drawn for winter, summer and annual maximum
206 flow events for both catchments under study. These plots provide a visual assessment of
207 the dependence between variables. Note that scatter plots are linked to the Kendall's τ
208 value, as the latter is a rank-based measure: more scattered ranks lead to smaller
209 Kendall's τ values (i.e., lower association), whereas less scattered ranks will entail the
210 opposite.

211 Next, changes in hydrograph shapes over time are investigated. The standardised mean
212 flood hydrographs of the Q - V pairs for a given time window (whole series, W1 or W2)
213 are plotted together by locating their time of peak on the same vertical (Miller *et al.*
214 2014), with the aim of visually comparing their average shape. Note that the mean flood
215 hydrographs are standardised by the largest observed peak value (Q_{peak}) in the sample,
216 considering the entire data length. The corresponding point-wise confidence intervals

217 $(\bar{y} - s, \bar{y} + s)$ are also obtained, where \bar{y} and s are the mean and standard deviation,
218 respectively, of the standardised flow values at each time step. This analysis is carried
219 out considering winter, summer and annual flood hydrographs.

220 The link between the hydrograph shape (which depends on the values of Q and V) and
221 Kendall's τ , can be understood by studying the relation between the corresponding
222 hydrograph shapes and the $(R_i/(n+1), S_i/(n+1))$ pairs. A didactic example extracted
223 from the annual data in Catchment 72014 is shown in Figure 6, in which specific a_l
224 pairs with $l = 1:7$ are selected from the scatter plot (Figure 6a). Overall, three distinct
225 clusters of events are evident. The first set is composed of pairs positioned close to the
226 main diagonal (e.g., a_1, a_2 and a_3). The second set consists of pairs located below the
227 main diagonal (e.g., a_4 and a_5). Finally, pairs located above the main diagonal (e.g.,
228 a_6 and a_7) constitute the third set. Each set is associated with a particular standardised
229 hydrograph shape, as it can be seen in Figure 6b generated following the procedure
230 explained in the previous paragraph. Shapes related to points in the second set are
231 steeper than the pairs of the first set. The opposite applies to the points of the third set,
232 where shapes are less flashy. Therefore, the closer the pairs are to the main diagonal
233 (i.e., the larger is Kendall's τ , as the larger is the correlation), the more balanced and
234 similar are the shape of the events. On the other hand, points located far away from the
235 diagonal, which would lead to smaller values of Kendall's τ , are generally characterised
236 by a larger variability in the hydrograph shapes.

237 The relationship between Q and V in the case study is investigated in Figure 7. The
238 scatter plots show the interplay of the scaled ranks of the two univariate variables, and
239 they are generated by first using the complete record, followed by a plot considering
240 each of the two time windows W1 and W2 (Figure 7a). Overall, it was found that ranks

241 related to W1 are more scattered than to W2 for Catchment 70005. The value of
242 Kendall's τ is also derived for each time window and drawn in a new plot to facilitate
243 the visual identification of the possible trend (Figure 7b). 95% confidence intervals are
244 also displayed in Figure 7b (Schneider *et al.* 2015). The Kendall's τ value is smaller for
245 W1 (indicating a more weak correlation) than for W2 (indicating a stronger correlation)
246 in Catchment 70005, as expected from the results of the scatter plots. Therefore, an
247 increase over time was observed in Kendall's τ for Catchment 70005. The opposite was
248 found for Catchment 72014.

249 The increasing correlation levels found in Catchment 70005 suggest that the hydrograph
250 shapes for this catchment would tend to become more regular in time, according to what
251 observed in Figure 6. On the contrary, the decrease of correlation seen in Catchment
252 72014 would indicate a larger variability of the flood hydrograph for this catchment. A
253 comparison between hydrograph shapes from the two time windows is shown in Figure
254 8. The mean and confidence intervals of the hydrograph shape associated with the entire
255 data record are also shown for illustration purposes. As it can be seen, the value of the
256 peak of the mean hydrograph increases from the first time period W1 to the second
257 period W2 for winter, summer and annual events (for both catchments). Note that the
258 largest increase is found for summer maximum flow events of Catchment 70005.
259 Results regarding confidence intervals support the Kendall's τ analysis presented in the
260 previous paragraph, showing that the difference between confidence interval boundaries
261 decreases from W1 to W2 for Catchment 70005 (i.e., the difference between events
262 decreases), while the opposite holds for Catchment 72014 (Figure 8) . No noticeable
263 differences were identified between mean hydrograph shapes, in neither of the time
264 windows nor catchments.

265 **Trend significance assessment: a permutation procedure**

266 A permutation test is suggested to check if the peak flow Q , the volume V or the
267 Kendall's τ coefficient are statistically different in the two time windows W1 and W2.
268 This is slightly different from testing whether time is related to the variable of interest,
269 as in the Mann-Kendall test, and allows using the same procedure to assess both
270 univariate and bivariate temporal flood trends. Also, permutation tests are non-
271 parametric (as well as the Mann-Kendall test) so that no formal distributional
272 assumption for the data is needed in order for the test to be valid, and, in some
273 situations, they provide exact inference (see, e.g., Ernst 2004; Good 2005, for an
274 introduction on permutation methods). The testing procedure consists of the following
275 steps: (i) choose a test statistic which gives a good representation of the scientific
276 question at hand; (ii) compute the test statistic for the observed data t_{obs} ; (iii) permute
277 without replacement the observed sample for $N_{\text{perm}} = 10\,000$ times; (iv) for each
278 permuted sample compute the test statistic $t_{\text{perm},i}$, with $i = 1 : N_{\text{perm}}$; (v) estimate the
279 empirical distribution (F_n) of the test statistic using all the N_{perm} permuted samples and
280 compute the (two-tailed) p -value as:

$$281 \quad p\text{-value} = 2 \min \left(\frac{\sum_{i=1}^{N_{\text{perm}}} 1_i}{N_{\text{perm}} + 1}, \frac{\sum_{i=1}^{N_{\text{perm}}} (1 - 1_i)}{N_{\text{perm}} + 1} \right), \quad \text{where } 1_i = \begin{cases} 1 & t_{\text{perm}}(i) > t_{\text{obs}} \\ 0 & t_{\text{perm}}(i) \leq t_{\text{obs}} \end{cases} \quad (1)$$

282 For p -values greater than 0.05 the null hypothesis is accepted at a 95% confidence level.
283 In this study, permutation methods are used to test if the location of the distribution of
284 both Q and V in the two different time windows is different. The difference between the
285 sample median (m_Q and m_V) in the two time windows is chosen as the test statistic to
286 represent the null hypothesis of equal locations. The observed difference between the
287 sample medians is compared with the distribution of the difference in the medians for

288 the permuted samples and the associated p -value is computed as in Equation (1).
289 Similarly, to further support the visual evidence of the previous sub-section, the null
290 hypothesis of constant association between Q and V is tested by using the difference
291 between Kendall's τ in the two windows as a test statistic.

292 P -values from Equation (1) by applying the permutation procedure to the case study are
293 shown in Table 3. Among the positive observed differences between m_Q and m_V in W1
294 and W2 for both catchments considering winter, summer and annual maximum flow
295 events, only the difference associated with summer maximum flow events of Catchment
296 70005 can be considered significant. Note that this trend was also found to be
297 significant when the Mann-Kendall test was applied considering the whole data length
298 (first sub-section of Methodology and Results Section). For the Kendall's τ , neither the
299 increase for Catchment 70005 nor the decrease for Catchment 72014 were found to be
300 statistically significant for any season.

301 **Analysis of bivariate flood trends by comparison of return period curves**

302 In the bivariate (Q - V) space, an infinite set of events given by their Q - V pairs are
303 located under the same return period curve, which can be estimated by copulas
304 (Salvadori & De Michele 2004; Requena *et al.* 2013). In this regard, the final step of the
305 assessment of the impact of urbanisation on flood properties entails the analysis of
306 trends in the bivariate Q - V space by the comparison between the return period curves in
307 windows W1 and W2, for a set of given return period values. As an initial step, the
308 analysis involves the selection of the joint distribution of (Q , V) that best characterises
309 the statistical behaviour of the variables, composed of the marginal distributions of Q
310 and V and a copula.

