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## Measuring the Impacts of Personal and

 Corporate Income Tax Cuts on a Small Island Open EconomyAli Bayar<br>Mário Fortuna<br>Cristina Mohora<br>Masudi Opese<br>Suat Sisik

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# Measuring the Impacts of Personal and Corporate Income Tax Cuts on a Small Island Open Economy 

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## RESUMOIABSTRACT

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In 1999, subsequent to a legislative review, the authorities of the Azores, an autonomous region of Portugal, decided to reduce income tax rates applicable locally by $30 \%$ in the case of corporate income and by $20 \%$ in the case of personal income. There was no debt or transfer compensation for this tax reduction, meaning that the regional budget was reduced by the equivalent amount of the tax reduction. The current paper analyses the impact of such a shock on various macro and micro variables pertaining to the Azorean economy, including social welfare, using a dynamic CGE model comprising forty five sectors, six household groups, three government levels and four trading partners. It is concluded that the short run impact on GDP is, as expected, negative, given that the marginal propensity to save of the private sector is positive and there was no compensating policy. There is an initial increase in unemployment due to the cut in government expenditures. In the long run, however, the impact becomes positive due to increased investment and private consumption. The stronger effect comes from the reduction in personal income taxes, a much greater proportion of all taxes collected in the region. Real wages net of personal income taxes rise as does the labour supply. The impact of the policy is shown to be positive for all household income groups, as evaluated through equivalent variation. The lowest income group ends up benefiting the most, in relative terms.

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# MEASURING THE IMPACTS OF PERSONAL AND CORPORATE INCOME TAX CUTS ON A SMALL ISLAND OPEN ECONOMY 

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#### Abstract

In 1999, subsequent to a legislative review, the authorities of the Azores, an autonomous region of Portugal, decided to reduce income tax rates applicable locally by $30 \%$ in the case of corporate income and by $20 \%$ in the case of personal income. There was no debt or transfer compensation for this tax reduction, meaning that the regional budget was reduced by the equivalent amount of the tax reduction. The current paper analyses the impact of such a shock on various macro and micro variables pertaining to the Azorean economy, including social welfare, using a dynamic CGE model comprising forty five sectors, six household groups, three government levels and four trading partners. It is concluded that the short run impact on GDP is, as expected, negative, given that the marginal propensity to save of the private sector is positive and there was no compensating policy. There is an initial increase in unemployment due to the cut in government expenditures. In the long run, however, the impact becomes positive due to increased investment and private consumption. The stronger effect comes from the reduction in personal income taxes, a much greater proportion of all taxes collected in the region. Real wages net of personal income taxes rise as does the labour supply. The impact of the policy is shown to be positive for all household income groups, as evaluated through equivalent variation. The lowest income group ends up benefiting the most, in relative terms.


## 1. Introduction

In 1999, subsequent to a legislative review, the authorities of the Azores, an autonomous region of Portugal, decided to reduce income tax rates applicable locally by $30 \%$ in the case of corporate income and by $20 \%$ in the case of personal income. Part of the rationale for the tax reduction was that, being an outermost region, far from the continent, with lagging economic development and with higher costs of living, it would be fair to reduce the tax burden on firms and on families. Prior to this, since 1986 , the value added tax applicable in this region was already reduced by $30 \%$ relative to the national rates.

In essence, the local authorities, under cover of legislation that allowed for the tax rate adaptation, lowered the tax rates pegging them to the national rates.

The 1999 adaptation of the tax law occurred with the approval of a new regime of intergovernmental transfers whereby the local government kept all the tax revenues that were generated by economic activity undertaken in the region plus transfers to a cohesion fund and additional transfers arising from national solidarity, based on a pre determined formula. For its financing, the government could also resort to debt, a prerogative that was later suspended when Portugal approached the upper deficit limit established by the stability and growth pact. Under the established tax regime, any tax reduction undertaken by the regional authorities had no compensation in other transfers from the central or other levels of government. As such, a tax reduction meant a transfer of financial resources from the government budget to firms and to families.

The current paper analyses the impact of such a shock on various macro and micro variables pertaining to the Azorean economy, including GDP, employment, social
welfare and household income group distribution, using a CGE model comprising forty five sectors, six household groups and four trading partners.

In what follows, in section two we proceed to characterize the tax and transfer system that applies in the Azores and the changes that were introduced with the 1999 tax reduction bills. In section three we present the main features of a CGE model of the Azorean economy and the expected impacts of a corporate and personal income tax reduction. Section four we analyses the results of the tax reduction package on various relevant variables. Finally, section five presents some concluding remarks and suggestions.

## 2. The Azorean Tax and Transfers Systems

The Azores, like Madeira, is an autonomous region of Portugal. The statute of autonomy was established in 1976 creating local authorities, including a regional assembly and a regional government, with extensive powers over the application of its own financial resources coming, mainly, from taxes, transfers and debt.

Until 1998, with the publication of a clarifying law, the regional government had no legal basis to adapt the national tax system to its own policy preferences. As such the tax system and the tax rates applicable in the Azores were those applicable in the rest of the country. The only exception was the rates of VAT which were $30 \%$ lower since 1986, by deliberation of the national authorities. In this casa, even though the tax rates on VAT were lower and even though the economic base of the Azores was considerably weaker than that of Portugal, VAT revenues were attributed to this region on the basis of the nation per capita VAT revenue. This implies, of course, that
registered VAT revenues were in fact a combination of two components: one that reflected the effectively generated tax on the basis of the transactions undertaken in this economy and a subsidy component, given that the national economy had a stronger average tax base and paid according to higher rates.

As of 1998, the regional authorities were empowered to either increase existing corporate and personal income taxes by a maximum of $10 \%$ or reduce them by a maximum of $30 \%$. They were also empowered to create other taxes they considered necessary.

In 1999, the regional authorities deliberated a corporate and personal income tax reduction of, respectively, $30 \%$ and $20 \%$, the latter one in two steps, $15 \%$ in 1999 and $20 \%$ in 2000.

The revenue formula for the regional budget is described in the following paragraphs.

The main revenue sources of the regional budget, previous to the tax change can be

$$
R_{i}^{*}=\sum_{j=1}^{J} t_{j}^{*} B_{j}^{i}+T_{i}\left(1+\eta_{z}\right)+T R O W
$$

represented by the following expression
where $\mathrm{R}_{\mathrm{i}}{ }^{*} \quad$ represents total normal revenues of region i , where i can be the Azores;
$\mathrm{t}_{\mathrm{j}} \quad$ is the national tax rate for each tax base j ;
$B_{j}^{i} \quad$ is the tax base j , in region i ;
$\mathrm{T}_{\mathrm{i}} \quad$ are transfers to region i , established by a predetermined formula;
is the rate factor that multiplies by the basic transfers to determine the additional transfers for investment (national cohesion funds);

TROW are transfers from the rest of the world, mainly EU funds.

Two restrictions apply to the above formula, one establishing a lower bound for transfers and another establishing a lower bound for VAT revenues.

The restriction on transfers safeguards that nominal transfers in any year is at least equal to the transfers of the previous year adjusted for the growth of current expenditures of the national budget.

$$
\mathrm{T}_{\mathrm{i}} \geq(1+\Upsilon) \mathrm{T}_{\mathrm{i}, \mathrm{t}-1}
$$

where $\Upsilon$ is the growth rate of current expenditures in the national budget.

The restriction on VAT contemplates the fact that the revenue should be, at minimum, according to the national per capita values.

$$
\mathrm{t}^{\mathrm{i}}{ }_{\mathrm{AAT}} \mathrm{~B}^{\mathrm{i}}{ }_{\mathrm{AT}}+\mathrm{Y} \geq\left(\mathrm{P}_{\mathrm{r}} / \mathrm{P}_{\mathrm{n}}\right) \mathrm{VAT}_{\text {national }}
$$

where $\mathrm{t}^{\mathrm{i}}{ }_{\text {VAT }}$ is the regional vat rate,
$B_{\text {VAT }}^{i}$ is the regional VAT base,
Y is the implicit transfer,
$\mathrm{P}_{\mathrm{r}} \quad$ is the regional population,
$\mathrm{P}_{\mathrm{n}} \quad$ is the national population,
$\mathrm{VAT}_{\text {national }}$ is the national VAT revenue

With the tax reduction the first term of the revenue expression becomes

$$
\sum_{j=1}^{J}\left(t_{i}^{j}-t^{* j}\right) B_{i}^{j}
$$

for $\mathrm{j} \neq \mathrm{VAT}$, where
$t_{i}^{j} \quad$ is the regional tax rate and
$\mathrm{t}^{* j} \quad$ is the national tax rate.
Revenues are therefore given by the following expression

$$
R_{i}=\sum_{j=1}^{J} t_{j}^{*} B_{j}^{i}-\sum_{j=1}^{J}\left(t_{i}^{j}-t_{j}^{*}\right) B_{i}^{j}+Y+T_{i}\left(1+\eta_{z}\right)+T R O W
$$

Given this expression, a tax reduction has no interference with other tax revenue sources or with other transfer sources or, for that matter, with any debt financing criteria. It becomes a simple transfer of resources from the government to the public.

## 3. The Model

The current version of the modelling platform of the Azores economy is represented by a dynamic multi-sectoral computable general equilibrium model (CGE), which incorporates the economic behaviour of six economic agents: firms, households, regional government, Mainland government, European Commission and the external sector.

The goods-producing sectors, consisting of both public and private enterprises, are disaggregated into 45 branches of activity. Households are divided into six income groups, to analyze the distributional effects of various policy measures. Special attention is paid to the economic links between the regional government, the

Mainland government and the European Commission. With regard to the rest of the world the economy is treated as a small open economy with no influence on (given) world market prices. Trade relations are differentiated according to four main trade partners: Mainland, EU, US and the rest of the world. The behaviour of each agent in the model is described in detail below.

The model has been solved by using the general algebraic modelling system GAMS (Rosenthal, 2006).

The following conventions are adopted for the presentation of the model. Variable names are given in capital letters, small letters denote parameters calibrated from the database (SAM) and elasticity parameters. The subscript $s$ stands for one of the production activities (45 branches of activity). The subscript $c$ stands for one of the commodities (45 types of commodities). The subscript qu stands for one of the households' income groups (6 households' income groups). The subscript ctm stands for one of the trade and transport services (7 types of trade and transport services), while nctm stands for all the other commodities except trade and transport services (38 types of commodities).

### 3.1. Firms

CGE models do not take into account the behaviour of individual firms, but of groups of similar ones aggregated into branches. A presentation of the production sectors considered in AzorMod is provided in Table 1.

The usual assumption for such a model is that producers operate in perfectly competitive markets and maximize profits (or minimize costs for each level of output) to determine the optimal levels of inputs and output. Furthermore, production prices
equal average and marginal costs, a condition implied by profit maximization for a constant returns to scale technology.

The level of production for each branch of activity is determined from a nested production structure (see Figure 1). In the first stage, producers are assumed to choose between intermediate inputs and value-added according to a Leontief production function. In the second stage, the optimal mix between capital and labour is given by another optimization process, where substitution possibilities between capital and labour are represented by a constant elasticity of substitution (CES) function. Firms' costs related to corporate income tax and social security contributions are also taken into account in the optimization process.


Figure 1. The nested Leontief and CES production technology for the domestic production by branch of activity

Value-added $\left(K L_{s}\right)$ is related to domestic production by branch $s\left(X D_{s}\right)$ through a Leontief production function, which assumes an optimal allocation of inputs:
$K L_{s}=a K L_{s} \cdot X D_{s}$
where $a K L_{s}$ is the well-known fixed coefficient relating value-added to domestic production. Similarly, total intermediate inputs used by industry $s\left(I_{s}\right)$ are derived as:
$I O_{s}=\sum_{c} i o_{c, s} \cdot X D_{s}$
where $i o_{c, s}$ are the technical coefficients. Thus, domestic production valued at basic prices net of taxes (tp $)$ but including direct subsidies ( $t s p_{s}$ ) on production from the regional government and direct subsidies on production from the European Agricultural Guidance and Guarantee Fund (EAGGF) (tspeuea ${ }_{s}$ ), from the Financial Instrument for Fisheries Guidance (FIFG) (tspeufis ${ }_{s}$ ), from the European Regional Development Fund (ERDF) (tspeuer ${ }_{s}$ ), from the European Social Fund (ESF) (tspeues ${ }_{s}$ ) and from US (tspusa $a_{\mathrm{s}}$ ), is given by the sum of value-added $\left(K L_{\mathrm{s}}\right)$ for branch $s$ valued at basic prices $\left(P K L_{s}\right)$ and intermediate commodities used by sector $s$ valued at the price of the commodities $\left(P_{c}\right)$, less subsidies on intermediate consumption (tsic $c_{c, s}$ ) but including the trade and transport margins $\left(\sum_{c t m}\right.$ tcictm $\left._{c m m, s, s} \cdot P_{c t m}\right)$ and value-added taxes (vatic $c_{c, s}$ ) on intermediate consumption:

$$
\begin{align*}
& P D_{s} \cdot\left(1-t p_{s}+t s p_{s}+t s p e u e a_{s} \cdot \text { MUtspeu }+t s p e u i_{s} \cdot \text { MUtspeu }+ \text { tspeuer }_{s} \cdot \text { MUtspeu }+\right. \\
& \text { tspeues } \left._{s} \cdot \text { MUtspeu }+ \text { tspusa }_{s}\right) \cdot \text { XD }_{s}=P K L_{s} \cdot K L_{s}+  \tag{3}\\
& \sum_{c}\left\{\text { io }_{c, s} \cdot X D_{s} \cdot\left[\left(1-\text { tsic }_{c, s}\right) \cdot P_{c}+\sum_{c t m} \text { tcictm }_{c t m, c, s} \cdot P_{c t m}\right] \cdot\left(1+\text { vatic }_{c, s}\right)\right\}
\end{align*}
$$

Parameter MUtspeu insures the consistency between the total EU funds provided as subsidies on production and the EU subsidies on production by branch of activity.

The trade and transport margins are valued at the price $\left(P_{c t m}\right)$ of the corresponding service (trade services or transport services), while tcictm $_{\text {cmm,s }}$ represents the trade and transport services ctm per unit of intermediate consumption of commodity $c$ by branch $s$.

Value-added is a CES aggregation of capital ( $K S K_{s}$ ) and labour $\left(L S K_{s}\right)$ :

$$
\begin{equation*}
K L_{s}=a F_{s} \cdot\left[\gamma F K_{s} \cdot K S K_{s}^{-\rho F_{s}}+\gamma F L_{s} \cdot L S K_{s}^{-\rho F_{s}}\right]^{-1 / \rho F_{s}} \tag{4}
\end{equation*}
$$

Minimizing the costs function:

Table 1: Activity and commodity disaggregation in AzorMod

| 1 | Agriculture, hunting and forestry, logging |
| :--- | :--- |
| 2 | Fishing |
| 3 | Mining and quarrying |
| 4 | Production of meat and meat products |
| 5 | Processing of fish and fish products |
| 6 | Manufacture of dairy products |
| 7 | Prepared animal feeds |
| 8 | Beverages \& tobacco products |
| 9 | Fruits, vegetables, animal oils, grain mill, starches |
| 10 | Textiles and leather |
| 11 | Wood and products of wood and cork |
| 12 | Pulp, paper products; publishing and printing |
| 13 | Coke, refined petroleum products and nuclear fuel |
| 14 | Chemicals and chemical products |
| 15 | Rubber and plastic products |
| 16 | Other non-metallic mineral products |
| 17 | Basic metals and fabricated metal products |
| 18 | Machinery and equipment n.e.c. |
| 19 | Electrical and optical equipment |
| 20 | Transport equipment |
| 21 | Manufacturing n.e.c. |
| 22 | Electricity, gas, steam and hot water supply |
| 23 | Collection, purification and distribution of water |
| 24 | Construction |
| 25 | Sale, maintenance, repair of motor vehicles and motorcycles |
| 26 | Wholesale trade and commission trade, except of motor vehicles and |
|  | motorcycles |
| 27 | Retail trade, except of motor vehicles and motorcycles |
| 28 | Hotels and restaurants |
| 29 | Land transport; transport via pipelines |
| 30 | Water transport |
| 31 | Air transport |
| 32 | Supporting transport activities; activities of travel agencies |
| 33 | Post and telecommunications |
| 34 | Financial intermediation, excluding insurance and pension funding |
| 35 | Insurance and pension funding, except compulsory social security |
| 36 | Activities auxiliary to financial intermediation |
| 37 | Real estate activities |
| 38 | Renting of machinery and equipment without operator |
| 39 | Computer and related activities; research and development |
| 40 | Other business activities |
| 41 | Public administration and defence; compulsory social security |
| 42 | Education |
| 43 | Health and social work |
| 44 | Other community, social and personal service activities |
| 45 | Activities of households as employers of domestic staff |

$$
\begin{align*}
& \operatorname{Cost}_{s}\left(K S K_{s}, L S K_{s}\right)=\left[P K_{s} \cdot\left(1+t k_{s}\right)+d_{s} \cdot P I\right] \cdot K S K_{s}+\left[P L \cdot\left(1+\text { premLSK }_{s}\right) .\right. \\
& \left.\left(1+t l_{s} /\left(1-t l_{s}\right)\right)\right] \cdot L S K_{s} \tag{5}
\end{align*}
$$

subject to (4) yields the demand equations for capital and labour:

$$
\begin{align*}
& K S K_{s}=K L_{s} \cdot\left\{P K L_{s} /\left[P K_{s} \cdot\left(1+t k_{s}\right)+d_{s} \cdot P I\right]\right\}^{\sigma F_{s}} \cdot \gamma F K_{s}^{\sigma F_{s}} \cdot a F_{s}^{\left(\sigma F_{s}-1\right)}  \tag{6}\\
& L S K_{s}=K L_{s} \cdot\left\{P K L_{s} /\left[P L \cdot\left(1+p r e m L S K_{s}\right) \cdot\left(1+t l_{s} /\left(1-t l_{s}\right)\right)\right]\right\}^{\sigma F_{s}} \cdot \gamma F L_{s}^{\sigma F_{s}} \cdot a F_{s}^{\left(\sigma F_{s}-1\right)} \tag{7}
\end{align*}
$$

and the associated zero profit condition:

$$
\begin{equation*}
P K L_{s} \cdot K L_{s}=P K_{s} \cdot\left(1+t k_{s}\right) \cdot K S K_{s}+P L \cdot\left(1+\text { premLSK }_{s}\right) \cdot\left(1+t l_{s} /\left(1-t l_{s}\right)\right) \cdot L S K_{s}+D E P_{s} \cdot P I \tag{8}
\end{equation*}
$$

where $P L$ is the national average wage and $\operatorname{premLSK}_{s}$ is the wage differential of branch $s$ with respect to the average wage $P L, t l_{s}$ is the social security contributions rate for industry $s, P K_{s}$ is the return to capital in branch $s, t k_{s}$ is the corporate income tax rate for branch $s$, and $d_{s}$ is the depreciation rate in industry $s$. The depreciation ( $D E P_{s}$ ) related to the private and public capital stock is valued at the investment price index (PI). The elasticity of substitution between capital and labour is given by $\sigma F_{s}$, where $\sigma F_{s}=1 /\left(1+\rho F_{s}\right)$, and $\gamma F K_{s}$ and $\gamma F L_{s}$ represent the distribution parameters corresponding to capital and labour.

