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Adaptive resonance theory based neural network for supervised chemical pattern recognition (FuzzyARTMAP)

Part 1: Theory and network properties

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Abstract

The FuzzyARTMAP algorithm is studied with respect to its usefulness for supervised chemical pattern recognition. The theory of this relatively complex artificial neural classifier is presented in detail for chemists. An instructive data set of moderate size, describing male and female participants in courses of chemometrics by their body measures, is used to demonstrate how FuzzyARTMAP works and what its basic properties are.

Keywords: Artificial neural networks; Adaptive resonance theory (ART); Fuzzy set theory; Pattern recognition

1. Introduction

Adaptive resonance theory based artificial neural networks (ART) form a particular family of pattern recognition methods. They were introduced by Grossberg [1,2] to overcome the so-called stability–plasticity dilemma [3]. This dilemma describes the general difficulty for each classifier to be able to distinguish between two types of new knowledge: new knowledge that fits into the existing classifier structure and knowledge, that does not fit. The first type of new knowledge only requires a certain plasticity of the classifier, for example an adaptation of some fitting coefficients (network weights). The second type of new knowledge requires that the classifier not only

adapts some weights but its structure to the new classification situation.

ART-1, ART-2, ART-2a, ART-3 and FuzzyART, for example, are methods for unsupervised grouping of n pattern vectors \mathbf{X} (dimension $n \times m$) of length m into c clusters. These ART methods can be compared with respect of some algorithmic properties, for example, with the sequential leader algorithm [4]. Differences among the four ART methods exist in the type of processable input data (binary, real), data preprocessing (type of scaling, type of transfer function), speed of training and the type of similarity measure (Euclidian angle based, Fuzzy set theory based) [5,6]. The $l = 1 \dots c$ clusters generated during the training, are described by $l = 1 \dots c$ individual directed vectors \mathbf{w} (dimension $1 \times m$) forming together a so-called weights matrix \mathbf{W} of dimension $c \times m$. Caudell presented the use of ART-1 in combination

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with parallel operating opto-electronic multichannel detector arrays for commercial and military applications [7]. Optical, opto-electronical and electronical hardware implementations of ART-1 and ART-2 were reported by Kane and Paquin [8], Wunsch et al. [9,10] and Ho et al. [11]. Wienke and Kateman used ART-1 to classify UV/VIS and IR spectra and showed the quantitative chemical interpretability of the ART weights [12]. Lin and Wang fitted industrial time series data and classified the parameter vectors by ART-2 [13]. Whitley and Davis [14,15] proposed to use ART-2 for monitoring and control of chemical reactors by real-time interpretation of sensor data taken from the reactor. Wienke et al. [16,17] applied ART-2a in on-line monitoring of the environment by a classification of airborne particles using their scanning electron microscopy image data and their X-ray fluorescence emission pattern. Another application of ART-2 to pattern recognition with image data was reported recently by Resch and Szabo [18]. In Ref. [19] body measures of female and male persons were clustered by ART-2a. A comparison of ART-2a versus the principal component analysis based SIMCA classifier and backpropagation multilayer neural networks for rapid sorting of post-consumer plastics by remote NIR spectroscopy has been recently given [20]. Reported advantages for those four unsupervised ART methods compared to other types of classifiers are short training times (usually less than 20 epochs), built-in detector for outliers and for extrapolations, the quantitative interpretability of weights and the on-line applicability of ART in chemical apparatus.

A second group of ART algorithms (ARTMAP and FuzzyARTMAP) has been recently proposed by Carpenter et al. for supervised pattern recognition [21,22]. Their aim was to overcome the less powerful discrimination power of the former pure unsupervised working ART methods in case of very closely located clusters in the m -dimensional features space. Supervised learning by ARTMAP (resp. FuzzyARTMAP) means a controlled clustering of the X -space that is monitored by a corresponding desired output in a second space Y . Note, that in contrast to other supervised working classifiers (discriminant analysis, SIMCA, PLS, multilayer feedforward neural networks, etc.) the number, c , of clusters in the X -space and the number, b , of clusters in the Y -space

in case of ARTMAP (resp. FuzzyARTMAP) are not priorly fixed. The correct number of clusters (groups of similar data vectors) will thus be formed during training. The network structure itself (number of required neurons) forms thus an important result of the training process and makes the design of the network structure less subjective due to different users. A further consequence of this approach is, that several distinct and distant clusters in the input space X can be related to one single (identical) desired output cluster. ARTMAP is restricted to binary input data making it less interesting for chemical applications. Therefore the present work concentrates on FuzzyARTMAP as the most advanced ART algorithm with no restriction with respect to the type of input data. It has been decided to split this study in two parts because of the complexity of the FuzzyARTMAP algorithm that includes aspects from adaptive resonance theory as well as from fuzzy set theory. By means of a moderate sized data set X of $n = 47$ human beings characterized by their individual $m = 5$ body measures and by their sex y ($p = 1$), the theory and the properties of FuzzyARTMAP are discussed in Part 1. The chosen data set allows a quantitative insight in the classification behavior of FuzzyARTMAP and a detailed presentation of the meaning of so-called network weights. Other moderate sized chemical data sets are presently under consideration of ART neural networks [28]. Part 2 of the present study [26] deals with the implementation of FuzzyARTMAP in a remote working near-infrared multisensor system for rapid on-line sorting of post-consumer plastics.

2. Theory and FuzzyARTMAP algorithm

The theory of FuzzyARTMAP follows the general ART paradigms developed by Grossberg [1,2]. According to these assumptions, a classifier should always first check if a currently offered input vector x_i fits into the actual model limits in the variables space covered by a set of training samples. If this check succeeds, the current input x_i 'resonates' with the ART network. Then the classifier model can be updated by upgrading corresponding coefficients (more specific: network weights). On the other hand, if the check of the current input fails, another action then fitting of

weights is required. Because this input deviates significant from the calibration space covered by the current classifier model, the structure of the classifier has to be extended towards the new area where the current deviating input sample is located. Structure adaptation during training plays thus in ART models an even important role as weights adaptation.

