Doctoral Thesis
Industrial Electronics and Telecommunications Engineering

# Performance enhancement in the design of amplifier and amplifier-less circuits in modern CMOS technologies 



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\begin{array}{ll}
\text { Author: } & \text { Elena Cabrera Bernal } \\
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\end{array}
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Electronic Engineering Department Higher Technical School of Engineering University of Seville

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Author:<br>Elena Cabrera Bernal

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Antonio Jesús Torralba Silgado
Clara Isabel Luján Martínez

Electronic Engineering Department<br>Higher Technical School of Engineering<br>University of Seville

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## Autor: Elena Cabrera Bernal

## Tutores: Antonio Jesús Torralba Silgado <br> Clara Isabel Luján Martínez

El tribunal nombrado para juzgar el Proyecto arriba indicado, compuesto por los siguientes miembros:

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A mi familia.

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## Abstract

In the context of nowadays CMOS technology downscaling and the increasing demand of high performance electronics by industry and consumers, analog design has become a major challenge.

On the one hand, beyond others, amplifiers have traditionally been a key cell for many analog systems whose overall performance strongly depends on those of the amplifier. Consequently, still today, achieving high performance amplifiers is essential.

On the other hand, due to the increasing difficulty in achieving high performance amplifiers in downscaled modern technologies, a different research line that replaces the amplifier by other more easily achievable cells appears: the so called amplifier-less techniques.

This thesis explores and contributes to both philosophies. Specifically, a lowvoltage differential input pair is proposed, with which three multistage amplifiers in the state of art are designed, analysed and tested. Moreover, a structure for the implementation of differential switched capacitor circuits, specially suitable for comparator-based circuits, that features lower distortion and less noise than the classical differential structures is proposed, an, as a proof of concept, implemented in a $\Delta \Sigma$ modulator.

## 1 Introduction

"Integrated circuits will lead to such wonders as home computers - or at least terminals connected to a central computer - automatic controls for automobiles, and personal portable communications equipment."
-G.E. Moore, 1965-

### 1.1 Motivation.

During the last decades, humanity has experimented the greatest technological revolution since the Industrial Revolution of the $19^{\text {th }}$ century. In fact, the technological changes have been so fast that great differences exist between today's lifestyle and the one just few decades ago.

This technological revolution goes abreast CMOS technology development as, since the idea of manufacturing several transistors on a single substrate was conceived, the number of transistors integrated in the same area has increased following Moore's Law [1], thus reducing the associated manufacturing cost and making electronics accessible to everyone. As a consequence of the popularization of electronics, the demand of high performance hand-helded battery powered devices has grown enormously and, hence, high performance electronics are nowadays required in any field.

Furthermore, CMOS technology scaling also entails the reduction of the supply voltages in order to ensure circuit reliability and lifetime. However, in modern submicrometric technologies, the reduction of the transistor size and the power consumption budget implies a serious degradation of transistors' performance and, therefore, the design of high performance analog circuits becomes more challenging [2],[3].

In this context, analog circuit design is going through a new paradigm, where high performances must be achieved either by new design techniques or by revisiting and adapting the traditional designs to the new technological challenges. Both design trends have been explored throughout this thesis.

### 1.2 Research Goals.

One of the most important blocks in traditional design is the amplifier. Achieving high gain and, in general, high performance in amplifiers has become more difficult to achieve, as in modern technologies intrinsic device gains and supply voltages have decreased. As a consequence, two different design philosophies have arisen:

- Amplifiers designed with new techniques able to provide the required performances.
- Alternative design techniques that eliminate the need of amplifiers.

The aim of this thesis is to explore and contribute to both approaches.

### 1.3 Contributions.

As results of the performed research, the following contributions to the design of amplifier and amplifier-less circuits in modern CMOS technologies are presented, for both philosophies:

- Amplifiers designed with new techniques able to provide the required performances.
- A Low-Voltage Bulk-Driven Three-Stage Class-AB Operational Transconductance Amplifier.
- A Low-Voltage Bulk-Driven Three-Stage Class-AB Operational Transconductance Amplifier with Bulk-Driven Slew-Rate Boosting.
- A Low-Voltage Bulk-Driven Four-Stage Class-AB Operational Transconductance Amplifier with Bulk-Driven Slew-Rate Boosting.
- Alternative design techniques that eliminate the need of amplifiers.
- A new Differential structure for switched capacitor circuits, specially suitable for comparator-based switched capacitor circuits.


### 1.4 Thesis Organization.

This thesis is organized in four chapters as follows: after this first introductory chapter, on chapter 2, the first line of this thesis is explored. After a brief revision of low voltage amplifier techniques, three low-voltage bulk-driven multistage OTAs are presented and analysed. On chapter 3 the second line is explored, starting with
a review of the main amplifier-less techniques and then presenting a new technique for differential switched capacitor circuits. The last chapter summarizes the conclusions of this research and identifies the future work that can be derived from it.

## 2. Low-Voltage Operational Transconductance Amplifiers

One of the most important blocks in analog microelectronics, is undoubtedly, the operational amplifier (OpAmp). It is used in a wide range of applications such as voltage regulation, filtering or analog to digital conversion among others, what makes it one of the most critical cell in any analog or mixed-signal system.

OpAmps are usually composed by a differential transconductance stage, one or more high-gain stages, a compensation network and an output buffer, that allows to drive low-resistance loads. OpAmps that are not intended to drive low resistance loads are usually called Operational Transconductance Amplifier (OTA) [4].

In this chapter, the first line of this thesis is explored: the classical OTA cell is revisited in order to achieve competitive performances at extremely low voltage solution with the aim of making it suitable for modern technologies. For that purpose, three multistage low voltage bulk-driven OTAs are presented.

### 2.1. Low Voltage Amplifier Design Techniques.

On the one hand, low power is one of the most important areas in nowadays electronics. The huge consumer demand of portable devices with great autonomy makes low power a key feature for product competitiveness. Therefore, the interest in low voltage has significantly increased due to the limitation in power consumption. On the other hand, in modern submicrometric technologies the maximum allowed voltage supply has decreased more abruptly than the threshold voltage, $\mathrm{V}_{\text {th, }}$ dramatically reducing the available voltage swing in classical OTA topologies. Nevertheless, achieving high enough gains has become more challenging as transistor's output resistance is reduced and, with the decrease of biasing voltages, the effective transconductance has also decreased [2]. Moreover, classical techniques such as cascoding are no longer appropriate for low voltage design.

Consequently, low voltage design techniques are lately receiving plenty of interest. An overview of the most important ones is presented below.

### 2.1.1. Threshold lowering.

As the main problem to achieve an appropriate signal swing in modern technologies is due to the high $V_{\text {th }}$ values altogether with the reduced supply voltage, the more straightforward idea to implement a low voltage design is by reducing it. In some technologies, there are special transistors that perform low $\mathrm{V}_{\text {th }}$ o even zero $V_{\text {th, }}$ but this usually implies higher costs and/or the use of special technologies.

Still, there is another option: in standard devices the $V_{\text {th }}$ values can be reduced using the bulk [5]-[10]. The threshold voltage is given by

$$
\begin{equation*}
V_{t h}=V_{t h 0}+\gamma\left(\sqrt{\left|2 \phi_{F}-V_{B S}\right|}-\sqrt{\left|2 \phi_{F}\right|}\right) \tag{2-1}
\end{equation*}
$$

where, $V_{t h 0}$ is the zero-bias threshold voltage, $\gamma$ is the bulk effect factor and $\phi_{\mathrm{F}}$ is the Fermi potential.

This technique can only be used in p-type MOS transistors in standard CMOS technologies.

### 2.1.2. Subthreshold.

Biasing transistors in the subthreshold region is an alternative way of increasing the voltage swing in a low voltage design [11]-[13]. Under these biasing conditions the gate-source voltage, $\mathrm{V}_{\mathrm{gs}}$, is slightly lower that $\mathrm{V}_{\text {th }}$ and the drain source voltage, $\mathrm{V}_{\mathrm{ds}}$, only needs to be around one hundred millivolts to be in saturation [14], thus the voltage headroom is increased compared to strong inversion operation.

Transistors in the subthreshold region are usually biased with small currents,
what is advantageous in a low power design context. However, low biasing currents entails less slew rate and bandwidth.

That is why this design technique is very common when low power consumption is required and speed is not a concern, for instance in biomedical applications [15].

### 2.1.3. Non-Tailed Pair.

The classical single-ended-OTA differential input stage is depicted in Figure 1 (a). It is well-known that in this structure, transistor Mx implements a current source that sets the bias current through the input pair transistors, $\mathrm{M}_{1}$ and $\mathrm{M}_{2}$. However, Mx consumes one $\mathrm{V}_{\mathrm{ds} s \text { sat }}{ }^{1}$ of the available voltage headroom. Hence, getting rid of it will increment the voltage swing, making the structure suitable for low voltage design.

In Figure 1 (b) the non-tailed version of the classical input stage is depicted. Removing the tail current, however, makes this stage pseudo-differential and with a severe deterioration of common-mode rejection ratio, needing additional techniques to achieve reasonable rejection [16]. A fully-differential version, with better common-mode rejection ratio can be achieved by the non-tailed input stage shown in Figure 1 (c) [10]. Nevertheless, both input stages of Figure 1 (b) and Figure 1 (c) need additional methods to control de biasing current through the input pair should be added as the lack of the tail current makes them extremely dependent on temperature and process variations [7]-[10], [17], [18].


Figure 1: (a) Differential input stage of a classical OTA (b) Non-tailed version of the classical input stage (c) Non-tailed fully differential input stage.

### 2.1.4. Floating Gate Transistors.

Floating Gate (FG) transistors were first proposed in [19] for the design of a low voltage differential input pair. The operation of FG transistors consist on a

[^0]weighted capacitive coupling at the gate of a conventional MOS transistor as shown in Figure 2.


Figure 2: Floating Gate transistor.
Capacitor values are usually chosen to ensure that $C_{2} \gg C_{1}$ and, given that

$$
\begin{equation*}
v_{G}=V_{b i a s} \frac{C_{2}}{C_{1}+C_{2}}+v_{1} \frac{C_{1}}{C_{1}+C_{2}} \tag{2-2}
\end{equation*}
$$

the transistor can be properly biased through $C_{2}$ and $V_{\text {bias }}$ while $v_{1}$ drives the signal, that is attenuated at the gate of the transistor, ensuring a wide input range [19], [20].

The main disadvantage of this technique is the reduction of the input stage transconductance and, thus, the total gain and bandwidth. Moreover, $C_{2}$ implementation may increase the consumed area. In deeply scaled technologies, the gate leakage current increases, jeopardizing the FG transistor behaviour.

### 2.1.5. Quasi-Floating Gate Transistors.

Similarly to FG transistors, in Quasi-Floating Gate (QFG) transistors [21], the input signal in capacitively coupled to a conventional MOS transistor, but instead of biasing the gate by a large capacitor, it is weakly connected to $V_{\text {bias }}$ through a large resistor, Rlarge, as shown in Figure 3.


Figure 3: Quasi-Floating Gate transistor.
The gate voltage, $v_{G}$ can be calculated as,

$$
\begin{equation*}
v_{G}=V_{\text {bias }} \frac{1}{1+s R_{\text {large }} C_{1}}+v_{1} \frac{s R_{\text {large }} C_{1}}{1+s R_{\text {large }} C_{1}} \tag{2-3}
\end{equation*}
$$

Thus, for $s=0$ the gate is biased to the $V_{\text {bias }}$ voltage, while the input signal $v_{1}$ will
be high pass filtered. However, as Rarge should be large enough, the cut off frequency of the filter should be placed at frequencies lower than the minimum operating frequency of the circuit.

QFG transistors does not suffer from the transconductance reduction that affects FG transistors and, in practice, Rlarge can be implemented using transistors in cut off region (pseudoresistors) reducing the FG area consumption. However, experimental results show that they suffer slow large signal dynamics when the circuit is turned on. Those dynamics are not usually well modelled in computer aided design (CAD) software, so special attention must be paid when performing simulations [22]. In modern technologies passive resistors with relatively large values are feasible to integrate, so that, if the operating frequency is high enough, there is no need to use pseudoresistors.

### 2.1.6. Complementary Input Pair.

With the aim of increasing the input voltage swing in headroom-limited designs, two complementary pairs can be used as OTA input stage [23]-[26] as shown in Figure 4 [23].


Figure 4: Complementary input pair.
The main idea is to have at least one pair operating over the complete input voltage range. Hence, when the input is too high for the p-type pair, the n-type is going to be active, and vice versa.

Despite complementary pairs indeed achieve rail-to-rail behaviour, the transconductance, as well as the slew rate, suffer important variations across the input signal swing, as the circuit passes through three different "states": only ptype pair active, both pairs active, only n-type pair active.

### 2.1.7. Level Shifting.

Similarly as in the complementary input pair, using two input pairs of the same, $p$ or $n$ type plus level shifters, can ensure rail-to-rail operation [27]. The idea is, again, turning on one of the pairs when the other turns off.


Figure 5: Double input pair with level shifters.
Level shifting presents the same disadvantages of transconductance and slew rate input dependence. It needs additional techniques to stabilize those parameters and additional circuitry to implement the level shifters.

### 2.1.8. Bulk Driven.

Bulk driven circuits use the bulk transconductance, $\mathrm{g}_{\mathrm{mb}}$, instead of the gate transconductance, $\mathrm{g}_{\mathrm{m}}$. The main advantage of driving the input though the bulk is that it has no threshold voltage associated and, as a result, the Vth limitation is avoided, making it specially suitable for low voltage designs.

Figure 6 (a) shows the regular gate driven transistor where the input is applied though the gate terminal and the bulk terminal is set to a constant bias voltage. In Figure $6(\mathrm{~b})$ a bulk driven transistor is depicted, where the input is applied through the bulk and the gate terminal is connected to a bias voltage that properly bias the transistor.

(a)

(b)

Figure 6: (a) Gate driven and (b) bulk driven PMOS transistors.
As this technique requires the bulk terminal to be accessible, in standard $n$-well technologies, only $p$-channel transistors can be bulk driven. The main disadvantage is the fact that $\mathrm{g}_{\mathrm{mb}}$ is significantly smaller than $\mathrm{g}_{\mathrm{m}}$ and, in amplifier design, this leads to poor DC gain and gain-bandwidth performances with larger noise and offset.

Specifically, if strong inversion is assumed, then the drain current is given by $I_{D}=\frac{\beta}{2}\left(V_{S G}-\left|V_{t h}\right|\right)^{2}$. If the threshold voltage is substituted by $V_{t h}=V_{t h 0}+$ $\gamma\left(\sqrt{\left|2 \phi_{F}-V_{B S}\right|}-\sqrt{\left|2 \phi_{F}\right|}\right)$, then [28],

$$
\begin{equation*}
g_{m b} \equiv \frac{\partial I_{D}}{\partial V_{S B}}=\frac{|\gamma|}{2 \sqrt{2\left|\phi_{F}\right|+V_{B S}}} \sqrt{2 \beta I_{D}}=\frac{|\gamma|}{2 \sqrt{2\left|\phi_{F}\right|+V_{B S}}} g_{m}=\eta g_{m} \tag{2-4}
\end{equation*}
$$

Depending on the technology $0.1<\eta<0.4$. The rest of the parameters have their usual meanings, being $\gamma$ the body effect parameter, $\phi_{F}$ the Fermi potential and $\beta=\mu C^{\prime}{ }_{o x}\left(\frac{W}{L}\right)$.

### 2.2. State of Art of Sub-1V Operational Transconductance Amplifiers.

In this section, the State of Art of Sub-1V OTAs is presented. First, previous works found on literature are briefly discussed and summarized, to finish with a comparison of their performances.

In order to discuss the different approaches found on literature, a chronological order is going to be followed here. In 2001 Lehmann et al. [5], propose a gate-driven folded cascade OTA implemented by a current driven bulk technique. In this proposal, the threshold voltage of the input pair is lowered by driving the bulk with a current instead of a voltage avoiding the possibility of forward biasing the bulk-source diode by maintaining the bulk current controlled under a certain value. Results demonstrate that the solution is able to work under 1 V supply in a 3.3 V technology with proper small signal performances but with poor SR.

In [29], Stockstad et al. propose a weak inversion OTA whose input pair is bulkdriven, but the input is applied through depletion-mode transistors used as buffers to minimize bulk currents. They achieve 70 dB gain and rail-to-rail behaviour at the input and the output under a 0.9 V supply in a $2.5 \mu \mathrm{~m}$ technology, with a reduced power consumption. However, the unity gain bandwidth is only 5.6 kHz .

Yao et al. propose, in [30], a single-stage gate-driven fully differential OTA, based on a current mirror amplifier with gain enhancement. Although it has very good small signal behaviour with a low power consumption, its slew rate is poor.

In [6] Chatterjee et al. propose two 0.5 V fully-differential OTA, both biased in moderate inversion. The first approach is bulk-driven while the second one is driven by the gate and implements threshold lowering through the bulk of $n$-type transistors, thus requiring triple-well devices. The proposed OTAs achieve good performances, but extremely limited input common-mode range.

In [31] Ferreira et al. propose an improved version of the traditional two-stage Miller OTA, operating at weak inversion and combining bulk-driven input and level-shifters to provide rail-to-rail operation. It effectively achieves low voltage $(0.6 \mathrm{~V}$ in a technology of 2.5 V ) and low power, but speed and slew rate are not particularly good.

In [32], Zuo et al. propose a two-stage bulk-driven folded-cascode OTA with transconductance enhancement able to operate under 1 V in a technology whose nominal supply voltage is 3.3 V . Although it achieves good small signal performances, the large signal behaviour is rather poor

Ferreira et al. presents, in [33], a two-stage bulk-driven folded-cascode OTA in weak inversion, able to operate under 0.25 V and very low-power consumption. It achieves very good performances, considering the extremely low supply and power consumption, by enhancing the transconductance and, also, the output resistance of transistors at the expense of area consumption.

In [16], a three-stage bulk-driven OTA with non-tailed input pair operating in subthreshold is presented by Abdelfattah et al.. The OTA is able to operate even under 0.35 V in a technology with a nominal supply voltage of 1.2 V . They show good measured performances but under a quite small loading capacitance.

Tang et al. propose in [34] a rail-to-rail bulk-driven two-stage OTA that operates under 0.9 V in a technology with a nominal supply of 1.8 V . It also implements a transconductance stabilization technique. Although it achieves good speed and slew rate, it consumes too much current.

Finally, in [7] Grasso et al. propose a gate-driven two-stage non-tailed OTA with threshold lowering that operates under 0.9 V in a 3.3 V technology, achieving a good common-mode range but limited slew rate.

Table 1 summarizes the main performance of the works that have been discussed here.

| Year, Ref. | Tech <br> [ $\mu \mathrm{m}$ ] | Supply <br> [V] |  | $\begin{gathered} C_{L} \\ {[\mathrm{pF}]} \end{gathered}$ | $\begin{gathered} \hline \text { DC } \\ \text { Gain } \\ \text { [dB] } \\ \hline \end{gathered}$ | $\begin{aligned} & \text { UGBW } \\ & \text { [MHz] } \end{aligned}$ | $\begin{gathered} \text { PM } \\ {\left[{ }^{\circ}\right]} \end{gathered}$ | Average SR <br> [ $\mathrm{V} / \mu \mathrm{s}$ ] | CMRR <br> [dB] |  | $\begin{gathered} \hline \mathrm{FoM}_{\mathrm{L}} \\ {[\mathrm{~V} \cdot \mathrm{pF} /} \\ (\mu \mathrm{s} \cdot \mathrm{~mW})] \\ \hline \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} 2001 \\ {[5]} \\ \hline \end{gathered}$ | 0.5 | 1 | 40 | 20 | 69 | 2 | 57 | 0.5 | - | 1000 | 250 |
| $\begin{aligned} & 2002 \\ & {[29]} \end{aligned}$ | 2.5 | 0.9 | 0.5 | 12 | 70 | 0.0056 | 62 | - | 26 | 149 | - |
| $\begin{aligned} & 2003 \\ & {[30]} \end{aligned}$ | 0.25 | 0.8 | 10 | 18 | 50 | 1.2 | 60 | 0.2 | - | 2700 | 450 |
| $\begin{gathered} 2005 \\ {[6]} \end{gathered}$ | 0.18 | 0.5 | 220 | 20 | 52 | 2.5 | - | 2.89 | 78 | 455 | 525 |
|  | 0.18 | 0.5 | 150 | 20 | 62 | 10 | - | 2.0 | 74 | 2666 | 533 |
| $\begin{gathered} 2007 \\ {[31]} \end{gathered}$ | 0.35 | 0.6 | 0.916 | 15 | 69 | 0.011 | 65 | 0.014 | 74 | 300 | 382 |
| $\begin{aligned} & 2013 \\ & \text { [32] } \end{aligned}$ | 0.35 | 1 | 197 | 15 | 88 | 11.67 | 66 | 1.95 | 40 | 889 | 148 |
| $\begin{aligned} & 2014 \\ & {[33]} \\ & \hline \end{aligned}$ | 0.13 | 0.25 | 0.072 | 15 | 60 | 0.002 | 52 | 0.0007 | - | 1667 | 583 |
| $\begin{gathered} 2015 \\ {[16]} \end{gathered}$ | 0.065 | 0.5 | 366 | 3 | 46 | 38 | 57 | 43 | 35 | 623 | 705 |
|  | 0.065 | 0.35 | 49 | 3 | 43 | 3.6 | 56 | 5.6 | 46 | 630 | 980 |
| $\begin{aligned} & 2015 \\ & {[34]} \end{aligned}$ | 0.18 | 0.9 | 290 | 17 | 76 | 7.11 | 72 | 2.98 | 55 | 463 | 194 |
| $\begin{gathered} 2017 \\ {[7]} \end{gathered}$ | 0.35 | 0.9 | 27 | 10 | 65 | 1 | 60 | 0.25 | 45 | 411 | 102 |

Table 1: Performance comparison of Sub-1V OTAs.