311 Although the information gained by studying the seasonal series can be useful for
312 identifying potential changes in the flood seasonality, the analysis of the bivariate return
313 period curves will focus on the annual series, since these are the ones that would be
314 used to estimate design floods. The methods could also be applied to summer or winter
315 maximum flow series.

316 **Selection of a joint distribution: margins and copula**

317 Following Sklar's theorem (Sklar 1959), the joint cumulative distribution function of
318 the random variables Q and V , $H(q, v)$, can be expressed as:

319
$$H(q, v) = C(F_Q(q), F_V(v)), \quad q, v \in \mathfrak{R}, \quad (2)$$

320 where q and v are given values of the variables Q and V , $F_Q(\cdot)$ and $F_V(\cdot)$ are the
321 marginal cumulative distributions functions of Q and V , respectively; and C is the
322 copula function, i.e., a joint cumulative distribution function with uniform margins.

323 Thus Equation (2) can be expressed as $C(u_1, u_2)$, where $u_1 = F_Q(q)$ and $u_2 = F_V(v)$.

324 The selection of both the marginal distributions that best represent the individual
325 variables, and the copula function that best characterises the dependence between Q and
326 V is then needed to achieve a complete description of $H(q, v)$.

327 Several distributions used in hydrology, such as the GEV, Generalised Logistic (GLO),
328 Generalised Normal (GNO), Generalised Pareto (GPA) and PE3 were considered as
329 potential marginal distributions of Q and V . The distribution that best characterises the
330 observed data was selected using the L-moment ratio diagram, in which the relations
331 between the theoretical coefficients of L-skewness (τ_3) and L-kurtosis (τ_4) for different
332 three-parameter distributions are shown through curves (Hosking & Wallis 1997). The
333 sample estimates of the coefficients of L-skewness (t_3) and L-kurtosis (t_4) are also

334 plotted in the same diagram, choosing the distribution curve closest to the sample
 335 values. The choice of the marginal distribution for each variable was performed using
 336 the series covering the whole data length, and the selected distribution applied to both
 337 time periods. This larger sample ensures that estimates of t_3 and t_4 are less biased.
 338 Location (ξ), scale (σ) and shape (γ) parameters of the three-parameter marginal
 339 distributions ($F_Q(\cdot)$ and $F_V(\cdot)$) are estimated by the method of L-moments. Since
 340 estimates of the shape parameter have a high uncertainty when using a short record
 341 (Stedinger & Lu 1995), the estimate $\hat{\gamma}$ obtained using the complete data series was used
 342 in each of the two time windows to reduce the uncertainty originating from the third-
 343 order statistic estimates.

344 In order to identify the copula that best characterises the dependence structure between
 345 Q and V , a representative set of potential copulas was tested: the Clayton, Frank and
 346 Gumbel copula belonging to the Archimedean family; the Galambos (and also the
 347 Gumbel) copula belonging to the extreme-value family and the Plackett copula
 348 representing other families. The goodness-of-fit test used for identifying possible copula
 349 candidates (see Genest *et al.* 2009) is based on the Cramér-von Mises statistic (S_n):

$$350 \quad S_n = \sum_{i=1}^n \left\{ C_n \left(\frac{R_i}{n+1}, \frac{S_i}{n+1} \right) - C \left(\frac{R_i}{n+1}, \frac{S_i}{n+1}; \hat{\theta} \right) \right\}^2, \quad (3)$$

351 where $C_n(\cdot)$ is the empirical copula and $C(\cdot)$ is the estimated copula with a $\hat{\theta}$
 352 parameter (obtained by the inversion of Kendall's τ method). The p -value needed to
 353 formally test if the copula is suitable is estimated by a validated bootstrap procedure
 354 (Genest & Rémillard 2008). This procedure (in a similar way to the aforementioned
 355 permutation procedure) derives an empirical distribution of the test statistic, S_n , using
 356 10 000 simulations. The copula is acceptable if the p -value is greater than 0.05.

357 Additional information is needed to choose the best copula among the ones that have
358 passed the goodness-of-fit test. By assessing the upper tail dependence, a further
359 analysis to check the ability of each copula to characterise the extreme values of the
360 studied variables is carried out (e.g., Poulin *et al.* 2007). For this purpose, the non-
361 parametric upper tail dependence coefficient of the observed data, $\hat{\lambda}_U^{CFG}$, is compared
362 with the theoretical upper tail dependence coefficient, $\hat{\lambda}_U$, of each copula (formulas in
363 Frahm *et al.* 2005). The copula is considered more appropriate as smaller is the
364 difference between $\hat{\lambda}_U^{CFG}$ and $\hat{\lambda}_U$ values. Remark that however, the reliability of $\hat{\lambda}_U^{CFG}$ is
365 limited, especially for a short data length. Moreover, the use of the Akaike information
366 criterion (AIC) as model selection criterion (Akaike 1974) can be helpful for ranking
367 the candidate copulas. Based on the latter, the best copula would be that with the
368 smallest AIC value.

369 Although in the present case study the observed changes in time considering jointly Q
370 and V (i.e., Kendall's τ trends in Trend Significance Assessment Sub-section) were not
371 identified as statistically significant (with p -values equal to 0.132 and 0.465 for
372 Catchment 70005 and 72014, respectively, see Table 3), they could still be
373 hydrologically relevant. Therefore, the implications of such trends for the flood
374 hydrograph shape should be analysed. For this analysis, the bivariate joint distribution
375 of the observed data was estimated for both time windows.

376 The marginal distribution $F_Q(\cdot)$ was chosen to be a GLO, which is generally the
377 preferred distribution for annual maximum peak flow data in the UK (Institute of
378 Hydrology 1999). However, no guidance exists in reference to hydrograph volumes, V .
379 The sample L-moment ratios of the V series for each catchment were plotted on an L-
380 moment ratio diagram (Figure 9). Figure 9 also shows the 95% confidence ellipsoids

381 based on the bivariate distribution of L-skewness and L-kurtosis, which are the basis of
382 the goodness-of-fit measure introduced by Kjeldsen & Prosdocimi (2015). The thicker
383 lines indicate the distributions that can be accepted according to the goodness-of-fit
384 measure; the selected distribution corresponds to the one for which the measure is
385 minimised for each catchment. The GLO distribution was selected to represent V for
386 Catchment 70005, while the GEV distribution was chosen for Catchment 72014. The
387 estimated parameters of the marginal distributions are shown in Table 4. As it can be
388 seen, the urban catchment has larger location parameters than the rural catchment, while
389 for both catchments and variables the skewness is negative. The estimated fitted
390 marginal flood frequency curves are displayed in Figure 10 along with the observed
391 data series. In the case of Catchment 70005, the marginal curve corresponding to W1
392 intersects that corresponding to W2 for both Q and V . That is, if small univariate return
393 periods (T) are considered, larger values of Q and V are expected for W2; the contrary
394 happens for larger T values. Intersection between marginal curves is not observed in
395 Catchment 72014.

396 Results for the copula selection criteria are shown in Table 5. Most of the considered
397 copulas passed the goodness-of-fit (i.e., p -values greater than 0.05), with the exception
398 of the Clayton copula that is rejected for several cases. Since all cases present upper tail
399 dependence, i.e., $\hat{\lambda}_U^{CFG}$ is greater than zero, the previously accepted copulas are cut
400 down accordingly to the $\hat{\lambda}_U$ values. In this regard, the Gumbel and Galambos copulas
401 show $\hat{\lambda}_U$ values close to $\hat{\lambda}_U^{CFG}$. Consequently, both of them could be chosen, as the
402 results of the AIC are also very similar. Because of the results in Table 5 and its
403 properties, the Gumbel copula was selected for the three time periods and both
404 catchments. This copula was also selected as the best copula in characterising the

405 dependence between peak flow and volume in other studies (e.g., Zhang & Singh 2006;
 406 Poulin *et al.* 2007; Karmakar & Simonovic 2009; Requena *et al.* 2013; Sraj *et al.* 2015).

