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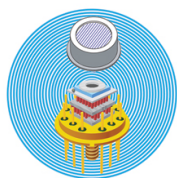
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The origins and properties of intrinsic nonradiative recombination centers in wide bandgap GaN and AlGaIn

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The nonradiative lifetime (τ_{NR}) of the near-band-edge emission in various quality GaN samples is compared with the results of positron annihilation measurement, in order to identify the origin and to determine the capture-cross-section of the major intrinsic nonradiative recombination centers (NRCs). The room-temperature τ_{NR} of various n-type GaN samples increased with decreasing the concentration of divacancies composed of a Ga vacancy (V_{Ga}) and a N vacancy (V_{N}), namely, $V_{\text{Ga}}V_{\text{N}}$. The τ_{NR} value also increased with increasing the diffusion length of positrons, which is almost proportional to the inverse third root of the gross concentration of all point defects. The results indicate that major intrinsic NRC in n-type GaN is $V_{\text{Ga}}V_{\text{N}}$. From the relationship between its concentration and τ_{NR} , its hole capture-cross-section is estimated to be about $7 \times 10^{-14} \text{ cm}^2$. Different from the case of 4H-SiC, the major NRCs in p-type and n-type GaN are different: the major NRCs in Mg-doped p-type GaN epilayers are assigned to multiple vacancies containing a V_{Ga} and two (or three) V_{N} s, namely, $V_{\text{Ga}}(V_{\text{N}})_n$ ($n = 2$ or 3). The ion-implanted Mg-doped GaN films are found to contain larger size vacancy complexes such as $(V_{\text{Ga}})_3(V_{\text{N}})_3$. In analogy with GaN, major NRCs in $\text{Al}_{0.6}\text{Ga}_{0.4}\text{N}$ alloys are assigned to vacancy complexes containing an Al vacancy or a V_{Ga} . *Published by AIP Publishing.* <https://doi.org/10.1063/1.5012994>

I. INTRODUCTION

For solving the energy crisis problem, the exploitation of energy-saving high-power electronic devices operating at high frequencies, as well as the present solid-state lighting using high efficiency light-emitting diodes (LEDs), is one of the significant ways of markedly decreasing total energy consumption. Gallium nitride (GaN) and related (Al,Ga,In)N alloys are a suitable candidate material system for this purpose because they provide practical benefits in the production of LEDs and laser diodes (LDs) operating in the ultraviolet (UV) to green wavelengths and white LEDs consisting of an InGaIn quantum well (QW) blue LED and yellow phosphors.¹ We note that such LEDs are fabricated on a heteroepitaxial GaN film grown on *c*-plane Al_2O_3 substrates, generally abbreviated as “GaN template” and therefore contain high density of threading dislocations (TDs) of the order of 10^8 to 10^9 cm^{-2} . Because such high threading dislocation density (TDD) InGaIn QWs have been exhibiting sufficiently high near-band-edge (NBE) emission intensity with the aid of defect-^{1,4} and polarization field^{1,2,4}-resistant radiation probability of the localized excitons in InGaIn alloys, the development of a low TDD bulk free-standing (FS) GaN substrate took a long time.

On another front, GaN has a potential to realize high-power electronic devices operating at high frequencies⁵ owing to its outstanding characteristics, including large bandgap energy (E_g), high break-down field, and high saturation velocity. Indeed, a normally off vertical GaN-based transistor on a FS-GaN substrate with a low specific on-state resistance (R_{ON}) of $1 \text{ m}\Omega \cdot \text{cm}^2$ and a high off-state break-down voltage (V_{BD}) of 1.7 kV has been demonstrated by using a p-type GaN/unintentionally doped (UID) AlGaIn/GaN heterostructure overgrown on the V-shaped grooves formed over the drift layer.⁶ However, further improvements in the device performances including the stability and reliability are mandatory for integrating GaN power devices in commercial systems. For this purpose, large-area, single-domain, mosaic- or bowing-free FS-GaN wafers with a negligible TDD are essential. In particular for fabricating vertically current-flowing devices, precisely controlled building blocks such as low-resistivity FS-GaN substrates with negligible lattice mismatch to overlayers, very low impurity concentration n-type drift layer, and structured n-type and p-type segments on their top are required.

For designing such advanced optical and electronic devices based on GaN, in-depth probing and control of the carrier lifetime in the constituent layers are essential. Especially, controlling the minority carrier lifetime (τ_{minority}) is indispensable because it reflects carrier recombination

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lifetime and determines the carrier diffusion length and eventually determines the device performances. For example, τ_{minority} limits the switching speed of insulating-gate bipolar transistors: as the energy loss of power-switching devices is a sum of R_{ON} and switching-loss, low R_{ON} and appropriate τ_{minority} are simultaneously required. Also, τ_{minority} is important for unipolar devices like Schottky barrier diodes. In the case of a direct bandgap semiconductor GaN, τ_{minority} can be measured by using time-resolved photoluminescence (TRPL) measurement under low-excitation conditions.⁴ The photoluminescence (PL) lifetime (τ_{PL}) of the NBE emission is equal to τ_{minority} and is expressed by

$$\tau_{\text{PL}}^{-1} = \tau_{\text{R}}^{-1} + \tau_{\text{NR}}^{-1}, \quad (1)$$

where τ_{R} and τ_{NR} are the radiative and nonradiative recombination lifetimes, respectively. Here, τ_{R} is inverse of the radiative recombination rate (R_{R}) and reflects the radiative performance of the material. Accordingly, τ_{R} of a homogeneous semiconductor material, which has zero inhomogeneous broadening, is unique to the material when there is no quantum confinement. On the other hand, τ_{NR} is inverse of the nonradiative recombination rate (R_{NR}) and therefore inversely proportional to the product of the capture rate and concentration of Shockley-Read-Hall (SRH)-type midgap nonradiative recombination centers (NRCs) (C_{NRC} and N_{NRC} , respectively);

$$\tau_{\text{NR}} = R_{\text{NR}}^{-1} = \frac{1}{C_{\text{NRC}} \cdot N_{\text{NRC}}}. \quad (2)$$

These parameters are quite important, since they determine the internal quantum efficiency (η_{int}) of the NBE emission under the relation

$$\eta_{\text{int}} = \frac{R_{\text{R}}}{(R_{\text{R}} + R_{\text{NR}})} = \frac{1}{1 + \frac{\tau_{\text{R}}}{\tau_{\text{NR}}}}. \quad (3)$$

The relationship among the generation rate (G) by a photon ($h\nu$), radiative recombination, and nonradiative recombination is schematically shown in Fig. 1(a). The role of a NRC with the minority carrier capture-cross-section, σ , and a minority carrier with the thermal velocity, v_{th} , is schematically shown in Fig. 1(b). Here, $C_{\text{NRC}} = \sigma \cdot v_{\text{th}}$. Accordingly, long τ_{NR} is preferred for optical devices such as LEDs, LDs, and solar cells. Long τ_{NR} is also required for high V_{BD} power devices because NRCs are the cause of recombination and generation currents and hence eventually lower V_{BD} .

As described above, N_{NRC} should be minimized in such devices. The accurate understanding of the origins and properties of major intrinsic NRCs, which most likely originate from native point defects, is a universal protocol for developing a technique to decrease them and consequently improve the device performances. There exist plenty of sources for NRCs such as large structural defects like voids and cracks, TDs with edge, screw, or mixed components, surface defects causing the surface recombination, and SRH-type deep levels (DLs). We note that Auger recombination is a nonradiative recombination process owing to

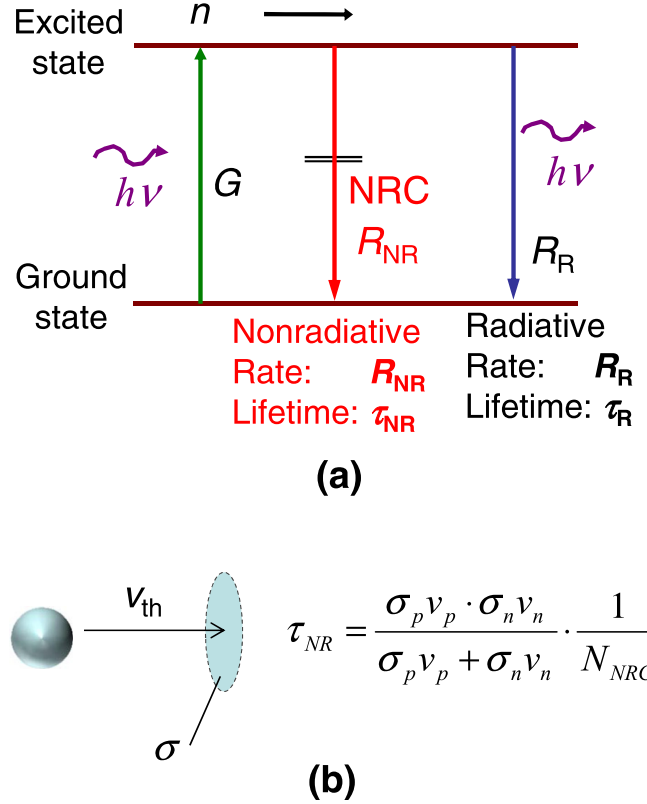


FIG. 1. (a) Schematic representation of the relationship among the generation of an electron-hole pair or an exciton by a photon $h\nu$ with the rate G , nonradiative recombination at a SRH-type NRC with the rate R_{NR} (lifetime τ_{NR}), and radiative recombination with the rate R_{R} (lifetime τ_{R}). (b) Schematic model of a NRC capturing minority carriers of a thermal velocity v_{th} and the capture-cross-section σ . In the case of n-type GaN, in which minority carriers are holes, τ_{NR} is expressed by $\frac{1}{\sigma_p v_p \cdot N_{\text{NRC}}}$.

