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1 **Title:**

2

3 **Polar-cap Plasma Patch Primary Linear Instability Growth-Rates Compared**

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13 **Key Points.**

14 Growth rates for plasma linear instability processes are investigated

15 Turbulence, Gradient Drift and Current Convective Instabilities can all be important

16 **Abstract**

17

18 Four primary plasma instability processes have been proposed in the literature to explain the  
19 generation of phase scintillation associated with polar-cap plasma patches. These are the  
20 Gradient Drift, Current Convective and Kelvin-Helmholtz instabilities and a small-scale  
21 “Turbulence” process. In this paper the range of possible values of the linear growth-rates for  
22 each of these processes is explored using Dynamics Explorer 2 satellite observations. It is found  
23 that the inertial Turbulence instability is the dominant process, followed by inertial Gradient  
24 Drift, collisional Turbulence and collisional shortwave Current Convective instabilities. The  
25 other processes, such as Kelvin-Helmholtz, collisional Gradient Drift and inertial shortwave  
26 Current Convective instabilities very rarely (<1% of the time) give rise to a growth rate  
27 exceeding 1/60, that is deemed to be significant (in publications) to give rise to GPS scintillation.

28

29 **Index terms:** 2439, 2471, 2772, 6929

30 **1. Introduction**

31 Large regions of enhanced electron concentration drifting according to an  $\mathbf{E} \times \mathbf{B}$  force from the  
32 auroral dayside ionosphere into the polar-cap region of the ionosphere were theorised by *Hill*  
33 [1963] as an explanation for “sporadic F” observations via  $f_oF2$  measurements in these areas.  
34 This theory was confirmed experimentally by *Buchau et al.* [1983] using optical all-sky camera  
35 images and the structures (100s – 1000s km in scale) became generally known as polar-cap

36 plasma patches. They were soon observed to cause radio scintillation on radio signals traversing  
37 them [e.g., *Weber et al.*, 1984]. Polar-cap plasma patches are also strongly correlated with  
38 backscatter of High Frequency (HF) Coherent Scatter Radar (CSR) signals, which occurs when  
39 the signals meet electron concentration irregularities [*Oksavik et al.*, 2006].

40 Irregularities cause scintillation through diffractive scattering [*Hargreaves*, 1992] or ionospheric  
41 lensing [*Booker and Majidihi*, 1981] of the signal. Scintillation inducing irregularities are  
42 considered to form through a cascade of energy from longer wavelengths to shorter ones in a  
43 manner analogous to that which occurs in the generation of turbulence in neutral fluids [*Kintner*  
44 *and Seyler*, 1985]. This requires some initial process to create wavelike structures in the plasma  
45 where there are none to start with – a primary plasma instability [*Kelley*, 2009].

46 A plasma instability is any wavelike structure that can grow exponentially in amplitude from  
47 some initial perturbation that is assumed to pre-exist. In order for this to happen, some source of  
48 free energy – energy available to do work – is required [*Mikhailovskii*, 1992]. Such energy  
49 derives from a combination of the Earth’s geo-magnetic field and electric field mapped from the  
50 magnetosphere to the high-latitude ionosphere, (day to night) electron density gradients and  
51 atmospheric gravity wave (TID) ‘seeding’ [e.g. *Hysell et al.*, 2014]. In this paper we consider  
52 only the linear regime, where the instability (consisting of alternating regions of higher and  
53 lower electron concentration) is assumed to grow exponentially in amplitude, at a particular  
54 growth rate. This linear regime is most likely to occur on the bottomside of the F-region, with  
55 non-linear processes dominating in the topside, particularly in the Equatorial region [*Hysell et*  
56 *al.*, 2014].

57

## 58 2. Theoretical background

59 In linear instability theory, the amplitude,  $A$ , of the unstable wave can be described as  $A = A_0 e^{\gamma t}$   
60 where  $A_0$  is the amplitude of the initial perturbation,  $t$  is the elapsed time since the start of the  
61 instability process and  $\gamma$  is the linear growth-rate of the instability. If there is more than one  
62 possible mode in a given set of physical circumstances, the relative magnitudes of  $\gamma$  provide a  
63 measure of which process will dominate the formation of irregularities within the plasma patch.  
64 It should, therefore be possible to calculate  $\gamma$  for each process and determine which instability is  
65 ultimately responsible for radio scintillation associated with plasma patches [e.g., *Burston et al.*,  
66 2009; 2010].

67 Doing this is complicated by the natural variation in the parameters that appear in the growth-  
68 rate equations from one patch to the next or even for a single patch, both spatially and  
69 temporally. For example, the electric field (which appears in all the growth-rate equations treated  
70 here) can be viewed as fluctuating in magnitude and direction around a quasi-D.C. component  
71 that in itself varies in magnitude and direction on a time scale of 10s of minutes and spatial scale  
72 of hundreds of kilometers [*Hanson et al.*, 1993] and the orientation of the field with respect to a  
73 gradient in electron concentration is always important. Hence, for any given instability the  
74 growth-rate can take a range of values, depending on the range of values possible for the  
75 parameters involved. For this reason different instabilities may dominate in different  
76 circumstances that depend on the frequencies of occurrence and ranges of values of various  
77 solar-terrestrial parameters that appear in growth-rate equations.