407 **Comparison between bivariate joint return period curves**

408 Bivariate joint return period curves are used here to investigate changes in flood events
 409 between W1 and W2. Combination of values belonging to the return period curves can
 410 be estimated by the selected copula. In this study, the bivariate return period used for
 411 analysing changes in flood events is the widely used OR return period (T_{OR}) (Salvadori
 412 & De Michele 2004), in which the thresholds q or v are exceeded by the random
 413 variable Q ‘or’ V , respectively (Equation (4)).

414
$$T_{OR} = \frac{\mu_T}{P(Q > q \vee V > v)} = \frac{\mu_T}{1 - P(Q \leq q \wedge V \leq v)} = \frac{\mu_T}{1 - C(F_Q(q), F_V(v))} = \frac{\mu_T}{1 - C(u_1, u_2)}, (4)$$

415 where μ_T is the mean inter-arrival time between two successive events, with $\mu_T = 1$ for
 416 annual maximum series. Finally, return period curves are obtained in original units by
 417 transforming the (u_1, u_2) pairs with the same T_{OR} into (Q_{sim}, V_{sim}) pairs by Equation (5),
 418 using the previously selected marginal distributions.

419
$$Q_{sim} = \hat{F}_Q^{-1}(u_1), \quad V_{sim} = \hat{F}_V^{-1}(u_2), \quad (5)$$

420 where $\hat{F}_Q^{-1}(\cdot)$ is the inverse marginal distribution of Q , $\hat{F}_Q(\cdot)$. The same holds for
 421 $\hat{F}_V^{-1}(\cdot)$. The bivariate return period curves associated with the separate time windows
 422 W1 and W2 and the whole data length are calculated.

423 Probability level curves (of the copula) for several values of p (i.e., points fulfilling
 424 $C(u_1, u_2; \hat{\theta}) = p$, where p is the simultaneous non-exceedance probability of the two
 425 variables) for both study catchments are shown in Figure 11. The plot also shows 100
 426 000 (u_1, u_2) pairs randomly generated from the fitted copula (grey points), showing that

427 smaller Kendall's τ values lead to a more scattered data. Results for W1, W2 and the
428 entire record are plotted and compared for both catchments. In Catchment 70005, curves
429 related to W2 (with larger Kendall's τ) are located below those corresponding to W1
430 (with smaller Kendall's τ), while converging in the extremes (i.e., the asymptotes). The
431 opposite occurs for Catchment 72014. As expected, curves related to the whole data
432 length are located between W1 and W2 curves.

433 Figure 12 shows simulated copula values and bivariate joint return period curves
434 associated with $T_{OR} = 2, 5, 100$ and 250 years (Equation (4)) in original units (by
435 Equation (5)). It should be noted that the results for high return periods should be taken
436 with caution, due to the relatively short data length available and the consequent large
437 uncertainty; yet they are shown as illustration. For Catchment 70005, curves move
438 downward to the left (from W1 to W2) as larger is the return period. Overall, the
439 decrease is larger for Q than for V , reflecting the findings for the univariate distributions
440 (Figure 10). This means that flood events tend to have a lower peak value, while at the
441 same time the flood hydrographs tend to be less flashy. For instance, the vertex of the
442 100-year return period curve for the urban catchment undergoes a 9.4% decrease in
443 peak and a 7.6% decrease in volume from W1 to W2. Also, in accordance with the
444 results presented in Figure 10, such a trend differs for small return periods, as margins
445 of different time windows cross at $T_{OR} \cong 5$ for Q values, while at $T_{OR} \cong 2-5$ for V
446 values. However, the opposite is observed for Catchment 72014, as return period curves
447 move upward to the right. Such a shift is larger for Q , meaning that flood events would
448 become larger, while flood hydrographs steeper. This is also in accordance with the
449 results obtained in the univariate case (Figure 10), where the increase of Q is greater
450 than that of V . For instance, the vertex of the 100-year return period curve for the rural
451 catchment undergoes a 20.3% increase in peak and a 14.1% increase in volume from

452 W1 to W2. Note that for both catchments, a higher return period generally results in a
453 larger shift of the curve. This could be caused by the increasing uncertainty related to
454 increasing return periods, in particular with the small sample sizes available in this
455 study.

456 In case that an estimate of a design flood is required, the effect of changes in
457 urbanisation extent on return period curves can be assessed using the results associated
458 with W2. Alternatively, if stationarity is assumed the most reliable estimate will be
459 obtained by using the return period curves associated with the whole data length. Also,
460 differences between return period curves in the two time windows (of Catchment
461 70005) give some insight into how the curves move in time because of the urban
462 development. Consequently, this behaviour could be extrapolated in the future by using
463 predictions of the urbanisation increase level expected in a given catchment.

464 **DISCUSSION**

465 Significant univariate trends in the observed peak value Q for summer maximum flow
466 events in the urban catchment (70005) have been identified by both the Mann-Kendall
467 test and the permutation procedure. The Mann-Kendall test also found a significant
468 trend in the observed annual maximum flow events in this catchment. No significant
469 univariate trends were found, neither in the observed volume V nor in any of the
470 variables extracted from the rural catchment (72014). The results of trends in the
471 seasonal series help understanding from which types of events the trends in the annual
472 series are most likely to be driven. The results suggest that for the urbanised catchment
473 the potential changes in the annual series would mostly be driven by change for the
474 summer events.

475 The visual analysis of bivariate (Q,V) series found an increase in Kendall's τ over time
476 for Catchment 70005, leading to increasingly more regular hydrograph shapes; whereas
477 the opposite was found for Catchment 72014, resulting in a larger variability of flood
478 hydrograph shapes. The visual analysis of the hydrograph shape variability in time,
479 using confidence intervals, confirmed this result.

480 The analysis of bivariate trends in the characteristics of flood events in the urban
481 catchment found no statistically significant trends based on Kendall's τ . However,
482 opposite results to those found in the rural catchment were obtained. The implications
483 of such trends when considering bivariate return period curves were also opposite,
484 suggesting that the trend in the urban catchment may be caused by changes in the flood
485 generating processes that may not be statistically detected. Thus, it is likely that, if
486 indeed a change is occurring in some of the flood characteristics, a larger sample size
487 would be needed for standard statistical tests to detect it (see also Prosdocimi *et al.*
488 2014, for a discussion on sample size problems in the analysis of hydrological series).
489 The selection and fit of both margins and copula would be more powerful and accurate
490 if longer data series were available; and large uncertainties in the estimate of both
491 margins and copula could have affected the results.

492 In addition, two larger flood events observed in the first time-window (W1) in
493 Catchment 70005 could lead to larger quantiles for high return periods than in the case
494 of W2. Therefore, as W1 and W2 are short, both univariate and bivariate estimates for
495 high return periods are highly dependent on the magnitude of the observed flood events
496 and, consequently, on the magnitude of rainfall events that drove such flood events in
497 each period. Finally, it is also interesting to highlight that the effect of the bivariate
498 trend found (for high return periods) in the urban catchment is different from what
499 would normally be expected in an urbanised catchment, as in general urbanisation

500 should lead to steeper hydrograph shapes. A possible explanation could also be the
501 influence of the sewer system or local flood mitigation measures when high return
502 period floods are considered, although looking into the causes is beyond the scope of
503 this paper. Also, results may point towards a more complex interaction between
504 urbanisation and flood characteristics than commonly assumed.

505 Remark that in future studies, the results of the present preliminary analysis could be
506 compared with those obtained by applying the proposed methodology to a much longer
507 data length (when it is available), as well as to flood events identified by applying a
508 detailed hydrograph separation method, for which an exhaustive analysis of rainfall and
509 streamflow should be performed.