different mechanisms. With respect to (Al,In,Ga)N epilayers and QWs, TDs had long been invoked to as the dominant NRCs to limit η_{int} of the NBE emission,⁷ as the NBE emission intensity of GaN generally increased with the decrease in TDD.^{1,7} However, as the authors have been suggesting based on the results of TRPL and positron (e^+) annihilation spectroscopy (PAS)^{8–11} measurements since 2005 (Ref. 12), point defect complexes containing a Ga vacancy (V_{Ga}) are the most likely true origin of predominant intrinsic NRCs in GaN,^{12,13} because τ_{PL} at room temperature, which nearly reflects τ_{NR} , decreases with increasing the concentration of V_{Ga} defects ($[V_{\text{Ga}}]$). We note that the importance of V_{Ga} s for the broad luminescence band at around 2.2 eV, which is called as “yellow luminescence (YL) band,”^{14–16} and the nonradiative recombination has been speculated^{17,18} earlier than 2005. Although experimental evidence has not been presented for the presence of V_{Ga} s. Our assignment^{12,13} is essentially consistent with the calculated results^{15,19,20} that the formation energy (E_{Form}) of negatively charged defects such as V_{Ga} s in wide bandgap semiconductors like GaN can become smaller due to the Fermi level (E_{F}) term ($+qE_{\text{F}}$).^{15,19,20} In analogy with the results for GaN,^{12,13} the authors have assigned²¹ point defect complexes containing a cation vacancy (V_{III}) as the origin of dominant intrinsic NRCs in $\text{Al}_{0.6}\text{Ga}_{0.4}\text{N}$ epilayers grown by metalorganic vapor phase epitaxy (MOVPE). We

note that E_{Form} of an Al vacancy (V_{Al}) in AlN has been calculated to have negative value in n-type AlN.^{20,22,23}

In the previous reports,^{12,13,21} the authors have used complementary TRPL and PAS⁸⁻¹¹ measurements to correlate τ_{NR} at room temperature and the concentration of V_{III} ($[V_{\text{III}}]$). PAS⁸⁻¹¹ is an established, nondestructive, and exclusive tool to detect negatively charged and neutral vacancy defects in a semiconductor. A e^+ is an antimatter of an electron (e^-) and has a positive charge with a mass identical to e^- . When a e^+ is implanted into condensed matter, it annihilates with a surrounding e^- and emits two 511 keV γ -rays according to $E_\gamma = mc^2$, where E_γ is the energy, m is the mass, and c is the speed of the light. The annihilating γ -ray spectra are broadened in energy due to the momentum component of the annihilating positron-electron (e^+e^-) pair p_L , which is parallel to the direction of the γ -rays. The energy of the γ -rays is given by the relation $E_\gamma = mc^2 \pm \Delta E_\gamma$ keV. The Doppler shift ΔE_γ is given by the relation $\Delta E_\gamma = p_L c/2$. A freely diffusing e^+ likely localizes in a vacancy-type defect because of the Coulomb repulsion from ion cores. Because the momentum distribution of e^- surrounding such defects is smaller than that in defect-free (DF) regions, the defects can be detected by measuring the Doppler broadening spectra of the annihilation radiation. The resulting change in the γ -ray spectra is characterized by the line-shape parameter S and the wing parameter W , where the former mainly reflects the fraction of annihilating e^+e^- pairs of small momentum distribution (mostly valence electrons) and the latter represents the fraction of the pairs of large momentum distribution (mostly core electrons). Since V_{Ga} s and their complexes are acceptor-type defects in GaN, they are the most probable candidates of e^+ trapping centers.^{10,11} Accordingly, S and W can be used as a measure of size and/or concentration of negatively charged V_{Ga} s and V_{Ga} -complexes. For epitaxial structures, characteristic S and positron diffusion length (L_+) in each layer can be determined by using a monoenergetic e^+ -beam,⁹⁻¹¹ by which the mean implantation depth of e^+ can be controlled. The analysis²⁴ involves solving the diffusion equation of e^+ as a function of acceleration energy E using the initial implantation profile. Here, L_+ can be used as a measure of gross concentration of e^+ trapping centers and scattering centers, because both of them shorten L_+ . In a three-dimensional (3D) space, L_+ may correspond to an inverse third root of gross point defect concentration. The scattering centers are positively charged and neutral point defects such as N vacancies (V_{N} s), interstitials (Ga_i and N_i), and certain complexes.

In this article, we review our knowledge on the origin and properties of major intrinsic NRCs in GaN. The τ_{NR} value of the NBE emission, which mostly represents τ_{minority} , in various quality GaN samples measured using TRPL is correlated with the results of PAS measurement, in order to assign the origin and determine σ of the major intrinsic NRCs. The room-temperature τ_{NR} in n-type GaN of a variety of TDD, growth orientations, polar directions, and polytypes, which were grown by various growth techniques, increased with the decrease in the concentration of divacancies composed of a V_{Ga} and a V_{N} ($[V_{\text{Ga}}V_{\text{N}}]$). The τ_{NR} value also increased with increasing L_+ , and these results indicate that

major intrinsic NRCs in GaN is $V_{\text{Ga}}V_{\text{N}}$. From the relationship between τ_{NR} and N_{NRC} , its hole capture-cross-section (σ_p) is determined to be $7 \times 10^{-14} \text{ cm}^2$. The major NRCs in the epitaxial and ion-implanted (I/I) Mg-doped GaN films are assigned to larger size multiple vacancy complexes such as $(V_{\text{Ga}})_3(V_{\text{N}})_3$. In analogy with GaN, major NRCs in $\text{Al}_{0.6}\text{Ga}_{0.4}\text{N}$ alloys are assigned to vacancy complexes containing V_{III} .

II. EXPERIMENTAL

A. GaN samples

For drawing relationships between τ_{minority} and S (τ - S) and τ_{minority} and L_+ (τ - L_+), various quality n-type GaN samples were prepared. They were (i) 80- μm -thick c -plane UID FS-GaN grown by MOVPE using the lateral epitaxial overgrowth (LEO) technique on a GaN template followed by polishing away the substrate [the sample identification (ID) name is abbreviated as MOVPE FS-GaN],¹² (ii) 1- and 5- μm -thick UID Ga-polar c -plane GaN grown by MOVPE on a c -plane Al_2O_3 [abbreviated as uid + c(1) and uid + c(5), respectively],¹² (iii) 0.7- μm -thick unintentionally O-doped ($n = 5 \times 10^{18} \text{ cm}^{-3}$) N-polar c -plane GaN grown by MOVPE on a c -plane Al_2O_3 (uid -c),¹² (iv) 2- μm -thick Si-doped c -plane GaN on a c -plane Al_2O_3 [Si-doped (1.6), Si-doped (1.9), and Si-doped (2.2), of which doping concentrations were the numbers in parentheses time 10^{18} cm^{-3}],¹¹ (v) 1- μm -thick unintentionally O-doped ($\geq 10^{18} \text{ cm}^{-3}$) cubic zinc blende (001) GaN grown by MOVPE on (001) GaAs with or without AlGaIn/GaN superlattice buffer layer [ZB(no SL) and ZB(SL)],¹² (vi) 1- μm -thick unintentionally O-doped (001) GaN grown by N_2 rf-plasma-assisted molecular-beam epitaxy (MBE) on (001) 3C-SiC with AlN/GaN multiple buffer layer [ZB(MBE)],¹² (vii) 15–16- μm -thick UID a -plane GaN grown by hydride vapor phase epitaxy (HVPE) on r -plane Al_2O_3 with or without LEO-GaN base [a -GaN(LEO) and a -GaN],¹² and (viii) unintentionally O-doped ($4 \times 10^{18} \text{ cm}^{-3}$) m -plane FS-GaN grown by HVPE on a LiAlO_2 substrate followed by delamination (m -GaN).¹² The TDD in these samples was varied between 10^5 and 10^{10} cm^{-2} (Ref. 12).

Another low TDD FS-GaN sample^{25,26} was grown using vertical-flow HVPE apparatus.²⁵ At first, approximately 1-cm-thick, transparent c -plane GaN boules were grown on a c -plane Al_2O_3 . Appropriate amount of gaseous HCl was flowed on heated Ga, and NH_3 was supplied from a separate gas line. Typical growth temperature and pressure were 1050 °C and atmospheric pressure, respectively. The growth duration was varied from 55 to 96 h. Approximately 325- μm -thick, $10 \times 10\text{-mm}^2$ -area, c - or m -plane FS-GaN wafers were sliced^{25,26} from such boules grown under various conditions. The surface of the wafers was polished with chemical treatment. Details of the growth and fundamental properties have been given in Refs. 25 and 26. The c -plane UID samples were abbreviated as C0, C1, C2, and C3, and Si-doped sample was named C4. The m -plane UID sample was abbreviated by M1: their electrical and optical properties are given in Ref. 13. In addition, an n-type low-resistivity ($\rho = 8.5 \times 10^{-3} \Omega \text{ cm}$), very low TDD ($\sim 10^4 \text{ cm}^{-2}$) m -plane FS-GaN wafer²⁷ named M2 was grown by HVPE on a nearly bowing-free bulk GaN

seed wafer, which was synthesized by the ammonothermal (AT) method in supercritical ammonia using an acidic mineralizer.²⁸ We note that particular AT method used by Mitsubishi Chemical Corporation is named *supercritical acidic ammonia technology* (SCAATTM).²⁸ The structural, electrical, and optical properties of M2 are given in Refs. 27 and 29.