Capital is industry specific, introducing rigidities in the capital market. The inter-sectoral wage differential is a parameter derived as the ratio between the wage by branch and the national average wage (Dervis, De Melo and Robinson, 1982). Holding the inter-sectoral wage differentials constant in counterfactual policy simulations introduces rigidities in the labour market.

Each branch of activity in AzorMod produces several types of goods and services. The optimal allocation of domestic production between the different types of commodities is given by a Leontief function:
$X D D E_{c}=\sum_{s} i o C_{s, c} \cdot X D_{s}$
where $X_{D D E}$ represents the domestic production of commodity $c$ by different branches, supplied on the home and foreign markets, $X D_{s}$ is the domestic production of branch $s$, and $i o C_{s, c}$ is a fixed coefficient expressing the volume of production of commodity $c$ by the industry $s$ per unit of production of industry $s$.

The corresponding zero profit condition is given by:
$P D_{s}=\sum_{c} i o C_{s, c} \cdot P D D E_{c}$
where $P D D E_{c}$ is the domestic price of commodity $c$ supplied on the home and foreign markets and $P D_{s}$ is the price index corresponding to domestic production by branch $s$.

Treated at an aggregate level, firms' savings are given by a share of the net operating surplus.

### 3.2. Households

Households are split into six income groups, the first group being the poorest one. The representative household in each income group receives a part of the capital income (net operating surplus), a part of the labour income, unemployment benefits from the Mainland government and other net transfers from the regional and Mainland governments. The representative household in each income group pays income taxes and saves a share of the net income. Household savings by income group qu ( $\mathrm{SH}_{q u}$ ) , are given by:

$$
S H_{q u}=M P S_{q u} \cdot\left(1-t y_{q u}\right) \cdot Y H_{q u}
$$

where $Y H_{q u}$ is the household income, $t y_{q u}$ is the personal income tax rate and $M P S_{q u}$ the household propensity to save. Household propensity to save reacts to changes in the aftertax average return to capital, according to:
$M P S_{q u}=M P S Z_{q u} \cdot\left\{\left[\left(1-t y_{q u}\right) \cdot P K a v r\right] /\left[\left(1-t y z_{q u}\right) \cdot P K a v r Z\right]\right\}^{e l a s S_{u u}}$
where $M P S Z_{q u}$ is the benchmark level of the propensity to save, PKavr is the real average return to capital received by the household, $P$ KavrZ is the benchmark level of $P K a v r,{ }^{\operatorname{tyz}} \mathrm{qu}$ is the benchmark level of the personal income tax rate and elas $S_{q u}$ is the elasticity of savings with respect to after-tax rate of return. Subsequently, household budget disposable for consumption $\left(C B U D_{q u}\right)$ is derived as:

CBUD $_{q u}=\left(1-t y_{q u}\right) \cdot Y H_{q u}-S H_{q u}$

The disposable budget for consumption is allocated between different goods and services according to a Stone-Geary utility function. Maximizing the utility function:

$$
\begin{equation*}
U\left(C_{c, q u}\right)=\prod_{c}\left(C_{c, q u}-\mu H_{c, q u}\right)^{\alpha H_{c q u}} \tag{14}
\end{equation*}
$$

subject to the budget constraint:

$$
\begin{equation*}
C B U D_{q u}=\sum_{c}\left\{\left[P_{c}+\sum_{c t m} \text { tchtm }_{c m, c, q u} \cdot P_{c t m}\right] \cdot\left(1+\text { texc }_{c, q u}\right) \cdot\left(1+\text { vatc }_{c, q u}+t c_{c, q u}\right) \cdot C_{c, q u}\right\} \tag{15}
\end{equation*}
$$

with: $\sum_{c} \alpha H_{c, q u}=1$, yields the demand equations for commodities:

$$
\begin{align*}
& {\left[P_{c}+\sum_{c m} \operatorname{tchtm}_{c m m, c, q u} \cdot P_{c t m}\right] \cdot\left(1+\operatorname{texc}_{c, q u}\right) \cdot\left(1+t c_{c, q u}+v a t c_{c, q u}\right) \cdot C_{c, q u}=\left[P_{c}+\sum_{c t m} \operatorname{tchtm}_{c c m, c, q u} \cdot P_{c t m}\right] .} \\
& \left(1+\operatorname{tex}_{c, q u}\right) \cdot\left(1+t c_{c, q u}+\text { vatc }_{c, q u}\right) \cdot \mu H_{c, q u}+\alpha H_{c, q u} \cdot\left\{C B U D_{q u}-\sum_{c c}\left[P_{c c}+\sum_{c t m} \operatorname{tchtm}_{c t m, c, q u} \cdot P_{c t m}\right] .\right.  \tag{16}\\
& \left.\left(1+\text { texc }_{c c, q u}\right) \cdot\left(1+t c_{c, q, u}+v a t c_{c, q u u}\right) \cdot \mu H_{c c, q u}\right\}
\end{align*}
$$

Consumption of commodity $c$ by income group $q u\left(C_{c, q u}\right)$ is valued at purchaser's prices, which include trade and transport margins $\left(\sum_{c t m} \operatorname{tchtm}_{c m m, q u} \cdot P_{c t m}\right)$, excise duties ( $\operatorname{tex}_{c, q u}$ ),
value-added taxes ( vatc $_{c, \text { qu }}$ ) and other taxes on consumption ( $t c_{c, q u}$ ), where $P_{c}$ is the price of commodity $c$ net of taxes. The trade and transport margins on private consumption are valued at the prices corresponding to the trade and transport services $\left(P_{c t m}\right)$, where tchtm $_{\text {ctmc,cqu }}$ represents the quantity of trade and transport services ctm per unit of commodity $c$ consumed by the income group $q u$.

In the allocation process, the consumer first decides on the minimum (subsistence) level of consumption of commodity $c\left(\mu H_{c, q u}\right)$. Then, the marginal income is allocated between different types of commodities according to the marginal budget shares $\left(\alpha H_{c, q u}\right)$. A schematic representation of households' decisions, by income group, is given in Figure 2.


Figure 2. Decision structure of the representative household by income group

Household welfare gains/losses are valued using the equivalent variation in income $\left(E V_{q u}\right)$, which is based on the concept of a money metric indirect utility function (Varian, 1992).

$$
\begin{align*}
& E V_{q u}=\prod_{c}\left\{\left\{\left[P Z_{c}+\sum_{c t m} t c h t m z_{c t m, c, q u} \cdot P Z_{c t m}\right] \cdot\left(1+t e x c z_{c, q u}\right) \cdot\left(1+t c z_{c, q u}+v a t c z_{c, q u}\right)\right\} /\right.  \tag{17}\\
& \left.\alpha H_{c, q u}\right\}^{\alpha A_{c, q u}} \cdot\left(V U_{q u}-V U I_{q u}\right)
\end{align*}
$$

The indirect utility function $\left(V U_{q u}\right)$ corresponding to the Linear Expenditures System (LES) in the counter-factual (policy scenario) equilibrium is defined as:

$$
\begin{align*}
& V U_{q u}=\left\{C B U D_{q u}-\sum_{c}\left[P_{c}+\sum_{c t c} \operatorname{tchtm}_{c t m, c, q u} \cdot P_{c t m}\right] \cdot\left(1+\text { texc }_{c, q u}\right) \cdot\left(1+t c_{c, q u}+v a t c_{c, q u}\right) \cdot\right. \\
& \left.\mu H_{c, q u}\right\} \cdot \prod_{c}\left\{\alpha H _ { c , q u } \left\langle\left[\{ P _ { c } + \sum _ { c t m } \text { tchtm } _ { c m m , q u } \cdot P _ { c t m } ] \cdot ( 1 + t e x c _ { c , q u } ) \cdot \left(1+t c_{c, q u}+\right.\right.\right.\right. \\
& \text { vatc } \left.\left.\left._{c, q u}\right)\right\}\right\}^{\alpha H_{c q u}} \tag{18}
\end{align*}
$$

and the indirect utility function $\left(V I_{q u}\right)$ in the benchmark equilibrium is given by:

$$
\begin{align*}
& V U I_{q u}=\left\{C B U D Z_{q u}-\sum_{c}\left[P Z_{c}+\sum_{c t m} \operatorname{tchtmz}_{c t m, c, u} \cdot P Z_{c t m}\right] \cdot\left(1+\text { texcz }_{c, q u}\right) \cdot\left(1+\text { tcz }_{c, q u}+v a t c c_{c, q u}\right)\right. \text {. } \\
& \left.\mu H_{c, q u}\right\} \cdot \prod_{c}\left\{\alpha H_{c, q u} /\left\{[ P Z _ { c } + \sum _ { c c m } \operatorname { t c h t m z } _ { c t m , q , q u } \cdot P Z _ { c t m } ] \cdot ( 1 + t e x c z _ { c , q u } ) \cdot \left(1+t c z_{c, q u}+\right.\right.\right.  \tag{19}\\
& \left.\left.\left.\operatorname{vatcz}_{c, q u}\right)\right\}\right\}^{\alpha H_{c q u}}
\end{align*}
$$

where $C B U D Z_{q u}$ is the benchmark level of the disposable budget for consumption, $P Z_{c}$ is the benchmark level of the price of commodity $c$ net of taxes, $\operatorname{tchtmz}_{c m m, c, u}$ is the benchmark level of the trade and transport margin rate, and $\operatorname{texcz}_{c, q u}, \operatorname{vatcc}_{c, q u}$ and $\operatorname{tcz}_{c, q u}$ are the benchmark rates corresponding to excise duties, value-added taxes, and other taxes on consumption, respectively.

Equivalent variation measures the income needed to make the household as well off as she is in the new counter-factual equilibrium (policy scenario) evaluated at benchmark prices. Thus, the equivalent variation is positive for welfare gains from the policy scenario and negative for losses.

### 3.3. Regional government

Regional government collects all the taxes, such as: taxes on income and wealth (TRPROP) and taxes on products and on production (TRPROD) and receives transfers from the

Mainland government, EU funds and transfers from the external sector (TRANSR) (see Figure 3):
$G R E V=T R P R O P+T R P R O D+T R A N S R$
where GREV stands for the total government revenues.


Figure 3. Structure of the regional government budget

The taxes on income and wealth are given by:

$$
\begin{equation*}
T R P R O P=\sum_{q u} t y_{q u} \cdot Y H_{q u}+\sum_{s} t k_{s} \cdot K S K_{s} \cdot P K_{s} \tag{21}
\end{equation*}
$$

In the derivation of each category of tax revenue the tax rate is applied to the corresponding tax base.

Taxes on products are differentiated in the model according to the category of consumption on which they apply: intermediate consumption, private consumption, and gross capital formation. Taxes on products and on production are provided by:

$$
\begin{align*}
& \text { TRPROD }=\sum_{s} t p_{s} \cdot X D_{s} \cdot P D_{s}+\sum_{c, q u}\left\{[ P _ { c } + \sum _ { c t m } \operatorname { t c h t m } _ { c t m , q , q u } \cdot P _ { c t m } ] \cdot \left[\text { texc }_{c, q u}+(1+\right.\right. \\
& \left.\left.\left.\operatorname{texc}_{c, q u}\right) \cdot\left(t c_{c, q u}+\text { vatc }_{c, q u}\right)\right] \cdot C_{c, q u}\right\}+\sum_{c}\left[P_{c}+\sum_{c t m} \operatorname{tcitm}_{c m, c} \cdot P_{c t m}\right] \cdot v a t i_{c} \cdot I_{c}+ \\
& \sum_{c, s}\left[\left(1-t s i c_{c, s}\right) \cdot P_{c}+\sum_{c t m} t c i c t m_{c t m, s, s} \cdot P_{c t m}\right] \cdot \text { vatic }_{c, s} \cdot 0_{c, s} \cdot X D_{s}+\sum_{c}\left(\text { tmus }_{c} \cdot P W M U S_{c} \cdot\right. \\
& \text { MUS } \left._{c} \cdot E R U S\right)+\sum_{c}\left(\text { tmrw }_{c} \cdot \text { PWMROW }_{c} \cdot \text { MROW }_{c} \cdot E R R O W\right) \tag{22}
\end{align*}
$$

where $I_{c}$ represents the investment demand for commodity $c$, tcitm $_{c t m, c}$ gives the trade and transport margin rate on investment good $c$, vatic gives the value-added tax rate on investment good $c$, tmus $_{c}$ represents the tariff rate on commodity $c$ coming from US, $M U S_{c}$ give the imports of commodity $c$ from US, $P W M U S S_{c}$ stands for the import price of commodity $c$ from US expressed in foreign currency and ERUS is the exchange rate with respect to the US dollar. Tariff rate on commodity $c$ coming from the rest of the world (ROW) ( $t m r w_{c}$ ) is applied to the imports of commodity $c$ from the ROW ( $\left.M R O W_{c}\right)$, valued at the import price expressed in foreign currency ( $P W M R O W_{c}$ ), and transformed in domestic currency using the exchange rate ERROW .

The total transfers received by the regional government (TRANSR) are given by transfers from the Mainland government (TRGML), transfers from EU as direct subsidies on production (TRGEC) and other transfers from EU (TRGEU), transfers from US (TRGUS) and transfers from the rest of the world (TRGW):

```
TRANSR = TRGML }\cdotERML+TRGEU EREU+TRGEC E EREU+TRGUS \cdotERUS+
TRGW\cdotERROW
```

where the transfers are expressed in domestic currency using the exchange rate with respect to Mainland (ERML), the exchange rate with respect to EU (EREU ), the exchange rate with respect to US (ERUS) and the exchange rate with respect to the rest of the world (ERROW).

Regional government expenditures (GEXP) comprise the public current consumption (CGBUD), total transfers by the government (TRANS) and subsidies on products and on production (SUBSID):

$$
\begin{equation*}
G E X P=C G B U D+T R A N S+S U B S I D \tag{24}
\end{equation*}
$$

The optimal allocation of the public current consumption between different types of goods and services is given by the maximization of a Cobb-Douglas function:
$U\left(C G_{c}\right)=\prod_{c} C G_{c}^{\alpha C G_{c}}$
subject to the budget constraint:

$$
\begin{equation*}
C G B U D=\sum_{c} P_{c} \cdot C G_{c} \tag{26}
\end{equation*}
$$

with: $\sum_{c} \alpha C G_{c}=1$. The maximization of $U\left(C G_{c}\right)$ yields the demand equations for public current consumption by type of commodity:

$$
\begin{equation*}
P_{c} \cdot C G_{c}=\alpha C G_{c} \cdot C G B U D \tag{27}
\end{equation*}
$$

where $C G_{c}$ represents the public demand for commodity $c, P_{c}$ is the price of commodity $c$ and $\alpha \mathrm{CG}_{c}$ gives the Cobb-Douglas preference parameter corresponding to commodity $c$.

Total transfers by the regional government include transfers to the households $\left(T R H G_{q u}\right)$ :

$$
\begin{equation*}
\text { TRANS }=\sum_{q u} T R H G_{q u} \cdot P C I N D E X \tag{28}
\end{equation*}
$$

translated into nominal terms by using the Laspeyres consumer price index (PCINDEX ).