510 **CONCLUSIONS**

511 A simple and general framework to investigate the effect of changes in a catchment land
512 cover on the univariate and bivariate behaviour of some flood characteristics is
513 introduced. The case study is composed of two nearby hydrologically and
514 climatologically similar catchments in the northwest of England, where the most
515 important difference is the increasing urbanisation extent in the urban catchment; hence
516 any difference observed in time can mostly be attributed to urbanisation. In general, no
517 statistical evidence of temporal change was identified in the univariate series, apart from
518 an increasing trend in summer peak flows in the urban catchment. It should be
519 mentioned that the permutation test used for trend significance assessment on the
520 differences between the location of the distribution of a given variable might be
521 applicable to other hydrological analyses.

522 The potential bivariate trend due to increasing urbanisation in the urban catchment was
523 found to lead to smaller flood peaks and less flashy flood hydrographs. However, these

524 results could be conditioned to the short available records and the use of larger data sets
525 could be advisable for its confirmation. In addition, further research in the identification
526 and modelling of the process control on storm runoff in urban catchments could help in
527 understanding this finding.

528 The methodology presented in this work could be applied to any pair of catchments that
529 can be considered hydrologically and climatologically similar except for one major
530 characteristic, which has changed in one of the two catchments. Finally, the proposed
531 methodology can help practitioners to describe trends in flood characteristics, in order
532 to improve estimates of the design floods by a non-stationarity approach.

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Table 1 Summary of the catchment descriptors for the two catchments under study.

Descriptors	Catchment					
	70005 (urban)			72014 (rural)		
AREA[km ²]	54.5			28.99		
BFIHOST	0.473			0.443		
FARL	0.964			0.975		
FPEXT[%]	0.14			0.08		
SAAR[mm]	1021			1183		
Statistics	Season			Season		
	Winter	Summer	Annual	Winter	Summer	Annual
Mean Q	22.18	17.31	23.62	16.06	11.42	17.43
Median Q	22.78	15.85	22.95	13.85	9.64	16.45
25th quantile Q	18.03	9.73	19.78	11.78	8.02	12.95
75th quantile Q	24.75	22.18	25.97	21.98	15.45	22.65
Mean V	0.57	0.32	0.56	0.28	0.14	0.28
Median V	0.50	0.22	0.50	0.26	0.13	0.24
25th quantile V	0.40	0.15	0.38	0.16	0.08	0.17
75th quantile V	0.63	0.47	0.66	0.38	0.20	0.34

Table 2 Results of the Mann-Kendall test. Values in bold indicate statistically significant trends.

Catchment	Season	Variable	τ	p -value
70005	Winter	Q	0.230	0.067
		V	0.097	0.446
	Summer	Q	0.300	0.016
		V	0.222	0.077
	Annual	Q	0.276	0.027
		V	0.101	0.427
72014	Winter	Q	0.190	0.131
		V	0.214	0.089
	Summer	Q	0.173	0.168
		V	0.133	0.292
	Annual	Q	0.157	0.212
		V	0.099	0.436

Table 3 *P*-values of the trend significance assessment performed by the permutation procedure. Values in bold indicate statistically significant trends.

Catchment	Season	Differences in		
		m_Q	m_V	τ
70005	Winter	0.264	0.644	0.123
	Summer	0.002	0.317	0.961
	Annual	0.150	0.362	0.132
72014	Winter	0.213	0.262	0.393
	Summer	0.332	0.256	0.355
	Annual	0.262	0.450	0.465

Table 4 $\hat{\xi}$, $\hat{\sigma}$ and $\hat{\gamma}$ parameters of the marginal distributions of Q and V (related to annual maximum flow series) fitted by L-moments with a given $\hat{\gamma}$ estimated with the entire data length.

Catchment	Variable	Distribution	Period	Estimated margin parameters		
				$\hat{\xi}$	$\hat{\sigma}$	$\hat{\gamma}$
70005	Q	GLO	1976–1992 (W1)	21.679	3.774	
			1993–2008 (W2)	23.824	2.576	-0.162
			1976–2008 (whole series)	22.739	3.222	
	V	GLO	1976–1992 (W1)	0.493	0.154	
			1993–2008 (W2)	0.497	0.141	-0.265
			1976–2008 (whole series)	0.496	0.146	
72014	Q	GLO	1976–1992 (W1)	15.717	3.349	
			1993–2008 (W2)	18.187	3.950	-0.079
			1976–2008 (whole series)	16.949	3.675	
	V	GEV	1976–1992 (W1)	0.186	0.103	
			1993–2008 (W2)	0.214	0.114	-0.122
			1976–2008 (whole series)	0.201	0.107	

Table 5 Estimates of the copula parameter and results of the goodness-of-fit test, upper tail dependence measure and AIC for copula selection. Values in bold indicate copulas that pass the test.

Catchment	Time period	Copula	$\hat{\theta}$	S_n	p -value	$\hat{\lambda}_U^{CFG}$	$\hat{\lambda}_U$	AIC
70005	1976–1992 (W1)	Clayton	2.286	0.055	0.126		0	-5.719
		Frank	6.377	0.043	0.454		0	-8.870
		Gumbel	2.143	0.046	0.310	0.604	0.618	-8.036
		Galambos	1.429	0.046	0.299		0.616	-8.330
		Plackett	13.869	0.044	0.403		0	-8.009
	1993–2008 (W2)	Clayton	7.231	0.049	0.066		0	-3.634
		Frank	16.636	0.035	0.439		0	-25.318
		Gumbel	4.615	0.036	0.341	0.803	0.838	-20.228
		Galambos	3.906	0.036	0.345		0.837	-19.892
		Plackett	95.667	0.037	0.354		0	-22.482
	1976–2008 (whole series)	Clayton	3.043	0.060	0.004		0	-2.391
		Frank	8.022	0.034	0.219		0	-27.034
		Gumbel	2.522	0.031	0.244	0.664	0.684	-26.040
		Galambos	1.810	0.031	0.241		0.682	-26.101
		Plackett	21.622	0.034	0.196		0	-25.201
72014	1976–1992 (W1)	Clayton	3.371	0.039	0.544		0	-16.647
		Frank	8.717	0.032	0.868		0	-13.654
		Gumbel	2.685	0.031	0.899	0.686	0.706	-12.614
		Galambos	1.974	0.031	0.903		0.704	-12.794
		Plackett	25.516	0.032	0.889		0	-12.932
	1993–2008 (W2)	Clayton	1.705	0.080	0.009		0	-5.572
		Frank	5.057	0.063	0.069		0	-5.036
		Gumbel	1.853	0.056	0.116	0.555	0.546	-5.055
		Galambos	1.136	0.056	0.123		0.543	-4.796
		Plackett	9.102	0.062	0.081		0	-5.400
	1976–2008 (whole series)	Clayton	2.062	0.060	0.010		0	-20.427
		Frank	5.876	0.041	0.113	0.575	0	-17.136
		Gumbel	2.031	0.033	0.249		0.593	-15.451