All samples described above were n-type GaN. For evaluating the major defect species^{30,31} and their influences on the optical properties³² in p-type GaN, epitaxial and I/I Mg-doped GaN (GaN:Mg) samples were prepared.^{30,31} Approximately 1- μm -thick GaN:Mg epilayers were grown on a 4- μm -thick UID GaN epilayer grown on a *c*-plane FS-GaN substrate grown by HVPE. Potential influences of TDs on the PL properties may be minimized, as TDD of the substrate used was in the range of 10^6 cm^{-2} . The Mg concentrations, [Mg], were 5×10^{17} , 2×10^{18} , and $4 \times 10^{19} \text{ cm}^{-3}$. For the I/I samples, Mg⁺ ions were implanted into the same 4- μm -thick UID GaN film with several energies ranging from 20 to 430 keV, in order to form a 500-nm-thick box-profile with [Mg] of 1×10^{17} , 1×10^{18} , and $1 \times 10^{19} \text{ cm}^{-3}$. The I/I was carried out at room temperature and followed by the deposition of a 300-nm-thick AlN decomposition-shield by a sputtering method. The samples were annealed at 1300 °C for 5 min in N₂ gas at atmospheric pressure. The decomposition-shield was chemically removed after annealing. The sample details are given in Ref. 32.

For discussing the major intrinsic NRCs²¹ in Al_{0.6}Ga_{0.4}N alloy films, approximately 0.8- μm -thick, Si-doped *c*-plane Al_{0.6}Ga_{0.4}N epitaxial films (Al_{0.6}Ga_{0.4}N:Si) were grown at $6.7 \times 10^3 \text{ Pa}$ by MOVPE on a 0.8- μm -thick AlN template, which was grown on a *c*-plane Al₂O₃ substrate. The Si concentration ([Si]) in the solid-phase was varied from 2×10^{16} to $4 \times 10^{18} \text{ cm}^{-3}$. The TDD having edge components (N_E) was estimated to be about $3 \times 10^8 \text{ cm}^{-2}$. Details of the growth conditions are given in Ref. 33.

B. Steady-state, time-resolved, and spatio-time-resolved luminescence measurements

For macroarea measurements, steady-state PL of GaN was excited using the 325.0 nm line of a cw He-Cd laser with the power density of $20 \text{ W} \cdot \text{cm}^{-2}$. For TRPL measurement, the NBE PL was excited using approximately 200 fs pulses of a frequency-tripled (3ω) mode-locked Al₂O₃:Ti laser operating at 80 MHz. The 3ω wavelength was approximately 267 nm. The excitation density was approximately 125 nJ cm^{-2} (per pulse), in order to ensure weak-excitation conditions.⁴ The spot diameter and estimated excited carrier concentration were 1 mm and a few times 10^{16} cm^{-3} , respectively, when τ_{PL} is 1 ns. The reason why both PL and TRPL were carried out under weak-excitation regime is to underline the nonradiative recombination processes in these materials. Because most of FS-GaN samples exhibited relatively long luminescence decay, the pulse repetition rate was reduced down to 8 MHz or 0.8 MHz using a pulse picker. The TRPL signal was collected using a standard streak camera. The TRPL signals were fitted using a single- or bi-exponential line shape function: $I(t) = A_1 \exp(-t/\tau_1) + A_2 \exp(-t/\tau_2)$, where $I(t)$ is the intensity at time t and A_1 (A_2) and τ_1 (τ_2) are the pre-exponential constant and the lifetime, respectively, of the fast (slow) decay component. The value of τ_1 , which mostly limits the cw PL intensity at room temperature, is used as the representative τ_{PL} .

As described in Sec. I, τ_{NR} and τ_{R} can be obtained by using Eqs. (1) and (3). Therefore, experimental values of τ_{PL} and η_{int} are required to obtain τ_{NR} . As depicted in Fig. 1(b), the nonradiative recombination eventually occurs when a minority carrier (or an exciton) is captured by a NRC having characteristic σ . In the case of n-type GaN, e⁻ is already captured by a NRC and the hole capture-cross-section σ_p limits this event. Because v_{th} of a hole, v_p , is $\sqrt{\frac{3k_B T}{m_p}}$, where k_B is the Boltzmann constant, T is the temperature, and m_p is the hole effective mass, finite T is necessary for a hole to gain a thermal velocity. Accordingly, η_{int} at 0 K in principle becomes unity when average distance of NRCs is far longer than the exciton Bohr diameter ($2a_B$) and excitons do not move (zero carrier temperature). However, when N_{NRC} exceeds the critical value, η_{int} at 0 K is no longer unity, because an electron-hole pair or an exciton recombines at NRCs without diffusion or drift. The probability that a diffusion-free (0 K) exciton is not captured by NRCs but decays with radiative recombination, which is defined³⁴ by

$$\eta_{\text{int}}^{\text{max}} = 1 - \frac{4}{3} \pi a_B^3 \cdot N_{\text{NRC}}, \quad (4)$$

gives the maximum η_{int} of the emission. Here, $\eta_{\text{int}}^{\text{max}}$ is calculated under the assumption that every NRC within the exciton volume causes the nonradiative recombination. In Fig. 2, $\eta_{\text{int}}^{\text{max}}$ for GaN is shown as a function of N_{NRC} (after Ref. 34). For comparison, the value of AlN is also shown. Here, a_B in GaN and AlN are 3.4 and 1.9 nm, respectively.¹ From this simple consideration, the commonly used assumption that η_{int} is close to (but not absolutely) unity at 2 to

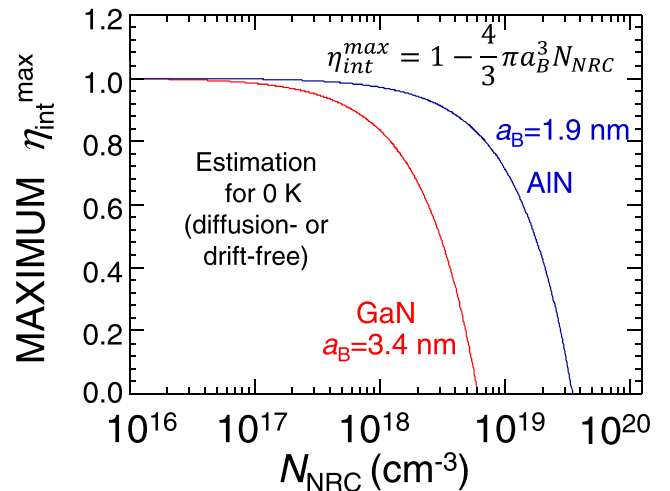


FIG. 2. Maximum η_{int} ($\eta_{\text{int}}^{\text{max}}$) at 0 K of a diffusion- or drift-free excitonic emission in GaN and AlN estimated as a function of NRC concentration, N_{NRC} . The values are calculated under the assumption that every NRC exists within the exciton volume causes nonradiative recombination. [Modified with permission from Chichibu *et al.*, Adv. Mater. **29**, 1603644 (2017). Copyright 2017 John Wiley and Sons.]³⁴

4.2 K is not absolutely incorrect when N_{NRC} is lower than approximately a few times 10^{16} cm^{-3} for GaN and a few times 10^{17} cm^{-3} for AlN.³⁴ We tentatively use these conditions and assumptions for discussing the high quality n-type HVPE FS-GaN samples.^{25–27}

For probing the local carrier dynamics, the spatio-time-resolved cathodoluminescence (STRCL) measurement^{35–38} was carried out on several HVPE FS-GaN samples.²⁵ By using STRCL, spatially resolved steady-state cathodoluminescence (SRCL) spectra and very local time-resolved cathodoluminescence (TRCL) signals can be obtained. A schematic drawing of our STRCL system will be found in Refs. 37 and 38. In this article, the data taken with the rear-excitation configuration^{35,36} photoelectron (PE)-gun are exclusively shown: by using a 300-mm focal-length fused silica lens, approximately 200 fs pulses of a 3ω mode-locked $\text{Al}_2\text{O}_3\text{:Ti}$ laser were irradiated from the back side of a negatively biased, 15-nm-thick Au photocathode. The spot size on the photocathode is estimated to be $2.8 \times 10^{-5} \text{ cm}^2$, giving rise to the maximum fluence of $35 \mu\text{J} \cdot \text{cm}^{-2}$ with an average power of 80 mW at 80 MHz repetition rate. The PEs were extracted through an extractor electrode and focused to the filament position of the scanning electron microscope (SEM). The cathodoluminescence (CL) from the sample was collected using an off-axis parabolic mirror ($R = 12 \text{ mm}$) placed above the sample and analyzed using a grating spectrometer equipped with a CCD and a streak-camera with a temporal resolution of approximately 7 ps. Typical acceleration voltage (V_{acc}) was 10 kV, and approximately 1.6 and 4 electrons per pulse were injected for TRCL and SRCL measurements, respectively. Using these conditions, approximately 5.6×10^{16} and $1.4 \times 10^{17} \text{ cm}^{-3}$ e-h pairs, respectively, would be generated. The former, at least, maintained the weak excitation conditions, in order to underline the non-radiative recombination process.

C. Positron annihilation measurements

A monoenergetic e^+ -beam line^{11–13,21,30,34} was used to measure the Doppler broadening spectra of annihilating γ -ray radiation as a function of incident positron energy E using a Ge detector. A spectrum with 3×10^6 counts was measured at each E . The low-momentum portion was characterized by the S parameter, defined as the number of annihilation events for the energy range of $511 \text{ keV} \pm \Delta E_\gamma$, where $\Delta E_\gamma = 0.76 \text{ keV}$, around the center of the peak, over the total counts. The W parameter was calculated for the annihilation events in the tail of the spectra ($3.4 \text{ keV} \leq |\Delta E_\gamma| \leq 6.8 \text{ keV}$) over the total counts. The relationship between S and E was analyzed by VEPFIT, a computer program developed by van Veen *et al.*²⁴ The one-dimensional (1D) diffusion model of e^+ is expressed by⁸

$$D_+ \frac{d^2}{dz^2} n(z) - \kappa_{\text{eff}}(z)n(z) + P(z, E) = 0, \quad (5)$$

where D_+ is the diffusion coefficient of e^+ , $n(z)$ is the probability density of e^+ at a distance z from the surface, $\kappa_{\text{eff}}(z)$ is the effective escape rate of e^+ from the diffusion process,

and $P(z, E)$ is the implantation profile of e^+ . The diffusion length of positrons, $L_+(z)$, is given by

$$L_+(z) = \sqrt{D_+ / \kappa_{\text{eff}}(z)}. \quad (6)$$

In the fitting procedure, a homogeneous distribution of defects was assumed. The S – E curve was fitted to the following equation:

$$S(E) = S_e F_e(E) + S_s F_s(E) + \sum S_i F_i(E), \quad (7)$$

where $F_e(E)$, $F_s(E)$, and $F_i(E)$ are the fraction of epithermal (nonthermalized) positrons annihilated at the surface, that of positrons annihilated at the surface, and that of positrons annihilated in the i th block, respectively [$F_e(E) + F_s(E) + \sum F_i(E) = 1$]. The values of S_e , S_s , and S_i are characteristic S parameters for the respective annihilation events. The analytical procedures used in this study are similar to those described in Ref. 11. To examine the annihilation characteristics of positrons in detail, the coincidence detection system¹¹ was also used. Spectra with about 5×10^6 counts were obtained and then characterized using the S and W parameters.