The two traditional Figures of Merit (FoM) [35]-[37] shown in equation (2-5) have been evaluated and included in Table 1.

$$
\begin{gather*}
F o M_{S}=\frac{U G B W \cdot C_{L}}{\text { Power }} \\
F o M_{L}=\frac{S R \cdot C_{L}}{\text { Power }} \tag{2-5}
\end{gather*}
$$

FoMs and FoMl allow a comparison of small signal and large signal performance, respectively. In both cases higher values mean better performances: in FOMs (where subscript $S$ stands for "small signal") higher unity-gain bandwidth, UGBW, and load capacitance, $\mathrm{C}_{\mathrm{L}}$, at low power consumption is preferred, whereas in FOML (where subscript $L$ stands for "large signal") higher slew rate, SR , higher, $\mathrm{C}_{\mathrm{L}}$ and low power consumption is preferred.

Figure 7 graphically shows the FoMs of each publication discussed above. It can be observed that the amplifiers with better FoMl [16] present poor FoMs and viceversa [6], [30].



Figure 7: FOMs and FOMl Vs Year of Publication of Sub-1V OTAs.

### 2.3. Contributions.

Taking advantage of more than one of the described low-voltage techniques is a common strategy [6], [7], [16], [24], [29], [31], [33], [38], [39].

For the OTAs proposed in this thesis, with the aim of achieving good small and large signal performances, a bulk-driven version of the non-tailed differential input pair of Figure 1 (c) is used as the first stage of all the three contributions, what allows extremely reduced biasing voltage and, as the quiescent current through the input pair is fixed by the gates while the input is driven through the bulk, no additional bias current control is required. This input stage is interesting, as it can implement either single-ended or fully-differential solutions as it is.

As a proof of concept, three single-ended OTA are proposed. In order to provide adequate DC gain, the first two proposed OTAs adopt three-stage architectures [13], [16] while the last one is a four-stage [40]. Class-AB outputs are chosen to enhance the large signal performances, and, additionally, for the last two contributions, the classical Class- AB output is improved taking once again advantage of the bulk terminal. The three proposed OTAs were fabricated in a standard 180 nm CMOS technology in order to validate their performances.

### 2.3.1. Non-Tailed Bulk-Driven Differential Input Stage.

The Non-Tailed Bulk-Driven Differential pair, used as the input stage for the three proposed OTAs, is the bulk-driven version of the input stage proposed on [8] and it is depicted in Figure 8. It is composed by transistors $\mathrm{M}_{1}$ and $\mathrm{M}_{2}$, whose quiescent currents are accurately set by transistor $\mathrm{Mr}_{\mathrm{R}}$ whose body is tied to the virtual ground (i.e., $(V D D+V S S) / 2)$. Hence, $\mathrm{M}_{\mathrm{R}}-\mathrm{M}_{1}$ and $\mathrm{M}_{\mathrm{R}}-\mathrm{M}_{2}$ form two accurate current mirrors, provided that also the bulk of $\mathrm{M}_{1}-\mathrm{M}_{2}$ is connected to the analog ground. The active load of the first stage is implemented by transistors $\mathrm{M}_{3}-\mathrm{M}_{4}$ and two resistors, $R$. Due to the fact that no DC current flows through resistors, the drains and gates of $\mathrm{M}_{3}-\mathrm{M}_{4}$ are at the same potential. This stage is specially suitable for low voltage design, as the minimum supply voltage (VDD-VSS) can be as low as $V_{D S 1,2}+V_{G S 3,4 .}$. Moreover, resistors $R$ accurately set the output DC common-mode voltage, what would not happen in the bulk-driven version of the classical nontailed pair of Figure 1 (b).

The transistors and biasing values used for the three implementations are summarized in Table 2.


Figure 8: Non-Tailed Bulk-Driven Differential Pair.

| Device | Value | Device | Value |
| :---: | :---: | :---: | :---: |
| $\boldsymbol{M}_{\boldsymbol{R}}, \boldsymbol{M}_{1}, \boldsymbol{M}_{\mathbf{2}}$ | $12 \mu \mathrm{~m} / 540 \mathrm{~nm}$ | $\boldsymbol{I}_{\boldsymbol{B}}$ | $4 \mu \mathrm{~A}$ |
| $\boldsymbol{M}_{3}, \boldsymbol{M}_{\mathbf{4}}$ | $2 \mu \mathrm{~m} / 540 \mathrm{~nm}$ | $\boldsymbol{R}$ | $250 \mathrm{k} \Omega$ |
|  |  | VDD-VSS | 0.7 V |

Table 2: Transistors dimensions and device values of the Non-Tailed Bulk-Driven Differential Pair.

As the three proposed OTAs share exactly the same implementation of the first stage, they also share the performances directly related to the first stage behaviour. Specifically: differential gain of the first stage, common mode rejection ratio (CMRR), input common mode range (ICMR) and noise.

### 2.3.1.1. Differential Gain.

In the input stage of Figure 8, the use of resistors $R$ in the active load enables fully differential operation of an otherwise pseudo-differential pair $\mathrm{M}_{1}-\mathrm{M}_{2}$. In order to illustrate this fact, a single-ended small-signal voltage, $v_{d}$, is applied at one input (e.g., the bulk of $\mathrm{M}_{1}$ ), while grounding the second input (bulk of $\mathrm{M}_{2}$ ).


Figure 9: Circuit for differential behaviour demonstration.

As depicted in Figure 9, voltage $v_{d}$ is converted into a current, $g_{m b 1 v_{d}}$, one half of which will flow through the resistor series and the other half through transistor $\mathrm{M}_{3}$ because $M_{3}$ and $M_{4}$ have the same gate-source voltage, $v_{8 s 3,4,}$ and the same transconductance, $g_{m 3,4}$, and must, consequently, carry the same current. Figure 9 shows then that a differential output voltage, $v_{01}-v_{02}$, is generated. The expression of the individual output voltages can be approximated by

$$
\begin{align*}
& v_{o 1}=v_{g s 3,4}-g_{m b 1} R \frac{v_{d}}{2} \\
& v_{o 2}=v_{g s 3,4}+g_{m b 1} R \frac{v_{d}}{2} \tag{2-6}
\end{align*}
$$

where the output resistances of the transistors have been neglected ${ }^{2}$. Given that $g_{m b 1,2} \frac{v_{d}}{2}=g_{m 3} v_{g s 3,4}$, then:

$$
\begin{align*}
& v_{o 1}=g_{m b 1,2}\left(\frac{1}{g_{m 3,4}}-R\right) \frac{v_{d}}{2} \\
& v_{o 2}=g_{m b 1,2}\left(\frac{1}{g_{m 3,4}}+R\right) \frac{v_{d}}{2} \tag{2-7}
\end{align*}
$$

Assuming that $g_{m 3,4} R \gg 1$, then (2-6) yields $v_{o 1}=-v_{o 2}=g_{m b 1} R \frac{v_{d}}{2}$, demonstrating differential operation, since the application of $v_{d}$ from only one input terminal produces a differential output, as opposed to a pseudo-differential topology. For the symmetry of the circuit, the same result holds also if the input signal is applied to the bulk of $\mathrm{M}_{2}$.

As a conclusion, the (single ended) gain of this first stage, can be approximated by ${ }^{3}$

$$
\begin{equation*}
A_{d}=\frac{v_{o 2}}{v_{d}} \approx \frac{g_{m b 1,2} R}{2} \tag{2-8}
\end{equation*}
$$

### 2.3.1.2 Common Mode Rejection Ratio.

Under a common mode excitation, as no current flows through resistors $R$, the drain and source terminal of $\mathrm{M}_{3}$ and $\mathrm{M}_{4}$ are set to the same potential. Referring to Figure 10, and taking in to account that $g_{m b 1}=g_{m b 2}=g_{m b 1,2}$ and $g_{m 3}=g_{m 4}=g_{m 3,4}$, this absence of current thought the resistors implies that $g_{m b 1,2 V_{c m}}$ must equal $g_{m 3,4 v_{g s 3,4}}$. Therefore, the common mode gain is

[^1]\[

$$
\begin{equation*}
A_{c m}=\frac{v_{o 2}}{v_{c m}}=-\frac{g_{m b 1,2}}{g_{m 3,4}} \tag{2-9}
\end{equation*}
$$

\]



Figure 10: Circuit for differential input stage CMRR analysis.
This outcome can be easily understood by considering that if no current flows through the resistors then $\mathrm{M}_{3}$ and $\mathrm{M}_{4}$ operate as they are connected in diode and offer an equivalent resistance equal to $1 / g_{m 3,4.4}$.

Hence, the (single ended) CMRR, defined as $\left|A_{d} / A_{c m}\right|$, is given by:

$$
\begin{equation*}
C M R R=\left|\frac{A_{d}}{A_{c m}}\right|=\frac{1}{2} \frac{g_{m b 1,2} R}{\frac{g_{m b 1,2}}{g_{m 3,4}}}=\frac{1}{2} g_{m 3,4} R \tag{2-10}
\end{equation*}
$$

From (6) we see that $R \gg 1 / g_{m 3,4}$ must be chosen to obtain adequate $C M R R$ values. In the classical implementation of Figure 1(b) the CMRR value is equal to 1, so in this terms, the proposed structure presents a valuable improvement.

### 2.3.1.3. Input Common Mode Range.

The input common mode range (ICMR) of the proposed differential pair is, in practice, limited by the maximum allowable input current.

Due to its bulk driven input, the input current is expected to be relatively high if compared to a gate driven input stage. As $V_{B S}$ changes from VDD to VSS this current is going to increase as the bulk-source $p n$ junction becomes more forward biased [28].

Hence, the maximum allowable input current has been chosen to be 4 nA at $27^{\circ} \mathrm{C}$. As the quiescent current through the input transistors is set to $4 \mu \mathrm{~A}$, the input current is thus 1000 times smaller and, thus, negligible. By simulation, this $V_{B S}=V_{B S \text { max }}=550 \mathrm{mV}$, what means an ICMR of 550 mV , from 150 mV to 700 mV .

### 2.3.1.4. Noise.

Noise performance of bulk driven circuits is also worsened if compared to its gate
driven counterpart [41]. For the proposed stage of Figure 8, considering only white noise for simplicity, the equivalent input-referred noise voltage power spectral density (PSD) of the proposed amplifier can be approximated as

$$
\begin{equation*}
S_{V, i n} \approx 2 S_{V 1,2}\left(\frac{g_{m 1,2}}{g_{m b 1,2}}\right)^{2}+2 S_{V 3,4}\left(\frac{g_{m 3,2}}{g_{m b 1,2}}\right)^{2}+S_{V R, i n} \tag{2-11}
\end{equation*}
$$

where $S_{V i}$ is the well-known gate-referred noise voltage Power Spectral Density (PSD) of transistor $M_{i}, S_{V R, i n}$ in the input-referred equivalent noise contribution of resistors $R, k$ is the Boltzmann's constant and $T$ is the absolute temperature.

For the calculation of $S_{V R, i n}$, the simplified small signal model illustrated in Figure 11 is used to find the voltage gain between $v_{n R}$ and the outputs of the first stage, $v_{01}$ and $v_{02}$.


Figure 11: Schematic for resistors $R$ noise analysis.
Then, it can be seen that

$$
\begin{gather*}
i_{R}=g_{m 3,4} v_{g s 3,4}+\frac{v_{o 2}}{R_{o 1}}=-g_{m 3,4} v_{g s 3,4}-\frac{v_{o 1}}{R_{o 1}} \\
v_{o 1}=v_{g s 3,4}+R i_{R}  \tag{2-12}\\
v_{o 1}=v_{g s 3,4}-R i_{R}+v_{n R}
\end{gather*}
$$

where $R_{o 1}$ is the output resistance of the stage $R_{01}=r_{d s 3,4} / / r_{d s 1,2}$.
Then, the transfer functions can be calculated as

$$
\begin{align*}
& \frac{v_{o 1}}{v_{n R}}=\frac{g_{m 3,4} R-1}{2\left(1+g_{m 3,4} R_{o 1}\right)\left(1+\frac{R}{R_{o 1}}\right)} \approx \frac{1}{2} \cdot \frac{R}{R+R_{o 1}} \\
& \frac{v_{o 2}}{v_{n R}}=\frac{1+g_{m 3,4}\left(R+2 R_{o 1}\right)}{2\left(1+g_{m 3,4} R_{o 1}\right)\left(1+\frac{R}{R_{o 1}}\right)} \approx \frac{1}{2} \cdot \frac{R+2 R_{o 1}}{R+R_{o 1}} \tag{2-13}
\end{align*}
$$

where the approximations hold for $g_{m 3,4} R \gg 1$ and $g_{m 3,4} R_{01} \gg 1$.
Due to the symmetry of the circuit, $v_{01} / v_{n R}$ represents also the transfer function from the noise source of the left-side resistor to $v_{02}$. This noise contribution of the left-side resistor is lower than that of the right-side resistor as can be seen by comparing both equations of (2-13) which imply the product of 0.5 by a quantity lower than the unity and greater than the unity, respectively. Finally, Svr,in is
evaluated by considering that the gain from the inverting input to the output of the first stage is $A_{d}=-\frac{g_{m b 1,2}\left(R_{01} / / R\right)}{2}$. Therefore we get:

$$
\begin{equation*}
S_{V R, i n}=S_{V R} \frac{1}{4}\left[\left(\frac{R}{R+R_{o 1}}\right)^{2}+\left(\frac{R+2 R_{o 1}}{R+R_{o 1}}\right)^{2}\right]\left(\frac{2}{g_{m b 1,2}\left(R_{o 1} / / R\right)}\right)^{2} \tag{2-14}
\end{equation*}
$$

Being $S_{v R}=4 k T R$ then:

$$
\begin{equation*}
S_{V R, i n}=4 k T R\left(\frac{1}{g_{m b 1,2} R_{o 1}}\right)^{2}\left[1+\left(1+\frac{2 R_{o 1}}{R}\right)^{2}\right] \tag{2-15}
\end{equation*}
$$

Therefore, according to (2-11)

$$
\begin{align*}
& S_{V, i n}=2 S_{V 1,2}\left(\frac{g_{m 1,2}}{g_{m b 1,2}}\right)^{2}+2 S_{V 3,4}\left(\frac{g_{m 3,4}}{g_{m b 1,2}}\right)^{2}+S_{V R, i n} \\
&=2 \frac{2}{3} 4 k T \frac{1}{g_{m b 1,2}}\left(\frac{g_{m 1,2}}{g_{m b 1,2}}+\frac{g_{m 3,4}}{g_{m b 1,2}}\right)  \tag{2-16}\\
&+4 k T R\left(\frac{1}{g_{m b 1,2} R_{o 1}}\right)^{2}\left[1+\left(1+\frac{2 R_{o 1}}{R}\right)^{2}\right]
\end{align*}
$$

where the well know $S_{V i}=\frac{2}{3} 4 k T \frac{1}{g_{m i}}$ has been substituted. The noise generated in the resistors can be neglected if $\left(g_{m 1,2}+g_{m 3,4}\right) R_{o 1} \gg \frac{3}{4} \frac{R}{R_{01}}\left[1+\left(1+\frac{2 R_{o 1}}{R}\right)^{2}\right]$ condition that is usually met. Thus,

$$
\begin{equation*}
S_{V, i n} \approx \frac{16}{3} k T \frac{1}{g_{m b 1,2}} \frac{g_{m 1,2}+g_{m 3,4}}{g_{m b 1,2}} \tag{2-17}
\end{equation*}
$$

Finally, if $g_{m 3,4} \ll g_{m 1,2}$ is selected, the noise of $\mathrm{M}_{3,4}$ could be neglected too, yielding to an equivalent input-referred noise voltage PSD of

$$
\begin{equation*}
S_{V, i n} \approx \frac{16}{3} k T \frac{1}{g_{m b 1,2}} \frac{1}{\eta}=\frac{16}{3} k T \frac{1}{g_{m 1,2}} \frac{1}{\eta^{2}} \tag{2-18}
\end{equation*}
$$

where $\eta=g_{\mathrm{mb} 1,2} / \mathrm{g}_{\mathrm{m} 1,2}$ However, $g_{m 3,4} \ll g_{m 1,2}$ cannot be easily set since large $g_{m 3,4}$ values are needed from (2-10) to achieve sufficient CMRR without requiring excessively large $R$ values. When compared to the classical approach of Figure 1 (b) additional resistors $R$ add more noise.

Noise in multistage amplifiers is usually dominated by the first stage provided that this first stage has a voltage gain considerably larger than unity.

### 2.3.1.5. Large signal behaviour.

Due to its non-tailed structure, the proposed input stage large signal behaviour is not limited by the tail current and, in fact, can deliver and sink instantaneous currents larger than its nominal quiescent current, which is characteristic of Class$A B$ circuits.

In order to further explain this, let us assume a unity-gain voltage follower configuration, where a negative step is applied to the positive input as shown in Figure 12. When the positive input goes down, the $v_{g s}$ of transistor $\mathrm{M}_{4}$ increases so $\mathrm{M}_{4}$ can instantaneously sink higher currents than its nominal value.


Figure 12: Large Signal behavior. Negative Step.
The opposite happens when a positive step is applied: $v_{g s}$ of $\mathrm{M}_{4}$ decreases almost switching off $\mathrm{M}_{4}$, so $\mathrm{M}_{2}$ delivers currents directly from VDD that again are larger than its quiescent values.


Figure 13: Large Signal behavior. Positive Step.
This Class-AB behavior is an additional enhancement of the input stage when compared to the classical one shown on Figure 1 (b).

Due to the advantages of the proposed bulk-driven non-tailed input stage in terms of CMRR, DC common mode output and large signal behavior when compared to the classical non-tailed stage, it has been chosen as the input stage for the three OTAs proposed in this thesis. This input stage is particularly advantageous for the implementation of fully-differential solutions, anyway, single-ended OTAs has been implemented in this thesis as a proof of concept for the validation and test of its performances. Fully differential implementation is straightforward and part of the future work.

### 2.3.2. Low-Voltage Bulk-Driven Three-Stage Class-AB OTA.

Using the proposed input stage of Figure 8, together with Class-AB stages the complete OTA of Figure 14 is proposed with the aim of achieving both good large and small signal performances under low voltage supply. It is made up of three gain stages: the already explained differential input stage $\left(\mathrm{M}_{1}-\mathrm{M}_{4}\right)$, a second common-source stage $\left(\mathrm{M}_{5}-\mathrm{M}_{6}\right)$ and a third common-source stage $\left(\mathrm{M}_{7}-\mathrm{M}_{10}\right)$. The implemented transistors dimensions and device values for this design are summarized in Table 3.


Figure 14: Three-stage Class-AB OTA.

| Device | Value | Device | Value |
| :---: | :---: | :---: | :---: |
| $\boldsymbol{M}_{\boldsymbol{R},} \boldsymbol{M}_{\mathbf{1}}, \boldsymbol{M}_{\mathbf{2}}, \boldsymbol{M}_{\mathbf{1 0}}$ | $12 \mu \mathrm{~m} / 540 \mathrm{~nm}$ | $\boldsymbol{I}_{\boldsymbol{B}}$ | $4 \mu \mathrm{~A}$ |
| $\boldsymbol{M}_{\mathbf{3}}, \boldsymbol{M}_{4}, \boldsymbol{M}_{\boldsymbol{9}}$ | $2 \mu \mathrm{~m} / 540 \mathrm{~nm}$ | $\boldsymbol{C}_{\mathbf{C}}$ | 550 fF |
| $\boldsymbol{M}_{\mathbf{5}}, \boldsymbol{M}_{\mathbf{7}}$ | $5 \mu \mathrm{~m} / 540 \mathrm{~nm}$ | $\boldsymbol{C}_{\mathbf{C 2}}$ | 30 fF |
| $\boldsymbol{M}_{\mathbf{6}}, \boldsymbol{M}_{\mathbf{8}}$ | $30 \mu \mathrm{~m} / 540 \mathrm{~nm}$ | $\boldsymbol{R}$ | $250 \mathrm{k} \Omega$ |
| $\boldsymbol{C}_{\boldsymbol{L}}$ | 20 pF | VDD-VSS | 0.7 V |

Table 3: Transistors dimensions and device values of the Three-Stage Class-AB OTA.