Galambos	1.316	0.033	0.244	0.591	-14.958
Plackett	11.908	0.038	0.142	0	-18.086

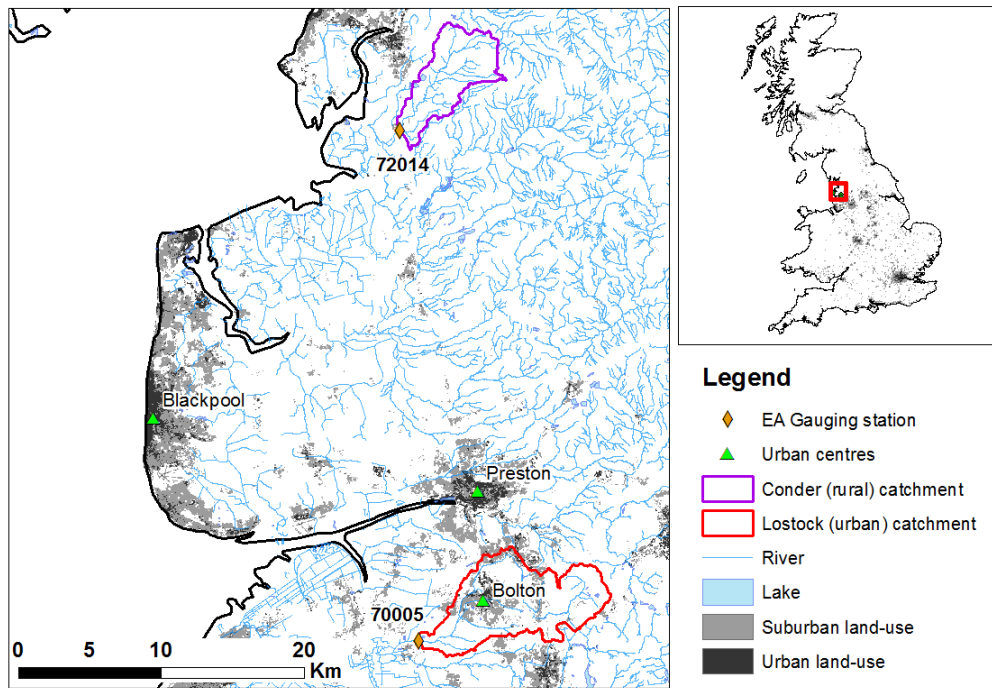


Figure 1 Location of the catchments.

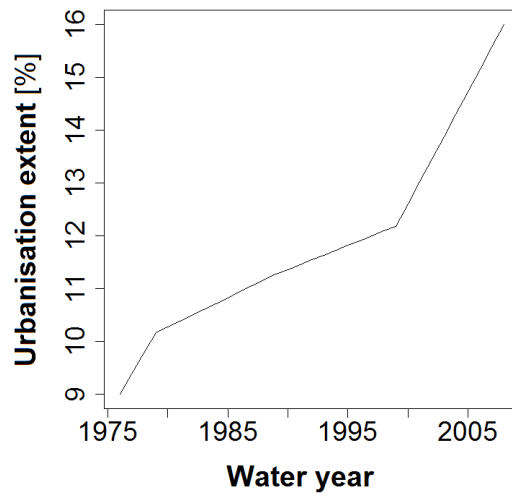


Figure 2 Evolution in time of the urbanisation level of Catchment 70005.

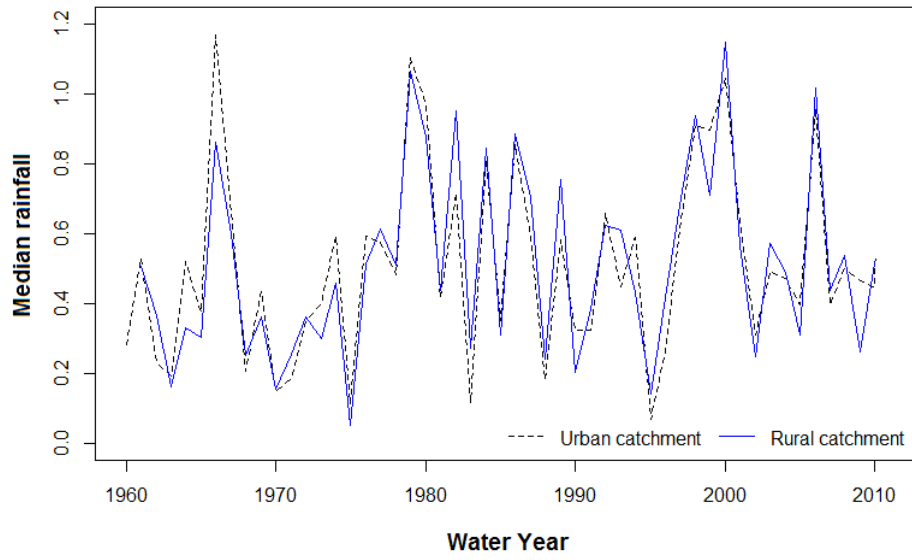


Figure 3 Example: median average daily rainfall series of the urban and rural catchments.

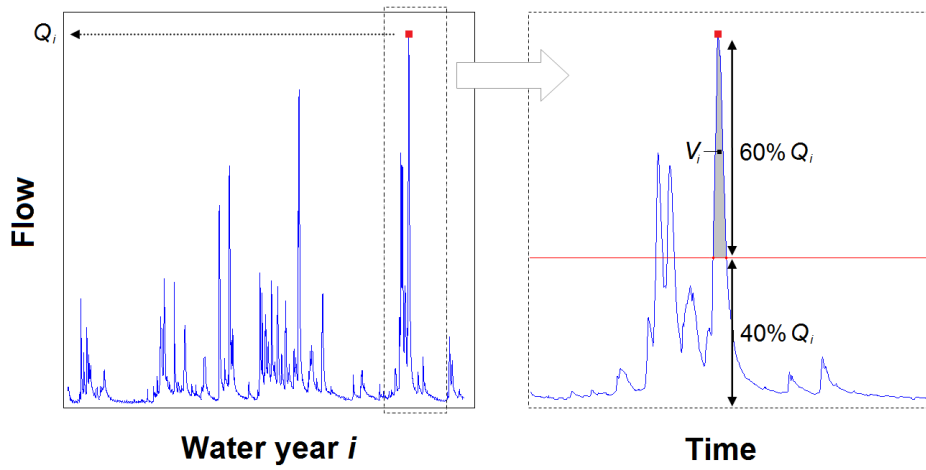


Figure 4 Example of (Q_i, V_i) extraction from a given water year i .