Doppler broadening spectra of the annihilating γ -rays were theoretically calculated using the QMAS (Quantum Materials Simulator) code,^{39,40} which uses valence-electron wavefunctions determined by the projector augmented-wave (PAW) method.^{41,42} To represent the exchange and correlation energies of electrons, the generalized gradient approximation was used.⁴³ The calculations were carried out on orthorhombic supercells equivalent to $4 \times 4 \times 2$ wurtzite cells containing 128 atoms when there exist no vacancies. The supercell dimensions were $2\sqrt{3}a_0 \times 4a_0 \times 2c_0$, where $a_0 = 0.3189 \text{ nm}$ and $c_0 = 0.518625 \text{ nm}$ were the lattice parameters of the wurtzite cell. For the supercell containing a defect, atomic positions in the fixed cell (with the experimental lattice parameters) were computationally optimized through a series of first-principles electronic-structure calculations. The formalism of the local density approximation⁴⁴ was used in the calculation of the positron wave functions. The Doppler broadening spectra resulted from the annihilation of positrons in the delocalized (DF) state and the trapped states in cation vacancies were calculated.⁴⁵ The simulated spectra were characterized by the S and W parameters.⁴⁵

III. RESULTS AND DISCUSSION

A. Origin of nonradiative recombination centers in n-type GaN

In order to elucidate the species of native defects in UID and doped n-type GaN, S – W relationship was studied. In Fig. 3, (S, W) values of various n-type GaN samples are plotted by closed symbols.^{12,13} The sample ID names are shown in the figure. Because (S, W) values for the HVPE FS-GaN samples (C0, C1, C2, C3, C4, M1, and M2) almost coincided with that of MOVPE FS-GaN, their (S, W) values are indicated by a single plot “FS-GaN in general.” The (S, W) values calculated⁴⁵ for the annihilation of positrons at the delocalized state in the DF region, V_{Ga} , V_{N} , and V_{GaVn}

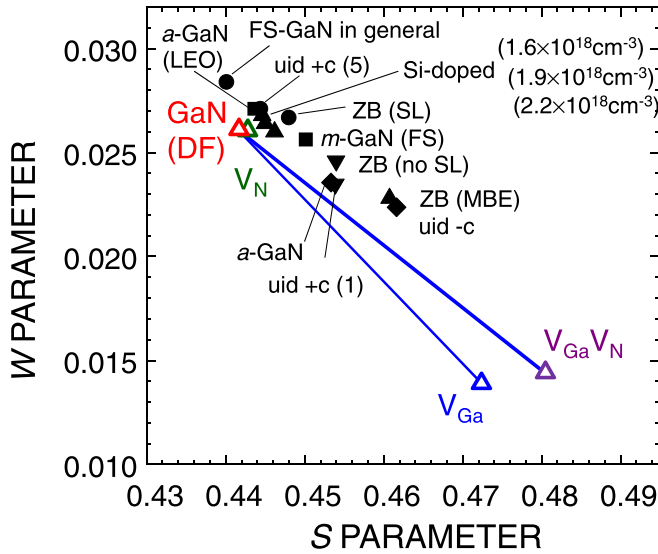


FIG. 3. S - W relationships for various UID and doped n-type GaN samples (closed symbols). The (S, W) values calculated using the QMAS code for positron annihilation at the defect-free (DF) region (delocalized state), V_{Ga} , V_{N} , and $V_{\text{Ga}}V_{\text{N}}$ divacancy are shown by open triangles.⁴⁵ The experimental data appear to align parallel to the line connecting $(S_{\text{DF}}, W_{\text{DF}})$ and $(S_{V_{\text{Ga}}V_{\text{N}}}, W_{V_{\text{Ga}}V_{\text{N}}})$, indicating that major intrinsic vacancy type defects in n-type GaN are $V_{\text{Ga}}V_{\text{N}}$ divacancies. [Experimental data plots are reproduced with permission from Appl. Phys. Lett. **86**, 021914 (2005). Copyright 2005 AIP Publishing LLC.]¹²

divacancy are shown by open triangles. In the S - W plot, when the sample contains single-species of vacancy-type defects, positrons annihilate from DF state or the trapped state due to the defects. In this case, (S, W) becomes a weighted average of the characteristic (S, W) values for DF and trapped states, namely $(S_{\text{DF}}, W_{\text{DF}})$ and $(S_{\text{defect}}, W_{\text{defect}})$, respectively, and it should lie on a line connecting those two values. Here we mention that the dynamic range of PAS measurement for V_{Ga} in GaN is approximately between 10^{16} and 10^{19} cm^{-3} , at which positrons implanted in the sample are nearly fully delocalized in DF regions and fully trapped by V_{Ga} s, respectively. Accordingly, $[V_{\text{Ga}}]$ is lower than 10^{15} cm^{-3} for $(S_{\text{DF}}, W_{\text{DF}})$ and higher than 10^{19} cm^{-3} for $(S_{V_{\text{Ga}}}, W_{V_{\text{Ga}}})$. In Fig. 3, the experimental data appear to align parallel to the line connecting $(S_{\text{DF}}, W_{\text{DF}})$ and $(S_{V_{\text{Ga}}V_{\text{N}}}, W_{V_{\text{Ga}}V_{\text{N}}})$.⁴⁵ More precisely, the measured (S, W) for FS-GaN lie to the higher left of the calculated (S, W) for DF-GaN. This difference could be due to several causes such as the limitations of first-principles calculations applied to Doppler broadening spectra, the experimental background, and/or the energy resolutions of our Ge detectors. Because FS-GaN in general showed the smallest S (and largest W), vacancy concentrations in them are close to or lower than the detection limit of PAS measurement being lower than 10^{16} cm^{-3} .⁴⁵ From these results, the major intrinsic vacancy type defects in n-type GaN is identified as $V_{\text{Ga}}V_{\text{N}}$ divacancies, and $[V_{\text{Ga}}V_{\text{N}}]$ of the samples shown in Fig. 3 are in the range between lower than 10^{16} cm^{-3} to approximately 5×10^{17} cm^{-3} .

The τ_1 values of the NBE emission in these n-type GaN at 293 K are plotted as functions of S and L_+ in Figs. 4(a) and 4(b), respectively. The data for the variety of samples¹²

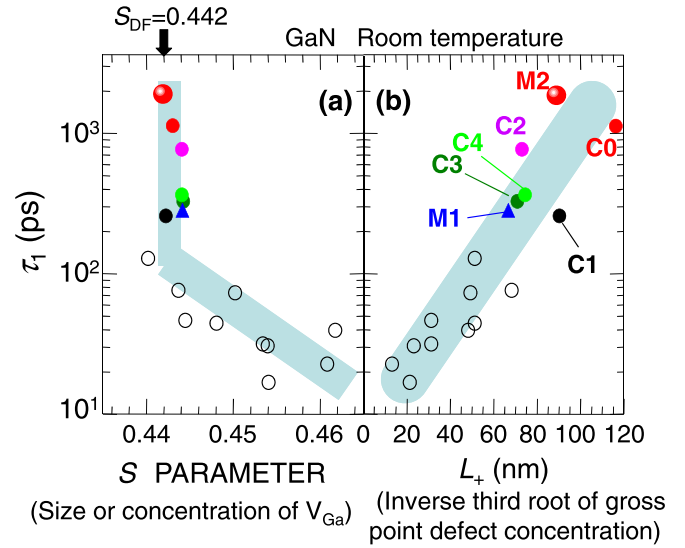


FIG. 4. Fast component of the TRPL decay curve (τ_1) for the NBE emission of GaN samples at room temperature as functions of (a) Doppler broadening S parameter and (b) positron diffusion length L_+ . The τ_1 values for a variety of GaN samples including Ga-polar and N-polar c-plane, a - and m -plane nonpolar, and zinc blende thin films and bulk crystals with high and low TDDs and high and low electron concentrations (n) are represented by open circles¹² and those of HVPE FS-GaN^{13,25-27,29} are represented by closed symbols. Characteristic S for DF-GaN ($S_{\text{DF}} = 0.442$) (Ref. 45) is shown by the arrow on the upper horizontal axis in (a). [Reproduced with permission from J. Appl. Phys. **111**, 103518 (2012). Copyright 2012 AIP Publishing LLC].¹³

with high and low electron concentrations (n) shown in Fig. 3 are represented by open circles and those for HVPE FS-GaN^{13,25-27,29} are represented by closed symbols. Characteristic S for DF-GaN ($S_{\text{DF}} = 0.442$) (Ref. 40) is shown by the arrow on the upper horizontal axis in Fig. 4(a). Obviously, τ_1 increases with decreasing S . Because S of FS-GaN samples has already reached S_{DF} , τ_1 distributes from 0.1 ns to 1.1 ns for the same S ($=S_{\text{DF}}$), as shown by the vertical guide to the eye. On the other hand, τ_1 increases with the increase in L_+ , and eventually reaches 1.1 ns for $L_+ = 116$ nm of the sample C0.¹³ Here we note that N_{NRC} calculated under the assumption that L_+ corresponds to an inverse third root of N_{NRC} are 10^{15} cm^{-3} nm for $L_+ = 100$ nm, 10^{16} cm^{-3} nm for $L_+ = 46$ nm, 10^{17} cm^{-3} nm for $L_+ = 22$ nm, and 10^{18} cm^{-3} nm for $L_+ = 10$ nm. The sample M2, which was grown²⁷ by HVPE on a SCAAT seed,²⁸ exhibited the longest τ_1 value.²⁹ These results confirm that principal limiting factor of τ_{NR} and thereby η_{int} at room temperature is gross concentration of point defects (and defect complexes), which are incorporated with V_{Ga} . From the results shown in Figs. 3 and 4, defect complexes containing V_{Ga} ,^{12,13} more precisely $V_{\text{Ga}}V_{\text{N}}$ divacancies, are identified as the major intrinsic NRCs in n-type GaN.