The total subsidies on products and on production are further derived as:

$$
\begin{align*}
& \text { SUBSID }=\sum_{c, s} \text { tsic }_{c, s} \cdot P_{c} \cdot i o_{c, s} \cdot X D_{s}+\sum_{s}\left[\left(t s p_{s}+\text { tspeuea }_{s} \cdot \text { MUtspeu }^{+}\right.\right. \tag{29}
\end{align*}
$$

The EU funds as direct subsidies on production are transferred to the regional government budget which allocates them between different branches of activity. MUtspeu is a scaling parameter which insures the consistency between the total EU funds and the total subsidies on production distributed to different branches of activity:
$T R G E C \cdot E R E U=$ MUtspeu $\cdot \sum_{s}\left[\left(\right.\right.$ tspeuea $_{s}+$ tspeufi $_{s}+$ tspeuer $_{s}+$ tspeues $\left.\left._{s}\right) \cdot X D_{s} \cdot P D_{s}\right]$

The difference between the regional government revenues and the government expenditures yields the government savings ( $S G$ ).

$$
\begin{equation*}
S G=G R E V-G E X P \tag{31}
\end{equation*}
$$

### 3.4. Mainland government

Mainland government collects all the social security contributions, provides unemployment benefits and makes transfers to the households (TRHML ${ }_{q u}$ ) and to the regional government(TRGML).

Social security contributions are derived by applying the social contributions rate ( $t l_{s}$ ) to gross wages. Unemployment benefits received by each household income group are determined by the combination of the replacement rate (trep), the national average wage (PL), the total number of unemployed (UNEMP), and the share of unemployed subject to unemployment benefits in each household income group (shUNEMPB ${ }_{q u}$ ).

The net transfers by the mainland government to Azores (SGML) , are provided by:

$$
\begin{align*}
& S G M L=\sum_{s}\left[t l_{s} /\left(1-t l_{s}\right) \cdot L S K_{s} \cdot P L \cdot\left(1+\text { premLSK }_{s}\right) / E R M L\right]-\sum_{q u} T R H M L_{q u}- \\
& \sum_{q u}\left(\operatorname{shUNEMPB_{qu}\cdot \operatorname {trep}\cdot PL\cdot UNEMP/ERML)-TRGML}\right. \tag{32}
\end{align*}
$$

### 3.5. European Commission

European Commission provides EU funds as direct subsidies to the production sectors (TRGEC) and other EU funds (TRGEU) to the regional government. The net transfers by the European Commission to Azores (SGEC) are given by:
$S G E C=-T R G E C-T R G E U$

### 3.6. Foreign trade

The specification of the foreign trade is based on the small-country assumption, which means that the country is a price taker in both its import and its export markets. Four different trade partners are distinguished in the model: Mainland, EU, US and the rest of the world.

On the import side, imperfect substitution is assumed between domestically produced and imported goods, according to the Armington function (see Figure 4). Thus, domestic consumers use composite goods ( $X_{c}$ ) of imported and domestically produced goods, according to a CES function:

$$
\begin{align*}
& X_{c}=a A_{c} \cdot\left(\gamma A 1_{c} \cdot M M L_{c}^{-\rho A_{c}}+\gamma A 2_{c} \cdot M E U_{c}^{-\rho A_{c}}+\gamma A 3_{c} \cdot M U S_{c}^{-\rho A_{c}}+\gamma A 4_{c} \cdot M R O W_{c}^{-\rho A_{c}}+\right.  \tag{34}\\
& \left.\gamma A 5_{c} \cdot X D D_{c}^{-\rho A_{c}}\right)^{-1 / \rho A_{c}}
\end{align*}
$$

Minimizing the cost function:

$$
\begin{align*}
& \operatorname{Cost}_{c}\left(M M L_{c}, M E U_{c}, M U S_{c}, M R O W_{c}, X D D_{c}\right)=P M M L_{c} \cdot M M L_{c}+P M E U_{c} \cdot M E U_{c}+ \\
& \text { PMS }_{c} \cdot M U S_{c}+P M R O W_{c} \cdot M R O W_{c}+P D D_{c} \cdot X D D_{c} \tag{35}
\end{align*}
$$

subject to (34) provides the demand for imports from Mainland (MML ${ }_{c}$ ), the demand for imports from EU $\left(M E U_{c}\right)$, the demand for imports from US $\left(M U S_{c}\right)$, the demand for imports from ROW ( $\mathrm{MROW}_{c}$ ), and the demand for domestically produced goods $\left(X D D_{c}\right):$

$$
\begin{equation*}
M M L_{c}=X_{c} \cdot\left(P_{c} / P M M L_{c}\right)^{\sigma A_{c}} \cdot \gamma A 1_{c}^{\sigma A_{c}} \cdot a A_{c}^{\left(\sigma A_{c}-1\right)} \tag{36}
\end{equation*}
$$

$M E U_{c}=X_{c} \cdot\left(P_{c} / P M E U_{c}\right)^{\sigma A_{A}} \cdot \gamma A 2_{c}^{\sigma A_{c}} \cdot a A_{c}^{\left(\sigma A_{c}-1\right)}$

MUS $_{c}=X_{c} \cdot\left(P_{c} / P M U S_{c}\right)^{\sigma A_{c}} \cdot \gamma A 3_{c}^{\sigma A_{c}} \cdot a A_{c}^{\left(\sigma A_{c}-1\right)}$

MROW $_{c}=X_{c} \cdot\left(P_{c} / P M R O W_{c}\right)^{\sigma A_{c}} \cdot \gamma A 4_{c}^{\sigma A_{A}} \cdot a A_{c}^{\left(\sigma A_{c}-1\right)}$
$X D D_{c}=X_{c} \cdot\left(P_{c} / P D D_{c}\right)^{\sigma A_{c}} \cdot \gamma A 5_{c}^{\sigma A_{c}} \cdot a A_{c}^{\left(\sigma A_{c}-1\right)}$
and the corresponding zero profit condition:

$$
\begin{align*}
& P_{c} \cdot X_{c}=P M M L_{c} \cdot M M L_{c}+P M E U_{c} \cdot M E U_{c}+P M U S_{c} \cdot M U S_{c}+P M R O W_{c} \cdot M R O W_{c}+ \\
& P D D_{c} \cdot X D D_{c} \tag{41}
\end{align*}
$$

where $P_{c}$ is the price index of the composite good $c$ incorporating the imported and domestically produced goods supplied on the domestic market, $P M M L_{c}$ represents the domestic price of imports from Mainland, $\mathrm{PMEU}_{c}$ is the domestic price of imports from EU, PMUS $_{c}$ gives the domestic price of imports from US (including tariffs), $P M R O W_{c}$ represents the domestic price of imports from ROW (including tariffs) and $P D D_{c}$ is the price of good $c$ from the domestic producers. $a A_{c}$ represents the efficiency parameter while $\gamma A 1_{c}, \gamma A 2_{c}, \gamma A 3_{c}, \gamma A 4_{c}$ and $\gamma A 5_{c}$ are the distribution parameters corresponding to imports from Mainland, imports from EU, imports from US, imports from ROW and domestic demand for the domestically produced goods, respectively. The elasticity of substitution between imports and domestically produced goods $\left(\sigma \mathrm{A}_{c}\right)$ is given by $1 /\left(1+\rho \mathrm{A}_{c}\right)$.

In a similar fashion, the differentiation between the exported goods by the domestic producers to Mainland ( $E M L_{c}$ ), to EU ( $E E U_{c}$ ), to US ( $E U S_{c}$ ) and to ROW ( $E R O W_{c}$ ) and the domestic goods supplied on the domestic market $\left(X D D_{c}\right)$ is captured through a constant elasticity of transformation (CET) function:

$$
\begin{align*}
& X D D E_{c}=a T_{c} \cdot\left(\gamma T 1_{c} \cdot E M L_{c}^{-\rho T_{c}}+\gamma T 2_{c} \cdot E E U_{c}^{-\rho T_{c}}+\gamma T 3_{c} \cdot E U S_{c}^{-\rho T_{c}}+\gamma T 4_{c} \cdot E R O W_{c}^{-\rho T_{c}}+\right.  \tag{42}\\
& \left.\gamma T 5_{c} \cdot X D D_{c}^{-\rho T_{c}}\right)^{-1 / \rho T_{c}}
\end{align*}
$$

where $X D D E_{c}$ is the domestic production of commodity $c$ by different branches, supplied on the home and foreign markets, $a T_{c}$ is the efficiency parameter, $\gamma T 1_{c}, \gamma T 2_{c}, \gamma T 3_{c}, \gamma T 4_{c}$ and $\gamma T 5_{c}$ are the distribution parameters corresponding to $E M L_{c}, E E U_{c}, E U S_{c}, E R O W_{c}$
and $X D D_{c}$, respectively, and the elasticity of transformation ( $\sigma T_{c}$ ) between domestically produced goods supplied on the domestic market and the exports by the domestic producers is given by $1 /\left(1+\rho T_{c}\right)$.

By maximizing the revenue:

```
Revenue \(_{c}\left(E M L_{c}, E E U_{c}, E U S_{c}, E R O W_{c}, X D D_{c}\right)=P E M L_{c} \cdot E M L_{c}+P E E U_{c} \cdot E E U_{c}+\)
PEUS \(_{c} \cdot E U S_{c}+\) PEROW \(_{c} \cdot E R O W_{c}+P D D_{c} \cdot X D D_{c}\)
```

subject to (42) we derive the supply of exports by the domestic producers to Mainland, to EU, to US and to ROW and the supply by the domestic producers to the domestic market:

$$
\begin{align*}
& E M L_{c}=X D D E_{c} \cdot\left(P D D E_{c} / P E M L_{c}\right)^{\sigma T_{c}} \cdot \gamma T 1_{c}^{\sigma T_{c}} \cdot a T_{c}^{\left(\sigma T_{c}-1\right)}  \tag{44}\\
& E E U_{c}=X D D E_{c} \cdot\left(P D D E_{c} / P E E U_{c}\right)^{\sigma T_{c}} \cdot \gamma T 2_{c}^{\sigma T_{c}} \cdot a T_{c}^{\left(\sigma T_{c}-1\right)}  \tag{45}\\
& E U S_{c}=X D D E_{c} \cdot\left(P D D E_{c} / P E U S_{c}\right)^{\sigma T_{c}} \cdot \gamma T 3_{c}^{\sigma T_{c}} \cdot a T_{c}^{\left(\sigma T_{c}-1\right)}  \tag{46}\\
& E R O W_{c}=X D D E_{c} \cdot\left(P D D E_{c} / P E R O W_{c}\right)^{\sigma T_{c}} \cdot \gamma T 4_{c}^{\sigma T_{c}} \cdot a T_{c}^{\left(\sigma T_{c}-1\right)}  \tag{47}\\
& X D D_{c}=X D D E_{c} \cdot\left(P D D E_{c} / P D D_{c}\right)^{\sigma T_{c}} \cdot \gamma T 5_{c}^{\sigma T_{c}} \cdot a T_{c}^{\left(\sigma T_{c}-1\right)} \tag{48}
\end{align*}
$$

and the corresponding zero profit condition:
$P D D E_{c} \cdot X D D E_{c}=P D D_{c} \cdot X D D_{c}+P E M L_{c} \cdot E M L_{c}+P E E U_{c} \cdot E E U_{c}+P E U S_{c} \cdot E U S_{c}+$ PEROW $_{c} \cdot$ EROW $_{c}$
where $P D D E_{c}$ is the price index corresponding to $X D D E_{c}, P E M L_{c}$ represents the domestic price of exports to Mainland received by the domestic producers, $P E E U_{c}$ gives the domestic price of exports to EU received by the domestic producers, $P E U S_{c}$ is the domestic price of exports to US and PEROW $_{c}$ represents the domestic price of exports to ROW.

In addition, export demand functions are introduced in the model (see Figure 4):
$E D M L_{c}=E D I M L_{c} \cdot\left(\text { PWEML }_{c} \cdot E R M L / P E M L_{c}\right)^{\text {elasE } E_{c}}$
$E D E U_{c}=E D I E U_{c} \cdot\left(\text { PWEEU }_{c} \cdot E R E U / P E E U_{c}\right)^{\text {elasE }}{ }_{c}$

EDUS $_{c}=$ EDIUS $_{c} \cdot\left(\text { PWEUS }_{c} \cdot E R U S / \text { PEUS }{ }_{c}\right)^{\text {elas } E_{c}}$

EDROW $_{c}=E D I R O W_{c} \cdot\left(\text { PWEROW }_{c} \cdot E R R O W / P E R O W_{c}\right)^{e l a s E_{c}}$
such that the export demand for domestically produced goods by the external sector, depends on the benchmark level of the export demand by the foreign sector, the relative price change and the price elasticity of export demand (elasE ${ }_{c}$ ).EDML $, E D E U_{c}, E D U S_{c}$ and $E D R O W_{c}$ represent the export demand for domestically produced goods by the Mainland, EU, US and ROW, respectively, while their benchmark levels are provided by EDIML $_{c}, E D I E U ~_{c}, E D I U S_{c}$ and $E D I R O W_{c}$, respectively. PWEML $_{c}$ represents the price of exports of commodity $c$ to Mainland, expressed in foreign currency, $P W E E U_{c}$ gives the price of exports to EU in foreign currency, PWEUS ${ }_{c}$ is the price of exports to US in foreign currency and $P W E R O W_{c}$ provides the price of exports to ROW in foreign currency.

The market clearing equations for exports:

$$
\begin{align*}
& E M L_{c}=E D M L_{c}  \tag{54}\\
& E E U_{c}=E D E U_{c}  \tag{55}\\
& E U S_{c}=E D U S_{c}  \tag{56}\\
& E R O W_{c}=E D R O W_{c} \tag{57}
\end{align*}
$$

determine the domestic price of exports received by the domestic producers.


Figure 4. Foreign trade specification

Balance of payments, expressed in foreign currency, takes into account all the trade and capital flows and is differentiated according to each trade partner:

$$
\begin{align*}
& S M L=\sum_{c}\left(M M L_{c} \cdot P W M M L_{c}-E M L_{c} \cdot P E M L_{c} / E R M L\right)+S G M L  \tag{58}\\
& S E U=\sum_{c}\left(M E U_{c} \cdot P W M E U_{c}-E E U_{c} \cdot P E E U_{c} / E R E U\right)+S G E C  \tag{59}\\
& S U S=\sum_{c}\left(M U S_{c} \cdot P W M U S_{c}-E U S_{c} \cdot P E U S_{c} / E R U S\right)-T R G U S
\end{align*}
$$

SROW $=\sum_{c}\left(\right.$ MROW $_{c} \cdot$ PWMROW $_{c}-E R O W_{c} \cdot P E R O W_{c} /$ ERROW $)-$ TRGW
where SML reflects the surplus/deficit of the current account with respect to Mainland, SEU is the surplus/deficit of the current account with respect to EU, SUS provides the balance of the current account with respect to US and SROW gives the balance of the current account with respect to ROW.

### 3.7. Investment demand

Total savings ( $S$ ) used to buy investment goods are given by:
$S=\sum_{q u} S H_{q u}+S F+S G \cdot G D P D E F+S M L \cdot E R M L+S E U \cdot E R E U+S U S \cdot E R U S+S R O W$. $E R R O W+\sum_{s} D E P_{s} \cdot P I$
where $S H_{q u}$ represents the households savings by income group, $S F$ stands for firms savings, $S G$ gives the regional government savings, expressed in nominal terms using the GDP deflator (GDPDEF), and $\sum_{s} D E P_{s} \cdot P I$ is the depreciation related to the private and public capital stock. The balance of the current accounts corresponding to Mainland, EU, US and ROW are expressed in domestic currency using the exchange rates with respect to Mainland (ERML), to EU (EREU ), to US (ERUS ) and to the rest of the world (ERROW).

The depreciation related to the private and public capital stock is valued at the price index of investments (PI) and is derived as:

$$
\begin{equation*}
D E P_{s}=d_{s} \cdot K S K_{s} \tag{63}
\end{equation*}
$$

where $d_{s}$ is the depreciation rate and $K S K_{s}$ gives the capital stock of industry $s$.

Total investments in real terms (ITT) are given by:
$P I \cdot I T T=S-\sum_{c} S V_{c} \cdot P_{c}$
where $S V_{c}$ stands for the inventories of commodity $c$.

The optimal allocation of total investments (ITT ) between different types of investment commodities $\left(I_{c}\right)$ is given by the Leontief function:
$I_{c}=i o I_{c} \cdot I T T$
where $i o I_{c}$ is a parameter that provides the composition of total investments in terms of investment goods.

The composite price (unit cost) of investments (PI) is defined as the weighted average of the price of investment goods:

$$
\begin{equation*}
P I=\sum_{c}\left\{\left(1+v a t i_{c}\right) \cdot\left[P_{c}+\sum_{c m} t_{c i t m_{c m, c}} \cdot P_{c t m}\right] \cdot i o I_{c}\right\} \tag{66}
\end{equation*}
$$

where $P_{c}$ stands for the price of (investment) commodity $c$, vatic is the value-added tax rate on investment goods $c$ and tcitm $_{\text {ctm,c }}$ is the trade and transport margin rate on investment good $c$.

### 3.8. Price equations

A common assumption for CGE models, which has also been adopted here, is that the economy is initially in equilibrium with the quantities normalized in such a way that prices of commodities equal unity. Due to the homogeneity of degree zero in prices, the model only determines the relative prices. Therefore, a particular price is selected to provide the numeraire against which all relative prices in the model will be measured. We choose the GDP deflator (GDPDEF) as the numeraire.

Different prices are defined for all the branches, exports and imports. As already explained, trade and transport margins are paid on all categories of demand in AzorMod except the government consumption (on intermediate consumption, on private consumption and on investment goods).

