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## FOCUS REVIEW

WIREs Computational Molecular Science

# Exploring High-Dimensional Free-Energy Landscapes of Chemical Reactions

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Molecular dynamics (MD) techniques are widely used in computing free-energy changes for conformational transitions and chemical reactions, in particular, to study such processes in condensed matter systems. Most of the MD-based approaches employ biased sampling of *a priori* selected coarse grained coordinates or collective variables (CV) and thereby accelerating otherwise infrequent transitions between different free-energy basins. A quick convergence in free-energy estimations can be achieved by enhanced sampling of large number of CVs. Conventional enhanced sampling approaches become exponentially slower with increasing dimensionality of the CV-space, and thus they turn out to be highly inefficient in sampling high-dimensional free-energy landscapes. Here we focus on some of the novel methods that are designed to overcome this limitation. In particular, we discuss four methods: bias exchange metadynamics, parallel bias metadynamics, adiabatic free-energy dynamics/temperature accelerated MD, and temperature accelerated sliced sampling. The basic idea behind these techniques are presented and the applications using these techniques are illustrated. Advantages and disadvantages of these techniques are delineated.

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**Abbreviations:** MD, Molecular Dynamics; AIMD, Ab Initio Molecular Dynamics; CV, Collective Variables; BEMetaD Bias Exchange Metadynamics; PBMetaD, Parallel Bias Metadynamics; AFED, Adiabatic Free Energy Dynamics; TAMM, Temperature Accelerated Molecular Dynamics; TASS, Temperature Accelerated Sliced Sampling

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**KEYWORDS**

Free-energy calculations, Enhanced sampling, Bias Exchange Metadynamics, Parallel-Bias Metadynamics, Adiabatic Free-Energy Dynamics, Temperature Accelerated Sliced Sampling

**1 | INTRODUCTION**

Free-energy changes along the reaction coordinate of a chemical reaction manifests the feasibility of the process at a given temperature. Reaction coordinate,  $\chi$ , on the other hand, can be an intricate function of nuclear coordinates even for a simple elementary reaction. To simplify,  $\chi$  can be written as a linear combination of several coarse grained coordinates or collective variables (CV),  $\mathbf{S}$ , as,

$$\chi(\mathbf{R}) = \sum_i c_i S_i(\mathbf{R}) ,$$

where  $\mathbf{R}$  is the set of all atomic coordinates, and  $\{c_i\}$  is the set of coefficients. Computing the free-energy landscape  $F(\mathbf{S})$  and finding the lowest free-energy path  $\chi(\mathbf{S})$  on this landscape could provide valuable information regarding the mechanism and kinetics of the reaction.[1, 2] Free-energy calculations using molecular dynamics (MD) simulations are widely used for this purpose, and is the most preferred approach while dealing with soft matter systems. MD based sampling enables one to account for entropic contributions, going beyond the standard quantum-harmonic approximations.

In order to compute  $F(\mathbf{S})$ , it is important that all the relevant conformational states for a given  $\mathbf{S}$  is sampled in MD simulations.[1, 2, 3, 4, 5, 6] On the other hand, probability ( $P(\mathbf{R})$ ) to visit a conformational state  $\mathbf{R}$  at temperature  $T$ , is proportional to  $e^{-\beta U(\mathbf{R})}$ , where  $U(\mathbf{R})$  is the potential energy,  $\beta = 1/(k_B T)$  and  $k_B$  is the Boltzmann constant. As a result, high potential regions are less visited or never visited compared to low-potential energy parts of the potential energy landscape in a finite length MD trajectory. Thus barrier crossing on a potential energy landscape turns out to be an infrequent or "rare" event in MD simulations. Even moderately (i.e. only a few  $k_B T$ ) high potential energy regions can be insufficiently sampled, resulting in poor statistics.

This problem can be alleviated by modifying the potential energy surface by adding a bias potential.[2] If the potential energy of the low-potential regions is raised, the barrier crossing events are accelerated. In such biased-sampling simulations, the probability of visiting  $\mathbf{R}$  gets modified as,

$$\tilde{P}(\mathbf{R}) \propto e^{-\beta[U(\mathbf{R})+V^b(\mathbf{S})]} .$$

Here  $V^b(\mathbf{S})$  is the bias potential added along a selected set of CVs or all the nuclear coordinates. Alternative way to speed-up the exploration of potential energy landscape is by increasing temperature  $T$  (i.e., by decreasing  $\beta$ ).

For the case of time-independent bias potential  $V^b(\mathbf{s})$ , the biased probability distribution of CVs,  $\tilde{P}(\mathbf{s})$ , is related to  $P(\mathbf{s})$  as,[7]

$$P(\mathbf{s}) = \tilde{P}(\mathbf{s}) e^{\beta V^b(\mathbf{s})} ,$$

where

$$\tilde{P}(\mathbf{s}) \equiv \left\langle \prod_i \delta(S_i(\mathbf{R}) - s_i) \right\rangle_{V^b},$$

and  $\langle \dots \rangle_{V^b}$  denotes the ensemble average from the biased MD simulation. Now, from  $P(\mathbf{s})$ , free-energy surface can be computed as,

$$F(\mathbf{s}) = -\beta^{-1} \ln P(\mathbf{s}) . \quad (1)$$

Free-energy surface can be also computed based on integrating the mean-force as

$$\Delta F(s) = \int^s ds' \left\langle \left( \frac{dF}{ds'} \right) \right\rangle .$$

Biased sampling techniques use different ways to obtain  $V^b(\mathbf{s})$  that compensates the underlying free-energy landscape. For e.g. metadynamics[8, 9] constructs the bias potential as a function of time by a time-dependent update of the bias, while umbrella sampling[7] (US) uses time-independent biases to compute  $P(\mathbf{s})$  directly. The bias potential is self-consistently obtained in recently developed variational enhanced sampling method.[10] Blue-moon ensemble[11] and Adaptive Bias Force methods (see Ref.[12] and references therein) are two examples which use the biased/unbiased mean-forces to compute free-energy.[2] In adiabatic free-energy dynamics (AFED) [13]  $P(\mathbf{s})$  is calculated directly from the high-temperature dynamics of CVs.

Alternatively, equilibrium probability distribution and free-energies can be computed using replica-exchange based global-tempering approaches.[2, 14, 15, 16, 17, 18] In the widely used parallel-tempering approach,[19] exploration of the potential energy landscape is enhanced in a high-temperature replica, while a low-temperature replica exchanges its coordinates with a higher-temperature replica with certain probability. The advantage of global tempering simulations is that *a priori* assumption of CVs is not necessary. Readers are directed to authoritative books[2, 1, 20] and reviews on various sampling methods for further details.[21, 6, 5, 22, 3, 23]

Other than the requirement of *a priori* selection of CVs, the major limitation of the CV-based approaches is its exponentially decreasing computational efficiency with increase in the dimensionality of the CV space. When modeling an elementary reaction, free-energy surface for the process can be often expressed with one or two collective coordinates in a way that free-energy of all the reactant states, transition state and product states can be obtained.[2] However, enhanced sampling of one or two CVs may not be sufficient to compute free-energies accurately, especially for processes in soft-matter systems. This arises from the fact that transverse degrees of freedoms are unbiased and their sampling is slow due to finite barriers prevailing in the orthogonal directions. Therefore, including more orthogonal CVs is beneficial for obtaining reliable free-energy estimates from short MD simulations. Requirement of methods that could enhance the sampling of perpendicular coordinates without loosing the efficiency of the simulation is now comprehensible. This review focuses on four such methods, which are designed to sample large number of CVs efficiently and have been already demonstrated for modeling rare-events in soft matter systems with more than 3 CVs.