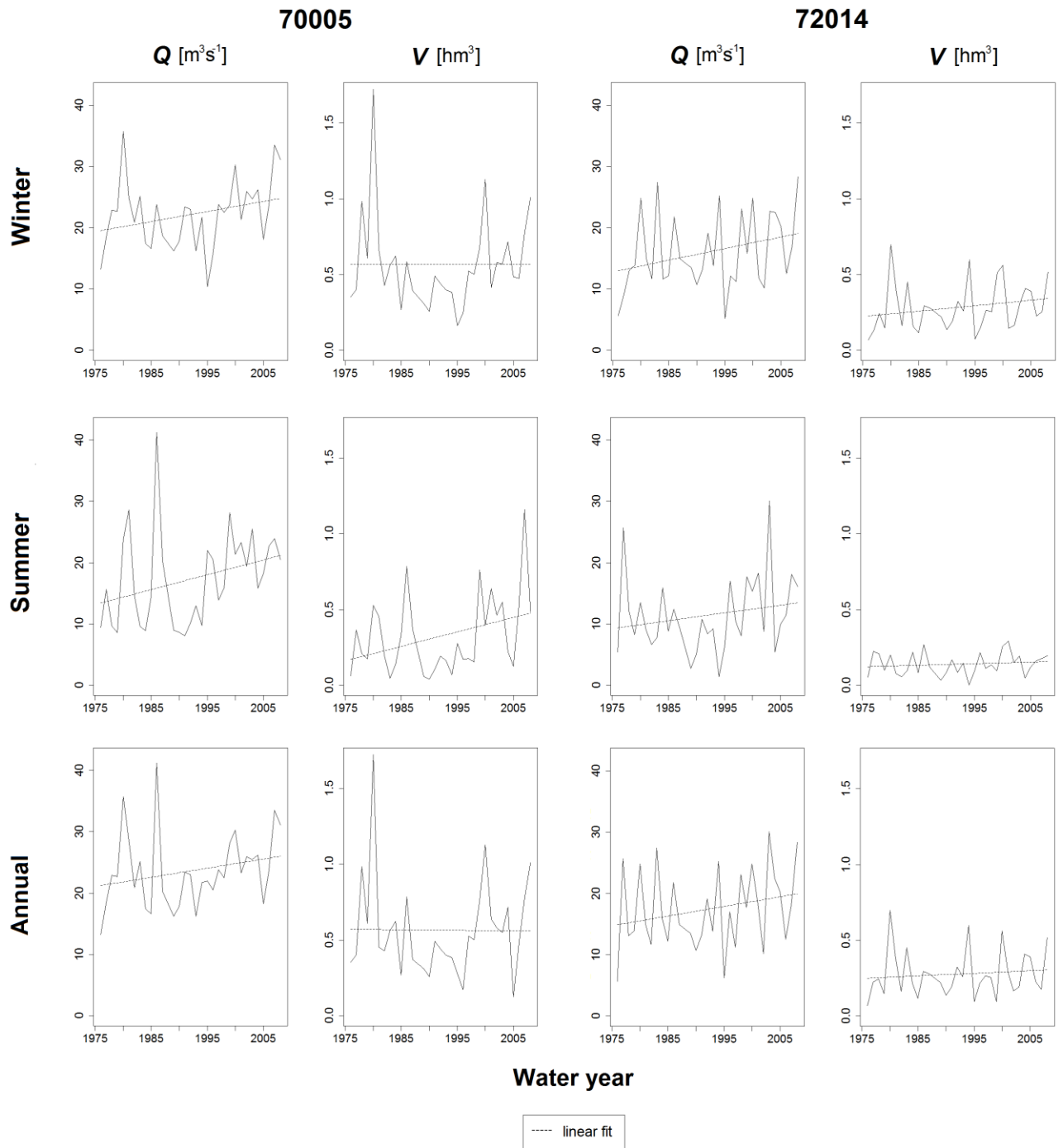
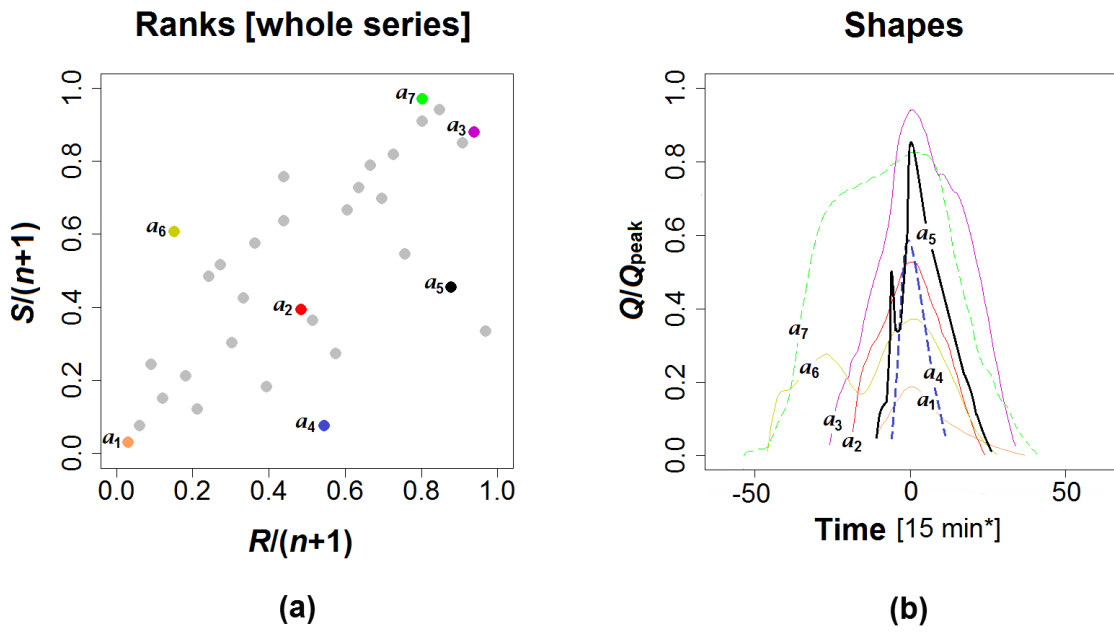


Figure 5 Evolution in time of Q and V .



(*) 1 day = 96 intervals (of 15 min)

Figure 6 Example of hydrograph shapes corresponding to different pairs of ranks: a) ranks; b) hydrograph shapes.

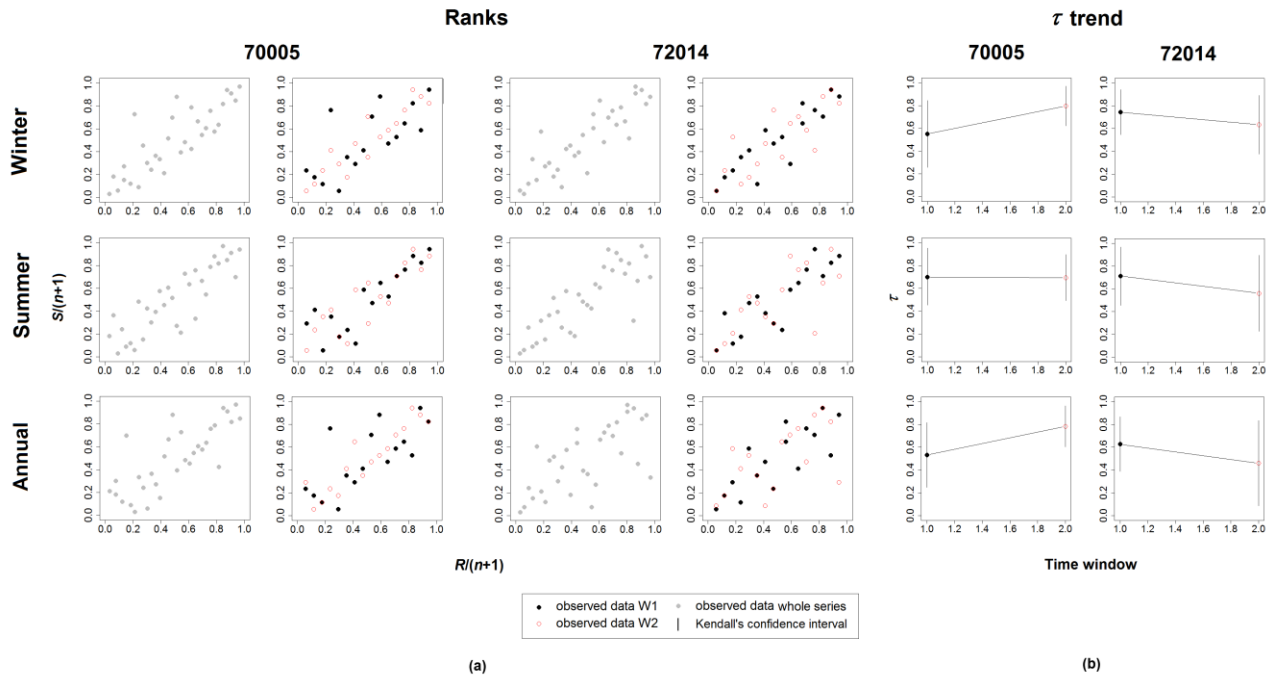
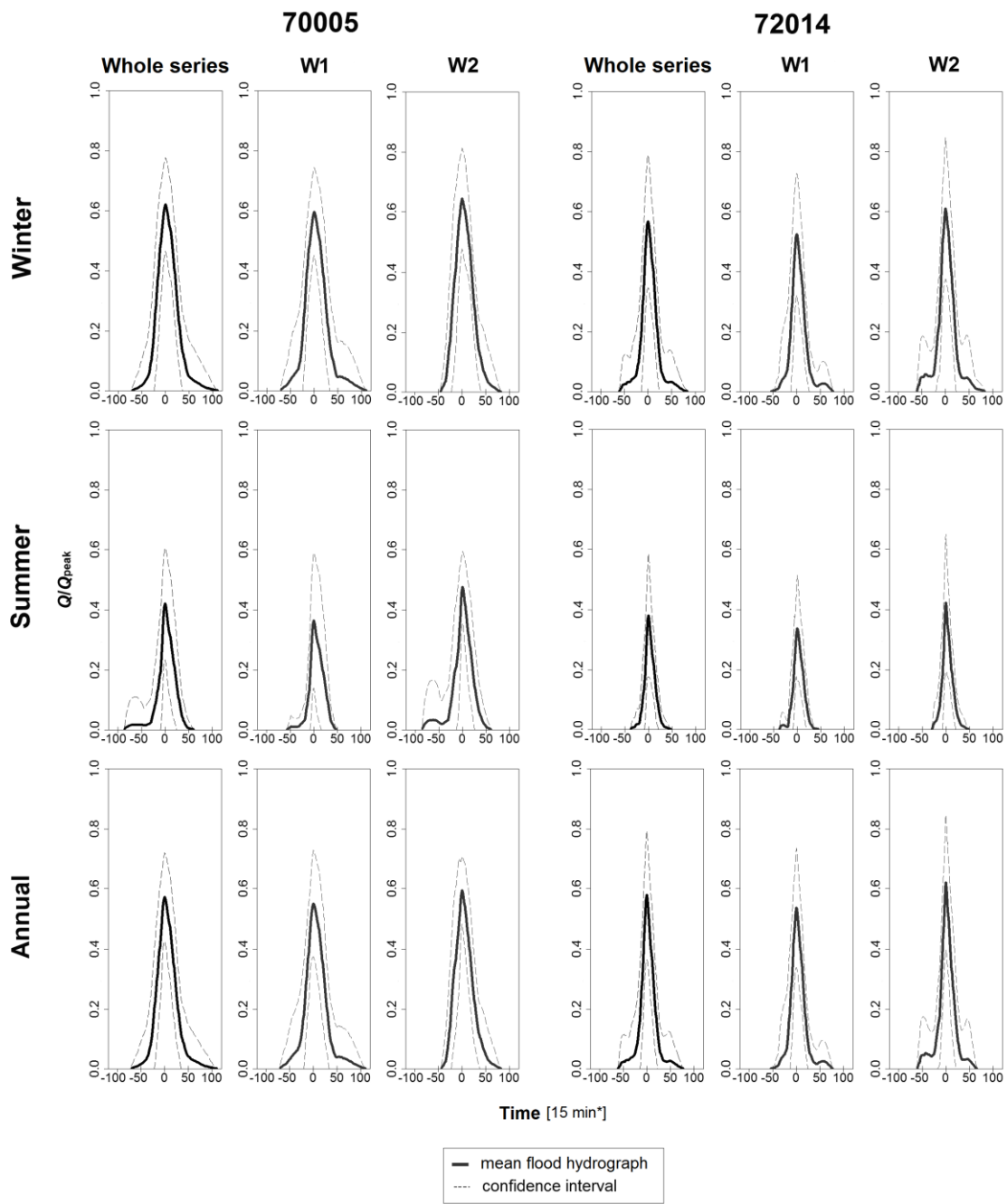