The domestic price of imports from Mainland ( $P M M L_{c}$ ) is determined by the price of imports from Mainland expressed in foreign currency $\left(P W M M L_{c}\right)$ and the exchange rate (ERML):
$P M M L_{c}=P W M M L_{c} \cdot E R M L$

Similarly, the domestic price of imports from EU $\left(\mathrm{PMEU}_{c}\right)$ is given by the price of imports from EU expressed in foreign currency $\left(P W M E U_{c}\right)$ and the corresponding exchange rate (EREU):

$$
\begin{equation*}
P M E U_{c}=P W M E U_{c} \cdot E R E U \tag{68}
\end{equation*}
$$

The domestic price of imports from US $\left(\mathrm{PMUS}_{c}\right)$ and from ROW $\left(\mathrm{PMROW}_{c}\right)$, further include the tariff rate on commodity $c$ for imports from US (tmus ${ }_{c}$ ) and the tariff rate on imports from ROW $\left(t m r w_{c}\right)$ :

PMUS $_{c}=P W M U S_{c} \cdot E R U S \cdot\left(1+\right.$ tmus $\left._{c}\right)$

PMROW $_{c}=$ PWMROW $_{c} \cdot E R R O W \cdot\left(1+t m r w_{c}\right)$
where $P^{2} M M S_{c}$ and $P W M R O W_{c}$ stand for the world price of imports from US and from ROW, respectively, and ERUS and ERROW provide the exchange rates with respect to US and ROW, respectively.

The consumer price index (PCINDEX ) used in the model is defined as:

$$
\begin{align*}
& \text { PCINDEX }=\sum_{c, q u}\left\{\left[P_{c}+\sum_{c t m} \operatorname{tchtm}_{c m m, q u} \cdot P_{c t m}\right] \cdot\left(1+t e x c_{c, q u}\right) \cdot\left(1+t c_{c, q u}+v a t c_{c, q u}\right) \cdot C Z_{c, q u}\right\} / \\
& \sum_{c, q u}\left\{\left[P Z_{c}+\sum_{c t m} t_{c h t m z_{c m, q u}} \cdot P Z_{c t m}\right] \cdot\left(1+\text { texcz }_{c, q u}\right) \cdot\left(1+t c z_{c, q u}+\text { vatcz }_{c, q u}\right) \cdot C Z_{c, q u}\right\} \tag{71}
\end{align*}
$$

where $P_{c}$ is the price index of commodity $c$ net of taxes and $P Z_{c}$ gives its benchmark level, tchtm $_{c m m, q \text { qu }}$ represents the trade and transport margin rate on private consumption and
tchtmz $_{c \text { cm, }, q u}$ is its benchmark level, texc $_{c, q u}$ gives the excise duties rate and texcz $_{c, q u}$ its benchmark level, vatc $c_{c, q u}$ provides the value-added tax rate and vatcz $_{c, \text {,qu }}$ its benchmark level and $t c_{c, q u}$ gives the tax rate corresponding to other taxes on private consumption, while $t C z_{c, q u}$ is its benchmark level. Finally, $C Z_{c, q u}$ accounts for the benchmark level of private consumption of commodity $c$ by income group $q u$.

Consumer prices ( $P C T_{c, q u}$ ) are further defined as:

$$
\begin{equation*}
P C T_{c, q u}=\left[P_{c}+\sum_{c t m} t^{2 h t m_{c t m, c, u}} \cdot P_{c t m}\right] \cdot\left(1+\text { texc }_{c, q u}\right) \cdot\left(1+t c_{c, q u}+\text { vatc }_{c, q u}\right) \tag{72}
\end{equation*}
$$

### 3.9. Labour market

The following identity defines the relation between the labour supply, the labour demand, and unemployment:

$$
\begin{equation*}
\sum_{s} L S K_{s}=L S R-U N E M P \tag{73}
\end{equation*}
$$

where $L S K_{s}$ stands for the number of employees in industry $s$, UNEMP represents the number of unemployed and $L S R$ reflects the active population.

The responsiveness of real wage to the labour market conditions is surprised by a wage curve (Sanz-de-Galdeano \& Turunen, 2006):
$\log (P L / P C I N D E X)=e l a s U \cdot \log (U N R A T E)+e r r$
where $P L$ is the nominal average wage corresponding to national employment (net of social security contributions), PCINDEX is the consumer price index, UNRATE provides the unemployment rate, err is the error term and elasU is the unemployment elasticity.

The labour supply is provided by the following equation:
$L S R=L S R I \cdot\{[P L \cdot(1-\text { tyavr }) \cdot P C I N D E X Z] /[P L Z \cdot(1-\text { tyavrz }) \cdot P C I N D E X]\}^{\text {lassLS }}$
where LSRI is the benchmark level corresponding to the active population, tyavr is the average personal income tax rate and tyavrz its benchmark level, and PLZ and PCINDEXZ are the benchmark levels corresponding to the nominal national wage and CPI, respectively. elasLS further provides the elasticity of labour supply.

The average personal income tax rate is determined as:
tyavr $=\sum_{q u}\left(t y_{q u} \cdot Y H_{q u}\right) / \sum_{q u} Y H_{q u}$
where $t y_{q u}$ stands for the personal income tax rate levied on the household income group $q u$ and $\mathrm{YH}_{q u}$ gives the total income of the household income group $q u$.

The national employment (EMPN) is defined as:
$E M P N=L S R-U N E M P$
The national average wage including social security contributions (PLAVRT) is determined as:
PLAVRT $\cdot(L S R-U N E M P)=\sum_{s}\left[P L \cdot\left(1+t l_{s} /\left(1-t l_{s}\right)\right) \cdot\left(1+\right.\right.$ premLSK $\left.\left._{s}\right) \cdot L S K_{s}\right]$
where $P L$ is the national average wage, $\operatorname{prem} L S K_{s}$ gives the wage premium is sector $s$ and $t l_{s}$ provides the social contributions rate in sector $s$.

### 3.10. Market clearing equations

The equilibrium in the product, capital and labour markets requires that demand equals supply at prevailing prices (taking into account unemployment for the labour market). Labour market clearing equation has already been presented above. Capital stock is sector specific, such that the equality between capital demand and supply determines the return to capital by branch of activity.

Separate market clearing equations are distinguished in the model for each commodity $c$. For the trade and transport services ctm , the sum of demand for intermediate consumption
of commodity $\mathrm{ctm}\left(\sum_{s} i o_{c t m, s} \cdot X D_{s}\right)$, the private demand for commodity $\operatorname{ctm}\left(C_{c m m, q u}\right)$, the public demand for commodity $\mathrm{ctm}\left(C G_{c t m}\right)$, the demand for investment goods $\left(I_{c t m}\right)$, the demand for inventories ( $S V_{c t m}$ ) and the demand for trade and transport services (MARGTM ${ }_{c t m}$ ) which are invoiced separately (trade and transport margins) should be equal with the total supply of commodity $\mathrm{ctm}\left(X_{c t m}\right)$ from imports and domestic production:

$$
\begin{equation*}
\sum_{s} i i_{c t m, s} \cdot X D_{s}+\sum_{q u} C_{c m m, q u}+C G_{c t m}+I_{c t m}+S V_{c t m}+M A R G T M_{c t m}=X_{c t m} \tag{78}
\end{equation*}
$$

The demand for trade and transport services ctm ( $\mathrm{MARGTM}_{c t m}$ ) invoiced separately (Löfgren, Harris and Robinson, 2002), is further derived as the sum of demand for trade and transport services on private consumption $\left(\sum_{c, q u} \operatorname{tchtm}_{c t m, q u} \cdot C_{c, q u}\right)$, of demand for trade and transport services on investment goods $\left(\sum_{c} \operatorname{tcitm}_{c t m, c} \cdot I_{c}\right)$ and of demand for trade and transport services on intermediate consumption $\left(\sum_{s, c}\right.$ tcictm $\left._{c t m, c, s} \cdot i i_{c, s} \cdot X D_{s}\right)$ :


The market clearing equations corresponding to all commodities nctm, except the trade and transport services are given by:
$\sum_{s} i o_{n c t m, s} \cdot X D_{s}+\sum_{q u} C_{n c t m, q u}+C G_{n c m}+I_{n c t m}+S V_{n c t m}=X_{n c t m}$

The demand for inventories for each commodity $c$ is defined as a fixed share of domestic sales:
$S V_{c}=s v r_{c} \cdot X_{c}$

### 3.11. Other macroeconomic indicators

Gross domestic product is provided at both constant prices (GDP) and at current market prices (GDPC):

$$
\begin{align*}
& G D P=\sum_{c, q u}\left\{C_{c, q u} \cdot\left\{P Z_{c}+\sum_{c t m} \operatorname{tchtmz}_{c t m, c, q u} \cdot P Z_{c t m}\right] \cdot\left(1+\text { texcz }_{c, q u}\right) \cdot\left(1+t c c_{c, q u}+v a t c z_{c, q u}\right)\right\}+ \\
& \sum_{c} C G_{c} \cdot P Z_{c}+\sum_{c}\left\{I_{c} \cdot\left(1+v a t i z_{c}\right) \cdot\left[P Z_{c}+\sum_{c t m} t^{2 i t m z_{c m, ~}} \cdot P Z_{c m m}\right]\right\}+\sum_{c} S V_{c} \cdot P Z_{c}+ \\
& \sum_{c} E M L_{c} \cdot P E M L Z_{c}+\sum_{c} E E U_{c} \cdot P E E U Z_{c}+\sum_{c} E U S_{c} \cdot P E U S Z_{c}+\sum_{c} E R O W_{c} \cdot P E R O W Z_{c}- \\
& \sum_{c} M M L_{c} \cdot P W M M L Z_{c} \cdot E R M L Z-\sum_{c} M E U_{c} \cdot \text { PWMEUZ }_{c} \cdot E R E U Z- \\
& \sum_{c} M U S_{c} \cdot P W M U S Z_{c} \cdot E R U S Z-\sum_{c} M R O W_{c} \cdot P W M R O W Z_{c} \cdot E R R O W Z  \tag{82}\\
& G D P C=\sum_{c, q u}\left\{C_{c, q u} \cdot\left[P_{c}+\sum_{c t m} \text { tchtm }_{c t m, c, q u} \cdot P_{c t m}\right] \cdot\left(1+\text { tex }_{c, q u}\right) \cdot\left(1+t c_{c, q u}+\text { vatc }_{c, q u}\right)\right\}+ \\
& \sum_{c} C G_{c} \cdot P_{c}+\sum_{c}\left\{I_{c} \cdot\left(1+v a t i_{c}\right) \cdot\left[P_{c}+\sum_{c m} t c i t m_{c m, c} \cdot P_{c t m}\right]\right\}+\sum_{c} S V_{c} \cdot P_{c}+\sum_{c} E M L_{c} \cdot P E M L_{c} \\
& +\sum_{c} E E U_{c} \cdot P E E U_{c}+\sum_{c} E U S_{c} \cdot \text { PEUS }_{c}+\sum_{c} E R O W_{c} \cdot \text { PEROW }_{c}- \\
& \sum_{c} M M L_{c} \cdot P W M M L_{c} \cdot E R M L-\sum_{c} M E U ~_{c} \cdot P W M E U_{c} \cdot E R E U- \\
& \sum_{c} \text { MUS }_{c} \cdot \text { PWMUS }_{c} \cdot E R U S-\sum_{c} \text { MROW }_{c} \cdot \text { PWMROW }_{c} \cdot \text { ERROW } \tag{83}
\end{align*}
$$

where vatiz ${ }_{c}$ stands for the benchmark level of the value-added tax rate on investment goods, $\mathrm{PEMLZ}_{c}, P E E U Z_{c}, P E U S Z_{c}$ and $P E R O W Z_{c}$ provide the benchmark levels of domestic price of exports to Mainland, EU, US and ROW, respectively, $P W M M L Z_{c}$,
 imports from Mainland, EU, US and ROW, respectively, and ERMLZ, EREUZ, ERUSZ and ERROWZ provide the benchmark levels of the exchange rates with respect to Mainland, EU, US and ROW, respectively.

Derivation of some other macroeconomic indicators like the components of GDP at constant prices and the private GDP at constant prices is provided in section 2.14.

### 3.12. Incorporation of dynamics

AzorMod has a recursive dynamic structure composed of a sequence of several temporary equilibria. The first equilibrium in the sequence is given by the benchmark year. In each time period, the model is solved for an equilibrium given the exogenous conditions assumed for that particular period. The equilibria are connected to each other through capital accumulation. Thus, the endogenous determination of investment behaviour is essential for the dynamic part of the model. Investment and capital accumulation in year $t$ depend on expected rates of return for year $t+1$, which are determined by actual returns on capital in year $t$.

The normal rate of return to capital in branch $s\left(R O R_{s}\right)$ is specified as an inverse logistic function (see Figure 5) of the proportionate growth in sector's $s$ capital stock (Dixon and Rimmer, 2002):

$$
\left.\begin{array}{l}
R O R_{s, t}=R O R H_{s}+\left(1 / B_{s}\right) \cdot\left[\ln \left(K S K g_{s, t}-K_{S K g} \min _{s}\right)-\ln \left(K_{S K g ~ m a x}^{s}\right.\right. \tag{84}
\end{array}-K S K g_{s, t}\right)-1
$$

where $\mathrm{RORH}_{s}$ is the historically normal rate of return in branch $s, K S K g_{s, t}$ is the capital growth rate in industry $s$ in year $t, K S K g \min _{s}$ and $\operatorname{KSKg}^{\max }{ }_{s}$ are the minimum and the maximum possible growth rates of capital stock in branch $s$, KSKtrend $_{s}$ is the industry's historically normal growth rate and $B_{s}$ is a positive parameter. The minimum possible growth rate is set at the negative of the rate of depreciation in branch $s$. This condition implies that investments in each branch of activity have positive values, such that once installed, capital cannot be shifted from one sector to another except for the gradual process of depreciation. The maximum possible growth rate of capital stock in industry $s$ is set at $K_{S K \text { trend }}^{s}$ plus $\lim I N V_{s}$ in order to avoid unrealistically large simulated growth rates (Dixon and Rimmer, 2002). In the current version $\lim _{\text {I }} I N V_{s}$ is taken equal to 6 per cent for
all the branches. For example, if the historically normal growth rate in an industry is 4 per cent, the upper limit in any year $t$ would not exceed 10 per cent.

Parameter $\left(B_{s}\right)$ reflects the sensitivity of capital growth in branch $s$ to variations in its expected rate of return. It is derived by differentiating equation (84) with respect to $\mathrm{KSKg}_{s, t}$ :
$B_{s}=$ SEA $^{\prime} \cdot\left[\frac{\text { KSKg max }_{s}-\text { KSKg min }_{s}}{\left(\text { KSKg max }_{s}-\text { KSKtrend }_{s}\right) \cdot\left(\text { KSKtrend }_{s}-\text { KSKg min }_{s}\right)}\right]$
where:
$S E A=\left(\frac{\partial R O R_{s, t}}{\partial K S K g_{s, t}}\right)^{-1}$

Evaluating (86) in the neighbourhood of $K S K g_{s, t}=K S K t r e n d_{s}$ provides:
$S E A=\left(\left.\frac{\partial R O R_{s, t}}{\partial K S K g_{s, t}} \right\rvert\, K S K g_{s, t}=K S K \text { trend }_{s}\right)^{-1}$
where SEA is the reciprocal of the slope of the RR' in Figure 5, which is considered to be the same for all industries due to the lack of detailed estimates by branch.

The present value $\left(P V K_{s, t}\right)$ of investing a unit of capital in industry $s$ in year $t$ is defined as:

$$
\begin{equation*}
P V K_{s, t}=-P I_{t}+\left[P K_{s, t+1}+P I_{t+1} \cdot d_{s}+P I_{t+1} \cdot\left(1-d_{s}\right)\right] /\left[1+N I N T_{t}\right] \tag{88}
\end{equation*}
$$

where $P I_{t}$ is the cost of buying a unit of capital (the price of composite investment good) in year $t, P K_{s, t}+P I_{t+1} \cdot d_{s}$ is the rental rate on industry's $s$ capital stock, $d_{s}$ is the depreciation rate in branch $s$ and $\operatorname{NINT}_{t}$ is the nominal interest rate in year $t$ (Dixon and Rimmer, 2002). The purchase of one unit of capital in year $t$ by industry $s$ involves an immediate expenditure $\left(P I_{t}\right)$, followed by two benefits in year $t+1$ which are discounted by $\left(1+N I N T_{t}\right)$ : the rental value of an extra unit of capital in year $t+1\left(P K_{s, t+1}+P I_{t+1} \cdot d_{s}\right)$,
including the depreciation, and the value at which the depreciated unit of capital can be sold in year $t+1\left[P I_{t+1} \cdot\left(1-d_{s}\right)\right]$.