78 Several primary instabilities have been proposed as the cause of scintillation inducing  
79 irregularities associated with plasma patches. These are the Gradient Drift Instability (GDI),

80 which has received the most attention by researchers [e.g., *Burston et al.*, 2009; 2010;  
81 *Gondarenko, and Guzdar*, 1999; 2001; 2004a; 2004b; 2006a; 2006b; *Gondarenko et al.*, 2003;  
82 *Guzdar et al.*, 1998; *Sojka et al.*, 1998], the Current Convective Instability (CCI) which is a  
83 modification of the GDI [*Kelley*, 2009], a “turbulent” process [*Burston et al.*, 2010; *Earle and*  
84 *Kelley*, 1993; *Kelley*, 2009] and the Kelvin-Helmholtz Instability (KHI) [*Basu et al.*, 1990;  
85 *Carlson et al.*, 2007; *Gondarenko, and Guzdar*, 2006a; *Oksavik et al.*, 2012].

86 With four instabilities under examination it would be expected that there would be four growth-  
87 rate equations but for a single instability, there can in fact be more than one equation. This is  
88 because the growth-rates may differ in the collisional and inertial plasma regimes and in the long  
89 and short perturbation wavelength assumptions. In the inertial regime only the bulk electric fields  
90 are important. In the collisional regime, the effects of individual particles’ electric fields must be  
91 taken into account. The peak of the F-region (at ~300km) of the ionosphere represents a  
92 transitional region from collisional to inertial regimes (delineated by where the collisional  
93 growth rate and ion-neutral collision rate become equal). Thus, it is necessary to consider both  
94 situations [e.g. *Sojka et al.*, 1998]. Each instability is outlined below in its own section, with the  
95 appropriate growth-rate equations given.

## 96 **2.1 The Gradient Drift Instability**

97 The Gradient Drift Instability (GDI) requires a horizontal gradient in electron concentration,  
98 parallel to the electric field and a vertical magnetic field. Polar-cap patches potentially meet all  
99 these requirements as the geo-magnetic field is approximately vertical in the polar-cap, the  
100 electric field has a large horizontal component and the patch itself has gradients in all horizontal  
101 directions [e.g., *Basu et al.*, 1990; *Burston et al.*, 2009; *Chaturvedi et al.*, 1994; *Gondarenko,*

102 and Guzdar, 1999; 2001; 2004a; 2004b; 2006a; 2006b; Gondarenko and Guzdar, 2004a;  
 103 Gondarenko et al., 2003; Gondarenko and Guzdar, 1999; 2001; 2004b; 2006; Guzdar et al.,  
 104 1998]. The growth-rate in the collisional regime is given by

$$105 \quad \gamma_{CGDI} = \frac{\mathbf{E} \times \mathbf{B}}{B^2} \left( \frac{\nabla n}{n} \right) \quad (1)$$

106 where  $\mathbf{E}$  is the electric field vector,  $\mathbf{B}$  is the magnetic field vector and  $n$  is the electron  
 107 concentration (Figure 1) and  $\nabla n$  is the gradient of electron concentration per metre (Figure 2). In  
 108 the inertial regime the growth rate is given by

$$109 \quad \gamma_{IGDI} = \left[ v_{in} \frac{\mathbf{E} \times \mathbf{B}}{B^2} \left( \frac{\nabla n}{n} \right) \right]^{\frac{1}{2}} \quad (2)$$

110 [Sojka et al., 1998] where  $v_{in}$  is the ion-neutral collision frequency, given by

$$111 \quad v_{in} = \pi n_n r^2 \left( \frac{4kT}{\pi M} \right)^{\frac{1}{2}} \quad (3)$$

112 where, in turn,  $r$  is the colliding particles' radius, assumed the same for all species and  $M$  is the  
 113 colliding species' mass, also assumed the same for all species.  $T$  is the temperature, assumed the  
 114 same for all species and  $n_n$  is the neutral concentration. The constant,  $k$ , is Boltzmann's constant  
 115 [Kauzman, 1966]. This formula for the ion-neutral collision frequency is in fact that for the  
 116 collision of two neutral species and a more accurate version would take into account the small  
 117 correction required for a singly ionized species colliding with a neutral species. The assumption  
 118 that  $T$  is the same for all species is valid in quiet geomagnetic conditions only ( $K_p < 2$ ) otherwise  
 119 the collision rate will be larger than those used in this study. In the following,  $n_n$  is taken as the

120 density of monatomic oxygen (figure 3) and  $T$  is the  $O^+$  ion temperature (figure 4) as these are  
 121 the main constituents of the neutral and ionized atmosphere at F-region heights.