Transistor Mr, whose bulk is tied to the virtual ground, as explained in the above section, sets the quiescent current of the differential pair ( $\mathrm{M}_{1}-\mathrm{M}_{2}$ ) and load ( $\mathrm{M}_{3}-\mathrm{M}_{4}$ ) of the first stage. At the same time, $\mathrm{Mr}_{\mathrm{r}}$ also sets the quiescent current of transistor $\mathrm{M}_{6}$ that acts as the load of the second stage. Due to the fact that no DC current flows through resistors $R$, the drains of $\mathrm{M}_{3}-\mathrm{M}_{4}$ are at the same potential of their gates and, consequently, the DC current of $\mathrm{M}_{5}$ is also accurately set by (pseudo) current-mirror ratios of $\mathrm{M}_{4}$ and $\mathrm{M}_{5}$

$$
\begin{equation*}
I_{D 5}=I_{D 4} \frac{\left(\frac{W}{L}\right)_{5}}{\left(\frac{W}{L}\right)_{4}} \tag{2-19}
\end{equation*}
$$

The matching between the DC currents of $\mathrm{M}_{5}$ and $\mathrm{M}_{6}$, causes the drain of $\mathrm{M}_{5}$ to be theoretically at the same potential of the drain of $M_{4}$, ultimately defining the current of $\mathrm{M}_{7}$, again through a mirror ratio

$$
\begin{equation*}
I_{D 7}=I_{D 4} \frac{\left(\frac{W}{L}\right)_{7}}{\left(\frac{W}{L}\right)_{4}} \tag{2-20}
\end{equation*}
$$

Note that current In8 is set through current mirror $\mathrm{M}_{8}-\mathrm{M}_{10}$ and pseudo current mirror $\mathrm{M}_{9}-\mathrm{M}_{4}$. Therefore, to theoretically nullify systematic offset, Ibs must be equal to ID7 leading to

$$
\begin{equation*}
\frac{\left(\frac{W}{L}\right)_{8}\left(\frac{W}{L}\right)_{9}}{\left(\frac{W}{L}\right)_{10}\left(\frac{W}{L}\right)_{4}}=\frac{\left(\frac{W}{L}\right)_{7}}{\left(\frac{W}{L}\right)_{4}} \tag{2-21}
\end{equation*}
$$

A final comment regards the Class-AB behaviour of the third stage. Both transistors $\mathrm{M}_{7}$ and $\mathrm{M}_{8}$ can deliver a maximum signal current that is not limited by any DC value. Indeed, $\mathrm{M}_{7}$ is in common source configuration, whereas the current in $\mathrm{M}_{8}$ increases when $V_{\text {in }}$ increases because $v_{G S 9}$ also increases.

### 2.3.2.1. Frequency compensation.

Frequency compensation of the differential (open loop) gain is obtained through Miller capacitors $C_{c 1}$ and $C_{c 2}$ and a current buffer [42] implemented by $\mathrm{M}_{3}-\mathrm{M}_{4}$, with a similar technique to that developed in [37] for a nested-Millercompensated OTA.

The simplified small signal model of the OTA of Figure 14 is depicted in Figure 15, where the parasitic capacitances have been neglected for simplicity and Roi represents the resistance of the output node of the $i^{\text {th }}$ stage. Values of transconductances and resistances for the proposed OTA are provided in Table 4: .


Figure 15: Small signal model of the Three-stage Class-AB OTA.

| Trans- <br> conductance | Value <br> $[\mu A / V]$ | Trans- <br> conductance | Value <br> $[\mu A / V]$ | Output resistance | Value <br> $[k \Omega]$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{g}_{m b 1,2}$ | 12 | $\boldsymbol{g}_{\boldsymbol{m} 7}$ | 150 | $R_{o 1}=r_{d s 1} / / r_{d s 3}$ | 1535 |
| $\boldsymbol{g}_{m 1,2}$ | 65 | $\boldsymbol{g}_{\boldsymbol{m} 8}$ | 150 | $R_{o 2}=r_{d 55} / / r_{d 56}$ | 214 |
| $\boldsymbol{g}_{\boldsymbol{m} 3,4}$ | 65 | $\boldsymbol{g}_{\boldsymbol{m} 9}$ | 60 | $R_{o 3}=r_{d s 5} / / r_{d s 8}$ | 224 |
| $\boldsymbol{g}_{\boldsymbol{m} 5}$ | 162 | $\boldsymbol{g}_{\boldsymbol{m} 10}$ | 60 | $R_{o x}=r_{d s 1} / /\left(1 / \boldsymbol{g}_{\boldsymbol{m} 10}\right)$ | 16 |
| $\boldsymbol{g}_{\boldsymbol{m b 6}}$ | 30 |  |  |  |  |

Table 4: Transconductances and output resistance values of the Three-Stage Class-AB OTA.

Solving the simplified small signal model circuit leads to the following open loop gain transfer function:

$$
\begin{equation*}
A(s) \approx A_{0} \frac{\left(1+\frac{s}{z_{1}}\right)}{\left(1+\frac{s}{p_{1}}\right)\left(a s^{2}+b s+1\right)} \tag{2-22}
\end{equation*}
$$

Assuming $g_{m i} R_{o i}, g_{m i} R \gg 1$, simple equations can be provided for the DC gain, $A_{0}$, zero, $z_{1}$, and dominant pole, $p_{1}$, as well as for the coefficients of the polynomial of the complex conjugate poles, $a, b$.

$$
\begin{gather*}
A_{0}=\frac{g_{m b 1} g_{m 5} g_{m 7} R R_{o 1} R_{o 2} R_{o 3}}{2\left(R+R_{o 1}\right)} \\
z_{1}=\frac{g_{m 5} g_{m 3}}{g_{m 5} C_{C 1}-g_{m 3} C_{C 2}} \\
p_{1}=\frac{2\left(R+R_{o 1}\right)}{g_{m 5} g_{m 7} C_{C 1} R R_{o 1} R_{o 2} R_{o 3}}  \tag{2-23}\\
a=\frac{C_{C 2} C_{L}\left(g_{m 3}+2 g_{m 5}\right)}{g_{m 3} g_{m 5} g_{m 7}} \\
b=\frac{C_{L}\left(C_{C 1}+g_{m 5} C_{C 2} R_{o 2}\right)}{g_{m 5} g_{m 7} C_{C 1} R_{o 2}}
\end{gather*}
$$

The damping coefficient of the pair of complex poles is given by

$$
\begin{equation*}
\xi=\frac{b}{2 \sqrt{a}}=\frac{C_{C 1}+C_{C 2} g_{m 5} R_{o 2}}{2 C_{C 1} R_{o 2}} \sqrt{\frac{C_{L} g_{m 3}}{g_{m 5} g_{m 7} C_{C 2}\left(2 g_{m 5}+g_{m 3}\right)}} \tag{2-24}
\end{equation*}
$$

Given $g_{m b 1,2}, C_{L}$ and $C_{c 1}$, one can derive from (2-24) a suitable value of $C_{C 2}$ in order to avoid peaking in the frequency response and to obtain a phase margin in the range of 60 to 70 degrees. Besides, $g_{m 5} / g_{m 3}>C_{c 2} / C_{c 1}$ can be chosen in order to obtain a negative zero from (2-23) useful to increase the phase margin.

From (2-23) the gain-bandwidth product, $\omega_{G B W,}$ is given by

$$
\begin{equation*}
\omega_{G B W}=\frac{g_{m b 1,2}}{C_{C 1}} \tag{2-25}
\end{equation*}
$$

Substituting the values given in Table 4 on the above equations, the calculated transfer function can be plotted. In Figure 16 the calculated Bode is depicted altogether with the postlayout simulated Bode diagram.

It can be seen that at low frequencies the equations provide a good approximation. In the vicinity of the unity gain frequency, the effect of parasitics makes the simulated and the calculated Bode differ. However, the proposed simplified model provides manageable equations and reasonably
good modelling. Further details regarding these discrepancies are provided on Appendix A.


Figure 16: Calculated and simulated frequency response of the Three-Stage ClassAB OTA.

### 2.3.2.2. Slew Rate.

The slew rate (SR) of an OTA is the maximum output voltage rate. It occurs when the maximum current flowing into a capacitor is limited [4]. Hence, in multistage amplifiers the SR is going to be determined by the slowest stage, i.e., $S R=\min \left[I_{x} / C_{x}\right]$, where $I_{x}$ is the maximum charging of discharging current of the load capacitor of the $x$-th stage, $C_{x}$.

For the proposed OTA implementation, the slowest stage is the last one as the loading capacitor $C_{L}$ is the largest. The negative $S R$ is determined by common source transistor M 7 , whose maximum instantaneous current is in principle larger than the maximum current that the load transistor, $\mathrm{M}_{8}$, can provide. This makes the positive slew rate smaller that the negative one. This fact is partially alleviated making the output stage Class- AB , as explained before, using the current mirror formed by transistors $\mathrm{M}_{8}$ and $\mathrm{M}_{10}$, however, still with this Class- AB operation the maximum current that $\mathrm{M}_{8}$ can provide to the load capacitor, $C_{L}$ is still smaller than the one that $\mathrm{M}_{7}$ provides, so that the unbalanced positive and negative SR persists. Simulations show positive SR of $2.16 \mathrm{~V} / \mu \mathrm{s}$ and negative SR of $4.42 \mathrm{~V} / \mu \mathrm{s}$ for nominal corner.

### 2.3.2.3. Power Supply Rejection Ratio.

The Power Supply Rejection Ratio (PSRR) defines the capability of a circuit to reject the variations of the power supply. It is defined as [4]

$$
\begin{equation*}
P S R R=\frac{\Delta V_{\text {supply }}}{\Delta V_{\text {out }}} A(s) \tag{2-26}
\end{equation*}
$$

A common strategy to determinate the PSRR is using the voltaje-follower configuration, where the output is fedback to the negative input of the OTA and the positive input is set to the analog ground. PSRR+ and PSRR- can be then calculated as PSRR $+=V_{\text {dd }} / V_{\text {out }}$ and PSRR- $=V_{\text {ss }} / V_{\text {out }}[4]$.

Figure 17 shows the low-frequency small signal model used for calculating the positive PSRR at DC, where $r_{d s i}=1 / g_{d s i}$ is the drain-source resistance of transistor $i$.


Figure 17: Small signal model for the calculation of PSRR+ at low frequencies for the Three-Stage Class-AB bulk-driven OTA.

Solving the circuit, the numerator and denominator of PSRR+ are given by

$$
\begin{gather*}
N U M_{P S R R+}=g_{m b 1,2} g_{m 3} g_{m 5} g_{m 7} R R_{o 1} R_{o 2} \\
D E N_{P S R R+}=2\left[( R + R _ { o 1 } + g _ { m 3 } \mathrm { R } _ { o 1 } ^ { 2 } + g _ { m 3 } \mathrm { R } R _ { o 1 } ) \left(g_{m 8}+g_{d s 8}-g_{m 8} g_{m 10} R_{o x}\right.\right.  \tag{2-27}\\
\\
\left.-g_{m 7}\left(g_{m b 6}+g_{d s 6}\right) R_{o 2}\right) \\
\\
\left.+R_{o 1}\left(R+R_{o 1}\right)\left(g_{m b 1}+g_{d s 1}\right)\left(g_{m 5} g_{m 7} R_{o 2}+g_{m 8} g_{m 9} R_{o x}\right)\right]
\end{gather*}
$$

For the calculation of the PSRR-, the low-frequency small signal model of Figure 18 was solved, giving a negative PSRR numerator and denominator that can be approximated by

$$
\begin{gather*}
N U M_{P S R R-}=g_{m b 1,2} g_{m 3} g_{m 5} g_{m 7} R R_{o 1} R_{o 2} \\
D E N_{P S R R-}=2\left[( R + R _ { o 1 } + g _ { m 3 } \mathrm { R } _ { o 1 } ^ { 2 } + g _ { m 3 } \mathrm { R } R _ { o 1 } ) \left(g_{m 7}+g_{d s 7}\right.\right.  \tag{2-28}\\
\left.-g_{m 8} R_{o x}\left(g_{m 9}+g_{d s 9}\right)-g_{m 7}\left(g_{m 5}+g_{d s 5}\right) R_{o 2}\right) \\
\left.+R_{o 1}\left(R+R_{o 1}\right)\left(g_{m 3}+g_{d s 3}\right)\left(g_{m 5} g_{m 7} R_{o 2}+g_{m 8} g_{m 9} R_{o x}\right)\right]
\end{gather*}
$$



Figure 18: Small signal model for the calculation of PSRR- at low frequencies for the Three-Stage Class-AB bulk-driven OTA.

Substituting the transconductance and resistance values of Table 4 on the provided equations, a positive and negative PSRR of 60 dB and 71 dB are obtained, while in simulations 62 dB and 72 dB , respectively, are obtained, validating the equations.

### 2.3.2.4. Implementation and validation.

As it has been mentioned before, the proposed OTA has been designed and implemented in a standard 180 nm CMOS technology with threshold voltages around $\mathrm{V}_{\text {thp }}=0.35 \mathrm{~V}$ and $\mathrm{V}_{\text {thn }}=0.45 \mathrm{~V}$. The design operates under a 0.7 V single supply.

Transistors' aspect ratios and transconductances, as well as the rest of the design parameters and values were summarized in the tables of Table 3 and Table 4. Resistors are physically implemented with $1792 \Omega / \square$ high-resistive poly. Each resistor occupies $13.47 \mu \mathrm{~m} \times 1.67 \mu \mathrm{~m}$. Figure 19 shows a microphotograph of the chip the designed layout, which occupies a total area of $0.019 \mathrm{~mm}^{2}$.


Figure 19: Microphotograph of the chip and layout of the Three-stage Class-AB OTA.

The proposed OTAs were designed for a certain technology option (Option 1) but due to foundry imposition they were finally fabricated in a different option (Option 2). That issue has negatively impacted on the measured performances.

Specifically, it has been observed that Option 2 has smaller transconductances, bigger output resistances and higher bulk and gate-related parasitics.

To note that the simulation results provided throughout all this chapter correspond to the technology option Option 1 for which the OTAs were designed.

Appendix B provides more details regarding the technology options.

In order to check the robustness of the standby current control in the last stage of the proposed structure, a MonteCarlo simulation is performed (process and mismatch, 1000 iterations). The associated histogram is plotted in Figure 20.


Figure 20: Histogram of the standby current of the third stage of the Three-stage Class-AB OTA.

From this analysis, a mean quiescent current of $8.9 \mu \mathrm{~A}$ is obtained (aspect ratios designed for $10 \mu \mathrm{~A})$. The standard deviation is only $0.7 \mu \mathrm{~A}$.

## Input Common Mode Range.

As stated before, the maximum ICMR is actually limited by the maximum allowable input current, that was set to 1000 times the drain current of the input pair $(4 \mathrm{nA})$ so that it can be neglected, resulting in a simulated ICMR of 550 mV pp (from 150 mV to 700 mV ).

The input current has been measured at $20^{\circ} \mathrm{C}$, obtaining the results shown in Figure 21.


Figure 21: Measured input current versus bulk-source voltage @ $20^{\circ} \mathrm{C}$ of the Threestage Class-AB OTA.

It can be observed from the results that the actual measured input current for $\left|V_{\text {bs }}\right|=550 \mathrm{mV}$ is lower than the estimation of the simulator; actually, 1.24 nA . This was expectable not only because the design was fabricated in another technology option but also because the current of a forward-biased $p n$ junction is usually overestimated in simulators [28].

Regarding the dependence with temperature of the input current, it is going to be presumably strong, as, again, it corresponds with the temperature dependence of the current through a $p n$ junction that approximately doubles each $10^{\circ} \mathrm{C}$ [4]. Thus, according to the measurements it can be inferred that if the ICMR is limited to 550 mV , then the input current will remain below 100 nA up to $80^{\circ} \mathrm{C}$.

A final comment regarding the input current stands for the possibility of latch up to occur if $\left|V_{B S}\right|>0.6 \mathrm{~V}$. With the ICMR limitation, the maximum $\left|V_{B S}\right|$ is limited to $\left|V_{B S}\right|_{\max }=550 \mathrm{mV}$ so the bulk-source diode should not enter conduction, hence latch up should not occur. Despite this, usual layout precautions (double guard rings) have been also taken. Indeed, during experimental verification latch up has not happened, even if the ICMR was forced to a higher value ( $\sim 0.7 \mathrm{~V}$ ).

## Frequency response.

The nominal postlayout simulated frequency response Bode plot is represented in Figure 22. Additionally, Figure 23 shows the results of MonteCarlo analysis (process and mismatch, 1000 iterations) for the DC gain, unity gain bandwidth (UGBW) and phase margin (PM).


Figure 22: Nominal simulated frequency response of the Three-Stage Class-AB OTA.


Figure 23: MonteCarlo results for (a) DC gain, UGBW (b) and (c) phase margin of the Three-Stage Class-AB OTA.

These results show the robustness of the solution. A mean DC gain of 61 dB , with standard deviation $(\sigma)$ of 0.7 dB is obtained. The mean UGBW is equal to 3.5 MHz , with a deviation of 0.2 MHz , while the phase margin mean value results to be $59^{\circ}$, with a standard deviation of $2.2^{\circ}$. That means, considering the $3-\sigma$ rule ${ }^{4}$, that even in the worst case the phase margin is above $45^{\circ}$ (actually, $52^{\circ}$ ) so the system should remain stable. These three parameters were also experimentally tested: Figure 24 shows a measurement of the UGBW and phase margin, carried out using a vector network analyzer (Rohde\&Schwarz ZVRL). A UGBW of 3 MHz and a phase margin of $60^{\circ}$ were measured.

[^2]

Figure 24: UGBW and phase margin measurement of the Three-stage Class-AB OTA.

For this OTA, despite being fabricated in a different option of the technology, measurements properly fit expected results.

## DC gain.

Regarding the DC gain, as the first pole is placed at a frequency lower than the vector analyzer's minimum frequency of operation ( 9 kHz ), it was measured using an oscilloscope (Agilent MS08104A), like proposed on [43] and depicted in Figure 25 , obtaining a value of 57.5 dB .


Figure 25: Low-frequency differential gain test circuit.
Resistor $R_{\text {test }}$ and capacitor $C_{t e s t}$ are chosen large enough $(3 \mathrm{M} \Omega, 1 \mu \mathrm{~F})$ for properly set the DC and, as they act as a high pass filter, the pole is set below the first pole of the OTA introduce so at certain frequencies the low frequency $A_{d}$ can be
measured.
Thereby, a value of 57.5 dB was measured. This value is lower than expected by MonteCarlo simulation, but easily explained if the fabricated technology presents lower $g_{m} \cdot r_{o}$ product.

## Common Mode Rejection Ratio.

The CMRR obtained via simulation is depicted on the histogram of Figure 26, corresponding to a MonteCarlo simulation of 1000 iterations for process and mismatch. A mean CMRR of 14.7 dB with a standard deviation of 2.6 dB is obtained.


Figure 26: Histogram of the CMRR of the Three-stage Class-AB OTA.
Experimental validation was fulfilled using and oscilloscope and the test circuit of Figure 27 [43], similarly as done for the differential gain. In this case, $C_{\text {test }}$ ensures that at proper frequency values both OTA inputs are driven by the same input $V_{i n}$, thus $A_{c m}$ can be measured, obtaining a value of 38.5 dB .


Figure 27: Low-frequency common-mode gain test circuit.
Hence, the CMRR can be obtained by simply:

$$
\begin{equation*}
\operatorname{CMRR}[d B]=A_{d}[d B]-A_{c m}[d B]=57.5 d B-38.5 d B=19 d B \tag{2-29}
\end{equation*}
$$

## Power Supply Rejection Ratio.

Statistical simulations of the positive and negative PSRR of the proposed OTA have been performed, assuming process and mismatch variations, and its histograms are depicted in Figure 28.


Figure 28: Histogram of the (a) PSRR+ and (b) PSRR- of the Three-stage Class-AB OTA @DC.

Huge variability is observed in the results, what evidences a strong dependency with the variability of the technology process and mismatch.

Measurements of five samples show mean results of 45 dB and 57 dB for the positive and negative PSRR, respectively. As the OTA was fabricated in a different technology and PSRR variability is high, it is expectable to obtain results that does not properly fit with the simulated results.

## Input Referred Noise.

The input referred noise was also experimentally validated. In Figure 29 the measured noise is plotted altogether with the noise simulated in the technology option in which the OTA was designed (Option 1). It can be observed that the measured results are below the simulations, with around $100 \mathrm{nV} / \sqrt{ } \mathrm{Hz}$ at 1 MHz of input referred noise density.

As the main contributor to noise is flicker noise, it makes sense that the simulations in the technology option where the OTA was fabricated are above the measured results, provided that the measured circuit is fabricated in other technology and that the flicker noise is strongly variable with process and mismatch ${ }^{5}$.

[^3]

Figure 29: Simulated and measured input referred noise spectral density of the Three-stage Class-AB OTA.

## Transient Response.

The simulation of the transient response for the voltage-follower configuration of Figure 30 is shown in Figure 31 for the nominal corner and an input of $500 \mathrm{mV} \mathrm{Vp}_{\mathrm{pp}}$.


Figure 30: Voltage-follower configuration.


Figure 31: Simulated voltage-follower step response to a $500 \mathrm{mV}_{\mathrm{pp}}$ input of the Three-stage Class-AB OTA.