The expected rate of return on investment in industry $s$ in year $t$ is given by dividing both sides of (88) by $P I_{t}$ :
$R O R_{s, t}=-1+\left[P K_{s, t+1} / P I_{t}+P I_{t+1} / P I_{t}\right] /\left[1+N I N T_{t}\right]$

Under static expectations, investors are assumed to anticipate that the asset prices (the cost of buying a unit of capital) and the net rental rates will increase by the current rate of inflation $\left(R I N F_{t}\right)$. Thus, the expected rate of return $\left(R O R_{s, t}\right)$ under static expectations is given by:
$R O R_{s, t}=-1+\left[P K_{s, t} \cdot\left(1+\right.\right.$ RINF $\left.\left._{t}\right) / P I_{t}+P I_{t} \cdot\left(1+R I N F_{t}\right) / P I_{t}\right] /\left[1+N I N T_{t}\right]$

Simplifying further, we get:
$R O R_{s, t}=-1+\left[P K_{\mathrm{s}, \mathrm{t}} / P I_{t}+1\right] /\left(1+\operatorname{RINT}_{t}\right)$
where the real interest rate $\left(\operatorname{RINT}_{t}\right)$ is defined as:
$1+$ RINT $_{t}=\left(1+\operatorname{NINT}_{t}\right) /\left(1+\right.$ RINF $\left._{t}\right)$


Figure 5. The expected rate of return for industry s

The weighted average real return to capital has been taken as a proxy for the real interest rate in AzorMod. The return to capital is expressed in real terms using the production price index:
$R I N T_{t}=\sum_{s}\left[\left(P K_{s, t} / P D_{s, t}\right) \cdot K S K_{s, t}\right] / \sum_{s} K S K_{s, t}$

The capital stock in industry $s$ in the next period (year $t+1$ ) is given by:
$K S K_{\mathrm{s}, t+1}=\left(1-d_{\mathrm{s}}\right) \cdot K S K_{\mathrm{s}, t}+I N V_{\mathrm{s}, t}$
where $K S K_{s, t}$ is the current capital stock (in year $t$ ) and $I N V_{s, t}$ stand for the investments by the branch $s$ in year $t$.

The capital growth rate in terms of capital stock in year $t+1$ and the capital stock in year $t$ is given by:

$$
\begin{equation*}
K S K g_{s, t}=K S K_{s, t+1} / K S K_{s, t}-1 \tag{95}
\end{equation*}
$$

whereas the actual growth rate of capital in industry $s$ can be derived from equation. (84) as:

$$
\begin{align*}
& \text { KSKg }_{s, t}=\left[\alpha R O R_{s, t} \cdot \text { KSKg max }_{s} \cdot\left(\text { KSKtrend }_{s}-\text { KSKg min }_{s}\right)+\right. \\
& \text { KSKg min } \left._{s} \cdot\left(\text { KSKg max }_{s}-\text { KSKtrend }_{s}\right)\right] /\left[\alpha R O R _ { s , t } \cdot \left(\text { KSKtrend }_{s}-\right.\right.  \tag{96}\\
& \text { KSKg min } \left.\left._{s}\right)+\left(\text { KSKg max }_{s}-\text { KSKtrend }_{s}\right)\right]
\end{align*}
$$

The parameter $\alpha R O R_{s, t}$ is given by:


A first estimate of investments in the branch $s$ in year $t\left(I N V S_{s, t}\right)$ is derived from equations (94)-(96) as:

```
INVS s,t,t KSK
(KSKgmax s}-\mp@subsup{\mathrm{ KSKtrend }}{s}{})]/[\alpha\mp@code{ROR s,t
(KSKgmax s}-\mp@subsup{\mathrm{ KSKtrend s}}{s}{})]+\mp@subsup{d}{s}{}\cdot\mp@subsup{KSK}{s,t}{
\(\left(\right.\) KSKgmax \(_{s}-\) KSKtrend \(\left.\left._{s}\right)\right]+d_{s} \cdot\) KSK \(_{s . t}\)
```

while the actual level of investments in branch $s$ in year $t$ is provided by:

$$
\begin{equation*}
I N V_{\mathrm{s}, t}=I N V S_{\mathrm{s}, t} / \sum_{\mathrm{ss}} I N V S_{\mathrm{s}, t} \cdot\left(S_{t}-\sum_{c} S V_{c, t} \cdot P_{\mathrm{ct}}\right) / P I_{t} \tag{99}
\end{equation*}
$$

which also insures the consistency between total investments and savings.

The model is solved dynamically with annual steps. The simulation horizon of the model has been set at 13 years but it can easily be extended.

### 3.13. Closure rules

The closure rules refer to the manner in which demand and supply of commodities, the macroeconomic identities and the factor markets are equilibrated ex-post. Due to the complexity of the model, a combination of closure rules is needed. The particular set of
closure rules should also be consistent, to the largest extent possible, with the institutional structure of the economy and with the purpose of the model.

In mathematical terms, the model should consist of an equal number of independent equations and endogenous variables. The closure rules reflect the choice of the model builder of which variables are exogenous and which variables are endogenous, so as to achieve ex-post equality.

Three macro balances are usually identified in CGE models that can be a potential source of ex-ante disequilibria and must be reconciled ex-post (Adelman and Robinson, 1989):

- The savings-investment balance;
- The government balance;
- The external balance.

The most widely used macro closure rule for CGE models is based on the investment and savings balance. In the model, the investment is assumed to adjust to the available domestic and foreign savings. This reflects an economy in which savings form a binding constraint.

Additional assumptions are needed with regard to regional government behaviour in AzorMod. First, regional government savings are fixed in real terms while regional government total current consumption adjusts to achieve the target set with respect to the government savings. The allocation between the consumption of different goods and services is provided by a Cobb-Douglas function. Secondly, the transfers received by the regional government from the Mainland government, from the EU, from the US and from the ROW are fixed in real terms. On the expenditure side, the regional government transfers to the households are also fixed in real terms.

For the external balance, the exchange rates are kept unchanged in the simulations, while the balances of the current accounts adjust. An alternative closure is also possible where the balances of the current accounts corresponding to US and ROW are set while the real exchange rates adjust.

The setup of the closure rules is important in determining the mechanisms governing the model. Therefore, the closure rules should be established also taking into account the policy scenario in question.

According to Walras' law if (n-1) markets are cleared the $n$th one is cleared as well. Therefore, in order to avoid over-determination of the model, the current account balance with respect to ROW has been dropped (see equation (61), section 2.6). However, the system of equations guarantees, through Walras' law, that the total imports from ROW less the total exports to ROW and the transfers from ROW equals the current account balance.

## 4. Calibration of the Model and Simulation of Tax Changes

The model was calibrated using a SAM matrix constructed for the year 2002 for the Azorean economy.

The scenario created, based on the policies effectively implemented, presumed a corporate income tax cut of $30 \%$ and a personal income tax cut of $20 \%$. The simulation was initiated in 2002 and impacts traced up to 2013. The main results, representing percentage changes relative to the base results, are presented in the following table.

As expected, in the short run, there is a negative impact on GDP. Because the marginal propensity to save is positive, not all the extra money left in private hands is channelled to expenditures. The negative impact, however, tapers off and by the year 2012 becomes
positive. Private consumption increases steadily while public consumption decreases.
Gross fixed investment increases as does private GDP. In the end, the economic outcome tends to recover the short term losses in GDP with gains in the private component of the economy and when compared to the public component. Table 1 presents the aggregate results of the exercise.

Table 1: Impacts of a $30 \%$ drop in CIT and a $20 \%$ drop in PIT

| Macroeconomic effects in <br> real terms (\% change <br> to the BAU) | 2002 | 2003 | 2004 | 2005 | 2006 | 2007 | 2008 | 2009 | 2010 | 2011 | 2012 | 2013 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| GDP | $-0,23$ | $-0,21$ | $-0,18$ | $-0,16$ | $-0,14$ | $-0,12$ | $-0,09$ | $-0,07$ | $-0,04$ | $-0,02$ | 0,01 | 0,03 |
| Private consumption | 0,37 | 0,39 | 0,42 | 0,45 | 0,47 | 0,50 | 0,52 | 0,55 | 0,57 | 0,60 | 0,63 | 0,65 |
| Government consumption | $-1,65$ | $-1,67$ | $-1,69$ | $-1,71$ | $-1,73$ | $-1,75$ | $-1,77$ | $-1,78$ | $-1,80$ | $-1,82$ | $-1,83$ | $-1,85$ |
| Gross fixed investment | 1,10 | 1,19 | 1,27 | 1,36 | 1,44 | 1,53 | 1,61 | 1,69 | 1,78 | 1,86 | 1,94 | 2,03 |
| Foreign balance | 0,76 | 0,81 | 0,85 | 0,90 | 0,95 | 0,99 | 1,04 | 1,09 | 1,13 | 1,18 | 1,22 | 1,27 |
| Exports | $-0,01$ | 0,02 | 0,04 | 0,07 | 0,10 | 0,12 | 0,15 | 0,18 | 0,21 | 0,24 | 0,27 | 0,31 |
| Imports | 0,47 | 0,51 | 0,55 | 0,59 | 0,63 | 0,67 | 0,71 | 0,74 | 0,78 | 0,82 | 0,86 | 0,90 |
| Private GDP | 0,54 | 0,58 | 0,63 | 0,67 | 0,72 | 0,76 | 0,81 | 0,85 | 0,90 | 0,95 | 1,00 | 1,04 |

A scenario was created to isolate each of the two taxes. Table 2 below reports the results of the $20 \%$ personal income tax reduction. As it turns out, the reduction of this tax has the bigger effect in GDP. In fact, more than $70 \%$ of the impact on GDP comes from this component and it is the driving effect on the turn of the variation on GDP. While the negative impact of the corporate income tax reductions lingers for the full period, the impact of the personal income tax becomes positive as of 2011.

Table 2: Impacts of a $20 \%$ drop in PIT

| Macroeconomic effects <br> in real terms (\% change <br> to the BAU) | $\mathbf{2 0 0 2}$ | $\mathbf{2 0 0 3}$ | $\mathbf{2 0 0 4}$ | $\mathbf{2 0 0 5}$ | $\mathbf{2 0 0 6}$ | $\mathbf{2 0 0 7}$ | $\mathbf{2 0 0 8}$ | $\mathbf{2 0 0 9}$ | $\mathbf{2 0 1 0}$ | $\mathbf{2 0 1 1}$ | $\mathbf{2 0 1 2}$ | $\mathbf{2 0 1 3}$ |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| GDP | $-0,17$ | $-0,15$ | $-0,13$ | $-0,11$ | $-0,10$ | $-0,08$ | $-0,06$ | $-0,04$ | $-0,02$ | 0,00 | 0,02 | 0,04 |
| Private consumption | 0,33 | 0,35 | 0,37 | 0,39 | 0,41 | 0,43 | 0,46 | 0,48 | 0,50 | 0,52 | 0,54 | 0,57 |
| Government consumption | $-1,30$ | $-1,31$ | $-1,33$ | $-1,34$ | $-1,36$ | $-1,37$ | $-1,38$ | $-1,40$ | $-1,41$ | $-1,42$ | $-1,43$ | $-1,44$ |
| Gross fixed investment | 0,85 | 0,93 | 1,00 | 1,07 | 1,14 | 1,21 | 1,28 | 1,35 | 1,42 | 1,50 | 1,57 | 1,64 |
| Foreign balance | 0,62 | 0,67 | 0,71 | 0,75 | 0,79 | 0,84 | 0,88 | 0,92 | 0,96 | 1,00 | 1,04 | 1,08 |
| Exports | $-0,01$ | 0,01 | 0,02 | 0,03 | 0,05 | 0,06 | 0,08 | 0,10 | 0,12 | 0,14 | 0,16 | 0,18 |
| Imports | 0,38 | 0,42 | 0,45 | 0,48 | 0,51 | 0,54 | 0,58 | 0,61 | 0,64 | 0,68 | 0,71 | 0,74 |
| Private GDP | 0,44 | 0,48 | 0,51 | 0,55 | 0,58 | 0,62 | 0,66 | 0,69 | 0,73 | 0,77 | 0,81 | 0,84 |

These results are in line with what would be expected since corporate income taxes represent a small percentage of personal income taxes.

The tax reduction policy implemented in the Azores in the early years of the XXI century led, according to the model specified, and assuming nothing else changed, to a short term reduction in GDP. In the long run, however, the tendency is for a recovery in the growth of this variable. The private sector grew relative to the public sector.

To assess the redistributive impact of the policy we can look at what it implied for the different household categories considered. Overall, real wages before tax decreased due to a decrease in employment. Real average wages net of taxes, however, increased as did the real average return to capital. Table 3 shows the results.

Table 3: Impacts of a Cut in PIT ( $20 \%$ ) and CIT ( $30 \%$ ) on Wages and Returns to Capital

| Effects on Real Wage and RTC | $\mathbf{2 0 0 2}$ | $\mathbf{2 0 0 3}$ | $\mathbf{2 0 0 4}$ | $\mathbf{2 0 0 5}$ | $\mathbf{2 0 0 6}$ | $\mathbf{2 0 0 7}$ | $\mathbf{2 0 0 8}$ | $\mathbf{2 0 0 9}$ | $\mathbf{2 0 1 0}$ | $\mathbf{2 0 1 1}$ | $\mathbf{2 0 1 2}$ | $\mathbf{2 0 1 3}$ |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Real average wage (Before tax) | $-0,33$ | $-0,30$ | $-0,26$ | $-0,23$ | $-0,20$ | $-0,16$ | $-0,13$ | $-0,09$ | $-0,06$ | $-0,03$ | 0,01 | 0,04 |
| Real average wage net of PIT | 0,38 | 0,41 | 0,45 | 0,48 | 0,51 | 0,55 | 0,58 | 0,62 | 0,65 | 0,69 | 0,72 | 0,76 |
| Real average return to capital | 0,91 | 0,86 | 0,81 | 0,76 | 0,71 | 0,66 | 0,61 | 0,56 | 0,50 | 0,44 | 0,38 | 0,32 |

At a more disaggregated level, we find that, for all household groups, there is a negative impact on gross income due to the fact that unemployment increased (Table 4). The measure of final welfare, the equivalent variation, comes out positive for all income groups with higher relative gains registered for the lower income groups, a result that is desired but was uncertain given that the tax reduction did not change the progressivety of the tax system (Table5).

Table 4: Tax Cut Impact on Total Household Income before Taxes

| Effects on household Real Income <br> (before tax) | HHgrp | $\mathbf{2 0 0 2}$ | $\mathbf{2 0 0 3}$ | $\mathbf{2 0 0 4}$ | $\mathbf{2 0 0 5}$ | $\mathbf{2 0 0 6}$ | $\mathbf{2 0 0 7}$ | $\mathbf{2 0 0 8}$ | $\mathbf{2 0 0 9}$ | $\mathbf{2 0 1 0}$ | $\mathbf{2 0 1 1}$ | $\mathbf{2 0 1 2}$ | $\mathbf{2 0 1 3}$ |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| HH1 | q 1 | $-0,12$ | $-0,10$ | $-0,09$ | $-0,07$ | $-0,05$ | $-0,03$ | $-0,02$ | 0,00 | 0,02 | 0,04 | 0,06 | 0,07 |
| HH2 | q 2 | $-0,24$ | $-0,21$ | $-0,19$ | $-0,17$ | $-0,15$ | $-0,12$ | $-0,10$ | $-0,08$ | $-0,06$ | $-0,03$ | $-0,01$ | 0,01 |
| HH3 | q 3 | $-0,21$ | $-0,19$ | $-0,17$ | $-0,15$ | $-0,13$ | $-0,10$ | $-0,08$ | $-0,06$ | $-0,04$ | $-0,02$ | 0,01 | 0,03 |
| HH4 | q 4 | $-0,28$ | $-0,25$ | $-0,23$ | $-0,20$ | $-0,18$ | $-0,16$ | $-0,13$ | $-0,11$ | $-0,09$ | $-0,06$ | $-0,04$ | $-0,01$ |
| HH5 | q | $-0,22$ | $-0,20$ | $-0,18$ | $-0,15$ | $-0,13$ | $-0,11$ | $-0,09$ | $-0,07$ | $-0,04$ | $-0,02$ | 0,00 | 0,02 |
| HH6 | q 6 | $-0,14$ | $-0,12$ | $-0,10$ | $-0,08$ | $-0,06$ | $-0,04$ | $-0,02$ | 0,00 | 0,02 | 0,04 | 0,06 | 0,08 |

Table 5: Tax Cut Impact on Total Equivalent Variation in Income

| Equivalent variation in income <br> (in \% of hh income) | HHgrp | $\mathbf{2 0 0 2}$ | $\mathbf{2 0 0 3}$ | $\mathbf{2 0 0 4}$ | $\mathbf{2 0 0 5}$ | $\mathbf{2 0 0 6}$ | $\mathbf{2 0 0 7}$ | $\mathbf{2 0 0 8}$ | $\mathbf{2 0 0 9}$ | $\mathbf{2 0 1 0}$ | $\mathbf{2 0 1 1}$ | $\mathbf{2 0 1 2}$ | $\mathbf{2 0 1 3}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| HH1 | q 1 | 0,61 | 0,63 | 0,64 | 0,65 | 0,67 | 0,68 | 0,70 | 0,71 | 0,73 | 0,74 | 0,76 | 0,77 |
| HH | q 2 | 0,42 | 0,44 | 0,46 | 0,48 | 0,50 | 0,52 | 0,54 | 0,56 | 0,58 | 0,60 | 0,62 | 0,64 |
| HH | q | 0,43 | 0,45 | 0,47 | 0,49 | 0,51 | 0,53 | 0,55 | 0,57 | 0,59 | 0,61 | 0,64 | 0,66 |
| HH 4 | q 4 | 0,25 | 0,28 | 0,30 | 0,32 | 0,34 | 0,37 | 0,39 | 0,41 | 0,44 | 0,46 | 0,48 | 0,51 |
| HH | q | 0,31 | 0,33 | 0,35 | 0,38 | 0,40 | 0,42 | 0,44 | 0,46 | 0,48 | 0,50 | 0,53 | 0,55 |
| HH | q | 0,23 | 0,25 | 0,27 | 0,29 | 0,31 | 0,33 | 0,35 | 0,37 | 0,39 | 0,41 | 0,43 | 0,45 |

The results for equivalent variation are consistent with the registered increases in real consumption (Table 6). In fact, the greater increases were found in the lower income groups. Only the fourth group presents a diversion from an otherwise clear pattern.