## 2 | BIAS EXCHANGE METADYNAMICS

Metadynamics approach uses a time dependent bias potential to enhance the sampling of the configurational space.[24, 9] Readers can refer to a number of reviews on the topic.[25, 26, 27, 28, 29, 22, 30, 21] The bias potential has the form

$$V^b(\mathbf{S}, t) = \sum_{\tau < t} w(\tau) \exp \left[ -\frac{(\mathbf{S} - \mathbf{S}_\tau)^2}{2 (\delta s)^2} \right]$$

which is the sum of Gaussian functions deposited along the trajectory of  $\mathbf{S}$  at discrete time  $\tau$ . Here,  $w$  is the height of the Gaussian (in the units of energy) and  $\delta s$  is the width parameter. The Lagrangian for performing metadynamics is

$$\mathcal{L}^{\text{MTD}}(\mathbf{R}, \dot{\mathbf{R}}) = \mathcal{L}_0(\mathbf{R}, \dot{\mathbf{R}}) - V^b(\mathbf{S}, t) ,$$

where  $\mathcal{L}_0$  is the unbiased Lagrangian of the system. The bias potential  $V^b$  that compensates the underlying potential is gradually built along the trajectory of CVs. As the bias flattens the free-energy basin, the system exits from one free-energy basin to the other. Most importantly, in metadynamics, the free-energy surface can be computed from the bias potential itself, as

$$F(\mathbf{S}) = -V^b(\mathbf{S}, t \rightarrow \infty) + \text{constant} .$$

In a simple metadynamics procedure the Gaussian parameters  $w_\tau$  and  $\delta s$  are fixed. However, there are procedures to change these parameters adaptively for obtaining proper convergence in free-energy estimates. [31, 32] Most importantly, the well-tempered version of metadynamics scales  $w(\tau)$  based on the underlying bias potential  $V^b$  at time  $\tau$ : [31]

$$w(\tau) = w(0) \exp \left( -\frac{V^b(\mathbf{S}, \tau)}{k_B \Delta T} \right) ,$$

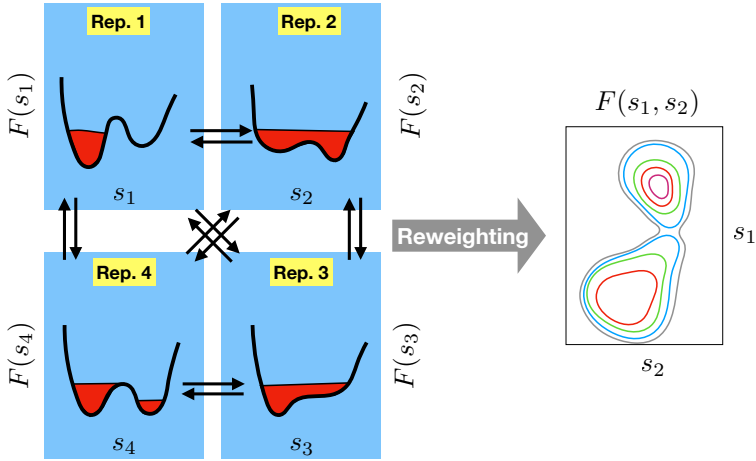
where  $w(0)$  is initial Gaussian height and  $\Delta T$  is the tempering parameter. In well-tempered metadynamics, free-energy can be computed as [31, 33]

$$F(\mathbf{S}) = -\gamma V^b(\mathbf{S}, t \rightarrow \infty) + \text{constant},$$

where  $\gamma = (T + \Delta T) / \Delta T$ .

In principle, the method requires no modification to sample large number of CVs. However, the number of Gaussian functions require to build the bias that compensates the underlying free-energy surface increases exponentially with the system size. In practice, metadynamics is used to sample low dimensional landscapes, most often using 2 CVs, rarely with 3 CVs, and in some special cases even higher; [27] see also Ref. [34].

In order to improve the efficiency of metadynamics in sampling high-dimensional free-energy surfaces, bias-exchange metadynamics (BEMetaD) approach was proposed by Piana and Laio.[35] In this approach,  $M$  number of replicas of the system at same temperature are initiated, and in each of these replicas, different small number of CVs are enhance-sampled using metadynamics bias built independently in each replica. Exchanges between randomly chosen two replicas are then attempted at regular time intervals, as in the case of other replica exchange MD schemes; see Figure 1. Each replica samples one or two dimensional CV space, therefore sampling a high-dimensional space becomes



**FIGURE 1** A sketch demonstrating the basic idea behind the BEMetaD method. Here the arrows are showing exchanges between two randomly selected replicas, which are attempted frequently. The bias added is shown in red. A reweighting procedure could be used to reconstruct a high-dimensional free-energy surfaces.

highly efficient. By the virtue of this, the efficiency of sampling doesn't deteriorate exponentially with the number of CVs.

Exchange between two replicas  $m$  and  $n$  are made with the probability  $P_{m,n}$  using the Metropolis-Hastings scheme, where

$$P_{m,n} = \min(1, \exp[\beta \Delta_{m,n}])$$

and

$$\begin{aligned} \Delta_{m,n} = & V_m^b[S_m(\mathbf{R}_m), t] - V_m^b[S_m(\mathbf{R}_n), t] \\ & + V_n^b[S_n(\mathbf{R}_n), t] - V_n^b[S_n(\mathbf{R}_m), t] . \end{aligned}$$

A later work by Galvelis and Sugita[36] has shown that exchange rates between two replicas and the convergence of free-energies can be expedited by using infinite swapping or the Suwa-Todo (ST) algorithms, replacing the Metropolis-Hastings scheme.