In Table 5 the slew rate and $1 \%$ settling time (ST), obtained for different corners, are summarized. The asymmetry between the values for the positive and negative slope that was explained on section 2.3.2.2 can be observed.

| Corner | SR+/SR- <br> $[\mathbf{V} / \boldsymbol{\mu}]$ | ST+/ST- <br> [ns] |
| :---: | :---: | :---: |
| Nominal | $2.16 / 4.42$ | $498 / 270$ |
| FF | $2.92 / 5.90$ | $437 / 237$ |
| SS | $1.59 / 3.22$ | $544 / 253$ |
| FS | $2.15 / 5.57$ | $497 / 253$ |
| SF | $2.00 / 3.44$ | $489 / 240$ |

Table 5: Simulated slew rate (SR) and settling time (ST) for different corners of the Three-Stage Class-AB OTA.

The measured step response is shown in Figure 32 where a positive $S R$ of $1.8 \mathrm{~V} / \mu \mathrm{s}$ and a negative SR of $3.8 \mathrm{~V} / \mu \mathrm{s}$ were obtained. Although SR results are in agreement with simulations the positive settling time is found to be doubled, obtaining around $0.9 \mu \mathrm{~s}$. Negative settling time is around $0.2 \mu \mathrm{~s}$.


Figure 32: Measured voltage-follower step response to a $500 \mathrm{mV} \mathrm{pp}_{\mathrm{pp}}$ input of the Three-stage Class-AB OTA.

## Performance Summary.

Table 6 shows a summary of the measured parameters of the proposed Three-Stage OTA.

| Parameter | Value |
| :---: | :---: |
| Supply voltage (VDD-VSS) [V] | 0.7 |
| Power dissipation [ $\mu \mathrm{W}$ ] | 25.4 |
| Area [ $\mathrm{mm}^{2}$ ] | 0.019 .8 |
| Offset (maximum) [mV] | 11 |
| ICMR [mV] | 550 (from 150 mV to 700 mV ) |
| Max Input Current [nA] @ 200 | 1.3 |
| Open-Loop DC Gain [dB] | 57.5 |
| UGBW [MHz] | 3 |
| Phase Margin [ ${ }^{\circ}$ ] | 60 |
| SR+/SR-[V/ $/ \mathrm{S}^{*}$ | 1.8/3.8 |
| 1\% ST (+/-) [ $\mu \mathrm{S}]^{*}$ | 0.9/0.2 |
| CMRR@DC[dB] | 19 |
| PSRR@DC (+/-) [dB] | 45/57 |
| Input Ref. Noise @1MHz [nV/vHz] | 100 |
| THD @100kHz, 400m $\mathrm{V}_{\text {p-p }}$ input [\%]** | 0.20 |
| THD@250kHz, 400mV ${ }_{\text {p-p }}$ input [\%]** | 0.99 |

*Voltage follower configuration
**Inverting configuration
Table 6: Measured performance parameters of the Three-Stage Class-AB OTA under 20 pF loading.

At the end of this chapter the performance of this OTA is discussed altogether with the other two proposed OTAs and compared with other State-Of-Art Amplifiers.

### 2.3.3. Low-Voltage Bulk-Driven Three-Stage Class-AB OTA with BulkDriven Slew-Rate Boosting.

### 2.3.4. Low-Voltage Bulk-Driven Four-Stage Class-AB OTA with BulkDriven Slew-Rate Boosting

### 2.4. Conclusions.

In this chapter, a Non-Tailed Bulk-Driven Differential Input Stage, suitable for very low-voltage design is presented and analysed. Three different multistage Class-AB OTAs have been implemented, all of them sharing the same proposed input stage, as a proof of concept: two three-stage, one of them with an additional technique to enhance the SR. Finally a four-stage OTA is presented.

The three OTAs were analysed, designed and fabricated. However, due to
foundry imposition, they were finally fabricated in a different technology option (details provided in Appendix B) with smaller transistor $g_{m}$, higher transistor $r_{o}$ and, higher parasitics. Due to the robustness of the design and compensation, this has barely affected the performances of the Three-Stages OTAs

Table 16 shows a comparison of the performances of the proposed OTAs altogether with the Sub-1V amplifiers found in the State-Of-Art that were commented in section 2.2. In order to carry out a quantitative comparison, the two traditional Figures of Merit ( FoMs and FoML ) are evaluated and, for convenience, shown again in equation (2-55).

$$
\begin{gather*}
F o M_{S}=\frac{U G B W \cdot C_{L}}{\text { Power }} \\
F o M_{L}=\frac{S R \cdot C_{L}}{\text { Power }} \tag{2-30}
\end{gather*}
$$

Figure 33 and Figure 34 show the comparison in a graphical way. It is apparent that the proposed amplifiers outperform almost all other previously reported bulk-driven OTAs. In particular, as far as parameter FoMl is concerned, the proposed OTAs display the maximum values by far. Regarding the FoMs parameter, Contribution 3 performs the best result, followed by [30] and [6] and then Contributions 1 and 2.


Figure 33: FOMs and FOML Vs Year of Publication of Sub-1V OTAs.
In Figure 34 FOMs and FOML are depicted together for further comparison.

As the proposed OTAs are the only ones placed in the upper-right quadrant it is apparent that their overall performance outstand the other solutions proposed in literature.

However, they perform the worst CMRR among all the other solutions found in the comparison, thus, an effort to overcome this issue should be accomplished in future research.


Figure 34: FOMs Vs FOMl of Sub-1V OTAs.
The achieved performances have been possible thanks to the combination of all the discussed techniques. Summarizing, the bulk-driven input, applied in a non-tailed differential pair, allows a very low-voltage supply while maintaining a wide input common-mode range. Gain is provided by multiple stages, and quiescent currents properly set structurally. Large signal performances are achieved through Class-AB stages, and, in the last two contributions, making use of the bulk to further enhance the Class-AB behavior. Nonetheless, the bulk-driven non-tailed structure means poor CMRR and PSRR and the noise worsening related to bulk-driven inputs.

| Year, Ref. | Tech. [ $\mu \mathrm{m}$ ] | Supply <br> [V] | DC Current [ $\mu \mathrm{A}$ ] | $\begin{gathered} \mathrm{C}_{\mathrm{L}} \\ {[\mathrm{pF}]} \end{gathered}$ | $\begin{gathered} \hline \text { DC } \\ \text { Gain } \\ \text { [dB] } \end{gathered}$ | $\begin{aligned} & \text { UGBW } \\ & \text { [MHz] } \end{aligned}$ | $\begin{gathered} \text { PM } \\ {\left[{ }^{\circ}\right]} \end{gathered}$ | Average <br> SR <br> [ $\mathrm{V} / \mu \mathrm{s}$ ] | CMRR [dB] | $\begin{aligned} & \text { PSRR } \\ & \text { [dB] } \end{aligned}$ | Noise [ $\mathrm{nV} / \mathrm{VHz}$ ] | FoMs [ $\mathrm{MHz} \cdot \mathrm{pF}$ /mW] | FoM [ $\mathrm{V} \cdot \mathrm{pF} /$ ( $\mu \mathrm{s} \cdot \mathrm{mW}$ )] |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $2001$ | 0.5 | 1 | 40 | 20 | 69 | 2 | 57 | 0.5 | - | - | - | 1000 | 250 |
| $\begin{aligned} & 2002 \\ & {[29]} \end{aligned}$ | 2.5 | 0.9 | 0.5 | 12 | 70 | 0.0056 | 62 | - | 26 | - | - | 149 | - |
| $\begin{aligned} & 2003 \\ & {[30]} \\ & \hline \end{aligned}$ | 0.25 | 0.8 | 10 | 18 | 50 | 1.2 | 60 | 0.2 | - | - | - | 2700 | 450 |
| 2005 | 0.18 | 0.5 | 220 | 20 | 52 | 2.5 | - | 2.89 | 78 | 76 | $\begin{aligned} & \hline 80 @ \\ & 1 \mathrm{MHz} \end{aligned}$ | 455 | 525 |
| [6] | 0.18 | 0.5 | 150 | 20 | 62 | 10 | - | 2.0 | 74 | 81 | $\begin{gathered} \hline 70 @ \\ 1 \mathrm{MHz} \end{gathered}$ | 2666 | 533 |
| $\begin{gathered} 2007 \\ {[31]} \end{gathered}$ | 0.35 | 0.6 | 0.916 | 15 | 69 | 0.011 | 65 | 0.014 | 74 | 53 | $\begin{gathered} 290 \\ @ 1 \mathrm{kHz} \end{gathered}$ | 300 | 382 |
| $\begin{gathered} 2013 \\ {[32]} \end{gathered}$ | 0.35 | 1 | 197 | 15 | 88 | 11.67 | 66 | 1.95 | 40 | 40/46 | $\begin{gathered} \hline 60 @ \\ 1 \mathrm{MHz} \\ \hline \end{gathered}$ | 889 | 148 |
| $\begin{aligned} & 2014 \\ & \text { [33] } \end{aligned}$ | 0.13 | 0.25 | 0.072 | 15 | 40 | 0.002 | 52 | 0.0007 | - | - | 3300 @- | 1667 | 583 |
| 2015 | 0.065 | 0.5 | 366 | 3 | 46 | 38 | 57 | 43 | 35 | 37 | - | 623 | 705 |
| [16] | 0.065 | 0.35 | 49 | 3 | 43 | 3.6 | 56 | 5.6 | 46 | 35 | - | 630 | 980 |
| $\begin{aligned} & 2015 \\ & \text { [34] } \\ & \hline \end{aligned}$ | 0.18 | 0.9 | 290 | 17 | 76 | 7.11 | 72 | 2.98 | 55 | 48 | $\begin{aligned} & \hline 800 @ \\ & 10 \mathrm{kHz} \\ & \hline \end{aligned}$ | 463 | 194 |
| $\begin{gathered} 2017 \\ {[7]} \end{gathered}$ | 0.35 | 0.9 | 27 | 10 | 65 | 1 | 60 | 0.25 | 45 | 55 | $\begin{gathered} 65 @ \\ 100 \mathrm{KHz} \end{gathered}$ | 411 | 102 |
| Contr. 1 | 0.18 | 0.7 | 36.3 | 20 | 57.5 | 3 | 60 | 2.8 | 19 | 45/57 | $\begin{aligned} & \hline 100 @ \\ & 1 \mathrm{MHz} \\ & \hline \end{aligned}$ | 2361 | 2204 |
| Contr. 2 | 0.18 | 0.7 | 76.2 | 33 | 57.7 | 2.6 | 50 | 4.6 | 14 | 43/47 | $\begin{aligned} & \hline 100 @ \\ & 1 \mathrm{MHz} \\ & \hline \end{aligned}$ | 1674 | 3155 |
| Contr. 3 | 0.18 | 0.7 | 50.16 | 33 | 91 | 2.9 | 11 | 2.6 | 13 | 35/44 | $\begin{aligned} & 100 @ \\ & 1 \mathrm{MHz} \end{aligned}$ | 3155 | 2443 |

Table 7: Performance comparison of Sub-1V OTAs.

## 3. Amplifier-Less Switched Capacitor Circuits

Switched Capacitor (SC) Circuits are one of the most commonly used type of circuits. Their versatility and suitability for being integrated have made them widely used since the early days of integrated electronics [46]. They are based on a charge transfer carried out by a charge conveyor (CC), switches and capacitors.

In traditional SC design, the CC is implemented by an OpAmp, but, as stated before, achieving proper performances in OpAmp design has become more challenging with the technological downscaling. Thus, recently, researchers try to substitute the OpAmp by other CC that do not suffer the OpAmp limitations: the so called amplifier-less techniques.

In this chapter the second line of this thesis is explored: a new differential structure for switched capacitor circuits, specially suitable for reducing low frequency noise and distortion and, thus, enhancing the dynamic range (DR) is presented.

### 3.1. Amplifier-less techniques.

### 3.1.1. Charge-Coupled devices.

One amplifier-less alternative for SC circuits is the use of charge-coupled devices (CCD) in standard CMOS technologies [47]. They were proposed by Boyle and Smith in 1970 [48] and are mainly used in imaging applications.

CCD are metal-oxide-semiconductor (MOS) structures, similar to MOS transistors, in which adjacent gates are close enough to allow channel overlapping. In Figure 35 the transversal view of a CCD structure is shown.


Figure 35: Transversal view of a CCD structure.
In consists of three different sections: input, transfer and output.

- Input section. It consist on a diffusion, and the input gate. The diffusion provides minority carriers and its potential can be controlled. The input gate potential can be turned on or off in order to allow the carriers pass from the diffusion to the input gate potential well.
- Transfer section. It consists on some control gates whose potential is controlled to allow the charge to pass through the structure.
- Output section. Consists on a reverse-biased junction capacitance. Its voltage changes depending on the amount on charge that receives. A switch resets the diode voltage after each charge transference.

Figure 36 depicts an example of how a charge transfer is carried out.


Figure 36: Charge transfer example.
CCD are used in SC circuits as they are based on charge transfer and its efficiency can be really high [47]. The main advantage of CCD structures is that they are not affected by thermal noise, charge injection or coupling from the substrate or clock but they need special process to be implemented and, usually, a high supply voltage is required for the clock signals.

### 3.1.2. Dynamic Amplifiers.

Another OpAmp-less technique for SC circuits substitutes the OpAmp by a group of switches that act as a dynamic amplifier [39], [49]. In charge transfer circuits, where the operation is based on a virtual ground condition, the implementation of dynamic amplifiers is straight-forward.


Figure 37: Classic OpAmp-based SC integrator.
In Figure 37 the classical OpAmp-based SC integrator is depicted. It is well know that the high gain and virtual ground condition of node $v_{x}$ is only needed during the charge transfer phase to fully complete the charge transfer from $C_{1}$ to $C_{2}$. Thus, the OpAmp can be substituted by a dynamic amplifier as shown in Figure 38.


Figure 38: SC integrator with dynamic amplifier implementation.
This structure recreates the virtual ground condition on node $v_{x}$ by the feedback provided by $C_{2}$ as follows: during the sampling phase, $\Phi_{1}$, the capacitor $C_{1}$ receives the charge from the input, then, at the beginning of the charge transfer phase, $\Phi_{2}$, the switch controlled by $\Phi_{2 P}$ closes. This precharges the output node, $v_{o}$ to the positive bias voltage, and, consequently, sets node $v_{x}$ to a voltage higher than the $M_{1}$ threshold voltage, $\mathrm{V}_{\text {th. }}$. After this preset phase, the switch opens and the switch controlled by $\Phi_{2 P 2}$ closes, beginning the amplification phase: node $v_{o}$ starts to discharge from the positive bias and, due to the capacitive coupling, the voltage at node $v_{x}$ also starts to diminish. When $v_{x}$ is under $\mathrm{V}_{\mathrm{th}}$, transistor $M_{1}$ is turned off and the virtual ground condition is achieved.

Even though dynamic amplifiers considerably reduce the power consumption that a OpAmp may require, there is still an analog feedback and, in fact, the output will never settle completely [50].

### 3.1.3. Parametric Amplifier.

In a parametric amplifier, the amplification is achieved though the variation of one circuit parameter or element [51]. For instance, in a capacitor, the voltage drop between its terminals is given by $V_{o u t}=Q / C$ where $Q$ is the stored charge and $C$ its capacitance. If it is charged to a certain value $V_{i n}$ and then the capacitance $C$ is lowered, the voltage drop, $V_{\text {out, }}$ increases achieving the amplification as shown in Figure 39.


Figure 39: Parametric amplification.
A varactor can be used instead of a traditional capacitor in order to electrically control the capacitance value and apply the amplification to sampled systems such as SC [51].

### 3.1.4. Inverter-Based Switched Capacitors Circuits.

In SC circuits the OpAmp can also be replaced by a logic inverter [52]. Figure 40 shows the implementation of an inverter-based single-ended integrator.


Figure 40: Inverter-Based SC integrator.
Its main advantage is that it can work under very low supply voltages. However, as the inverter only has one input terminal it is not able to provide an inherent virtual ground, instead, the node $v_{x}$ is kept close to the offset voltage of the inverter. As this offset is unknown and sensitive to any process, size, supply variation, offset cancellation techniques must be implemented. Figure 41 shows an integrator with offset cancellation [52].


Figure 41: Inverter-Based SC integrator with offset cancellation.

### 3.1.5. Comparator-Based Switched Capacitor Circuits.

In Comparator-Based SC (CBSC) circuits [53] the OpAmp is replaced by a comparator and a current source, as depicted in Figure 42 (a). As the comparator operates in open loop configuration, the requirements of gain and power consumption are substantially relaxed, but speed and accuracy are strongly related to the comparator and current source implementation.

The contribution of this chapter is based on the CBSC technique so it is explained in detail in next section.

### 3.2. Comparator-Based Switched Capacitors

A CBSC integrator is depicted again for reference in Figure 42 (a), as mentioned before, this technique substitutes the amplifier by a comparator and a current source. The main idea of this technique is that, for properly transfer the charge from $C_{1}$ to $C_{2}$, the CC needs to stablish a virtual ground condition on node $v_{x}$.


Figure 42: (a) CBSC integrator (a) structure (b) clock phases and operation.
Hence, the comparator controls the activation of the current source, $I_{b 1}$, responsible for the charge of the output node, $v_{o}$. At the beginning of the charge transfer phase, $\Phi_{2}$, during a brief time, called preset phase, signal $\Phi_{P 2}$, Figure 42 (b), is activated so that node $v_{0}$ is short-circuited to the negative bias voltage, VSS, ensuring that node $v_{x}$ always starts below $V \subset M$. At the end of $\Phi_{P 2}$ the comparator activates the current source $I_{b 1}$, which starts the charge of $v_{o}$. As a consequence, as $v_{x}$ and $v_{o}$ are capacitively coupled in an integrator, $v_{x}$ increases until it equals $V_{C M}$. At this moment the virtual ground condition is achieved so the charge transfer is completed and the comparator turns $I_{b 1}$ off.

Let us now consider a non-ideal integrator, where the comparator has some delay and the current source is not perfectly linear. Under these realistic conditions an error in the output appears: the overshoot error, which is explained in next section.

### 3.2.1. Overshoot Error.

In a CBSC integrator, as the one depicted in Figure 42, due to comparator time delay, $t_{d}$, the current source, $I_{b 1}$, will not turn off exactly when the ground condition is achieved but later. This causes the so-called overshoot error, vos, represented in Figure 43.

(1) Virtual ground condition detected
(2) $I_{b 1}$ turns off

Figure 43: Overshoot Error.
The overshoot error is proportional to the current $I_{b 1}$, as it is responsible of the slope of $v_{o}$. Thus, for a given $t_{d}$, small currents minimize $v o s$, but it needs to be large enough to assure node $v_{x}$ reaches $v_{c m}$ during $\Phi_{2}$. This implies that a compromise between speed and accuracy needs to be stablished. Moreover, since the current source is not completely lineal, the overshoot is going to introduce distortion.

In order to overcome this error, in [53] authors propose the use of two current sources: the first one, larger, provides the speed but implies large overshoot error, and the other one, smaller, is activated later to reduce the overshoot. In [54] and [55] authors make use of variable current sources to improve speed while maintaining accuracy. Other contributions, such as modifying the charging algorithm [56], [57], using hybrid schemes [58] or dynamic comparators [59] have been proposed to further improve the performances and overcome the speed-accuracy compromise.

In addition, some works present differential implementations, [60]-[63], as they have the advantages of double signal swing, extrinsic noise and common mode rejection and linearity enhancement among others. Moreover, in SC circuits, charge injection issues are greatly reduced [64].

In the next section, differential CBSC implementations are discussed.

### 3.2.2. Differential CBSC Implementation.

As in the traditional OpAmp-based SC circuits, a differential implementation can be carried out in different ways: Fully-Differential (F-D) and Pseudo-Differential (PD). In Figure 44 the differential CBSC integrators are depicted.


Figure 44: (a) F-D and (b) P-D CBSC integrators.
The F-D implementation of Figure 44(a) uses a SE comparator to generate both outputs, $v_{0+}$ and $v_{0 .}$. At the beginning of the charge transfer phase, $\Phi_{2}$, the outputs $v_{0+}$ and $v_{o-}$ are pushed to the supply rails, $V S S$ and $V D D$, respectively, during the preset phase, $\Phi_{2 P}$. Then, both current sources are turned on and when $v_{x+}$ crosses $\mathrm{V}_{x}$ - they are turned off. Due to the comparator time delay, the current sources are not closed immediately and some overshoot error happens. This overshoot error is a differential error in F-D CBSC structures, as it can be observed in Figure 45(a).

(a)

(b)

Figure 45: Output signals evolution in (a) F-D and (b) P-D CBSC integrators.
On the contrary, in P-D structures (Figure $44(\mathrm{~b})$ ), during the present phase, $v_{0+}$ and $v_{0-}$ are both pushed to the same voltage value, VSS, and, when the current sources are turned on they both charge the output nodes in the same direction until $v_{x+}$ and $v_{x-}$ reach $v_{c m}$, as it can be observed in Figure 45(b). In this case, the overshoot error leads to a common mode error, than can be easily removed by a common mode control circuit. As it is easier to eliminate common mode errors than differential errors, the pseudo-differential implementation is usually preferred [63].

### 3.3. Contribution.

### 3.4. Conclusions.

## 4. Conclusions and Future Work

$T$hroughout this thesis two different design philosophies that have arisen in the context of deeply scaled analog integrated electronics have been undertaken.

First, on Chapter 2, three multistage bulk-driven OTA that share the same proposed low-voltage non-tailed differential input stage were proposed. When compared with other sub-1V amplifiers, the proposed OTAs outstand the state of the art.