122

## 123 **2.2 The Current Convective Instability**

124 The Current Convective Instability may occur when the criteria for the GDI are met and current  
 125 flows parallel to the magnetic field (z-axis). Additionally, the initial perturbation must have a  
 126 finite component along the direction of  $\nabla n$  (y-axis). For the CCI, there is a wavelength  
 127 dependency as well as a difference between the collisional and inertial regimes, leading to four  
 128 equations [*Chaturvedi and Ossakow, 1979; 1981; Huba, 1984; Kelley, 2009; Ossakow and*  
 129 *Chaturvedi, 1979*]:

130 The growth rate for the CCI, collisional long wavelength regime is given [e.g. *Huba, 1984*] by

$$131 \quad \gamma_{lwcCCI} = -k_z \left( \frac{qB}{m_i v_{in}} \right) \left( \frac{n_1 - n_2}{n_1 + n_2} \right) \left( \frac{\mathbf{E} \times \mathbf{B}}{B^2} \right) \left\{ 1 + \left( \frac{k_z}{k_y} \right)^2 \left( \frac{q^2 B^2}{m_i m_e v_{in} v_{ei}} \right) \right\}^{-\frac{1}{2}} \quad (4)$$

132 where  $q$  is the charge on the electron,  $k_z$  and  $k_y$  are the wavenumbers in the z and y directions  
 133 respectively,  $n_1$  and  $n_2$  are the electron concentrations either side of a step-boundary  
 134 perturbation (with  $n_2 > n_1$ ),  $m_e$  is the mass of an electron,  $m_i$  is the mass of an ion and  $v_{ei}$  is  
 135 the electron-ion collision frequency. The latter, in S.I. units, is given [e.g. *Ichimaru, 1973*] by

$$136 \quad v_{ei} = \frac{nq^4}{4\pi\epsilon_0^2 m_e^{1/2} (3kT)^{3/2}} \ln \left[ 12\pi n \left( \frac{nq^2}{\epsilon_0 kT} \right)^{-3/2} \right] \quad (5)$$

137



138 The growth rate for the CCI collisional short wavelength regime is given [e.g. *Huba*, 1984] by

$$139 \quad \gamma_{swcCCI} = -\frac{k_z}{k_y} \left( \frac{qB}{m_i v_{in}} \right) \left( \frac{\nabla n}{n} \right) \left( \frac{\mathbf{E} \times \mathbf{B}}{B^2} \right) \left\{ 1 + \left( \frac{k_z}{k_y} \right)^2 \left( \frac{q^2 B^2}{m_i m_e v_{in} v_{ei}} \right) \right\}^{-1} \quad (6)$$

140 The growth rate for CCI inertial long wavelength regime is given [e.g. *Huba*, 1984] by

$$141 \quad \gamma_{lwiCCI} = \left( \frac{v_{ei} m_e B^2}{m_i \mathbf{E} \times \mathbf{B}} \right)^{1/3} \left[ k_y \left( \frac{n_1 - n_2}{n_1 + n_2} \right) \right]^{2/3} \frac{\mathbf{E} \times \mathbf{B}}{B^2} \quad (7)$$

142 CCI, inertial short wavelength:

$$143 \quad \gamma_{swiCCI} = \left( \frac{v_{ei} m_e n B^2}{4 m_i \mathbf{E} \times \mathbf{B} \nabla n} \right)^{1/3} \frac{\mathbf{E} \times \mathbf{B} \nabla n}{B^2 n} \quad (8)$$

144 The short wavelength regime applies when  $kL \ll 1$  and the long wavelength regime applies  
 145 when  $kL \gg 1$ , where  $k$  is the perturbation wavenumber and  $L = n/\nabla n$  is the electron  
 146 concentration gradient scale length.  $L$  is given by *Huba and Ossakow* [1980] as 10-100km. The  
 147 perturbation wavelength on a plasma patch will be of the order of several tens of km or less,  
 148 making the short wavelength equations the more applicable.

### 149 **2.3 Turbulence**

150 The Turbulence process was first put forward by *Kelley and Kintner* [1978] and further  
 151 examined in *Burston et al.* [2010] and *Kelley* [2009]. It takes into account the fact that the  
 152 electric field fluctuates around the quasi-D.C. component indicated by  $\mathbf{E}$  in the preceding  
 153 equations. If it is assumed that these fluctuations are random in direction then there is always a  
 154 direction in which the instability can occur. The growth-rate equation replaces the velocity

155 (given by  $(\mathbf{E} \times \mathbf{B})/B^2$ ) with its equivalent integrated over all relevant wavenumbers of the  
 156 fluctuations of the electric field.

$$157 \quad \left[ \int_{k_L}^{\infty} E(k)^2 dk \right]^{\frac{1}{2}} / B \quad (9)$$

158 where  $k_L$  is the smallest relevant wavenumber, in this case  $2\pi/(\text{scale of patch})$ , or of order  
 159  $2\pi/100,000\text{m}$ . Substituting Eq.9 into Eq.1 gives the growth rate for the turbulent collisional  
 160 regime as

$$161 \quad \gamma_{cT} = \left[ \int_{k_L}^{\infty} E(k)^2 dk \right]^{\frac{1}{2}} \left( \frac{v_n}{nB} \right). \quad (10)$$

162 Substituting Eq.9 into Eq.2 gives the growth for the turbulent inertial regime as

$$163 \quad \gamma_{iT} = \left\{ v_{in} \left[ \int_{k_L}^{\infty} E(k)^2 dk \right]^{\frac{1}{2}} \left( \frac{v_n}{nB} \right) \right\}^{\frac{1}{2}} \quad (11)$$