Technically considered, the FuzzyARTMAP algorithm consists of two independently operating, self-organizing FuzzyART neural networks (Fig. 1). One of them clusters the $i = 1 \dots n$ pattern vectors in their m -dimensional \mathbf{X} -space, the other one in their p -dimensional \mathbf{Y} -space. m is the number of variables in the \mathbf{X} -space and p the number of variables in the \mathbf{Y} -space. A third algorithmic element, called ‘mapfield’, monitors and controls simultaneously both clustering processes.

2.1. Initial settings

Before training, two so-called weight matrices, \mathbf{W}^x (dimension $m \times cmax$) and \mathbf{W}^y (dimension $p \times bmax$) need to be initialized, whereby $cmax$ and $bmax$ are large constants, corresponding to the maximum expected number of clusters in the data sets (maximum is n). Usually the elements of \mathbf{W}^x and \mathbf{W}^y are initialized by $w_{j,l}^x = 1/\sqrt{m}$ (resp. $w_{k,h}^y = 1/\sqrt{p}$), whereby $j = 1 \dots m$ and $k = 1 \dots p$. The third weight matrix in a FuzzyARTMAP neural network, the so-called mapfield, \mathbf{W}^{xy} (dimension $cmax \times bmax$), has to be initialized by zeros.

Training parameters such like learning rates η^x , $\eta^{x,y}$ and η^y and vigilance parameters $\rho^{x,max}$, $\rho^{x,y,max}$ and $\rho^{y,max}$ for all three networks have to be defined in advance (between 0 and 1, mostly around 0.1). A necessary scaling constant, $0 < \alpha < 1$ has also to be set.

2.2. Network training

After this initialization, the training is done by random offer of corresponding pairs $[\mathbf{x}_i, \mathbf{y}_i]$ of training pattern vectors to the initialized network. \mathbf{x}_i is applied to the input of the network in the \mathbf{X} -space and \mathbf{y}_i to the input of the corresponding network in the \mathbf{Y} -space. In the very beginning, when no cluster exists, \mathbf{x}_i and \mathbf{y}_i are copied as initial estimate of the first

weight vectors \mathbf{w}_1^x (resp. \mathbf{w}_1^y). Later on, a pairwise comparison is done between the current inputs, \mathbf{x}_i and \mathbf{y}_i , with all active $l = 1 \dots c$ weight vectors \mathbf{W}^x (resp. $h = 1 \dots b$ in \mathbf{W}^y) by calculating the fuzzy distance d_i^x (resp. d_i^y) for dissimilarity

$$d_{i,i}^x = |\mathbf{x}_i \wedge \mathbf{w}_i^x| / (\alpha + |\mathbf{w}_i^x|) \quad (1)$$

between the current inputs and all individual weight vectors with $|\mathbf{z}| = \text{length of a vector } \mathbf{z}$. The fuzzy set theory based operator ‘ \wedge ’ (intersection) provides a resulting vector $\mathbf{z} = \min(\mathbf{x}_i, \mathbf{w}^x)$ (resp. $\mathbf{z} = \min(\mathbf{y}_i, \mathbf{w}^y)$) which has as elements the corresponding minimum element values of the two considered vectors. Geometrically considered, this new resulting vector is always spatially located in between both vectors. Then, for each of both networks, a weight vector, \mathbf{w}_{winner}^x (resp. \mathbf{w}_{winner}^y) can always be found having a minimum distance (highest similarity) to the present input vector. This weight vector is called winner. In the following step, called in ART ‘resonance check’, with the formula

$$\rho_i^x = |\mathbf{x}_i \wedge \mathbf{w}_{winner}^x| / |\mathbf{x}_i| \quad (2)$$

it is calculated if the present inputs are inside or outside winner’s existing cluster. If the calculated distances are smaller than the so-called ‘vigilance’ parameters $\rho^{x,max}$ (resp. $\rho^{y,max}$) according to

$$\rho_i^x < \rho^{x,max} \quad (3)$$

then the present input vector is inside an existing cluster (high similarity), or in other words, the input came into resonance with the network. If not, the secondly placed winner according (1) is checked by (2)–(3) and so on. In the following, ‘network learning’ will happen. In contrast to conventional neural networks, this step is called in ART ‘adaptation’. Adaptation means more than simply fitting a fixed number of coefficients (network weights). Adaptation can also mean in ART an extension of the current network structure by additional weight vectors.

For sequential fitting its weights \mathbf{W}^x , FuzzyARTMAP uses the learning rule

$$\mathbf{w}_{winner}^{new,x} = \eta^x (\mathbf{x} \wedge \mathbf{w}_{winner}^{old,x}) + (1 - \eta^x) \mathbf{w}_{winner}^{old,x} \quad (4)$$

(corresponding formulae for fitting both other weight matrices \mathbf{W}^y and $\mathbf{W}^{x,y}$ have simultaneously to be applied).

Expressed in classical terms of data fitting, the learning rates η are the step sizes for moving a current winning weight vector w_{winner}^x in its spatial direction towards the currently offered input vector x_i (resp. w_{winner}^y towards y_i). For the influence of the size of η 's on the training of an ART network, consult, for example, Ref. [12].

Additionally, the element in the l th row and the h th column in the mapfield W^{xy} , corresponding to the two separate winners in both networks, is set to one in the learning step. Alternative ways of mapfield learning are the use of the binary coded output vector y^{out} of the Y-network or of the real-coded vector of $d_{i,i}^x$ values (length c) as inputs to the mapfield. The mapfield as a real weight matrix is then trained by the corresponding training rule similar to Eq. (4).