Table 6: Tax Cut Impact on Household Real Consumption

| Effects on household Real Consumption | HHgrp | 2002 | 2003 | 2004 | 2005 | 2006 | 2007 | 2008 | 2009 | 2010 | 2011 | 2012 | 2013 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| HH1 | q1 | 0,59 | 0,61 | 0,63 | 0,65 | 0,66 | 0,68 | 0,70 | 0,72 | 0,74 | 0,76 | 0,77 | 0,79 |
| HH2 | q2 | 0,41 | 0,43 | 0,45 | 0,48 | 0,50 | 0,52 | 0,55 | 0,57 | 0,59 | 0,62 | 0,64 | 0,66 |
| HH3 | q3 | 0,44 | 0,47 | 0,49 | 0,51 | 0,54 | 0,56 | 0,58 | 0,60 | 0,63 | 0,65 | 0,67 | 0,70 |
| HH4 | q4 | 0,28 | 0,30 | 0,33 | 0,35 | 0,38 | 0,41 | 0,43 | 0,46 | 0,48 | 0,51 | 0,54 | 0,56 |
| HH5 | q5 | 0,37 | 0,39 | 0,42 | 0,44 | 0,47 | 0,49 | 0,52 | 0,54 | 0,57 | 0,60 | 0,62 | 0,65 |
| HH6 | q6 | 0,35 | 0,38 | 0,41 | 0,44 | 0,46 | 0,49 | 0,52 | 0,55 | 0,58 | 0,61 | 0,64 | 0,67 |

The propensity to save of each household group is also affected in an expected manner. The impact of the tax cut should be greater for higher income groups. That is, in fact, what happens. The lower income group, with a low savings propensity, does not register any significant change in its savings behaviour. The highest income group registers the highest increase.

| Propensity to Save | HHgrp | 2002 | 2003 | 2004 | 2005 | 2006 | 2007 | 2008 | 2009 | 2010 | 2011 | 2012 | 2013 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Propensity to save (\%) | q1 | 0,71 | 0,71 | 0,71 | 0,71 | 0,71 | 0,71 | 0,71 | 0,71 | 0,71 | 0,71 | 0,71 | 0,71 |
| Propensity to save (\% points difference with BAU) | q1 | 0,00 | 0,00 | 0,00 | 0,00 | 0,00 | 0,00 | 0,00 | 0,00 | 0,00 | 0,00 | 0,00 | 0,00 |
| Propensity to save (\%) | q2 | 1,85 | 1,85 | 1,85 | 1,85 | 1,85 | 1,85 | 1,85 | 1,85 | 1,85 | 1,85 | 1,85 | 1,85 |
| Propensity to save (\% points difference with BAU) | q2 | 0,01 | 0,01 | 0,01 | 0,01 | 0,01 | 0,01 | 0,01 | 0,01 | 0,01 | 0,01 | 0,01 | 0,01 |
| Propensity to save (\%) | q3 | 3,86 | 3,86 | 3,86 | 3,86 | 3,86 | 3,86 | 3,86 | 3,86 | 3,86 | 3,86 | 3,86 | 3,85 |
| Propensity to save (\% points difference with BAU) | q3 | 0,02 | 0,02 | 0,02 | 0,02 | 0,02 | 0,02 | 0,02 | 0,02 | 0,02 | 0,02 | 0,02 | 0,02 |
| Propensity to save (\%) | q4 | 7,81 | 7,81 | 7,81 | 7,81 | 7,81 | 7,80 | 7,80 | 7,80 | 7,80 | 7,80 | 7,80 | 7,79 |
| Propensity to save (\% points difference with BAU) | q4 | 0,05 | 0,05 | 0,04 | 0,04 | 0,04 | 0,04 | 0,04 | 0,04 | 0,03 | 0,03 | 0,03 | 0,03 |
| Propensity to save (\%) | q5 | 12,07 | 12,07 | 12,06 | 12,06 | 12,06 | 12,06 | 12,05 | 12,05 | 12,05 | 12,05 | 12,04 | 12,04 |
| Propensity to save (\% points difference with BAU) | q5 | 0,08 | 0,07 | 0,07 | 0,07 | 0,07 | 0,06 | 0,06 | 0,06 | 0,06 | 0,05 | 0,05 | 0,05 |
| Propensity to save (\%) | q6 | 29,54 | 29,53 | 29,53 | 29,52 | 29,52 | 29,51 | 29,50 | 29,50 | 29,49 | 29,48 | 29,48 | 29,47 |
| Propensity to save (\% points difference with BAU) | q6 | 0,20 | 0,19 | 0,19 | 0,18 | 0,17 | 0,17 | 0,16 | 0,16 | 0,15 | 0,14 | 0,14 | 0,13 |

## 5. Conclusions

The current paper set out to measure the impact of a corporate and personal income tax cut undertaken in the Azores, an autonomous region of Portugal.

For this purpose a dynamic CGE model was used. The calibration of the model used a
SAM matrix constructed with 2002 data with a considerable level of detail which was not
fully reported in this exercise.

The main concern here was to analyse the impact of the measure on a few major economic indicators, particularly GDP.

As expected, the reduction in taxes with a corresponding reduction in government expenditures led to a reduction in GDP in the short run. This result is, however, inverted in the longer run.

Government expenditures are reduced for the full period while private expenditures are increased, when compared to the base scenario of no tax cut.

In the end, the private sector tends to become relatively bigger and GDP to recover its growth path.

The impact of the policy benefits relatively more the lower income families that get a bigger increase in their wellbeing as measured by equivalent variation.

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## ANNEXES

## Model equations

### 3.13.1. Firms

$S F=\operatorname{shYKF} \cdot \sum_{s} P K_{s} \cdot K S K_{s}$
$K L_{s}=a K L_{s} \cdot X D_{s}$
$K S K_{s}=K L_{s} \cdot\left\{P K L_{s} /\left[P K_{s} \cdot\left(1+t k_{s}\right)+d_{s} \cdot P I\right]\right\}^{\sigma F_{s}} \cdot \gamma F K_{s}^{\sigma F_{s}} \cdot a F_{s}^{\left(\sigma F_{s}-1\right)}$
$L S K_{s}=K L_{s} \cdot\left\{P K L_{s} /\left[P L \cdot\left(1+\text { premLSK }_{s}\right) \cdot\left(1+t l_{s} /\left(1-t l_{s}\right)\right)\right]\right\}^{\sigma F_{s}} \cdot \gamma F L_{s}^{\sigma F_{s}} \cdot a F_{s}^{\left(\sigma F_{s}-1\right)}$
$P K L_{s} \cdot K L_{s}=P K_{s} \cdot\left(1+t k_{s}\right) \cdot K S K_{s}+P L \cdot\left(1+\operatorname{premLSK}_{s}\right) \cdot\left(1+t l_{s}\left(1-t l_{s}\right)\right) \cdot L S K_{s}+D E P_{s} \cdot P I$
$P D_{s} \cdot\left(1-t p_{s}+t s p_{s}+t s p e u e a_{s} \cdot M U t s p e u+t s p e u i_{s} \cdot M U t s p e u+t s p e u e r ~_{s} \cdot\right.$
MUtspeu + tspeues $_{s} \cdot$ MUtspeu $^{+}$tspusa $\left._{s}\right) \cdot X D_{s}=P K L_{s} \cdot K L_{s}+$
$\sum_{c}\left\{i_{c, s} \cdot X D_{s} \cdot\left[\left(1-t s i_{c, s}\right) \cdot P_{c}+\sum_{c t m} t_{c i c t m_{c m, c, s}} \cdot P_{c t m}\right] \cdot\left(1+\right.\right.$ vatic $\left.\left._{c, s}\right)\right\}$

### 3.13.2. Households

$\left[P_{c}+\sum_{c t m} t c h t m_{c t m, c, q u} \cdot P_{c t m}\right] \cdot\left(1+t e x c_{c, q u}\right) \cdot\left(1+t c_{c, q u}+v a t c_{c, q u}\right) \cdot C_{c, q u}=\left[P_{c}+\sum_{c t m} t c h t m_{c t m, c, q u} \cdot P_{c t m}\right]$.
$\left(1+\right.$ texc $\left._{c, q u}\right) \cdot\left(1+t c_{c, q u}+\right.$ vatc $\left._{c, q u}\right) \cdot \mu H_{c, q u}+\alpha H_{c, q u} \cdot\left\{C B U D_{q u}-\sum_{c c}\left[P_{c c}+\sum_{c t m}\right.\right.$ tchtm $\left._{c t m, c c, q u} \cdot P_{c t m}\right]$.
$\left(1+\right.$ texc $\left.\left._{c c, q u}\right) \cdot\left(1+t c_{c c, q u}+v a t c_{c c, q u}\right) \cdot \mu H_{c c, q u}\right\}$
$Y H_{q u}=s h Y K H_{q u} \cdot \sum_{s} P K_{s} \cdot K S K_{s}+\operatorname{shYLH}_{q u} \cdot \sum_{s} P L \cdot\left(1+\right.$ premLSK $\left._{s}\right) \cdot L S K_{s}+$ TRHML $_{q u}$.
$E R M L+$ shUNEMPB $B_{q u} \cdot$ trep $\cdot P L \cdot U N E M P+$ TRHG $_{q u} \cdot$ PCINDEX
$C B U D_{q u}=\left(1-t y_{q u}\right) \cdot Y H_{q u}-S H_{q u}$
$S H_{q u}=$ MPS $_{q u} \cdot\left(1-t y_{q u}\right) \cdot Y H_{q u}$
$M P S_{q u}=M P S Z_{q u} \cdot\left\{\left[\left(1-t y_{q u}\right) \cdot P K a v r\right] /\left[\left(1-t y z_{q u}\right) \cdot P K a v r Z\right]\right\}^{\text {elass }_{w u}}$
3.13.3. Regional government
$G R E V=T R P R O P+T R P R O D+T R A N S R$
TRPROP $=\sum_{q u} t y_{q u} \cdot Y H_{q u}+\sum_{s} t k_{s} \cdot K S K_{s} \cdot P K_{s}$
TRPROD $=\sum_{s} t p_{s} \cdot X D_{s} \cdot P D_{s}+\sum_{c, q u}\left\{\left[P_{c}+\sum_{c t m} \operatorname{tchtm}_{c t m, q, q u} \cdot P_{c t m}\right] \cdot\left[\right.\right.$ texc $c_{c, q u}+(1+$
texc $\left._{c, q u}\right) \cdot\left(t c_{c, q u}+\right.$ vatc $\left.\left.\left._{c, q u}\right)\right] \cdot C_{c, q u}\right\}+\sum_{c}\left[P_{c}+\sum_{c t m} t c i t m_{c m, c} \cdot P_{c t m}\right] \cdot$ vati $_{c} \cdot I_{c}+$
$\sum_{c, s}\left[\left(1-t s i c_{c, s}\right) \cdot P_{c}+\sum_{c t m} t c i c t m_{c t m, s, s} \cdot P_{c t m}\right] \cdot$ vatic $_{c, s} \cdot O_{c, s} \cdot X D_{s}+\sum_{c}\left(\right.$ tmus $_{c} \cdot P W M U S_{c} \cdot$
MUS $\left._{c} \cdot E R U S\right)+\sum_{c}\left(\right.$ tmrw $_{c} \cdot$ PWMROW $_{c} \cdot$ MROW $_{c} \cdot$ ERROW $)$

TRANSR $=$ TRGML $\cdot E R M L+T R G E U \cdot E R E U+T R G E C \cdot E R E U+T R G U S$.
ERUS + TRGW $\cdot$ ERROW
$G E X P=C G B U D+T R A N S+S U B S I D$
$P_{c} \cdot C G_{c}=\alpha C G_{c} \cdot C G B U D$
TRANS $=\sum_{q u} T R H G_{q u} \cdot$ PCINDEX
SUBSID $=\sum_{c, s} t s i c_{c, s} \cdot P_{c} \cdot i i_{c, s} \cdot X D_{s}+\sum_{s}\left[\left(t\right.\right.$ tsp $_{s}+$ tspeuea $_{s} \cdot$ MUtspeu +

TRGEC $\cdot$ EREU $=$ MUtspeu $\cdot \sum_{s}\left[\left(t\right.\right.$ speuea $_{s}+$ tspeufis + tspeuer $_{s}+t$ speues $\left.) \cdot X D_{s} \cdot P D_{s}\right]$
$S G \cdot G D P D E F=G R E V-G E X P$
$r T R P R O P G D P=T R P R O P / G D P C \cdot 100$
$r T R P R O D G D P=T R P R O D / G D P C \cdot 100$
$r$ TRANSRGDP $=$ TRANSR/GDPC $\cdot 100$
$r C G B U D G D P=C G B U D / G D P C \cdot 100$
$r$ TRANSGDP $=$ TRANS/GDPC $\cdot 100$
$r S U B S I D G D P=S U B S I D / G D P C \cdot 100$
$r S G G D P=S G \cdot G D P D E F / G D P C \cdot 100$

### 3.13.4. Mainland government

$S G M L=\sum_{s}\left[t l_{s} /\left(1-t l_{s}\right) \cdot L S K_{s} \cdot P L \cdot\left(1+\right.\right.$ premLSK $\left.\left._{s}\right) / E R M L\right]-\sum_{q u} T R H M L_{q u}-$ $\sum_{q u}\left(\right.$ shUNEMPB ${ }_{q u} \cdot$ trep $\left.\cdot P L \cdot U N E M P / E R M L\right)-T R G M L$
3.13.5. European Commission

SGEC $=-$ TRGEC - TRGEU
3.13.6. Domestic supply to domestic and foreign markets

$$
\begin{align*}
& X D D E_{c}=\sum_{s} i o C_{s, c} \cdot X D_{s}  \tag{A.31}\\
& P D_{s}=\sum_{c} i o C_{s, c} \cdot P D D E_{c} \tag{A.32}
\end{align*}
$$

### 3.13.7. Foreign sector

$$
\begin{align*}
& E M L_{c}=X D D E_{c} \cdot\left(P D D E_{c} / P E M L_{c}\right)^{\sigma T_{c}} \cdot \gamma T 1_{c}^{\sigma T_{c}} \cdot a T_{c}^{\left(\sigma T_{c}-1\right)}  \tag{A.33}\\
& E E U_{c}=X D D E_{c} \cdot\left(P D D E_{c} / P E E U_{c}\right)^{\sigma T_{c}} \cdot \gamma T T_{c}^{\sigma T_{c}} \cdot a T_{c}^{\left(\sigma T_{c}-1\right)}  \tag{A.34}\\
& E U S_{c}=X^{c} E_{c} \cdot\left(P D D E_{c} / P E U S_{c}\right)^{\sigma \tau_{c}} \cdot \gamma T 3_{c}^{\sigma T_{c}} \cdot a T_{c}^{\left(\sigma T_{c}-1\right)} \tag{A.35}
\end{align*}
$$