Figure 46: FOMs Vs FOMl of Sub-1V OTAs.
Despite the competitive results, there is still place for further improvement. Firstly, the amplifiers may be refabricated in order to overcome the limitation of a non-controlled fabrication. Secondly, the design of a fully-differential version. But, among all the future work, enhancing the parameters that have obtained less satisfactory results may be a priority. In this line, a new input stage with CMRR
improvement shall be developed.
On Chapter 3, amplifier-less switched-capacitor circuits were studied and a new differential technique that intrinsically reduces noise and distortion is proposed.

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## ApPENDIX A

## APPENDIX B

## APPENDIX C

## APPENDIX D

In this appendix the publications of the author of this thesis are attached for reference.

1. E. Cabrera-Bernal, C. Lujan-Martinez, R. G. Carvajal, and J. Ramirez-Angulo, "Limitations of CAD Tools for Modeling Transistors that Implement Large Resistors," in 2012 XXVII Conference On Design of Circuits and Integrated Systems(DCIS), 2012.
2. E. Cabrera-Bernal, S. Pennisi, and A. D. Grasso, "Bulk-Driven Three-Stage Class-AB CMOS OTA," in 2014 XXIX Conference On Design of Circuits and Integrated Systems(DCIS), 2014.
3. E. Cabrera-Bernal, S. Pennisi, and A. D. Grasso, " $0.7-\mathrm{V}$ bulk-driven three-stage classAB OTA," in 2015 IEEE 13th International New Circuits and Systems Conference (NEWCAS), 2015, pp. 1-4
4. E. Cabrera-Bernal, S. Pennisi, A. D. Grasso, A. Torralba, and R. G. Carvajal, " $0.7-\mathrm{V}$ Three-Stage Class-AB CMOS Operational Transconductance Amplifier," IEEE Trans. Circuits Syst. I Regul. Pap., vol. 63, no. 11, pp. 1807-1815, Nov. 2016.

# Limitations of CAD Tools for Modeling Transistors that Implement Large Resistors 

E. Cabrera-Bernal, C. Lujan-Martinez<br>and R.G. Carvajal<br>Electronic Engineering Department<br>University of Seville<br>Seville, Spain<br>\{elena.cabrera, clara.lujan, carvajal\}@gie.esi.us.es

J. Ramirez-Angulo<br>Klipsch School of Electrical Engineering<br>New Mexico State University<br>Las Cruces (New Mexico) USA<br>jramirez@nmsu.edu


#### Abstract

The QFG technique has proven to be very effective for low power and low voltage analog design with a moderate increase in the circuit area thanks to the implementation of pseudo-resistors by means of MOS transistors in the cut-off region. However, the implementation of these pseudoresistors introduces some parasitic effects whose study is required to prevent undesired dynamics, or to take profit of these structures in some other applications with extremely slow time behavior. In this paper, a study of the accuracy of the CAD tools to model certain structures based on transistors in the cutoff region is presented. A comparison between simulations and measurements shows the need of a simple but reliable model for this kind of structures.


Keywords- Low power; low voltage; biomedical applications; Quasi-floating gate (QFG) transistors; CAD tools

## I. INTRODUCTION.

Nowadays, handheld electronic devices have acquired huge importance in modern lifestyle. From mobile phones to personal laptops, the requirement of low power and low voltage is compulsory to extend the battery lifetime. ${ }^{1}$

In biomedical applications, the need of ambulatory monitoring is undisputable as it allows long-term patient monitoring, reduces their hospitalization costs and provides trustable data as they are acquired during their normal daily activity. However, these devices have been traditionally rather uncomfortable and aesthetic leading patients to stay at home during the tests. As a consequence, the accuracy of diagnosis is crippled by the unrealistic conditions of the data acquisition.

Thus, the design of truly miniaturized wearable devices is a current challenge for this kind of applications where the stringent requirements of size, weight, battery lifetime and performance imply a great effort on low power and low voltage electronic design. The interest of the scientific community is clearly reflected in recent literature [1], [2].

The first stage of biomedical signal acquisition is the sensor; hence, the sensor interface is a critical block, as it has to provide to the next processing stages a clear input signal.

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Biomedical signals are usually characterized by extremely low frequency and generally very low amplitude. Nevertheless, they usually introduce an unknown and appreciable dc offset, due to some electrochemical effects that takes place between sensor and organic tissues. These facts pose a complex problem, as it is indispensable to filter the large dc offset (as it can lead to severe problems in the signal processing) while maintaining the low-frequency signals unfiltered. This results in the use of extremely low cut-off frequency high pass filters. Moreover, integrating large passive resistors or capacitors to implement those low cut off frequency filters in existing MOS technologies is not feasible.

Recently, the high pass filtering capability of the QuasiFloating Gate (QFG) technique has been highlighted in [3], where an extremely low cutoff frequency was achieved by means of an extremely high resistor implemented by a MOSFET transistor working in subthreshold or cutoff region. In addition, QFG transistors have been successfully used in a number of different, not only biomedical, applications as stated in [4], [5]. In the field of biomedical sensor interfacing, some contributions based on these pseudo-resistors have been also proposed [6], [7].

However, in [8] a time dependency of the DC voltage on some structures, that used these pseudo-resistors, was reported. From the results published in the literature these problems seem to be related to the implementation of the pseudoresistors.

Although this voltage drift is not a serious problem, as it can be easily overcome, a detailed study of this drift highlights the lack of fair modeling present CAD simulators when working with transistors in cutoff region. With a proper model this voltage drift could be anticipated and corrected. Even in certain cases some profit could be taken from it for some applications that require extremely slow time dynamics.

This deficiency in transistor modeling makes the design work quite complicated, as simulation results are unreliable.

In this paper a thorough study of different ways to use circuit simulators with transistors working in cutoff region is presented. In section II, the QFG transistor technique is reviewed. In section III, two selected implementations of pseudo-resistors for a test circuit used in this study are presented. In section IV, some simulation techniques and their
results are presented. Later, in section V, measurement results are compared to simulation ones. Finally, in section VI, some conclusions are drawn.

## II. QFG Transistors.

Theoretical foundation and practical aspects of the QFG transistors are presented in [3]. They are MOSFET transistors whose gates are capacitively coupled to the inputs as shown in Figure 1. Moreover, a very large resistor connects the gate to a dc bias voltage. Hence, as the gate is not really floating, they are called quasi-floating gate transistors (Fig. 1).


Figure 1. QGF transistor.
This simple structure allows gate biasing while filtering the inputs dc level. Thus, in the gate of the transistor we have the weighted sum of the ac component of the inputs plus the desired bias voltage established through the large resistor. This is important for sensor interface, as it filters out the non-desired dc offset of the input signals.

## III. TEST CIRCUIT AND PSEUDORESISTORS

## A. Test circuit.

For testing purposes two pseudoresistors will be used in the simple voltage follower depicted in Fig. 2, where Rlarge is replaced by the selected pseudoresistor implementation. This circuit has been chosen because the voltage drift in the pseudoresistor can be easily measured in the circuit output.

The circuit shown in Figure 2 consists of two simple and identical voltage followers. The first one has a QFG transistor with a pseudoresistor at the input terminal, while the latter do not. The principle of operation is quite simple: the outputs $v_{o 1}$ and $v_{o 2}$ will follow $M 1$ and $M 2$ gate voltage respectively, with an ideal voltage gain of 1 . In this circuit $v_{1}$ is the bias voltage while $v_{2}$ is a sinusoidal input signal. Consequently, the circuit allows the differences between the QFG follower dc output $\left(v_{o 1}\right)$ and the classical follower dc output $\left(v_{o 2}\right)$ to be easily observed.

Concerning the pseudoresistor implementation many different structures can be found in the literature [6], [7]. In this paper two simple pseudo-resistor implementations have beenchosen, as their simplicity will facilitate the development of basic circuit models. Comparing simulated to experimental results obtained with the proposed structure will provide an in-
depth understanding of the physical phenomena that occur in the devices components and in their implementation. From these results new powerful models could be developed for more complex structures.


Figure 2. Test circuit, voltage follower.

## B. Pseudoresistor 1

In Fig. 3, the first pseudoresistor implementation is shown. As the gate node is connected to the source node, no transistor channel is created. In addition, in our test circuit (Fig. 2), the PN junction between source and drain is always reverse biased, as node $X$ always has a voltage higheror equal than node $Y$, so the current flowing through the structure is expected to be quite small. For all these reasons, pseudo-resistor 1 is expected to present a huge ohmic value.


Figure 3. Pseudoresistor 1. (a) Symbol. (b) Physical structure.

## C. Pseudoresistor 2

In Fig. 4, the second pseudoresistor structure considered in this paper is shown. Just like in Pseudoresistor 1, no channel
can be created, as gate and source nodes are connected together, so a very small current flow is expected through the transistor channel. However, as in our test circuit (Fig. 2) the PN junction between node $X$ and node $Y$ will always be forward biased, a higher value of the current through this structure is now expected in comparison to Pseudoresistor 1 implementation.


Figure 4. Pseudoresistor 2. (a) Symbol. (b) Physical structure.

## IV. SIMULATION TECHNIQUE AND RESULTS

In this section some particularities, difficulties and solutions encountered while simulating this kind of circuits are detailed. All the simulations have been done in Cadence and for a standard $0.5 \mu \mathrm{~m}$ CMOS technology.

## A. High precision simulation technique.

Considering that we are trying to simulate structures that deal with extremely low current values, standard simulation precision parameters must be modified, as high precision is required to compute those current values. In our study, relative convergence criterion (reltol) is set to $1 \mathrm{e}-6$, voltage and current absolute tolerance convergence criterion (vabstol, iabstol) are set to $1 \mathrm{e}-9$ and $1 \mathrm{e}-15$, respectively, and minimum conductance across all semiconductor junctions (gmin) is set to $1 \mathrm{e}-18$.

These parameter values will usually lead to convergence problems that could be solved by relaxing the simulation precision, at the cost of imprecise simulations. However, these convergence problems have been solved by facilitating the computation of the operating point to the simulator by means of ramp-up simulation.

## B. Ramp-up simulation technique.

As it was described above, the simulator will present convergence problems when changing the convergence parameters. Furthermore, as we are trying to simulate transient
phenomena, we must emulate, as far as possible, the real circuit behavior.

For all this, every independent current and voltage source were simulated using Piece Wise Linear (pwl) sources. Using these sources we are able to set all circuit excitation to zero at the beginning of the simulation and, after a brief period of time, set them to their final values following an rising ramp, in a way similar to what it is expected when the power source of a real circuit is switched on.

In addition, pwl sources facilitate the operating point computation as, at the beginning of the simulation, all voltages and currents are equal to zero.

Although Cadence offers the possibility of running an automatic ramp-up simulation, using pwl sources have the advantage of providing more controllable simulation parameters.

## C. Simulation time.

First of all, note that the circuits to be simulated have very large time constants. As a consequence, in order to see the full transient behavior, a long period of time must be simulated. It leads to large simulation files that could run computers out of memory. Fortunately, in Cadence, just a limited amount of data can be managed when plotting simulation result. Then, to avoid these problems, neither circuit node voltage nor branch currents must be saved. Instead of that, AHDL code have been used to save into a text file the average voltage of the signals of interest in the test circuit shown in Fig. 2, which are $v_{o 1}$ and $v_{o 2}$ in this case. Later, these text files are processed using MatLab.

## D. Simulation results.

Simulation results are now presented. As we are only interested in the dc voltage drift, for these simulations, $v_{1}$ is the bias voltage while $v_{2}$ is also a dc source. In the following graphs the dc voltage of the outputs $v_{o 1}$ and $v_{o 2}$ are represented.

## 1) Pseudoresistor 1.



Figure 5. Pseudoresistor 1 simulation results.

## 2) Pseudoresistor 2 .



Figure 6. Pseudoresistor 2 simulation results.
Unfortunately these simulations require such an amount of time to be completed that it is not usually handy. As we are only interested in the dc voltage and the transient dynamic is slow enough, one way to accelerate the simulations is to increase the transient simulation step. Simulation results obtained this way are shown below, where the simulation transient time step was artificially set to 0.02 s .

## 3) Pseudoresistor 1



Figure 7. Pseudoresistor 1 simulation results using a large transienttime step.

## 4) Pseudoresistor 2 .



Figure 8. Pseudoresistor 2 simulation results using a large transient time step.

It can be observed that both simulations with standard, selfadjusted, and with large, fixed transient timesteps, approximately provide the same results. Then, whenever it is possible, selecting a time step as big as possible is the first solution to be tried for faster simulation of the dc voltage drift.

How big? This question is no easy to answer. In our case we obtained a proper value by a trial and error procedure.

## V. MEASUREMENT TECHNIQUE AND RESULTS

In order to test the accuracy of the simulations, the test circuit was laid out and sent for fabrication and some measurement results are presented here.


Figure 9. Microphotograph of the chip..
As the measurement of these circuits takes a long period of time, an automated measurement technique has been used. The circuit outputs are taken to an oscilloscope, which is connected to a computer with LabView programmed to take periodic measurements and to save them to a text file. Later, these files are processed using MatLab.

Measurements results are shown below.

## 1) Pseudoresistor 1 .



Figure 10. Pseudoresistor 1 experimental results.
It can be observed that the experimental results do not match with simulation results, as the experimentally measured time constant is rather lower than that obtained by simulation. This fact highlights that simulators are not able to reproduce real circuit behavior, as MOS transistors working in cut-off are not properlymodeled.
2) Pseudoresistor 2.


Figure 11. Pseudoresistor 2 experimental results.
Once again, it can be observed that the experimental results do not match with those obtained by simulation. In this pseudoresistor, not only the time constant is different, there are also certain transient dynamic effects clearly visible in the experimental measurements which do not appear in the simulations. Once again, it can be concluded that the simulation model for the MOSFET working in the cutoff region is not accurate.

## VI. CONCLUSIONS

Circuits containing pseudoresistors implemented by transistors working in the cutoff region have shown to be extremely useful and versatile in many low power and low voltage applications. As a consequence, a thorough study of the transient behavior of different implementations of pseudoresistor implementations is required.

It has been revealed that many effects that are usually ignored when the transistors are working in active regions cannot be neglected when working in cutoff region. The study presented in this paper reveals the lack of a reliable model provided by standard simulators and highlights the need of developing a trustable model in order to gain an in-depth understanding of its behavior, in order to be able to control and exploit it. This is especially important for deep submicron technologies where additional effects such as drain and gate
leakage could change the dynamic behavior of these pseudoresistors.

The study presented here also addresses the problem associated to the long simulation times required by these structures, due to their extremely large time constants.

Presently, from the results presented here, an accurate and simple model for the transient behavior of these circuits is being developed, and new algorithms and methods to control them in a predictable way are being devised.

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# Bulk-Driven Three-stage Class-AB CMOS OTA 

E. Cabrera-Bernal<br>Electronic Engineering Department<br>University of Seville<br>Seville, Spain<br>ecabrera@gie.us.es

S. Pennisi, A. D. Grasso<br>DIEEI<br>University of Catania<br>Catania, Italy<br>salvatore.pennisi@dieei.unict.it


#### Abstract

In this paper a bulk-driven three-stage class-AB operational transconductance amplifier (OTA) is presented. The design is suitable for very low voltage design and, concretely, a 0.7 V supply voltage is applied. The OTA is designed in $180-\mathrm{nm}$ standard CMOS technology and achieves a 61 dB open loop gain and a unity gain bandwidth of 3.71 MHz while driving a capacitive load of 20 pF .


Keywords-Bulk-driven; Low-Voltage; OTA; class-AB; CMOS

## I. Introduction

The continuous downscaling of transistor size in CMOS technologies implies, unavoidably, the decrease of the supply voltage in order to ensure circuit reliability and lifespan. Moreover, electronic industry is continuously demanding for portable devices with increasingly operation time in order to satisfy modern lifestyle, where portable devices have become ubiquitous.

However, while supply voltages decrease, threshold voltages $\left(V_{T}\right)$ do not decrease in the same proportion. This is a main concern in analog design, where transistors operating in saturation are usually preferred to achieve higher transconductances, lower noise and overall better performance.

Therefore, in order to maintain good circuit performances in low voltage conditions, new topologies and design techniques must be developed to deal with low power supply and large $V_{T}$, while maintaining acceptable signal swing. Techniques such as floating gate transistors [1][1], level shifting techniques [2] or special low $V_{T}$ devices are some examples of low voltage techniques. Bulk-driven techniques have also been extensively used for low voltage design ([3][8]). In this approach, the bulk terminal of the MOS transistor is driven by the signal while the transistor is properly biased from its gate terminal. Applying the signal through the bulk allows modifying the $V_{T}$, thus modifying the current through the device and obtaining a bulk transconductance, $g_{m b}$.

In this paper, a bulk-driven three-stage class-AB amplifier, which works under $0.7-\mathrm{V}$ supply, is presented. A brief review of bulk driven technique is provided in Section II. The
proposed bulk-driven three-stage class-AB amplifier topology is presented in Sec. III. The main simulation results of the proposed amplifier, as well as a comparison with other sub 1-V amplifiers, are carried out in Sec. IV. Conclusions are drawn in Sec. V.

## II. Bulk Driven Technique

In traditional gate-driven transistors, the conductivity of the channel and, thus, the drain current, $I_{D}$, is usually controlled by the gate-source voltage $V_{G S}$, but, as already stated, the drain current can also be controlled by the bulk-source voltage $V_{B S}$. This is, normally, an unwanted parasitic effect but in a bulk driven transistor, the idea is to use that $g_{m b}$ instead of the source transconductance $g_{m}$. The bulk terminal has no threshold voltage associated and, as a result, the $V_{T}$ drawback is eliminated. This makes the technique especially suitable for low voltage design.

One of the main disadvantages of bulk driven technique is the fact that $g_{m b}$ is smaller than $g_{m}$, as shown in (1)

$$
\begin{equation*}
g_{m b}=\frac{\gamma g_{m}}{2 \frac{\varphi_{F}+V_{B S}}{2}}=\eta g_{m} \tag{1}
\end{equation*}
$$

where $\eta$ is usually between 0.2 and 0.4 . When designing amplifiers, this leads to poor DC gain performance, larger noise and offset. In the proposed structure a third stage is added in order to counteract the drawback of low DC gain.

Another issue that must be considered is the fact that the bulk-driven technique requires each bulk to be accessible, hence, in standard CMOS technologies, only p-channel transistors can be driven from the bulk.

## III. Proposed Bulk-Driven Class-AB Amplifier

The schematic of the proposed solution is shown in Fig.1. It is made up of three gain stages, namely the differential stage $M_{1}-M_{4}$, the second common-source stage $M_{5}-M_{6}$ and the third common-source stage $M_{7}-M_{8}$.


Fig. 1. Proposed bulk-driven three-stage class-AB amplifier.

The differential stage is made up of the bulk-driven differential pair, $M_{1}-M_{2}$, biased by diode-connected transistor, $M_{R}$, whose body is tied to the analog ground, i.e., $(\mathrm{VDD}+\mathrm{VSS}) / 2$. In this way, $M_{R}-M_{1}$ and $M_{R}-M_{2}$ form two current mirrors that accurately set the DC current, provided that also the body of $M_{1}-M_{2}$ is connected to the analog ground. The active load of the first stage is realized with transistors $M_{3}-M_{4}$. The use of resistors $R$ enables true differential mode operation from pair $M_{l}-M_{2}$ that is otherwise intrinsically pseudo differential. Indeed, the small-signal voltage at the drain of $M_{4}$ (output of the first stage) depends on both Vin+ and Vin-. The first stage DC gain can be approximated by $g_{m b} \cdot R$.

Resistors $R$ set also the common-mode voltage at the drain of $M_{3}-M_{4}$ to be equal to their gate voltage. The DC current in the second stage is set through current generator $M_{6}$, and thanks to the mirroring action between $M_{4}$ and $M_{5}$ (they have the same $\left.V_{G S}\right), M_{5}$ can be dimensioned so as to minimize systematic offset (by setting equal nominal DC current in $M_{5}$ and $M_{6}$ ). The last stage is biased by current generator $M_{8}$, whose current is set by the pseudo current mirror formed by $M_{4}$ and $M_{9}$. Note that this current is signal dependent and that increases when Vin+ increases. In other words, both $M_{7}$ and $M_{8}$ can deliver a large-signal current greater than the standby value, and therefore the third stage works in class $A B$.

Frequency compensation is obtained through Miller capacitors $C_{C 1}$ and $C_{C 2}$ and a current buffer implemented by $M_{3}-M_{4}$, with a technique similar to that developed in [9] for a nested Miller compensated OTA. Dominant pole is hence
achieved through $C_{C 1}$, and the unity-gain bandwidth (GBW) is equal to $g_{m b 1,2} / C_{C 1}$.

Transistors aspect ratios, as well as the main circuit devices values are summarized in Table I.