Spectrally integrated TRPL signals and the quenching ratio (R_q), which is defined as the integrated spectral intensity of whole NBE PL at a given T divided by that at 7–10 K [$I_{\text{PL}}(T \text{ K})/I_{\text{PL}}(7 \text{ K})$] under the weak excitation regime,^{4,12,13} of sample C0 are shown as a function of T in Figs. 5(a) and 5(b), respectively.¹³ In this particular sample, substitution of R_q as $\eta_{\text{int}}^{\text{eq}}$ is reasonable, as $N_{\text{NRC}} (<10^{16}$ $\text{cm}^{-3})$ is far lower than the critical value given in Fig. 2. Evidence to support this is that R_q at 300 K [2.3% in Fig. 5(b)] almost agrees with

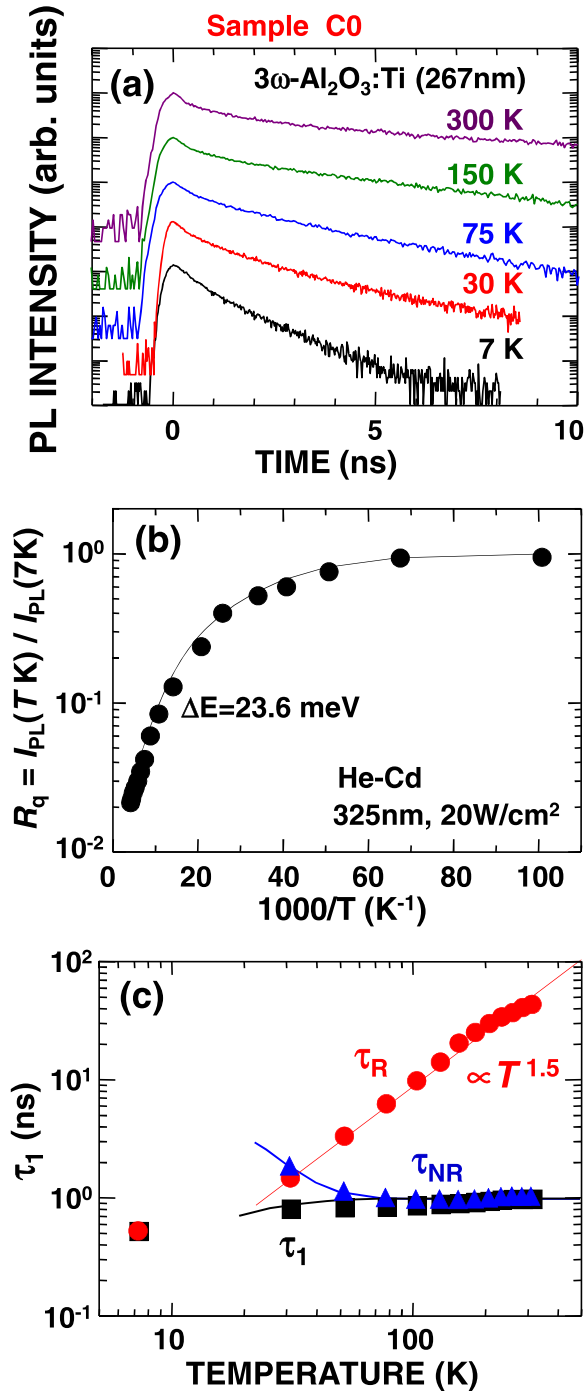


FIG. 5. (a) Spectrally integrated TRPL decay signals measured for whole NBE emissions of the *c*-plane FS-GaN (C0) as a function of T . (b) Spectrally integrated whole NBE PL intensity at a given T divided by that at 7 K [quenching ratio $R_q = I_{\text{PL}}(T \text{ K})/I_{\text{PL}}(7 \text{ K})$] as a function of $1/T$. At 300 K, R_q is 2.3%. (c) Temperature dependencies of τ_1 , τ_R , and τ_{NR} . The values of τ_R and τ_{NR} are derived from τ_1 and R_q using Eqs. (1) and (3), where τ_1 and R_q are substituted for τ_{PL} and η_{int} , respectively. [Reproduced with permission from J. Appl. Phys. **111**, 103518 (2012). Copyright 2012 AIP Publishing LLC].¹³

the value obtained using the omnidirectional photoluminescence (ODPL) spectroscopy,⁴⁶ by which absolute η_{int} can be obtained from absolute external quantum efficiency (η_{ext}) being 2% to 3% at the same excitation power density of $20 \text{ W} \cdot \text{cm}^{-2}$ at 300 K. We note that this assumption fails when using high-excitation conditions like very initial excitation stage of TRPL/TRCL measurements. The TRPL signal

showed nearly double-exponential decay shape, and the decay curve became modest with increasing T . The appearance of two (or three) decay components most probably reflects the fact that several portions of different N_{NRC} , which are away beyond the diffusion length of minority carriers (L_{minority}), are simultaneously observed in our macro-area measurements with 1-mm-diameter spot size, where $L_{\text{minority}} = \sqrt{D \cdot \tau}$ and D and τ are their diffusivity and lifetime, respectively. This issue will be discussed later with the results of STRCL measurement.

The τ_1 value slightly increased with T up to 100 K and leveled off at approximately 1.1 ns above 150 K, as plotted by squares in Fig. 5(c). For considering the temperature dependency of recombination dynamics, τ_R and τ_{NR} are deduced from the measured τ_1 and R_q using Eqs. (1) and (3), where τ_1 and R_q are substituted for τ_{PL} and η_{int} , respectively. The results are plotted in Fig. 5(c) by circles and triangles, respectively, for τ_R and τ_{NR} . As η_{int} decreases to 0.5, τ_R and τ_{NR} crossover at around 40 K. Below (above) this temperature, τ_1 is dominated by τ_R (τ_{NR}). As shown, τ_{NR} lies on an asymptote with temperature rise, and the room temperature value is 1.1 ns. The longest τ_{NR} value among the samples measured under the same excitation conditions was 2.07 ns for M2.²⁹ A saturation of the decrease in τ_{NR} indicates that NRCs are fully activated, reflecting low gross N_{NRC} . The decrease in η_{int} at elevated temperatures is, therefore, due to the increase in τ_R . As a result, η_{int} is estimated to be 2.3% at 300 K. As stated above, this value nearly agrees with the η_{int} value obtained by the ODPL measurement.⁴⁶ It should be noted that τ_R increases according to $T^{1.5}$, which is characteristics of particles in 3D space.^{47,48} The τ_R value is extrapolated to 130 ps at 7 K and 40–50 ns at 300 K. The latter value is consistent with τ_R value for the NBE PL peak in low TDD FS-GaN at 300 K reported recently using simultaneous photoluminescence and photo-acoustic measurements⁴⁹ being 50 ns. These experimental facts that two independent measurements^{13,49} showed the same τ_R at 300 K being 40–50 ns and other two independent measurements^{13,46} showed the same η_{int} at 300 K being 2%–3% at the same excitation power densities support the accuracy of the analysis carried out herein.

In order to visualize spatial variations of η_{int} and τ_{NR} for the NBE emission, STRCL measurement was conducted near the region surrounded by the inversion domain boundaries (IDBs) in the HVPE FS-GaN sample C3. We note that IDBs are occasionally formed by some growth perturbations. Figures 6(a)–6(c), respectively, illustrate SEM image and CL intensity (I_{CL}) images recorded for the NBE emission at 293 K and 20 K.³⁷ These CL images were taken with a probe current of 100 pA and a dwell time of 200 ms, corresponding to 30 min per image. The SEM image showed a trapezoidal dimple surrounded by the IDBs. Also, several dark spots were found although their contrasts were rather faint. These spots were also observed as the dark spots in the CL image at 293 K, as shown in Fig. 6(b). The CL image at 293 K showed complex structures since its contrast reflects spatial distribution of NRCs, while its spatial resolution is limited by L_{minority} . The sharpness of the CL image taken at 20 K was greatly improved because D approaches zero towards