Reconstructing the high-dimensional free-energy surface requires appropriate reweighting; see Refs. [35, 37] for details. The unbiased probability contribution due to the bias from a replica  $h$  can be written as

$$P_h(\mathbf{s}) = \left\langle \prod_i \delta(S_i - s_i) e^{\beta \left[ \sum_h V_h^b(S_h) - f_h \right]} \right\rangle .$$

Here,  $\bar{V}_h^b(S_h)$  is the average bias potential in replica  $h$ , given by

$$\bar{V}_h^b(S_h) = \frac{1}{t_{\text{final}} - t_{\text{ini}}} \int_{t_{\text{ini}}}^{t_{\text{final}}} dt V_m^b(S_h, t)$$

where the reweighting is done for a time interval  $t_{\text{ini}}$  and  $t_{\text{max}}$  during which the average bias potential only increases uniformly across the domain of  $\mathbf{S}$  of our interest. In the above,  $f_h$  is some constant, and has to be determined. Now, using the weighted histogram analysis method[38] (WHAM) one can combine  $\{P_h(\mathbf{s})\}$  to get the total reweighted probability density  $P(\mathbf{s})$ , and hence the free-energy  $F(\mathbf{s})$ . A detailed review of the method and other technical details can be found in Ref. [37]. Laio and co-workers have also designed a visual interface program for reweighting and analysis of PBMetaD simulations.[39] Another simpler approach for reweighting was suggested by Yu and Lin [40], where a standard time-independent reweighting is done using the converged free-energies  $F_h(S_h)$ .

Alternatively, time dependent bias can be directly used for reweighting following the works of Tiwary and Parrinello. [6] Here,

$$P_h(\mathbf{s}) = \left\langle \prod_i \delta(S_i - s_i) e^{\beta [V_h^b(S_h, t) - c_h(t)]} \right\rangle. \quad (2)$$

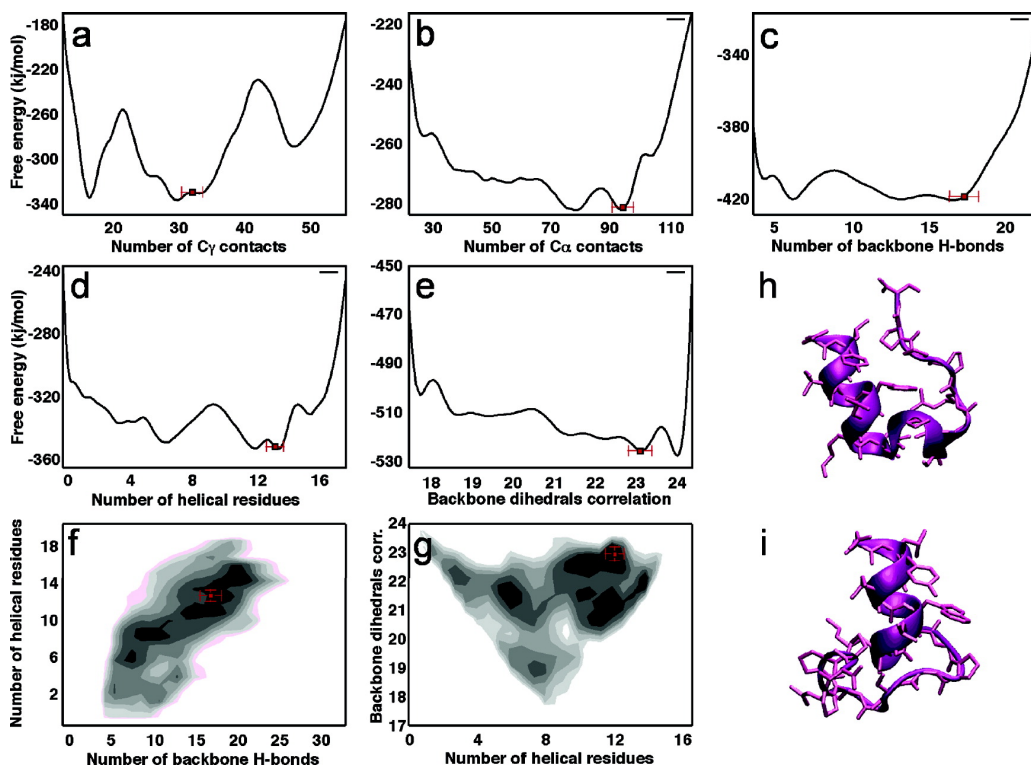
where  $c_h(t)$  is a time dependent constant, given by

$$c_h(t) = \beta^{-1} \ln \left[ \frac{\int dS_h e^{\beta \gamma V_h^b(S_h, t)}}{\int dS_h e^{\beta (\gamma-1) V_h^b(S_h, t)}} \right]$$

considering that a well-tempered bias potential is used. Employing WHAM, one can then combine the reweighted free-energy surfaces from each replica  $h$ , similar to the procedure used by Awasthi et al. [41]. It is noted that the WHAM approach for combining the distributions of different replicas can only work if the distributions have enough overlap.

A number of applications using BEMetaD in studying biological systems can be found in the literature. Piana and Laio [35] employed 5 CVs to study the folding of Trp-Cage in explicit water. They used number of  $C_\gamma$  contacts (CV1), number of  $C_\alpha$  contacts (CV2), number of backbone H-bonds (CV3), number of backbone  $\psi$  dihedrals within the  $\alpha$ -domain of the Ramachandran map (CV4), and correlation between the successive  $\psi$ -dihedral angles (CV5). These simulations were performed with 8 replicas, where 5 replicas were using one-dimensional biases to sample one of the five CVs. Two replicas were using a two-dimensional bias to sample (CV3,CV4) and (CV4,CV5) CV-space. The last replica was a neutral one, i.e. without any bias, and it was permitted to exchange with other walkers. The neutral replica was used to monitor the convergence, which in principle should result in a canonical distribution. In their work, within 20 ns, convergence in free-energy was observed. Free-energy profile along different CVs are given in Figure 2. The trajectories from these simulations have been used to perform cluster analysis and the folding kinetics has been obtained.[42]

A number of different problems have been studied by BEMetaD. For sampling various conformations of chromophores attached to a protein, Delor et al.[43] used BEMetaD. Structural changes in RNA nucleotides and ligand binding were studied using this approach by Mlýnský and Bussi.[44] BEMetaD was used for investigating more complex problems like DNA G-Quadraplex [45] folding, and formation of RNA pseudoknot[46]. Ligand and drug association and dissociation studies in proteins [47, 48, 48, 49, 50, 51, 52, 53, 54], peptides [55] and lipids[56] and conformations of protein:ligand complex[57] have been also carried out using this method. BEMetaD simulation of ion binding in RNA [58] has been recently reported. A number of studies used BEMetaD to study protein folding. [59, 60, 61, 62, 63, 64, 65, 66, 67] Literature of BEMetaD also includes conformational sampling in  $\alpha$ -helical