TABLE I. Transistors Dimensions and Devices Values.

| Device | Value | Device | Value |
| :---: | :---: | :---: | :---: |
| $\mathbf{M}_{\mathbf{1}}, \mathbf{M}_{\mathbf{2}}$ | $12 \mu \mathrm{~m} / 540 \mathrm{~nm}$ | $\mathbf{I}_{\mathbf{B}}$ | $4 \mu \mathrm{~A}$ |
| $\mathbf{M}_{\mathbf{3}}, \mathbf{M}_{\mathbf{4}}$ | $2 \mu \mathrm{~m} / 540 \mathrm{~nm}$ | $\mathbf{C}_{\mathbf{C} \mathbf{1}}$ | 500 fF |
| $\mathbf{M}_{\mathbf{5}}, \mathbf{M}_{\mathbf{6}}$ | $5 \mu \mathrm{~m} / 540 \mathrm{~nm}$ | $\mathbf{C}_{\mathbf{C} \mathbf{2}}$ | 50 fF |
| $\mathbf{M}_{\mathbf{7}}, \mathbf{M}_{\mathbf{8}}$ | $30 \mu \mathrm{~m} / 540 \mathrm{~nm}$ | $\mathbf{R}$ | $250 \mathrm{k} \Omega$ |
| $\mathbf{M}_{\mathbf{9}}$ | $2 \mu \mathrm{~m} / 540 \mathrm{~nm}$ | $\mathbf{C}_{\mathbf{L}}$ | 20 pF |
| $\mathbf{M}_{\mathbf{1 0}}$ | $12 \mu \mathrm{~m} / 540 \mathrm{~nm}$ | $\mathbf{V}_{\mathbf{D D}}$ | 0.7 v |
| $\mathbf{M}_{\mathbf{R}}$ | $12 \mu \mathrm{~m} / 540 \mathrm{~nm}$ |  |  |

## IV. Results

In this section, the main simulation results of the proposed amplifier are shown. At the end of the section, a brief comparison of performances among this amplifier and other low voltage amplifiers is also carried out.

Fig. 2 illustrates the frequency response of the proposed amplifier. The open loop gain is 61 dB and the unity-gain
bandwidth is 3.7 MHz . The phase margin resulted to be around $62^{\circ}$. The common mode rejection ratio, CMRR, and the power supply rejection ratio, PSRR, have also been simulated. Their DC values are 46.8 dB for the CMRR and 61.2 dB and 72.4 dB for the positive and negative PSRR, respectively.

The amplifier was connected in inverting unity gain configuration as shown in Fig. 3 ( $R a=R b=100 \mathrm{k} \Omega$ ). The response to an input step of 600 mV is illustrated in Fig. 4. The positive (negative) slew rate was $2.2 \mathrm{~V} / \mu \mathrm{s}(4.9 \mathrm{~V} / \mu \mathrm{s})$ besides, $1 \%$ settling time was 594 ns (positive step) and 379 ns (negative step), respectively. It is seen that an almost rail-torail output swing is achieved. The input common mode range (ICMR) is also in principle rail to rail but is, actually, set by the maximum allowed input current that flows into the bulk. Thus, it should be limited to 400 mV in order to maintain the input current below 3nA.


Fig. 2. Frequency respose of the proposed amplifier.
Main performance parameters of the proposed OTA are summarized in Table II. A comparison with other sub-1V amplifiers is also presented in Table III where a figure of merit (FOM) is included in order to make the comparison easier. The FOM is defined in (2), where $I$ is the standby current consumption and $C_{L}$ is the load capacitance [12]. Highperformance amplifiers are characterized by a larger FOM.

$$
\begin{equation*}
F O M=100 \cdot \frac{G B W \cdot C_{L}}{I} \tag{2}
\end{equation*}
$$

It is apparent from TABLE III. that the proposed solution exhibits the best FOM among the considered sub-1V amplifiers. The FOM value versus the year of publication for the amplifiers appearing in TABLE III. is also plotted in Fig. 5.


Fig. 3. Amplifier in inverting closed loop configuration.


Fig. 4. Step response of the proposed OTA in unty gain configuration.
TABLE II. RESULTS SUMMARY.

| Parameter | Value |
| :---: | :---: |
| Supply voltage [V] | 0.7 |
| Power dissipation [ uW ] | 22.4 |
| ICMR [mV] | 400 |
| Max Input current [nA] | 2.96 |
| Open Loop Gain [dB] | 61.07 |
| Open Loop Unity Gain BW [MHz] | 3.7 |
| Phase Margin [ ${ }^{\circ}$ ] | 62 |
| SR+/SR-[V/us] | 2.2/4.9 |
| 1\% Settling time (+/-) [ns] | 594/379 |
| CMRR@DC [dB] | 46.8 |
| PSRR+@DC [dB] | 61.2 |
| PSRR-@DC [dB] | 72.4 |
| Input Ref. Noise @1MHz [ $\mathrm{nV} / \sqrt{ } \mathrm{Hz}$ ] | 273 |
| THD $@ 100 \mathrm{kHz}(250 \mathrm{mV}$ input) [\%] | 0.058 |
| @ $250 \mathrm{kHz}(250 \mathrm{mV}$ input) [\%] | 0.460 |

## V. Conclusions

In this paper, a bulk-driven three-stage class-AB CMOS OTA, suitable for very low voltage supplies has been presented. Operation under 0.7 V was simulated using the models of a $180-\mathrm{nm}$ standard CMOS technology and results compared with the state-of-the-art sub-1V amplifiers. The proposed solution exhibits the best FOM. Future work will be aimed to balance the positive and negative slew rate in order to reduce the settling time and drive even larger load capacitors.

TABLE III. PERFORMANCE COMPARISON OF SUB-1V Amplifiers.

| Works | Technology <br> $[\boldsymbol{\mu m}]$ | $\mathbf{C}_{\mathbf{L}}$ <br> $[\mathbf{p F}]$ | $\mathbf{U G B W}$ <br> $[\mathbf{M H z}]$ | $\mathbf{P M}$ <br> $\left[{ }^{\circ}\right]$ | SR+/- <br> $[\mathbf{V} / \mathbf{u s}]$ | Supply <br> $[\mathbf{V}]$ | Power <br> $[\boldsymbol{\mu W}]$ | $\mathbf{F O M}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{1 9 9 8}[\mathbf{3 ]}$ | 2 | 22 | 1.3 | 57 | $0.7 / 1.6$ | 1 | 287 | 10 |
| $\mathbf{2 0 0 1 [ 4 ]}$ | 0.5 | - | 2 | 57 | 0.5 | 1 | 40 | 50 |
| $\mathbf{2 0 0 2 [ 5 ]}$ | 2.5 | - | 0.56 | 62 | - | 0.9 | 0.45 | 13.4 |
| $\mathbf{2 0 0 5 [ 6 ] \text { Bulk Driven (BD) }}$ | 0.18 | 20 | 2.5 | - | 2.89 | 0.5 | 110 | 22.7 |
| $\mathbf{2 0 0 5 [ 6 ] ~ G a t e ~ D r i v e n ~ ( G D ) ~}$ | 0.18 | 20 | 10 | - | 2 | 0.5 | 75 | 133.4 |
| $\mathbf{2 0 0 9 [ 7 ] ~}$ | 0.35 | 2.5 | 0.54 | 52 | - | 0.9 | 9.9 | 12.3 |
| $\mathbf{2 0 1 3 [ 8 ]}$ | 0.35 | 15 | 11.67 | 66 | $2.53 / 1.37$ | 1 | 197 | 88.9 |
| $\mathbf{2 0 0 0 [ 1 0 ]}$ | 1.2 | 15 | 1.9 | 61 | $0.8 / 1$ | 1 | 410 | 13.7 |
| 2003[11] | 0.25 | 18 | 1.2 | 60 | 0.2 | 0.8 | 8 | 218 |
| This work | 0.18 | 20 | 3.7 | 62 | $2.2 / 4.9$ | 0.7 | 22.4 | 231.8 |



Fig. 5. FOM vs Year of Publication for the amplifiers appearing in the comparison of TABLE III.

## ACKNOWLEDGMENT

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# 0.7-V Bulk-Driven Three-Stage Class-AB OTA 

E. Cabrera-Bernal<br>Electronic Engineering Department<br>University of Seville<br>Seville, Spain<br>ecabrera@gie.us.es

S. Pennisi, A. D. Grasso<br>DIEEI<br>University of Catania<br>Catania, Italy<br>[spennisi, agrasso]@dieei.unict.it


#### Abstract

A high-performance architecture for bulk-driven operational transconductance amplifiers (OTAs) is presented. The solution exploits a three-gain-stage topology and, as a distinctive behavior, provides an inherent class-AB performance with simple and robust standby current control. A 0.7-V supply OTA is designed using a $180-\mathrm{nm}$ standard CMOS technology. Post layout simulations show a 61-dB open loop gain and a unity gain bandwidth of 3.6 MHz , under a capacitive load of 20 pF . Significant performance improvement when compared to prior art is achieved, so that the best figure of merit is found.


Keywords—Bulk-driven; Low-Voltage; OTA; class-AB; CMOS

## I. InTRODUCTION

The continuous downscaling of transistor size in CMOS technologies implies, unavoidably, the decrease of the supply voltage in order to ensure circuit reliability and lifespan. Moreover, electronic industry is continuously demanding for portable devices with increasingly operation time in order to satisfy modern lifestyle, where portable devices have become ubiquitous.

However, while supply voltages decrease, threshold voltages $\left(V_{T}\right)$ do not decrease in the same proportion. This is a main concern in analog design, where transistors operating in saturation are usually preferred to achieve higher transconductances, lower noise and overall better performance.

Consequently, in order to preserve circuit performances in low voltage conditions, new topologies and design techniques must be developed to deal with low power supply and large $V_{T}$, while maintaining acceptable signal swing. Techniques such as floating gate transistors [1], level shifting [2] or employing special low $V_{T}$ devices are some examples of low voltage design approaches. Bulk-driven techniques have also been extensively exploited ([3]-[8]). In this approach, the bulk terminal of the MOS transistor is driven by the signal, while the transistor is properly biased from its gate terminal. Applying the signal through the bulk allows modifying the $V_{T}$, thus modifying the current through the device and obtaining a bulk transconductance, $g_{m b}$. The main drawback of this method is the low achievable transconductance that, especially in the design of amplifiers, implies low gain, low bandwidth and high noise.

In this paper, a bulk-driven class- AB operational transconductance amplifier (OTA) in $0.18-\mu \mathrm{m}$ CMOS, which works under $0.7-\mathrm{V}$ supply, is presented. The OTA provides
more than $60-\mathrm{dB}$ DC gain thanks to a three-stage architecture that is used to compensate for the transconductance reduction. The added stage, however, does not sacrifice the gainbandwidth product, which resulted larger than 3 MHz under a load capacitance of 20 pF , a value comparable with three-stage gate-driven OTAs under the same load and current consumption [9]. After a brief review of bulk driven technique in Section II, the proposed OTA topology is presented in Sec. III. The main post layout simulation results along with a comparison with other sub 1-V solutions are carried out in Sec. IV. Conclusions are drawn in Sec. V.

## II. Bulk Driven Technique

In traditional gate-driven transistors, the conductivity of the channel and, thus, the drain current, $I_{D}$, is controlled by the gate-source voltage $V_{G S}$, but, as already stated, the drain current can also be controlled by the bulk-source voltage $V_{B S}$. This is normally an unwanted parasitic effect, but in a bulk driven transistor the idea is to use that $g_{m b}$ instead of the source transconductance $g_{m}$. The bulk terminal has no threshold voltage associated and, as a result, the $V_{T}$ drawback is eliminated. This makes the technique especially suitable for low voltage design.

One of the main disadvantages of bulk driven technique is the fact that $g_{m b}$ is smaller than $g_{m}$, as quantified in (1)

$$
\begin{equation*}
g_{m b}=\frac{\gamma g_{m}}{2 \sqrt{2 \varphi_{F}+V_{B S}}}=\eta g_{m} \tag{1}
\end{equation*}
$$

where $\eta$ is usually between 0.2 and 0.4 . When designing amplifiers, this leads to poor DC gain performance, larger noise and offset. In the proposed structure a third stage is added in order to counteract the drawback of low DC gain.

Another issue that must be considered is the fact that the bulk-driven technique requires each bulk to be accessible, hence, in standard CMOS technologies, only $p$-channel transistors can be driven from the bulk.

## III. Proposed Bulk-Driven Class-AB Amplifier

The schematic of the proposed solution is shown in Fig.1. It is made up of three gain stages, namely the differential stage $M_{1}-M_{4}$, the second common-source stage $M_{5}-M_{6}$ and the third common-source stage $M_{7}-M_{8}$.
The differential stage is made up of the bulk-driven differential pair, $M_{1}-M_{2}$, biased by diode-connected transistor, $M_{R}$, whose body is tied to the virtual ground, i.e., $\left(\mathrm{V}_{\mathrm{DD}}+\mathrm{V}_{\mathrm{SS}}\right) / 2$
(it should be noted that the proposed structure can work under double or single supply). In this way, $M_{R}-M_{1}$ and $M_{R}-M_{2}$ form two current mirrors that accurately set the DC current, provided that also the body of $M_{1}-M_{2}$ is connected to the analog ground. The active load of the first stage is realized with transistors $M_{3}-M_{4}$. The use of resistors $R$ enables true differential mode operation from pair $M_{1}-M_{2}$ that is otherwise intrinsically pseudo differential. Indeed, the small-signal voltage at the drain of $M_{4}$ (output of the first stage) depends on both $V_{\text {in }}$ and $V_{i n \text {. }}$. The first stage DC gain can be approximated by $g_{m b} \cdot R$.


Fig. 1. Schematic diagram of the proposed OTA.

TABLE I. Transistors Dimensions and Devices Values.

| Device | Value | Parameter | Value |
| :---: | :---: | :---: | :---: |
| $\mathrm{M}_{\mathrm{R}}, \mathrm{M}_{1}, \mathrm{M}_{2}, \mathrm{M}_{10}$ | $12 \mu \mathrm{~m} / 540 \mathrm{~nm}$ | $I_{B}$ | $4 \mu \mathrm{~A}$ |
| $\mathrm{M}_{3}, \mathrm{M}_{4}, \mathrm{M}_{9}$ | $2 \mu \mathrm{~m} / 540 \mathrm{~nm}$ | $C_{C 1}$ | 550 fF |
| $\mathrm{M}_{5}, \mathrm{M}_{7}$ | $5 \mu \mathrm{~m} / 540 \mathrm{~nm}$ | $C_{C 2}$ | 30 fF |
| $\mathrm{M}_{6}, \mathrm{M}_{8}$ | $30 \mu \mathrm{~m} / 540 \mathrm{~nm}$ | $R$ | $250 \mathrm{k} \Omega$ |
| $C_{L}$ | 20 pF | $V_{D D}-V_{S S}$ | 0.7 V |

Resistors $R$ set also the common-mode voltage at the drain of $M_{3}-M_{4}$ to be equal to their gate voltage. The DC current in the second stage is set through current generator $M_{6}$, and thanks to the mirroring action between $M_{4}$ and $M_{5}$ (they have the same $\left.V_{G S}\right), M_{5}$ can be dimensioned so as to minimize systematic offset (by setting equal nominal DC current in $M_{5}$ and $M_{6}$ ). The last stage is biased by current generator $M_{8}$, whose current is set by the pseudo current mirror formed by $M_{4}$ and $M_{g}$. Note that this current is signal dependent and that increases when Vin+ increases. In other words, both $M_{7}$ and $M_{8}$ can deliver a large-signal current greater than the standby value, and therefore the third stage works in class $A B$.

Frequency compensation is obtained through Miller capacitors $C_{C 1}$ and $C_{C 2}$ and a current buffer implemented by $M_{3}-M_{4}$, with a technique similar to that developed in [10] for a nested Miller compensated OTA. Dominant pole is hence
achieved through $C_{C 1}$, and the unity-gain bandwidth (GBW) is equal to $g_{m b 1,2} / C_{C 1}$.

Transistors aspect ratios, as well as the main circuit devices values are summarized in Tab. I.

## IV. Post Layout Simulation Results

The OTA shown in fig. 1 was designed in a $180-\mathrm{nm}$ standard CMOS technology. The layout of the amplifier is shown in fig. 2. The occupied area is $120 \times 165 \mu \mathrm{~m}^{2}$.

Figure 3 illustrates the frequency response of the proposed amplifier. The open loop gain is 61 dB and the unity-gain bandwidth is 3.6 MHz . The phase margin resulted to be around $60^{\circ}$. The common mode rejection ratio, CMRR, and the power supply rejection ratio, PSRR, have also been simulated. Their DC values are 46.7 dB for the CMRR and $60.2 \mathrm{~dB} / 72.6 \mathrm{~dB}$ for the positive/negative PSRR, respectively.

The amplifier was connected in inverting unity gain configuration as shown in Fig. $4 \quad\left(R_{a}=R_{b}=100 \mathrm{k} \Omega\right)$. The response to an input step of 600 mV is illustrated in Fig. 5. The positive (negative) slew rate was $2 \mathrm{~V} / \mu \mathrm{s}(4.4 \mathrm{~V} / \mu \mathrm{s})$ besides, $1 \%$ settling time was 733 ns (positive step) and 380 ns (negative step), respectively. It is seen that an almost rail-to-rail output swing is achieved. The input common mode range (ICMR) is also in principle rail to rail but is actually set by the maximum allowed input current that flows into the bulk. Thus, it should be limited to 400 mV in order to maintain the input current below 4 nA .


Fig. 2. Layout of the proposed amplifier, area is $120 \times 165 \mu \mathrm{~m}^{2}$.

Main performance parameters of the proposed OTA are summarized in Tab. II.

The effect of temperature and process variations on the amplifier's performance has been investigated via corner simulations at $27^{\circ} \mathrm{C},-40^{\circ} \mathrm{C}, 125^{\circ} \mathrm{C}$. Results are summarized in Tab. III. The proposed amplifier remains stable across the extreme temperature and process corners.

A comparison with other sub-1V amplifiers is also presented in Tab. IV where a figure of merit (FOM) is included in order to make the comparison easier. The FOM is defined as [9]

$$
\begin{equation*}
F O M=100 \cdot \frac{G B W \cdot C_{L}}{I_{D D}} \tag{2}
\end{equation*}
$$

where $I_{D D}$ is the standby current consumption and $C_{L}$ is the load capacitance. High-performance amplifiers are characterized by a larger FOM.

The FOM value versus the year of publication for the amplifiers appearing in TABLE IV. is also plotted in Fig. 6. It is apparent from TABLE IV. that the proposed solution exhibits the best FOM. Besides, it provides one of the highest GBW values with reduced DC current consumption.


Fig. 3. Frequency response of the proposed amplifier (magnitude and phase).


Fig. 4. Amplifier in inverting closed loop configuration.


Fig. 5. Step response of the proposed OTA in inverting unity gain configuration.