If condition (3) is not fulfilled, the current input vectors are outside all currently existing clusters. In such a case FuzzyARTMAP will give a 'reset' signal and it will create a new additional cluster. In case of the network in the X-space, the number of formed clusters will grow from $l = 1 \dots c$ to $l = 1 \dots c + 1$ by increasing the dimension of the weight matrix W^x by one. The same happens for W^y with $h = 1 \dots b$ weight vectors if a reset is given in the Y-space. That input vector that has caused a reset will directly be copied into the new formed weight vector. In this way a new

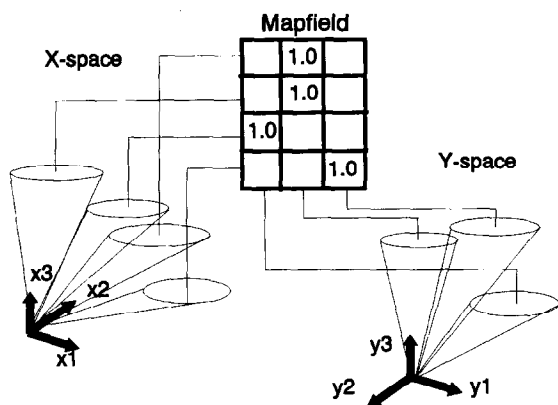


Fig. 1. The mapfield completes two FuzzyART neural networks to a FuzzyARTMAP network. The mapfield monitors and controls both simultaneous running clustering processes (network training). The number and the size of formed clusters depends for each single network from the size of the prior chosen vigilance parameter (see also Fig. 2).

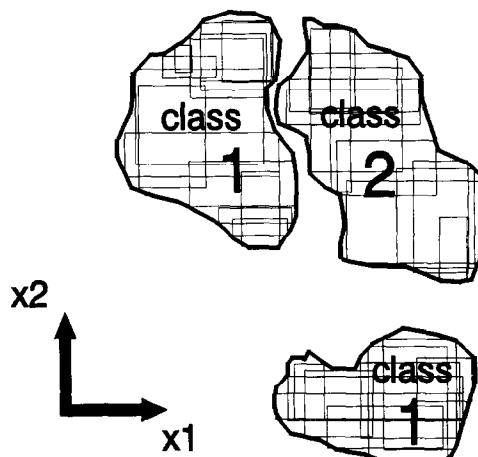


Fig. 2. Complement coding (see text) in combination with fuzzy distance measures provides hyperrectangular shaped clusters. Each cluster box grows during training to its maximum size. In this way, arbitrary shaped clouds of experimental data points are approximated by overlapping hyperrectangulars. FuzzyARTMAP's mapfield allows a link of very distant clusters in the X-space to one common cluster in the Y-space. On the other hand, it allows the dedication of spatially close located clusters in X to distinct clusters in Y.

additional cluster is always be initialized by its first offered pattern vector.

The mapfield W^{xy} increases its dimensions simultaneously by closely following the cluster numbers c and b of W^x and W^y . Another network reset happens, if a winner in the X-space does not correspond to a winner in the Y-space. This happens mostly for very close located clusters in variables space if they belong to different desired outputs. In such a case a reset is given by the mapfield, because the mapfield is that part of the entire network that covers the information which cluster in the X-space is linked to which cluster in the Y-space (Fig. 1). Two independent running neural networks that interact via a mapfield allow the link of distant clusters from X-space to an identical desired output cluster in the Y-space. As an example, NIR spectra of several grades of high density and low density polyethylene polymers ('PE') form distant clusters in the spectral space X. However, via the mapfield these distant clusters can be linked together to the same desired output 'PE'. On the other hand, close located clusters can be precisely separated (Fig. 2).

Table 1

Anonymized experimental data matrices Y and X of five body measures of 12 female (f) and 35 male (m) participants in training courses in chemometrics (for details, see Experimental)