#### 164 **2.4 Kelvin-Helmholtz Instability**

165 The idea that primary ordinary Kelvin-Helmholtz Waves structure plasma patches was examined  
 166 observationally by *Basu et al.* [1990] and modelled by *Gondarenko, and Guzdar* [2006a] who  
 167 concluded that primary shear slows the development of the GDI. The idea was advanced again  
 168 by *Carlson et al.* [2007] who, in contradiction of this earlier work suggested it would accelerate  
 169 the generation of irregularities. The Carlson hypothesis was further tested in a case-study by  
 170 *Oksavik et al.* [2012] where it was found not to be dominant over the GDI except in a narrow  
 171 band of wavelengths. The growth-rate used in these KHI studies of  $2\Delta U/L$  (where  $\Delta U$  is the  
 172 velocity change across a shear zone and  $L$  is the distance scale length) disguises the electric and

173 geomagnetic field dependence and is therefore not appropriate for comparison with the equations  
 174 already given in this paper. Instead, the equation used here is derived as a special case of the  
 175 dispersion relation equation given in *Mikhailovskii* [1992] for ordinary Kelvin-Helmholtz  
 176 Waves.

$$177 \quad \frac{(\omega - kV_1)^2}{C_{A1}^2} + \frac{(\omega - kV_2)^2}{C_{A2}^2} - 2k^2 = 0 \quad (12)$$

178 where  $C_1$  is the Alfven speed in zone 1,  $C_2$  is the Alfven speed in zone 2,  $V_1$  is the plasma  
 179 velocity in zone 1 and  $V_2$  is the plasma velocity in zone 2 and  $k$  the perturbation wavenumber. If  
 180  $n_1$  and  $n_2$  are the electron densities in zone 1 and 2 respectively, then the Alfven speed is given  
 181 by  $C_j^2 = \frac{B^2}{\mu_0(m_i + m_e)n_j}$  with  $j = 1$  or  $j = 2$  for the two different zones and  $m_i$  and  $m_e$  are the ion and  
 182 electron masses respectively.

183

184 Assuming that the patch (taken as zone 1) is moving and its surroundings (taken as zone 2) is  
 185 stationary then  $V_1 = V = |(\mathbf{E} \times \mathbf{B})/B^2|$  and  $V_2 = 0$ . Hence, Eq.12 becomes

$$186 \quad \frac{(\omega - kV)^2}{C_1^2} + \frac{\omega^2}{C_2^2} - 2k^2 = 0 \quad (13)$$

187 Solving for  $\omega$  gives:

$$188 \quad \omega = \left( \frac{kVC_2^2}{C_1^2 + C_2^2} \right) \pm \frac{\{4k^2V^2C_2^4 - 4(C_1^2 + C_2^2)(k^2V^2C_2^2 - 2k^2C_1^2C_2^2)\}^{\frac{1}{2}}}{2(C_1^2 + C_2^2)} \quad (14)$$

189 and a growth-rate (rightmost term) given by

190 
$$\gamma_{KH} = \frac{k\{V^2 C_2^4 - (C_1^2 + C_2^2)(V^2 C_2^2 - 2C_1^2 C_2^2)\}^{\frac{1}{2}}}{(C_1^2 + C_2^2)} \quad (15)$$

191 which simplifies to

192 
$$\gamma_{KH} = \frac{kC_1 C_2 \{2(C_1^2 + C_2^2) - V^2\}^{\frac{1}{2}}}{(C_1^2 + C_2^2)} \quad (16)$$

193 with instability condition

194 
$$V^2 > 2(C_1^2 + C_2^2) \quad (17)$$

195 For unstable growth, there must be an imaginary component to  $\omega$ , which implies a negative  
 196 square root in Eq.16.

197 Substituting  $V$ ,  $C_1^2$  and  $C_2^2$  into Eq.16 gives

198 
$$\gamma_{KH} = \frac{k(n_1 n_2)^{1/2}}{(n_1 + n_2)} \left[ \frac{2B^2}{\mu_0(m_i + m_e)} \left( \frac{1}{n_1} + \frac{1}{n_2} \right) - \left( \frac{|\mathbf{E} \times \mathbf{B}|}{B^2} \right)^2 \right]^{1/2} \quad (18)$$

199 The instability condition becomes

200 
$$\left| \frac{\mathbf{E} \times \mathbf{B}}{B^2} \right|^2 > \frac{2B^2}{\mu_0(m_i + m_e)} \left( \frac{1}{n_1} + \frac{1}{n_2} \right) \quad (19)$$

201 It is notable that the instability condition is independent of wavenumber but larger wavenumbers  
 202 (shorter wavelengths) will grow faster.

203

204 The above four processes can be divided into two categories; those that are dependent on a  
205 specific geometrical relationship between the electric field and the electron concentration  
206 gradient and those that are not. The GDI, whether collisional or inertial, falls into the former  
207 category, whereas the others fall into the latter. Specifically, the GDI requires that the electric  
208 field be parallel to the gradient, which in turn means it will only operate on the trailing edge of a  
209 patch. (On the leading edge, the electric field would be anti-parallel to the gradient.) At first  
210 glance it might be thought that this should apply to the Turbulence process, too, but in fact,  
211 because it is assumed that the A.C. fluctuations in the electric field have no directional bias, all  
212 slopes are unstable approximately half the time.