TABLE II. Simulation Results Summary ( $\left.\mathrm{C}_{\mathrm{L}}=20 \mathrm{PF}\right)$.

| Parameter | Value |
| :---: | :---: |
| Supply voltage ( $\mathrm{V}_{\mathrm{DD}}-\mathrm{V}_{\mathrm{Ss}}$ ) [V] | 0.7 |
| Power dissipation [ $\mu \mathrm{W}$ ] | 22.4 |
| ICMR [mV] | 400 |
| Max Input current [nA] | 3.5 |
| Open Loop Gain [dB] | 61 |
| GBW [MHz] | 3.6 |
| Phase Margin [deg] | 60 |
| Gain Margin | 5.08 |
| SR+/SR- [V/ $\mu \mathrm{s}$ ] | 2/4.4 |
| 1\% Settling time (+/-) [ns] | 733/380 |
| CMRR@DC [dB] | 46.7 |
| PSRR+@DC [dB] | 60.2 |
| PSRR-@DC [dB] | 72.6 |
| Input Ref. Noise @1MHz [nV/ $\sqrt{\text { Hz}}]$ | 273 |
| $\begin{gathered} \text { THD } \\ @ 100 \mathrm{kHz}, 250 \mathrm{mV} \text { input [\%] } \end{gathered}$ | 0.061 |
| $\begin{gathered} \text { THD } \\ @ 250 \mathrm{kHz}, 250 \mathrm{mV} \text { input [\%] } \end{gathered}$ | 0.509 |

TABLE III. Main performance parameters Over Process and TEmperature Variations.
$\mathrm{T}=27^{\circ} \mathrm{C}$

| Corner | TT | FF | SS | SF | FS |
| :---: | :---: | :---: | :---: | :---: | :---: |
| DC Gain [dB] | 60.9 | 61.3 | 60.2 | 61.1 | 60.6 |
| GBW [MHz] | 3.57 | 3.70 | 3.41 | 3.54 | 3.57 |
| $\mathbf{P M}\left[{ }^{\circ}\right]$ | 59.74 | 61.2 | 58.90 | 60.57 | 59.28 |
| GM [dB] | 5.08 | 5.06 | 5.32 | 5.16 | 5.15 |
| SR+/SR- [V/ $/ \mathbf{\mu s}]$ | $1.9 / 4.5$ | $2.4 / 6.2$ | $1.5 / 3.3$ | $1.9 / 5.7$ | $1.8 / 3.5$ |
| $\mathbf{1 \% ~ T s}+/ \mathbf{T s}-[\mathbf{n s}]$ | $733 / 380$ | $655 / 366$ | $843 / 408$ | $729 / 378$ | $761 / 391$ |

$\mathrm{T}=125^{\circ} \mathrm{C}$

| Corner | TT | FF | SS | SF | FS |
| :---: | :---: | :---: | :---: | :---: | :---: |
| DC Gain $[\mathbf{d B}]$ | 58.4 | 58.4 | 58.1 | 58.2 | 58.4 |
| GBW [MHz] | 3.15 | 3.24 | 3.04 | 3.10 | 3.18 |
| PM [$]$ | 56.81 | 58.45 | 55.90 | 57.87 | 56.20 |
| GM [dB] | 5.10 | 5.20 | 5.16 | 5.28 | 5.03 |
| SR+/SR- $[\mathbf{V} / \boldsymbol{\mu s}]$ | $1.4 / 4.3$ | $1.5 / 5.7$ | $1.2 / 3.3$ | $1.4 / 5.3$ | $1.3 / 3.5$ |
| $\mathbf{1 \%} \mathbf{T s}+/ \mathbf{T s}-[\mathbf{n s}]$ | $803 / 418$ | $643 / 403$ | $896 / 442$ | $698 / 414$ | $837 / 426$ |

$\mathrm{T}=-40^{\circ} \mathrm{C}$

| Corner | TT | FF | SS | SF | FS |
| :---: | :---: | :---: | :---: | :---: | :---: |
| DC Gain [dB] | 62.0 | 62.6 | 60.7 | 62.3 | 61.1 |
| GBW [MHz] | 4.01 | 4.17 | 3.77 | 3.99 | 3.96 |
| $\left.\mathbf{P M ~}^{\circ}{ }^{\circ}\right]$ | 60.59 | 61.90 | 59.72 | 61.11 | 60.22 |
| GM [dB] | 5.27 | 5.13 | 5.74 | 5.28 | 5.53 |
| SR+/SR- [V/ $\mathbf{\mu s}]$ | $1.9 / 4.4$ | $2.6 / 6.5$ | $1.4 / 3.1$ | $1.9 / 5.9$ | $1.7 / 3.2$ |
| $\mathbf{1 \%} \mathbf{T s}+/ \mathbf{T s}-[\mathbf{n s}]$ | $706 / 340$ | $603 / 329$ | $871 / 357$ | $705 / 339$ | $755 / 346$ |

TABLE IV. PERFORMANCE COMPARISON OF SUB-1V AMPLIFIERS.

| Works ${ }^{\text {b }}$ |  | Technology [ $\mu \mathrm{m}$ ] | Supply [V] | $\begin{aligned} & \text { DC Current } \\ & {[\mu \mathrm{A}]} \end{aligned}$ | $\begin{gathered} \mathbf{C}_{\mathbf{L}} \\ {[\mathbf{p F}]} \end{gathered}$ | DC Gain [dB] | $\begin{aligned} & \text { GBW } \\ & {[\mathbf{M H z}]} \end{aligned}$ | $\underset{\left.{ }^{\circ}{ }^{\circ}\right]}{\mathbf{P M}}$ | $\begin{aligned} & \mathrm{SR}+/- \\ & {[\mathrm{V} / \mu \mathrm{s}]} \end{aligned}$ | $\begin{gathered} \text { FOM } \\ {[\mathrm{MHz} \cdot \mathbf{p F} / \mu \mathrm{A}]} \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1998 [3] | GD | 2 | 1 | 287 | 22 | 48.8 | 1.3 | 57 | 0.7/1.6 | 10 |
| 2001 [4] | BD | 0.5 | 1 | 40 | 20 | 62-69 | 2 | 57 | 0.5 | 100 |
| 2002 [5] | BD | 2.5 | 0.9 | 0.5 | 12 | 79 | 0.56 | 62 | - | 13.4 |
| 2005 [6] | BD | 0.18 | 0.5 | 220 | 20 | 52 | 2.5 | - | 2.89 | 22.7 |
|  | GD | 0.18 | 0.5 | 150 | 20 | 62 | 10 | - | 2 | 133.4 |
| 2009 [7] | BD | 0.35 | 0.9 | 11 | 2.5 | 62 | 0.54 | 52 | - | 12.3 |
| 2013 [8] | BD | 0.35 | 1 | 197 | 15 | 88.3 | 11.67 | 66 | 2.53/1.37 | 88.9 |
| 2000 [11] | GD | 1.2 | 1 | 410 | 15 | 87 | 1.9 | 61 | 0.8/1 | 6.9 |
| 2014 [12] | BD | 0.13 | 0.25 | 0.072 | 15 | 40 | 0.002 | 52 | 0.71 | 42 |
| 2013 [13] ${ }^{\text {a }}$ | BD | 0.05 | 0.5 | 200 | 20 | 74 | 4.8 | $49^{\circ}$ | 3.4 | 0.48 |
| This work ${ }^{\text {a }}$ | BD | 0.18 | 0.7 | 32 | 20 | 61 | 3.6 | 60 | 2/4.4 | 225 |

${ }^{\text {a }}$ Simulations.
${ }^{\mathrm{b}}$ BD: Bulk Driven. GD: Gate Driven.


Fig. 6. FOM vs Year of publication for the amplifiers appearing in TABLE IV.

## IV. CONCLUSIONS

In this paper, a bulk-driven three-stage class- AB CMOS OTA, suitable for very low voltage supplies has been presented. Operation under 0.7 V was demonstrated through simulations using the models of a $180-\mathrm{nm}$ standard CMOS technology. Compared to the state-of-the-art sub-1V amplifiers, the proposed solution exhibits a significant improvement in small-signal and large-signal performance thanks to an efficient class AB configuration, as a result, it presents the best FOM. Future work will be aimed to balance the positive and negative slew rate in order to reduce the settling time and drive even larger load capacitors. Besides, fully-differential solutions to increase signal swing and CMRR should be developed.

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# 0.7-V Three-Stage Class-AB CMOS Operational Transconductance Amplifier 

Elena Cabrera-Bernal, Student Member, IEEE, Salvatore Pennisi, Senior Member, IEEE, Alfio Dario Grasso, Senior Member, IEEE, Antonio Torralba, Senior Member, IEEE, and Ramón Gonzalez Carvajal, Senior Member, IEEE


#### Abstract

A simple high-performance architecture for bulkdriven operational transconductance amplifiers (OTAs) is presented. The solution, suitable for operation under sub 1-V single supply, is made up of three gain stages and, as an additional feature, provides inherent class-AB behavior with accurate and robust standby current control. The OTA is fabricated in a $180-\mathrm{nm}$ standard CMOS technology, occupies an area of $19.8 \cdot 10^{-3} \mathrm{~mm}^{2}$ and is powered from 0.7 V with a standby current consumption of around $36 \mu \mathrm{~A}$. DC gain and unity gain frequency are 57 dB and 3 MHz , respectively, under a capacitive load of 20 pF . Overall good large-signal and small-signal performances are achieved, making the solution extremely competitive in comparison to the state of the art.


Index Terms-Bulk-driven, class-AB, CMOS analog integrated circuits, low-voltage, operational transconductance amplifier.

## I. Introduction

0NE of the main trends of modern consumer electronics industry is towards the extension of portable devices autonomy through the adoption of low power design techniques [1]-[5]. This has reinforced the interest in the development of low-voltage design approaches and techniques for the limitation of power consumption. Considering the CMOS technology, the most straightforward methodologies to enable operation below $1-\mathrm{V}$ supplies are subthreshold biasing and bulk driving (or body driving) and even a combination of both [6]-[20].

Subthreshold transistors can be biased with currents in the range of a few nanoamperes, but this also implies low unitygain frequency and low achievable slew rate values. Therefore, subthreshold operation is particularly suitable in wireless sensor networks, biomedical applications and in all those applications where speed is not a concern, e.g., for bandwidth specifications in the range of a few kilohertz [21].

[^4]

Fig. 1. Schematic diagram of the proposed OTA.
As said, bulk-driven has also been exploited extensively for low voltage applications. While in traditional gate-driven transistors, the conductivity of the channel and, hence, the drain current, $I_{D}$, is controlled by the gate-source voltage $V_{G S}$, in bulk driven transistors the drain current is controlled by the bulk-source voltage $V_{B S}$. The main idea is to use the bulk transconductance, $g_{m b}$, instead of the gate transconductance, $g_{m}$, since the bulk terminal has no threshold voltage associated and, as a result, the $V_{T}$ limitation is eliminated. Note that the bulk-driven technique requires the MOS bulk terminal to be accessible, hence, in standard $n$-well CMOS technologies, only $p$-channel transistors can be utilized. One of the main disadvantages of the bulk driven technique is the fact that $g_{m b}=\gamma g_{m} / 2 \sqrt{2 \varphi_{F}+V_{B S}}=\eta g_{m}$, with $0.1<\eta<0.4$. This means that $g_{m b}$ is smaller than $g_{m}$ and, specifically for amplifiers design, this leads to poor DC gain and gain-bandwidth performance with larger noise and offset.

In this paper, a high performance bulk-driven three-stage class-AB amplifier topology able to work under sub- 1 V supply is presented. To provide adequate DC gain, the solution adopts a three-gain stage architecture, as also recently proposed in [22]-[24] for a subthreshold OTA. The proposed topology will be thoroughly explained and analyzed with the derivation of useful design equations in Sections II and III. Implementation and experimental results are presented in Sections IV as well as a comparison with other similar amplifiers. Some conclusions are drawn in Section V.

## II. Circuit Description

The schematic of the proposed OTA is shown in Fig. 1. As already mentioned, it is made up of three gain stages,
namely the differential stage $M_{1}-M_{4}$, the second commonsource stage $M_{5}-M_{6}$ and the third common-source stage $M_{7}-M_{10}$.

Transistor $M_{R}$, whose body is tied to the virtual ground, i.e., $\left(V_{D D}+V_{S S}\right) / 2$, sets through mirror ratios the quiescent current of the differential pair $M_{1}-M_{2}$ and of its load $M_{3}-M_{4}$, as well as of transistor $M_{6}$ acting as a load of the second stage. Indeed, $M_{R}-M_{1}$ and $M_{R}-M_{2}$ form two current mirrors that accurately set the DC current in the pair, provided that also the body of $M_{1}-M_{2}$ is connected to the analog ground. The active load of the first stage is realized with transistors $M_{3}-M_{4}$ and two resistors, R. Due to the fact that no DC current flows through resistors, the drains of $M_{3}-M_{4}$ are at the same potential of their gates and, consequently, the DC current of M5 is also accurately set by (pseudo) current-mirror ratios

$$
\begin{equation*}
I_{D 5}=\frac{I_{D 4}\left(\frac{W}{L}\right)_{5}}{\left(\frac{W}{L}\right)_{4}} \tag{1}
\end{equation*}
$$

The excellent matching between the DC currents of $M_{5}$ and $M_{6}$, causes the drain of $M_{5}$ to be theoretically at the same potential of the drain of $M_{4}$, ultimately defining the current of $M_{7}$, again through a mirror ratio

$$
\begin{equation*}
I_{D 7}=\frac{I_{D 4}\left(\frac{W}{L}\right)_{7}}{\left(\frac{W}{L}\right)_{4}} \tag{2}
\end{equation*}
$$

Note that current $I_{D 8}$ is set through current mirror $M_{8}-$ $M_{10}$ and pseudo-current mirror $M_{9}-M_{4}$. Therefore, to theoretically nullify systematic offset, $I_{D 8}$ must be equal to $I_{D 7}$ leading to

$$
\begin{equation*}
\frac{\left(\frac{W}{L}\right)_{8}\left(\frac{W}{L}\right)_{9}}{\left[\left(\frac{W}{L}\right)_{10}\left(\frac{W}{L}\right)_{4}\right]}=\frac{\left(\frac{W}{L}\right)_{7}}{\left(\frac{W}{L}\right)_{4}} \tag{3}
\end{equation*}
$$

In our design $(W / L)_{9}=(W / L)_{4}$ was assumed for simplicity, but $(W / L)_{9}<(W / L)_{4}$ could be used to slightly reduce current consumption. The minimum supply voltage ( $V_{D D}-$ $\left.V_{S S}\right)$ can be as low as $V_{D S 1,2}+V_{G S 3,4}$.

A final comment regards the class AB behavior of the third stage. Both transistors $M_{7}$ and $M_{8}$ can deliver a maximum signal current that is not limited by any DC value. Indeed, $M_{7}$ is in common source configuration, whereas the current in $M_{8}$ increases when $V_{\text {in+ }}$ increases because $v_{G S 9}$ also increases.

## III. Analysis and Design

In this section the main behavior of the proposed amplifier will be analyzed and design equations derived.

## A. Differential Gain

The use of resistors $R$ in the active load of the input stage enables fully differential operation of an otherwise pseudodifferential pair $M_{1}-M_{2}$. To understand this fact, let us apply a single-ended small-signal voltage, $v_{d}$, at one input (e.g., the body of $M_{1}$ ), while grounding the second input. Referring to Fig. 3, voltage $v_{d}$ is converted into a current, $g_{m b 1} v_{d}$, one half


Fig. 2. Equivalent circuit used for demonstrating the differential behavior of the adopted solution.
of which will flow through the resistor series and the other half through transistor $M_{3}$, because $M_{3}$ and $M_{4}$ have the same $v_{g s}$, have the same transconductance and must consequently carry the same current. Fig. 2 shows then that a differential output voltage, $v_{o 1}-v_{o 2}$, is generated. The expression of the individual output voltages is approximated by ${ }^{1}$ :

$$
\begin{align*}
& v_{o 1}=v_{g s}-g_{m b 1} R \frac{v_{d}}{2}=g_{m b 1}\left(\frac{1}{g_{m 3}}-R\right) \frac{v_{d}}{2}  \tag{4a}\\
& v_{o 2}=v_{g s}+g_{m b 1} R \frac{v_{d}}{2}=g_{m b 1}\left(\frac{1}{g_{m 3}}+R\right) \frac{v_{d}}{2} \tag{4b}
\end{align*}
$$

where in the second equality we used the following result: $g_{m b 1}\left(v_{d} / 2\right)=g_{m 3} v_{g s}$. Given that $g_{m b 1}=g_{m b 2}=g_{m b 1,2}$ and $g_{m 3}=g_{m 4}=g_{m 3,4}$. Assuming that $g_{m 3,4} R \gg 1$, then (4a), (4b) yield $v_{o 1}=-v_{o 2} \cong g_{m b 1,2} R\left(v_{d} / 2\right)$, demonstrating differential operation, since the application of $v_{d}$ from only one input terminal produces a differential output, as opposed to a pseudodifferential topology.

For the symmetry of the circuit, the same result holds also if we apply the input signal from the body of $M_{2}$. As a conclusion, the (single ended) gain of this first stage, $v_{o 2} / v_{d}$ can be approximated by $g_{m b 1,2} R / 2$. This outcome can be easily understood by referring to the fact that under small-signal differential input the gate of $M_{3}-M_{4}$ is at virtual ground and therefore the load seen by the couple $M_{1}-M_{2}$ is $R$ (or, more accurately, $R / / r_{d s 1} / / r_{d s 3}$, as explained in footnote 1 ).

From the above considerations, it follows that the proposed solution is well suited to implement a fully differential OTA. In this paper, for the sake of simplicity, we will limit the design to a single-ended topology to focus our attention on the operating principles and to determine basic design equations.

## B. Common Mode Rejection Ratio

Resistors R have the additional role of setting the commonmode voltage at the drain of $M_{3}-M_{4}$ to be equal to their gate voltage (because no current flows in the resistors under common-mode input). Referring to Fig. 3, under common mode

[^5]

Fig. 3. Differential input stage CMRR analysis.
input no current flows onto resistors R and $g_{m b 2} v_{c m}$ must equal $g_{m 3} v_{g s}$. Therefore, the common mode gain is

$$
\begin{equation*}
A_{c m}=\frac{v_{o 2}}{v_{c m}}=-\frac{g_{m b 1,2}}{g_{m 3,4}} \tag{5}
\end{equation*}
$$

This outcome can be easily understood by considering that if no current flows through the resistors then $M_{3}$ and $M_{4}$ operate as they are connected in diode and offer an equivalent resistance equal to $1 / g_{m 3,4}$.

The (single ended) common mode rejection ratio, defined as $\left|A_{d} / A_{c m}\right|$, is hence

$$
\begin{equation*}
\mathrm{CMRR}=\left|\frac{A_{d}}{A_{c m}}\right|=\frac{1}{2} \frac{g_{m b 1,2} R}{\frac{g_{m b 1,2}}{g_{m 3,4}}}=\frac{1}{2} g_{m 3,4} R \tag{6}
\end{equation*}
$$

From (6) we see that $R \gg 1 / g_{m 3,4}$ must be chosen to obtain adequate CMRR values.

## C. Frequency Compensation

Frequency compensation of the differential (open loop) gain is obtained through Miller capacitors $C_{C 1}$ and $C_{C 2}$ and a current buffer [25] implemented by $M_{3}-M_{4}$, with a technique similar to that developed in [26] for a nested-Millercompensated OTA. Dominant pole is hence achieved through $C_{C 1}$. Assuming both $g_{m i} r_{o i}, g_{m i} R \gg 1$, where $g_{m i}$ is the gate transconductance of transistor $i$ and $r_{o j}$ is the resistance of the output node of the amplifier $j$ th stage, the OTA loop gain transfer function can be approximated as

$$
\begin{equation*}
A(s) \approx A_{0} \frac{1+\frac{s}{z_{1}}}{\left(1+\frac{s}{p_{1}}\right)\left(a s^{2}+b s+1\right)} \tag{7}
\end{equation*}
$$

where the DC gain, $A_{0}$, the dominant pole, $p_{1}$, and the zero, $z_{1}$, are given by ${ }^{2}$

$$
\begin{align*}
A_{0} & =\frac{g_{m b 1,2} g_{m 5} g_{m 7}\left(R / / r_{o 1}\right) r_{o 2} r_{o 3}}{2}  \tag{8a}\\
p_{1} & =\frac{2}{g_{m 5} g_{m 7}\left(R / / r_{o 1}\right) r_{o 2} r_{o 3} C_{C 1}}  \tag{8b}\\
z_{1} & =\frac{g_{m 5} g_{m 3}}{2 C_{C 1} g_{m 5}-C_{C 2} g_{m 3}} \tag{8c}
\end{align*}
$$

[^6]And for the remaining non-dominant complex conjugate poles, the coefficients of the polynomial in (7) are

$$
\begin{align*}
a & =\frac{C_{C 2} C_{L}\left(2 g_{m 5}+g_{m 3}\right)}{g_{m 3} g_{m 5} g_{m 7}}  \tag{9a}\\
b & =\frac{C_{C 1} C_{L}+C_{C 2} C_{L} g_{m 5} r_{o 2}}{C_{C 1} g_{m 5} g_{m 7} r_{o 2}} \tag{9b}
\end{align*}
$$

The damping coefficient of this pair of complex poles is given by

$$
\begin{equation*}
\xi=\frac{b}{2 \sqrt{a}}=\frac{C_{C 1}+C_{C 2} g_{m 5} r_{o 2}}{2 C_{C 1} r_{o 2}} \sqrt{\frac{C_{L} g_{m 3}}{g_{m 5} g_{m 7} C_{C 2}\left(2 g_{m 5}+g_{m 3}\right)}} . \tag{10}
\end{equation*}
$$

Given $g_{m b 1,2}, C_{L}$, and $C_{C 1}$, one can derive from (10) a suitable value of $C_{C 2}$ in order to avoid peaking in the frequency response and to obtain a phase margin in the range of 60 to $70^{\circ}$. Besides, $g_{m 5} / g_{m 3}>C_{C 2} /\left(2 C_{C 1}\right)$ can be chosen in order to obtain a negative zero from (8c) useful to increase the phase margin.

From (8a) and (8b) the gain-bandwidth product, $\omega_{G B W}$, is

$$
\begin{equation*}
\omega_{G B W}=\frac{g_{m b 1,2}}{C_{C 1}} \tag{11}
\end{equation*}
$$

## D. Noise

Noise in multistage amplifiers is usually dominated by the first stage provided that this first stage has a voltage gain considerably larger than the unity. Considering only white noise for simplicity, the equivalent input-referred noise voltage power spectral density (PSD) of the proposed amplifier can be approximated as (see the Appendix for the calculation of the inputreferred equivalent noise contribution of resistors, $S_{V R, \text { in }}$ )

$$
\begin{align*}
S_{V, i n} \approx & 2 S_{V 1,2}\left(\frac{g_{m 1,2}}{g_{m b 1,2}}\right)^{2}+2 S_{V 3,4}\left(\frac{g_{m 3,4}}{g_{m b 1,2}}\right)^{2}+S_{V R, i n} \\
= & 2 \frac{2}{3} 4 k T \frac{1}{g_{m b 1,2}}\left(\frac{g_{m 1,2}}{g_{m b 1,2}}+\frac{g_{m 3,4}}{g_{m b 1,2}}\right) \\
& +4 k T R\left(\frac{1}{g_{m b 1,2} r_{o 1}}\right)^{2}\left[1+\left(1+\frac{2 r_{o 1}}{R}\right)^{2}\right] \\
\approx & \frac{16}{3} k T \frac{1}{g_{m b 1,2}} \frac{g_{m 1,2}+g_{m 3,4}}{g_{m b 1,2}} \tag{12}
\end{align*}
$$

where $S_{V i}$ is the gate-referred noise voltage PSD of the $i$-th transistor and $k$ and $T$ are the Boltzmann's constant and the absolute temperature.