Figure 7 Ranks considering (by columns): a) whole data length, and data belonging to W1 and W2. b) Kendall's τ trend obtained from the two time windows.



(*) 1 day = 96 intervals (of 15 min)

Figure 8 Mean and confidence interval of the hydrograph shape.

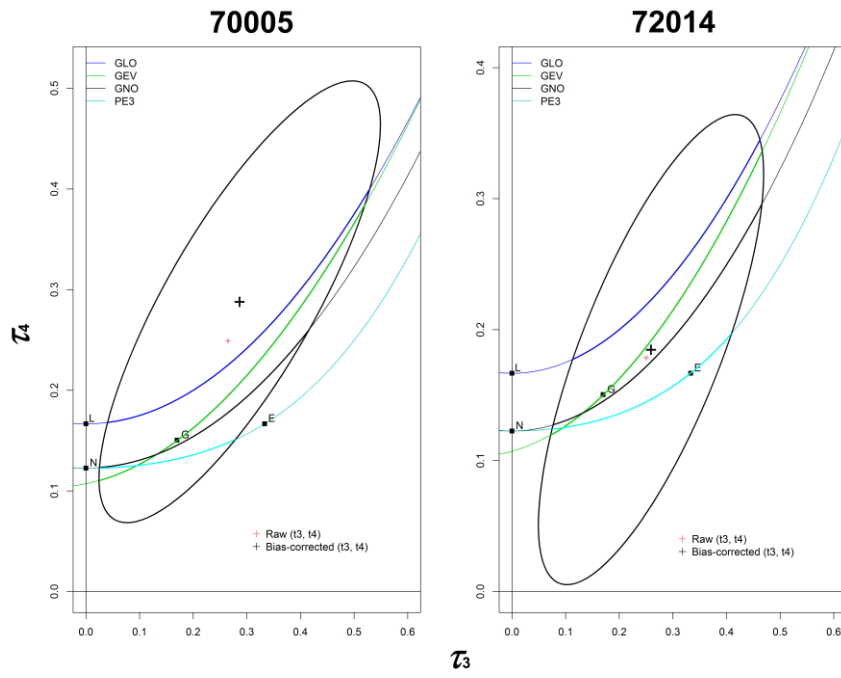


Figure 9 L-moment ratio diagram for the complete V series. The 95% ellipse identifying the acceptable distribution according to the Kjeldsen and Prosdocimi (2015) measure are also shown.

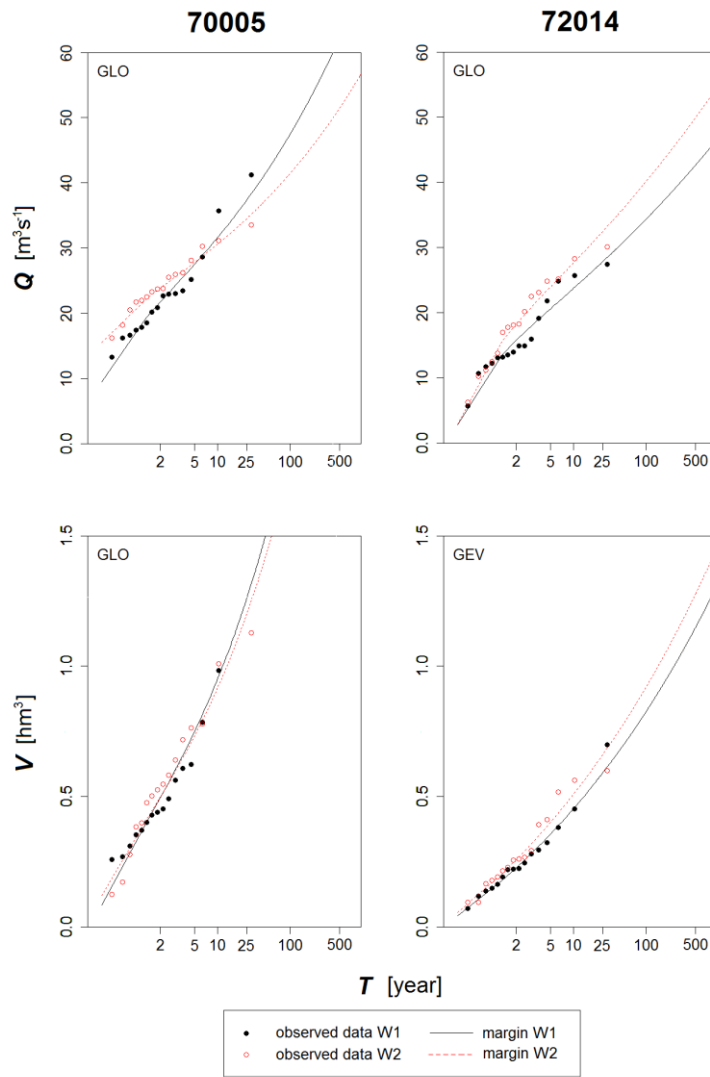


Figure 10 Fit of the selected marginal distribution (of annual maximum flow events) to the observed data for the two time windows.