213 It should be noted here that another possibility has been suggested for the structuring of plasma  
214 patches; particle precipitation during formation. Anisotropic precipitation of energetic particles  
215 from above the ionosphere would lead to localized regions of increased ionization and hence  
216 gradients in electron concentration within the plasma patch. By modifying  $n$  and  $\nabla n$  in the patch  
217 and causing localized heating, this process would affect the subsequent growth-rate of all plasma  
218 instabilities discussed here. This process would only occur during the formation of the patch and  
219 would cease once the patch left the region of the cusp [*Oksavik et al.*, 2012; *Walker et al.*, 1999].  
220 Since it is not itself an instability process it cannot be directly investigated by the method  
221 outlined below.

### 222 **3.0 Method**

223 The possible magnitudes of the growth-rate for the four processes discussed above (for both  
224 inertial and collisional regimes) are assessed below using some 550 days of data from the  
225 Dynamics Explorer 2 (DE2) satellite covering August 1981 to February 1983. Thus, the DE2

226 data are concentrated at the peak of solar-cycle (#21) and therefore do not represent a whole  
227 solar cycle. Similarly, only data recorded by the satellite when at 300 – 400 km altitude and  
228 greater than 65° magnetic latitude (north and south) are used in order to constraint our study to  
229 the F2 peak and polar cap regions. For illustration we do not separate the two hemispheres.  
230 However, it should be noted that there will be differences between hemispheres because of  
231 measurement times and the offset of the geographic from the geomagnetic and dip poles [e.g.  
232 *Coley and Heelis, 1998*]. The DE2 data were chosen as all of the parameters in the growth rates  
233 equations used are either directly observed by, or can be calculated from, DE2 observations, with  
234 a minimum in the way of approximation or assumption, except with regard to the electric field  
235 because of a partial instrument failure (discussed below) and the wavenumbers of initial  
236 perturbations, the range of values of which are assumed. Full details of the instruments aboard  
237 the satellite can be found in [*Hoffman et al., 1981*]. In the following, the relative magnitudes of  
238 growth-rates for all the relevant processes are compared. This done by randomly sampling the  
239 data for each parameter, which are then use to calculate all possible values of growth-rate for  
240 each growth-rate equation.

241

242 The values of  $v_{in}$  and  $v_{ei}$  used in the following were calculated from DE2 data by using Eq.3  
243 and Eq.5 respectively. The values for  $T$  are taken as the ( $O^+$ ) ion temperatures (whose histogram  
244 of occurrence is displayed in Figure 4),  $n_n$  is the neutral monatomic oxygen concentration  
245 (histogram of occurrence displayed in Figure 3) and  $n = n_i$  (i.e. the ion and electron  
246 concentrations are assumed equal and histogram of occurrence is displayed in Figure 1). The full  
247 field strength  $B$  (histogram of occurrence displayed in Figure 5) is also approximated by the

248 vertical magnetic field component ( $B_z$ ). In the following only the magnitude of the growth rate is  
249 calculated (vector quantities are replaced by scalar ones in all cases) simplifying the equations  
250 slightly.

251

252 The Electric field data comes from the Vector Electric Field Instrument (VEFI) on board DE2.  
253 This consisted of three mutually perpendicular instruments measuring orthogonal electric field  
254 strength components, allowing recovery of the full electric field strength vector  $\mathbf{E}$  [Heppner *et*  
255 *al.*, 1978a; 1978b]. Unfortunately the z-axis instrument did not deploy and no z-axis data were  
256 recorded. Because the axes were relative to the spacecraft, it is not possible to determine the  
257 components of the field in the Earth centred co-ordinate system without the z-axis data. Hence a  
258 method of approximating values of  $E = |\mathbf{E}|$  had to be applied. Examination of the relevant data  
259 recorded in the x-y plane (spacecraft co-ordinates) showed that 50% of the time the values of  
260 each component  $E_x$  and  $E_y$  were the same order of magnitude and over 90% of the time  $E_x$  and  
261  $E_y$  differed by no more than one order of magnitude (See Table 1). In the case of the A.C. field  
262 (see also Table 1) the  $E_x$  and  $E_y$  components also differed from each other by no more than one  
263 order of magnitude over 90% of the time. Since the spacecraft co-ordinate system continuously  
264 varied in relation to the Earth centred co-ordinate system, it was assumed that  $E_z$  would also  
265 rarely differ from  $E_x$  and  $E_y$  by more than this. Hence the approximation