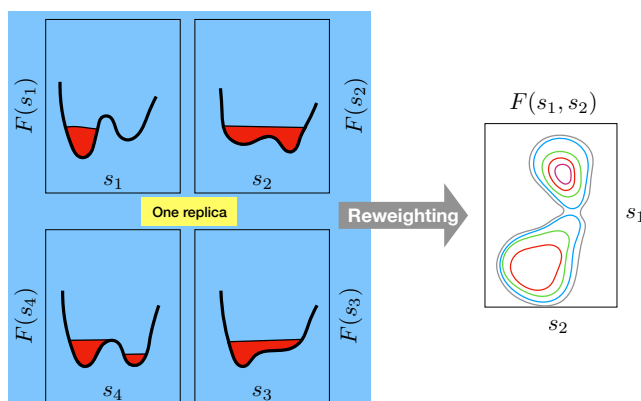
**FIGURE 2** (a-g) Free-energy profiles along different CVs used in the BEMetaD simulation of Trp-cage protein folding.[35] These free-energy profiles are made based on the metadynamics bias constructed in each replica; Figures (h,i) are the structures of the folded and the "pseudo-folded" states of the protein. Reprinted with permission from *J. Phys. Chem. B* 2007;111:4553 Copyright (2018) American Chemical Society



glycoproteins [68], Bovine Chymosin [69], peptides [70, 40, 71], conformational sampling of intrinsically disordered as well as other proteins [72, 73, 74, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90], conduction through ion channels [91, 92, 93, 94, 95], and protein aggregation. [96, 97, 98] The method has also helped to resolve the structure of large and complex systems like protein-RNA complex [99], and membrane inserted influenza fusion peptide [100]. Clearly, a substantial number of complex biophysical problems have been addressed by the approach.

One of the major limitations of this approach is the requirement of the replica-exchange. Care should be given to achieve a proper overlap of probability distributions between the replicas. These limit BEMetaD computations to be used for studying chemical reactions in *ab initio* molecular dynamics (AIMD) where computationally expensive first-principle based QM forces are used to propagate the atomic motion. Study of chemical reactions using BEMetaD and AIMD has not been reported so far.

### 3 | PARALLEL BIAS METADYNAMICS



**FIGURE 3** Sketch showing the working of PBMetaD. Here, low-dimensional free-energy surfaces are sampled parallelly within the same replica. Gaussian height of the bias added along one CV is scaled according to the bias added along other CVs. Reweighting methods can recover the high-dimensional free-energy landscapes.

Another variant of metadynamics method called the Parallel Bias metadynamics (PBMetaD)[101] alleviates some of the limitations of BEMetaD. In this method low-dimensional (usually one-dimensional) biases are added along CVs concurrently. Only one replica of the system is considered. To ensure that the one-dimensional bias potentials added on different one-dimensional CVs converge to the correct free-energy, bias potential along each CV is dynamically scaled. The Gaussian height at a time  $\tau$  for a CV  $i$  is computed as

$$w_i(\tau) = w_i(0) \exp\left(-\frac{V_i^b(s_j, \tau)}{k_B(\Delta T)_i}\right) p_i(\tau)$$

with

$$\rho_i(\tau) = \frac{\exp(-\beta V_i^b(s_i, \tau))}{\sum_i \exp(-\beta V_i^b(s_i, \tau))}$$

Here  $V_i^b(s_i, \tau)$  is the total bias for a CV  $i$  at a time  $t$ . These biases are constructed in the same way as in the conventional well-tempered metadynamics. The effective bias acting on the system at a time  $t$  is

$$V_{\text{PB}}^{\text{bias}}(\mathbf{s}, t) = -\beta^{-1} \ln \left[ \sum_i \exp(-\beta V_i^b(s_i, t)) \right] + V_0$$

where  $V_0 = \beta^{-1} \ln 2$  is added to avoid negative bias. Free-energy along a CV  $s_i$  can be computed as

$$F(s_i) = -\gamma \lim_{t \rightarrow \infty} V_i^b(s_i, t) .$$

High-dimensional free energy surfaces can be also reconstructed by reweighting the trajectory from a fixed-bias simulation or employing the the Tiwary-Parrinello[6] reweighting (with appropriate modifications) using the dynamic bias  $V_{\text{PB}}^b(\mathbf{s}, t)$ .

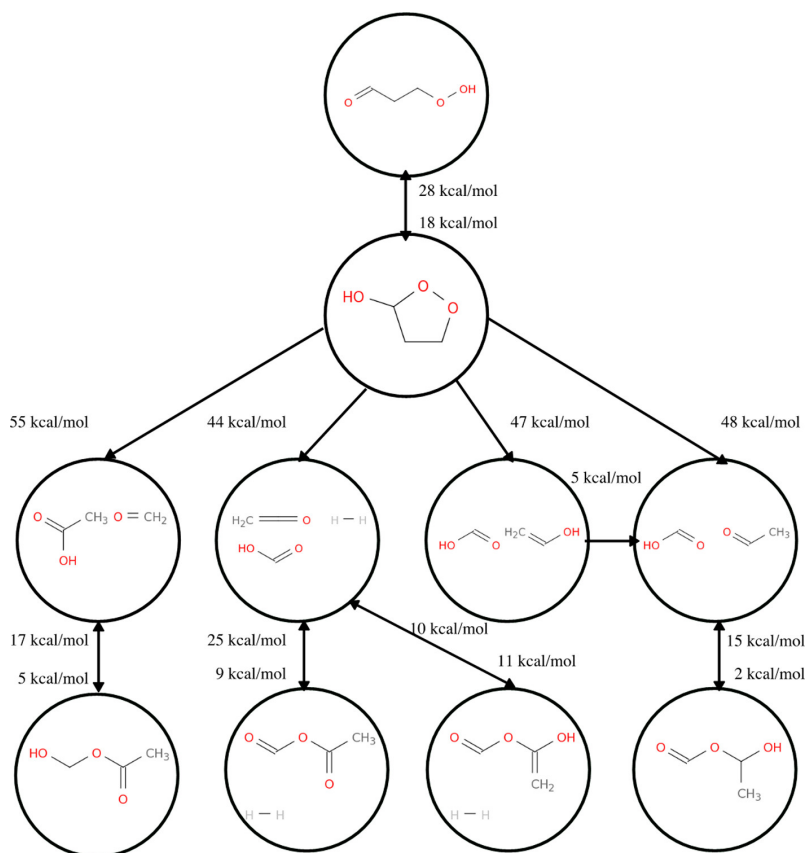
The major advantage compared to BEMetaD is that only one-replica is used for biasing more than one CVs. Especially, replica exchange is avoided in the approach.

Pfaendtner and Bonomi have used this approach in studying the conformational changes in the Tryp-cage protein with implicit solvent.[101] Authors have used six CVs with each CV being biased with one-dimensional bias potentials. The CVs chosen were number of  $C_\gamma$  contacts, number of backbone H-bonds,  $\alpha$ -helicity,  $\beta$ -similarity, correlation between the successive backbone dihedral angles, and radius-of-gyration. They compared the performance of the method with BEMetaD and it was found that the free-energy convergence behavior of PBMetaD is as good as BEMetaD. BEMetaD together with the Metadynamic Metainterface method was used to explore the structural ensembles of ligand-association in a disordered protein.[102, 103] Conformational sampling of peptoids at the hydrophobic and hydrophilic surface-water interface was modeled by Prakash et al.[104]

Recently, PBMetaD was used to obtain the reaction network of decomposition of  $\gamma$ -ketohydroperoxid.[105] In this work, Fu and Pfaendtner used the SPRINT (social permutation invariant) collective coordinates[106] as CVs for sampling different reaction pathways. SPRINT coordinates allows one to explore the potential energy landscape and the reaction pathways with least chemical knowledge and input. On the other hand, one SPRINT CV per atom is required and thus for a reasonably large system, the number of coordinates become very large and efficient sampling by conventional approaches become difficult. Since PBMetaD enables parallel sampling of one-dimensional CVs with one-dimensional MetaD biases, the method is well suited to sample large number of SPRINT CVs. Authors have used the PM6 method within the AMBER program to sample 12-CVs. The obtained reaction pathways were then refined using static QM calculations; see Figure 4.