In the above expression noise from $M_{R}$ was neglected since it is seen as a common-mode signal and rejected. Besides, also the noise from $R$ results to be negligible provided that $\left(g_{m 1,2}+\right.$ $\left.g_{m 3,4}\right) r_{o 1} \gg(3 / 4)\left(R / r_{o 1}\right)\left[1+\left(1+\left(2 r_{o 1} / R\right)\right)^{2}\right]$. This condition is usually met.

Finally, it is also seen from (12) that to make noise of $M_{3,4}$ negligible, $g_{m 3,4} \ll g_{m 1,2}$ must be selected, yielding

$$
\begin{equation*}
S_{V, \text { in }} \approx \frac{16}{3} k T \frac{1}{g_{m b 1,2}} \frac{1}{\eta}=\frac{16}{3} k T \frac{1}{g_{m 1,2}}\left(\frac{1}{\eta}\right)^{2} \tag{13}
\end{equation*}
$$

However, $g_{m 3,4} \ll g_{m 1,2}$ cannot be easily set since large $g_{m 3,4}$ values are needed from (6) to achieve sufficient $C M R R$ without requiring excessive $R$ values.

TABLE I
Transistors Dimensions and Device Values

| Device | Value | Parameter | Value |
| :---: | :---: | :---: | :---: |
| $\mathrm{M}_{\mathrm{R}}, \mathrm{M}_{1}, \mathrm{M}_{2}, \mathrm{M}_{10}$ | $12 \mu \mathrm{~m} / 540 \mathrm{~nm}$ | $I_{B}$ | $4 \mu \mathrm{~A}$ |
| $\mathrm{M}_{3}, \mathrm{M}_{4}, \mathrm{M}_{9}$ | $2 \mu \mathrm{~m} / 540 \mathrm{~nm}$ | $C_{C 1}$ | 550 fF |
| $\mathrm{M}_{5}, \mathrm{M}_{7}$ | $5 \mu \mathrm{~m} / 540 \mathrm{~nm}$ | $C_{C 2}$ | 30 fF |
| $\mathrm{M}_{6}, \mathrm{M}_{8}$ | $30 \mu \mathrm{~m} / 540 \mathrm{~nm}$ | $R_{1}, R_{2}$ | $250 \mathrm{k} \Omega$ |
| $C_{L}$ | 20 pF | $V_{D D}-V_{S S}$ | 0.7 V |

TABLE II
Transconductances (Simulated)

| Transconductance | Value <br> $[\boldsymbol{\mu} \mathbf{A} / \mathbf{V}]$ |
| :---: | :---: |
| $g_{m b 1,2}$ | 12 |
| $g_{m 1,2}$ | 65 |
| $g_{m 3,4}$ | 65 |
| $g_{m 5}$ | 162 |
| $g_{m 7}$ | 150 |

## E. Slew Rate

In multi-stage amplifiers, the slew rate, $S R$, is dictated by the slowest stage, i.e., $S R=\min \left[I_{x} / C_{x}\right]$, where $I_{x}$ is the maximum charging or discharging current and $C_{x}$ the load capacitor of $x$-th stage. If, as usual, the load capacitor is the largest one, then the output node is the most critical regarding the slew rate performance. This problem is alleviated if the last stage operates in class $A B$, leaving $S R$ essentially determined by the first stage that drives the largest of the two compensation capacitors. Assuming $C_{C 1} \gg C_{C 2}$, slew rate can be expressed as

$$
\begin{equation*}
S R \approx \frac{\left(I_{D 1}-I_{D 1, \max }\right)}{C_{C 1}} \tag{14}
\end{equation*}
$$

where $I_{D 1}-I_{D 1 \text {, max }}$ is the minimum current charging capacitor $C_{C 1}$ as $I_{D 1}$ is the quiescent current of $M_{1}$ and $I_{D 1, \text { max }}$ is the maximum instantaneous value. Current driving $C_{C 1}$ under large signals can be considerably different from the quiescent $I_{D 1,2}$ value. Indeed, assuming a buffer configuration, for positive-going input voltage steps the current available from $M_{1}$ decreases as $V_{T H 1}$ increases, whereas for negative-going steps the current available from $M_{1}$ increases. This yields to an unbalanced $S R$ performance with $S R^{+}<S R^{-}$.

## IV. Implementation and Experimental Validation

In order to validate the proposed OTA topology and associated design criteria, the amplifier in Fig. 1 was implemented in a $180-\mathrm{nm}$ standard CMOS technology (thresholds around 0.4 V ) under a $0.7-\mathrm{V}$ single supply. Aspect ratios and standby currents were set in order to achieve a unity gain-bandwidth of 3.5 MHz with a load capacitor of 20 pF and a damping factor of the complex conjugated poles equal to 0.5 .

The transistors aspect ratios together with the main circuit design parameters are summarized in Table I. The transconductances are summarized in Table II. Observe that $g_{m 3,4}=$ $g_{m 1,2}=65 \mu \mathrm{~A} / \mathrm{V}$ was chosen and that the two resistors $R$ were set to $250 \mathrm{k} \Omega$ in order to find a trade-off between acceptable noise performance from (12) and sufficient CMRR from (6). Resistors are implemented with $1792 \Omega / \square$ high resistive poly. Each resistor occupies $13.47 \mu \mathrm{~m} \times 1.67 \mu \mathrm{~m}$.


Fig. 4. Layout over microphotograph of the fabricated amplifier.


Fig. 5. Monte Carlo results for the standby current of the third stage.

Fig. 4 shows the layout of the amplifier superimposed to the microphotograph of the chip. The OTA occupies a silicon area of $19.8 \cdot 10^{-3} \mathrm{~mm}^{2}$.

To check the robustness of the standby current control in the last stage of the OTA we performed 1000 Monte Carlo iterations (process and mismatch). Fig. 5 summarizes the simulated results. The mean of the standby current of the last stage is $8.94 \mu \mathrm{~A}$ and the standard deviation is only $0.66 \mu \mathrm{~A}$ (the nominal designed value is $10 \mu \mathrm{~A}$ ). Of course, any output mismatch current, $i_{o, o s}$, when referred the input produces an offset voltage $v_{i, o s}=i_{o, o s} /\left(g_{m b 1,2} R / / r_{o 1} g_{m 5} r_{o 2} g_{m 7}\right)$. For instance, with the circuit parameters $2 \mu \mathrm{~A}$ of $i_{o, o s}$ produces about 0.24 mV of input offset.

Fig. 6 illustrates the postlayout simulation of the Bode plot (magnitude and phase) of the loop gain, as well as process and mismatch Monte Carlo results for DC gain, GBW and phase margin for 1000 iterations. For the nominal case, the DC gain is 61 dB and GBW is 3.5 MHz , with phase margin of $59^{\circ}$. Standard deviations are respectively, $0.7 \mathrm{~dB}, 200 \mathrm{kHz}$, and $2.2^{\circ}$, showing that the proposed solution is robust against process mismatches.

The measured frequency response of the loop gain is shown in Fig. 7. GBW and phase margin are around 3 MHz and $60^{\circ}$, respectively. The slight difference of GBW from simulation is attributed to process tolerances. The DC gain has been measured using an oscilloscope, obtaining a value of 57.5 dB . The measured CMRR at DC was 19 dB , in close agreement


Fig. 6. Postlayout simulations. (a) Nominal open loop frequency response (magnitude and phase) and Monte Carlo results for (b) DC gain, (c) GBW, and (d) phase margin.


Fig. 7. Measured open loop frequency response (magnitude and phase).


Fig. 8. Measured input current versus bulk-source voltage @ $20^{\circ} \mathrm{C}$.


Fig. 9. Measured time response of the OTA in inverting unity gain to an input step of 400 mV .
with (6). The power supply rejection ratio, PSRR, at DC was $52.1 \mathrm{~dB} / 66.4 \mathrm{~dB}$ for the positive/negative-supply PSRR, respectively. Regarding gain, CMRR and PSRR, classical measurement schemes have been used. Configurations shown in [27], setup I, were used for the gain and CMRR measurement. PSRR measurement set up is also well known [28].

The input common mode range (ICMR) is, in principle, rail to rail but it is actually limited by the maximum allowed input current that flows into the bulk. Indeed, the maximum input current occurs when $V_{B S}$ is maximum. That means that the ICMR should be restricted in its lower bound and simulations show that ICMR should then be limited to 550 mV (from 150 mV to 700 mV ) in order to maintain the input current below 4 nA at $27^{\circ} \mathrm{C}$. Measurements of the input current versus bulk-source voltage, performed at $20^{\circ} \mathrm{C}$ are shown in Fig. 8. It can be seen that when $V_{B S}=V_{B S \text { max }}=550 \mathrm{mV}$ the input current results to be around 1.3 nA . Since bulk current approximately doubles each $10{ }^{\circ} \mathrm{C}$ [29], it can be inferred that input current will remain below 100 nA up to $80^{\circ} \mathrm{C}$. It is worth noting that to avoid any latch-up problem conventional layout strategies such as double guard rings have been implemented and that extensive experimental measurements show that latch-up did not occur.

The measured time response to a $400 \mathrm{mV}_{p p}$ input step with the OTA in inverting unity gain configuration is plotted in Fig. $9(100 \mathrm{k} \Omega$ resistors used). The positive and negative slew rate values were $1.8 \mathrm{~V} / \mu \mathrm{s}$ and $3.8 \mathrm{~V} / \mu \mathrm{s}$, respectively. Besides, $1 \%$ settling time was $1.3 \mu \mathrm{~s}$ (positive step) and $1.0 \mu \mathrm{~s}$ (negative step).


Fig. 10. Measured (a) and simulated (b) input referred noise spectral density versus frequency.

Noise measurements and simulation are shown in Fig. 10. The input referred noise density measured at 1 MHz is around $100 \mathrm{nV} / \sqrt{ } \mathrm{Hz}$.

In order to carry out a quantitative comparison of the performance achieved through the implemented solution against other sub-1 V amplifiers, the two traditional figures of merit (FoM) [26], [30], [31] shown in (15) have been also evaluated in Table III. $\mathrm{FoM}_{S}$ and $\mathrm{FoM}_{L}$ allow a comparison of small signal and large signal performance, respectively

$$
\begin{align*}
& \mathrm{FoM}_{S}=\frac{\mathrm{GBW} \cdot C_{L}}{\text { Power }}  \tag{15a}\\
& \mathrm{FoM}_{L}=\frac{S R \cdot C_{L}}{\text { Power }} \tag{15b}
\end{align*}
$$

It is apparent that the proposed amplifier outperforms almost all other previously reported body-driven OTAs. In particular, as far as parameter $\mathrm{FoM}_{L}$ is concerned, the proposed OTA displays the maximum value, 2204, that is around 2.25 times greater than the best result previously reported [23]. Regarding the $\mathrm{FoM}_{S}$ parameter, the proposed OTA displays the second best result (2361) that is close to the maximum value obtained by [10] i.e., 2700. Fig. 11 shows the comparison in a graphical way.

The OTA main performance is summarized in Table IV. In addition to the parameters discussed before, Table IV includes offset (the maximum value measured from the available samples) and the total harmonic distortion (THD) of the output voltage with the OTA in inverting unity gain for $400-\mathrm{mV}_{p-p}$ input and two different frequencies.

## V. Conclusion

The bulk terminal of MOS transistors and its exploitation for low-voltage applications have recently received a renewed interest from analog and digital designers [33]-[38]. In this paper, a high-performance architecture for sub-1 V bulk-driven OTAs has been presented. The proposed solution exploits a three-gain-stage topology and uses a class AB output stage to improve DC gain and drive capability, respectively. A singleended OTA using the proposed topology and derived design equations was fabricated in a $180-\mathrm{nm}$ standard CMOS technology and experimentally tested. Measurements were found in

TABLE III
Performance Comparison of Sub-1 V Amplifiers


Fig. 12. Simplified schematic for resistors R noise analysis.
solution. Future work will be aimed to improve CMRR and to balance the positive and negative $S R$ in order to reduce the settling time and drive even larger load capacitors.

## APPENDIX

Let us consider the noise generated by the right-side resistor $R$, which is connected between the gate and drain of $M_{4}$ in Fig. 1. The simplified small signal model illustrated in Fig. 12 is utilized to find the voltage gain between $v_{n R}$ and the outputs of the first stage, $v_{o 1}$ and $v_{o 2}$.

From inspection of the figure we write the expr essions of $i_{R}$, $v_{o 1}$, and $v_{o 2}$

$$
\begin{align*}
i_{R} & =g_{m 3,4} v_{g s 3,4}+\frac{v_{o 2}}{r_{o 1}}=-g_{m 3,4} v_{g s 3,4}-\frac{v_{o 1}}{r_{o 1}}  \tag{A1}\\
v_{o 1} & =v_{g s 3,4}+R i_{R}  \tag{A2}\\
v_{o 2} & =v_{g s 3,4}-R i_{R}+v_{n R} . \tag{A3}
\end{align*}
$$

From (A1)-(A3) we get the transfer functions

$$
\begin{align*}
\frac{v_{o 1}}{v_{n R}} & =\frac{g_{m 3,4} R-1}{2\left(1+g_{m 3,4} r_{o 1}\right)\left(1+\frac{R}{r_{o 1}}\right)} \approx \frac{1}{2} \frac{R}{R+r_{o 1}}  \tag{A4}\\
\frac{v_{o 2}}{v_{n R}} & =\frac{1+g_{m 3,4}\left(R+2 r_{o 1}\right)}{2\left(1+g_{m 3,4} r_{o 1}\right)\left(1+\frac{R}{r_{o 1}}\right)} \approx \frac{1}{2} \frac{R+2 r_{o 1}}{R+r_{o 1}} \\
& =\frac{1}{2}\left(1+\frac{r_{o 1}}{R+r_{o 1}}\right) \tag{A5}
\end{align*}
$$

where the approximations hold for $g_{m 3,4} R \gg 1$ and $g_{m 3,4} r_{o 1} \gg 1$.
Observe that for the symmetry of the circuit, $v_{o 1} / v_{n R}$ represents also the transfer function from the noise source of the left-side resistor to $v_{o 2}$. This noise contribution of the left-side resistor is lower than that of the right-side resistor as can be seen by comparing (A4) and (A5) which imply the product of 0.5 by a quantity lower than the unity and greater than the unity, respectively.

The resistors noise referred to the input is evaluated by considering that the gain from the inverting input to the output of the first stage is $-(1 / 2) g_{m b 1,2} R / / r_{o 1}$. Therefore we get

$$
\begin{align*}
S_{V R, \text { in }} & =S_{V R} \frac{1}{4}\left[\left(\frac{R}{R+r_{o 1}}\right)^{2}+\left(\frac{R+2 r_{o 1}}{R+r_{o 1}}\right)^{2}\right]\left(\frac{2}{g_{m b 1,2} r_{o 1} / / R}\right)^{2} \\
& =4 k T R\left(\frac{1}{g_{m b 1,2} r_{o 1}}\right)^{2}\left[1+\left(1+\frac{2 r_{o 1}}{R}\right)^{2}\right] . \tag{A6}
\end{align*}
$$

The above input-referred resistor noise is used in (12).

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Elena Cabrera-Bernal (S'15) was born in Seville, Spain. She received the telecommunication engineering degree and the electronics, signal processing and communications M.Sc degree from the University of Seville, Seville, Spain, in 2011 and 2013, respectively.

Since 2013 she has been with the Department of Electronic Engineering, School of Engineering, University of Seville, where she is currently working towards the Ph.D. degree, granted by the Spanish Government. She was a Visiting Researcher at University of Catania in 2014 and at Imperial College of London in 2015. Her research interests are related to low-voltage low-power analog circuit design and analog and mixed signal microelectronics.


Salvatore Pennisi (M'00-SM'04) received the Laurea degree in electronic engineering and the Ph.D. degree in electrical engineering, both from the University of Catania, Italy, in 1992 and 1997, respectively.

In 1996, he became a Researcher (Assistant Professor) and in 2002 he was appointed an Associate Professor. In 2014 he received the Italian National Scientific Qualification for the position of Full Professor. He teaches undergraduate and graduate courses on microelectronics and basic electronics. His main research interests include circuit theory and analog design with emphasis on low-voltage and current-mode techniques, multi-stage amplifiers, data converters, analysis of high-frequency distortion in analog circuits, driving circuits for liquid crystal displays and micro-energy harvesting. He has published over 80 international journal papers, 120 contributions in conference proceedings, and is the coauthor of the books CMOS Current Amplifiers (1999), Feedback Amplifiers: Theory and Design (2001), both edited by Kluwer Academic Publishers, and Liquid Crystal Display Drivers-Techniques and Circuits (Springer, 2009).

Dr. Pennisi is member of the IEEE CASS Analog Signal Processing Technical Committee and served as an Associate Editor of the IEEE Trans actions on Circuits and Systems-Part II: Express Briefs and of the International Journal of Circuit Theory and Applications.


Alfio Dario Grasso (S'99-M'03-SM'15) was born in Catania, Italy, in 1978. He received the Laurea degree (summa cum laude) and the Ph.D. degree in electronic engineering from the University of Catania, Italy, in 2003 and 2006, respectively.

From 2006 to 2011 he was a Freelance Engineer in the field of electronic systems. From 2009 to 2010 he has held the position of Adjunct Professor of electronics at the University Kore of Enna, Italy. In 2011 he became a Researcher (Assistant Professor) and in 2015 he was appointed an Associate Professor at the University of Catania. He teaches undergraduate and graduate courses on advanced VLSI digital design, microelectronics, and basic electronics.

His current research interests include low-voltage low-power analog circuit design, D/A conversion and analog and mixed signal processing for energy harvesting applications. He has coauthored more than 50 papers on referred international journals and conference proceedings.


Antonio Torralba (M'89-SM'02) received the industrial engineering (M.Sc. in electrical engineering) and Ph.D. degrees from the University of Seville, Seville, Spain, in 1983 and 1985, respectively.

Since 1983, he has been with the Department of Electronics Engineering, School of Engineering, University of Seville, where he was an Assistant Professor, Associate Professor from 1987 to 1996, Professor since 1996, and since 2008 he is the Director of the Department, where he leads a research group on mixed signal design. In 1999, he was a Visiting Researcher in the Klipsch School of Electrical Engineering, New Mexico State University, Las Cruces, NM, USA, and in the Department of Electrical Engineering, Texas A\&M University, College Station, TX, USA. He is coauthor of 90 papers in international journals and his research interests include low power low voltage analogue and mixed signal microelectronics.


Ramón Gonzalez Carvajal (M'99-SM'04) was born in Seville, Spain. He received the Electrical Engineering and Ph.D. degrees (hons) from the University of Seville, Seville, Spain, in 1995 and 1999, respectively.

Since 1996, he has been with the Department of Electronic Engineering, School of Engineering, University of Seville, where he actually holds the position of professor since 2008. Dr. Gonzalez Carvajal has been visiting professor in research centers like Texas A\&M University, New Mexico State University, The Imperial College of Engineering and Medicine (London), University of Catania or INAOE. He also holds the position of Adjunct Professor at the Klipsch School of Electrical Engineering, NMSU. He is co-author of ten patents, five of them under exploitation contract. He has published more than 300 research works, including 100 journal indexed papers. He has also participated in more than 70 research projects funded by organizations like NASA, National Science Foundation, EPSRC, EUREKA or the European Framework Program, among others. His research interests are related to lowvoltage low-power analog circuit design, A/D and D/A conversion, and analog and mixed signal processing. Between 2009 and 2015 he has hold the positions of Vice-rector of Technology Transfer, General manager of the Research Foundation, and coordinator of the Excellence Campus AndalucTECH at the University of Seville.


[^0]:    ${ }^{1} \mathrm{~V}_{\mathrm{ds}}$ sat is the $\mathrm{V}_{\mathrm{ds}}$ saturation voltage.

[^1]:    ${ }^{2}$ More accurate expression of the output voltage should include the parallel of $R, r_{d s 1,2}$ and $r_{d s 3,4}$, instead of $R$ alone.
    ${ }^{3}$ To note that in a fully-differential implementation, the gain of the proposed input stage will be in the order of that achieved in the classical differential non-tailed pair of Figure 1 (b) as long as $R$ is large enough.

[^2]:    ${ }^{4} 3-\sigma$ rule states that $99.7 \%$ of the outcomes lie within three standard deviations of the mean.

[^3]:    ${ }^{5}$ Moreover, the model provided by the foundry for the flicker noise of Option 1 tends to overestimate it.

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    E. Cabrera-Bernal, A. Torralba, and R. G. Carvajal are with the Ingenieria Electronica, University of Seville, Escuela Técnica Superior de Ingenieria, 41012 Seville, Spain (e-mail: ecabrera3@us.es; torralba@us.es; carvajal@us.es).
    S. Pennisi and A. D. Grasso are with the Dipartamento de Ingegneria Elettrica Elettronica e Informatica, University of Catania, Catania I-95125, Italy (e-mail: salvatore.pennisi @dieei.unict.it; alfio.grasso@dieei.unict.it).

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[^5]:    ${ }^{1}$ We are neglecting for simplicity the output resistance of $M_{1}\left(M_{2}\right)$ and $M_{3}$ $\left(M_{4}\right)$. If this is not the case, a more accurate expression of the output voltage should include the parallel of $R, r_{d s 1}$, and $r_{d s 3}$, instead of $R$ alone.

[^6]:    ${ }^{2}$ In this accurate computation of the DC gain, the MOS transistors output resistances are included.