| Participant identifier | $y = \text{sex}$ | $x_1 = \text{body length (cm)}$ | $x_2 = \text{body weight (kg)}$ | $x_3 = \text{shoe size (/a.u.)}$ | $x_4 = \text{belly outline (cm)}$ | $x_5 = \text{neck (cm)}$ |
|------------------------|------------------|---------------------------------|---------------------------------|----------------------------------|-----------------------------------|--------------------------|
| m1 | 0 | 185 | 91 | 44.5 | 103 | 42 |
| m2 | 0 | 196 | 98 | 43.5 | 100 | 39 |
| m3 | 0 | 186 | 75 | 45.5 | 90 | 39 |
| m4 | 0 | 169 | 59 | 41 | 83 | 38 |
| f5 | 1 | 160 | 57 | 37 | 74 | 34 |
| m6 | 0 | 178 | 72 | 44 | 85 | 37 |
| f7 | 1 | 162 | 55 | 38 | 70 | 31 |
| m8 | 0 | 183 | 65 | 41 | 75 | 34 |
| m9 | 0 | 177 | 66.5 | 41 | 90 | 37 |
| f10 | 1 | 170 | 63 | 39 | 72 | 35 |
| m11 | 0 | 160 | 57 | 39 | 81 | 35 |
| m12 | 0 | 190 | 80 | 46 | 83 | 36 |
| m13 | 0 | 172 | 82 | 42 | 93 | 41 |
| m14 | 0 | 183 | 70 | 43 | 91 | 38 |
| m15 | 0 | 181 | 71 | 42 | 91 | 39 |
| m16 | 0 | 185 | 78 | 42 | 89 | 39 |
| m17 | 0 | 183 | 77 | 44 | 105 | 41 |
| m18 | 0 | 183 | 90 | 42 | 106 | 46 |
| m19 | 0 | 180 | 80 | 41 | 58 | 41 |
| m20 | 0 | 187 | 81 | 44 | 87 | 41 |
| f21 | 1 | 163 | 60 | 38 | 76 | 34 |
| f22 | 1 | 164 | 55 | 39 | 76 | 31 |
| m23 | 0 | 170 | 74 | 41 | 94 | 39 |
| f24 | 1 | 170 | 75 | 37 | 99 | 37 |
| f25 | 1 | 173 | 56 | 38.5 | 65 | 32 |
| m26 | 0 | 168 | 75 | 41 | 99 | 39 |
| m27 | 0 | 176 | 72 | 41.5 | 85 | 38 |
| m28 | 0 | 172 | 73 | 41 | 92 | 41 |
| m29 | 0 | 180 | 83 | 43 | 89 | 38 |
| m30 | 0 | 172 | 82 | 42 | 100 | 41 |
| f31 | 1 | 162 | 55 | 39 | 68 | 32 |
| m32 | 0 | 186 | 105 | 45 | 115 | 43 |
| m33 | 0 | 187 | 90 | 43 | 93 | 41 |
| f34 | 1 | 165 | 55 | 37.5 | 76 | 33 |
| m35 | 0 | 181 | 78 | 45 | 99 | 40 |
| m36 | 0 | 188 | 72 | 43.5 | 77 | 33 |
| m37 | 0 | 185 | 81 | 44.5 | 95 | 40 |
| m38 | 0 | 188 | 75 | 44.5 | 87 | 37 |
| m39 | 0 | 187 | 73 | 43 | 85 | 39 |
| m40 | 0 | 178 | 84 | 43 | 98 | 41 |
| f41 | 1 | 173 | 61 | 38 | 70 | 33 |
| m42 | 0 | 189 | 75 | 45 | 87 | 38 |
| m43 | 0 | 177 | 70 | 41 | 89 | 37 |
| m44 | 0 | 181 | 76 | 42 | 87 | 39 |
| f45 | 1 | 170 | 70 | 39 | 81 | 35 |
| f46 | 1 | 170 | 57 | 39 | 70 | 35 |
| m47 | 0 | 186 | 85 | 42 | 87 | 38 |
| minimum | 0 | 160 | 55 | 37 | 58 | 31 |
| maximum | 1 | 196 | 105 | 46 | 115 | 46 |

2.3. Complement coding as a special preprocessing procedure

Eqs. (1)–(2) require, that the elements of the input vectors \mathbf{x}_i (resp. \mathbf{y}_i) are positive numbers in the range 0...1. This can be reached, for example, by data preprocessing using range scaling. A second condition has to be fulfilled. The input vectors have to be additionally 'complement coded'. This means that \mathbf{x}_i is doubled in its length by appending its complement vector $1 - \mathbf{x}_i$. \mathbf{y}_i is complement coded by its corresponding vector $1 - \mathbf{y}_i$. Calculation examples for complement coding are given, for example, in Refs. [27,28]. From an algebraic point of view, complement coding adds redundant information only. From the point of view of fuzzy set theory, a single crisp feature in a data vector is substituted by a function of this feature (here: a simple range between a lower and an upper feature limit). Thus, calculations (1)–(2) deal with functions of features instead of single crisp features. For two or more features, in this way, hyperrectangular shaped boxes for each cluster (Fig. 2) are obtained instead of single directed vectors. The boxes grow during training (network weights adaptation) from a small point vector to a large hyperrectangular. The mathematical proof for this effect can be found in Carpenter et al. [21,22]. Thus, an experimental data cluster will be approximated by FuzzyARTMAP by a sequence of overlapping hyperrectangulars. The outer limits of such a hyperrectangular are called in the present work 'upper fuzzy bounds' and 'lower fuzzy bounds'. Another effect of complement coding is, that it gives 'absent features', having low data values, even high contributions in the fuzzy similarity measures (1)–(2) as 'present features' that usually have higher values.

2.4. Qualification versus quantification

Each cluster formed by a FuzzyARTMAP artificial neural network describes a limited local region in the variables space. In this way, complicated shaped clouds of experimental data are approximated, in principle, by a sequence of overlapping hyperrectangulars. This is true for the data cloud in the \mathbf{X} -space and in the \mathbf{Y} -space. This approach of locally overlapping partial clusters the FuzzyARTMAP network is rather useful for supervised pattern recognition

(qualification) than for function fitting (quantification). It has been shown [21–24] in studies with simulated and experimental data sets, that FuzzyARTMAP can successfully approximate data clouds that are located within each other and data clouds that are formed from combined spirals. This gives an impression of its discrimination power, for example, compared with MLF-BP neural networks [29]. However, the more a data set forms a continuous function, the more new single weight vectors are needed by FuzzyARTMAP. Function fitting is thus possible, but the costs one has to pay for this are a rapid proliferation of an enormous number of new single clusters.

3. Experimental

During the international COMETT Course in Chemometrics in Heyen (The Netherlands) that was organised in 1991 by the Laboratory of Analytical Chemistry of the Catholic University of Nijmegen the present author asked the participants for their individual body measures 'body length', 'body weight', 'foot size', 'belly' and 'neck'. The aim was to get an experimental data set that could be used in the exercises of multivariate data analysis and multivariate statistics. The same experiment has been repeated once more again during a chemometrics course for chemistry teachers at the technical college Utrecht (The Netherlands) in 1991. Both data sets were anonymized and merged providing a complete data matrix \mathbf{X} (size 47×5) of $n = 47$ persons, characterized by $m = 5$ features, and their corresponding sex \mathbf{Y} (dimension 47×1) as desired $p = 1$ -dimensional output (Table 1).

4. Computations and software

A program 'FuzzyARTMAP.c' has been written by the author in ANSI-C computer language for UNIX computers (SUN) for the gcc-compiler. The alternative WINDOWS-version, now implemented in the master PC of an POLYTEC XDAP near-infrared diode array spectrometer, will be described in Part 2 of this publication series.