## 4 | ADIABATIC FREE-ENERGY DYNAMICS AND TEMPERATURE ACCELERATED MOLECULAR DYNAMICS

Rosso et al. [13, 107, 2] proposed a very unique enhanced sampling scheme called adiabatic free-energy dynamics (AFED) that relies on temperature accelerated sampling of CVs. In AFED, enhanced sampling of CVs is achieved by

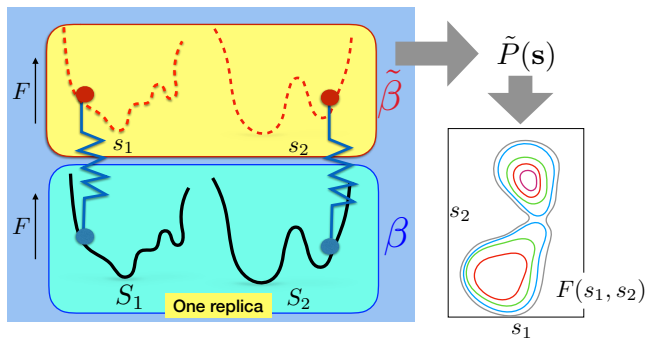


**FIGURE 4** Reaction pathways of  $\gamma$ -ketohydroperoxid explored by PBMetaD.[105] Reprinted with permission from J. Chem. Theory Comput. 2018;14:2516 Copyright (2018) American Chemical Society.

introducing high temperature  $\tilde{T}$ , such that  $\tilde{T} \gg T_0$  for  $n$  CV degrees of freedom while the remaining degrees of freedom are maintained at the desired physical temperature  $T_0$ . In particular, the temperature  $\tilde{T}$  is chosen such that CVs can cross the high energy barriers on the potential energy landscape. It is, however crucial that energy flow from the ‘‘hot’’ CV degrees of freedom to the rest of the ‘‘cold’’ nuclear degrees of freedom is avoided. Adiabatic separation between the two subsystems is achieved by choosing a larger mass for the CV degrees of freedom compared to the rest of the nuclear degrees of freedom. Further thermostats are coupled to maintain the temperature of the two subsystems. Under the condition of adiabatic decoupling it was shown that free-energy along the CVs,  $F(\mathbf{S})$ , at  $T_0$  can be constructed directly from the probability distribution  $\tilde{P}(\mathbf{S})$  as, [13, 2]

$$F(S_1, \dots, S_n) = -\frac{1}{\tilde{\beta}} \ln \tilde{P}(S_1, \dots, S_n) + \text{constant} , \quad (3)$$

where  $\tilde{\beta} = 1/(k_B \tilde{T})$ . The advantage of this approach is that sampling efficiency does not scale exponentially with



**FIGURE 5** Basic idea behind the TAMD/d-AFED method is shown graphically. Here, auxiliary variable  $\mathbf{s}$  are introduced and are coupled with the CVs  $\mathbf{S}$  with a harmonic potential. The  $\mathbf{s}$  degrees of freedom are connected to a thermostat with inverse temperature  $\tilde{\beta}$  while the physical system coordinates  $\mathbf{S}$  are thermostatted to an inverse temperature  $\beta$ , with  $\tilde{\beta} \ll \beta$ . Free-energy of the system at  $\beta$  along the CVs can be computed directly from the probability distribution of  $\mathbf{s}$  at  $\tilde{\beta}$ .

the dimension of the CV-space, especially when the changes along the CVs are uncorrelated. However, enhance-sampling of the CV subspace from the full coordinate-space requires coordinate transformation from Cartesian to CV. Implementation of such transformation is not straightforward for many non-linear CVs and the method requires major changes in an existing MD code.

Maragliano et al. [108] alleviated the problem of coordinate transformation in AFED by introducing an extended Lagrangian scheme, like in Ref.[9], and reformulated AFED in the extended CV-space. This method is called Temperature Accelerated MD or driven-AFED (TAMD/d-AFED) [108, 109]. Here a set of auxiliary variables  $\{s_\alpha\}$  are introduced that are coupled with the CVs  $\{S_\alpha\}$  through a harmonic potential having force constant  $k_\alpha$ . The Lagrangian for TAMD/d-AFED is,

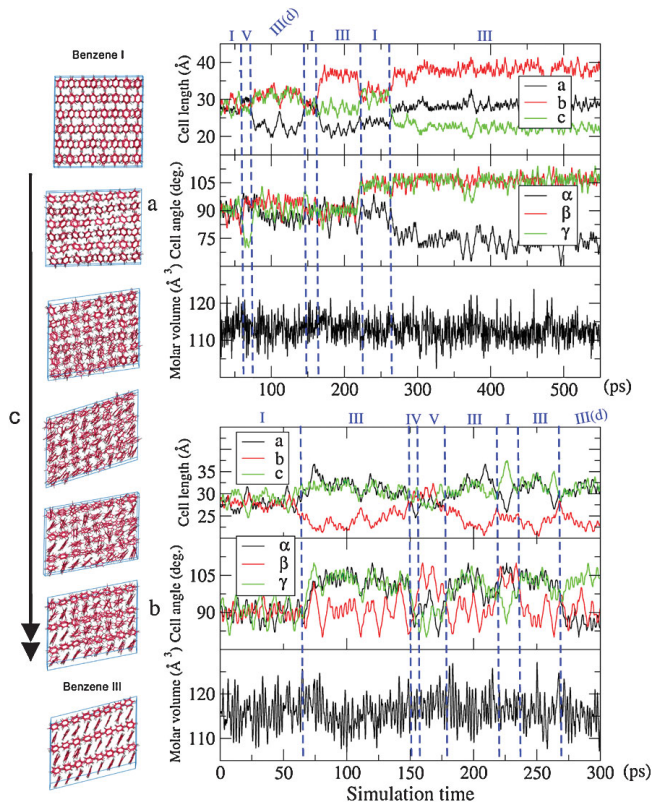
$$\mathcal{L}_{\text{TAMD}}(\mathbf{R}, \dot{\mathbf{R}}, \mathbf{s}, \dot{\mathbf{s}}) = L_0(\mathbf{R}, \dot{\mathbf{R}}) + \sum_{\alpha=1}^n \frac{1}{2} \mu_\alpha \dot{s}_\alpha^2 - \sum_{\alpha=1}^n \frac{k_\alpha}{2} (S_\alpha - s_\alpha)^2 . \quad (4)$$

Here, the auxiliary subsystem  $\{s_\alpha\}$  is thermostatted to a high-temperature  $\bar{T}$ , while the physical system is thermostatted to a much lower temperature  $T_0$ . The mass for the auxiliary variables ( $\mu_\alpha$ ) is taken to be much larger than the atomic masses in the system to ensure adiabatic decoupling of the auxiliary variables from the rest of degrees of freedom. Tuckerman et al. [2, 109, 110] have shown that

$$F(s_1, \dots, s_n) = -\frac{1}{\beta} \ln \bar{P}(s_1, \dots, s_n) . \quad (5)$$

Here  $\bar{P}(s)$  is the probability distribution of  $\{s_\alpha\}$  of the auxiliary system at temperature  $\bar{T}$ .