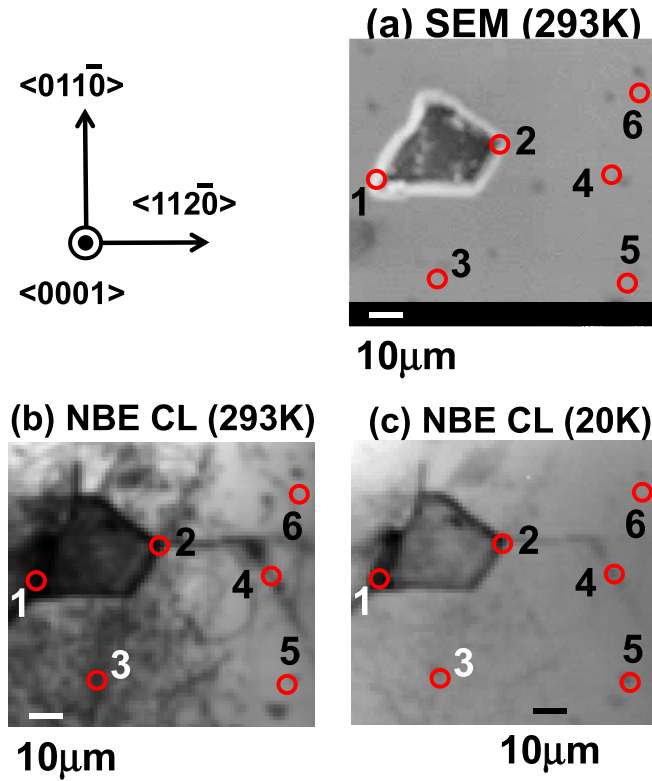


FIG. 6. (a) SEM image, (b) NBE CL intensity image taken at 293 K, and (c) NBE CL intensity image taken at 20 K for the FS-GaN sample C3. [Reproduced with permission from Appl. Phys. Lett. **101**, 212106 (2012). Copyright 2012 AIP Publishing LLC].³⁷

0 K according to Einstein's relation $D = \mu \frac{k_B T}{q}$, where k_B is the Boltzmann constant, q the electric charge, and μ the mobility. Therefore, the dark areas and lines that remain in Fig. 6(c) are possibly due to the clusters of NRCs and/or the absence of the material itself. In both Figs. 6(b) and 6(c), it can be seen that some straight line structures run from the corners of the trapezoid parallel to m -planes. This implies that the tensile stress accumulated around the IDBs is relaxed by introducing cracks.³⁷ Since there are no corresponding structures in the SEM image, it is likely that these cracks are atomically thin and run under the surface, and which can specifically be detected in the CL images due to the finite implantation depth of the e -beam and the longitudinal diffusion of the minority carriers.

The virtue of STRCL is that it is readily accessible to the local recombination dynamics for a particular emission peak. Local time-integrated cathodoluminescence (TICL) and TRCL decay signals for the NBE emission of C3 measured at room temperature at the positions 1 to 6 encircled in Fig. 6 are shown in Figs. 7(a) and 7(b), respectively.³⁷ In this instance, the probe current was decreased to 25 pA, which amounts to 1.6 electrons per pulse, in order to prevent any degradation in temporal resolution.³⁷ The resultant number of excited electron-hole pairs in GaN is deduced to be less than 2000 from the empirical relation given in Ref. 50. We note that this excitation power density gives the τ_1 value for the TRPL decay constant of a GaN template when excited with the laser fluence of $2 \mu\text{J} \cdot \text{cm}^{-2}$ (Ref. 51). This value is an order of magnitude higher than that used for the TRPL

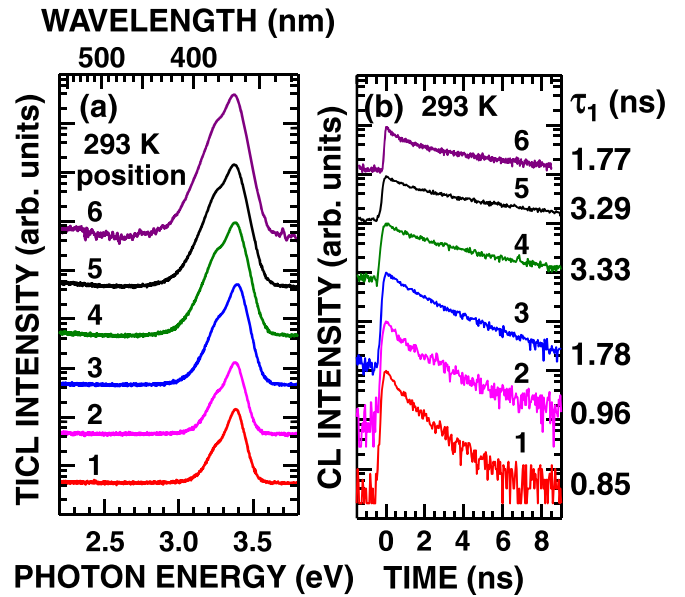


FIG. 7. Position dependent (a) TICL spectra and (b) TRCL decay signals for the NBE emission of FS-GaN sample C3 measured at 293 K. The number corresponds to the position encircled in Fig. 6. [Reproduced with permission from Appl. Phys. Lett. **101**, 212106 (2012). Copyright 2012 AIP Publishing LLC].³⁷

measurement. However, weak excitation conditions are still maintained. In these local CL spectra in Fig. 7(a), subtle redshifts of the NBE emission peak inside and on the peripheries of the trapezoid were found. This can be attributed to the local strain or increased residual electron concentration. Although we fitted the TRCL decay curves in Fig. 7(b) by a double exponential function, the curves at several positions can be mostly fitted by a single exponential function, different from the macroarea TRPL decay curve at room temperature shown in Fig. 5(a). This result may indicate that local excitation by a focused e -beam gives rise to the excitation of a portion of nearly homogeneous N_{NRC} within L_{minority} . As shown, τ_1 significantly varied depending on the positions. The decrease of τ_1 near the visual defects in the CL image at 293 K [see Fig. 7(b)] can be understood as enhanced recombination at NRCs because τ_1 at room temperature is dominated by τ_{NR} , as shown in Fig. 5(c). By contrast, local τ_1 values measured at 10 K were almost independent of the positions being 180 ps (data not shown here). This is reasonable since τ_{R} dominates the CL lifetime (τ_{CL}) at low temperature.

The values of local R_q [$I_{\text{CL}}(T \text{ K})/I_{\text{CL}}(20 \text{ K})$] for the NBE CL of HVPE FS-GaN (C3 and C4) are plotted as a function of τ_1 in Fig. 8. For the sample C3, R_q values measured at the positions 1–6 are used. The R_q value can be used as η_{int} since N_{NRC} in FS-GaN is lower than the critical value shown in Fig. 2 and STRCL was carried out under the weak excitation conditions.³⁷ The macroarea PL data for C0, M2, and GaN templates are also shown. As can be seen, η_{int} appears to linearly increase with the increasing τ_1 . This result is reasonable according to Eq. (3), when we assume that τ_{R} of GaN is 40 ns (Ref. 13) and τ_{CL} is dominated by τ_{NR} at room temperature. Although the overall trend of higher η_{int} in the local measurement may indicate somewhat higher excitation

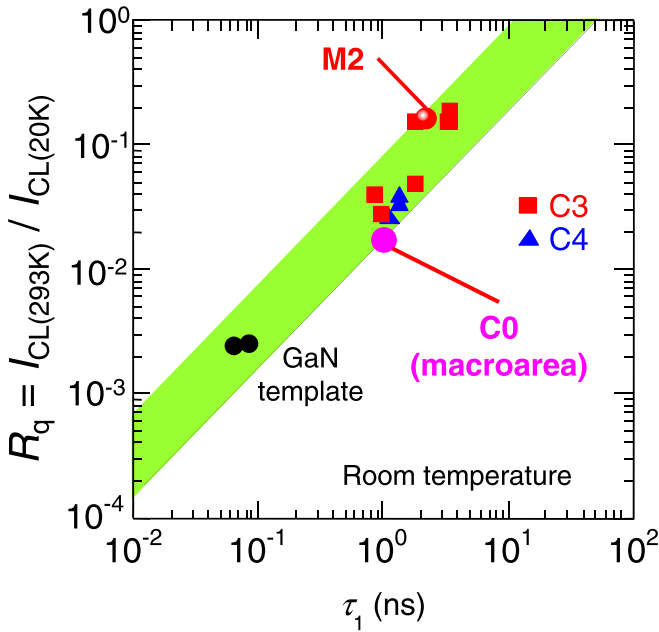


FIG. 8. Spatially resolved local R_q at room temperature [$I_{CL}(293\text{K})/I_{CL}(20\text{K})$] for the NBE emission of HVPE FS-GaN samples C3 and C4,³⁷ as a function of τ_1 . The macroarea PL data for C0, M2, and GaN templates are also shown. [Reproduced with permission from Appl. Phys. Lett. **101**, 212106 (2012). Copyright 2012 AIP Publishing LLC].³⁷

density used,³⁸ the spatially focused excitation in STRCL can selectively probe highly luminescent regions that are less affected by NRCs. As a result, a record high η_{int} of about 20% was obtained for position 4 in Fig. 2, where τ_1 was about 3.33 ns.³⁷

For understanding the role of NRCs on the recombination dynamics, τ_{PL} of HVPE FS-GaN (C0) and MOVPE FS-GaN at 300 K is plotted as a function of N_{NRC} in Fig. 9 by closed circles.³⁴ Here, $[V_{\text{Ga}}V_{\text{N}}]$ estimated from Figs. 3 and 4 are used as N_{NRC} . Right y-axis shows η_{int} at 300 K derived from Eqs. (1) and (3) using the intrinsic τ_{R} of 40 ns.^{13,37,49}

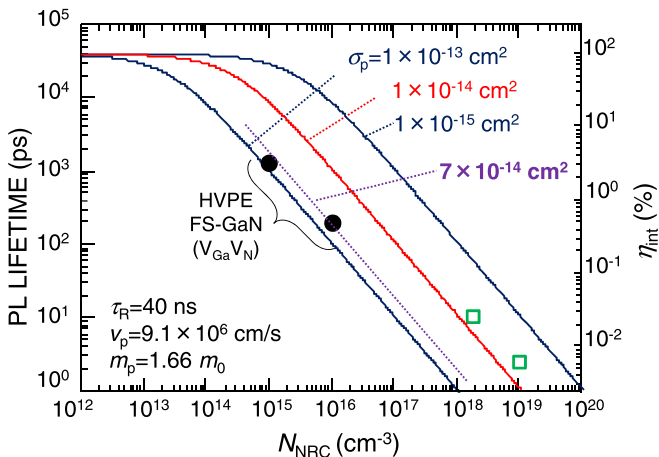


FIG. 9. PL lifetime (τ_{PL}) and corresponding η_{int} at 300 K of HVPE FS-GaN (C0) and MOVPE FS-GaN as a function of N_{NRC} , which is $[V_{\text{Ga}}V_{\text{N}}]$ (closed circles). The τ_{PL} data for Fe-doped GaN⁵² are also shown by open squares for comparison. Three $\tau_{\text{PL}}-N_{\text{NRC}}$ curves are drawn for the cases with σ_p ranging from 1×10^{-15} to 1×10^{-13} cm^2 . [Reproduced with permission from Chichibu *et al.*, Adv. Mater. **29**, 1603644 (2017). Copyright 2017 John Wiley and Sons].³⁴