$$
\begin{align*}
& E R O W_{c}=\text { XDDE }_{c} \cdot\left(\text { PDDE }_{c} / \text { PEROW } W_{c}\right)^{\sigma T_{c}} \cdot \gamma T 4_{c}^{\sigma T_{c}} \cdot a T_{c}^{\left(\sigma T_{c}-1\right)}  \tag{A.36}\\
& X D D_{c}=X D D E_{c} \cdot\left(P D D E_{c} / P D D_{c}\right)^{\sigma T_{c}} \cdot \gamma T 5_{c}^{\sigma T_{c}} \cdot a T_{c}^{\left(\sigma T_{c}-1\right)}  \tag{A.37}\\
& P D D E_{c} \cdot X D D E_{c}=P D D_{c} \cdot X D D_{c}+P E M L_{c} \cdot E M L_{c}+P E E U_{c} \cdot E E U_{c}+P E U S_{c} \cdot E U S_{c}+ \\
& \text { PEROW }_{c} \cdot \text { EROW }_{c}  \tag{A.38}\\
& E^{E D R O W}{ }_{c}=E D I R O W_{c} \cdot\left(\text { PWEROW }_{c} \cdot E R R O W / P E R O W_{c}\right)^{\text {elas } E_{c}}  \tag{A.43}\\
& M M L_{c}=X_{c} \cdot\left(P_{c} / P M M L_{c}\right)^{\sigma A_{c}} \cdot \gamma A 1_{c}^{\sigma A_{c}} \cdot a A_{c}^{\left(\sigma A_{c}-1\right)}  \tag{A.44}\\
& \text { MEU }_{c}=X_{c} \cdot\left(P_{c} / P M E U_{c}\right)^{\sigma A_{A}} \cdot \gamma A 2_{c}^{\sigma A_{c}} \cdot a A_{c}^{\left(\sigma A_{c}-1\right)}  \tag{A.45}\\
& \text { MUS }_{c}=X_{c} \cdot\left(P_{c} / P M U S_{c}\right)^{\sigma A_{c}} \cdot \gamma A 3_{c}^{\sigma A_{c}} \cdot a A_{c}^{\left(\sigma A_{c}-1\right)}  \tag{A.46}\\
& \text { MROW }_{c}=X_{c} \cdot\left(P_{c} / P M R O W_{c}\right)^{\sigma A_{A}} \cdot \gamma A A_{c}^{\sigma A_{c}} \cdot a A_{c}^{\left(\sigma A_{c}-1\right)}  \tag{A.47}\\
& X D D_{c}=X_{c} \cdot\left(P_{c} / P D D_{c}\right)^{\sigma A_{c}} \cdot \gamma A 5_{c}^{\sigma A_{c}} \cdot a A_{c}^{\left(\sigma A_{c}-1\right)}  \tag{A.48}\\
& P_{c} \cdot X_{c}=P M M L_{c} \cdot M M L_{c}+P M E U_{c} \cdot M E U_{c}+P M U S_{c} \cdot \text { MUS }_{c}+\text { PMROW }_{c} \cdot \text { MROW }_{c}+ \\
& P D D_{c} \cdot X D D_{c}  \tag{A.49}\\
& M_{c}=\left(P W M M L_{c} \cdot E R M L \cdot M M L_{c}+P W M E U_{c} \cdot E R E U \cdot \text { MEU }_{c}+P W M U S S_{c} \cdot E R U S \cdot M U S_{c}+\right. \\
& \text { PWMROW }_{c} \cdot \text { ERROW }^{\prime} \cdot \text { MROW }_{c} \text { )/INDEXM }{ }_{c}  \tag{A.50}\\
& S M L=\sum_{c}\left(M M L_{c} \cdot P W M M L_{c}-E M L_{c} \cdot P E M L_{c} / E R M L\right)+S G M L  \tag{A.51}\\
& S E U=\sum_{c}\left(\text { MEU }_{c} \cdot P W M E U_{c}-E E U_{c} \cdot P E E U_{c} / E R E U\right)+S G E C  \tag{A.52}\\
& S U S=\sum_{c}\left(\text { MUS }_{c} \cdot P W M U S_{c}-E U S_{c} \cdot P E U S_{c} / E R U S\right)-\text { TRGUS }  \tag{A.53}\\
& \text { SROW }=\sum_{c}\left(\text { MROW }_{c} \cdot P W M R O W_{c}-E R O W_{c} \cdot P E R O W_{c} / E R R O W\right)-T R G W  \tag{A.54}\\
& \text { 3.13.8. Investment } \\
& S=\sum_{q u} S H_{q u}+S F+S G \cdot G D P D E F+S M L \cdot E R M L+S E U \cdot E R E U+S U S \cdot E R U S+S R O W . \\
& E R R O W+\sum_{s} D E P_{s} \cdot P I  \tag{A.55}\\
& I_{c}=i o I_{c} \cdot I T T  \tag{A.56}\\
& P I=\sum_{c}\left\{\left(1+v a t i_{c}\right) \cdot\left[P_{c}+\sum_{c m} t_{c i t m_{c m, c}} \cdot P_{c t m}\right] \cdot i o I_{c}\right\} \tag{A.57}
\end{align*}
$$

$P I \cdot I T T=S-\sum_{c} S V_{c} \cdot P_{c}$
$S V_{c}=s v r_{c} \cdot X_{c}$
$D E P_{s}=d_{s} \cdot K S K_{s}$

### 3.13.9. Labor market

$\log (P L / P C I N D E X)=e l a s U \cdot \log (U N R A T E)+e r r$
$L S R=L S R I \cdot\{[P L \cdot(1-\text { tyavr }) \cdot P C I N D E X Z] /[P L Z \cdot(1-\text { tyavrz }) \cdot P C I N D E X]\}^{\text {elasLS }}$
tyavr $=\sum_{q u}\left(t y_{q u} \cdot Y H_{q u}\right) / \sum_{q u} Y H_{q u}$
$E M P N=L S R-U N E M P$
UNRATE $=$ UNEMP/LSR

### 3.13.10. Trade and transport margins

MARGTM $_{c t m}=\sum_{c, q u} \operatorname{tchtm}_{c m m, c, q u} \cdot C_{c, q u}+\sum_{c} t c i t m_{c t m, c} \cdot I_{c}+\sum_{s, c}{t c i c t m_{c m m, s,}} \cdot i o_{c, s} \cdot X D_{s}$
3.13.11. Market clearing
$\sum_{s} L S K_{s}=L S R-U N E M P$
$\sum_{s} i i_{c t m, s} \cdot X D_{s}+\sum_{q u} C_{c m, q u}+C G_{c t m}+I_{c t m}+S V_{c t m}+M A R G T M_{c t m}=X_{c t m}$
$\sum_{s} i o_{n c t m, s} \cdot X D_{s}+\sum_{q u} C_{n c t m, q u}+C G_{n c m}+I_{n c t m}+S V_{n c t m}=X_{n c t m}$
$E M L_{c}=E D M L_{c}$
$E E U_{c}=E D E U_{c}$
$E U S_{c}=E D U S_{c}$
3.13.12. Price definitions

PCINDEX $=\sum_{c, q u}\left\{\left[P_{c}+\sum_{c t m}\right.\right.$ tchtm $\left._{c m m, c, u} \cdot P_{c t m}\right] \cdot\left(1+\right.$ texc $\left.\left._{c, q u}\right) \cdot\left(1+t c_{c, q u}+v a t c_{c, q u}\right) \cdot C Z_{c, q u}\right\} /$
$\sum_{c, q u}\left\{\left[P Z_{c}+\sum_{c m m} \operatorname{tchtmz}_{c m m, q u} \cdot P Z_{c t m}\right] \cdot\left(1+t e x c z_{c, q u}\right) \cdot\left(1+t c z_{c, q u}+v a t c c_{c, q u}\right) \cdot C Z_{c, q u}\right\}$
INDEXE $_{c}=\left(\right.$ PEML $_{c} \cdot E M L Z_{c}+$ PEEU $_{c} \cdot E E U Z_{c}+$ PEUS $_{c} \cdot E U S Z_{c}+$ PEROW $\left._{c} \cdot E R O W Z_{c}\right) /$
$\left(\right.$ PEMLZ $_{c} \cdot E M L Z ~_{c}+$ PEEUZ $_{c} \cdot E E U Z_{c}+$ PEUSZ $_{c} \cdot E U S Z ~_{c}+$ PEROWZ $\left._{c} \cdot E R O W Z ~_{c}\right)$
INDEXM $_{c}=\left(P W M M L_{c} \cdot E R M L \cdot M M L Z ~_{c}+P W M E U_{c} \cdot E R E U \cdot M E U Z ~_{c}+P W M U S_{c} \cdot E R U S\right.$.
MUSZ $_{c}+$ PWMROW $_{c} \cdot E R R O W \cdot$ MROWZ $\left._{c}\right)\left(\right.$ PWMMLZ $_{c} \cdot E R M L Z \cdot M M L Z_{c}+P W M E U Z_{c} \cdot$
$\left.E R E U Z \cdot M E U Z_{c}+P W M U S Z_{c} \cdot E R U S Z \cdot M U S Z_{c}+P W M R O W Z_{c} \cdot E R R O W Z \cdot M R O W Z{ }_{c}\right)$

$$
\begin{align*}
& P M M L_{c}=P W M M L_{c} \cdot E R M L  \tag{A.77}\\
& P M E U_{c}=P W M E U_{c} \cdot E R E U  \tag{A.78}\\
& P M U S_{c}=P W M U S_{c} \cdot E R U S \cdot\left(1+t m u s_{c}\right)  \tag{A.79}\\
& P M R O W_{c}=P W M R O W_{c} \cdot E R R O W \cdot\left(1+t m r w_{c}\right)  \tag{A.80}\\
& R I N T=\sum_{s}\left[\left(P K_{s} / P D_{s}\right) \cdot K S K_{s}\right] / \sum_{s} K S K_{s}  \tag{A.81}\\
& P K a v r=\sum_{s}\left[\left(P K_{s} / P C I N D E X\right) \cdot K S K_{s}\right] / \sum_{s} K S K_{s}  \tag{A.82}\\
& P C T_{c, q u}=\left[P_{c}+\sum_{c t m} t c h t m_{c t m, c, q u} \cdot P_{c t m}\right] \cdot\left(1+t e x c_{c, q u}\right) \cdot\left(1+t c_{c, q u}+\text { vatc }_{c, q u}\right)  \tag{A.83}\\
& P L A V R T \cdot(L S R-U N E M P)=\sum_{s}\left[P L \cdot\left(1+t l_{s} /\left(1-t l_{s}\right)\right) \cdot\left(1+\text { premLSK }_{s}\right) \cdot L S K_{s}\right] \tag{A.84}
\end{align*}
$$

3.13.13. Gross domestic product at current and constant market prices

$$
\begin{align*}
& G D P C=\sum_{c, q u}\left\{C_{c, q u} \cdot\left[P_{c}+\sum_{c t m} \text { tchtm }_{c t m, c, q u} \cdot P_{c t m}\right] \cdot\left(1+\text { texx }_{c, q u}\right) \cdot\left(1+t c_{c, q u}+\text { vatc }_{c, q u}\right)\right\}+ \\
& \sum_{c} C G_{c} \cdot P_{c}+\sum_{c}\left\{I_{c} \cdot\left(1+v a t i_{c}\right) \cdot\left[P_{c}+\sum_{c m} t^{2 i t m} m_{c m, c} \cdot P_{c t m}\right]\right\}+\sum_{c} S V_{c} \cdot P_{c}+\sum_{c} E M L_{c} \cdot P E M L_{c} \\
& +\sum_{c} E E U_{c} \cdot P E E U_{c}+\sum_{c} E U S_{c} \cdot P E U S_{c}+\sum_{c} E R O W_{c} \cdot \text { PEROW }_{c}- \\
& \sum_{c} M M L_{c} \cdot P W M M L_{c} \cdot E R M L-\sum_{c} M E U_{c} \cdot P W M E U_{c} \cdot E R E U- \\
& \sum_{c} \text { MUS }_{c} \cdot \text { PWMUS }_{c} \cdot \text { ERUS }-\sum_{c} \text { MROW }_{c} \cdot P W M R O W_{c} \cdot E R R O W  \tag{A.85}\\
& G D P=\sum_{c, q u}\left\{C_{c, q u} \cdot\left[P Z_{c}+\sum_{c t m} \text { tchtmz }_{c t m, c, q u} \cdot P Z_{c t m}\right] \cdot\left(1+\text { texcc }_{c, q u}\right) \cdot\left(1+t c c_{c, q u}+v a t c z_{c, q u}\right)\right\}+ \\
& \sum_{c} C G_{c} \cdot P Z_{c}+\sum_{c}\left\{I_{c} \cdot\left(1+v a t i z_{c}\right) \cdot\left[P Z_{c}+\sum_{c t m} t c i t m Z_{c m m, c} \cdot P Z_{c t m}\right]\right\}+\sum_{c} S V_{c} \cdot P Z_{c}+ \\
& \sum_{c} E M L_{c} \cdot P E M L Z_{c}+\sum_{c} E E U_{c} \cdot P E E U Z_{c}+\sum_{c} E U S_{c} \cdot P E U S Z_{c}+\sum_{c} E R O W_{c} \cdot P E R O W Z_{c}- \\
& \sum_{c} M M L_{c} \cdot P W M M L Z_{c} \cdot E R M L Z-\sum_{c} M E U_{c} \cdot P W M E U Z_{c} \cdot E R E U Z- \\
& \sum_{c} \text { MUS }_{c} \cdot P W M U S Z_{c} \cdot E R U S Z-\sum_{c} \text { MROW }_{c} \cdot P W M R O W Z ~ \cdot E R R O W Z ~  \tag{A.86}\\
& G D P P=\sum_{c, q u}\left\{C_{c, q u} \cdot\left[P Z_{c}+\sum_{c t m} \operatorname{tchtmz}_{c t m, c, u} \cdot P Z_{c t m}\right] \cdot\left(1+\text { texcz }_{c, q u}\right) \cdot\left(1+t c z_{c, q u}+v a t c z_{c, q u}\right)\right\}+ \\
& \sum_{c}\left\{I_{c} \cdot\left(1+v a t i z_{c}\right) \cdot\left[P Z_{c}+\sum_{c t m} t c i t m z_{c t m, c} \cdot P Z_{c t m}\right]\right\}+\sum_{c} S V_{c} \cdot P Z_{c}+\sum_{c} E M L_{c} \cdot P E M L Z_{c}+ \\
& \sum_{c} E E U_{c} \cdot P E E U Z_{c}+\sum_{c} E U S_{c} \cdot P E U S Z_{c}+\sum_{c} E R O W_{c} \cdot P E R O W Z_{c}- \\
& \sum_{c} M M L_{c} \cdot P W M M L Z_{c} \cdot E R M L Z-\sum_{c} M E U_{c} \cdot P W M E U Z_{c} \cdot E R E U Z- \\
& \sum_{c} M U S_{c} \cdot P W M U S Z_{c} \cdot E R U S Z-\sum_{c} M R O W_{c} \cdot P W M R O W Z_{c} \cdot E R R O W Z \\
& \text { GDPDEF }=\text { GDPC/GDP } \tag{A.87}
\end{align*}
$$

3.13.14. Components of GDP at constant prices
$C T=\sum_{c, q u}\left\{C_{c, q u} \cdot\left[P Z_{c}+\sum_{c t m} \operatorname{tchtmz}_{c t m, c, q u} \cdot P Z_{c t m}\right] \cdot\left(1+t e x c c_{c, q u}\right) \cdot\left(1+t c c_{c, q u}+v a t c z_{c, q u}\right)\right\}$
$C G T=\sum_{c} C G_{c} \cdot P Z_{c}$
$I T=\sum_{c}\left\{I_{c} \cdot\left(1+v a t i z_{c}\right) \cdot\left[P Z_{c}+\sum_{c t m} t \operatorname{tcitmz_{cm,c}} \cdot P Z_{c t m}\right]\right\}+\sum_{c} S V_{c} \cdot P Z_{c}$
$E T=\sum_{c}\left(E M L_{c} \cdot P E M L Z_{c}+E E U_{c} \cdot P E E U Z_{c}+E U S_{c} \cdot\right.$ PEUSZ $\left._{c}+E R O W_{c} \cdot P E R O W Z_{c}\right)$
$M T=\sum_{c}\left(M M L_{c} \cdot P W M M L Z_{c} \cdot E R M L Z+M E U_{c} \cdot P W M E U Z_{c} \cdot E R E U Z+\right.$

### 3.13.15. Equivalent variation in income

$V U_{q u}=\left\{C B U D_{q u}-\sum_{c}\left[P_{c}+\sum_{c t m}\right.\right.$ tchtm $\left._{c t m, c, q u} \cdot P_{c t m}\right] \cdot\left(1+\right.$ texc $\left._{c, q u}\right) \cdot\left(1+t c_{c, q u}+\right.$ vatc $\left._{c, q u}\right)$.
$\left.\mu H_{c, q u}\right\} \cdot \prod_{c}\left\{\alpha H_{c, q u} /\left\{\left[P_{c}+\sum_{c t m}\right.\right.\right.$ tchtm $\left._{c t m, c, q u} \cdot P_{c t m}\right] \cdot\left(1+\right.$ texc $\left._{c, q u}\right) \cdot\left(1+t c_{c, q u}+\right.$
vatc $\left.\left.\left._{c, q u}\right)\right\}\right\}^{\alpha H_{c q u}}$
$V U I_{q u}=\left\{C B U D Z_{q u}-\sum_{c}\left[P Z_{c}+\sum_{c t m} \operatorname{tchtmz}_{c t m,, q u} \cdot P Z_{c t m}\right] \cdot\left(1+\right.\right.$ texcz $\left._{c, q u}\right) \cdot\left(1+t c z_{c, q u}+v a t c z_{c, q u}\right)$.
$\left.\mu H_{c, q u}\right\} \cdot \prod_{c}\left\{\alpha H_{c, q u} /\left\{\left[P Z_{c}+\sum_{c t m} \operatorname{tchtmz}_{c t m, c, q u} \cdot P Z_{c m m}\right] \cdot\left(1+t e x c c_{c, q u}\right) \cdot\left(1+t c c_{c, q u}+\right.\right.\right.$
$\left.\left.\left.\operatorname{vatcc}_{c, q u}\right)\right\}\right\}^{\alpha H_{c q u}}$
$E V_{q u}=\prod_{c}\left\{\left\{\left[P Z_{c}+\sum_{c t m} t c h t m z_{c m m, q, q u} \cdot P Z_{c m m}\right] \cdot\left(1+t e x c c_{c, q u}\right) \cdot\left(1+t c c_{c, q u}+v a t c z_{c, q u}\right)\right\} /\right.$
$\left.\alpha H_{c, q u}\right\}^{\alpha H_{c q u}} \cdot\left(V U_{q u}-V U I_{q u}\right)$

### 3.13.16. Capital accumulation

$R O R_{s, t}=-1+\left(P K_{\mathrm{s}, t} / P I_{t}+1\right) /\left(1+R I N T_{t}\right)$