Number of different applications using TAMD/d-AFED have been reported in the literature. Abrams et al. [112]



**FIGURE 6** Changes in the crystal structures of benzene explored by TAMD/d-AFED.[111] Reprinted figure with permission from Yu, TQ and Tuckerman, ME, Phys. Rev. Lett., 107, 015701, 2011. Copyright (2018) by the American Physical Society.

employed TAMD/d-AFED for studying large-scale conformational sampling of proteins. In this study, they considered 69 CVs to enhance the conformational transitions which involve rotational as well as translation motion of domains in HIV-1 gb120. All the CVs were thermostatted at 6 kcal/mol. For studying the conformational changes in the activation-loop of the insulin receptor kinase domain, Vashisth et al. [113] used TAMD/d-AFED. Maragliano et al. [114] and Lapelosa et

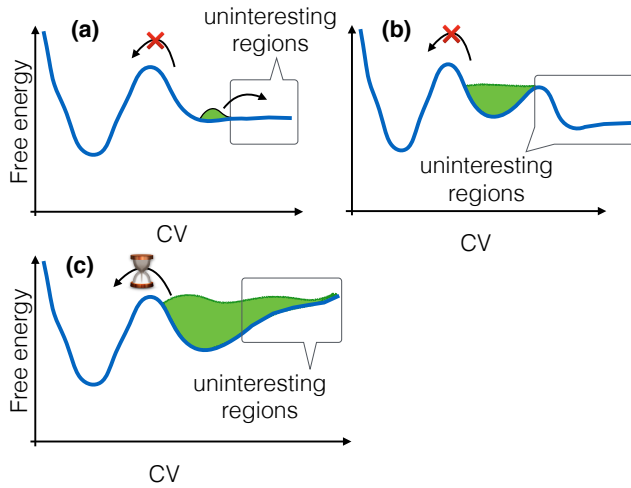
al. [115] used this method to study the CO migration in Myoglobin. Tzanov et al. [116] and Cortes-Ciriano et al. [117] used this approach to predict peptide conformations. TAMD/d-AFED and the Monte-Carlo version of TAMD were employed to study vacancy diffusion in crystals, [118] wherein very complex CVs were used such as moments computed by the quantum-mechanical (QM) probability density of a pseudo probe particle. In another interesting application of TAMD, 720 three-dimensional vectorial CVs were used to sample the conformational changes in hydrated Nafion polymeric system. [119] Yu and Tuckerman have extended the TAMD/d-AFED approach to study crystal structure changes.[111] This was achieved by using supercell vectors or  $\mathbf{h}$ -matrix elements as the CVs in a flexible-cell  $NPT$  ensemble MD simulation. This approach was shown to be very efficient in sampling crystal structures, including organic crystals.[120, 121, 122, 123] In Figure 6, TAMD/d-AFED trajectories exploring crystal structures of benzene at 100 K and 2 GPa are shown.[111] In that work,[111]  $\mathbf{h}$  matrix elements were used as the CVs and  $\bar{T}$  of 31000 K was taken for enhancing the conformational changes between different polymorphs of benzene. It is worth noting that TAMD/d-AFED combined with DFT based AIMD was used by Samanta et al. [122] to study the melting of high-pressure phase of  $\text{SiO}_2$ . To improve the efficiency of sampling by TAMD/d-AFED, Tuckerman and co-workers [124] integrated it with biased sampling of CVs, which they named as the Unified Free-Energy Dynamics (UFED) method. In UFED, high temperature and bias potential were simultaneously applied on all the CVs. TAMD/d-AFED and UFED methods have been used to compute accurate mean-forces and then used to optimize structures and reaction pathways on free-energy surfaces.[125, 126] These techniques were also used to compute free-energy differences between two conformations or structures by combining with alchemical free-energy perturbation methods [127, 128] and by calculating free-energies along an arbitrary pathway which connects two conformations.[129]

## 5 | TEMPERATURE ACCELERATED SLICED SAMPLING

In many chemical reactions, broad and unbound free-energy surfaces can be seen along the crucial “reactive” CVs; see Figure 7. Ideal examples include free-energy profile for A+B type reaction (along A-B distance), drug binding (along drug-active site distance), and protein-folding (along end-to-end distance). As a result, the system will be driven towards uninteresting regions of the free-energy landscape during the enhanced sampling simulations. Thus, the reaction of interest may not be observed or might require long MD simulations. This issue becomes more serious while modeling chemical reactions using AIMD, since the free-energy estimations with AIMD have to be carried out within few tens of picoseconds.

Methods based on metadynamics and TAMD/d-AFED suffer from this problem. A controlled sampling of CVs is crucial to overcome this limitation. This could be achieved by US [7] where the CVs are restrained at different CV positions, and probability along the CV is obtained by combining the biased-probabilities from different umbrella-windows using WHAM [130, 38] or other methods.[131, 2] However, standard US is often performed using one CV. In that case, transverse coordinates may relax slowly leading to slow converge of free-energy estimates, as discussed earlier.

To overcome this problem, Awasthi et al. combined US with metadynamics (which we termed as “well-sliced metadynamics”), where the CV along which a flat unbound free-energy surface is expected is sampled by US in a controlled manner, while the orthogonal coordinates are sampled by well-tempered metadynamics. [41] Well-sliced metadynamics approach was then extended to accommodate large-number of CVs, by combining it with TAMD/d-AFED approach.[132] This method is called Temperature Accelerated Sliced Sampling (TASS). In TASS, the following



**FIGURE 7** A cartoon showing the issues with metadynamics sampling when the free-energy surface along the crucial reactive CV is broad and unbound.[41] Reprinted figure with permission from J. Comput. Chem., 37, 1413, 2016. Copyright (2018) by the John Wiley and Sons.