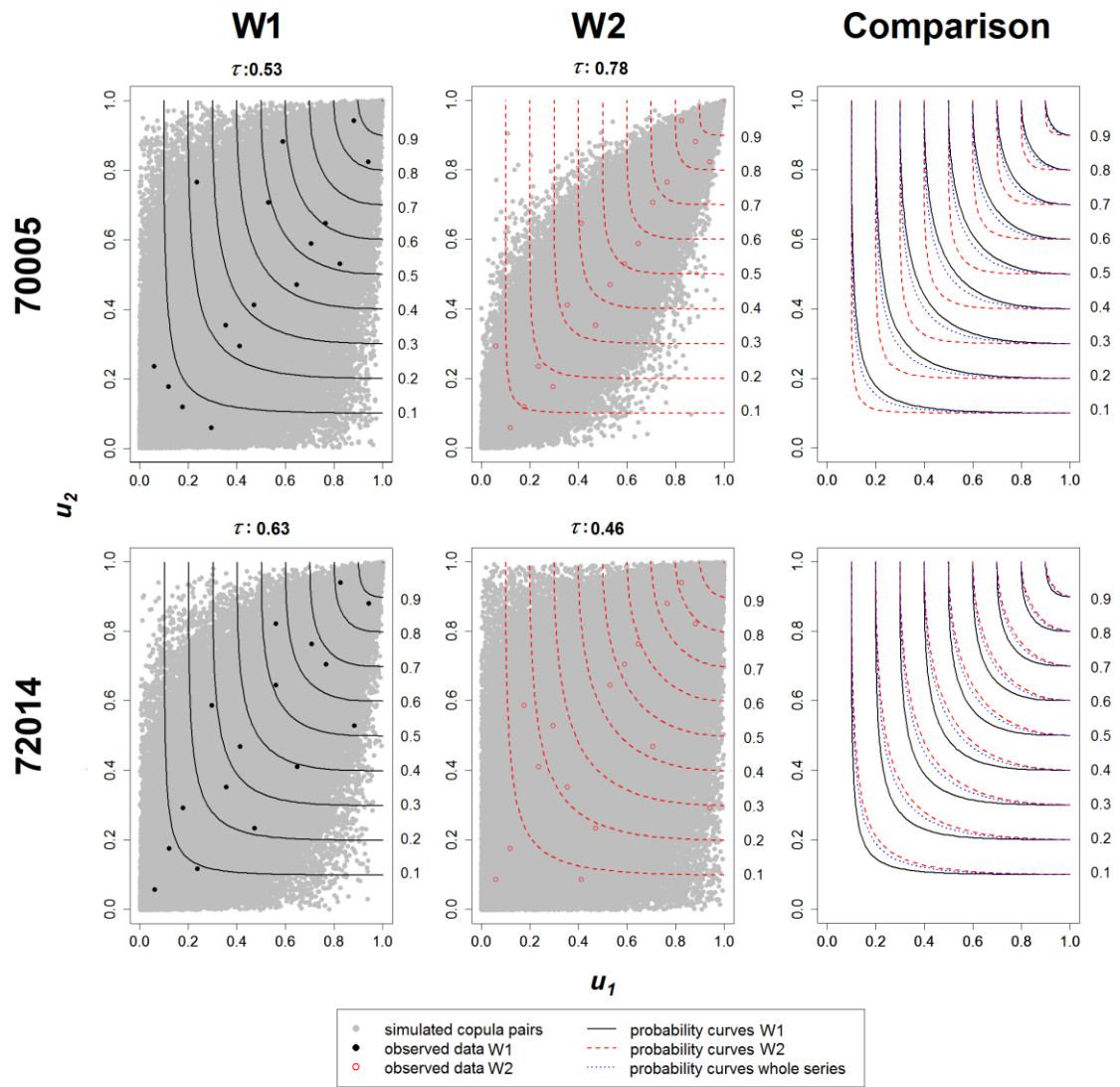


Figure 11 Probability level curves, and observed and simulated (u_1, u_2) data (copula scale) for time periods W1, W2 and whole data length.

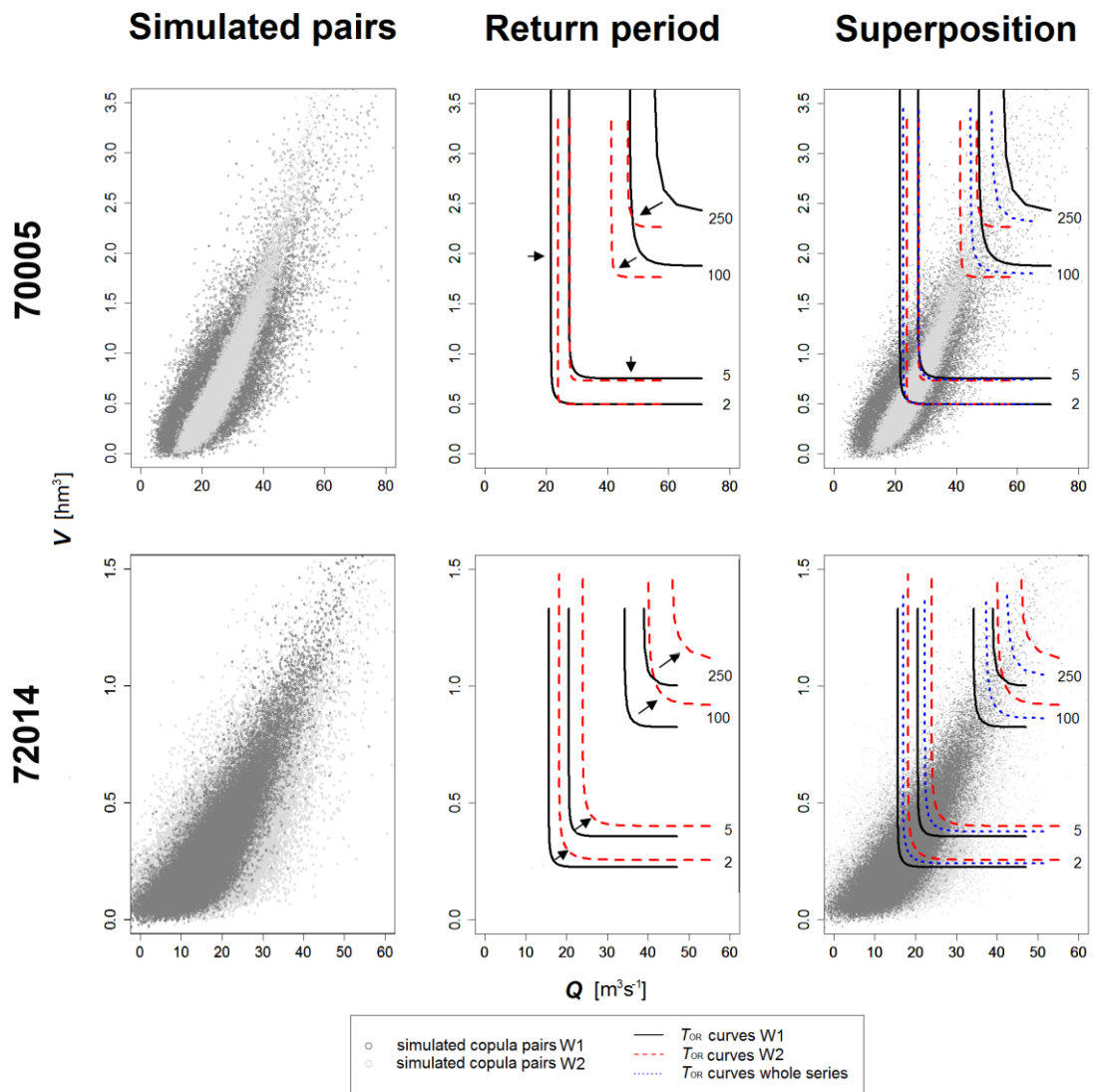


Figure 12 Simulated data and comparison among return period curves (original units) for W1, W2 and whole data length.