The τ_{PL} values reported by Aggerstam *et al.*⁵² for Fe-doped GaN are shown by open squares for comparison, as $\text{Fe}_{\text{Ga}}^{2+/3+}$ deep acceptors act as killer NRCs. Obviously, τ_{PL} is decreased by increasing N_{NRC} . In n-type GaN, τ_{NR} is limited by C_p , which is a product of σ_p and v_p ($C_p = \sigma_p \cdot v_p$), and N_{NRC} . Then, $\tau_{\text{PL}}-N_{\text{NRC}}$ relationship can be predicted using the relation $1/\tau_{\text{PL}} = 1/\tau_{\text{R}} + v_p \cdot \sigma_p \cdot N_{\text{NRC}}$. This relationship predicts that $\tau_{\text{PL}}-N_{\text{NRC}}$ relation shows a straight line under low excitation and high N_{NRC} conditions, where τ_{NR} dominates τ_{PL} . In Fig. 9, three ideal curves are drawn for representative σ_p of 1×10^{-15} , 1×10^{-14} , and 1×10^{-13} cm^2 using $\tau_{\text{R}} = 40$ ns and $m_p = 1.66m_0$, where m_0 is a free electron mass. As shown, σ_p of the intrinsic NRCs in GaN ($V_{\text{Ga}}V_{\text{N}}$) is obtained as approximately 7×10^{-14} cm^2 . It seems that $V_{\text{Ga}}V_{\text{N}}$ has larger σ_p than isolated $\text{Fe}_{\text{Ga}}^{2+/3+}$ center⁵² as it is a complex defect. The present σ_p value is close to those previously reported for a carbon deep acceptor on a N site (C_{N})¹⁶ or another acceptor-type defects in GaN (Refs. 53 and 54), as well as those of the $Z_{1/2}$ center⁵⁵ in 4H-SiC being 6.5×10^{-14} cm^2 (Ref. 56), of which origin is a C vacancy, V_{C} .⁵⁷

B. Influences of N vacancies in Mg-doped GaN

Different from the case of n-type GaN, V_{N} formation^{15,20,58} influences the optical properties of epitaxial and I/I GaN:Mg. In this section, low temperature and room temperature PL features of those samples are discussed in order. The PL spectra at 10 K of the UID and epitaxial GaN:Mg films fabricated on a HVPE FS-GaN substrate after annealing at 1300 °C are shown in Figs. 10(a)–10(d) by upper solid lines.³² The PL intensity axis has a unit of count per second (cps); hence, the absolute intensities can be compared. As shown in Fig. 10(a), the UID GaN film exhibited distinct NBE PL peaks and shoulders originating from the recombination of free excitons (FXs), recombination of excitons bound to a neutral donor (DBEs), and their LO phonon replicas at the energies higher than 3.2 eV. In addition to these, YL band^{14–16} was also found. It may have two independent origins, namely, the transition of an electron in the conduction band (CB) or bound to a donor to C_{N} deep acceptor⁵⁶ and a donor-acceptor-pair (DAP) recombination between a donor impurity such as an oxygen on a N site and a V_{Ga} .¹⁵ The dominant excitonic emission peak switched from DBE in UID GaN to the peak originating from the recombination of excitons bound to a neutral Mg_{Ga} acceptor (ABE) in the epitaxial GaN:Mg with $[\text{Mg}]$ of 5×10^{17} and 2×10^{18} cm^{-3} , as shown in Figs. 10(b) and 10(c), respectively. In addition, a UV luminescence (UVL) band originating from a transition of an electron in CB or bound to a shallow donor to a Mg_{Ga} acceptor at around 3.26 eV (Ref. 58) appeared in the PL spectra of epitaxial GaN:Mg films [Figs. 10(b)–10(d)]. Such a simultaneous observation of ABE and UVL indicates the formation of Mg_{Ga} acceptors. Their PL spectra also exhibited characteristic emission bands originating from deep levels (DLs) at around 2.35 and 1.80 eV, instead of YL. They are generally known as the green luminescence (GL) band and red luminescence (RL) band, respectively.⁵⁸ Accordingly, the emergence of GL and RL is also attributable to one of the basic Mg-doping effects in GaN. By using the first-

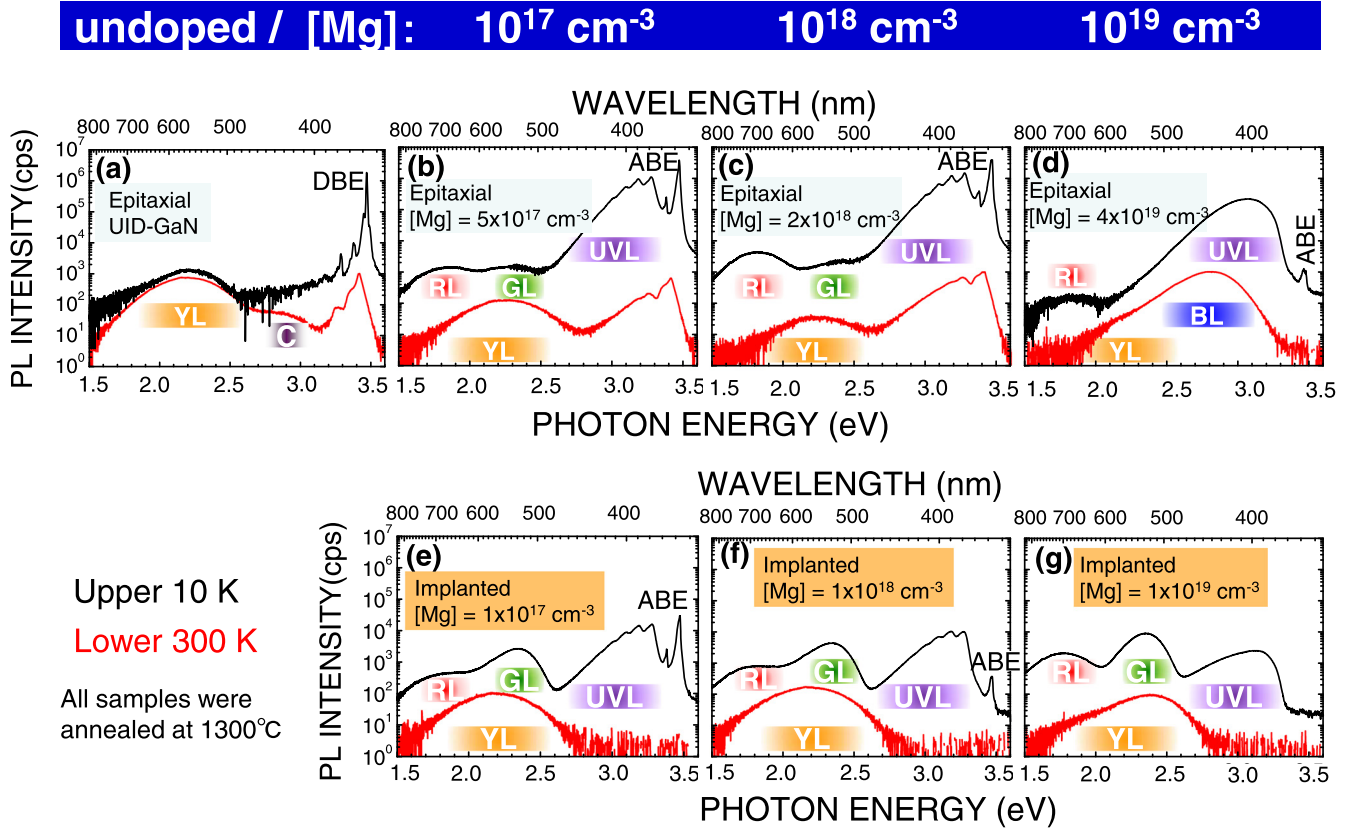


FIG. 10. Steady-state PL spectra of (a) UID GaN, (b)–(d) epitaxial GaN:Mg, and (e)–(g) I/I GaN:Mg films grown on HVPE FS-GaN substrates. The $[Mg]$ values for the epitaxial GaN:Mg were (b) 5×10^{17} , (c) 2×10^{18} , and (d) $4 \times 10^{19} \text{ cm}^{-3}$. The $[Mg]$ values for the flat concentration region (nearly 500 nm from the surface) of I/I GaN:Mg were (e) 1×10^{17} , (f) 1×10^{18} , and (g) $1 \times 10^{19} \text{ cm}^{-3}$. The PL measurement was carried out at 10 K (top traces) and 300 K (bottom traces). [Reproduced with permission from Kojima *et al.*, Appl. Phys. Express **10**, 061002 (2017). Copyright 2017 The Japan Society of Applied Physics].³²

principles calculations, Reshchikov *et al.*⁵⁸ have suggested that V_N is the origin of GL, because UID GaN epitaxial films grown by MBE under Ga-rich conditions frequently exhibit GL without Mg-doping at 300 K, where such UID films were highly resistive. The enhanced formation of V_N in GaN:Mg films is likely as E_{Form} of V_N and $V_N\text{-Mg}_{\text{Ga}}$ complexes decrease with lowering E_F .^{20,58} In GaN:Mg film with $[Mg]$ of $4 \times 10^{19} \text{ cm}^{-3}$, integrated spectral NBE emission intensity was lower than that of UID and less Mg-doped samples, as shown in Fig. 10(d). In such heavily Mg-doped GaN epilayers, UVL usually broadens and its lower energy tail overtakes GL. The peak energy of such DL emission was lower than those in lightly doped GaN:Mg due to the randomly fluctuating potentials.⁵⁹ It should be noted that $[Mg]$ of 3 to $4 \times 10^{19} \text{ cm}^{-3}$ is routinely used to obtain a p-type GaN ($p = 1 \times 10^{18} \text{ cm}^{-3}$) hole-injecting layer in light-emitting devices, and the emergence of blue luminescence (BL) band at 300 K in Fig. 10(d) is a fingerprint of p-type conductivity of GaN:Mg.