5. Results and discussion

First, the 47×5 data matrix (Table 1) has been analyzed in a classical way using multivariate statistical methods. This helps in understanding the following results provided by the FuzzyARTMAP neural network.

5.1. An introducing multivariate-statistical study

The present data set (Table 1) has been recently studied by hierarchical cluster analysis and principal component analysis [19]. The dendrograms for two different clustering methods of the columnwise autoscaled 47×5 data matrix showed some single outliers (m8, m18, m19, m32, m36). A group with a high contribution of 10 females and one single male participant (m11) has been found. Another large cluster concerns all remaining 34 male participants including two females f24 and f45 that were left. This large group splits into three subclusters whereby the classification result differs slightly due to Ward's and due to the average linkage method. The main result from hierarchical cluster analysis was, that obviously the

five chosen body features provide combined information about differences between men and women. However, some few participants (m11, f24 and f45) were misclassified. Comparing their data with those ones from men in general makes these misclassifications understandable (Table 1). Principal component analysis over the 5×5 correlation matrix of \mathbf{X} provided a distribution of the percentage contributions of the total variance over the five factors into 74.4%, 15.0%, 5.0%, 3.8% and 1.8%. Multivariate correlations were found between the five body measures. An example for this is that a high body weight can be caused by a large body length or/and a large belly. Thus, small men with a big belly can get an even high weight as tall but slender women. On the other hand, this does not necessary mean that a correlation between belly outline and body length exists. Fig. 3 summarizes quickly the results from the multivariate statistical study. So the reader will get somewhat feeling for the data before application of FuzzyARTMAP. The linear mapping result in Fig. 3 looks similar to the already published PCA scores plots [19]. The position of the 47 participants scores are in agreement with the cited clustering results. The two

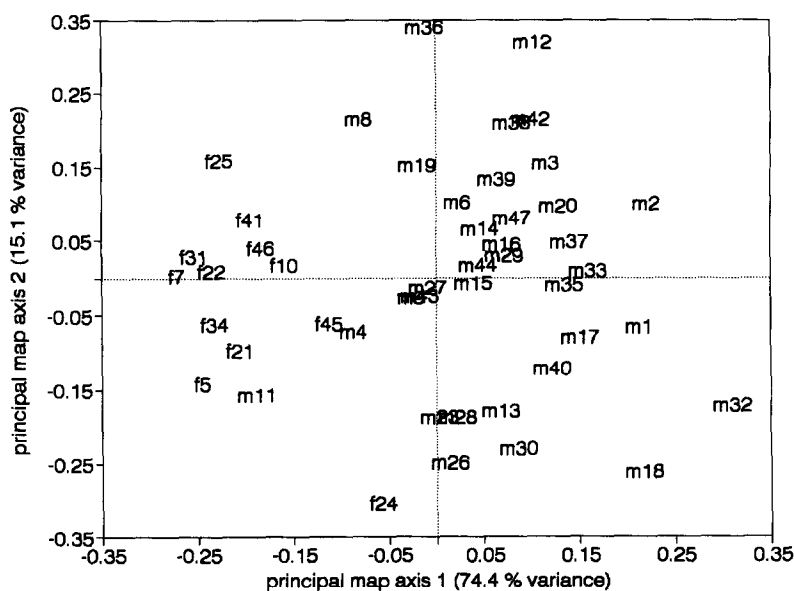


Fig. 3. Presentation of the two first principal axis obtained from a multidimensional scaling (MDS, Torgerson's method [30]) of data from Table 1. Female participants (f) are found in the left handed lower region that is mainly determined by low values in 'body size', 'body weight' and 'shoe measure'. Male participants (m) mostly can be found in the right handed region characterized by higher values in 'body length', 'belly', 'neck' and 'weight'.

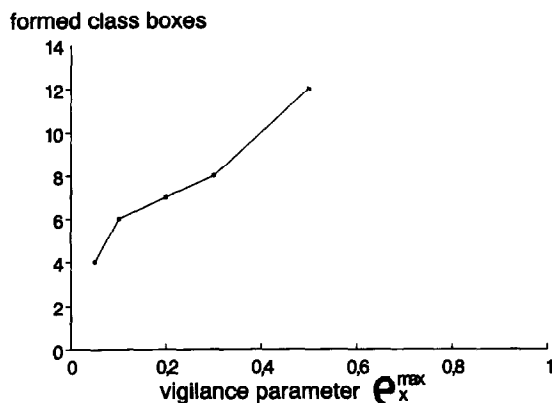


Fig. 4. Presentation of the growing resolution of a data set into finer subclusters by an increase of the vigilance parameter (here: ρ_x^{max}) in the X-space. The more compact the data are, the less they scatter. In such a case a change of ρ does not have nearly any effect (here: between 0.1 and 0.5). The more the data scatter or if they form a continuous function in place of a cluster the more sensitive the resolution reacts on small changes in ρ (here: 0.5–1.0).

large clusters of male and female participants occupy distinct areas in the space. Females show lower values in all five features compared to males. However, there are some exceptions and there is some overlap. Only combinations of several PC provided a perfect

and distant separation of men and women. The reason is that special combinations of PC characterized the participants that took part in the courses of chemometrics coming from all over Europe. A few tall and gangling northern european women, for example, could compete with selected small european men according the combination of the three variable combination 'length + weight + foot size', for example. The closeness of the males m11, m4, m23 and m26 to the females group proofs this. On the other hand, men's combined measure ratios in belly outline and neck size allowed to distinguish them from female participants.