266  $E_z^2 \approx (E_x^2 + E_y^2)/2$  was adopted, leading to

267 
$$E \approx \sqrt{\frac{3}{2}(E_x^2 + E_y^2)}. \quad (20)$$

268 Given all of the above, the equation used for the collisional GDI growth rate, Eq.1, becomes

269 
$$\gamma_{cGDI} = \frac{E}{B} \frac{|\nabla n|}{n} \quad (21)$$

270  $\nabla n$  was derived from DE2 Langmuir probe observations of electron concentration  $n$  (as  
271 displayed in Figure 1) in the following manner: First, only data recorded at 300 – 400 km altitude  
272 were admitted, in order to retain only F-region altitudes. Second, only data at  $> 65^\circ$  magnetic  
273 latitude were admitted (in either hemisphere), in order to retain only geographical regions where  
274 patches plausibly occur. The  $65^\circ$  magnetic latitude was chosen to capture patches during storms  
275 equatorward of the polar cap, as patches are more prevalent during such storm time conditions.  
276 Third, only gradients in the remaining data, indicative of a plasma patch, were admitted. Such  
277 gradients were defined as being at least 40% slopes over a distance of 140 ( $\pm 5\%$ ) km, following  
278 [Coley and Heelis, 1995]. We believe that using this distance should exclude the smaller non-  
279 patch structures within the auroral oval. Such gradients were calculated by dividing the electron  
280 concentration data into sequences covering 140 ( $\pm 5\%$ ) km, performing a linear regression on  
281 them and taking the resulting straight-line slope as  $|\nabla n|$ . Note that such sequences may overlap  
282 each other and that these slopes do not necessarily represent the steepest gradients possible on a  
283 given structure as they are only the slope in the direction of motion of the satellite. The  
284 histogram of  $|\nabla n|$  occurrence, as derived from DE2 is displayed in Figure 2.

285

286 The values of all other parameters used in this and all subsequent cases were those observed  
287 during the time periods when admissible gradients were present. Hence the subset of the DE2



288 data used plausibly represents conditions within patches. No attempt has been made to  
 289 independently verify the existence of patches at these times and places.

290 For the inertial GDI case, Eq.2 becomes

$$291 \quad \gamma_{iGDI} = \left( v_{in} \frac{E|\nabla n|}{Bn} \right)^{1/2} \quad (22)$$

292 For the collisional, short wavelength CCI, Eq.6 becomes

$$293 \quad \gamma_{swcCCI} = \frac{k_z}{k_y} \left( \frac{qE|\nabla n|}{nm_i v_{in}} \right) \left\{ 1 + \left( \frac{k_z}{k_y} \right)^2 \left( \frac{q^2 B^2}{m_i m_e v_{in} v_{ei}} \right) \right\}^{-1} \quad (23)$$

294 For the inertial, short wavelength CCI, Eq.8 becomes:

$$295 \quad \gamma_{swiCCI} = \left( \frac{v_{ei} m_e |\nabla n|^2 E^2}{4m_i n^2 B^2} \right)^{1/3} \quad (24)$$

296 For the KHI, Eq.18 becomes

$$297 \quad \gamma_{KH} = \frac{k(n_1 n_2)^{1/2}}{(n_1 + n_2)} \left[ \frac{2B^2}{\mu_0(m_i + m_e)} \left( \frac{1}{n_1} + \frac{1}{n_2} \right) - \left( \frac{E}{B} \right)^2 \right]^{1/2} \quad (25)$$

298 with  $n_1$  and  $n_2$  taken as the maximum and minimum figures in the electron concentration used to  
 299 calculate  $|\nabla n|$ .

300 In Eqs.21-25, inclusive, the parameter,  $E$ , refers to the quasi-D.C. measurements of the electric  
 301 field. For the two Turbulence equations, the A.C. component is required. This was measured by  
 302 DE2 in the range 4Hz-1024Hz across eight channels, so the integral over the measured region  
 303 becomes  $\sum_{k=2\pi/1024}^{2\pi/4} E(k)^2$  taking Eq.20 into account for each  $E(k)$  before summation.

304 Eq.10, for the collisional turbulent growth rate becomes

$$305 \quad \gamma_{cT} = \left( \sum_{k=2\pi/1024}^{2\pi/4} E(k)^2 \right)^{1/2} \left( \frac{|\nabla n|}{nB} \right) \quad (26)$$

306 For the inertial turbulent regime, Eq.11 becomes

$$307 \quad \gamma_{iT} = \left\{ v_{in} \left( \sum_{k=2\pi/1024}^{2\pi/4} E(k)^2 \right)^{1/2} \left( \frac{|\nabla n|}{nB} \right) \right\}^{1/2} \quad (27)$$

308

309 The ideal approach to exploring the range of values of the growth rates for each process is to  
310 calculate a value of  $\gamma$  for every possible combination of the necessary input measurements (e.g.  
311 the Magnetic and Electric field data as summarized in Figures 5-7). However, given the subset of  
312 DE2 data selected this would become unmanageably large. Hence, in order to handle the number  
313 of output values of  $\gamma$  in a sensible time it was necessary to take representative samples of the full  
314 data sets of each input parameter. The method of simple random sampling was adopted, using  
315 the following equation to determine the minimum sample size,  $S$ , required:

316

$$317 \quad S = p/[1 + p/P] \quad (28)$$

318 Where  $p = Z^2/(4M^2)$ ,  $M$  is the desired margin of error expressed as a fractional percentage,  $P$   
319 is the size of the population being sampled and  $Z$  is a factor chosen dependent on the required  
320 confidence limit. The practical memory constraint led to the best possible sampling regime of a

321 95% confidence limit, corresponding to  $Z = 1.95$ , and a margin of error of 9% ( $M = 0.09$ )  
322 leading to a sample size of ~116 for each parameter (as given in Table 2).