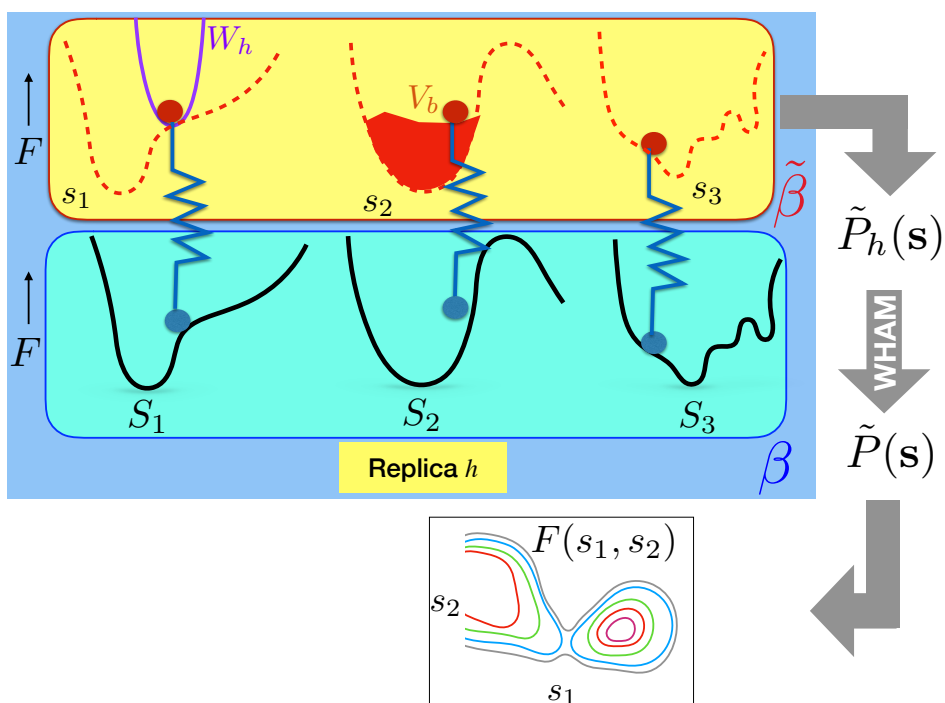
extended-Lagrangian is used:

$$\mathcal{L}_h(\mathbf{R}, \dot{\mathbf{R}}, \mathbf{s}, \dot{\mathbf{s}}) = \mathcal{L}_{\text{TAMD},h}(\mathbf{R}, \dot{\mathbf{R}}, \mathbf{s}, \dot{\mathbf{s}}) - W_h^b(s_1) - V_h^b(s_2, t)$$

where  $h = 1, \dots, M$  number of umbrella-windows are considered. The extended Lagrangian approach used here is similar to the TAMd/d-AFED method discussed in the previous section. All the auxiliary variables are coupled to a high temperature bath and nuclear degrees of freedom are thermostatted to a physically relevant colder temperature. Mass  $\mu_\alpha$  of an auxiliary variable is taken much higher than the nuclear mass to ensure adiabatic separation between the auxiliary and the nuclear subsystems. The main difference to the TAMd/d-AFED method is that, umbrella-bias  $W_h(s_1) = \frac{1}{2}\kappa_h (s_1 - s_1^0)^2$  is applied along one of the CVs, while one or more other CVs are chosen to sample by the metadynamics bias  $V^b$ . Thus for each umbrella window  $h$ , transverse CVs are enhance-sampled by both metadynamics bias as well as high-temperature. The CVs that are not biased by  $W_h$  and  $V_h^b$  are enhanced only by high temperature (as in TAMd/d-AFED). A cartoon showing the basic working principle behind the TASS method is given in Figure 8.

In this way, TASS samples a high-dimensional slice of the free-energy surface along the US coordinate. Biased probability distribution obtained from each slice  $h$ ,  $\bar{P}_h(\mathbf{s})$ , is then reweighted, as in Eqn (2), and then combined using the WHAM method; see Ref.[132, 41] for more details. As in the TAMd/d-AFED method, free-energy can be obtained using Eqn (5).

Thus, this method can be viewed as an improvement over metadynamics and TAMd/d-AFED as it can sample flat, broad, and unbound surfaces in an efficient manner, and it has the advantage that large number of transverse CVs can be sampled like in TAMd/d-AFED. TASS can also be considered as an improvisation of the US method by enabling sampling of large number of orthogonal CVs in a simultaneous manner, thus achieving quick convergence in free-energy



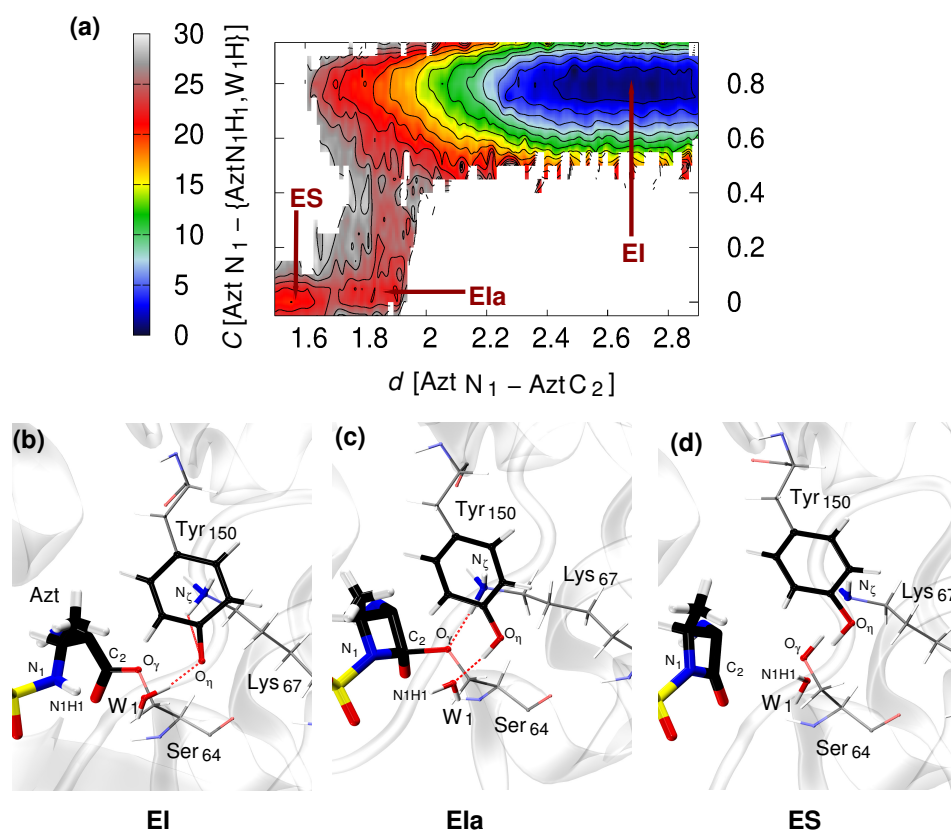
**FIGURE 8** A schematic representation on the working principle of the TASS method is shown for a case with three CVs  $s_1, s_2$ , and  $s_3$ . Note that for  $h = 1, \dots, M$  number of replicas with different umbrella bias  $W_h(s_1)$ , MD simulations are performed independently. Here metadynamics bias potential ( $V_b$ ) is applied along  $s_2$  (only). All the auxiliary variables  $\{s_\alpha\}$  are connected to a thermostat with inverse temperature  $\tilde{\beta}$  and the physical system is thermostatted to an inverse temperature  $\beta$ , with  $\tilde{\beta} \ll \beta$ .

estimates. Furthermore, TASS has the flexibility to choose different orthogonal CVs for different umbrella windows. This feature is particularly useful when studying complex chemical reactions where the crucial transverse coordinates change with the progress of the reaction along the “reactive” CV (which is the US CV in most of the cases).