5.2. FuzzyARTMAP study

FuzzyARTMAP can be used to study data sets in three distinct directions. First, training runs with distinct chosen sizes of $\rho^{x,max}$, $\rho^{xy,max}$ and $\rho^{y,max}$ resolve the X and the Y matrix into distinct numbers of clusters and subclusters. In this way the raw structure and the fine structure of the data cloud can be explored. Second, after such a training, the obtained network weights can be decoded and rescaled again back to the original variables space for quantitative

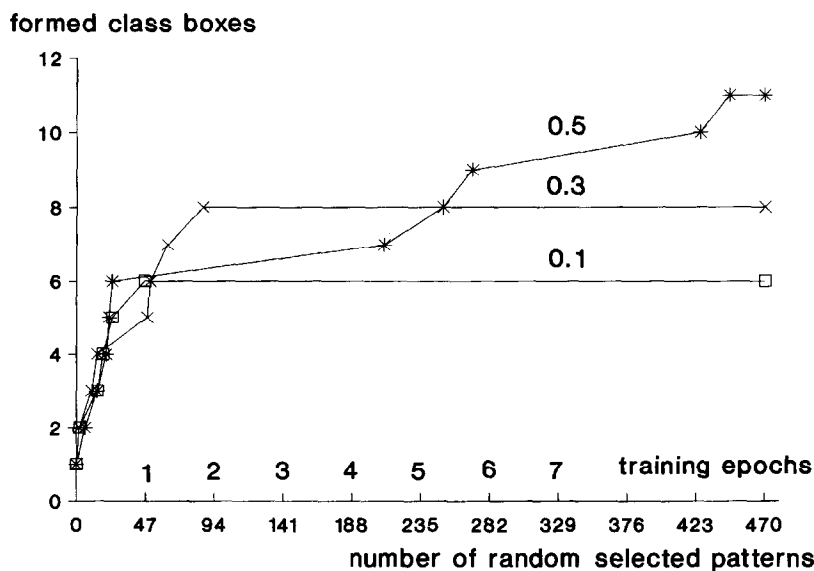


Fig. 5. Presentation of the formation of the final number of clusters as function of the number of training epochs for three distinct sizes of the vigilance parameter $\rho_x^{max} = 0.1, 0.3, 0.5$. In general, fast convergence of the training process can be observed for a FuzzyARTMAP network within a few epochs. The higher the desired cluster resolution is the more time the convergence takes (see also Fig. 6).

interpretation of the network structure. This helps to trace the nature of the formed clusters and it helps to understand why they were formed. Third, a trained FuzzyARTMAP network can be used to classify unknown pattern vectors.

Fig. 4 shows for increasing vigilance parameter $\rho^{x,max}$ (thus for decreasing cluster size), how the network needs additional single clusters (hyperrectangulars) to approximate the entire data cloud. This effect is also well known from the unsupervised working ART neural networks. Between 0.05 and 0.5 for the $\rho^{x,max}$ value the number of formed clusters does not change so much. That simply means that the more compact and focused to a single point a data cluster is, the less important the influence of the chosen size of $\rho^{x,max}$ is. On the other hand, it also indicates a disadvantage of all ART networks. The more a data cloud scatters (from noisy or wrong features) the more the FuzzyARTMAP network will tend to proliferation of single new clusters.

The next important property, that has been studied here, was the speed of the convergence of the training process. Carpenter et al. mentioned in their ART-2a study [5] the enormous gain in training speed by ART if it is compared, for example, with a multi-

Table 2

Weights matrix W^{xy} (mapfield) links seven clusters of the five-dimensional X-space (body measures of participants) to two clusters in the one-dimensional Y-space (sex of participants). This particular cluster structure was obtained for the data from Table 1 with following settings for the FuzzyARTMAP algorithm: learning rates: $\eta^x = 0.1$, $\eta^{x,y} = 0.1$, $\eta^y = 0.1$; vigilance parameters: $\rho^{x,max} = 0.2$, $\rho^{xy,max} = 0.6$, $\rho^{y,max} = 0.9$; scaling factor $\alpha = 0.01$. The network has been trained by 3 epochs

| Cluster k/l | $Y_{out,1}$ | $Y_{out,2}$ |
|---------------|-------------|-------------|
| $X_{out,1}$ | 1.0 | 0.0 |
| $X_{out,2}$ | 0.0 | 1.0 |
| $X_{out,3}$ | 1.0 | 0.0 |
| $X_{out,4}$ | 1.0 | 0.0 |
| $X_{out,5}$ | 0.0 | 1.0 |
| $X_{out,6}$ | 0.0 | 1.0 |
| $X_{out,7}$ | 1.0 | 0.0 |

layer feedforward backpropagation neural network. Even for large data sets with many thousands of pattern vectors [21,22,24,25] a remarkable small number of training epochs were reported. For FuzzyARTMAP a significant speed has been observed, too, in the present work (Fig. 5). It can be seen, that FuzzyARTMAP converges for the training data from

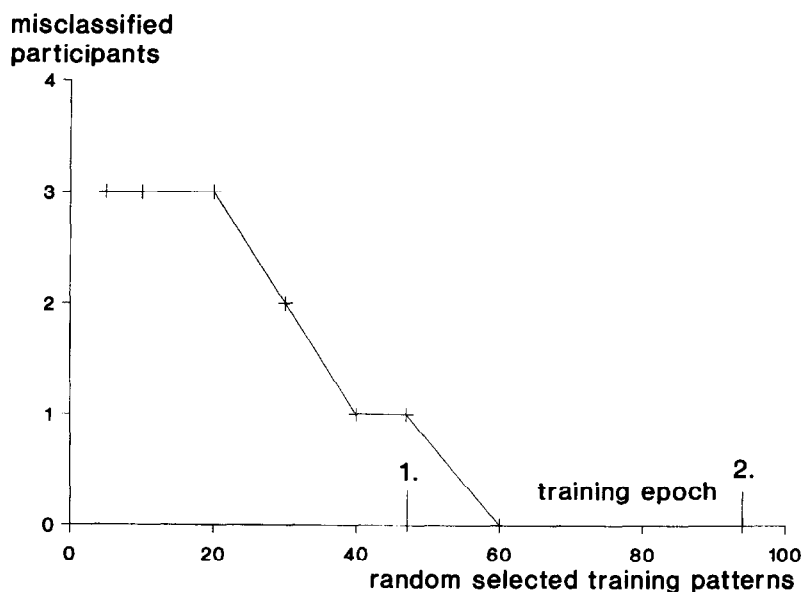


Fig. 6. Convergence of FuzzyARTMAP's training process shown by a presentation of the reclassification error (data set, Table 1) as function of the number of training epochs. In general, the reclassification error rapidly decreases within the first few epochs (here after less than two epochs).