323

#### 324 **4. Results**

325

326 In general there are two sources of error relating to these results: instrument error and sampling  
327 error. The former applies to all the basic input measurements and introduces some level of  
328 uncertainty in their values; these are then combined when the calculation is made, generating an  
329 over-all level of uncertainty that could be estimated from the individual uncertainties. The  
330 second arises since, instead of calculating gamma for every possible combination of input  
331 measurements (a practical impossibility) a representative sample of each input population has  
332 been used, instead. Again, an overall uncertainty due to this sampling could be calculated and  
333 combined with the instrumental error. However there is a third source of error relating  
334 specifically to the electric and magnetic fields. These have been taken as their full-field  
335 magnitudes when, more rigorously, the horizontal and vertical components, respectively, should  
336 be used. This introduces an over-estimating bias in both of these measurements. Finally, the  
337 approximation necessitated by the failure of the z-axis Langmuir probe to deploy leads to an  
338 error in the electric field magnitude such that the values used can only be considered accurate to  
339 order-of-magnitude. This final source of error swamps the others. Hence, all values of  $\gamma$   
340 presented below should be considered to be only order-of-magnitude accurate.

341

342 In [Carlson *et al.*, 2007] evidence for a rise-time ( $1/\gamma$ ) of 60s or less is presented for patches  
343 still in the cusp region. Hence, in the following the various growth rate mechanisms are  
344 compared to find which can give values for  $\gamma > 1/60$  and under what circumstances. The  
345 percentage of derived growth rates (using the sample data) exceeding,  $1/6$ ,  $1/60$  and  $1/600$  for  
346 each of the four processes are presented in Table 3. All processes except Kelvin-Helmholtz  
347 Instabilities (KHI) are found capable of giving rise-times less than 60s using the DE2 data. For  
348 collisional Gradient Drift and shortwave inertial Current Convective instabilities this occurs less  
349 than 1% of the time, but occurs for the majority of the time for inertial Turbulence instabilities  
350 and around 10% of the time for inertial Gradient Drift and collisional Turbulence and shortwave  
351 Current Convective instabilities.

352

## 353 **5. Conclusions**

354 The derived distributions of possible linear growth-rates for each mechanism show that only  
355 Turbulence, inertial GDI and shortwave collisional CCI would regularly give the rise-times of  
356 approximately 60s or less observed in the cusp region during patch formation [e.g. Carlson *et al.*  
357 *et al.*, 2007 and references there-in]. However, the relative importance of the various mechanisms  
358 could be significantly different in the non-linear regime [Gondarenko, and Guzdar, 2006;  
359 Gondarenko and Guzdar, 2004a; Gondarenko *et al.*, 2003; Gondarenko and Guzdar, 1999;  
360 2004b; Guzdar *et al.*, 1998]. In this regard, the linear regime assumes the instability grows  
361 exponentially in amplitude, at the growth rate  $\gamma$  given by the above. Whilst there are various  
362 mechanisms that can drive an instability, one possibility is an increasing velocity shear,  $\delta V$  (due  
363 to an exponentially increasing perturbation in electric field,  $\delta E = \delta E_0 e^{\gamma t}$ ) which over time could

364 become large enough to drive secondary, Kelvin-Helmholtz Instabilities (KHI) that damp the  
 365 growth of the instability, ending the linear growth regime. Based on Eq. 19, taking  $n_1 = n + \delta n$ ,  
 366  $n_2 = n - \delta n$  (where  $n$  is the background electron density) and making the not unreasonable  
 367 assumptions that  $n^2 \gg \delta n^2$  and  $m_i + m_e \approx m_i$ , this occurs for the ordinary KHI when  $t > t_c$   
 368 where

$$369 \quad t_c \sim \left(\frac{1}{\gamma}\right) \ln \left(\frac{2B^2}{\delta E_0} \sqrt{\frac{1}{\mu_0 n m_i}}\right) \quad (28)$$

370 Using the sample mean values for  $B$ ,  $E$  and  $n$  this would indicate that the linear regime would  
 371 likely last for a duration of order  $10/\gamma$ . This would indicate that grow rates greater than  $1/6$   
 372 would imply that the mechanism becomes non-linear within minutes, whereas growth rates less  
 373 than  $1/600$  would take several hours for the mechanism to become unstable.

374

375 There are two limitations with regard to the method deployed here for comparing growth-rates  
 376 for candidate irregularity generating mechanisms associated with polar-cap plasma patches that  
 377 cannot easily be overcome. First, the data are concentrated at the peak of solar-cycle 21 (late  
 378 1981 – early 1983) and therefore do not represent a whole solar cycle. Second, there is a tacit  
 379 assumption that all the input variables in the growth-rate equations are uncorrelated with all of  
 380 the others. This may not be entirely accurate, especially with regard to the electric and magnetic  
 381 fields and the electron concentration and its gradient.

382

383 Because the output values of growth rate are considered accurate only to order of magnitude, the  
384 relatively limited sampling of the populations is not considered a significant draw-back. Nor is  
385 the use of full field values of the electric and magnetic fields or the approximation made in order  
386 to obtain values of electric field strength in the absence of z-axis data.