Awasthi and Nair have showed the applicability of the method for computing free energy surfaces of chemical reactions in AIMD and hybrid QM/MM MD simulations.[132] Free-energy surface of alanine tripeptide was also mapped using 4 CVs, and free-energies were showing good convergence within 10 ns per umbrella window (and 31 umbrella windows were used).[132] Awasthi et al. [133] used TASS to study deacylation and reverse acylation reactions of Aztreonam drug catalyzed by class-C  $\beta$  lactamase enzyme. These simulations were using DFT based QM/MM MD methods. For studying the reverse acylation reaction, i.e.  $EI \rightarrow ES$  in Figure 9, authors used eight CVs. In this reaction  $C_2$  makes a bond with  $N_1$  and recycles the  $\beta$ -lactam ring; see Figure 9 for labeling. Several conformational changes of the side-chains of the active site ligands are anticipated during this reaction. As these conformational changes are likely to be infrequent events (at least within the small timescale accessible for the QM/MM simulations), enhance sampling of these events were also carried out by appropriate choice of CVs. Two different proton transfer routes were also probed with the CVs considered. The distance  $d[AztN_1 - AztC_2]$  (CV1) was chosen for the US bias, as this CV samples the recyclization of the  $\beta$ -lactam ring. At the same time, a broad free energy basin is expected along this CV since different



conformations of the ring-opened drug is possible in the EI state. Another CV (CV2), namely the coordination of AztN<sub>1</sub> to its hydrogen and to the hydrogen atoms of the active site water W<sub>1</sub> ( $C[\text{AztN}_1 - \{\text{AztN}_1\text{H}_1, \text{W}_1\text{H}_1\}]$ ), was chosen for biasing with one-dimensional metadynamics bias. This choice was made as relatively high free-energy barrier is expected for covalent-bond breaking and the free-energy surface along CV2 should have a bound and narrow topology. Temperature of the auxiliary variables was set to 1000 K while the system temperature was kept at 300 K. In total 16 umbrella windows were placed at equal distance from 1.3 to 2.9 Å along CV1. It was observed that the free-energy barrier converges within 9 ps (per umbrella window).[133] The converged free energy surface was computed using the reweighting procedure explained in Ref. [132] and then projected to CV1 and CV2 as shown in Figure 9.



**FIGURE 9** Free-energy surface for the reverse acylation of the aztreonam drug catalyzed by class-C  $\beta$  lactamase enzyme is shown. Here the nine-dimensional free-energy surface is projected to CV1-CV2 space. Contour lines are drawn at 2 kcal mol<sup>-1</sup> intervals. Sub-figures (b), (c), and (d) show representative snapshots of EI, Ela, and ES. Atom colors: S (yellow), O (red), N (blue), C (black), H (white). Protein backbone is shown as transparent ribbons.[133] Reprinted with permission from J. Phys. Chem. B 2018;122:4299 Copyright (2018) American Chemical Society.

TASS was also used in the study of Mg<sup>2+</sup> assisted pyrophosphate release in a sugar nucleotidyltransferase. [134] In that work, 10 CVs were chosen, which included several torsional angles of the side-chain residues which interacted with the pyrophosphate. It was shown that US predicts a slightly different mechanism and a higher free energy barrier

compared to TASS as a result of poor sampling of orthogonal coordinates by the former method. Sahoo and Nair used TASS to simulate proton exchange reaction between methane and acid-sites within the H-ZSM-5 zeolite using DFT based QM/polarized-MM simulations. [135] Without invoking a controlled sampling of distance between CH<sub>4</sub> and the acid site in zeolite, CH<sub>4</sub> molecule diffuses away from the acid-sites during the simulation. By the virtue of the umbrella-bias in the TASS formulation, controlled sampling of this coordinate could be carried out, thus making the free-energy computations highly efficient.

## 6 | CONCLUSIONS

Accelerating large number of CVs and thus exploring a high-dimensional free-energy landscape is crucial to obtain a quick free-energy convergence in MD simulations. Conventional methods like US and metadynamics are inefficient in exploring high-dimensional landscapes, as sampling efficiency decreases exponentially with the number of CVs. We have discussed four promising methods in detail which mitigate the limitations imposed by the dimensionality of the CV-space.

BEMetaD is quite popular today and is mostly applied to study wide variety of problems in bimolecular systems. However, the main limitation of this method is the need of replica-exchange which requires overlapping probability distributions between two replicas. This decreases the computational efficiency of the method. As a result, BEMetaD based AIMD simulation of chemical reaction in soft matter systems has not been reported yet. PBMetaD alleviates this problem by parallel sampling of CVs within single replica. PBMetaD has the scope of sampling large number of CVs, and has been also used in studying conformational changes in bimolecular systems and chemical reactions using AIMD (with semi-empirical Hamiltonian). Efficiency of PBMetaD would also diminish with the increase of number of CVs due to the mutually dependent scaling of biases. On the other hand, TAMd/d-AFED approach is shown to be very powerful in enhanced sampling with a few hundreds of CVs. However, TAMd/d-AFED method should be carefully carried out as maintaining adiabatic separation between CV subsystem and physical subsystem is vital. Further, increasing CV temperature can result in unphysical structural changes, especially when the force-fields are not designed to operate at high temperatures. TAMd/d-AFED method has been used in AIMD simulations, conformational sampling in biomolecular systems and crystal structure predictions. On the other hand, all the three methods discussed above can become inefficient in exploring free-energy basins that are broad and unbound. A controlled sampling of CVs is preferred to avoid sampling myriad of uninteresting configurations. This is achieved in the relatively new TASS sampling method which combines US, metadynamics and TAMd/d-AFED. The method has been shown to be powerful for computing high-dimensional free-energy surfaces of chemical reactions, including enzymatic reactions. Even the computationally expensive DFT based QM/MM methods have been used with TASS and a quick free-energy convergence was reported. One of the shortcoming of TASS is that prior chemical knowledge is required to select the type of biasing along the CVs in an efficient manner.

A variety of problems like protein-folding, ligand binding in proteins and nucleic acids, structural refinements of biomolecules based on experimental data, crystal structure predictions, exploration of reaction pathways, and modeling of enzymatic reactions require quick sampling of large number of transverse CVs, which can now be studied using the aforementioned methods. Combining these CV-based approaches with global-tempering methods could further strengthen these computational methods to study more complex problems.

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