Table 3

Weights matrix W^x describes seven rectangular shaped clusters among the $n = 47$ X pattern (Table 1). Each cluster is limited by the lower and upper 'fuzzy bounds' of the five contributing variables. W^x has been obtained after training the FuzzyARTMAP network with range scaled features (Table 1) using the network parameter given in Table 2. The sex identifier 'M' = male and 'F' = female are available via the mapfield (Table 2)

| Scaled feature | Type of cluster | | | | | | |
|--------------------|-----------------|------|------|------|------|------|------|
| | M1 | F1 | M2 | M3 | F2 | F3 | M4 |
| lower fuzzy bounds | | | | | | | |
| length (a.u.) | 0.30 | 0.00 | 0.51 | 0.00 | 0.07 | 0.27 | 0.25 |
| weight (a.u.) | 0.33 | 0.01 | 0.20 | 0.04 | 0.00 | 0.15 | 0.08 |
| shoes (a.u.) | 0.47 | 0.00 | 0.44 | 0.22 | 0.16 | 0.13 | 0.44 |
| belly (a.u.) | 0.47 | 0.24 | 0.15 | 0.40 | 0.19 | 0.28 | 0.43 |
| neck (a.u.) | 0.40 | 0.14 | 0.16 | 0.26 | 0.00 | 0.26 | 0.46 |
| upper fuzzy bounds | | | | | | | |
| length (a.u.) | 0.86 | 0.20 | 0.70 | 0.00 | 0.22 | 0.27 | 0.25 |
| weight (a.u.) | 0.87 | 0.10 | 0.36 | 0.04 | 0.00 | 0.34 | 0.08 |
| shoes (a.u.) | 0.93 | 0.08 | 0.57 | 0.22 | 0.22 | 0.22 | 0.44 |
| belly (a.u.) | 0.89 | 0.32 | 0.48 | 0.40 | 0.31 | 0.53 | 0.43 |
| neck (a.u.) | 0.86 | 0.22 | 0.46 | 0.26 | 0.04 | 0.32 | 0.46 |

Table 1 usually in less than three training epochs. With respect to a correct reclassification (Fig. 6) the convergence has been usually already reached after less than two epochs. The formation of the final fine-tuned cluster structure needed usually some additional training epochs (Fig. 5). This effect is caused by a few single patterns that are located at the border line of a formed cluster. Such single patterns have the same statistical chance to be randomly selected like

the other ones that form together the center of a multi-pattern cluster. In this way the position of a cluster covering many of the training pattern is much faster formed than the position of a cluster with only a single pattern. The main clusters covering the majority of all training pattern were mostly formed within less than two training epochs. This is also almost independent from the chosen size of ρ and the number n of data set size (see Part 2 [26]). The split-

Table 4

Same weights matrix W^x from Table 3, but decoded and rescaled to original features space

| Feature | Type of cluster | | | | | | |
|--------------------|-----------------|--------|--------|--------|--------|--------|--------|
| | M1 | F1 | M2 | M3 | F2 | F3 | M4 |
| lower fuzzy bounds | | | | | | | |
| length (cm) | 171.12 | 160.00 | 178.40 | 160.00 | 162.62 | 170.00 | 169.00 |
| weight (kg) | 71.84 | 55.95 | 65.00 | 57.00 | 55.00 | 62.93 | 59.00 |
| shoes (a.u.) | 41.24 | 37.00 | 41.00 | 39.00 | 38.50 | 38.18 | 41.00 |
| belly (cm) | 85.13 | 71.82 | 67.03 | 81.00 | 68.91 | 74.06 | 83.00 |
| neck (cm) | 37.09 | 33.19 | 33.53 | 35.00 | 31.00 | 35.00 | 38.00 |
| upper fuzzy bounds | | | | | | | |
| length (cm) | 190.96 | 167.53 | 185.34 | 160.00 | 168.21 | 170.00 | 169.00 |
| weight (kg) | 98.66 | 60.26 | 73.22 | 57.00 | 55.46 | 72.04 | 59.00 |
| shoes (a.u.) | 45.43 | 37.80 | 42.19 | 39.00 | 39.00 | 39.00 | 41.00 |
| belly (cm) | 108.99 | 76.68 | 85.65 | 81.00 | 76.00 | 88.37 | 83.00 |
| neck (cm) | 43.92 | 34.39 | 37.95 | 35.00 | 31.71 | 35.81 | 38.00 |

and 5) the cluster results are obvious and not that much exciting. However, for future processing of spectral, environmental-analytical or process-analytical Y-data this consideration can provide interesting results, too.