387

388 It is remarkable that under the conditions selected as representative of patches, the A.C.  
389 component of the electric field is often larger than the quasi-D.C. component. This implies that  
390 the Turbulence process can be a cause of scintillation on its own and that all slopes of a patch  
391 can, in the right circumstances, be sufficiently unstable to cause measurable phase scintillation.  
392 In the past it has been assumed that patches showing irregularities or scintillation through-out all  
393 regions, rather than just on the trailing edge had undergone the GDI to such an extent that the  
394 irregularities had penetrated throughout the patch having started forming only on the trailing  
395 edge. The present results show that the same situation could be obtained by the action of the  
396 Turbulence process on all slopes, with irregularities forming on the entire circumference and  
397 working towards the centre. In this situation the maximum irregularity amplitude need only be  
398 the radius of the patch, rather than the entire diameter. This mechanism would therefore appear  
399 at first glance to take approximately half the time to cause irregularities to form through-out an  
400 entire patch. In fact, because the electric field is fluctuating in magnitude and direction, the  
401 growth rate in any one particular direction should be halved. The time to reach complete  
402 instability is still accelerated, however.

403

404 The values of  $\gamma_{GDI}$  and  $\gamma_T$  obtained suggest that irregularities should be observed in association  
405 with most patches. This is not backed by the observational record on either count. The  
406 explanation arises from the use here of local, linear theory to obtain the growth-rate equations  
407 used. Non-local, 3-dimensional, non-linear theory tends to strongly reduce growth-rate values  
408 and introduces wavelength dependencies if none were present in the local, linear theory [e.g.,  
409 *Gondarenko et al.*, 2003; *Gondarenko and Guzdar*, 1999; 2001; 2004a; 2004b; 2006a; 2006b;  
410 *Guzdar et al.*, 1998; *Kelley*, 2009]. It is possible, that results may differ if non-linear processes  
411 dominate.

412

413 This does not affect the main conclusion that the KHI is not important as it was negligible to start  
414 with. However, these results are based on the statistical analysis, and thus in this context the KHI  
415 is not the main player for the patch structuring. However, these results do not exclude the  
416 situation where the KHI dominates under conditions of the strong flow shears. Nor is the  
417 conclusion that Turbulence is a process that must be taken into account affected, as its rise-time  
418 will be reduced to a similar extent to that for the GDI, but not more so. If, taking the full  
419 complexities into account, none of the processes considered here can give a rise-time less than  
420 60s, then the most probable explanation of the appearance of phase scintillation very rapidly,  
421 whilst the patch is still in the cusp, is that inhomogeneous precipitation of energetic particles into  
422 the patch as it is forming accelerates the action of the GDI and/or Turbulence processes [*Oksavik*  
423 *et al.*, 2012].

424

425 To completely understand what is happening, an extension of the work in *Gondarenko et al.*  
 426 [2003]; *Gondarenko and Guzdar* [1999; 2001; 2004a; 2004b; 2006a; 2006b] and *Guzdar et al.*  
 427 [1998] must be made so that the effects of particle precipitation during formation are included,  
 428 along with the effects of the A.C. electric field. Additionally, the patch geometry and initial  
 429 electron concentration distribution should take account of recent observations in order to be fully  
 430 realistic. (The assumption that patches are approximately circular through-out their life-time,  
 431 having been demonstrated by Ionospheric Ray Tomography to be particularly unsound [e.g., *Yin*  
 432 *et al.*, 2009].)

433

434 Further complications arise when compound processes are considered. For example GDI and  
 435 Turbulence processes will be acting on the trailing edge of the patch at the same time. For such  
 436 processes, the ratio  $\gamma_{GDI}/\gamma_T$  indicates which dominates. This is given by

437 
$$\frac{\gamma_{GDI}}{\gamma_T} = \frac{|E_{D.C.}|}{\left[ \int_{k_L}^{\infty} (E_{A.C.}(k))^2 \right]^{1/2}} \quad (29)$$

438 Hence, this can be obtained whenever simultaneous measurements of both the D.C. and A.C.  
 439 components are available. Unless one or the other (or both) is negligible, the compound action of  
 440 both will accelerate irregularity production compared to either one acting alone. This could lead  
 441 to a situation where radar back-scatter from irregularities is present throughout a patch but  
 442 stronger from the trailing edge. The relative impact of Turbulence vs. the GDI should also be  
 443 more thoroughly examined by analysis of observational data based on Eq.29 for each admissible  
 444 electron concentration gradient. In this regard, it is interesting that comparing the quasi-D.C. and  
 445 A.C. electric field strengths (Figures 6 and 7) shows that, under the conditions described for the



446 selection of the data above, the summed A.C. field is usually stronger than the quasi-D.C. field  
447 and Turbulence dominates (Figure 8).

448

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450

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455

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565

566

567 **Figure Captions**

568 Figure 1: Histogram of DE2 electron concentration data.

569 Figure 2: Histogram of the gradient of electron concentration as derived from DE2 data.

570 Figure 3: Histogram of the DE2 neutral monatomic oxygen concentration data.

571 Figure 4: Histogram of the DE2 O<sup>+</sup> ion temperature data.

572 Figure 5: Histogram of DE magnetic field strength data.

573 Figure 6: Histogram of the quasi-D.C. electric field strength data.

574 Figure 7: Histogram of the A.C. electric field data (as summed over the measured range of 4Hz-  
575 1024Hz).

576 Figure 8: The percentage of derived growth rates exceeding the given growth rate for  
577 ‘turbulence’ (Turb) and gradient drift (GDI) in both the inertial and collisional regimes. The  
578 inertial turbulent regime is most likely to exceed any given growth rate and is therefore the more  
579 important.

580

581