Uedono *et al.*³⁰ have studied vacancy-type defects in GaN:Mg films fabricated on FS-GaN substrates by MOVPE using the PAS method. They have concluded that $[V_{\text{Ga}}]$ in GaN:Mg films with $[Mg]$ lower than $2 \times 10^{18} \text{ cm}^{-3}$ was comparable to or lower than that in UID GaN before and after activation annealing.^{11,30} However, the effects of the change in E_F on the charge state of V_{Ga} -related defects, which modifies the e^+ trapping probability, have not been considered for analyzing $[V_{\text{Ga}}]$ from S in p-type GaN.³⁰

Nevertheless, GaN:Mg films with $[Mg]$ of $4 \times 10^{19} \text{ cm}^{-3}$ has been concluded to contain multiple vacancies such as $V_{\text{Ga}}(V_N)_2$ or $V_{\text{Ga}}(V_N)_3$, most probably $V_{\text{Ga}}(V_N)_2$, both before and after annealing.³⁰ Although the defect concentration was slightly decreased by increasing the annealing temperature (T_a),³⁰ it was clearly higher than the detection limit of PAS being approximately a few times 10^{15} cm^{-3} (in n-type GaN). Because PAS is insensitive to positively charged or interstitial-type point defects⁸ such as V_N and Mg interstitials, GaN:Mg films of low $[Mg]$ may contain certain amounts of V_N owing to the Fermi-level effect^{15,20,58} and surface nonstoichiometry during the growth.²¹ The incorporation of V_N likely results in weak but detectable GL and RL bands, as shown in Figs. 10(b)–10(d). By comparing Figs. 10(a)–10(c) and Fig. 10(d), it is obvious that NBE (UVL) emission intensity of the sample with $[Mg]$ of $4 \times 10^{19} \text{ cm}^{-3}$ is more than an order of magnitude lower than those of UID or lower $[Mg]$ samples even at 10 K. This result implies that the highest $[Mg]$ sample contains higher concentration NRCs. Judging from Fig. 2, N_{NRC} of this particular sample is predicted to be higher than, at least, a few times 10^{16} cm^{-3} . This concentration range agrees with that of unknown donors (or donor-type defects) obtained from temperature-variable Hall effect measurements⁶⁰ on epitaxial GaN:Mg films of quite similar $[Mg]$, which were grown on FS-GaN substrates manufactured by the same supplier (Mitsubishi Chemical Corp.). Such defects may act as NRCs as the energy level is higher than E_F of the p-type GaN:Mg sample.

The Mg I/I drastically changed the electronic properties of GaN, as follows.³² The top traces of Figs. 10(e)–10(g) show the low-temperature PL spectra of I/I GaN:Mg after annealing at 1300 °C. It is noted that all I/I samples exhibited UVL band, and the result indicates successful formation of Mg_{Ga} acceptors by using I/I with subsequent annealing. This fact encourages to fabricate vertical and lateral current-flow power-switching transistors because the fabrication of p-type GaN by I/I is generally very difficult till now.^{61–63} However, as revealed from Figs. 10(b)–10(g), the absolute intensities of the ABE peak and UVL band were more than two orders of magnitude lower than that of epitaxial GaN:Mg films with comparable [Mg] even at 10 K. In addition, GL band intensities of I/I samples were slightly higher than those of the epilayers, and eventually GL overtook UVL for the highest [Mg] sample, as shown in Fig. 10(g). These results indicate that Mg implantation generates high concentration NRCs and simultaneously increases the concentration of point defects relevant to GL, namely $[V_N]$.⁵⁸ According to the fact that N_{NRC} and $[V_N]$ increased simultaneously, NRCs in I/I GaN:Mg and GL may have a common origin, V_N , whose concentration is sufficiently low in the epitaxial GaN:Mg films. Uedono *et al.* have examined I/I GaN:Mg ($[Mg] = 4 \times 10^{19} \text{ cm}^{-3}$) by using PAS method to find that I/I damage generates multiple vacancies, whose size is larger than that in the epitaxial GaN:Mg:^{30,31} $(V_{Ga})_m(V_N)_n$ clusters, where both m and n may be close to 3.³¹ They also reported³⁰ that the concentration of $(V_{Ga})_m(V_N)_n$ decreased with increasing T_a . However, it did not recover either, and S of I/I GaN:Mg (0.453) was larger than that of epitaxial GaN:Mg films (0.449)³⁰ or S_{DF} (0.442). Accordingly, the present I/I GaN:Mg films likely contain high concentrations of $(V_{Ga})_3(V_N)_3$ clusters.³⁰ Because SRH-type major intrinsic NRCs in n-type GaN are $V_{Ga}V_N$, the donor-type $(V_{Ga})_3(V_N)_3$ most likely acts as NRCs in compensated semi-insulating and p-type²⁰ GaN.

In 4H-SiC, the origin of major intrinsic NRCs in n-type and p-type materials⁵⁵ is the same, namely, $Z_{1/2}$ center, which has similar capture-cross-sections for an electron and a hole.⁵⁶ However, in the case of GaN, the defect species of NRCs in n-type and p-type materials are different. Because the size of NRCs in GaN:Mg $[V_{Ga}(V_N)_2]$ in the epitaxial and $(V_{Ga})_3(V_N)_3$ in the I/I GaN:Mg^{30,31} is larger than that in n-type material $(V_{Ga}V_N)$, their electron capture-cross-sections (σ_n) would be larger than σ_p of $V_{Ga}V_N$ ($\sim 7 \times 10^{-14} \text{ cm}^2$).³⁴ Because electron mobility is higher than hole mobility in GaN, the NBE emission intensity in p-type GaN becomes significantly weaker than that in n-type material. As a matter of fact, τ_{PL} of the NBE emission in GaN:Mg epilayer was significantly shorter than the n-type GaN,³² and the I/I GaN:Mg did not emit the NBE emission at room temperature, as shown in Figs. 10(e)–10(g).

C. Nonradiative recombination centers in $Al_{0.6}Ga_{0.4}N$

Because E_{Form} of V_{Al} in AlN is very low and even negative^{20,22,23} in n-type materials, V_{Al} has been found to be the major vacancy defects in AlN (Ref. 64) and $Al_xGa_{1-x}N$ alloys ($x \neq 0$).⁶⁵ Therefore, impacts of point defects

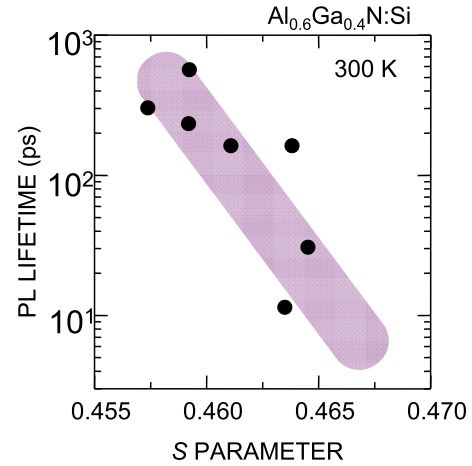


FIG. 11. τ_{PL} - S relationship for the $Al_{0.6}Ga_{0.4}N:Si$ films at various [Si]. [Reproduced with permission from J. Appl. Phys. **113**, 213606 (2013). Copyright 2013 AIP Publishing LLC].²¹

introduced by impurity doping on the recombination dynamics in $Al_xGa_{1-x}N$ must be studied carefully, as V_{Al} -complexes may also act as NRCs. It is noteworthy that significant correlation between τ_1 and S (τ_1 - S relation) seen in GaN is also remarkable in $Al_{0.6}Ga_{0.4}N:Si$ films, as shown in Fig. 11. Almost linear τ_1 - S relation indicates that the major NRCs in the $Al_{0.6}Ga_{0.4}N:Si$ films are most likely composed of V_{III} , such as $V_{Al}X$ and $V_{Ga}X$, because τ_{PL} at room temperature is generally dominated by τ_{NR} . In analogy with n-type GaN, $V_{Al}V_N$ and $V_{Ga}V_N$ divacancies are the most alarming culprits.

IV. CONCLUSION

The limiting factors of $\tau_{minority}$ (τ_{NR} of the NBE emission) in various quality n-type GaN, GaN:Mg, and $Al_{0.6}Ga_{0.4}N:Si$ alloy films were investigated using time-resolved luminescence and PAS measurements. The room-temperature τ_{NR} in n-type GaN of a variety of TDD, growth orientations, polar directions, and polytypes, which were grown by various growth techniques, increased with the decrease in $[V_{Ga}V_N]$. The τ_{NR} value also increased with the increase in L_+ , and these results indicate that major intrinsic NRC is $V_{Ga}V_N$. From the relationship between τ_{NR} and N_{NRC} , its σ_p was determined as $7 \times 10^{-14} \text{ cm}^2$. The major NRCs in the epitaxial and I/I GaN:Mg are assigned to larger size multiple vacancy complexes such as $V_{Ga}(V_N)_n$ ($n=2$ or 3) and $(V_{Ga})_3(V_N)_3$, respectively. In analogy with GaN, major NRCs in $Al_{0.6}Ga_{0.4}N$ alloys are assigned to vacancy complexes containing V_{III} such as $V_{Al}V_N$ and $V_{Ga}V_N$ divacancies.

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