5.3. Verification of the trained FuzzyARTMAP network

A test data set (Table 8) has been used to verify the trained network. This set contains body measures of as well male, female adults as of children. The children group (between 6 and 7 years old) forms with its specific body measures an extrapolation re-

gion in the features space, because the training set (Table 1) covered only data from adults. The test run has been performed in two different ways. First a validation run was done, for which the network has been undertrained with the training data from Table 1 using a growing number of training epochs. For each undertrained network the test adults (from Table 8) were predicted (Fig. 7). Similar to the decrease of the classification error it can be observed that the prediction error also rapidly decreases within a few training epochs (compare Figs. 6 and 7). Finally, all unknown adults have been correctly predicted by FuzzyARTMAP according their sex (male, female) based on their body measures if at least 2–3 training

Table 8
Anonymized test data set X^{test} of five body measures of female (f) and male (m) adults and of children (c) used for validation of trained FuzzyARTMAP neural network

| Person | x_1 = body length (cm) | x_2 = body weight (kg) | x_3 = shoe size (a.u.) | x_4 = belly outline (cm) | x_5 = neck (cm) |
|--------|--------------------------|--------------------------|--------------------------|----------------------------|-------------------|
| f13 | 172 | 65 | 41 | 74 | 33 |
| f14 | 160 | 68 | 36 | 88 | 38 |
| m36 | 183 | 80 | 45 | 85 | 43 |
| c1 | 121 | 24 | 32 | 54 | 25 |
| f15 | 166 | 64 | 39 | 80 | 33 |
| m37 | 186 | 80 | 43 | 93 | 42 |
| m38 | 175 | 66 | 40 | 86 | 42 |
| m39 | 183 | 75 | 43 | 79 | 38 |
| m40 | 189 | 87 | 45 | 86 | 40 |
| f16 | 158 | 51 | 36 | 74 | 40 |
| m41 | 183 | 70 | 43 | 78 | 36 |
| m42 | 193 | 72 | 45 | 80 | 38 |
| m43 | 177 | 67 | 42 | 75 | 38 |
| m44 | 170 | 89 | 43 | 102 | 41 |
| m45 | 180 | 78 | 42 | 89 | 35 |
| m46 | 197 | 84 | 45 | 88 | 36 |
| m47 | 194 | 87 | 46 | 86 | 38 |
| f17 | 173 | 63 | 39 | 69 | 32 |
| f18 | 162 | 65 | 39 | 76 | 34 |
| f19 | 170 | 70 | 38 | 79 | 36 |
| f20 | 170 | 61 | 38 | 70 | 29 |
| f21 | 171 | 61 | 40 | 71 | 30 |
| f22 | 171 | 62 | 40 | 72 | 35 |
| c2 | 114 | 22 | 29 | 47 | 22 |
| c3 | 113 | 23 | 30 | 49 | 24 |
| c4 | 124 | 28 | 33 | 59 | 26 |
| c5 | 114 | 24 | 30 | 54 | 27 |
| c6 | 120 | 27 | 31 | 55 | 26 |
| c7 | 120 | 23 | 29 | 51 | 23 |
| c8 | 116 | 24 | 30 | 51 | 25 |
| c9 | 121 | 26 | 31 | 56 | 25 |
| c10 | 113 | 20 | 28 | 46 | 20 |

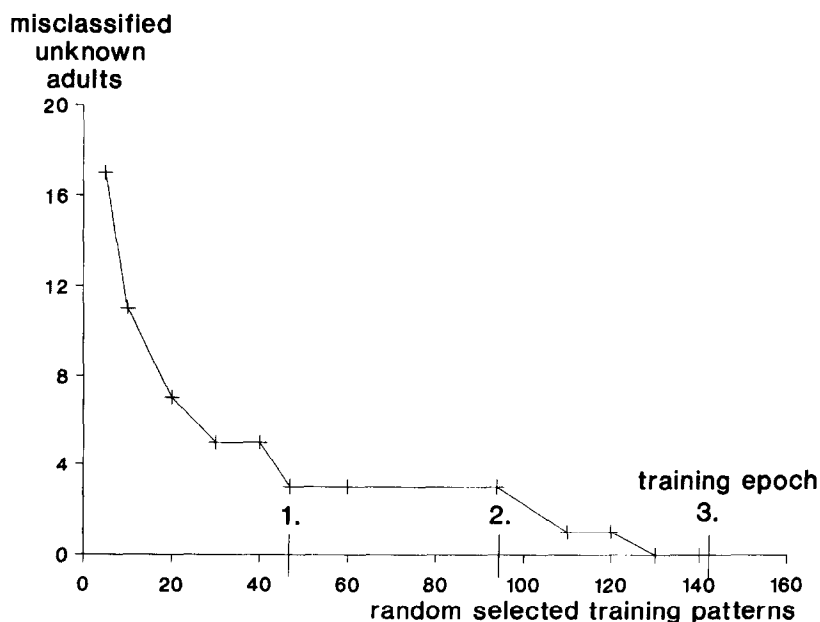


Fig. 7. Convergence of FuzzyARTMAP's training process, presented by the size of prediction error for a test data set (Table 8) as a function of the number of epochs for a training data set (Table 1).

epochs were applied. For this test run it was the network not allowed to go on with learning by modifying any weights of existing clusters (from training).

A second experiment has been performed with the test data set (Table 8) including now also the children's data. Now the network it was allowed to keep learning its weights as well its structure. Based on the random order of test vectors the weight vectors of the existing cluster (of adults) did only oscillate a little bit around their previous position. However, the first child's pattern vector from the test data set (Table 8) that was offered to the network, could not be classified into any existing adults's cluster. The network gave a reset and created in the X -space an additional new cluster and asked to declare a corresponding Y -pattern for this unknown. All following test vectors for children were classified then correctly by FuzzyARTMAP in this common new cluster.

6. Conclusions

FuzzyARTMAP is an alternative neural classifier for supervised pattern recognition with remarkable short training time and with full interpretability of its

weights in terms of original variables. These two properties make the classifier interesting for quantitative pattern recognition studies. The built-in detector against outliers and extrapolations make FuzzyARTMAP also interesting for robust and save working technical applications in analytical-chemical process control and environmental monitoring tasks.

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