INVS $_{s, t}=$ KSK $_{s, t} \cdot\left[\alpha\right.$ ROR $_{s, t} \cdot$ KSKgmax $_{s} \cdot\left(\right.$ KSKtrend $_{s}-$ KSKgmin $\left._{s}\right)+$ KSKgmin $_{s}$.
$\left(\right.$ KSKgmax $_{s}-$ KSKtrend $\left.\left._{s}\right)\right] /\left[\alpha R O R_{s, t} \cdot\left(\right.\right.$ KSKtrend $_{s}-$ KSKgmin $\left._{s}\right)+$
$\left(\right.$ KSKgmax $_{s}-$ KSKtrend $\left.\left._{s}\right)\right]+d_{s} \cdot$ KSK $_{s, t}$
$I N V_{\mathrm{s}, t}=I N V S_{\mathrm{s}, t} / \sum_{\mathrm{ss}} I N V S_{\mathrm{ss}, t} \cdot\left(S_{t}-\sum_{\mathrm{c}} S V_{\mathrm{c}, \mathrm{t}} \cdot P_{\mathrm{c}, \mathrm{t}}\right) P I_{t}$
$K S K_{s, t+1}=\left(1-d_{s}\right) \cdot K S K_{s, t}+I N V_{s, t}$

## List of Endogenous variables

| $\mathrm{CBUD}_{\text {qu }}$ | households budget disposable for consumption by income group |
| :---: | :---: |
| $\mathrm{C}_{\mathrm{c}, \mathrm{qu}}$ | consumer demand for commodity $c$ by income group qu |
| CGBUD | regional government current expenditures |
| CG ${ }_{\text {c }}$ | public current consumption of commodity $c$ by the regional government |
| CGT | total public consumption by the regional government at constant prices |
| CT | total private consumption at constant prices |
| $\mathrm{DEP}_{\text {s }}$ | depreciation related to public and private capital stock |
| $\mathrm{EDEU}_{\mathrm{c}}$ | export demand of commodity $c$ from EU |
| $\mathrm{EDML}_{\text {c }}$ | export demand of commodity $c$ from Mainland |
| $\mathrm{EDROW}_{\text {c }}$ | export demand of commodity $c$ from the rest of the world |
| EDUS ${ }_{\text {c }}$ | export demand of commodity $c$ from US |
| $\mathrm{EEU}_{\text {c }}$ | export supply of commodity $c$ by the domestic producers to EU |
| $\mathrm{EML}_{\text {c }}$ | export supply of commodity $c$ by the domestic producers to Mainland |
| EMPN | national employment |
| $\mathrm{EROW}_{\text {c }}$ | export supply of commodity $c$ by the domestic producers to the rest of the world |
| ET | total exports at constant prices |
| EUS $_{\text {c }}$ | export supply of commodity $c$ by the domestic producers to US |
| $\mathrm{EV}_{\text {qu }}$ | equivalent variation in income, by household income group |
| GDP | gross domestic product at constant prices |
| GDPC | gross domestic product at current market prices |
| GDPP | private gross domestic product at constant prices |
| GEXP | total regional government expenditures |
| GREV | total regional government revenues |
| $\mathrm{I}_{\text {c }}$ | demand for investment good $c$ |
| $\mathrm{INDEXE}_{\text {c }}$ | price index corresponding to exports by type of commodity $c$ |
| $\mathrm{INDEXM}_{\text {c }}$ | price index corresponding to imports by type of commodity $C$ |
| $\mathrm{INV}_{\text {s }}$ | investments carried out in branch $s$ (actual level) |
| $\mathrm{INVS}_{\text {s }}$ | investments carried out in branch $s$ (first estimate) |
| IT | total gross capital formation at constant prices (including inventories) |
| ITT | total investments in real terms |
| $\mathrm{KL}_{\text {s }}$ | value-added by branch |
| $\mathrm{LSK}_{\text {s }}$ | number of employees in branch $s$ |
| LSR | active population |
| MARGTM $_{\text {ctm }}$ | trade and transport margins |
| MEU ${ }_{\text {c }}$ | imports of commodity $c$ from EU |
| $\mathrm{MML}_{\text {c }}$ | imports of commodity $c$ from Mainland |
| MPS ${ }_{\text {qu }}$ | households propensity to save, by income group |
| $\mathrm{MROW}_{\text {c }}$ | imports of commodity $c$ from the rest of the world |


| MT | to |
| :---: | :---: |
| MUS ${ }_{\text {c }}$ | imports of commodity c from US |
| $\mathrm{P}_{\mathrm{c}}$ | price level of domestic sales (composite commodities coming from imports and domestic production) |
| PCINDEX | consumer price index |
| $\mathrm{PCT}_{\text {c,qu }}$ | consumer prices (including taxes) |
| $\mathrm{PDD}_{\text {c }}$ | price index of domestic production delivered to home market by type of good $c$ |
| $\mathrm{PDDE}_{\mathrm{c}}$ | price index of domestic production delivered to home and foreign markets by type of good $c$ |
| $\mathrm{PD}_{\text {s }}$ | price index of domestic production by branch of activity |
| $\mathrm{PEEU}_{\mathrm{c}}$ | domestic price of exports to EU received by the domestic producers |
| PEML $_{\text {c }}$ | domestic price of exports to Mainland received by the domestic producers |
| PEROW ${ }_{\text {c }}$ | domestic price of exports to the rest of the world received by the domestic producers |
| PEUS ${ }_{\text {c }}$ | domestic price of exports to US received by the domestic producers |
| PI | price index corresponding to composite investment good |
| PKavr | real average return to capital received by the household |
| $\mathrm{PKL}_{\text {s }}$ | price index corresponding to value-added by branch of activity |
| $\mathrm{PK}_{\text {s }}$ | return to capital by branch of activity |
| PL | national average wage (excluding social security contributions) |
| PLAVRT | national average wage (including social security contributions) |
| $\mathrm{PMEU}_{\mathrm{c}}$ | domestic price of imports from EU |
| $\mathrm{PMML}_{\text {c }}$ | domestic price of imports from Mainland |
| $\mathrm{PMROW}_{\text {c }}$ | domestic price of imports from the rest of the world (including tariffs) |
| PMUS $_{\text {c }}$ | domestic price of imports from US (including tariffs) |
| RINT | average return to capital corresponding to firms |
| $\mathrm{ROR}_{\mathrm{s}, \mathrm{t}}$ | normal rate of return to capital |
| rSGGDP | regional government savings to the GDP ratio |
| rSUBSIDGDP | total subsidies by the regional government to the GDP ratio |
| rTRANSGDP | total transfers by the regional government to the GDP ratio |
| rTRANSRGDP | total transfers received by the regional government to the GDP ratio |
| rTRPRODGDP | regional government revenues from taxes on products and on production to the GDP ratio |
| rTRPROPGDP | regional government revenues from taxes on income and wealth to the GDP ratio |
| S | total savings |
| SEU | balance of the current account with respect to EU |
| SF | firms savings |
| SGEC | net transfers by the European Commission to Azores |
| SGML | net transfers by the Mainland government to Azores |
| $\mathrm{SH}_{\mathrm{qu}}$ | households savings by income group |
| SML | balance of the current account with respect to Mainland |
| SROW | balance of the current account with respect to ROW |
| SUBSID | total subsidies by the regional government |


| SUS | balance of the current account with respect to US |
| :---: | :---: |
| $\mathrm{SV}_{\mathrm{c}}$ | inventories |
| TRANS | total transfers by the regional government |
| TRANSR | total transfers received by the regional government |
| TRPROD | regional government revenues from taxes on products and on production |
| TRPROP tyavr | regional government revenues from taxes on income and wealth average personal income tax rate |
| UNEMP | number of unemployed |
| UNRATE | unemployment rate |
| $\mathrm{VU}_{\mathrm{qu}}$ | level of indirect utility corresponding to the households, by income group |
| $\mathrm{X}_{\text {c }}$ | domestic sales of composite commodities coming from imports and domestic production |
| $\mathrm{XDD}_{\text {c }}$ | domestic production delivered to home market |
| $\mathrm{XDDE}_{\mathrm{c}}$ | domestic production delivered to home and foreign markets (by type of commodity) |
| $\mathrm{XD}_{\text {s }}$ | domestic production by branch of activity |
| $\mathrm{YH}_{\mathrm{qu}}$ | households income, by income group |
| $\alpha \mathrm{ROR}_{\mathrm{s}, \mathrm{t}}$ | parameter in the supply of capital function |

## List of Exogenous variables

| $\mathrm{CZ}_{\mathrm{c}, \mathrm{qu}}$ | consumer demand for commodity $c$ (benchmark value) |
| :---: | :---: |
| EDIEU $_{\text {c }}$ | export demand of commodity $c$ from EU (benchmark value) |
| EDIML ${ }_{\text {c }}$ | export demand of commodity $c$ from the Mainland (benchmark value) |
| EDIROW $_{\text {c }}$ | export demand of commodity $c$ from the rest of the world (benchmark value) |
| EDIUS $_{\text {c }}$ | export demand of commodity $c$ from US (benchmark value) |
| EREU | exchange rate with respect to EU |
| EREUZ | exchange rate with respect to EU (benchmark value) |
| ERML | exchange rate with respect to Mainland |
| ERMLZ | exchange rate with respect to Mainland (benchmark value) |
| ERROW | exchange rate with respect to the rest of the world |
| ERROWZ | exchange rate with respect to the rest of the world (benchmark value) |
| ERUS | exchange rate with respect to US |
| ERUSZ | exchange rate with respect to US (benchmark value) |
| GDPDEF | GDP deflator |
| KSK ${ }_{\text {s }}$ | capital demand by branch (capital stock) |
| LSRI | active population (benchmark value) |
| $\mathrm{MPSZ}_{\text {qu }}$ | households propensity to save, by income group (benchmark value) |
| PCINDEXZ | consumer price index (benchmark value) |
| PEEUZ ${ }_{\text {c }}$ | domestic price of exports to EU received by the domestic producers (benchmark value) |
| PEMLZ ${ }_{\text {c }}$ | domestic price of exports to Mainland received by the domestic producers (benchmark value) |
| PEROWZ ${ }_{\text {c }}$ | domestic price of exports to the rest of the world received by the domestic producers (benchmark value) |
| $\mathrm{PEUSZ}_{\text {c }}$ | domestic price of exports to US received by the domestic producers (benchmark value) |
| PKavrZ | real average return to capital received by the household (benchmark value) |
| PLZ | national average wage (excluding social security contributions) benchmark value |
| $\mathrm{PWEEU}_{\text {c }}$ | price of exports to EU in foreign currency |
| $\mathrm{PWEML}_{\text {c }}$ | price of exports to Mainland in foreign currency |
| PWEROW ${ }_{\text {c }}$ | price of exports to ROW in foreign currency |
| PWEUS ${ }_{\text {c }}$ | price of exports to US in foreign currency |
| $\mathrm{PWMEU}_{\text {c }}$ | price of imports from EU in foreign currency |
| PWMEUZ ${ }_{\text {c }}$ | price of imports from EU in foreign currency (benchmark value) |
| PWMML ${ }_{\text {c }}$ | price of imports from Mainland in foreign currency |
| PWMMLZ ${ }_{\text {c }}$ | price of imports from Mainland in foreign currency (benchmark value) |
| PWMROW | price of imports from ROW in foreign currency |
| $\mathrm{PWMROWZ}_{\text {c }}$ | price of imports from ROW in foreign currency (benchmark value) |


| PWMUS $_{\text {c }}$ | price of imports from US in foreign currency |
| :---: | :---: |
| PWMUSZ ${ }_{\text {c }}$ | price of imports from US in foreign currency (benchmark value) |
| $\mathrm{PZ} \mathrm{c}_{\mathrm{c}}$ | price level of domestic sales (composite commodities coming from imports and domestic production) - benchmark value |
| $\mathrm{RORH}_{\text {s }}$ | historically normal rate of return to capital |
| SG | regional government savings |
| TRGEC | transfers received by the regional government from EU as direct subsidies on production |
| TRGEU | other transfers received by the regional government from EU |
| TRGML | transfers received by the regional government from the Mainland government |
| TRGUS | transfers received by the regional government from US |
| TRGW | transfers received by the regional government from the rest of the world |
| $\mathrm{TRHG}_{\mathrm{qu}}$ | transfers received by the households from the regional government, by income group |
| $\mathrm{TRHML}_{\mathrm{qu}}$ | transfers received by the households from the Mainland government, by income group |
| $\mathrm{VUI}_{\mathrm{qu}}$ | level of indirect utility corresponding to the household, by income group (benchmark level) |

## List of Parameters

| $\mathrm{aA}_{\mathrm{c}}$ | efficiency parameter in the Armington function for imports <br> efficiency parameter in the CES production function of the firm |
| :--- | :--- |
| $\mathrm{aF}_{\mathrm{s}}$ | Leontief parameter - share of value added in domestic production <br> efficiency parameter in the CET function for exports |
| $\mathrm{aKL}_{\mathrm{s}}$ | depreciation rate by branch of activity $^{\text {price elasticity of export demand }}$ |


| $\mathrm{tk}_{\text {s }}$ | corporate tax rate in branch $s$ |
| :---: | :---: |
| $\mathrm{tl}_{\text {s }}$ | social security contributions rate in branch $s$ |
| $\mathrm{tmrw}_{\mathrm{c}}$ | tariff rate applied on imports of commodity $c$ from ROW |
| tmus $_{\text {c }}$ | tariff rate applied on imports of commodity $c$ from US |
| $\mathrm{tp}_{\mathrm{s}}$ | tax rate on production in branch $s$ |
| trep | replacement rate out of national average wage (net of social security contributions) |
| $\operatorname{tsic}_{\text {c,s }}$ | subsidy rate on intermediate consumption |
| tspeuea $_{\text {s }}$ | subsidy rate on production from the European Agricultural Guidance and Guarantee Fund (EAGGF) |
| tspeuer $_{\text {s }}$ | subsidy rate on production from the European Regional Development Fund (ERDF) |
| $\mathrm{tspeues}_{\text {s }}$ | subsidy rate on production from the European Social Fund (ESF) |
| tspeufi $_{\text {s }}$ | subsidy rate on production from the Financial Instrument for Fisheries Guidance (FIFG) |
| $\mathrm{tsp}_{\mathrm{s}}$ | subsidy rate on production in branch $s$ |
| tspusa $_{\text {s }}$ | subsidy rate on production from US |
| tyavrz | average personal income tax rate (benchmark level) |
| $t y_{\text {qu }}$ | personal income tax rate by income group |
| $\mathrm{tyz}_{\text {qu }}$ | personal income tax rate by income group (benchmark level) |
| vatc $_{\text {c,qu }}$ | value-added tax rate on private consumption of commodity $c$ |
| vatcz ${ }_{\text {c, }, \text { u }}$ | value-added tax rate on private consumption of commodity $c$ (benchmark value) |
| vati $_{\text {c }}$ | value-added tax rate on investment good $c$ |
| vatic $_{\text {c,s }}$ | value-added tax rate on intermediate consumption of commodity |
| vatiz ${ }_{\text {c }}$ | value-added tax rate on investment goods (benchmark level) |
| $\alpha \mathrm{CG}_{\mathrm{c}}$ | Cobb-Douglas preference parameter in the regional government utility function |
| $\alpha \mathrm{H}_{\mathrm{c}, \mathrm{qu}}$ | marginal budget shares in the Stone-Geary utility function |
| $\gamma \mathrm{Al}{ }_{\text {c }}$ | CES distribution parameter for imports from Mainland in the Armington function |
| $\gamma \mathrm{A} 2_{\text {c }}$ | CES distribution parameter for imports from EU in the Armington function |
| $\gamma \mathrm{A} 3_{\text {c }}$ | CES distribution parameter for imports from US in the Armington function |
| $\gamma \mathrm{A} 4_{\text {c }}$ | CES distribution parameter for imports from ROW in the Armington function |
| $\gamma \mathrm{A} 5_{\text {c }}$ | CES distribution parameter for the domestic demand from the domestic producers in the Armington function |
| $\gamma \mathrm{FK}_{\text {s }}$ | CES distribution parameter for capital in the production function of the firm |
| $\gamma \mathrm{FL}_{\text {s }}$ | CES distribution parameter for labour in the production function of the firm |
| $\gamma \mathrm{T} 1_{\text {c }}$ | CET distribution parameter for exports to Mainland |
| $\gamma \mathrm{T} 2_{\text {c }}$ | CET distribution parameter for exports to EU |
| $\gamma \mathrm{T} 3_{\text {c }}$ | CET distribution parameter for exports to US |
| $\gamma \mathrm{T} 4_{\text {c }}$ | CET distribution parameter for exports to ROW |
| $\gamma \mathrm{T} 5_{\mathrm{c}}$ | CET distribution parameter for domestic production delivered to home markets |

subsistence level out of consumer demand for commodities substitution elasticities for the Armington function
$\sigma \mathrm{F}_{\mathrm{s}}$ CES capital-labour substitution elasticities by branch $\sigma \mathrm{T}_{\mathrm{c}}$ elasticities of transformation in the CET function

## List of indices used in the model

| c | a subscript for one of the commodities (45 types of commodities) <br> cc <br> the same as $c$ (used for exposition purposes) |
| :--- | :--- |
| ctm | a subscript for trade and transport services (7 types of trade and <br> transport services) |
| nctm | a subscript for all the other commodities except trade and transport <br> services (38 types of commodities) <br> a subscript for one of the households income groups (6 households <br> income groups) |
| su | a subscript for one of the production activities (45 branches of <br> activity) <br> the same as $s$ (used for exposition purposes) |
| Ss | a subscript for year $t$ |

